

# Producing Hollow Shafts in a New Horizontal Mill by Novel Flat-Knifing Cross-Wedge Rolling With Single Guide

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## Research Article

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1           **Producing hollow shafts in a new horizontal mill by novel flat-**  
2                           **knifing cross-wedge rolling with single guide**

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29 **Abstract**

30 To meet the requirement of lightweight, there are increasing solid shafts being  
31 designed to be hollow in transportation industry. In this study, a novel method of flat-  
32 knifing cross-wedge rolling (FCWR) with single guide is proposed including a  
33 modified roller, a horizontal mill and a single-guide structure, and its key problems are  
34 studied by numerical simulations and experimental tests. A mathematical model of  
35 FCWR roller is established, which reveals the wedge length of rollers is effectively  
36 reduced by modifying knifing wedge from normalized roller. Further, a horizontal  
37 multifunctional mill is invented and constructed to carry out the FCWR experiment  
38 with single guide. According to the results from the numerical simulations and  
39 corresponding experiments, it is observed that the typical defects of hole expansion and  
40 knifing groove are absolutely avoided because the improved flat-knifing wedge  
41 produces a radial force to shrink the inner hole and avoid the deformation concentration  
42 of the outer surface during knifing stage. Moreover, the single guide rolling performed  
43 in the horizontal mill efficiently improve rolling stability because the workpiece is  
44 restricted into a smaller workspace. To the authors' knowledge, all these integrated  
45 improvements of FCWR roller, single guide rolling and horizontal mill are innovative,  
46 which are of great engineering significance to manufacture hollow shafts on account of  
47 the advantages of avoiding forming defect, reducing roller diameter, improving rolling  
48 stability and simplifying mill structure.

49 **Keywords:** Flat-knifing cross-wedge rolling; Horizontal cross-wedge rolling mill;  
50 Multifunctional rolling mill; Single guide rolling; Hollow shafts rolling

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**Nomenclature**

57

$\alpha$  Forming angle

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$\beta$  Stretching angle

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$B$  Knifing width

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$L$  Sizing width

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$\eta$  Workpiece reduction

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$h$  Wedge height

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$d_m$  Mandrel diameter

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$D_0, d_0$  Outer and inner diameter of workpiece before rolling

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$D_1, d_1$  Outer and inner diameter of workpiece after rolling

66

$L_{N1}, L_{F1}$  Knifing length of NCWR wedge and FCWR wedge

67

$L_{N2}, L_{F2}$  Stretching length of NCWR wedge and FCWR wedge

68

$L_{N3}, L_{F3}$  Sizing length of NCWR wedge and FCWR wedge

69

$L_R$  Wedge length reduction from NCWR to FCWR

70

## 71 **1 Introduction**

72 Since hollow shafts have advantages of lightweight structure, low rotating inertia  
73 and convenient flaw detection, more and more solid parts are designed to be hollow  
74 such as railway axles [1], engine valves [2], and truck shafts [3]. Up to now, these  
75 hollow shafts are mainly formed by forging, extrusion and drilling, which result in the  
76 waste of material and low production efficiency.

77 Cross wedge rolling (CWR), a near-net shape metal manufacturing process with  
78 high production efficiency and low material consumption, has an extensive application  
79 in solid shafts including large-elongated parts (e.g., automobile camshafts, stepped  
80 shafts) and die-forging preforms (e.g., engine valves, connecting rods, double-ended  
81 spanners) as reviewed by Hu et al. [4] and Pater et al. [5]. Hu et al. [4] pointed out they  
82 have established more than 300 production lines worldwide with an estimated  
83 production value of more than \$200 million per year, and highlighted that the weight of  
84 CWR products has over 400,000 tons with an amount of 2 billion pieces per year in  
85 China. However, although CWR has been successfully used on solid shafts, it is less  
86 common on hollow shafts.

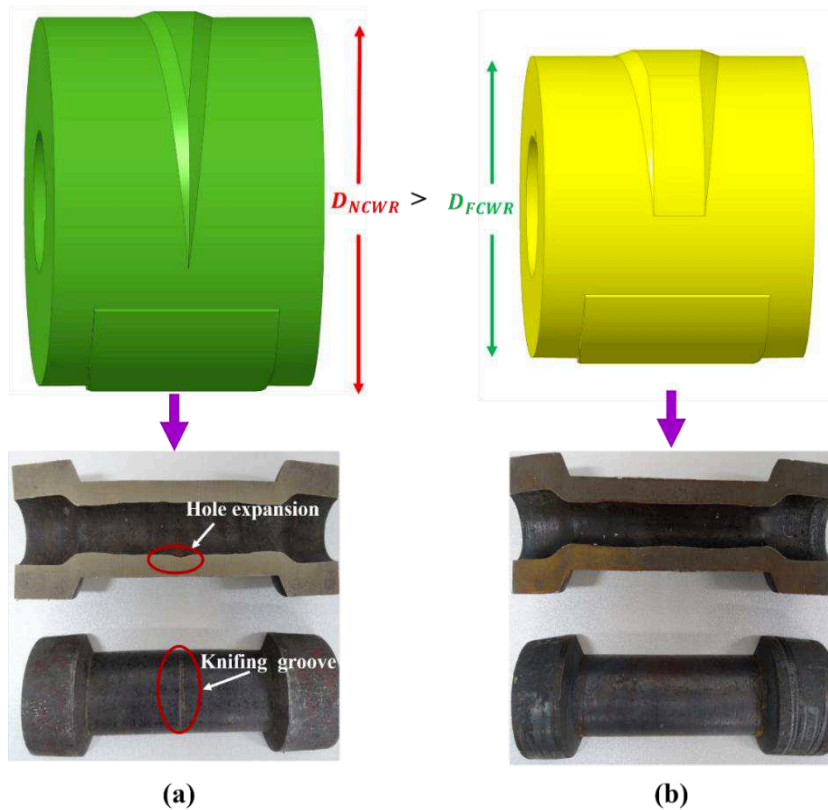
87 Compared with forging, extrusion and drilling process, CWR of hollow shafts has  
88 advantages of high efficiency, not need lubricant and less loading. Researchers have  
89 been concerned about its applications. Huo et al. [6] presented a CWR process for high-  
90 speed railway axles, and predicted the microstructure and ductile damage at hot forming.  
91 Ji et al. [2] proposed to manufacture hollow valve-preforms by CWR, and investigated  
92 the influence of process parameters. Yang et al. [3] developed a process of CWR hollow  
93 axle sleeve, and studied the elliptical behavior of inner hole. Pater et al. [7] presented a  
94 conception of the three-roller cross rolling process of hollow rail axles, and found that  
95 the walls of formed steps are thickened. Peng et al. [8] used a multi-wedge CWR  
96 without mandrel to produce hollow high-speed railway axle, and reached a conclusion  
97 that the double-wedge CWR for large and long thick-walled hollow shafts is feasible.  
98 These works are meaningful and have pointed out a new approach to manufacture

99 hollow shafts.

100 To establish a reliable technique for rolling hollow shaft, CWR without mandrel  
101 was early proposed and investigated. Bartnicki and Pater [9, 10] analyzed the numerical  
102 simulation results and found the thinner wall thickness may cause the slipping and  
103 flattening of billet, and concluded the three-roller CWR can improve rotation conditions.  
104 Urankar et al. [11] proposed a dimensionless crushing parameter to predict forming  
105 limit of the hollow products, and the defect of hole expansion was shown in their study.  
106 However, CWR without a mandrel has a common shortcoming that its inner hole is  
107 unable to be regularly formed because the hole is formed randomly.

108 A process of CWR with mandrel was proposed to control the dimensions of inner  
109 hole, and researches have been done to improve its forming performance. Neugebauer  
110 et al. [12] proposed two ways to control the movements of mandrel: fixed or freedom  
111 mandrel. Landgrebe et al. [13] modified the typical CWR via adding a drilling mandrel,  
112 therefore a hollow shaft can be directly rolled from a solid billet. Shen et al. [14, 15]  
113 used a compensated mandrel to produce hollow shafts with a variable inner diameter.  
114 Recently, Shen et al. [16] based on the volume consistency principle, and established a  
115 theoretical model to predict the critical mandrel diameter. However, many of these  
116 researches have focused on mandrel design and parameter optimization, but pay less  
117 attention to roller modification.

118 In normalized CWR with mandrel, as shown in Fig.1, although inner hole can be  
119 controlled, it brings about the defects of hole expansion and knifing groove [17-20].  
120 Hole expansion exists on the inner hole, while knifing groove on the outer surface.  
121 These defects reduce the utilization of materials and increase the cost of post-processing.  
122 Ji et al. [17] employed variable stretching angle to avoid hole expansion, but make roller  
123 design complicated. In engineering practice, skilled workers generally solve the hole  
124 expansion by chamfering knifing-wedge. Actually, both hole expansion and knifing  
125 groove occur in the knifing position of rolled shafts. Therefore, modifying the shape of  
126 roller on knifing zone is of great significance.



127 **Fig. 1** Contrast between two methods for hollow shafts: (a) normalized CWR; (b)  
 128 flat-knifing CWR

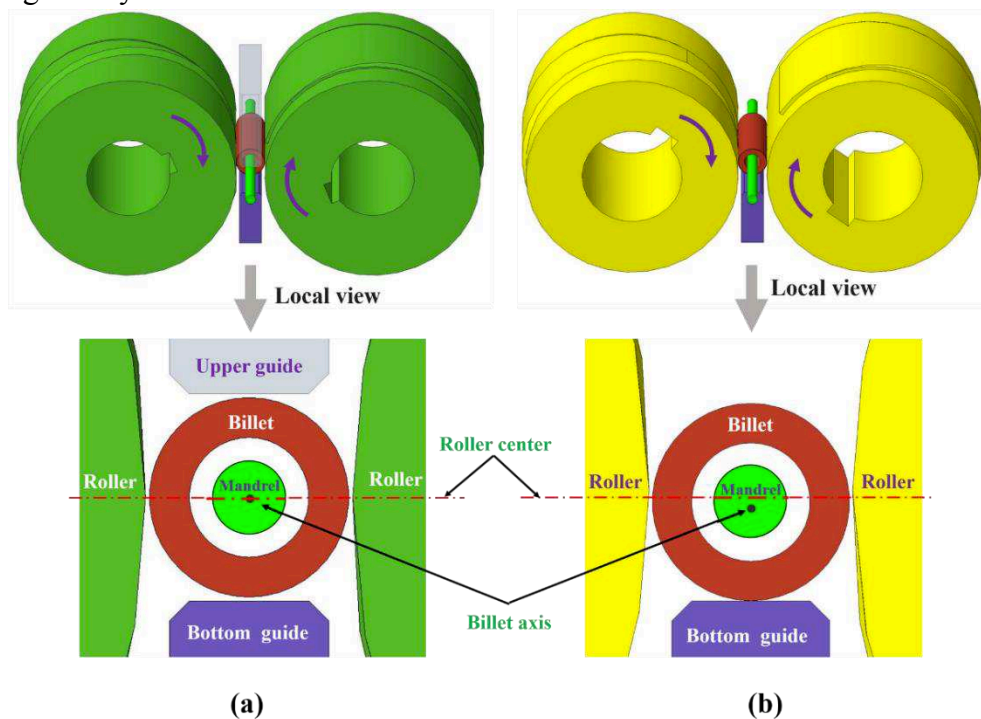
129 In this study, a novel flat-knifing cross-wedge rolling (FCWR) with single guide  
 130 for hollow shafts (Fig.1b) is proposed whereby modifying roller and mill from the base  
 131 of normalized cross-wedge rolling (NCWR), which takes advantages of avoiding the  
 132 defects of hole expansion and knifing groove, reducing the diameter of rollers,  
 133 improving rolling stability and simplifying mill structure.

134 In order to study the new process systematically, its key points are investigated by  
 135 numerical simulation and experimental research. Firstly, the new process of FCWR  
 136 with single guide is described in detail. Secondly, the mathematical model of FCWR  
 137 roller is established and the length reduction is calculated and visually presented.  
 138 Thirdly, numerical simulations are conducted to compare the NCWR and FCWR  
 139 process from the aspects of defect formation mechanisms, workpiece deformation  
 140 characteristics and influences of new parameter. At last, corresponding physical FCWR  
 141 experiments are performed to verify the FE results, and the advantages and  
 142 disadvantages of these improvements are discussed.

## 143 2 Flat-knifing cross-wedge rolling with single guide

### 144 2.1 Novel process principle

145 The process principles of normalized cross-wedge rolling (NCWR) with two  
146 guides and flat-knifing cross-wedge rolling (FCWR) with single guide are shown in Fig.  
147 2. They have same deform mechanism that a cylindrical hollow billet is deformed into  
148 a stepped hollow shaft under the action of roller whereby wedged rollers moving  
149 tangentially relative to each other.



150 **Fig. 2** Process principle: (a) NCWR with two guides; (b) FCWR with single guide

151 There are some improvements: 1) the knifing wedge of FCWR roller is flatted,  
152 while that of NCWR is sharpened; 2) differing from NCWR has a vertical structure,  
153 FCWR process changes into a horizontal arrangement that can achieve single guide  
154 rolling under gravity; 3) by single guide rolling, FCWR workpiece is steadily restricted  
155 into a smaller workspace. As a result, the novel process is estimated has advantages of:

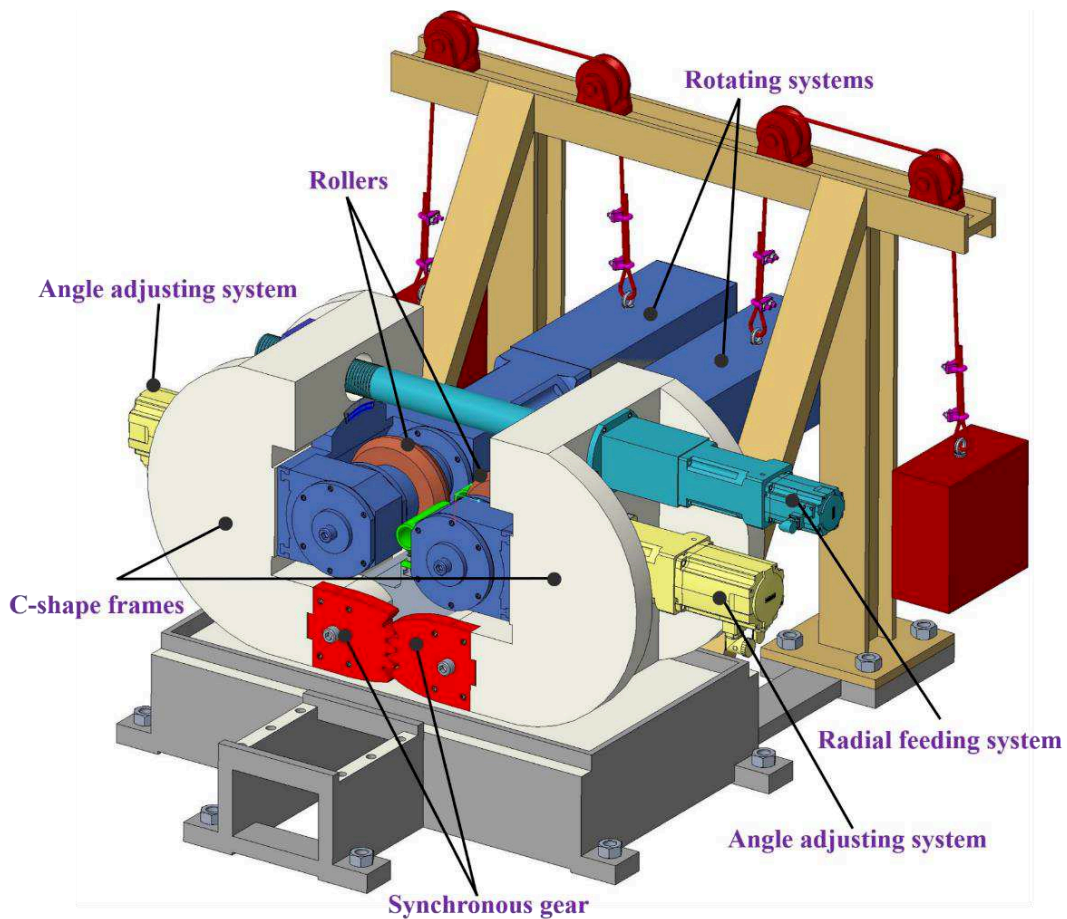
- 156 • the defects of hole expansion and knifing groove can be absolutely avoided;
- 157 • the diameter of two rollers can be evidently shortened;
- 158 • the mill can be simplified into single guide structure;
- 159 • The rolling stability can be improved.



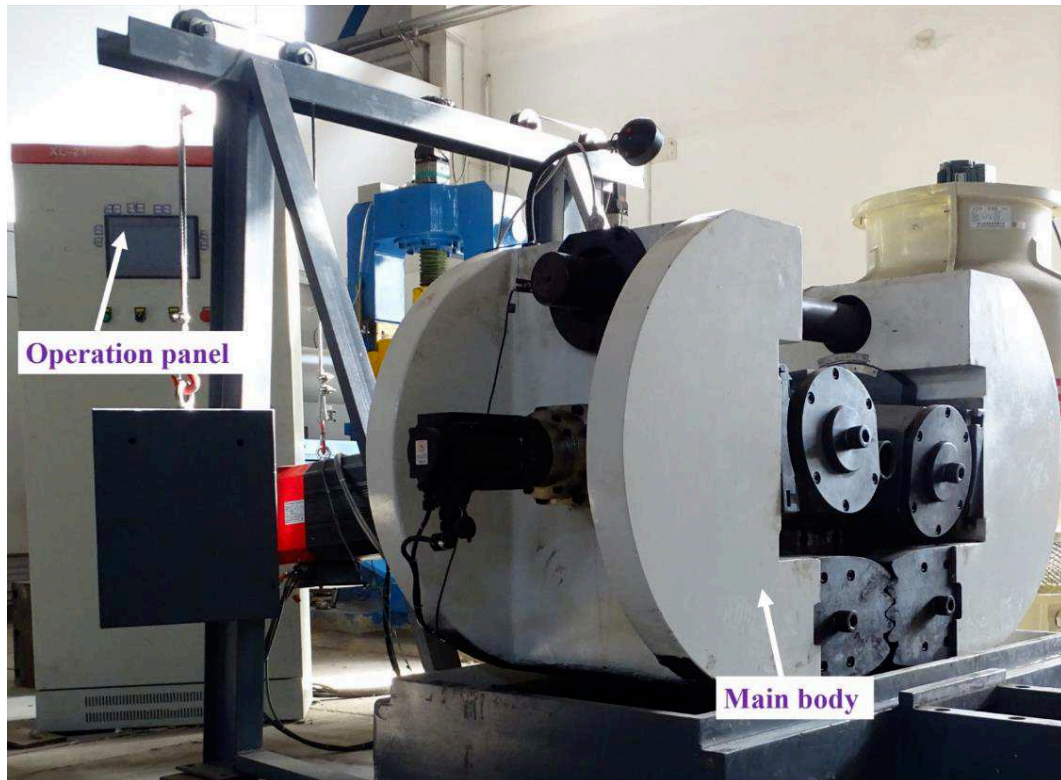
160 **2.2 New type of horizontal multifunctional mill**

161 In order to achieve the technical objective of single guide rolling, a laboratory mill  
162 with a horizontal structure is indispensable. Up to now, the traditional CWR mills  
163 commonly have a vertical structure [4, 5, 22], which apparently cannot meet the  
164 requirement of this study.

