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Magnetization dynamics of nanoscale magnetic materials: A perspective **FREE**

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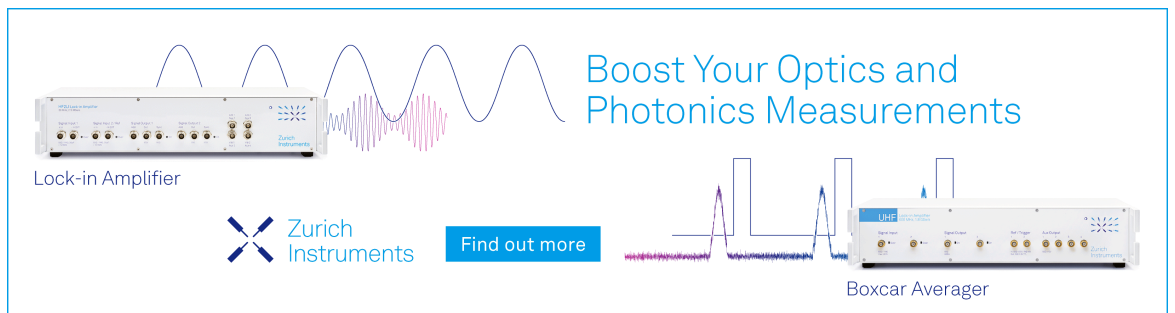


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ABSTRACT

Nanomagnets form the building blocks for a gamut of miniaturized energy-efficient devices including data storage, memory, wave-based computing, sensors, and biomedical devices. They also offer a span of exotic phenomena and stern challenges. The rapid advancements of nanofabrication, characterization, and numerical simulations during the last two decades have made it possible to explore a plethora of science and technology applications related to nanomagnet dynamics. The progress in the magnetization dynamics of single nanomagnets and one- and two-dimensional arrays of nanostructures in the form of nanowires, nanodots, antidots, nanoparticles, binary and bi-component structures, and patterned multilayers have been presented in detail. Progress in unconventional and new structures like artificial spin ice and three-dimensional nanomagnets and spin textures like domain walls, vortex, and skyrmions has been presented. Furthermore, a huge variety of new topics in the magnetization dynamics of magnetic nanostructures are rapidly emerging. A future perspective on the steadily evolving topics like spatiotemporal imaging of fast dynamics of nanostructures, dynamics of spin textures, and artificial spin ice have been discussed. In addition, dynamics of contemporary and newly transpired magnetic architectures such as nanomagnet arrays with complex basis and symmetry, magnonic quasicrystals, fractals, defect structures, and novel three-dimensional structures have been introduced. Effects of various spin-orbit coupling and ensuing spin textures as well as quantum hybrid systems comprising of magnon-photon, magnon-phonon, and magnon-magnon coupling and antiferromagnetic nanostructures have been included. Finally, associated topics like nutation dynamics and nanomagnet antenna are briefly discussed. Despite showing great progress, only a small fraction of nanomagnetism and its ancillary topics have been explored so far and huge efforts are envisaged in this evergrowing research area in the generations to come.

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I. INTRODUCTION

The quest of designing miniaturized and energy-efficient devices has led the scientific community to explore new paradigms of structuring and patterning materials into nanoscale. The journey started in the last century from extensive research work ranging from natural nanocomposites to the patterning of artificial nanostructures.^{1,2} The overriding goal has always been to eradicate the excess energy consumption while enhancing the storage capacity, operating speed, and endurance of a device. For example, as the celebrated Moore's law is ending because of the physical limitations in the pursuit of increasing density of transistors on a chip, it is imperative

to search for suitable alternatives for charge-based semiconductor devices. Magnetic nanostructures have the potential to fulfill such demands. As the device performance relies on the nature of physical processes occurring within the nanomagnetic systems, researchers have invested relentless efforts for understanding these processes over the years. The developments of the state-of-the-art fabrication and characterization techniques have unraveled some exotic dynamical phenomena associated with various length and time scales. The magnetization dynamics refers to the dynamics of the population and phase of spins in an ensemble of interacting spins. Some of the crucial parameters associated with spin dynamics are ultrafast demagnetization time, magnetization quenching, precessional

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frequency, relaxation time, and magnetic damping, which play a pivotal role in determining the efficiency of spin-based devices.^{3,4} All these phenomena can be described in terms of magnetic interactions, namely, spin-orbit interaction, Heisenberg exchange, Dzyaloshinskii–Moriya interaction (DMI), magnetostatic effects, and magnetic anisotropy. The total free energy of a ferromagnetic system in the presence of an external magnetic field can be expressed as a sum of different competing energy terms.⁵ These interactions originated from the “mixture” of atomic and macroscopic physics, which eventually govern the dynamics. The competition between these energies plays a prominent role in configuring magnetization distribution in the nanostructures which are completely different from their bulk counterparts.

Magnetite (Fe_3O_4) nanoparticles (NPs) that are involved in bio-magnetic phenomena and rock magnetism⁶ and other ferromagnetic oxides found in ferrofluids and meteorites exemplify some of the naturally produced magnetic nanostructures. However, current research in nanomagnetism primarily deals with a materials-by-design strategy. A fascinating approach is to develop engineered nanostructures, which are generally not encountered in nature. Engineered nanostructures can be of various types, such as nanodots,⁷ nanoholes or antidots,⁸ nanostripes,⁹ nanowires,¹⁰ nanorings, NPs,¹¹ granular media, nanojunctions, and multilayered nanostructures.¹² In the early days, studies were generally devoted to magnetization dynamics in unpatterned magnetic slabs and multilayers (MLs).^{13,14} The focus gradually shifted to the dynamics in the confined magnetic systems such as single nanostructures and their one-dimensional (1D) arrays. Later, two-dimensional (2D) arrays were started to be fabricated and studied extensively. If an external perturbation is applied to a magnetic system, the exchange energy cost for a single-spin reversal is reduced by spreading the disturbance over long wavelength. This propagation of exchange-coupled spins forms the spin wave (SW). The concept of SW was first introduced by Bloch in 1930.¹⁵ SWs are low lying excited states in magnetic systems. In general, one can expect SWs to exist whenever there is a direction associated with the local order that can vary spatially in a continuous manner at a cost in energy that becomes smaller as the wavelength of the variation becomes longer. The quanta of SW are known as magnons, and the quantization proceeds exactly as for photons and phonons. Recently, “magnonics” has emerged as a sub-branch of “nanomagnetism,” which deals with the generation and manipulation of SWs in a magnetic medium with periodically modulated magnetic properties offering periodic potentials to propagating magnons. Such artificial magnetic structures are termed as magnonic crystals (MCs),^{16,17} which are the magnetic analogs of photonic and phononic crystals. By varying the geometrical parameters artificially, the nature of magnetic interaction and hence the SW dynamics, including the magnonic band structure and bandgap, can be modulated. More recently, hybridization of magnonics with other physical excitations has led to new fields such as “magnon–spintronics,”¹⁸ magphronics, and magnon–polaritronics.

Current research focuses more on the application potential of magnetic nanostructures. Nanostructured MLs with magnetoresistive properties have become the bedrock of magnetic recording technology.^{12,19} Nanomagnets are considered the key elements for the various related applications, such as bit patterned media,²⁰

magnetic logic,²¹ data storage,²² spin-based transistors,²³ reconfigurable waveguide for energy-efficient transmission of signals,²⁴ spin Hall nano-oscillators (SHNO),²⁵ spin-torque nano-oscillator (STNO),²⁶ neuromorphic and quantum computing,²⁷ and biomedical devices. In the nanomagnetism family, MCs have shown superior potential for on-chip microwave communication and processing to the electromagnetic wave-based devices due to their inherent non-reciprocity, energy efficiency, and nanoscale wavelength in the GHz to sub-THz frequency range. A plethora of studies on the quasistatic and dynamic properties of 1D and 2D MCs have been carried out to explore their fundamental SW properties besides their promising applications in SW logic, resonator, filter, phase shifter, splitter, directional coupler, and many other magnonic devices.^{2,17,18,28} Intense efforts have been focused on reprogrammable MCs, whose static and dynamic response can be changed on demand.²⁹ The 1D MCs with a reprogrammable band structure typically have the form of periodic nanowire arrays with complex unit cells where the two subunits switch independently of one another.³⁰ Reprogrammability of magnonic band structure in layered 1D MCs have opened new avenues to the magnetic field-controlled reconfigurable MCs with multimodal frequency transmission characteristics.³¹ The extension toward the third dimension (3D) of magnetic nanostructures may give rise to many complex magnetic configurations with unprecedented properties.³² In spite of such advancements, nanomagnetism still faces many stern challenges. Harnessing the full potential of the magnetic nanostructures needs further experimental and theoretical groundworks in the coming years.

The ultrafast magnetization dynamics of magnetic nanostructures involve complex and nontrivial physics. In this Perspective article, we have deciphered some of these complexities by introducing a clear classification of nanostructured materials in different length scales and associated magnetization dynamics in characteristic time scales. A detailed discussion about the static and dynamic properties of the nanostructures having periodicity in different dimensions is presented based on the available literature. In addition, multilayered nanostructures and their application potentials have been briefly described. We have introduced some of the recent developments in the area of 3D nanostructures. We have also shared our perspective on the emergent phenomena like topological magnetic textures, strong coupling, antiferromagnetic nanomagnets, and ultrahigh resolution spatiotemporal imaging of SWs. We have finally illustrated the scope in these fields with the hope that further research in these directions will help unlock new computational paradigms with magnetic nanostructures.

II. BACKGROUND AND CURRENT STATUS OF THE PROBLEM

Fabrication of the nanostructures with high-quality lateral features, surface, and interface with dimensions down to almost atomic range involves massive effort by the experts in the field of nanoscience and technology. Several electrical, optical, electro-optical, and atomic interaction-based characterization techniques have been developed relentlessly to probe their magnetic properties. One of the major goals to this end has been to achieve unprecedented spatiotemporal resolution. The quantitative and qualitative characterization of

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SW dynamics of the nanostructures can now be easily performed in space, time, frequency, wavevector, and phase domains. Various micromagnetic and atomistic simulators along with theoretical models have been developed to underpin the intriguing physics of magnetic nanostructures. In this section we have articulated an overview of the background and current status of this field.

A. Importance of length and time scales

The spin configurations undergo enormous variation while sculpting down the magnetic material from micro- to nanoscale. The energy landscapes and hence the ensuing static and dynamical properties also modify drastically. For example, micrometer-sized soft-magnetic disks accommodate magnetic vortex state with in-plane spin configuration and an out-of-plane core. When the size is gradually reduced to nanoscale, the system undergoes a phase transition via a quasi-single-domain to a single-domain structure. On the other hand, magnetization dynamics can be classified based on the characteristic time scales as follows: the fastest process is the fundamental exchange interaction occurring within about 10 fs. The spin-orbit coupling (SOC) and related phenomena also occur in the fs time scale. The laser-induced ultrafast demagnetization takes place in sub-hundred-fs to sub-ps range. The fast remagnetization covers the time span of few ps, which is followed by a slow remagnetization, precession, damping, and SW dynamics over few hundreds of ps to few ns time scale. The relatively slower processes are vortex core gyration, core switching (hundreds of ps to several ns), and domain wall (DW) motion (few ns to few μ s). A pictorial description of various phenomena in different time and length scale is presented in Figs. 1(a) and 1(b).

B. Overview of sample fabrication techniques

The state-of-the-art fabrication techniques developed over the last few decades have brought a revolution to the accessible length scale unfurled from micrometer to nanometer. Furthermore, the continuous hunt for miniaturized devices has urged the scientists to push the boundary beyond atomic limits. High-quality samples can be prepared by using both top-down and bottom-up approaches.

1. Top-down approach

The top-down approach relies on lateral patterning of bulk materials by subtractive or additive methods. Some of the lithography methods that follow this approach are photolithography, electron beam lithography, deep ultraviolet lithography, ion-beam lithography, scanning lithography, soft lithography, nanosphere lithography, scanning probe lithography, colloidal lithography, etc.^{35–35} There are several other methods under this category, such as shadow masking, laser or ion-beam irradiation, nanocontact printing, ion implantation, laser machining, deposition, and diffusion. This approach is reliable to fabricate a range of structures, viz., nanodot array, antidot array, nanostripes, quasicrystals, patterned magnetic thin films, and MLs with high repeatability but low yield.

2. Bottom-up approach

The bottom-up approach relies on the chemical synthesis and mesoscopic pattern formation. Thus, NPs, nanowires, and

micro-organisms are the nanostructures that can be synthesized using this approach by using suitable templates, such as track-etched polymers, anodic alumina, and di-block copolymer membranes.^{36,37} Several methods that follow this approach are plasma arcing, chemical vapor deposition, molecular beam epitaxy, sol-gel synthesis, molecular self-assembly, etc. More recently, genetically or mechanically modified magnetosomes from magnetotactic bacteria have been used to grow well controlled structures for biologically encoded magnonics.³⁸ However, it is worth mentioning that a much-improved controllability will be required to make this process competitive for device fabrication.

In the recent past, one of the major hurdles was to fabricate high-quality 3D structures. Two-photon lithography (TPL) combined with the electrodeposition technique,³⁹ laser micromachining, 3D printing, advanced chemical synthesis, etc., have emerged as powerful techniques to cross this hurdle.

C. Characterization of magnetic properties

Magnetic properties of these nanostructures can be characterized by using several techniques that image the spin configurations and measure the quasistatic and fast dynamic magnetic properties besides conventional magnetometry. In addition, there are various numerical tools available to simulate these properties.

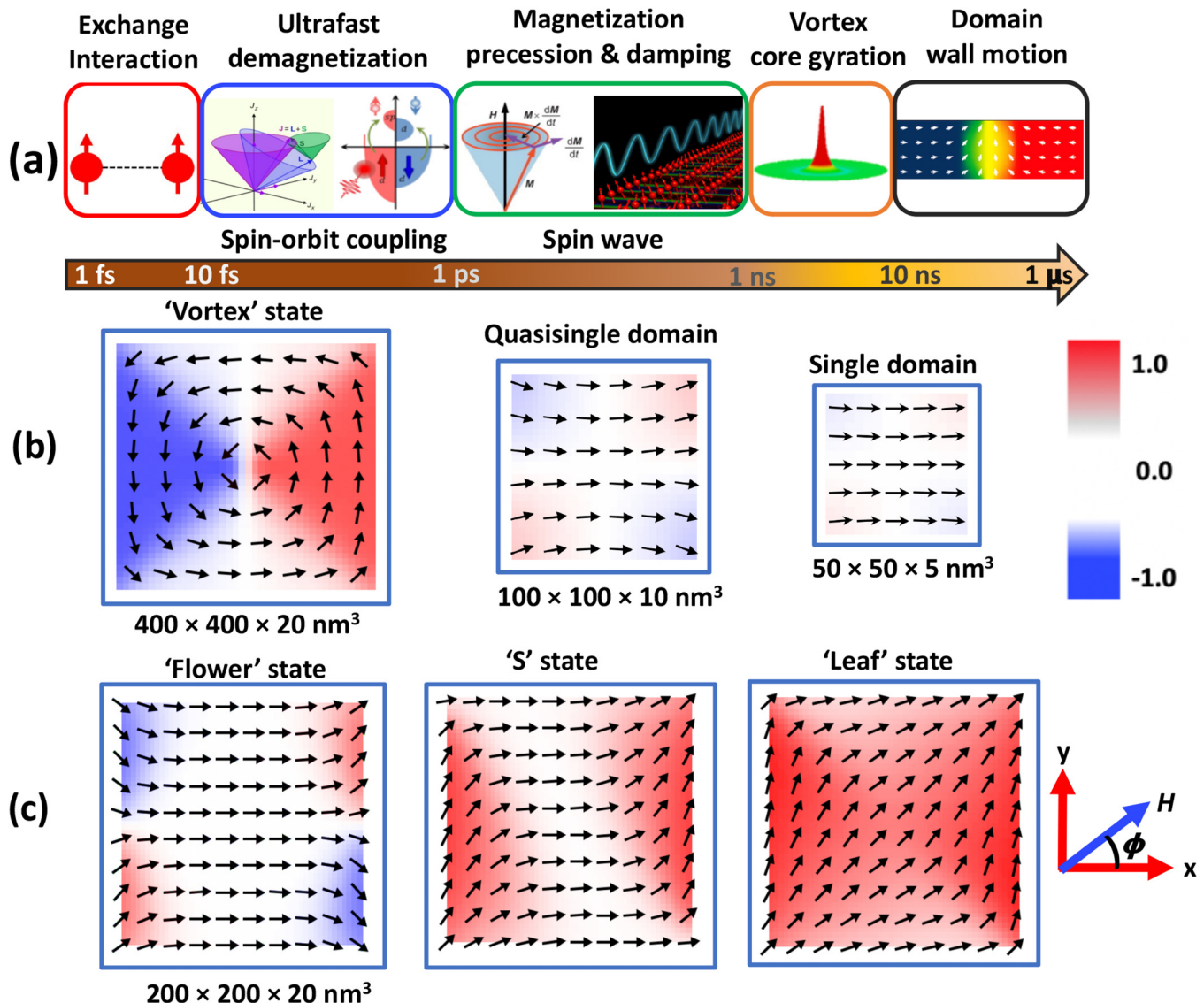
1. Imaging

Intricate properties such as spin textures and stray field distributions in magnetic nanostructures can be probed using magnetic force microscopy (MFM), magneto-optical Kerr effect (MOKE) microscopy,^{40,41} Lorentz transmission electron microscopy (LTEM), etc. Spatial resolution of MFM is bounded by the tip curvature and by optical diffraction limit for MOKE microscopy. Thus, it was necessary to implement high-resolution techniques like LTEM, spin-polarized low-energy electron microscopy (SPLEEM), photoemission electron microscopy (PEEM), spin-polarized scanning tunneling microscopy (SPSTM), scanning electron microscopy with polarization analysis (SEMPA), and ballistic electron magnetic microscopy (BEMM) to successfully image the spin distribution combined with topographical characteristics.⁴² Electron holography technique also provides amplitude and phase information of the magnetic nanostructures with resolution down to 2 nm.

2. Characterization of quasistatic magnetic properties

The static magnetic properties of nanostructures, such as magnetic moment, coercivity, saturation field, remanence, and Curie temperature, can be characterized by using superconducting quantum interference device (SQUID) magnetometry with high sensitivity, whereas vibrating sample magnetometry (VSM) is suitable for characterizing relatively thicker films, bulk materials, and large assembly of magnetic nanoparticles (MNPs). MOKE in different geometries, such as longitudinal, transverse, and polar, is a very useful technique to characterize the quasistatic magnetic properties in a local and noninvasive manner. Several magnetoresistive methods and Hall effects are used to probe anisotropic magnetoresistance (AMR), spin Hall magnetoresistance (SMR), anomalous Hall effect (AHE), etc.

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FIG. 1. (a) Schematic representation of the time scale of magnetization dynamics. Representative spin configurations of nanomagnets with varying (b) size and (c) applied magnetic field orientation, $\phi = 0^\circ, 15^\circ,$ and 45° . The dimensions of the nanomagnets are represented at the bottom of the structures. The structures are not in scale. The corresponding color bar to the magnetization map is shown at the right-hand side of the figure.

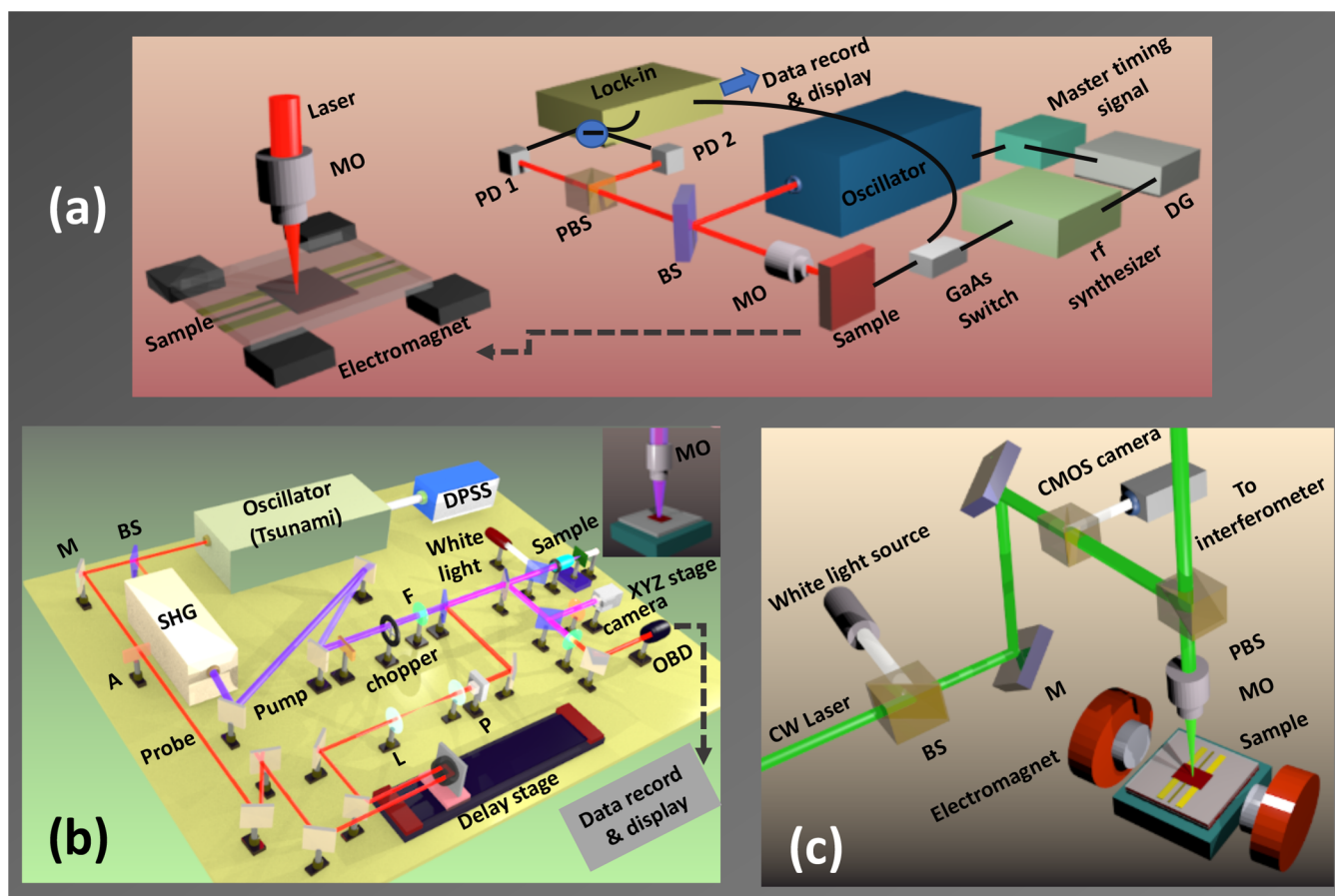
3. Characterization of dynamic magnetic properties

Many state-of-the-art techniques have been developed to excite and probe the magnetization dynamics in magnetic nanostructures occurring over microsecond to femtosecond regimes. Among those, time-resolved MOKE (TRMOKE), ferromagnetic resonance (FMR), and Brillouin light scattering (BLS) are three most well-used techniques to characterize the magnetization dynamics in time, frequency, wave-vector, space, and phase domains.^{4,43} The TRMOKE technique can be categorized into field-pumped and optically pumped approaches. The temporal resolution is determined by either the

field pulse width (in the field-pumped technique) or the optical pulse width (in the optically pumped technique), and together they can resolve ultrafast demagnetization, remagnetization, magnetization precession, damping, SW confinements, nonlinear optical effects, optically induced spin transfer (OISTR), strong coupling effects, as well as carrier and phonon dynamics. This offers a local measurement and can probe the magnetization dynamics by avoiding linewidth broadening due to spatial nonuniformities. Modal composition and damping of individual modes can also be reliably characterized with this technique. Time-resolved scanning Kerr

microscopy (TRSKM)⁴⁴ facilitates the imaging of the temporal evolution of spatial magnetization distribution by fixing the time delay and using scanning MOKE microscopy at various delays. However, the diffraction-limited spatial resolution is only a few hundred nm, which can go down to sub-100 nm by using near-field MOKE.⁴⁵ In the frequency domain, ranging from MHz to tens of GHz, broadband FMR is a very useful technique to globally excite the sample by using absorption from the external source in the frequency spectrum. It has other variants, such as conventional resonant cavity FMR, spatially resolved FMR, and spin-torque FMR (ST-FMR).^{46–48} However, the delicate micro-fabrication of waveguide structures on the sample makes this technique more cumbersome. The BLS technique is primarily advantageous due to its wave-vector sensitivity, which allows the measurement of SW dispersion and magnonic band structure of various MCs.⁴⁹ Magnonic bandgaps (MBGs) and group velocity can also be reliably studied using this technique. Another advantage of BLS is that it is a noninvasive technique where the SW dynamics can be excited using thermal energy at

room temperature, and hence no external excitation source and synchronization of the probe with the external source is required. However, by launching rf current, spin-torque, or other external stimuli at specific resonant frequencies, the SW propagation for that particular frequency can be spatially mapped in the micro-BLS technique. It can also have variants like time-resolved and phase-resolved BLS, making it one of the most versatile techniques for SW measurement. Figure 2 shows schematic diagrams of some of these microscopy techniques. In the spatially resolved FMR setup⁴⁷ [Fig. 2(a)], an optical pulse train, generated from a mode-locked laser, is first synchronized to the reference signal. A sinusoidal high-frequency signal applied from a rf synthesizer is then phase-locked to the reference signal. The excitation frequencies can be in the order of several GHz. The magnetic sample is placed on top of a coplanar transmission line. The drive field applied through this transmission line and the optical pulses interact with the sample stroboscopically. The Kerr rotation of the reflected pulse is detected by using a set of analyzers and photodiodes. The high-frequency signal is chopped by a



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FIG. 2. Schematic diagram of (a) the spatially resolved FMR technique, (b) TRMOKE microscopy, and (c) BLS microscopy. The notations for the components are given as follows: BS = beam splitter; PBS = polarized beam splitter; M = mirror; A = attenuator; L = lens; OBD = optical bridge detector; F = filter; P = polarizer; PD = photodiode; DG = delay generator; MO = microscope objective; SHG = second harmonic generator; DPSS = diode-pumped solid state laser.

photoconductive switch and the frequency is fed to a lock-in amplifier as a reference signal during the phase-sensitive detection. The process is repeated for a series of scan points, while scanning over the sample, which allows the spatial distribution of the magnetic response to be mapped.