165 Therefore, a new type of rolling mill is invented and constructed by the authors  
166 [23]. The freedoms of this mill has been increased by two angle adjusting systems, one  
167 radial feeding system, and a synchronous unit (worked by two matched gears). Its 3D  
168 model is shown in Fig. 3, the mill is presented in Fig. 4, and the technical specifications  
169 are given in Table. 1.



170 **Fig. 3** Geometrical model of the horizontal multifunctional mill [23]



**Fig. 4** The constructed horizontal multifunctional mill [23]

**Table 1** Technical specifications of the horizontal multifunctional mill

Parameter	Unit	Value
Power of main rotating motor	kW	2×30
Speed of main rotating	rpm	0~43
Power of Radial feeding motor	kW	3
Speed of Radial feeding	mm/s	1~5
Power of angle adjusting motor	kW	2×2.3
Speed of angle adjusting	°/s	1~10
Range of angle adjusting	°	±12
Maximum diameter of roller	mm	350
Maximum diameter of billet	mm	80
Overall dimensions	m	1.8×1.7×1.6
Total power	kW	70
Total weight	ton	5

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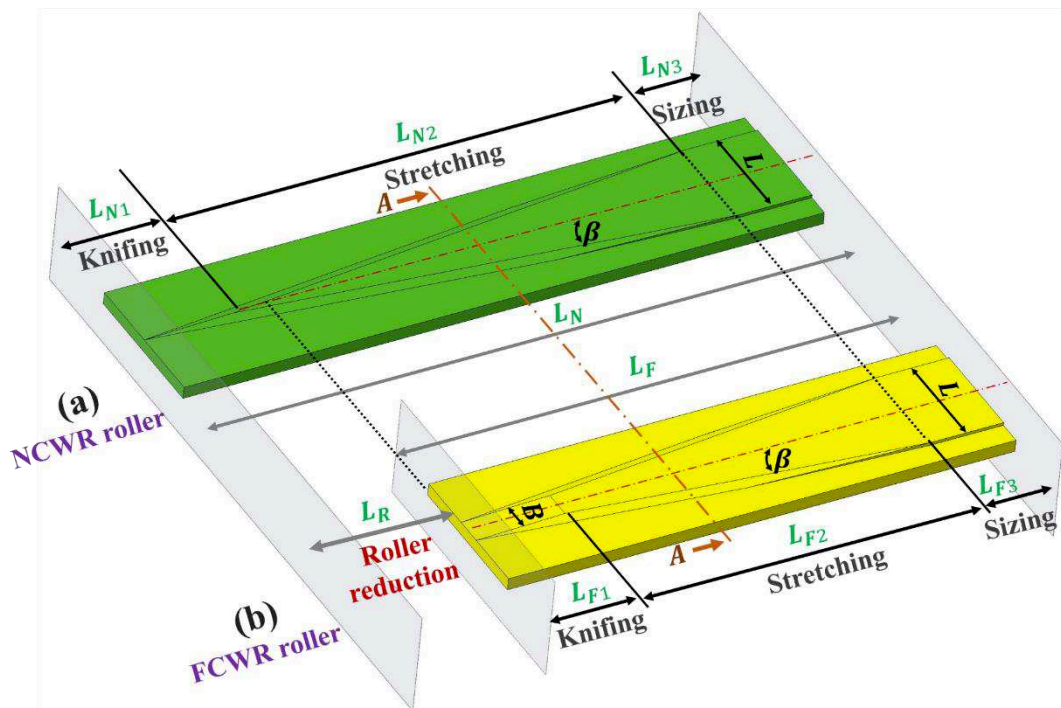
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175 This mill is characteristic of multiple freedom degree because has several  
 176 movements of circumferential rotating, radial feeding and angle adjusting, and thus it  
 177 can be used for different types of laboratory rolling tests such as longitudinal rolling,  
 178 cross rolling, and skew rolling.

179 All the motions of this mill are directly driven by servo motors that mill structure  
 180 is compact. As signed in Fig.3, two C-type frames are used to enhance mill strength,  
 181 the automation system is controlled by a accurate servo drive which programed in PLC  
 182 language. All these features may take this type of mill advantages of compact structure,  
 183 high strength and high precision, so that it can be expected to be industrially applied as  
 184 thread rolling mill, ball rolling mill and CWR mill.

### 185 2.3 New type of flat-knifing roller

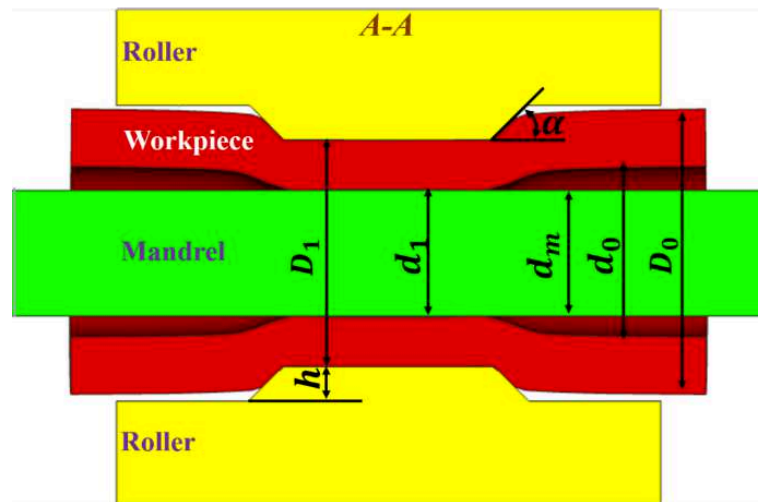
186 Roller modification is a main innovation of this paper. In the hope of  
 187 mathematically describing the FCWR roller in detail, both the geometrical models of  
 188 FCWR and NCWR roller are designed and shown in Fig. 5 with a plane layout way.



189 **Fig. 5** Configuration and major parameters of NCWR and FCWR roller

190 There is an obvious difference observed in the figure that the knifing zone of  
 191 NCWR roller is designed as a V-shaped wedge, while FCWR roller is a flat-wedge with

192 a width of  $B$ . Further, the FCWR roller only changes the wedge shape in the knifing  
 193 zone, and their configurations are identically divided into three sections as knifing zone,  
 194 stretching zone and sizing zone. Fig. 6 shows that their contact models (extracted from  
 195 the A-A view of Fig. 5) between roller, mandrel and workpiece of FCWR and NCWR  
 196 roller are exactly same on stretching zone. To make an analysis, on the one hand, the  
 197 main deformation of FCWR rolling is occurred in stretching zone, where FCWR has  
 198 the same contact model with NCWR. On the other hand, FCWR process have the same  
 199 sizing zone with NCWR. As a conclusion, these modifications have not changed the  
 200 process parameters form the NCWR, so that both NCWR and FCWR may have the  
 201 same process parameters such as forming angle  $\alpha$ , stretching angle  $\beta$  and mandrel  
 202 diameter  $d_m$ .



203 **Fig. 6** Contact model of roller, mandrel and workpiece at the stretching stage

204 In order to mathematically compare FCWR and NCWR roller, the calculation of  
 205 wedge length is a basic work, which need to be undertaken primarily.

206 At the knifing zone, notwithstanding the different geometries, the wedge lengths  
 207 of FCWR and NCWR roller are equally formulated as Eq. 1, where  $h$  is the height of  
 208 wedge,  $\alpha$  is forming angle, and  $\beta$  is the stretching angle.

$$209 \quad L_{N1} = L_{F1} = h \cot \alpha \cot \beta \quad (1)$$

210 At the stretching zone, because the initial position of FCWR wedge have a straight  
 211 section,  $L_{N2}$  is obviously longer than  $L_{F2}$ , and they are respectively calculated by Eq. 2

212 and Eq. 3, where  $L$  represents the sizing width (signed in Fig. 5) and  $B$  represents the  
 213 knifing width.

$$214 \quad L_{N2} = 0.5L \cot \beta \quad (2)$$

$$215 \quad L_{F2} = 0.5(L - B) \cot \beta \quad (3)$$

216 Owing to the geometries at sizing zone of NCWR and FCWR are exactly same,  
 217 they have same sizing length which can be formulated by Eq. 4, where  $D_0$  and  $D_1$  are  
 218 the outer diameter of the workpiece before and after rolling.

$$219 \quad L_{N3} = L_{F3} > 0.25\pi(D_0 + D_1) \quad (4)$$

220 Because the length of each zone is determined through the above equations, the  
 221 length reduction  $L_R$  can be calculated by Eq. 5.

$$222 \quad L_R = 0.5B \cot \beta \quad (5)$$

223 For a purpose of a more intuitive comparison of the wedge length of roller, their  
 224 formulas are summarized in Table 2. It can be concluded that the lengths of knifing  
 225 wedge and sizing wedge of NCWR and FCWR roller are equal in value, while FCWR  
 226 stretching length is shorter than that of NCWR.

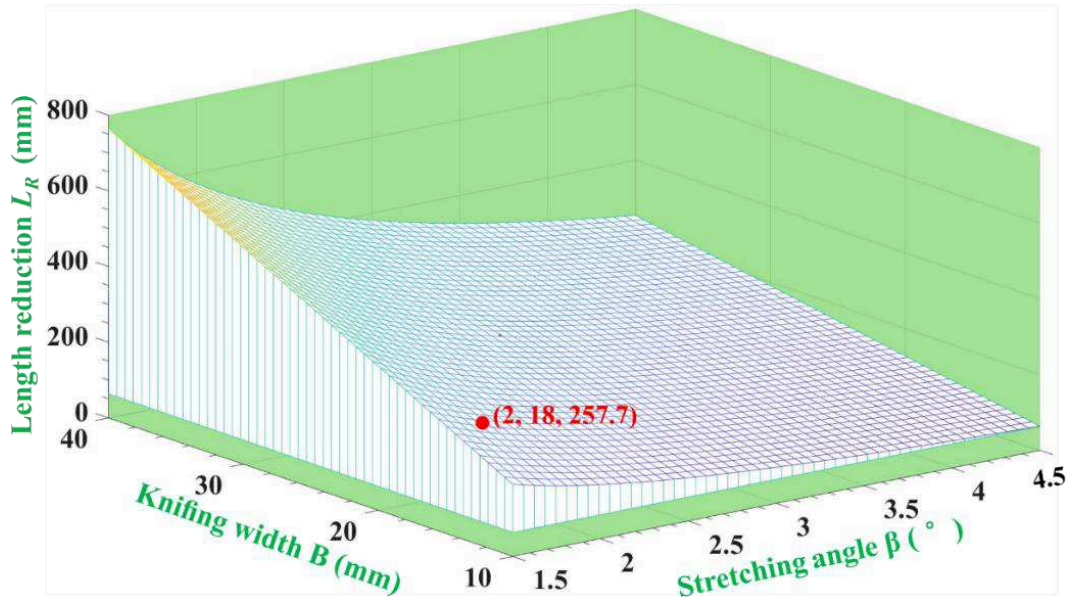
227 **Table 2** Mathematical comparison of the wedge lengths of NCWR and FCWR roller

Type	NCWR	FCWR	Comparison
	$L_{N1} = h \cot \alpha \cot \beta$	$L_{F1} = h \cot \alpha \cot \beta$	$L_{N1} = L_{F1}$
Equation	$L_{N2} = 0.5L \cot \beta$	$L_{F2} = 0.5(L - B) \cot \beta$	$L_{N2} > L_{F2}$
	$L_{N3} = 0.25\pi(D_0 + D_1)$	$L_{F3} > 0.25\pi(D_0 + D_1)$	$L_{N3} = L_{F3}$
Length reduction	$L_R = 0.5B \cot \beta$		

228 In order to visually reveal the relationship between wedge-length reduction and  
 229 process parameters, a three-dimensional graphic have been drawn as expressed in Fig.  
 230 7. The length reduction  $L_R$  is only related to stretching angle  $\beta$  and knifing width  $B$ ,  
 231 which increases with the increase of  $B$  and  $\beta$  in range of 200~800mm. Take an example  
 232 of the roller used in the experiment of later study:  $\beta=2^\circ$ ,  $B=18$  mm, its wedge length

233 reduction reaches up to 257.7 mm.

234



235 **Fig. 7** Relationship between wedge-length reduction and process parameters

### 236 **3 Parameter ranges and research schemes**

237 Considering process parameters will directly affect whether this novel process is  
238 successful or not, the ranges of major parameters are discussed and summarized based  
239 on the previous research of NCWR hollow shafts [16, 17, 24].

240 (1) The workpiece reduction  $\eta$ . Workpiece reduction reflects deformation degree  
241 and the flattening of workpiece. In the case of hollow billet with thin wall, the large  $\eta$   
242 make the rolling piece undergo serious flattening deformation and then the rolling status  
243 is instability, so that the products become elliptical finally. In addition, when the hollow  
244 billet has a thick wall, in this case the rolled piece has a better resistance to flattening  
245 deformation, the roundness of the rolled products is improved under the condition of a  
246 larger  $\eta$  because of the good flow of axial metal. The workpiece reduction  $\eta$  is expressed  
247 and ranged as Eq. 6.

248 
$$0.2 < \eta = \frac{D_0 - D_1}{D_0} < 0.4 \quad (6)$$

249 (2) The forming angle  $\alpha$ . Forming angle is an important roller parameter, which  
250 directly determines the contact surface of of forming area and then affects the metal

251 flow. In the reason that hollow billet is more prone to elliptical and then the axial flow  
252 of the metal may become worse, the forming angle of the hollow shafts rolling is  
253 generally greater than that of solid shafts, whose value is usually derived as follows:

$$254 \quad 30^\circ < \alpha < 50^\circ \quad (7)$$

255 (3) The stretching angle  $\beta$ . Stretching angle is another important tool parameter.  
256 Increasing its value is beneficial to decrease the length of roller but enlarges the  
257 tangential deformation of the workpiece, as a result, it is easy to cause oval deformation.  
258 Therefore, the stretching angle for hollow shafts is generally smaller than solid shafts,  
259 its range is:

$$260 \quad 1.5^\circ < \beta < 4.5^\circ \quad (8)$$

261 (4) The mandrel diameter  $d_m$ . The mandrel is used to control the shapes and  
262 dimensions of inner hole. When its diameter is too small, mandrel will unable to contact  
263 inner hole and out of service. And when its value gets too large, it makes the rolling  
264 wall thin seriously and wall deformation become severe, thus billet cannot rotate  
265 normally. Its value is usually designed as Eq. 9, in which  $d_0$  is the initial diameter of  
266 inner hole.

$$267 \quad 0.5d_0 < d_m < 0.9d_0 \quad (9)$$

268 (5) The knifing width  $B$ . Knifing width is a new parameter which only exists on  
269 FCWR roller. On the basis of previous explorations (discussed in later sections), larger  
270 knifing width allow for less length of wedge but increase workpiece ellipticity, rolling  
271 force, and rotating torque. Its value is generally selected as:

$$272 \quad 10 \text{ mm} < B < 40 \text{ mm} \quad (10)$$

273 On the basis that the selection ranges of main parameters have been determined, a  
274 research scheme combined FE simulations and experimental tests has been worked out  
275 as demonstrated in Table 3. The FE simulation is adopted to compare the distinction on  
276 NCWR and FCWR from the aspects of defect mechanisms, deformation characteristics  
277 and influences of new parameter. Correspondingly, the physical FCWR tests are  
278 conducted to verify the FE results and reveal the advantages and disadvantages of

279 FCWR process.

280

**Table 3.** Research schemes and parameter values

Parameter symbol (unit)	Billet inner diameter $d_0$ (mm)	Mandrel diameter $d_m$ (mm)	Knifing width $B$ (mm)	Method
NCWR	30	none	none	FE
	30	22	none	FE
FCWR	30	none	18	FE, Test
	30	22	14, 18, 22	FE
	30, 28, 26, 24	22, 20.5, 19, 17.6	18	Test

281

Besides,  $D_0=50$  mm,  $\alpha=45^\circ$ ,  $\beta=2^\circ$ ,  $h=6$  mm,  $T=1050$  °C,  $d_m/d_0=0.73$ .

282

## 4 Numerical simulations of NCWR and FCWR with single guide

283

### 4.1 Finite element modeling

284

Preliminary feasibility study was done by numerical simulations. Both NCWR and

285

FCWR finite element (FE) models were established. It should be pointed out that, the

286

FE model of NCWR and FCWR only changed the rollers while other parameters such

287

as billet dimensions, rolling temperature and mandrel dimensions stayed the same. The

288

FE scheme and parameter were carried out according to Table 3.

289

The FE projects were performed in Simufact.Forming software, which has been

290

successfully employed in numerical analysis of CWR process [25, 26] and skew rolling

291

process [27, 28], and their FE results have a good agreement with experimental results.

292

The FE projects of NCWR and FCWR with single guide were modeled as Fig. 8 shows.