A schematic of the TRMOKE microscope based on two-color optical pump-probe technique is presented in Fig. 2(b). Here, the second harmonic of a femtosecond laser pulse is used to excite (pump) the dynamics while the fundamental laser is used as a probe to detect the time-resolved polar Kerr rotation (or ellipticity) from the sample. A delay stage introduces spatial delay between the pump and probe pulses, which provides the necessary temporal delay during the time-resolved measurement. Both the beams are incident collinearly on the sample, which are tightly focused by a microscope objective with the diffraction-limited spot size in sub-micrometer range. The sample position is controlled by a high precision piezoelectric scanning stage during the spatiotemporal scanning. The pump beam is modulated and the change of polarization and intensity in the reflected probe beam is detected by using a balanced photodiode detector and lock-in amplifiers in a phase-sensitive manner.⁴ Figure 2(c) shows the schematic of a micro-BLS setup where a single mode laser is collimated and broadened before entering into a microscope objective with high magnification and long working distance. The range of angle of incidence and hence the transformed wave vector depends on the numerical aperture. The scattered beam is collected by the same objective in backscattered geometry and sent to the tandem Fabry-Pérot interferometer for frequency analysis. The sample is mounted on a set of high precision translation stages. In order to increase the density of measured magnons, electrical excitation with a rf source is launched using a coplanar waveguide to the sample.

All these benchtop techniques are extremely sensitive and require extreme care and regular maintenance. Apart from these popular tools, a pulse inductive microwave magnetometer (PIMM) is an oscilloscope-based time domain detection tool to measure the dynamics with tens of ps resolution. Another recently evolved imaging technique is magnetic resonance force microscopy (MRFM), which bridges the gap between magnetic resonance imaging (MRI) and scanning probe microscopy (SPM). Attosecond spectroscopy, higher-harmonic generation, neutron scattering, and x-ray microscopy based on x-ray magnetic circular- and linear-dichroism (XMCD and XMLD) processes are high-end facilities that can probe the static and dynamic magnetic responses from ferromagnetic, ferrimagnetic, and antiferromagnetic thin films and nanostructures.

4. Theoretical and numerical methods

The equation of motion of magnetization in the presence of an external magnetic field can be written as

$$\frac{d\mathbf{M}}{dt} = -\gamma(\mathbf{M} \times \mathbf{H}). \quad (1)$$

The above equation is called the Landau-Lifshitz equation (without damping), where $\gamma = \frac{g\mu_B}{\hbar}$ is the gyromagnetic ratio and g is the Lande g -factor.

The above equation can be generalized by replacing \mathbf{H} by the effective magnetic field \mathbf{H}_{eff} . This equation implies that the tip of the magnetization vector precesses around the effective magnetic field in a circular orbit for an infinitely long time with an angular frequency $\omega = \gamma H_{eff}$. Practically, the precession amplitude decreases with time and the tip of the magnetization vector follows a spiral path. Therefore, a damping or relaxation term (R) should be added with the Landau-Lifshitz equation,⁵⁰

$$\frac{d\mathbf{M}}{dt} = -\gamma(\mathbf{M} \times \mathbf{H}_{eff}) + R(\mathbf{M}, \mathbf{H}_{eff}). \quad (2)$$

Landau-Lifshitz suggested the following:⁵¹

$$R = -\frac{\lambda}{M_S^2} \mathbf{M} \times (\mathbf{M} \times \mathbf{H}_{eff}). \quad (3)$$

Subsequently, Gilbert suggested the following:^{52,53}

$$R = \frac{\alpha}{M_S} \left(\mathbf{M} \times \frac{d\mathbf{M}}{dt} \right). \quad (4)$$

Consequently, the equation of motion of magnetization vector in the presence of damping can be expressed as

$$\frac{d\mathbf{M}}{dt} = -\gamma(\mathbf{M} \times \mathbf{H}_{eff}) + \frac{\alpha}{M_S} \left(\mathbf{M} \times \frac{d\mathbf{M}}{dt} \right). \quad (5)$$

Equation (5) is known as the Landau-Lifshitz-Gilbert (LLG) equation. Here, α is the Gilbert damping parameter. The value of α is much less than 1 for transition metals, which ensures that the magnetization precesses a number of times around the effective field before coming to the equilibrium position.

The equation of motion and Maxwell equation can be solved considering the electrodynamic boundary conditions. The exchange boundary condition such as Rado and Weeterman can be derived from the equation of motion of magnetization,

$$\frac{1}{\gamma} \frac{\partial \mathbf{M}}{\partial t} + \mathbf{M} \times \mathbf{H}_{eff} + q\mathbf{M} \times \nabla^2 \mathbf{M} + \mathbf{M} \times \mathbf{H}_s = 0, \quad (6)$$

where $q\nabla^2 \mathbf{M}$ is the nonuniform part of the exchange effective field and \mathbf{H}_s is the effective field of the surface anisotropy, which exists in thin boundary layers. In the case of small oscillations, substituting $\mathbf{M} = \mathbf{M}_0 + m \exp(i\omega t)$ and assuming \mathbf{M}_0 as constant, the exchange boundary conditions for complex amplitude m can be written in the form as proposed by Soohoo,⁵⁴

$$\frac{\partial m_x}{\partial n} + \varepsilon m_x \cos 2\theta = 0 \quad \frac{\partial m_y}{\partial n} + \varepsilon m_y \cos^2 \theta = 0, \quad (7)$$

where $\varepsilon = \frac{2K_s}{qM_0^2}$, K_s is the surface anisotropy constant, θ is the angle between \mathbf{M}_0 and the normal to the boundary surface. Here, ε characterizes the degree of pinning of magnetic moments or the pinning

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parameter. In the absence of pinning ($\varepsilon = 0$), Eq. (7) becomes

$$\frac{\partial m}{\partial n} = 0. \quad (8)$$

Kalinikos and Slavin⁵⁵ developed the SW dispersion relation in ferromagnetic films considering both the dipole–dipole and the exchange interactions and by using the classical perturbation theory. Considering the general case of mixed exchange boundary conditions, they obtained a set of dispersion relations. In the case when both components of the magnetization vector are pinned uniformly but still different on the different sides of the film, the dispersion is similar to the form of the well known dispersion equation for SW in the unlimited media.⁵⁶

The lateral confinement also influences the SW excitations in confined magnetic elements. The nonuniform internal magnetic field further complicates the SW mode profiles in such structures. The theory of SW in ferromagnetic slabs¹³ and disks⁵⁷ were developed in the 1960s. Bryant *et al.* showed that the problem of an infinite magnetic strip can be reduced to a 1D eigenvalue problem, which can be solved numerically. Furthermore, the effects of the nonuniform demagnetization field on the spatial patterns and frequencies of the modes were also revealed.⁵⁸ Fletcher and Kittel developed the dispersion relation, magnetization distribution, and group velocity of magnetostatic waves in an infinite circular cylinder with a bias magnetic field parallel to the cylinder axis.⁵⁹ The quantized SW modes in a thin axially magnetized magnetic element were described more precisely by introducing effective “pinning” boundary conditions of a purely dipolar nature.⁶⁰ In confined 2D elements, the complexity of boundary conditions and non-uniform demagnetization fields pose difficulty in deriving exact analytical forms for the dispersion relations, making way to the numerical methods to solve such complex problems.

Micromagnetic and atomistic simulations, alongside the density functional theory and Monte Carlo methods, have played pivotal roles in predicting a wide variety of magnetic phenomena in confined magnetic systems over the years. A series of micromagnetic simulators has been developed, which are extremely useful to simulate the magnetization dynamics covering a broad time scale. Object oriented micromagnetic framework (OOMMF) (<https://math.nist.gov/oommf/>), LLG Micromagnetic Simulator (<http://llgmicro.home.mindspring.com/>), MicroMagus (<https://lapth.cnrs.fr/micromegas/>), Magpar (<http://www.magpar.net/>), Nmag (<http://nmag.soton.ac.uk/nmag/>), Mumax³ (<https://mumax.github.io/>), MagOasis (<http://magnetism.eu/43-software.htm>), Magnum (<http://micromagnetics.org/magnum.fe>), Fidimag (<https://computationalmodelling.github.io/fidimag/>), Boris (<https://www.boris-spintronics.uk/>), etc., are all popular softwares that are based on the finite difference or finite element method. Atomistic simulators such as Vampire (<https://vampire.york.ac.uk/>), UppASD (<https://www.physics.uu.se/forskning/materialteori/pagaende-forskning/uppasd/>), Spirit (<https://spirit-code.github.io/>), and Fidimag have been developed to simulate magnetic materials with atomic resolution from Angstroms to several micrometers. Micromagnetic simulations cannot precisely capture the microscopic origin of complex physical effects such as exchange bias, spin–orbit effects, spin transport, heat assisted magnetic effects, and ultrafast demagnetization. Atomistic simulations can

bridge the gap between electronic structure and micromagnetic method by treating the material at its natural atomic length scale. Numerous theoretical models and packages are available to reliably calculate the electronic band structures and electronic properties of magnetic materials. To this end, plane wave method (PWM) based numerical calculations have become popular for calculating magnonic band structures in 1D, 2D, and 3D MCs.

D. Intrinsic dynamics of isolated nanomagnet

With spatial confinement, domain formation should be completely suppressed at the nanoscale according to Brown’s fundamental theorem. An individual nanomagnet should thus behave as a giant spin comprising of numerous isotropic spins compactly residing together. However, a non-ellipsoidal nanomagnet exhibits anisotropy arising from its geometric configuration other than magnetocrystalline and magnetostrictive anisotropies. Cowburn *et al.* in 1998 reported a strong configurational anisotropy in a single square-shaped supermalloy nanomagnet having sub-micrometer size by using the MOKE technique.⁶¹ The presence of shape-dependent fourfold and weak eightfold anisotropy were evidenced. Additionally, the spin configuration can vary with relative orientation between the applied magnetic field and the anisotropy field,⁶² which is shown for a square-shaped nanomagnet in Fig. 1(c). Confinement from micrometer through sub-micrometer to nanometer scale imposes several phase transitions. In 1999, another work by Cowburn *et al.* showed that the magnetization reversal behavior changes from a squeezed hysteresis loop to a square loop. This indicates the presence of two different phases in circular nanomagnets: vortex and single-domain states⁶³ according to their aspect ratio (thickness/radius). Figure 3 represents a simulated phase diagram for circular-shaped Permalloy (Ni₈₀Fe₂₀, Py hereafter) dot, revealing in-plane, vortex, and out-of-plane magnetic microstates depending upon the disk radius and thickness.