293

Both the geometric models of NCWR and FCWR were consisted of two rollers, one

294

guide, one mandrel and one workpiece. The positional relationships between each part

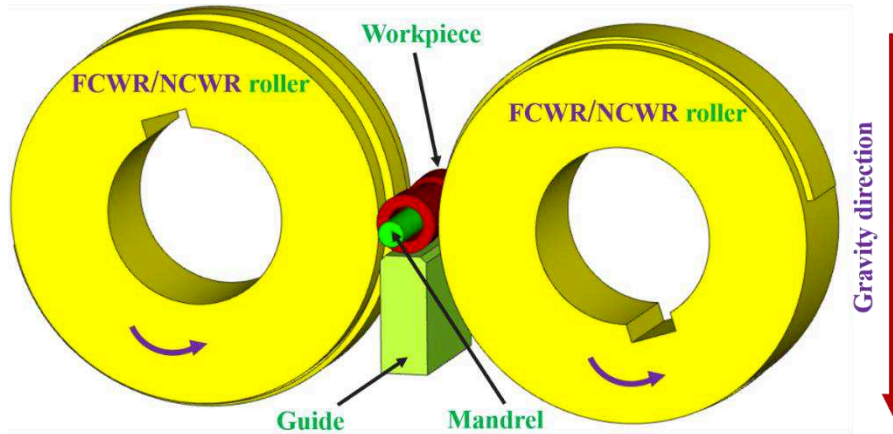
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were set up as marked in Fig. 2. The workpiece axis was downwardly offset from roller

296

centre with a 3 mm distance.





297 **Fig. 8.** FE projects of FCWR and NCWR with single guide.

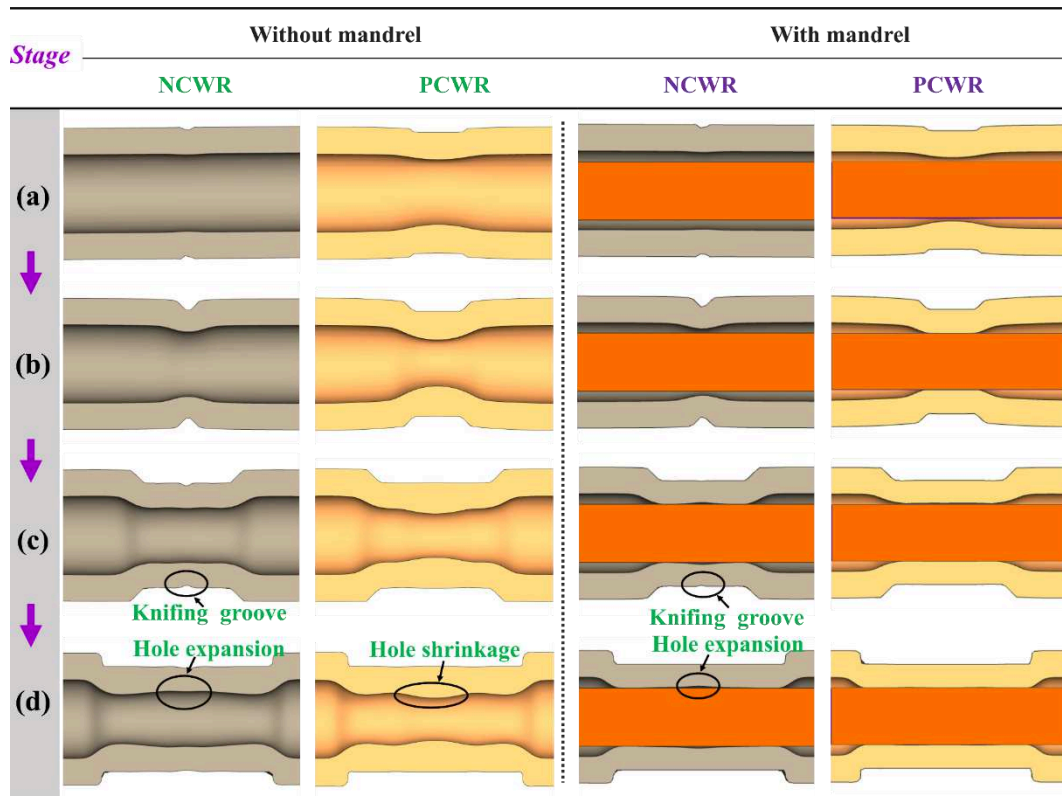
298 The billet is C45 steel rod with an outer diameter of 50 mm, an inner diameter of  
 299 30 mm and a length of 100 mm. Its material data were taken from Simufact.Material.  
 300 The properties (i.e., density, Young's modulus and Poisson's ratio) were set as default.  
 301 The flow stress of C45 steel was defined by Eq. 11, in which  $\sigma_F$  is the flow stress (MPa),  
 302  $\phi$  is the effective strain (-) and  $T$  is the temperature ( $^{\circ}\text{C}$ ):

$$303 \quad \sigma_F = 2589.85e^{-0.003125T} \phi^{(0.00004466T-0.10127)} e^{(-0.000027T+0.0008183)/\phi} \dot{\phi}^{(0.00015T-0.002749)} \quad (11)$$

304 The friction coefficients between tools and workpiece were modeled by Shear  
 305 model (two rollers were 0.8, guide and mandrel were 0.2. [28] The temperature of tools  
 306 (rollers, guide and mandrel) was constantly maintained at 300  $^{\circ}\text{C}$  [28]. The initial  
 307 temperature of workpiece was 1050  $^{\circ}\text{C}$  and the coefficient of heat transfer between tools  
 308 and workpiece was 10  $\text{kW}/\text{m}^2\text{K}$  [28]. Besides, the mesh of billet was created by  
 309 ringmesh mesher, whose element size equals to 1.4 mm, and will be automatically  
 310 reconstructed if the effective strain increases by 0.4 [28]. Both the NCWR and FCWR  
 311 rollers rotated at a same speed of 6 rpm.

## 312 4.2 Comparison of forming defects

313 Four FE results with the parameters of  $D_0=50$  mm,  $d_0=30$  mm,  $\alpha=45^{\circ}$ ,  $\beta=2^{\circ}$ ,  
 314  $d_m=22$  mm and  $B=18$  mm was extracted from the software postprocessor and shown in  
 315 Fig. 9. With the help of the numerical simulation, the shape of rolling workpiece can be  
 316 acquired at every moment.



317 **Fig. 9** FE results of NCWR and FCWR: (a) middle of knifing stage; (b) end of knifing  
318 stage; (c) middle of stretching stage; (d) end of stretching stage

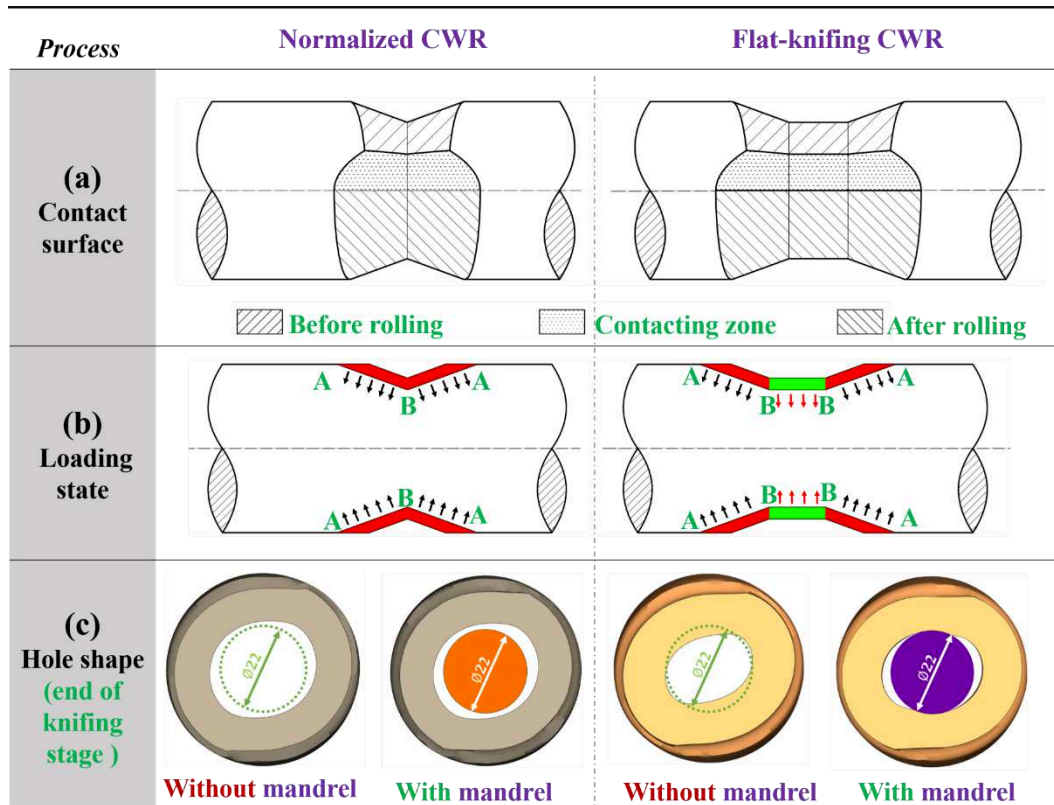
319 At the middle of knifing stage, all the workpieces are not contact with mandrel.  
320 But at the end of knifing stage, there is a difference that FCWR workpiece contacts with  
321 mandrel while NCWR does not. Considering the values of mandrel diameters are the  
322 same, it can be concluded that, the radial deformation of inner hole in FCWR process  
323 is more serious than that in NCWR during the whole knifing stage.

324 The defects of hole expansion and knifing groove primitively appear on the  
325 NCWR shafts at the middle of stretching stage regardless of whether it has mandrel or  
326 not (Fig.9c). But in the case of FCWR shafts at this stage, these defects are completely  
327 absent. Inversely, there is a hole shrinkage on the FCWR shaft without mandrel. As a  
328 result, we can get the FE conclusion that: 1) no matter with or without mandrel, NCWR  
329 rolled shafts universally have the defects of hole expansion and knifing groove; 2)  
330 FCWR process without mandrel have a defect of hole shrinkage; 3) the FCWR process  
331 with mandrel has a good geometric accuracy on outer and inner surface. The conclusion  
332 optimistically verifies the technological assumptions, as a result, the FCWR with

333 mandrel was adopted on hollow shafts forming in later studies.

#### 334 4.2.1 Hole expansion

335 Since hole expansion is a major defect in this study, it is necessary to reveal its  
 336 formation mechanism from aspects of contact surface, loading states and the shape of  
 337 inner hole (Fig. 10).



338 **Fig. 10** Formation mechanism of hole expansion (end of knifing stage): (a) contact  
 339 surface; (b) loading states; (c) hole shape

340 The contact surface of workpiece was drawn by Boolean subtraction operation in  
 341 CAD software, which has indicated the different of deformation morphology between  
 342 NCWR and FCWR. As shown the Fig. 10a, under the same forming angle  $\alpha$  and  
 343 stretching angle  $\beta$ , the main difference between NCWR and FCWR contact surface is  
 344 that there is a rectangle contacting zone on the middle of FCWR workpiece.

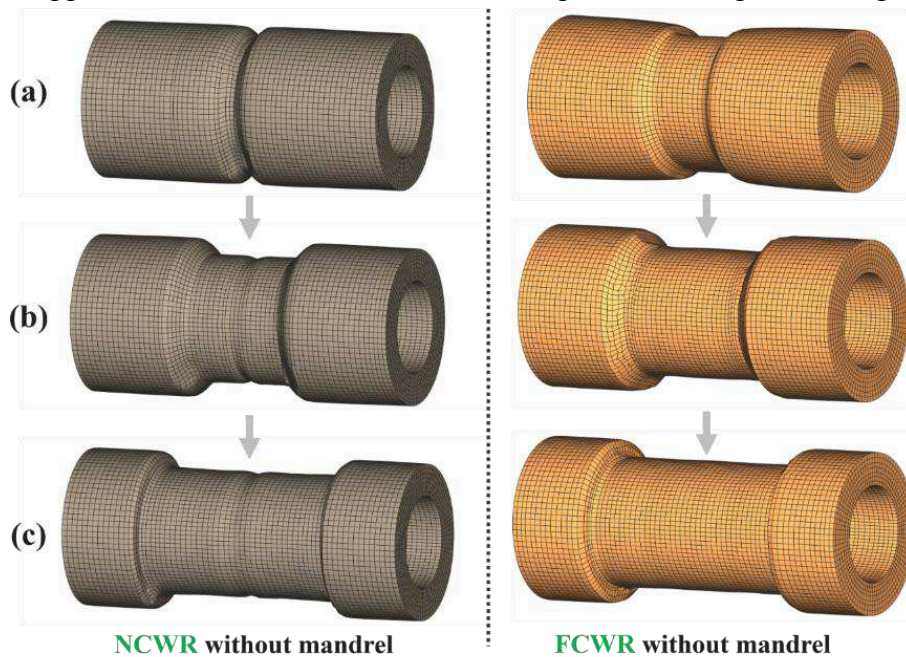
345 Based on the drawn contact surface, the loading states can be acquired as Fig. 10b  
 346 shows. At the NCWR knifing stage, because AB and BA segments individually produce  
 347 a axial component on the side of knifing position, the inner hole is tensioned in axial

348 direction and then expanded radially. But in FCWR process, the added BB segment  
349 provides a radial force during the knifing stage that promotes the radial flow of the  
350 metal, and thus the inner hole is shrunk. Eventually, FCWR hole contacts with the  
351 mandrel while NCWR does not (Fig. 10c).

352 In short, FCWR process has an added radial force during knifing stage, which is  
353 helpful to the radial flow of the metal and then shrink the inner hole, so that the defect  
354 of hole expansion can be avoided in principle.

#### 355 4.2.2 Knifing groove

356 Another defect concerned about in this study is the knifing groove, which typically  
357 appears on the CWR shafts regardless of whether they are hollow or solid [18, 19].  
358 According to engineering practice, this defect can be avoided via chamfering the  
359 knifing-wedge. Obviously, this method cannot solve this defect at design stage. The  
360 geometric appearances of NCWR and FCWR workpiece are compared in Fig. 11.



361 **Fig. 11** Geometry comparison between NCWR and FCWR workpiece: (a) end of  
362 knifing stage; (b) middle of stretching stage; (c) end of stretching stage

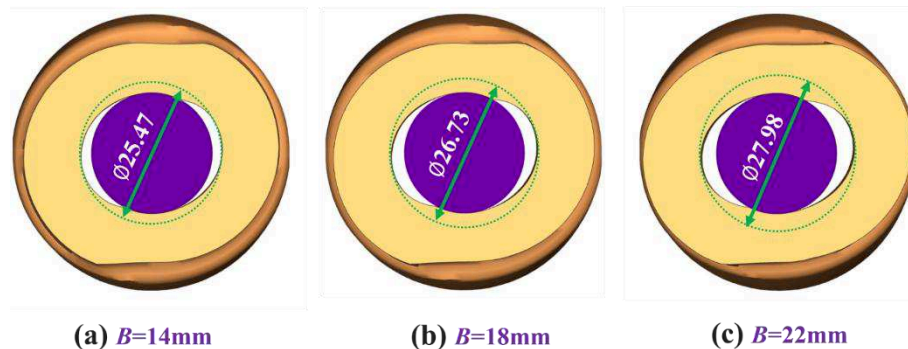
363 The knifing groove initially appears on the NCWR shaft at the end of knifing stage  
364 and then remains until the end. It can be explained that deformation concentration exists  
365 on NCWR knifing area which makes the metal of surface undergo a severe local

366 deformation. As a result, a groove appears on the knifing position. When it comes to  
367 stretching and sizing stage, this defect is hard to be resolved because the height of  
368 wedge is constant. In the FCWR process, there is a flat segment BB existing on the  
369 middle as Fig. 10b shows, which can avoid the concentrated deformation that the defect  
370 of knifing groove does not appeared fundamentally.

### 371 4.3 Effect of new parameter

#### 372 4.3.1 Hole ovality

373 The novel process introduces a new process parameter named knifing width  $B$ .  
374 Since it has an influence on the ovality of inner hole, an observation section selected  
375 from the axial centre of the workpiece are contrastively compared in Fig 12, which  
376 demonstrates that, as the knifing width  $B$  increases, the ovalization of inner hole  
377 becomes serious.



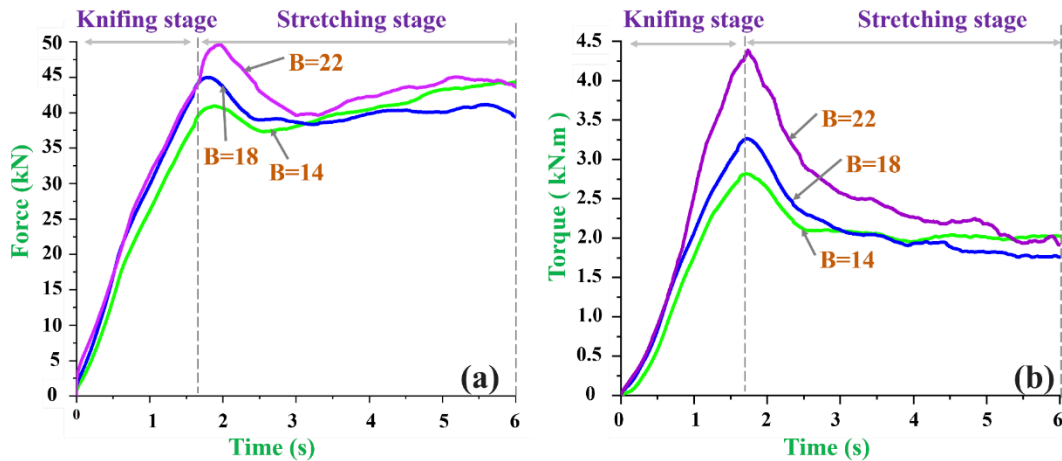
378 **Fig. 12** Relationship between knifing width and hole ovality (end of knifing stage)

379 The ovality of inner hole has negative effect on rolling stability. When the ovality  
380 of inner hole is too large, the radial deformation of workpiece will be unstable. Under  
381 this situation, even if rollers are rotating normally, the slipped billet cannot rotate  
382 regularly. Hence, considering elliptical hole is bad for rolling stability, the value of  
383 knifing width should not be too large.

#### 384 4.3.2 Rolling force and rotating torque

385 Rolling force in the radial direction and rotating torque are the basic data of rolling  
386 equipment, which directly determine the capacity of mill and can be predicted by FE

387 results as shown in Fig. 13.



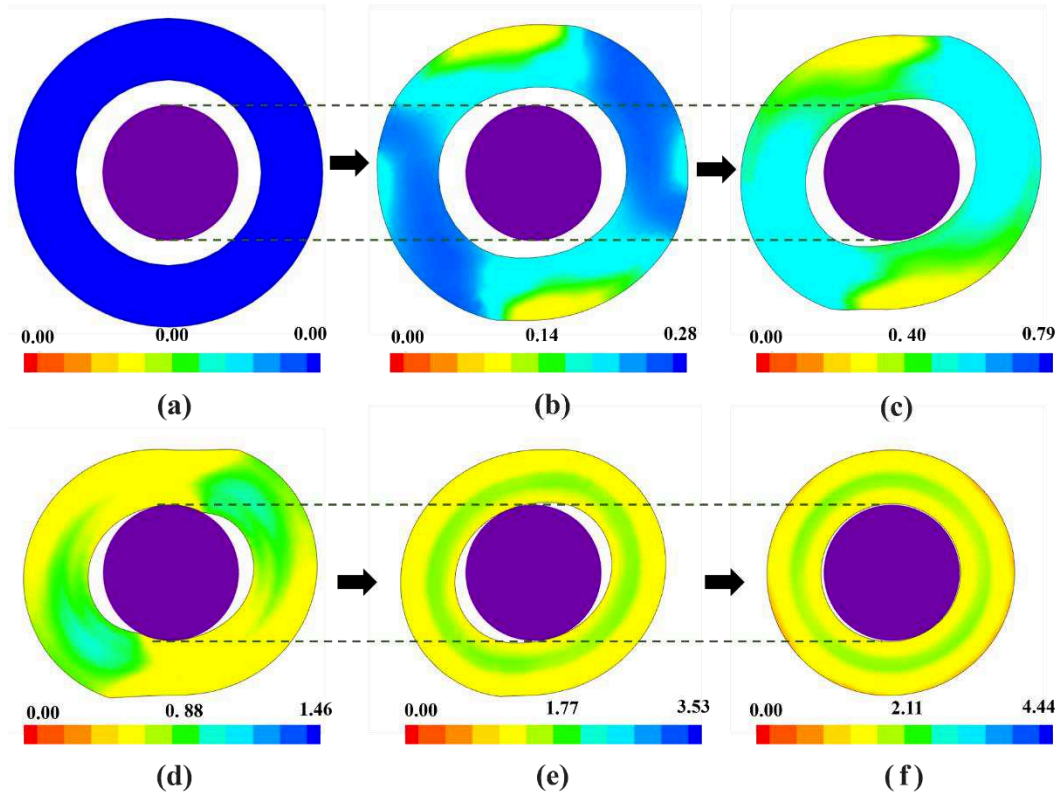
388 **Fig. 13** Relationship between knifing width, (a) rolling force, and (b) rotating torque

389 The trends of rolling force and rotating torque are similar. Both rolling force and  
390 rotating torque gradually increase at the knifing stage and then decrease at the beginning  
391 of stretching stage. The maximum values of rolling force and rotating torque  
392 concurrently appear at the end of knifing stage. Significantly, the knifing width has an  
393 effect on the maximum values of rolling force and rotating torque. With knifing width  
394  $B$  increases, the maximums of rolling force and rotating torque rise as well.

395 Based on above analysis, it can be concluded that large knifing width deteriorates  
396 the ellipse of hole and increases rolling force and rotating torque.

#### 397 4.4 Formation of the inner hole

398 The formation of inner hole is a critical problem of hollow shafts rolling, which  
399 directly influences the forming accuracy and the rolled-wall performance. A cross-  
400 section is selected from the axial center of workpiece and observed at different rolling  
401 stages as Fig. 14 shows.



402

403 **Fig. 14** Formation of the FCWR hole (with strain distribution): (a) initial status; (b)  
 404 begin of workpiece flattening; (c) begin of mandrel contacting; (d) begin of hole sizing;  
 405 (e) middle of hole sizing; (f) end of hole sizing

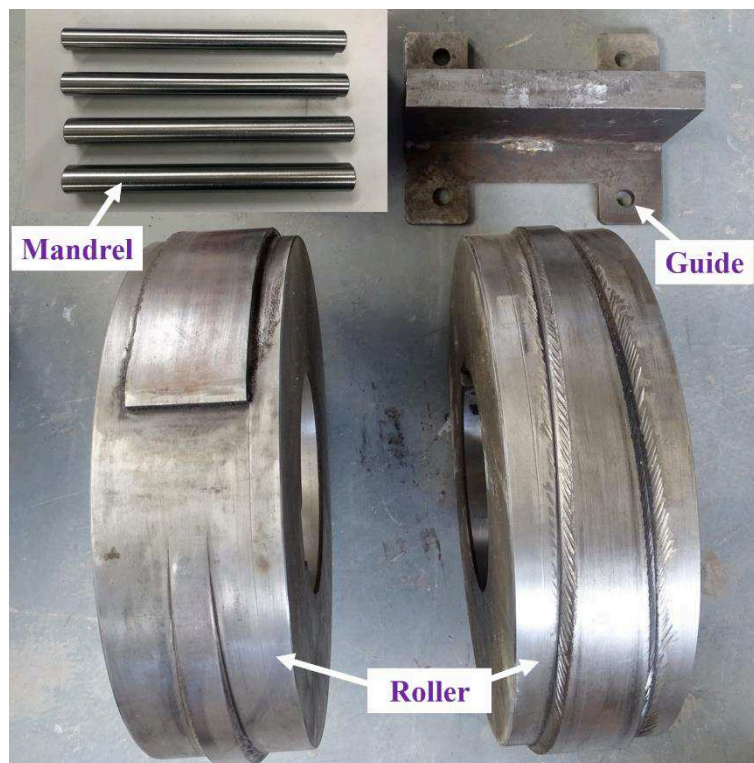
406 Because mandrel diameter  $d_m$  is only 0.73 times of billet hole diameter  $d_0$  as  
 407 mentioned in Table 3, the mandrel is away from the inner hole and out of work at the  
 408 initial stage. However, as rolling process goes on, the inner hole becomes elliptical and  
 409 then workpiece is beginning to contact the mandrel. Latterly, under the double action  
 410 of mandrel and rollers, the ovality of inner hole becomes small and small and finally  
 411 growth into round.

412 The strain distribution of the workpiece is also obtained in Fig. 14. Initially, the  
 413 billet has local strain at the contacting zone with a small value. But at the hole sizing  
 414 stage, both the outer and inner of billet undergo a large strain with a value approximate  
 415 1.7, which have demonstrated an important advantage of FCWR with mandrel – the  
 416 wall of workpiece is rolled by external roller and internal mandrel that the properties of  
 417 rolled wall can be improved effectively.

## 418 5 Experiments of FCWR with single guide

### 419 5.1 Rolling experiments

420 The experiments of FCWR hollow shafts with single guide were performed at  
421 University of Science and Technology Beijing in the new type of horizontal mill.  
422 Experimental tools consisted of two FCWR rollers, several mandrels and one guide as  
423 shown in Fig. 15.

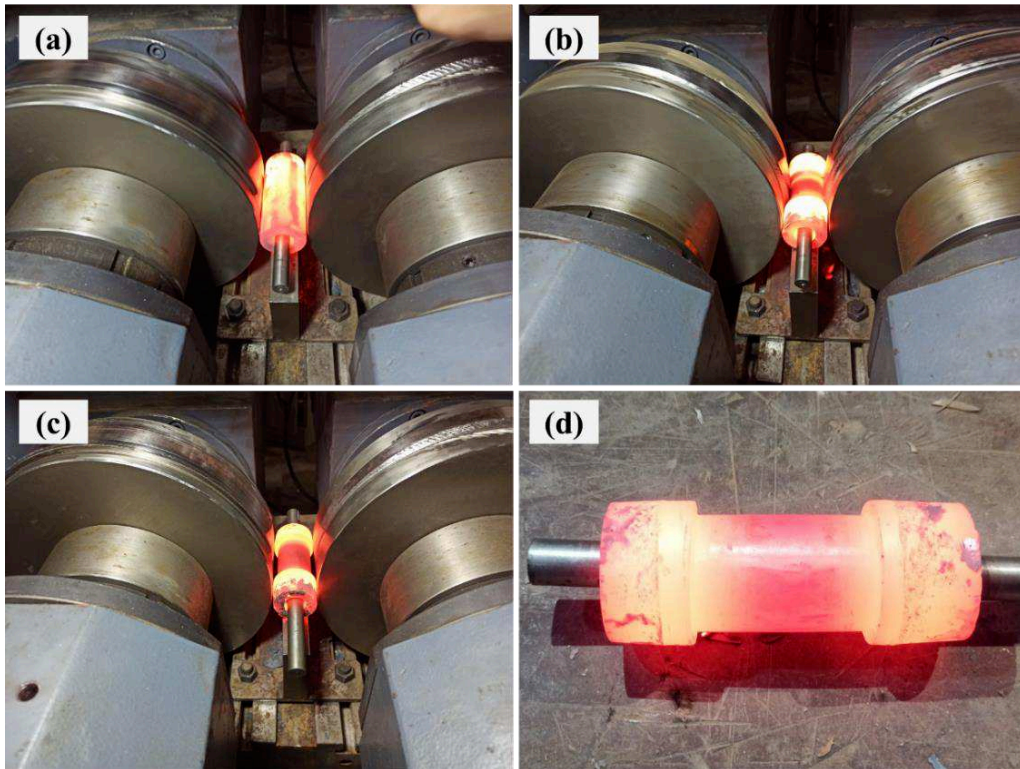


424 **Fig. 15** Tools for FCWR experiments with single guide for hollow shafts

425 The process parameters of physical experiments corresponded to those of  
426 numerical simulations as shown in Tab.3. The guide was mounted between two rollers  
427 and downwardly offset from roller centre line with a 28 mm distance.

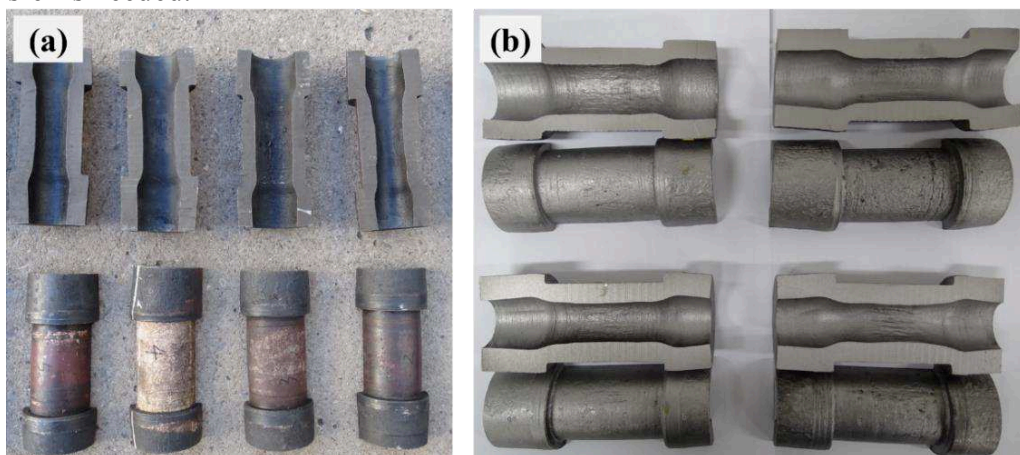
428 The rolling experiments was conducted as Fig. 16 shows. Prior to the rolling, the  
429 billet was preheated to 1050 °C in an electric tube furnace and then immediately  
430 transferred to the mill. During the rolling stage, the billet was rotated and deformed  
431 under the action of rotating wedges of rollers. After the rolling, the rolled product laid  
432 on the top of the guide and then hollow shaft was gained.





433 **Fig. 16** FCWR rolling experiments in horizontal multifunctional mill with single  
 434 guide: (a) beginning; (b) rolling stage; (c) ending stage; (d) rolled hollow shaft

435 By the FCWR tests, it can be observed that the workpiece was rolled stably, which  
 436 has verified the feasibility of the FCWR process and new horizontal multifunctional  
 437 mill. The produced hollow axles of FCWR rolling tests were cut and shown in Fig. 17a,  
 438 and its shot peening products are shown in Fig. 17b. These hollow shafts are free from  
 439 the typical defects of hole expansion and knifing groove. However, it raises a new  
 440 question that the rolled shaft cannot be automatically ejected from the mill that a manual  
 441 transfer is needed.

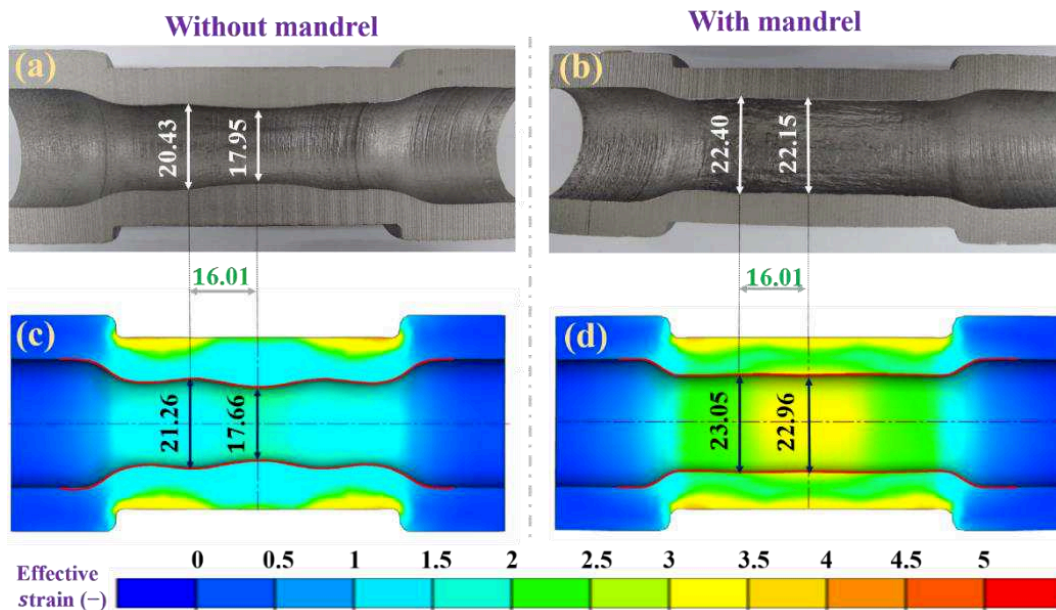


442 **Fig. 17** The FCWR produced hollow shafts: (a) initial status; (b) after shot peening

443 **5.3 Results and Discussion**

444 **5.3.1 Validating of the FEM results**

445 A verification method of geometric comparison is employed in this study. The  
446 geometries of inner holes are compared to verify the FEM results in consideration of  
447 its shapes are related to the flow behavior of material, rolling temperature, friction state  
448 and so on. Two groups of experiments including without and with mandrel are  
449 compared in Fig.18.



450 **Fig. 18** Geometry comparison between (a, b) physical experiments and (c, d)  
451 numerical simulations

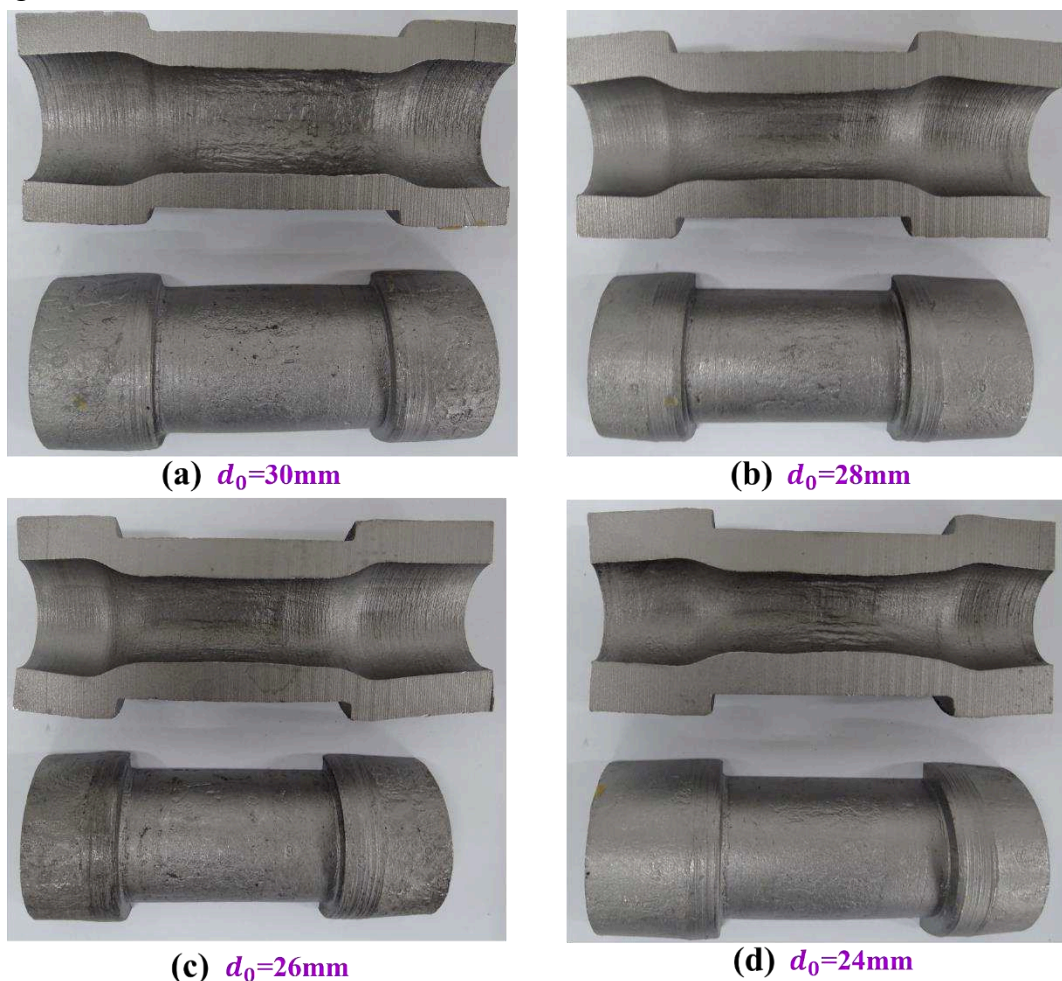
452 The shape of rolled shafts of experimental tests have a good agreement with FE  
453 results. In the rolling process without mandrel, both physical and FE shafts have a  
454 defect of hole shrinkage on knifing position. But under the circumstance of having a  
455 mandrel, this defect is improved and both physical and FE shafts have a uniformed  
456 inner diameter.