In 2004, Demidov *et al.* performed a pioneering experiment with a square-shaped individual Py magnet with sub-micrometer size fabricated on top of a CoFe microstructure separated by a copper spacer.⁶⁴ They demonstrated this individual magnet with typical memory-element like geometry as a genuine source of microwave radiation. The micro-focused BLS measurement showed radiation of SWs into the surrounding magnetic film occurring at discrete frequencies corresponding to the frequencies of quantized modes of the element at around 10–12 GHz. It is pertinent to mention here that very rapidly, the researchers realized the importance of high aspect ratio nanomagnets to be embedded in the microwave devices and the focus immediately shifted to nanoscale elements. However, the confined magnetic elements show various localized, extended, and standing SW modes, which need to be understood before their possible applications. Exemplary simulation results of SW spectra and the corresponding SW mode profiles of circular- and square-shaped nanodots and circular-shaped antidots made of 20 nm-thick Py are presented in Fig. 4. The lateral dimensions (given in the caption of Fig. 4) are chosen in such a way that they can accommodate different types of modes as described below. For the square and circular-shaped nanodots, the lowest frequency mode (M1) is localized in the edge demagnetized regions, known as the edge mode or the end mode (EM). The mode with the highest

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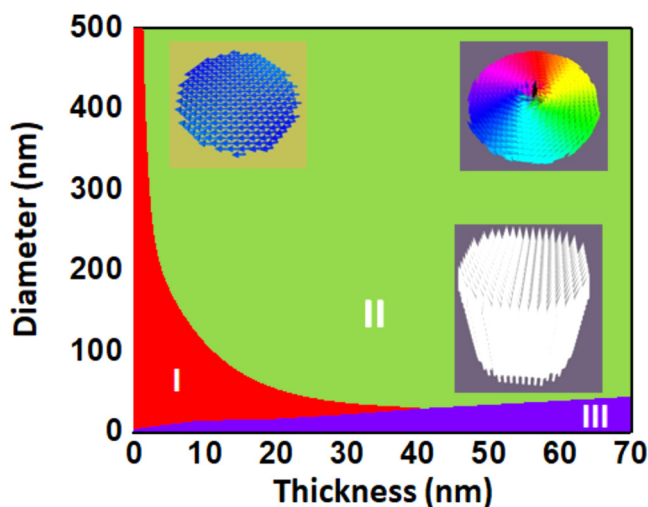


FIG. 3. The simulated phase diagram of a single Py nanodot. The roman numbers mark the regions separated by the solid lines corresponding to different ground states of the dot formed at different combinations of thicknesses and diameters: regions I, II, and III correspond to the state with uniform in-plane magnetization, vortex state, and uniform out-of-plane magnetization. Representative simulated images of the ground states are shown inside the figure.

power in the FFT spectra in both cases (M2) has its power distributed over an extended region around the center of the element, popularly known as the center mode (CM). The square element shows a low-power mode (M3) that shows a standing SW character with nodal planes perpendicular to the bias magnetic field, i.e., in the backward volume (BV) geometry. In the antidots, the lowest frequency mode (M1) is an EM, while M2 and M3 are two extended modes in the Damon–Eshbach (DE) geometry, i.e., SW is extended perpendicular to the bias magnetic field. M4 is again a standing SW mode in the BV geometry. The magnetic field dispersion of SW frequencies obtained from BLS measurements supported by micromagnetic analysis also revealed that a nanomagnet can accommodate these stable CM, EM, and confined standing SW modes of DE, BV, and hybrid nature.⁶⁵

The ambition of probing the temporal variation of magnetization in single nanomagnets well below the diffraction limit led to the development of the cavity-enhanced MOKE (CEMOKE) technique.⁶⁶ In 2006, Barman *et al.* reported the ps dynamics of Ni nanomagnets with different sizes by exploiting this highly sensitive CEMOKE technique.⁶⁷ A significant speed up in the magnetization dynamics from sub-GHz to GHz frequency range was observed as the cylindrical magnet enters from the multidomain to single-domain state. Also, with the decrease in the diameter of these cylindrical nanomagnets, the damping of the coherent precessional mode decreased sharply to finally settle down to its intrinsic value

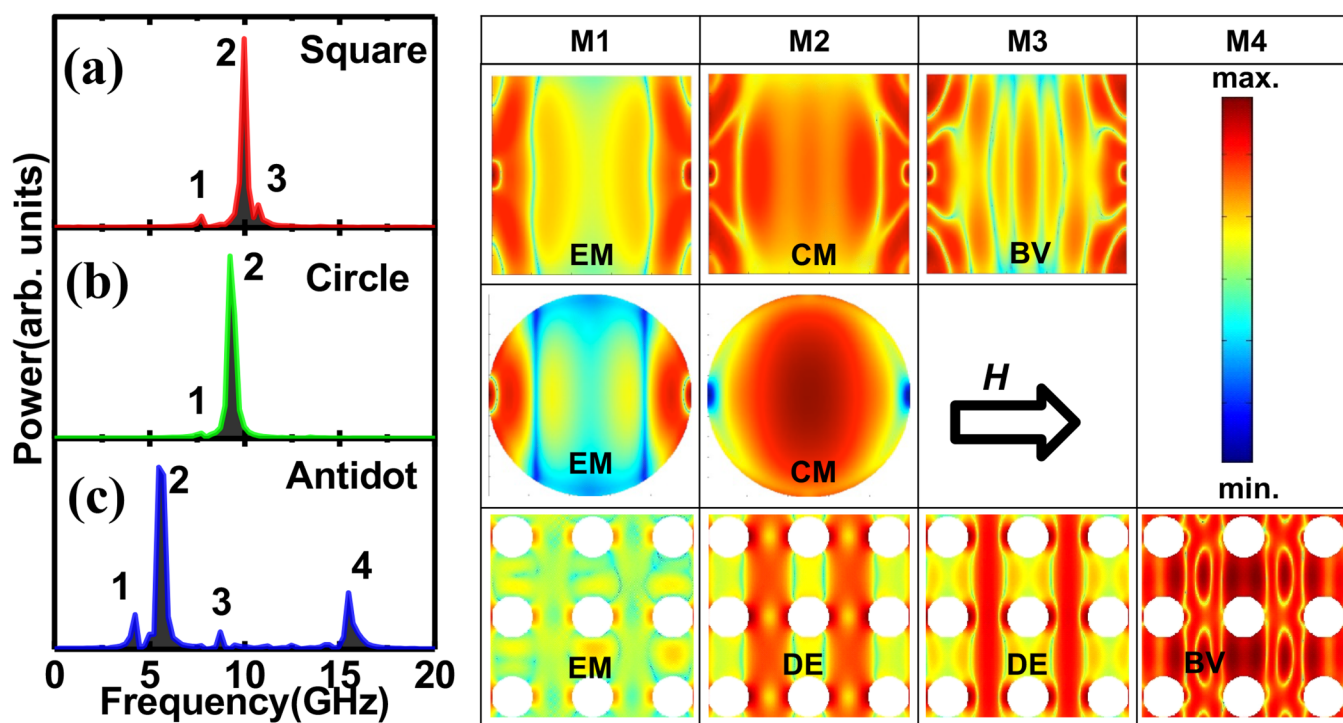


FIG. 4. Simulated power spectra of (a) a single square nanodot of width 500 nm, (b) a single circular nanodot of diameter 500 nm, and (c) an array of circular antidot with hole diameter 100 nm and lattice constant 200 nm. The mode numbers are indicated in numerical figures within the figure. Power profiles are shown in the right-side table. Edge mode (EM), center mode (CM), standing wave mode in backward volume (BV) geometry, and extended mode in Damon–Eshbach (DE) geometry are observed. Simulation parameters: saturation magnetization, $M_s = 860$ emu/cc; anisotropy constant, $K = 0$; exchange constant, $A_{ex} = 13 \times 10^{-12}$ J/m; damping coefficient, $\alpha = 0.008$.

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in the single-domain regime. The bias field-dependent precessional frequency confirmed an extrinsic contribution to damping in micrometer-sized magnets. There a lower-frequency EM got overlapped with the fundamental mode with decreasing field, causing significant dephasing.⁶⁸ However, such an extrinsic contribution was not observed for the nanomagnets leading toward field-independent damping. During the same time, Laraoui *et al.* reported the ultrafast demagnetization, precession,⁶⁹ and relaxation⁷⁰ of CoPt₃ sub-micrometer-sized single dots using an all-optical TRMOKE system having femtosecond temporal resolution and high spatial resolution (~300 nm) obtained with a reflective confocal Kerr microscope. In particular, the fast relaxation time of a few ps, where electrons and spins exchange energy with the lattice, and the slow relaxation time of hundreds of ps, where electrons and the lattice exchange energy with the environment, were reported from single nanomagnets. In 2008, Liu *et al.* measured the time-resolved magnetization dynamics of individual Py disks of 160 nm diameter using time-resolved Kerr microscopy. By sweeping the bias magnetic field, the internal spin configuration underwent transition between the vortex and quasi-single-domain states, leading to distinct hysteresis behavior of fundamental mode frequency as a function of the in-plane bias field. The critical fields for triggering the vortex annihilation and nucleation processes have been determined in this study.⁷¹ The year 2011 witnessed some very important developments in single nanomagnet dynamics. Rana *et al.* measured the time-resolved precessional dynamics of isolated 50-nm-wide Py dots showing a dominant EM without having any trace of CM.⁷² They also observed quadrupolar interaction between the nanodots with increased areal density and a dynamic dephasing for the enhancement of damping in agreement with previous theoretical work from the same group.⁷³ On the other hand, Liu *et al.* detected high-frequency dynamics of a single 150 nm wide nanomagnet from a lower-frequency background of 500 nm wide nanomagnets by placing them in the same array. They claimed that the optical diffraction limit could be beaten since the characteristic behavior of the studied nanomagnet is sufficiently different from its neighbors.⁷⁴ Naletov *et al.* used MRFM to study the radial and azimuthal eigenmodes in a Py/Cu/Py spin-valve-like nanopillar by applying a spatially uniform rf field or rf current flowing through the nanopillar. They found a selection rule for exciting different modes by adjusting the excitation geometry.⁷⁵ Keatley *et al.* demonstrated controlled suppression of EM in an individual nanomagnet by excitation of larger amplitude coherent precession of CM. This is necessary for nanoscale spin transfer torque (STT) oscillators and bi-stable switching devices where more uniform spin dynamics are desirable.⁷⁶

The focus steadily shifted toward the use of unconventional external stimuli for exciting single nanomagnet dynamics. It has been known that nanomagnets driven by spin-polarized current can exhibit high-frequency magnetization dynamics and can act as a microwave resonator.⁷⁷ Furthermore, the antidamping torque from pure spin current can set the magnetization precession to auto-oscillation by suppressing its intrinsic damping. Investigation showed that spin-orbit torque (SOT) generated from an adjacent heavy metal layer to a ferromagnet can switch the nanomagnet in a deterministic way, which can be used to construct a field free clocking and nanomagnetic logic analogous to the current CMOS

technology.²⁵ All-optical helicity dependent switching in a single nanomagnet revealed intriguing physics that can lead to direct and fast data writing. To this end, the observation of smaller nanoelements settling to their final magnetization states faster (~2 ps) after switching than larger elements ushers new hope.⁷⁸ The faster switching speed is attributed to the electron–lattice and spin–lattice interactions with higher spin temperatures for smaller nanoelements.⁷⁹ Strong coupling of magnon with photon, phonon, or other magnon can lead to hybrid systems for quantum transduction. To this end, direct observation of strongly coupled magnon–phonon dynamics via the orientation of the applied magnetic field was an important development.⁸⁰ Besides, strain-induced switching has found to establish a successful Boolean operation in the recent past.⁸¹ Recently, hybrid magnetodynamical modes have been observed in single quasi-elliptical magnetostrictive Co nanomagnet deposited on a Pb(Mg_{1/3}Nb_{2/3})O₃–PbTiO₃ (PMN-PT) substrate using the TRMOKE microscope (see Fig. 5).⁸² The intense electric field of a pump laser-induced periodic strain in the substrate and generated surface acoustic waves (SAWs), giving rise to an oscillation in the nanomagnet's magnetization via the Villari effect. Hybrid modes, viz., mixed mode with azimuthal quantization at higher frequency and tilted EM in the lower frequencies, were generated due to the dynamical mixing of the periodic strain-induced magnetization oscillation and laser-induced precessional motion. This could enable the development of strain actuated magnetoelastic nano-oscillator and magnonic logic circuits.

E. Dynamics of 1D arrays of magnetic nanostructures

The research work carried out on 1D arrays of magnetic nanostructures can be broadly classified into three categories: (a) realization of magnonic waveguides (MAW) for SW propagation, (b) development of 1D MCs formed of arrays of nanostripes, and (c) investigation of SW dynamics in 1D nanostripes/nanowires. These structures are important candidates for racetrack memory, interconnects, MAW, and nanochannels.^{83,84}

In the first category, SW propagation has been investigated along the length of the magnonic waveguide in the DE geometry. Due to the strong demagnetizing fields near the edges, the internal field in the stripe varies significantly across its width. Thus, close to the edges of the waveguide reduction of internal field creates SW wells, which, in turn, influence the SW propagation. Experimental investigations have demonstrated that one can efficiently channel, split, and manipulate propagating SWs in microscopic magnetic film waveguides.⁸⁵ 1D MAWs have been realized in the form of nanostripes with periodic modulation of geometric (e.g., thickness or width of nanowires) or magnetic (such as the magnetic anisotropy, saturation magnetization, strength, and orientation of magnetic field) parameters,⁸⁶ which are important components of integrated magnonic nanocircuits. A key requirement of magnonic nanocircuit is to have SWs turning a sharp bend or a corner without significant dissipation, which was successfully demonstrated in a “S” shaped bend in a Py waveguide.⁸⁷ Numerical simulations have shown the opening of MBG by introducing a row of antidots in a MAW,⁸⁸ which makes these patterned MAWs a promising candidate for magnonic nanocircuits with integrated filters. Efficient engineering of the magnonic band structure has also been

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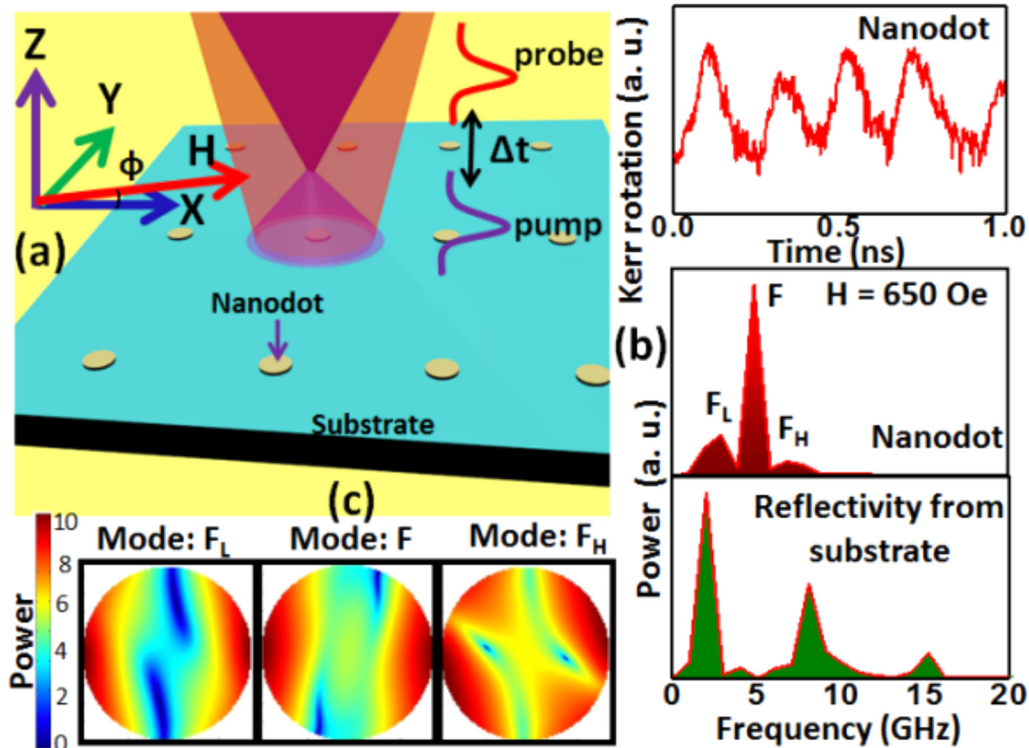


FIG. 5. (a) Schematic diagram of the experimental geometry. (b) Kerr rotation data and corresponding frequency spectra obtained from a Co nanodot for bias magnetic field $H = 650$ Oe. The peaks in the latter spectrum correspond to the frequencies of the SAWs excited in the PMN-PT substrate. (c) Simulated power profile of the SW modes in the nanomagnet. Adapted with permission from Mondal *et al.*, ACS Appl. Mater. Interfaces **10**, 43970 (2018). Copyright 2018 American Chemical Society.⁶²

achieved by mirror symmetry breaking in a MAW and subsequent application of an external magnetic field.⁸⁹

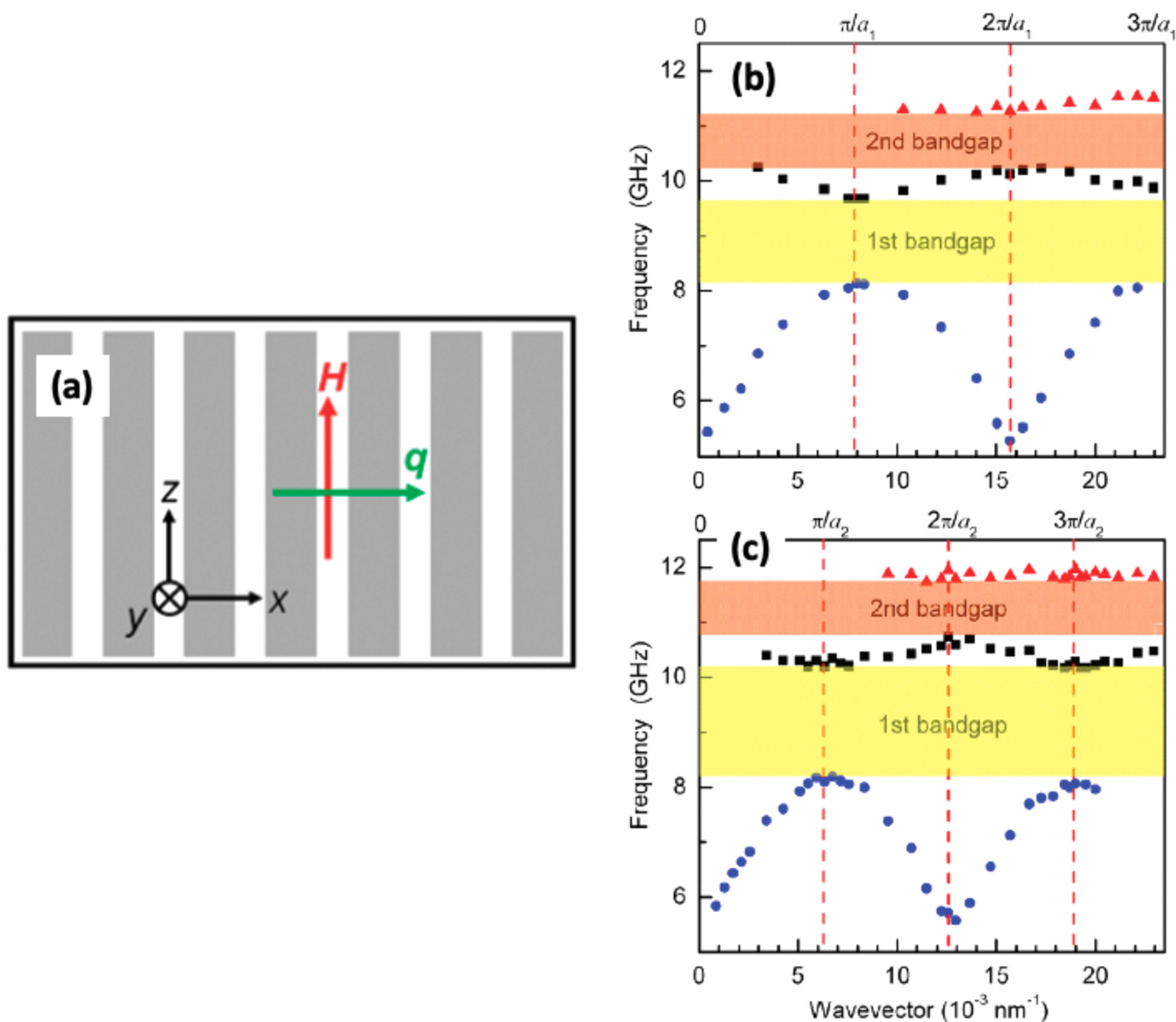
1D MCs in the form of ordered arrays of ferromagnetic nanostripes or nanowires have attracted considerable interest, where the magnetic shape anisotropy plays a significant role, leading to the bi-stable magnetic states. In high aspect ratio ferromagnetic nanowires, the shape anisotropy naturally occurs along the long-axis of the wire. Hence, the preferred orientation of magnetization, i.e., the intrinsic easy axis lies along the long-axis, whereas the short-axis is the intrinsic hard axis of the wire. Topp *et al.*⁹⁰ observed that Py nanowires having a bi-stable magnetic configuration show two different magnon band structures depending on the magnetic ordering (parallel and antiparallel alignment) of the neighboring nanowires. At a zero in-plane magnetic field, the SW modes of the antiparallel case were close to those obtained by zone folding of the SW dispersions of the parallel case, whereas for a non-zero magnetic field, a forbidden frequency gap was opened at the Brillouin zone (BZ) boundary. Wang *et al.* fabricated MCs consisting of Co/Py nanostripes having stripe widths of 150, 250, 350, 400, and 500 nm.⁹¹ Figure 6 shows their measured SW dispersion curves featuring the MBG in Co(150 nm)/Py (250 nm) and Co(250 nm)/Py(250 nm) MCs. The nonmonotonic variation in the width of the MBG (in the order of 1.4–2.6 GHz) was observed at the BZ boundaries by varying the stripe width.

Such tailoring of MBG can enable controlled transmission of SWs within the magnonic devices.

All-optical TRMOKE study of the SW dynamics in Py nanostripes showed a stark variation in the frequency, anisotropy, and spatial nature of SWs depending on the stripe width and the orientation of the magnetic field.⁹² The quantization axis of the SW modes inside the stripes was found to deviate from the stripe axis and complicated spatial distribution of SW amplitudes was observed. Single-crystal Ni nanowires with a high aspect ratio revealed that standing and uniform SW modes can merge to a form a single uniform SW mode by tuning the magnetic field.⁹³ The nonlinear effect of propagating SWs has also been observed in ferromagnetic microstripes.⁹⁴ Width modulated stripes have been claimed to have rich potential for magnonic band tunability simply by varying the modulation parameters⁹⁵ and only few experimental studies exist to that end.⁹⁶ A recent study showed that the MBG in an asymmetric saw-tooth-shaped ferromagnetic array forming a pseudo-1D MC can be easily reconfigured by changing the orientation of the applied magnetic field.⁹⁷

F. Dynamics of magnetic nanoparticles

Chemical synthesis of MNPs is relatively easier compared to nanofabrication based on lithography. Their dimensions can reach



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FIG. 6. (a) Directions of applied magnetic field H for saturation of samples and magnon wavevector q relative to orientation of their nanostripes. Measured dispersion relations, featuring bandgap structures, of spin waves in (b) 150 nm Co/250 nm Py and (c) 250 nm Co/250 nm Py magnonic crystals, with respective lattice constants $a_1 = 400$ nm and $a_2 = 500$ nm. Experimental data are denoted by symbols. The first and second frequency bandgaps are represented by the shaded bands, while the Brillouin zone boundaries ($q = n\pi/a$) are denoted by the dashed lines. Adapted with permission from Wang *et al.*, ACS Nano 4, 643 (2010). Copyright 2010 American Chemical Society.⁹¹

close to the atomic scale, and they are susceptible to an external magnetic field. Hence, they find applications in multidisciplinary fields, such as nanoelectronics, magnetic data storage, sensors, contrast enhancement in magnetic imaging, drug delivery, and other biomedical applications.^{98,99} Magnetization reversal of MNPs have been studied extensively, and it was shown that the 2D Stoner–Wohlfarth model is too simple and higher order anisotropy terms are essential to

understand their magnetization reversal dynamics both in classical and quantum limits.¹⁰⁰ Furthermore, the issue of a high switching field of MNPs with smaller size have been resolved by the simultaneous application of a small dc field with a rf field in a 20-nm-diameter Co particle using micro-SQUID measurement.¹⁰¹ The magnetization reversal mechanisms for assembly of MNPs mediated by the exchange and dipolar interactions have been studied in detail.^{11,102}