457 The maximum and minimum diameters of inner holes are used for quantitative  
458 verification. The minimum inner hole diameter of FCWR without mandrel appears on  
459 the knifing position with a value equal to 17.95 mm of physical shaft and 17.66 mm of  
460 FE result, and its maximum hole diameter is equal to 20.43 mm in physical test and

461 21.26 mm in FE result. The maximum relative deviation (relative to physical result) of  
462 four comparative diameters is 4% which lower than 10%, so the FE results are reliable.

### 463 5.3.2 Advantages and disadvantages

464 Beside the validation experiments, some deformation tests were carried out with  
465 varied values of hole diameters. Simultaneously, the mandrel diameters were changed  
466 accordingly as  $dm/d_0=0.73$ . The other process parameters stayed the same as  $D_0=50$   
467 mm,  $\alpha=45^\circ$ ,  $\beta=2^\circ$ ,  $h=6$  mm,  $B=18$  mm and  $T=1050^\circ\text{C}$ . The rolled shafts are presented  
468 in Fig. 19.



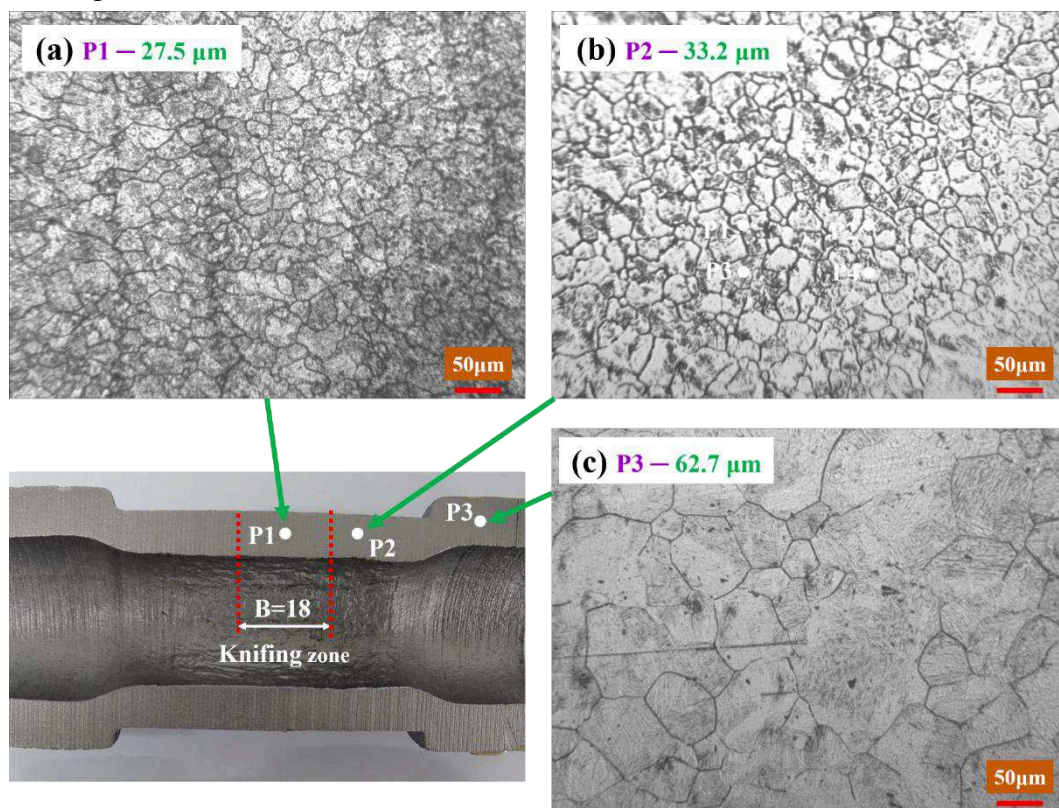
469 **Fig. 19** Hollow shafts formed by FCWR with single guide in the horizontal  
470 multifunctional mill

471 By observing the geometric appearances, we can find that all the rolled pieces are  
472 free from knifing groove and hole expansion. Therefore, a conclusion can be gained  
473 that the new process can absolutely avoid the forming defects of knifing groove and

474 hole expansion.

475 Moreover, these hollow shafts have a good forming accuracy. For example, the  
476 right-angle steps are precisely rolled and the typical limitations are absent, such as  
477 spiral-grooved surface [15, 18], ellipse of formed shafts [19, 20]. These experimental  
478 performances indicate that single guide rolling can improve rolling stability.

479 The grain size of rolled part is one of the most significant indicators, which decides  
480 the mechanical properties of the hollow products. The microstructure morphology of  
481 the rolled shaft is obtained in a microscope with 200 times magnification. As Fig. 20  
482 shows, the grain sizes of the rolled regions (P1, P2) are significantly smaller than that  
483 of unrolled region (P3), which can be explained that the grains are refined under FCWR  
484 deformation. Besides, the grain size at the knifing position (P1) is smaller than that at  
485 the stretching position (P2), which is consistent with the distribution of strain shown in  
486 Fig.18d, and can be considered that the knifing zone has a larger deformation than the  
487 stretching zone.



488 **Fig. 20** Grain size of the FCWR rolled shaft at different locations

489 Although this new process has the above advantages, there are some disadvantages

490 as well. As arisen in the numerical simulations and physical experiments, the rolled  
491 shaft cannot be automatically ejected from the mill so a new discharging device is  
492 needed. Besides, FCWR process deteriorates the ellipse of hole and increases rolling  
493 force and rotating torque.

### 494 **5.3.3 Application to the solid shafts**

495 For solid shafts, the FCWR advantage of avoiding hole expansion is no longer  
496 necessary. However, it also takes advantages of avoiding knifing groove and reducing  
497 the perimeter of rollers.

498 The major considerations for solid shafts rolling are whether billet can rotate  
499 normally and whether central cracks can be avoided. On the one hand, because an BB  
500 section (shown in Fig. 10b) is added at the knifing zone, the friction conditions at  
501 knifing stage are improved theoretically owing to the contacting area increases. On the  
502 other hand, the trend of central cracking is relieved because the added radial  
503 compression-force is beneficial to metal bonding. And when it comes to stretching and  
504 sizing stage, the deformation of NCWR and FCWR is the same. Therefore, it can be  
505 estimated that this novel FCWR process can be used for solid shafts under the condition  
506 of reasonable knifing width.

## 507 **6 Summary and conclusions**

508 In this paper, a novel process of flat-knifing cross-wedge rolling (FCWR) with  
509 single guide was proposed to manufacture hollow shafts, including a CWR roller, single  
510 guide rolling and a horizontal multifunctional mill. The following conclusions are  
511 obtained:

512 (1) The defects of hole expansion and knifing groove are absolutely avoided  
513 because FCWR roller produces a radial force to shrink the hole and avoids the  
514 deformation concentration of outer surface during knifing stage;

515 (2) The new type of horizontal multifunctional mill can be used to perform  
516 laboratory tests such as longitudinal rolling, cross rolling and helical rolling and

517 expected to have industrial application as thread rolling mill, ball rolling mill and cross-  
518 wedge rolling mill;

519 (3) The single guide rolling can be realized by workpiece axis offset from the  
520 center line of two rollers, and can improve the rolling stability and simplify the mill  
521 structure;

522 (4) The flat-knifing roller reduce the wedge length in the range of 200~800 mm;

523 (5) The process of flat-knifing cross-wedge rolling with single guide brings the  
524 shortcomings of non-automatic ejecting, hole ellipse and increase of rolling force  
525 and rotating torque;

526 (6) The process of FCWR with single guide is estimated to form the solid shafts  
527 under the condition that knifing width is designed reasonably.

## 528 **Compliance with Ethical Standards**

### 529 **Acknowledgments**

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### 533 **Conflict of interest statement**

534 We declare that we have no financial and personal relationships with other people  
535 or organizations that can inappropriately influence our work, there is no professional or  
536 other personal interest of any nature or kind in any product, service and/or company  
537 that could be construed as influencing the position presented in, or the review of, the  
538 manuscript entitled.

### 539 **Ethical approval**

540 This article does not contain any studies with human participants or animals  
541 performed by any of the authors.

### 542 **Informed consent**

543 All the authors listed have approved the manuscript that is enclosed.

### 544 **Authors' contributions**

545 Longfei Lin: Software, Validation, Methodology, Writing-Original Draft. Baoyu  
546 Wang: Project administration, Supervision, Funding acquisition. Jinxia Shen:  
547 Methodology, Writing-Reviewing & Editing. Tao Liu: Investigation, Data Curation,  
548 Writing-Reviewing & Editing.

#### 549 **Availability of data and materials**

550 The datasets generated and/or analysed during the current study are available from  
551 the corresponding author on reasonable request.

#### 552 **Consent to participate**

553 Applicable.

#### 554 **Consent to publish**

555 Applicable.

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# Figures

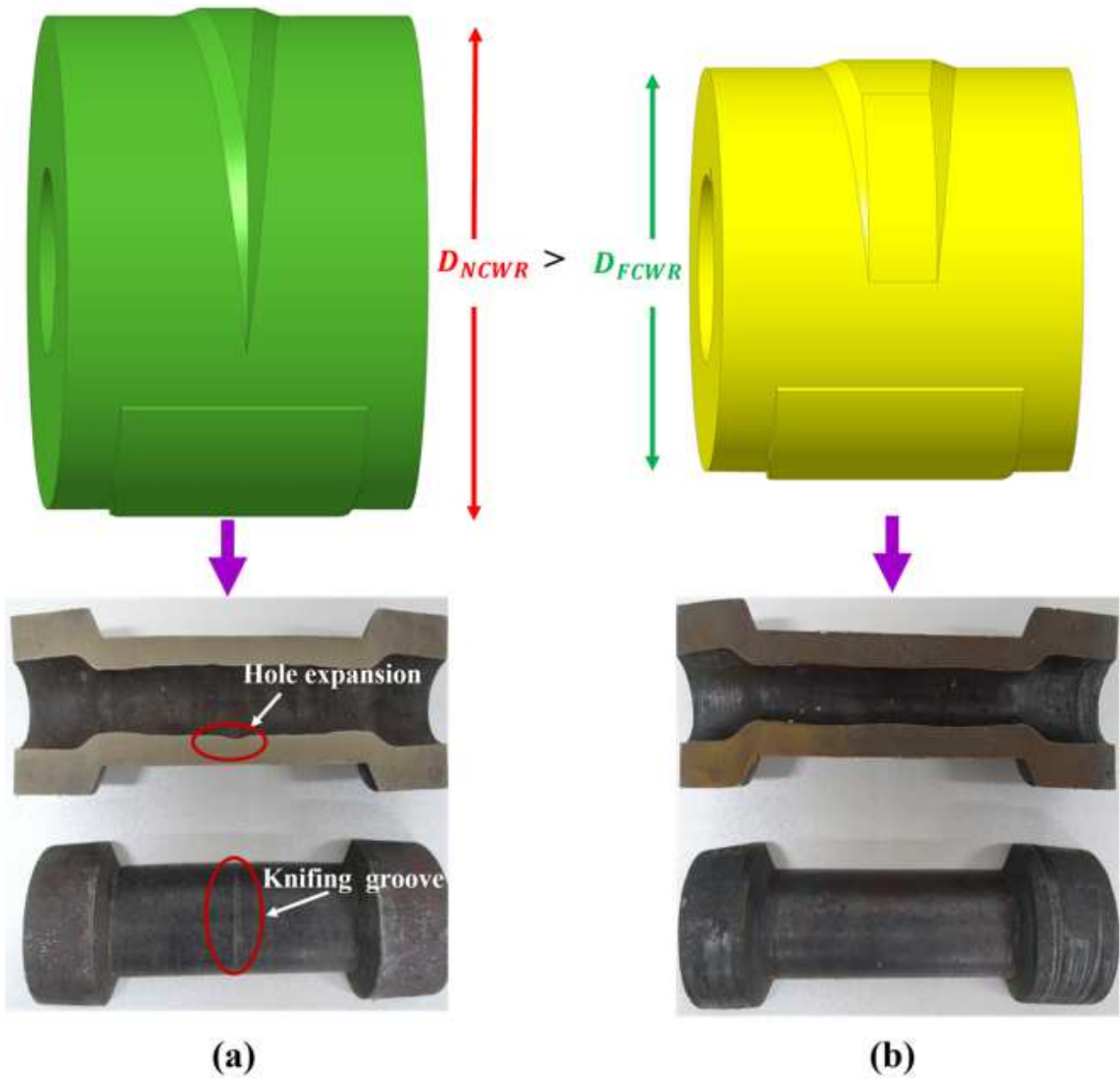
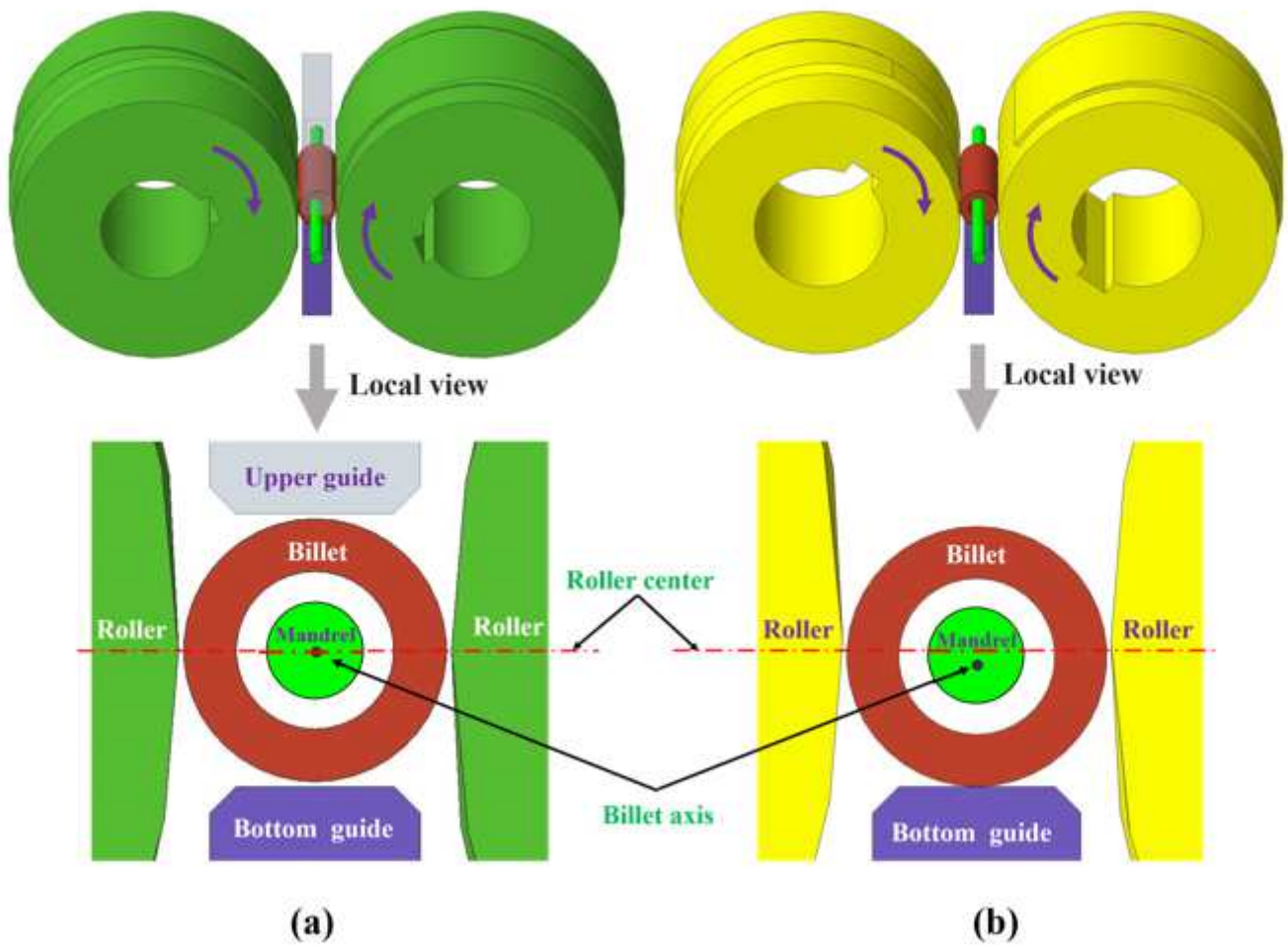


Figure 1

Contrast between two methods for hollow shafts (a) normalized CWR; (b) flat-knifing CWR



**Figure 2**

Process principle: (a) NCWR with two guides; (b) FCWR with single guide

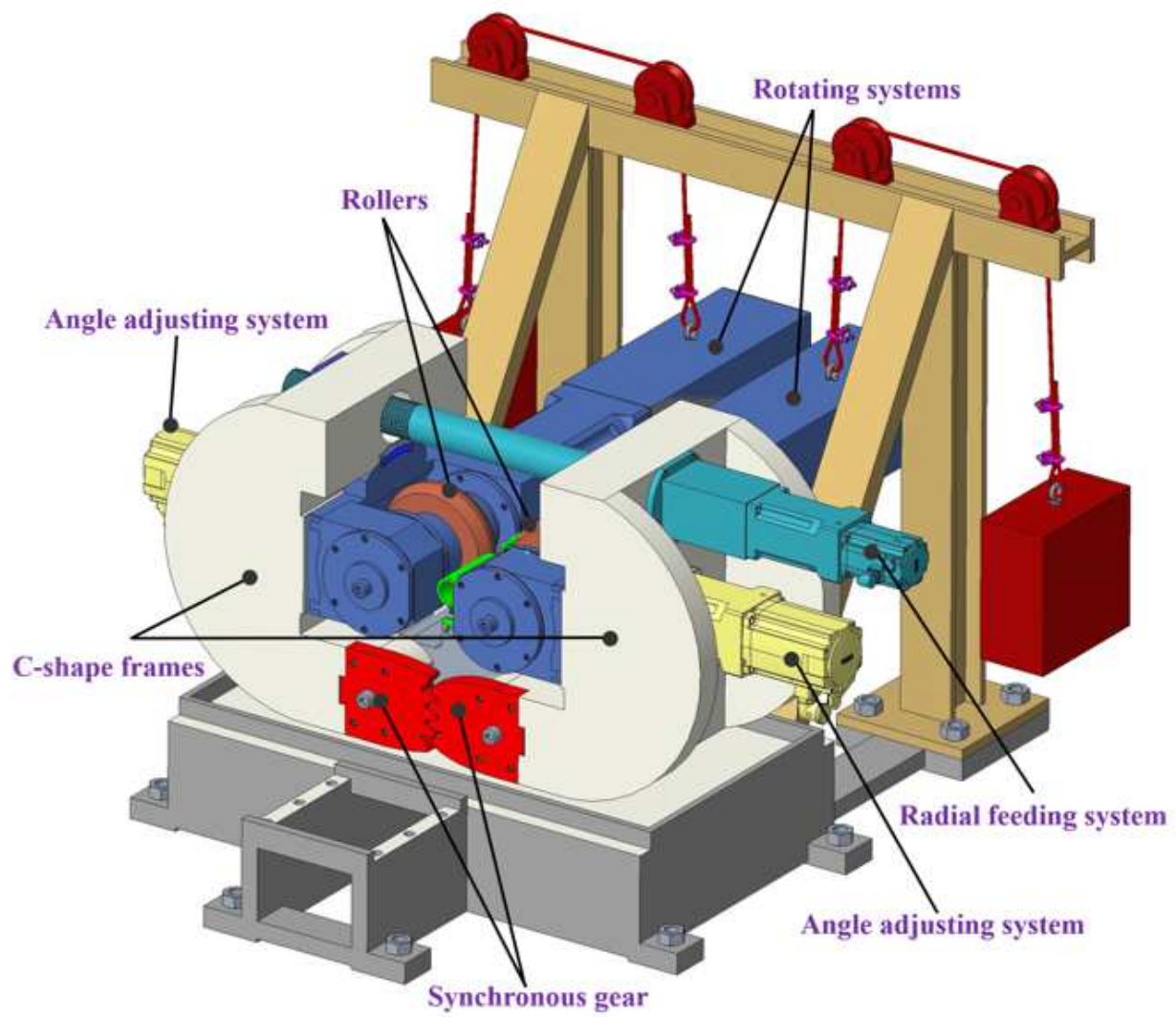
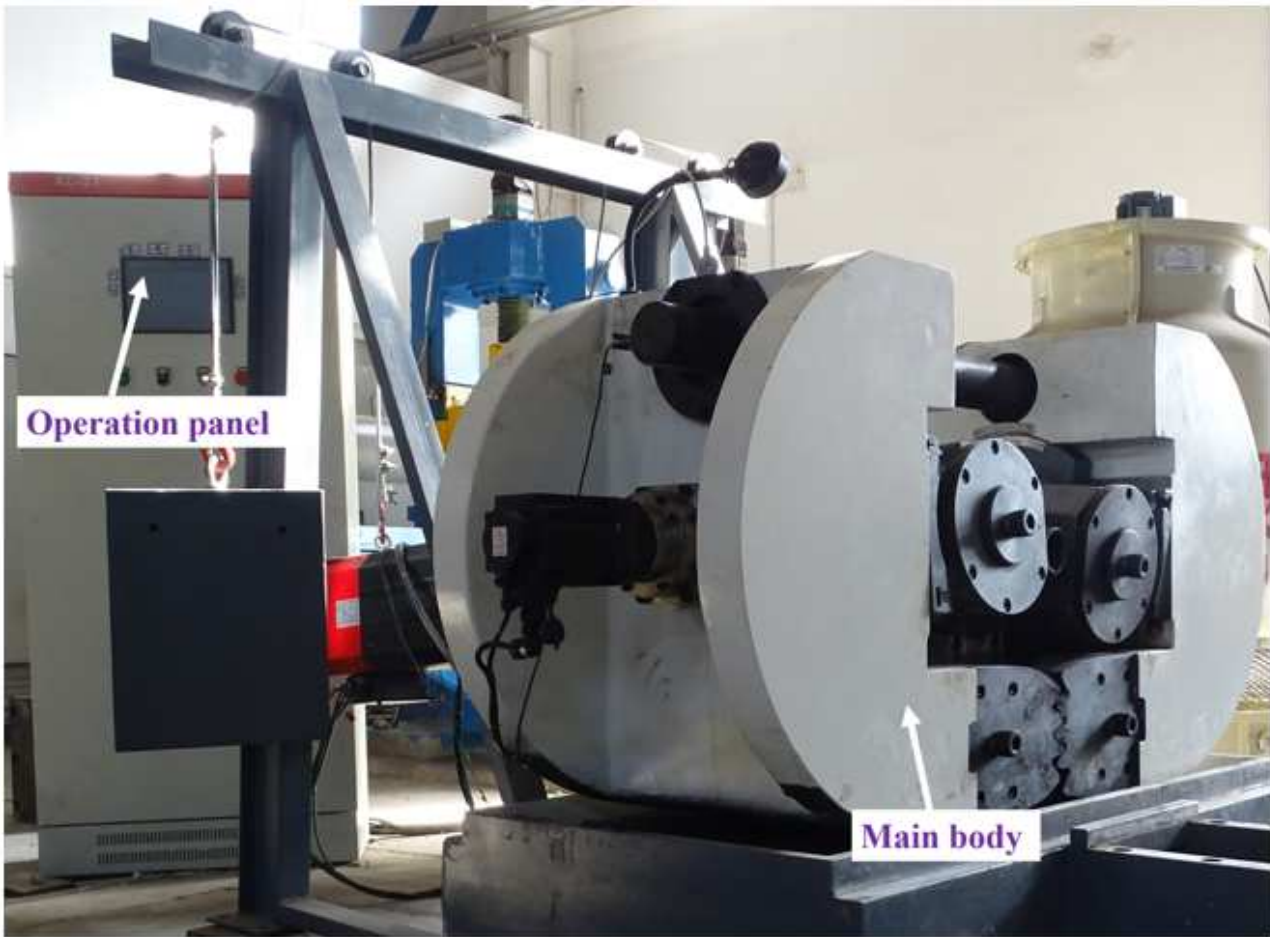


Figure 3

Geometrical model of the horizontal multifunctional mill



**Figure 4**

The constructed horizontal multifunctional mill

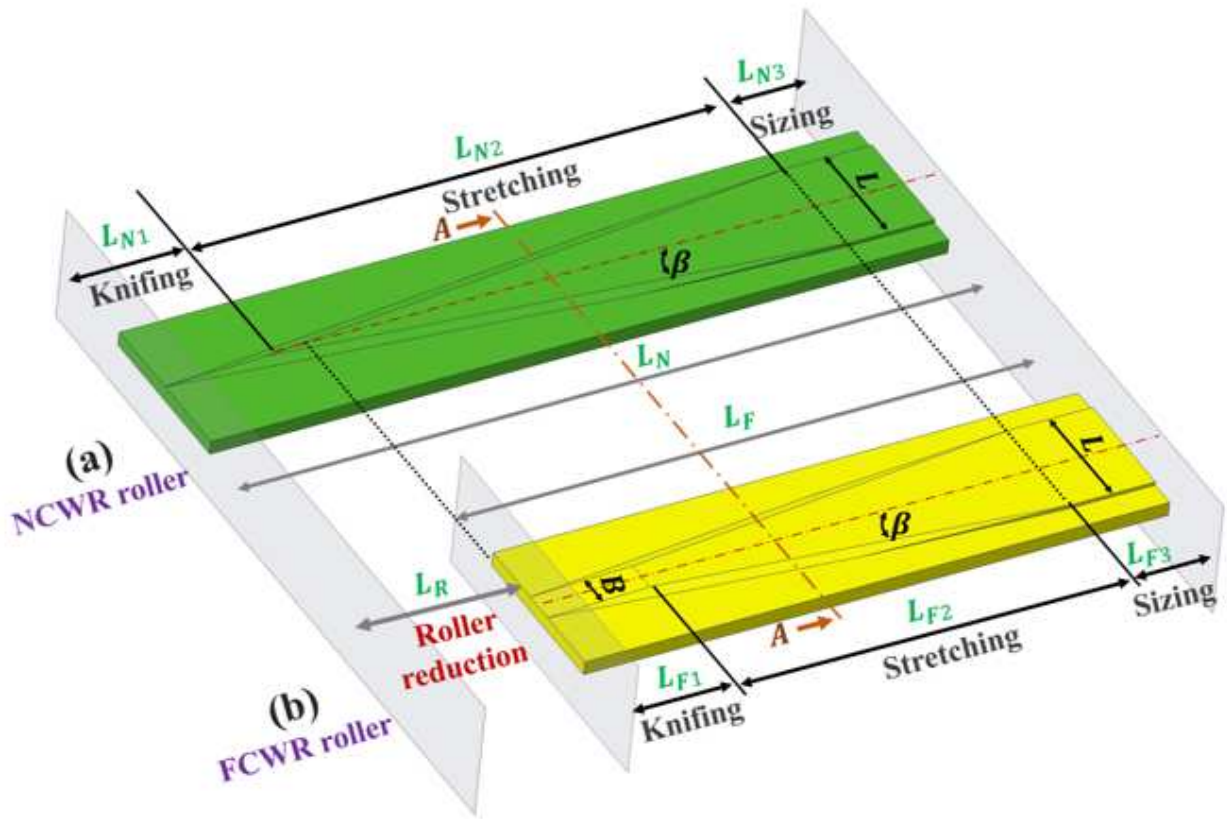


Figure 5

Configuration and major parameters of NCWR and FCWR roller

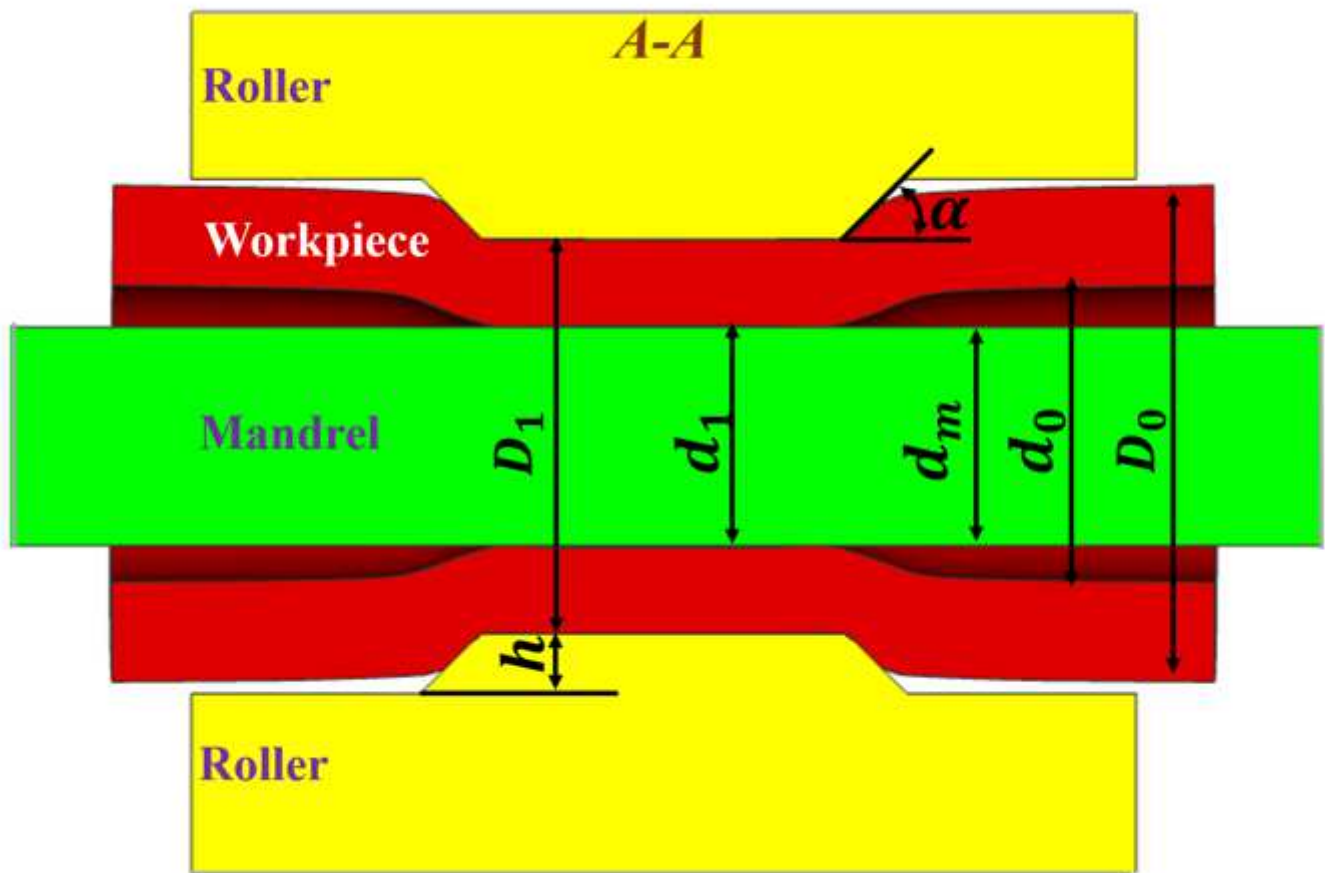
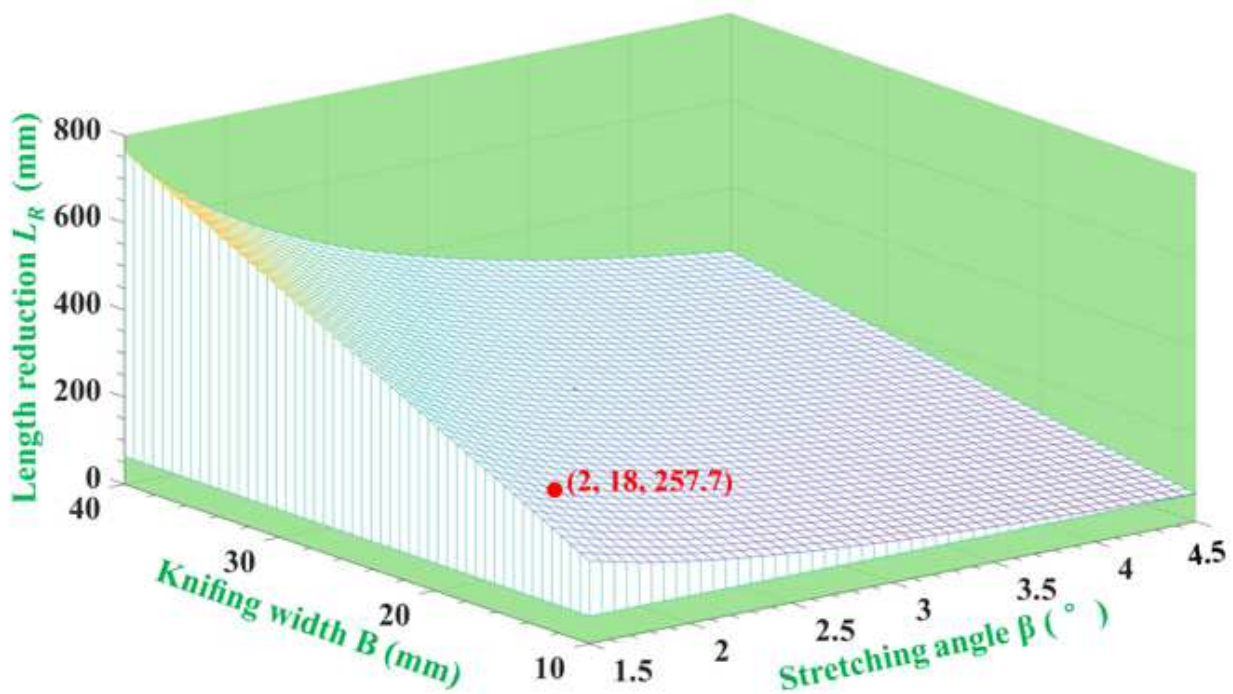