The first measurement of ultrafast spin dynamics of MNPs was reported by Buchanan *et al.*, who studied the magnetic field pulse-induced precessional dynamics of Fe nanocrystals of 25 nm size embedded in an SiO₂ matrix.¹⁰³ Observation of high resonance frequency, strong effective damping, and electrically insulating character of the samples were considered favorable for application in ultrafast magnetic sensors. Andrade *et al.* measured the optical pulse-induced coherent precessional dynamics in superparamagnetic Co particles with sizes down to 2.5 nm in Al₂O₃ matrix. For the smallest particles, the precession was found to be critically damped, preventing their coherent magnetization reversal. A complete gyroscopic pathway during magnetization reversal of small superparamagnets was, therefore, considered unlikely.¹⁰⁴ The time-resolved ultrafast demagnetization and subsequent relaxation processes of colloidal ferrites showed a strong size and magnetic ordering dependence of the amount of magnetization quenching and recovery but no such variation in the demagnetization time. The partial re-establishment of ferrimagnetic ordering before electronic relaxation was correlated to the faster recovery (~2 ps), while the slow recovery was correlated to the electronic relaxation.¹⁰⁵ The same authors investigated the time-resolved magnetization dynamics of Fe₃O₄ nanocrystals with size down to 5 nm to understand the relative efficiency of the spin–lattice relaxation on the surface of the nanocrystals with respect to its interior.¹⁰⁶ In Co(core)–Pt(shell) NPs with 5 nm core diameter and 1.5 nm shell width, the effect of hard laser annealing was found to cause diffusion of Pt into the Co core, resulting in the formation of CoPt alloy and an increase in the magnetocrystalline anisotropy. The latter caused a femtosecond laser-induced GHz frequency magnetization precession in CoPt NPs, which was absent in their superparamagnetic counterparts.¹⁰⁷ Rana and Barman reported a cluster configuration independent ultrafast demagnetization in Ni NPs with chain, bundle, dendrite, and random assemblies.¹⁰⁸ However, the fast- and slow-recovery times and precessional dynamics were found to be strongly dependent on the agglomeration geometry due to their internal distribution and interaction with the environment. The precession frequencies decreased with the ordering in the agglomeration geometry most likely due to the decrease in the shape anisotropy. More recently, the measurement of spatially resolved demagnetization inside FePt NPs using time-resolved coherent x-ray scattering showed inhomogeneous demagnetization within the NPs, which occurred more rapidly at the boundary of the NP. It further showed the formation of the shell region with reduced magnetization driven by a superdiffusive spin flux and its inward propagation at a supermagnonic velocity.¹⁰⁹ Various theoretical models of MNP dynamics and computational nonequilibrium models⁹⁹ exist to underpin the intriguing physics of these system, and it is still an open field of research.

G. Dynamics of 2D arrays of magnetic nanostructures

Patterning of magnetic thin films in 2D down to the nanoscale can lead to connected and disconnected structures with the recent advancement of fabrication technologies. Based on their structural features, they can be broadly classified as nanodot, antidot, nanoring, bi-component, and binary nanostructures. In this subsection, we will briefly discuss their high-frequency dynamics.

1. Magnetic nanodots

The early theoretical studies of high-frequency response of ferromagnetic nanodot arrays commenced in the late 1990s, where the effects of inter-dot dipolar coupling on the dynamics by varying array geometry and magnetic field orientation have been studied.^{110,111} In an array of nanodots, a distribution of quasiuniform magnetization configuration, namely, “S”, “C”, flower, and leaf state, is possible due to the inevitable edge defects of the elements even in presence of a strong external magnetic field.¹¹² The initial experimental studies of FMR spectra of periodic nanodot arrays showed decomposition of a single resonance peak into multimodal oscillations, whose position strongly depends on the orientation of the external magnetic field and the interparticle interaction.¹¹³ This was followed by a slow upsurge of experiments in this field, viz., BLS studies of cylindrical Py nanodots showing two classes of modes, namely, higher-frequency DE-like and lower-frequency BV-like SW branches,¹¹⁴ spin excitation in similar nanodots over a wide magnetic field range covering uniformly magnetized and vortex states,¹¹⁵ and FMR study of perpendicularly magnetized nanodots showing a large number of modes independent of interdot separation stemming from the dipole–exchange interaction.¹¹⁶ Subsequently, the study of time-resolved magnetization dynamics in square-shaped Co₈₀Fe₂₀/Ni₈₈Fe₁₂ bilayer nanodot arrays with varying size down to 64 nm showed a non-monotonic variation of the precession frequency with dot size owing to a crossover from CM to EM domination below a dot diameter of 220 nm.¹¹⁷ This was followed by important observations like dynamical configurational anisotropy¹¹⁸ and SW modes in non-ellipsoidal elements with nonuniform ground states.¹¹⁹ In 2009, Shaw *et al.* used the frequency-resolved MOKE experiment in Py nanoelements having a diameter between 50 and 200 nm to observe that the intrinsic Gilbert damping parameter is generally unaffected by the nanopatterning process despite a large linewidth dependence on the size of the nanomagnets. The linewidth of the CM and EM were also found to differ considerably, most likely due to the sensitivity of the EM to small variations and imperfection of the shape and edge materials.¹²⁰

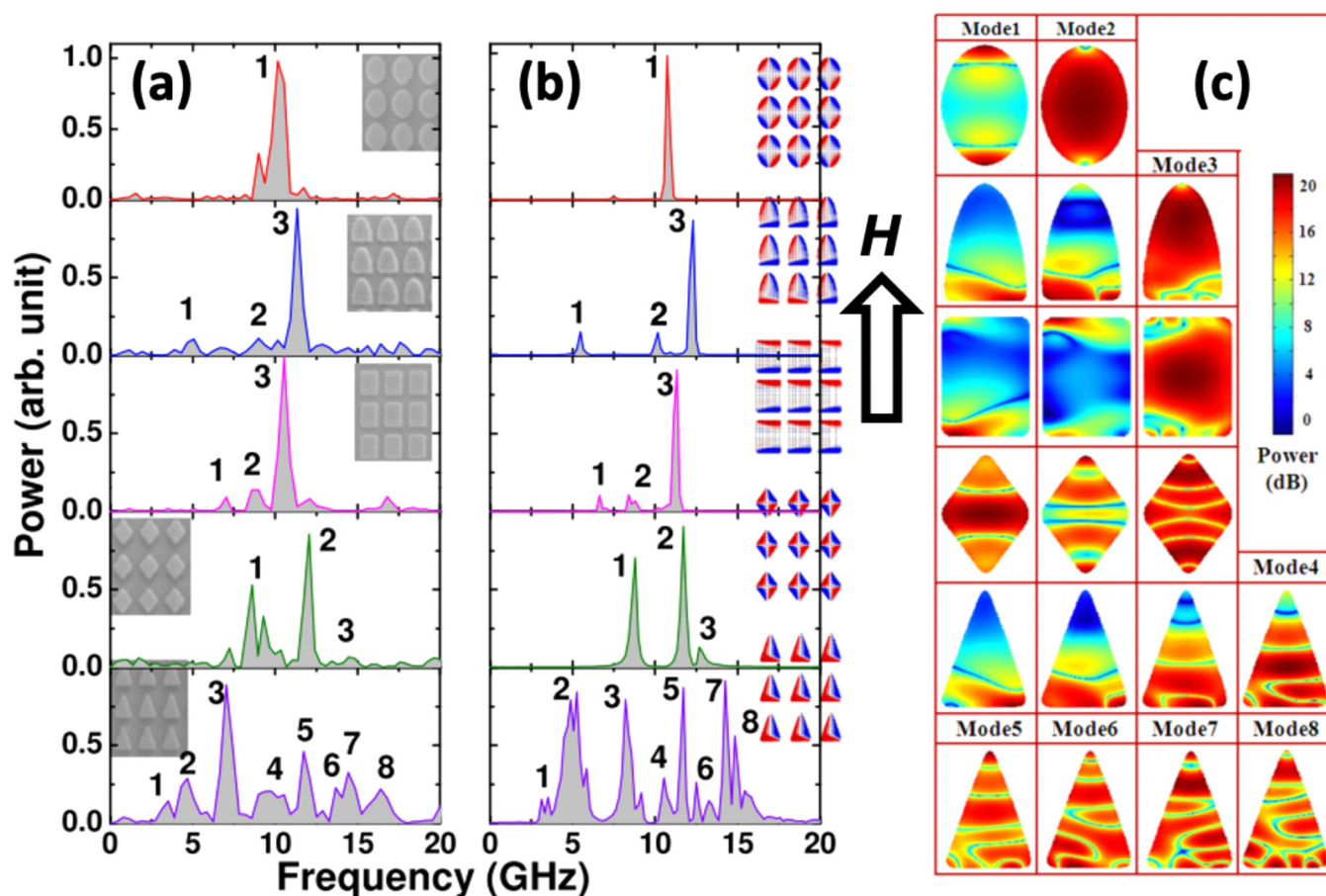
In the next decade, the focus shifted toward the observation of collective magnonic modes in strongly coupled arrays of nanoelements. In 2010, collective magnonic modes were detected in an array of closely spaced elements where the array appears as tailored magnonic metamaterials to spin and electromagnetic waves with a wavelength well beyond the period of the array.¹²¹ Anisotropic dynamic coupling for propagating collective modes were observed in 2D arrays of square elements.¹²² Further study in square-shaped Py nanodots arranged with varying areal density showed a transition from a single uniform collective mode at a very high areal density through weakly collective dynamics at an intermediate areal density to completely isolated dynamics of the individual nanodots at a very small areal density.¹²³ In the same year, collective SW excitations in the form of Bloch waves propagating through chains of dipolar-coupled nanodots characterized by magnonic energy bands were reported.¹²⁴ Bondarenko *et al.* showed collective modes for a ferromagnetic dot array with perpendicular magnetization.¹²⁵ The effects of lattice symmetry started to be explored when the magnetodynamical response of large-area close-packed arrays of

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circular dots on hexagonal lattice fabricated by nanosphere lithography was reported. Saha *et al.* reported a comprehensive study of the effects of varying lattice symmetry where a stark variation of collective SW modes was observed when the lattice symmetry of circular-shaped Py nanodot arrays were varied from square to octagonal through rectangular, hexagonal, and honeycomb lattices.¹²⁶

The effects of dot shape were also explored where a cross-shaped nanoelement showed a strong anisotropic behavior¹²⁷ and varying shapes like elliptical, half-elliptical, rectangular, triangular, and diamond-shaped elements showed a strong variation in SW spectra due to the internal field profile and the ensuing mode quantization.¹²⁸ Figures 7(a) and 7(b) show the experimental and simulation study of the SW spectra of 20-nm-thick Py nanodot arrays with varying dot shapes having lateral dimensions of $200 \times 250 \text{ nm}^2$ of individual dots and edge-to-edge interdot separation of 75 nm, at a bias magnetic field of 1.12 kOe.¹²⁸ Stark variation in the number of SW modes was observed between different

nanodot shapes. The power distributions of simulated SW modes for single nanodots of different shapes are shown in Fig. 7(c). Mode 1 for the elliptical, half-elliptical, and rectangular dots is an EM. Mode 2 for elliptical and Mode 3 for half-elliptical and rectangular dots are the CM. Mode 3 forms a quantized mode in the DE geometry near the base of the half-elliptical dot and the horizontal edges of the rectangular dot. Mode 2 for half-elliptical and rectangular dots is the EM and DE modes, respectively. In diamond dots, all the modes are quantized modes in the BV geometry with varying mode number. The triangular dot shows a more complicated mode structure as opposed to the other shapes. In this case, Mode 1 is a localized mode near the base of a triangle. Modes 2–8 extend from the base to the vertex and form mixed quantized modes of BV and DE characters. Figure 8 shows the effects of dot shape on the bias field-dependent SW frequencies for 2D nanodot arrays with the above-mentioned shapes. The experimental data are plotted for selected frequency for each dot shape as shown in the



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FIG. 7. (a) Experimental and (b) simulated SW spectra at an applied field of 1.12 kOe of 20-nm-thick $\text{Ni}_{80}\text{Fe}_{20}$ nanodots arrays with varying dot shapes [shown in inset of (a)] having lateral dimensions of $200 \times 250 \text{ nm}^2$ of individual dots and edge-to-edge interdot separation of 75 nm. (c) Simulated power profiles of single nanomagnet of different shapes. Applied magnetic field (H) direction is shown. Adapted with permission from Mahato *et al.*, Appl. Phys. Lett. **105**, 012406 (2014). Copyright 2014 AIP Publishing LLC.¹²⁸