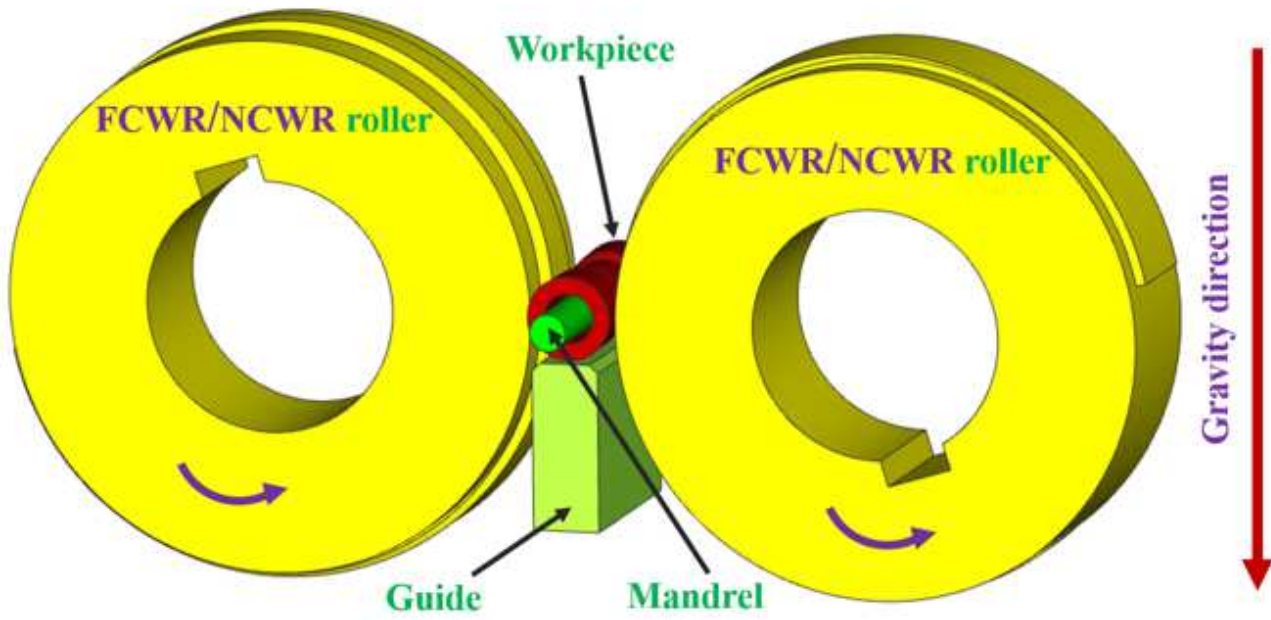
Figure 6

Contact model of roller, mandrel and workpiece at the stretching stage



**Figure 7**

Relationship between wedge-length reduction and process parameters



**Figure 8**

FE projects of FCWR and NCWR with single guide



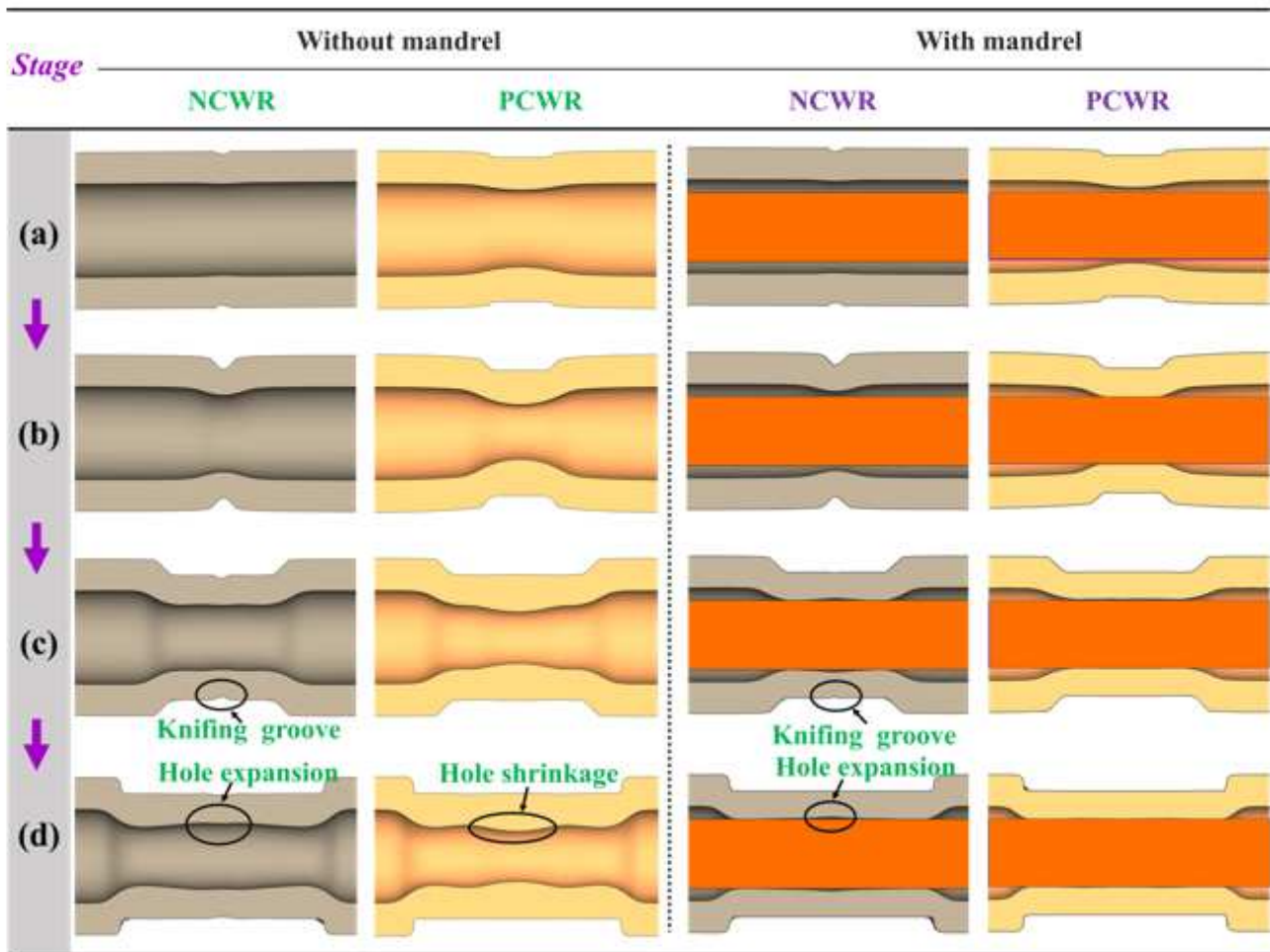


Figure 9

FE results of NCWR and FCWR: (a) middle of knifing stage; (b) end of knifing stage; (c) middle of stretching stage; (d) end of stretching stage

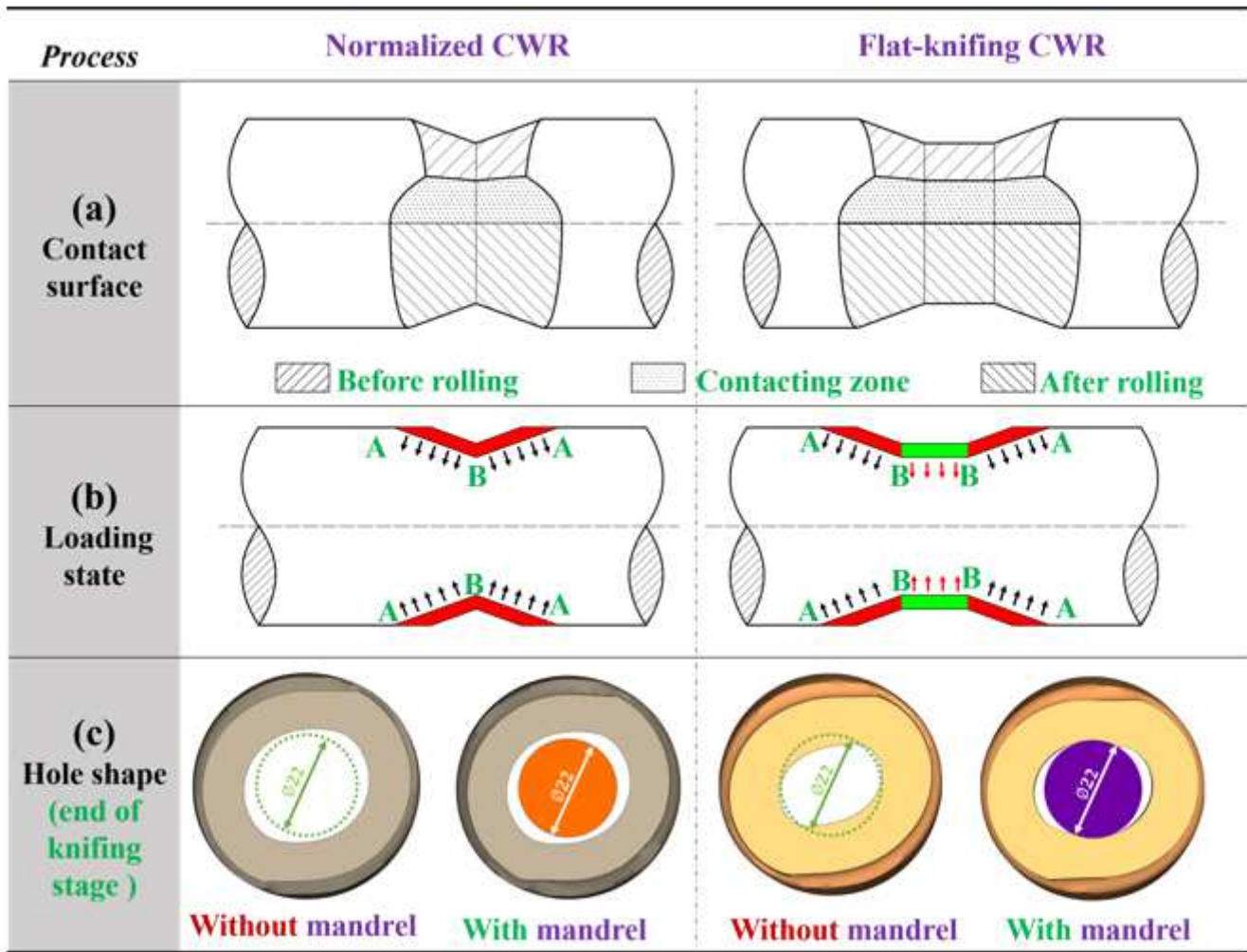


Figure 10

Formation mechanism of hole expansion (end of knifing stage): (a) contact surface; (b) loading states; (c) hole shape

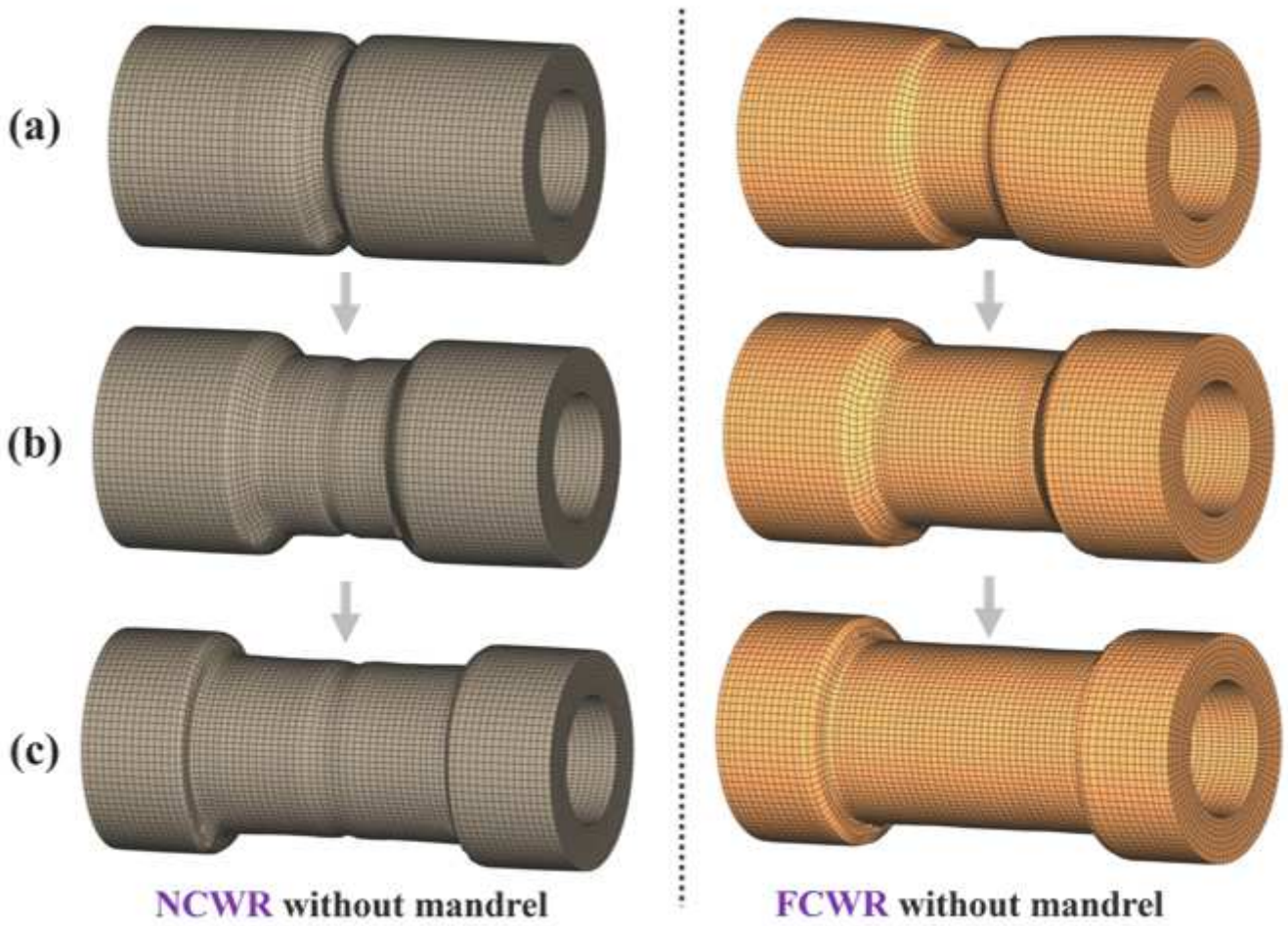


Figure 11

Geometry comparison between NCWR and FCWR workpiece: (a) end of knifing stage; (b) middle of stretching stage; (c) end of stretching stage

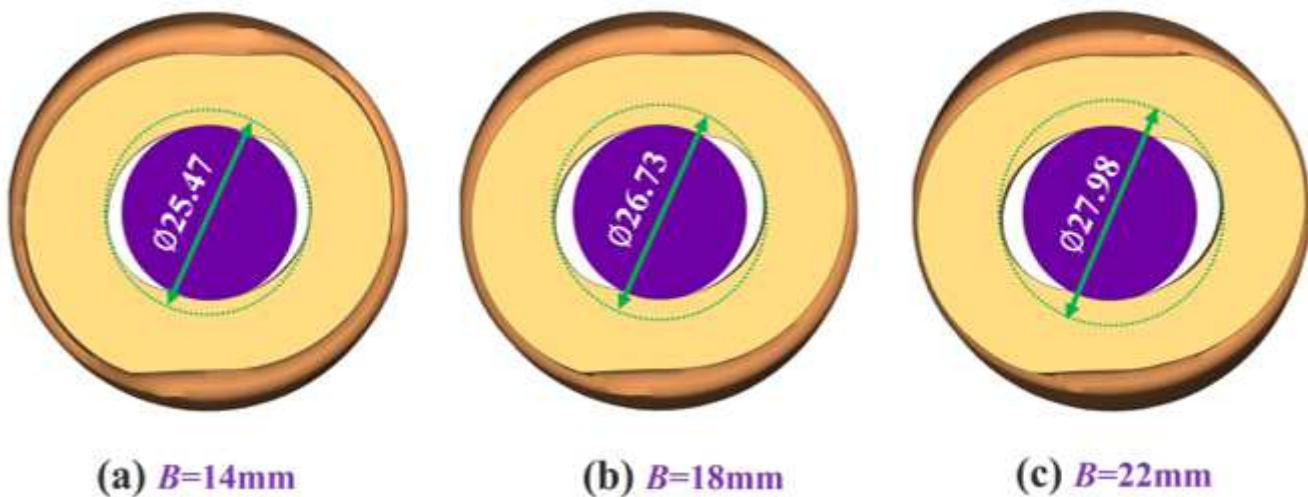


Figure 12

Relationship between knifing width and hole ovality (end of knifing stage)