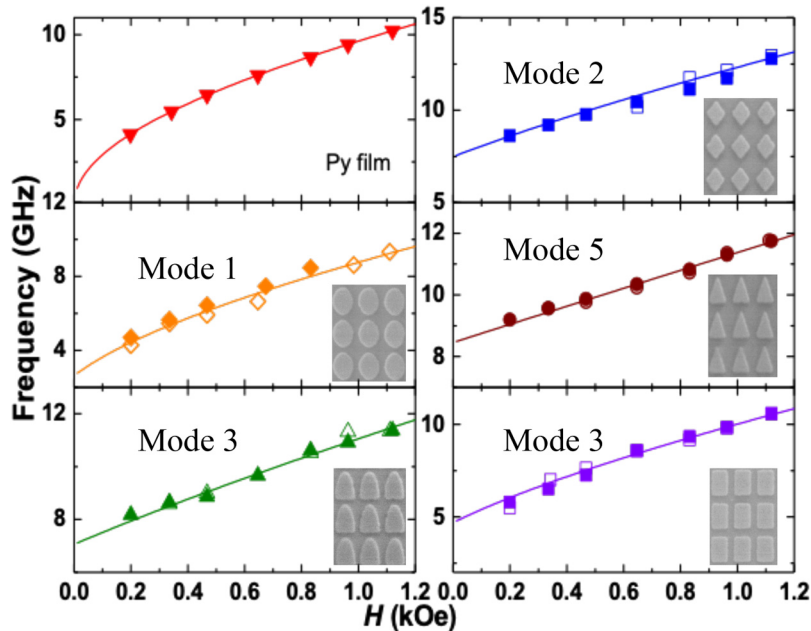


FIG. 8. Bias magnetic field-dependent frequency of the uniform precessional mode of a 20-nm-thick $\text{Ni}_{80}\text{Fe}_{20}$ thin film and nanodot arrays with varying dot shapes having lateral dimensions of $200 \times 250 \text{ nm}^2$ of individual dots and edge-to-edge interdot separation of 75 nm. The mode numbers are mentioned in each panel, which can be mapped with Fig. 7. The filled symbols show the experimental data obtained from the TRMOKE experiment and open symbols are micromagnetic simulation results. The solid line is a fit with the Kittel formula. The SEM images of the nanodots are shown in the insets.

figure. The data are fitted with the Kittel formula¹²⁹

$$f = \frac{\gamma}{2\pi} \sqrt{(H + (N_x - N_x)4\pi M_s)(H + (N_z - N_y)4\pi M_s)}, \quad (9)$$

where N_x , N_y , and N_z ($N_x + N_y + N_z = 1$) are the demagnetizing factors for the nanodots. From the fits, we obtained (N_x, N_y, N_z) as (0.103, 0.193, 0.704) for elliptical dots, (0.011, 0.079, 0.910) for diamond dots, (0.137, 0.337, 0.526) for triangular dots, and (0.027, 0.047, 0.926) for rectangular dots. However, the obtained demagnetizing factors contain contributions from both the individual elements and the stray field mediated inter-element interactions. The cross-shaped element continued to show great prospects with observations like mode softening, mode crossover, mode splitting, and merging of SW frequency branches with the bias field strength and orientation¹³⁰ and more recently a strong magnon–magnon coupling and nonlinear FMR behavior.¹³¹ Microwave power dependent nonlinear FMR shift of the resonant modes has also been previously observed in patterned magnetic systems.^{132,133}

2. Magnetic antidots

Magnetic antidot lattices (ADLs), i.e., periodically perforated ferromagnetic thin films are considered to be a strong candidate for designing reconfigurable MCs. The ADLs have some unique advantages over the isolated nanomagnet arrays due to the absence of any small isolated magnetic entity. Here, the entire film remains exchange-coupled and hence offers higher SW propagation velocity and longer propagation distance for the SWs as opposed to isolated nanomagnets. The ADLs can also be described as a mess of connected networks, which do not suffer from the superparamagnetic lower limit as opposed to the isolated nanomagnets. Extensive

experimental and numerical investigations on the dynamics of standing and propagating SWs in magnetic antidots have led toward important findings.

Martyanov *et al.*¹³⁴ reported the first experimental study of the magnetization dynamics of Co antidot arrays by FMR, which showed evidence that characteristic inhomogeneities in the magnetization distribution around the antidots give rise to the changes of the resonance modes with the in-plane direction of the magnetization. This was immediately followed by study of SW localization between nearest and next nearest holes of ADL.⁸ Subsequently, observation of the magnonic normal mode,¹³⁵ Bloch-wave mode, and an unusual bias field independent mode¹³⁶ in ADL were reported. Anisotropic propagation, damping, and velocities of SWs with bias field orientation¹³⁷ were important developments besides the tunability of transmission coefficient of SW by the orientation of an external magnetic field claiming a tunable metamaterial response.¹³⁸ Some key phenomena of SW dispersion in magnetic ADL appeared in a flurry, e.g., Bragg diffraction of SW from ADL and ensuing MBG,¹³⁹ high-symmetry magnonic modes in perpendicularly magnetized ADL,¹⁴⁰ and complete MBG for magnetostatic forward volume waves in 2D ADL.¹⁴¹ Subsequently external and internal control of SW modes in ADL started by varying the lattice constant,¹⁴² antidot shape,¹⁴³ lattice symmetry,¹⁴⁴ base material,^{145,146} bias field strength, and orientation.^{137,147} Furthermore, several interesting phenomena such as mode conversion,¹⁴⁸ mode crossover and mode hopping,¹⁴⁹ mode softening,¹⁵⁰ as well as the formation of magnonic mini band¹⁵¹ have been reported.

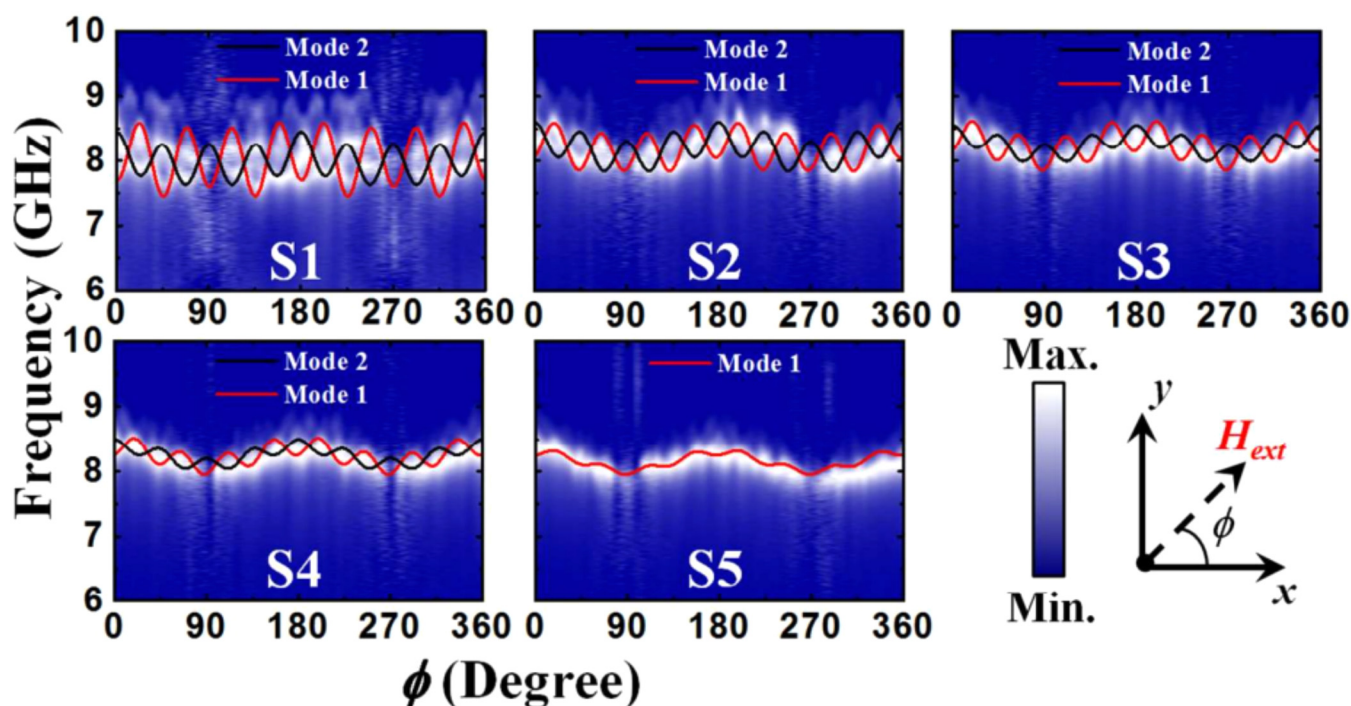
Defects play important roles in MCs. It can either be inadvertent defects originating from nanofabrication or tailored defects that can be used to our advantage for further tunability of magnonic bands and creation of defect states. Numerical studies

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showed that the magnonic spectra of an hexagonal array of antidot is quite robust to random defects.¹⁵² Introduction of a line defect, on the other hand, showed elevated frequency of the fundamental mode due to the increase in internal field in antidot-free region and generation of a new extended mode with wider profile.¹⁵³ An extensive study of defects showed softening of the EM and localized modes accompanied by a possible amplification of the extended modes at quasi-saturation fields and to a local alteration of SW mode profiles. At low fields, new SW modes are observed in the continuous regions due to the non-synchronous rotation of the magnetization with respect to patterned areas.¹⁵⁴ Unconventional structures like magnonic quasicrystals (MQCs) in the form of octagonal lattice of antidots,¹⁵⁵ binary ADL with alternating hole diameter,¹⁵⁶ and defective honeycomb lattice¹⁵⁷ have been developed in the pursuit of greater tunability of SW spectra and anisotropy. Figure 9 shows that the lower-frequency SW modes of octagonal ADLs exhibit an unconventional eightfold rotational anisotropy superposed with weak twofold and fourfold anisotropies. Significantly, the contribution of eightfold anisotropy gradually reduces with the increase in lattice constant. New measurement techniques like all-electrical measurement by using the inverse spin Hall effect (ISHE)¹⁵⁸ have also fuelled new interests in this field. Potential applications using ADL includes development of highly reprogrammable magnetic arrays¹⁵⁹ and tunable magnonic filters¹⁶⁰ integrated in a MAW.¹⁶¹

3. Magnetic rings

Ferromagnetic nanorings are high-symmetry structures in which magnetization forms a circulation state without the presence of a vortex core as opposed to a disk. The magnetic normal modes in nanorings are also simpler than those in disks. The study of spin dynamics in a ring structure is also of direct practical importance, as the circulation direction in ring structures has been proposed to be useful in vertical magnetoresistive random access memory (MRAM) cells.¹⁶² They can have two types of magnetic states: a flux closure or “vortex” state and an “onion” state with same moment orientation in each half of a ring. They exhibit a range of different switching mechanisms including DW and vortex core nucleation, annihilation, and propagation. Initial studies showed that the transitions from onion-to-vortex and vortex-to-reverse onion states are strongly dependent on the edge-to-edge-spacing of the rings due to dipolar interactions as well as shape anisotropy.¹⁶³ The seminal work on the dynamics of the ring structure showed the excitation of two dominant modes by uniform perpendicular and in-plane pulsed field, respectively. Those were a circularly symmetric uniform mode and a rotationally antisymmetric mode, while other modes were of very small amplitude.¹⁶⁴ In the same year, Giesen *et al.* showed that depending on the ring width, a splitting of the uniform precession mode occurs, and the high-intensity FMR modes are localized in specific segments of the ring.¹⁶⁵



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FIG. 9. Variation of SW frequency with the azimuthal angle (ϕ) varying from 0° to 360° for NiFe ADLs with various lattice spacing (S1–S5) are presented at a bias magnetic field $H_{ext} = 800$ Oe. The surface plots represent the experimental results while the solid lines describe the sinusoidal fits for the observed anisotropic SW modes in all the samples (S1–S5). The color map associated with the surface plots and the schematic of the orientation of the external applied field (H_{ext}) are given at the bottom right corner of the figure. Reproduced with permission from Choudhury *et al.*, ACS Nano 11, 8814 (2017). Copyright 2017 American Chemical Society.¹⁵⁵

Investigation of spatially resolved dynamic eigenmode spectrum in Co rings revealed up to five resonant modes in the frequency range from 45 MHz to 20 GHz as a function of an external magnetic bias field. The vortex and onion states led to well-defined and distinctive mode structures, which were affected by the dynamic inter-ring coupling.¹⁶⁶ The applied magnetic field has also been used to split the radial and azimuthal excitations due to either mode localization or symmetry.¹⁶⁷ Figure 10 represents the