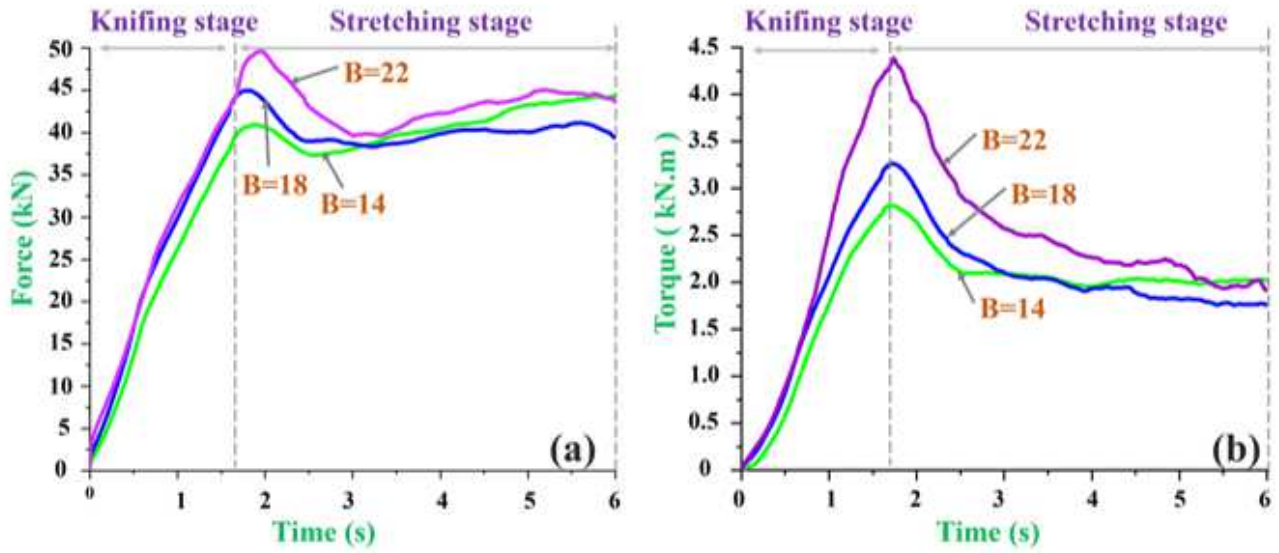


Figure 13

Relationship between knifing width, (a) rolling force, (b) rotating torque

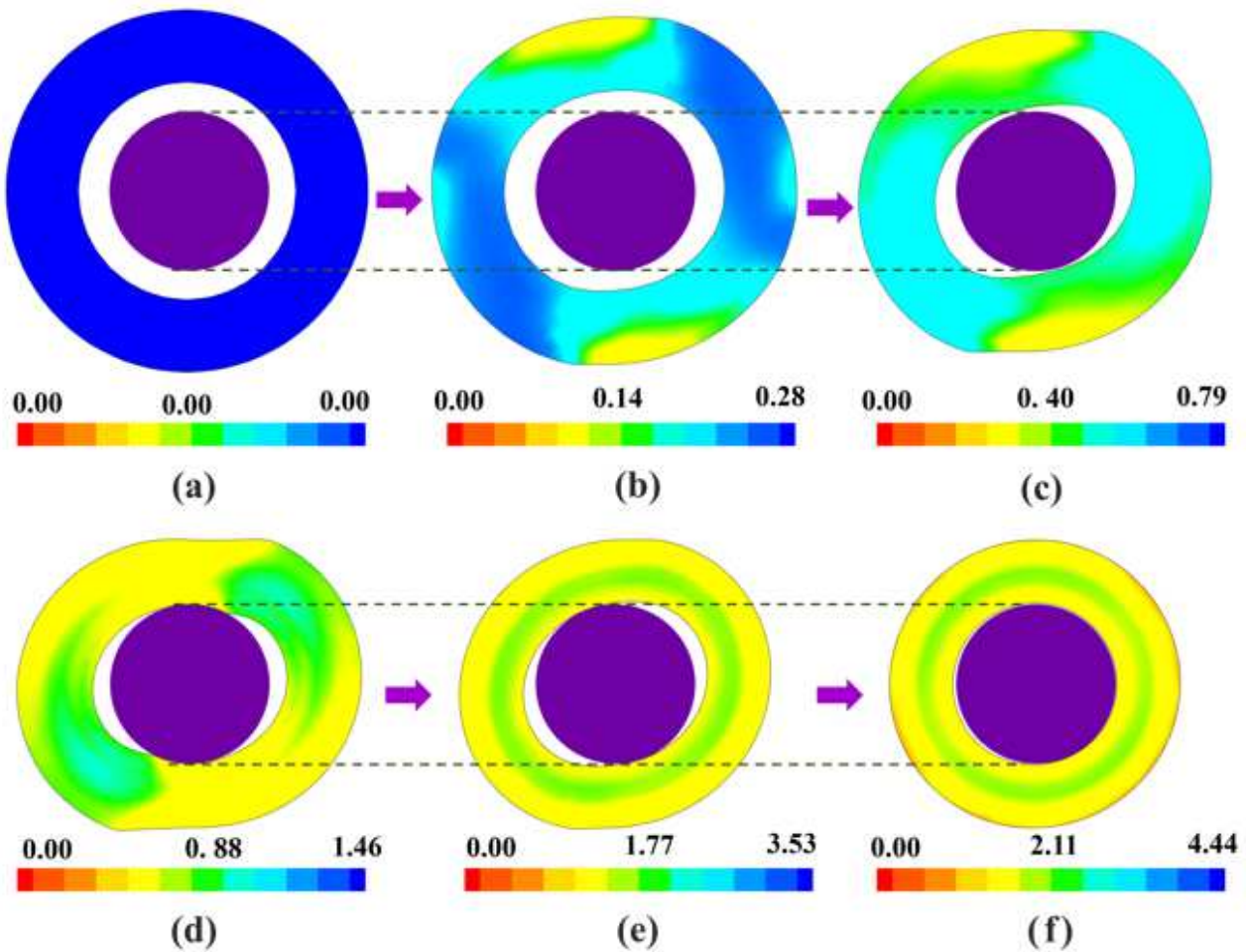


Figure 14

Formation of the FCWR hole (with strain distribution): (a) initial status; (b) begin of workpiece flattening; (c) begin of mandrel contacting; (d) begin of hole sizing; (e) middle of hole sizing; (f) end of hole sizing

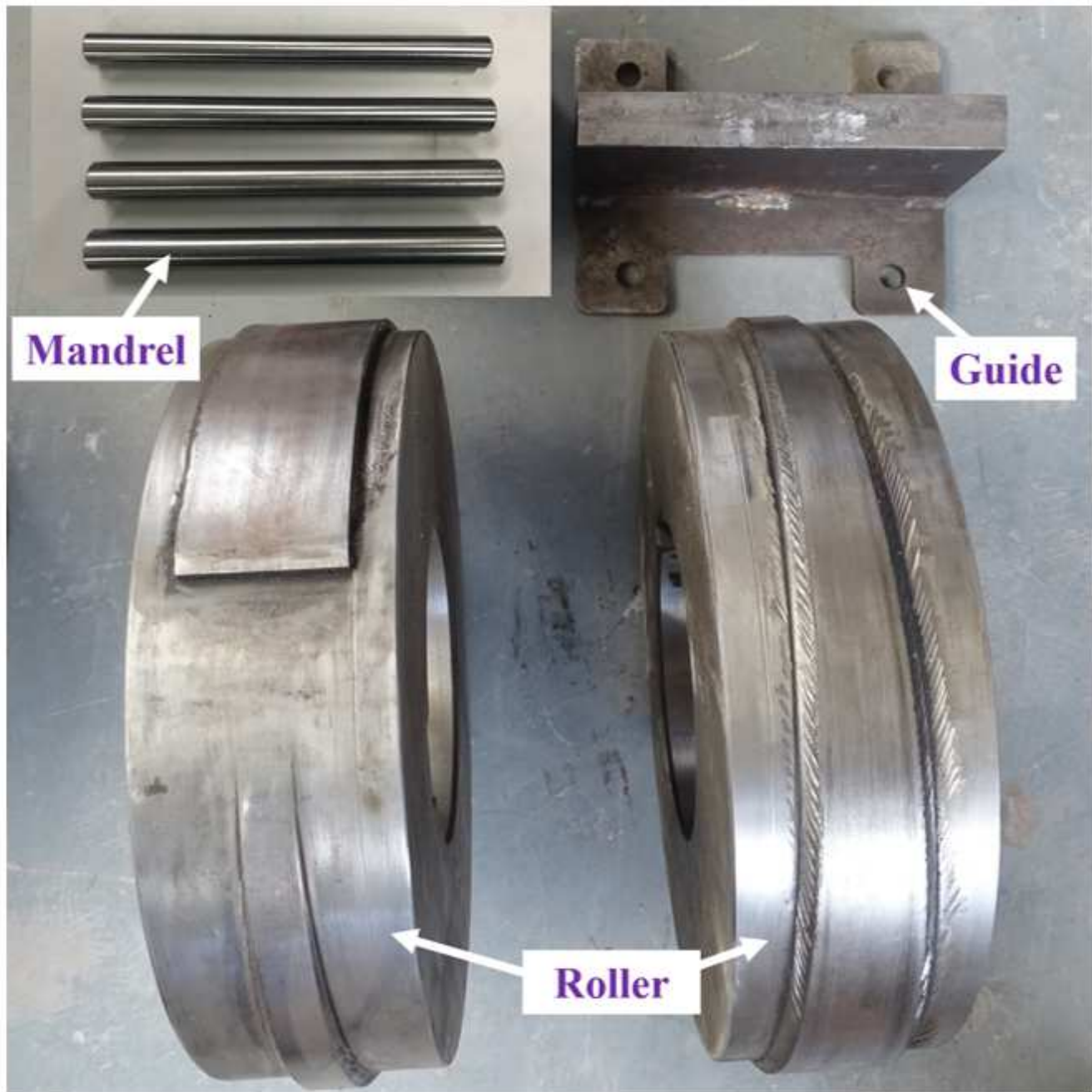
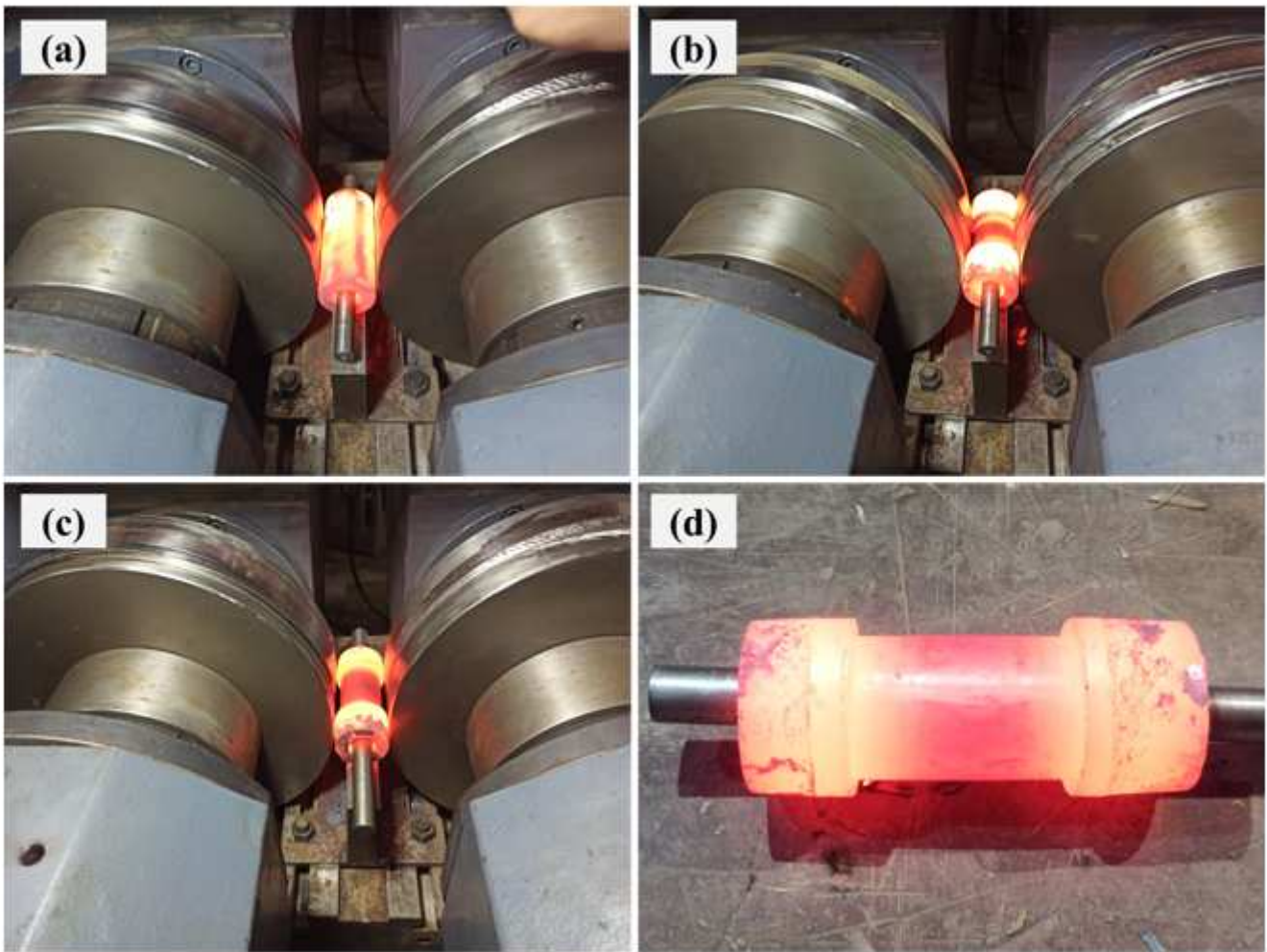


Figure 15

Tools for FCWR experiments with single guide for hollow shafts



**Figure 16**

FCWR rolling experiments in horizontal multifunctional mill with single guide: (a) beginning; (b) rolling stage; (c) ending stage; (d) rolled hollow shaft



Figure 17

The FCWR produced hollow shafts: (a) initial status; (b) after shot peening

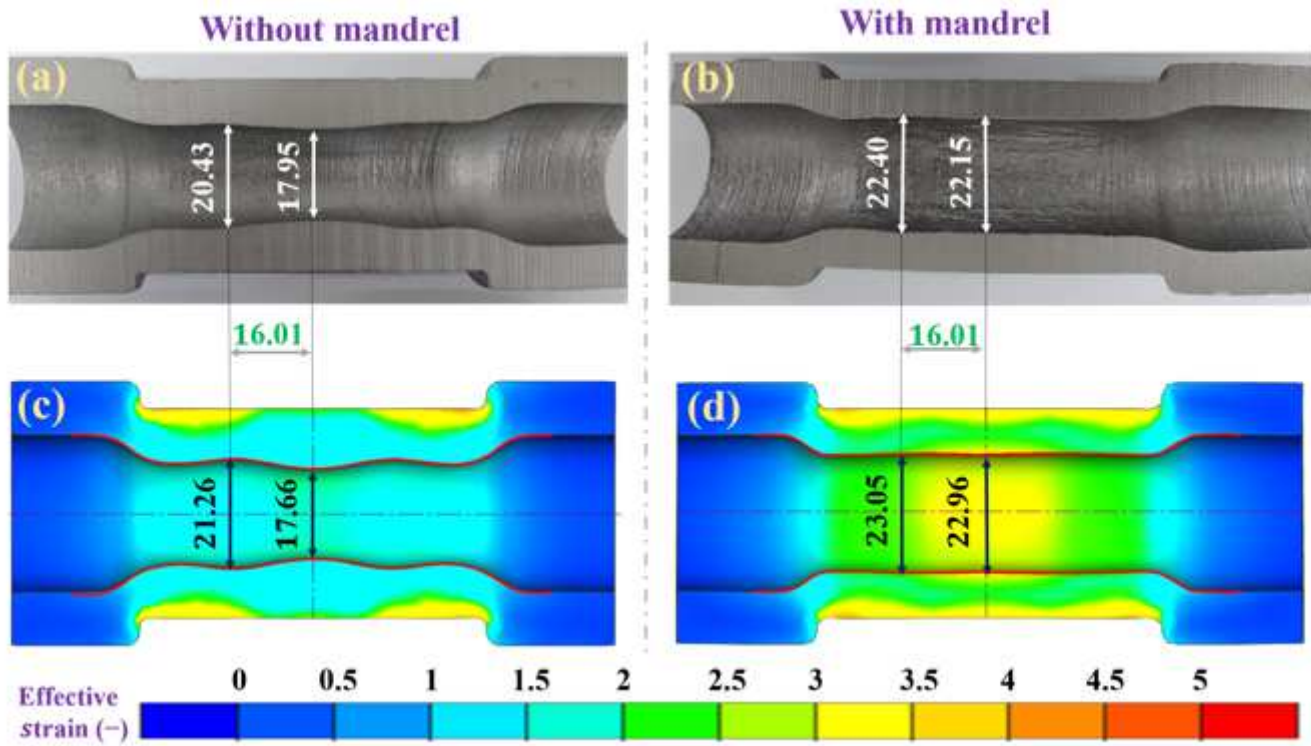


Figure 18

Geometry comparison between (a, b) physical experiments and (c, d) numerical simulations



**(a)**  $d_0=30\text{mm}$



**(b)**  $d_0=28\text{mm}$



**(c)**  $d_0=26\text{mm}$



**(d)**  $d_0=24\text{mm}$

**Figure 19**

Hollow shafts formed by FCWR with single guide in the horizontal multifunctional mill



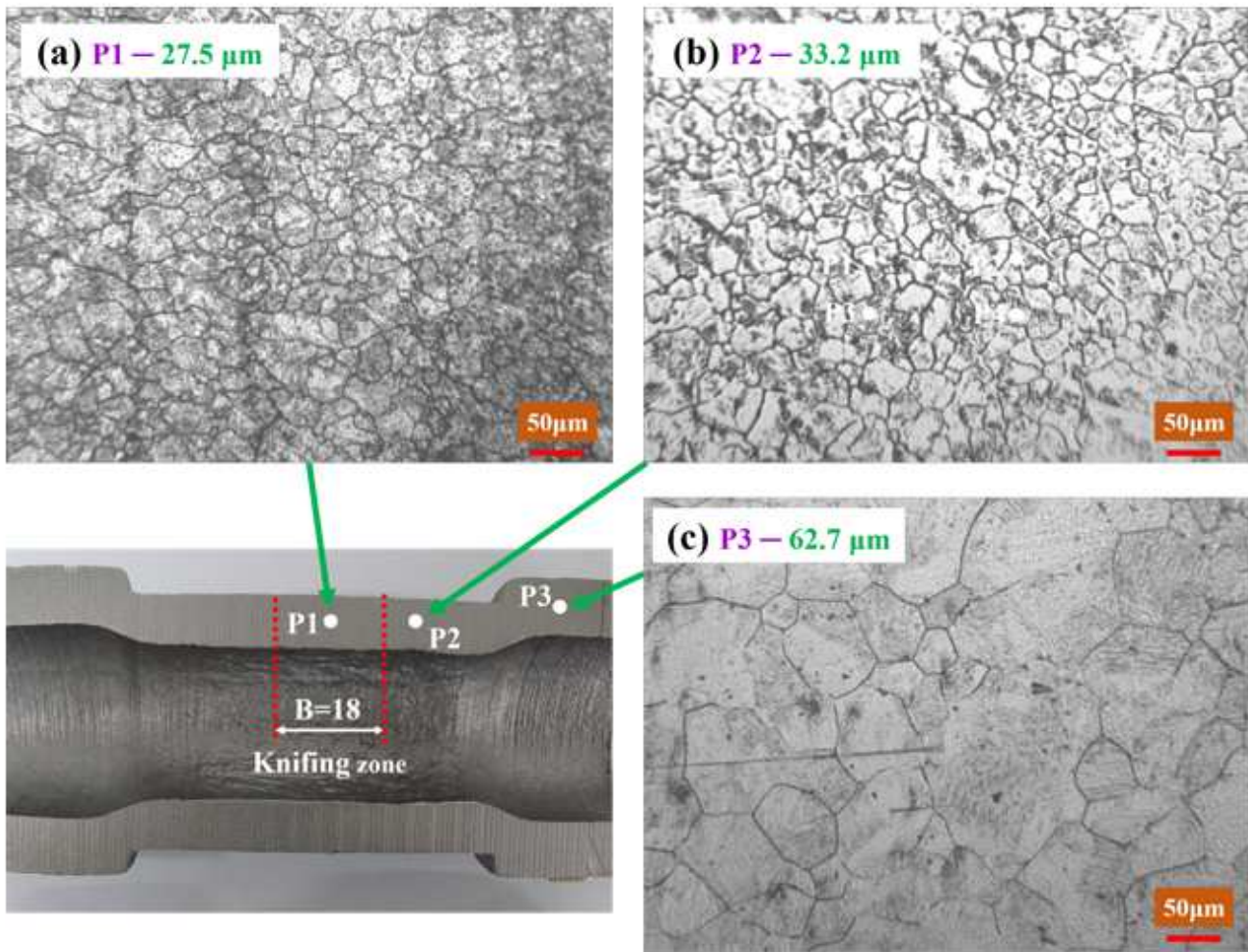


Figure 20

Grain size of the FCWR rolled shaft at different locations