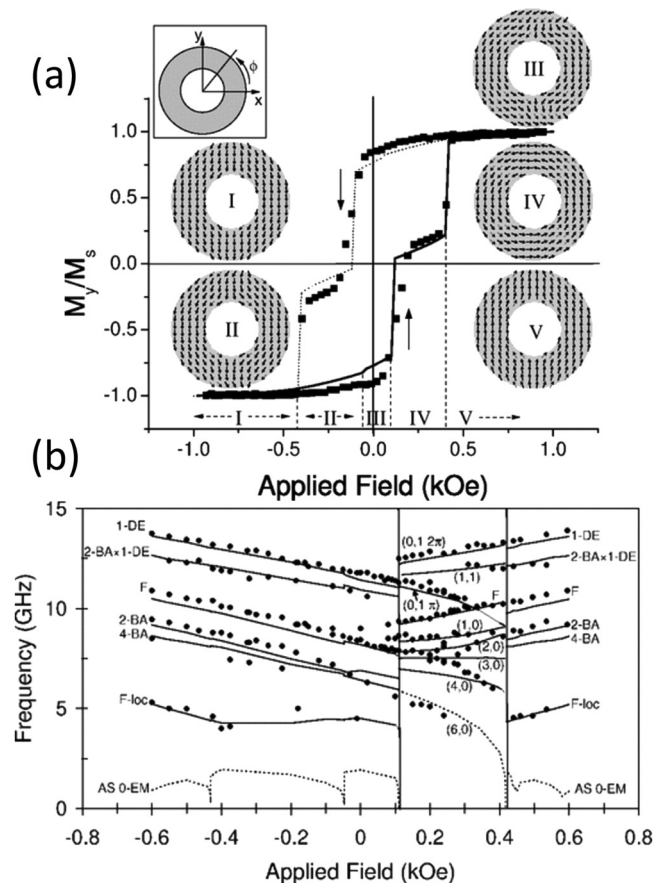


FIG. 10. (a) Experimental longitudinal Kerr hysteresis loop (symbols). Calculated loop in the micromagnetic approach: solid line refers to the increasing applied field and dotted line to the decreasing field. M_y/M_s is the component of the magnetization in the direction of the applied field in unit of the saturation magnetization M_s . Five configurations of the equilibrium magnetization are sketched and labeled by Roman numbers: onion state (phase I), distorted onion states (II and III), vortex state (IV), and reversed-onion state (V). The inset shows the reference system. (b) BLS measured frequencies of the spin modes (symbols) starting from negative to positive applied field values. The calculated frequency dispersions of the modes (lines) are labeled according to the character of the modes. (m,n) are the vortex modes. DE, BA, F, and EM are Damon-Eshbach-type, backwardlike, fundamental, and end modes, respectively. The two thin vertical lines mark the critical fields $H_{c1} = 110$ Oe (onion-to-vortex transition) and $H_{c2} = 417$ Oe (vortex-to-onion transition). Adapted with permission from Montoncello *et al.*, Phys. Rev. B **78**, 104421 (2008). Copyright 2008 American Physical Society.¹⁶⁸

transition between “vortex” and “onion” states and the influence of their internal spin configuration on the field-dependent precession frequencies during this transition.¹⁶⁸ Furthermore, a distinct series of quantized azimuthal modes in a vortex state stemmed from the constructive interference of circulating SWs was observed. This can be considered as a magnetic ring resonator resolved up to the fourth order.¹⁶⁹ Observation of coherence and partial decoherence in Py rings in the onion state was mapped by micro-focused BLS.¹⁷⁰ The shape of the ring added additional complexity in the statics and dynamics and as opposed to a circular ring, triangular¹⁷¹ and square¹⁷² nanorings showed larger number of modes, the nature and frequencies of which strongly depend on the orientation of the applied magnetic field. A width-dependent transition from radial to azimuthal modes was observed in the square ring. Anti-rings are another type of interesting structure, and direct mapping of static and dynamic magnetizations and their potential application in bio-sensing have been reported.¹⁷³ More recently, SW mode conversion and mode hopping in anti-ring structures have been observed,¹⁷⁴ leading toward their potential use in magnonics.

4. Bi-component magnetic nanostructures

MCs have been conventionally studied in the form of single component nanodot arrays or antidot arrays, while a combination of more than one material or structure may offer greater control on magnonic spectra and band structure. To this end, bi-component MC (BMC) and binary structures are important developments in MCs. Interestingly the first report on MC was a composite or bi-component medium where a ferromagnetic material embedded in a ferromagnetic background (Fe cylinders in an EuO matrix) showed MBG.¹⁷⁵ Although theoretical works progressed in this field,¹⁷⁶ it was not until 2009 when MBG in a 1D bi-component stripe (Co/Py) was revealed.¹⁷⁷ The size tunability of MBG in 1D BMC was an important development.⁹¹ Soon after this, investigation on 2D BMC was started and Co nanodisks embedded in Py antidots showed two channels of SWs, one through the Co nanodisk and another in between them.¹⁷⁸ In a parallel work on SW dispersion, 2D BMC consisting of Co square dots embedded in Py matrix showed larger frequency width of magnonic bands than the constituent antidots and a complicated magnonic band structure, where the Co dots act as amplifiers of dipole coupling between the Py dots.¹⁷⁹ The tunability of the forbidden frequency gap with periodically varying magnetic parameters is investigated for the first and the second BZs of a 2D BMC, consisting of circular-shaped Co nanodots embedded in a Py matrix by Tacchi *et al.* (see Fig. 11).¹⁸⁰

A major challenge in the fabrication of a 2D BMC was to achieve direct physical contact between the two different magnetic materials. Choudhury *et al.*¹⁸¹ achieved this feat in Py-filled CoFe ADLs, where they obtained a strong signature of inter-element exchange interaction across the interface and ensuing enhancement of the SW propagation velocity by a factor of three as opposed to the ADL only. The shape of the BMC has also been varied in this study, and a more recent report on triangular BMC showed strong anisotropic SWs.¹⁸² In an important development, 2D CoFeB/Py bi-component lattices have been used as an omnidirectional

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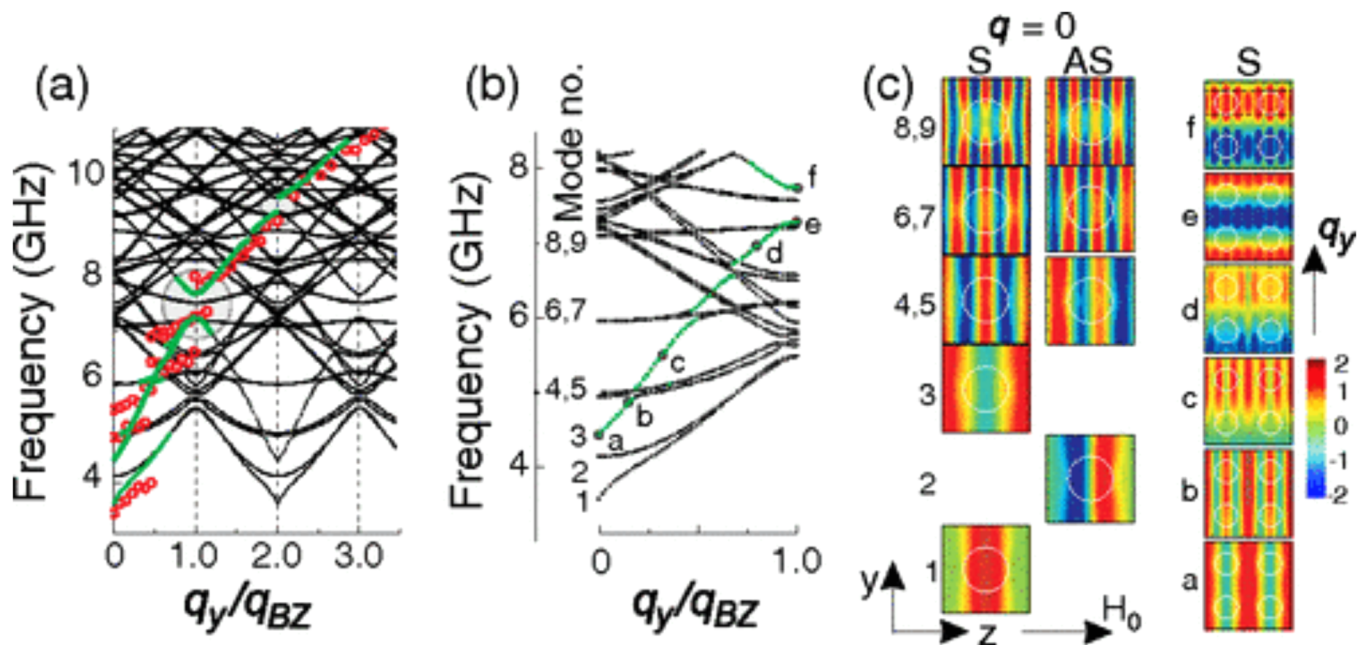


FIG. 11. (a) Magnonic band structure of the Co/Py 2D BMC calculated by the PWM (black dotted lines). The bold solid lines mark the calculated bands with the largest intensities. We replot the BLS data from Fig. 2 as open circles. Filled gray circles highlight the magnonic gaps opened at the first and second BZ boundaries (indicated by vertical dashed lines). (b) The enlarged part of the calculated magnonic band structure from the first BZ shown in (a). The modes are numbered from 1 to 9 according to arrangements at the center of the BZ. (c) Left panel: x components of the magnetization vector, m_x , for modes 1–9. Right panel: evolution of mode 3 for wave vector values $q_y/q_{BZ} = 0, 0.18, 0.34, 0.8,$ and 1 , as indicated by filled dots and indexed with small letters from a to f in (b). In points e and f, the horizontal broken lines indicate the regions where the stationary waves have the maximum of the spin precessional motion. Reproduced with permission from Tacchi *et al.*, Phys. Rev. Lett. **109**, 137202 (2012). Copyright 2012 American Physical Society.¹⁸⁰

nanograting coupler, which showed an enhancement of the amplitude of the short-wavelength SWs as compared to a bare microwave antenna.²⁸ The improved functionalities of BMCs come at the expense of more complicated fabrication processes, such as multi-step lithography and TPL.

Another form of BMC, namely, binary nanostructures, can provide similar flexibility along with simpler single-step lithography process by placing two structures of same or different material next to each other forming the basis of the crystal. A Py/Co binary nanostructure grown by a simple self-aligned shadow deposition technique showed rich SW spectra and large anisotropy of SW.¹⁸³ A binary nanostructure in the form of a diatomic nanodot array (dipolar-coupled Py nanodots forming a complex double-dot basis) showed excellent tunability of the magnonic band structure by changing the orientation of the bias magnetic field in the BLS measurements. New interaction modes appeared in this structure due to strong dipolar coupling between the inter-dot interaction in the diatomic unit.¹⁸⁴ A strong anisotropy in the SW dispersion is observed in this structure, which is also evident in the iso-frequency curves, promising their applications in magnon focusing and defocusing.¹⁸⁵ Observation of spectral narrowing and mode conversion in novel binary nanostructures has been reported where square-shaped Py nanodots of two different sizes are diagonally connected to form a binary basis.¹⁸⁶

H. Dynamics of nanoscale magnetic multilayers

Magnetic multilayers (MMLs) offer a huge versatility in quantum magnetic properties, including spin-dependent scattering, spin tunneling, exchange anisotropy, orbital hybridization, perpendicular magnetic anisotropy (PMA), interfacial DMI (IDMI), pure spin current, SHE, the Rashba–Edelstein effect, spin caloric effect, voltage controlled magnetic anisotropy (VCMA), and topological spin textures. A variety of existing or proposed spintronic devices are based on MLs, namely, giant magnetoresistive sensor, MRAM cells, STNOs, racetrack memory, and non-reciprocal magnonic devices. In all forms of devices, nanopatterning is the key. However, inclusion of this huge field in this subsection is beyond our scope. Hence, we discuss three important aspects, namely, patterned PMA structures, STNO structures, and pure spin current-driven nanomagnet dynamics using SHE.

MMLs with PMA are prospective candidates for bit patterned media. They also have applications in skyrmions, VCMA, and various other fields. Although significant works on the magnetization dynamics of thin film MML with PMA have been reported,^{187–190} very few efforts have been made on the dynamics of nanostructured MML with PMA. Some reports exist on magnetization reversal and DW study with defects and edge corrugations,¹⁹¹ increase of coercive field¹⁹² in Co/Pd antidots, and DW pinning in

Co/Pt antidots.¹⁹³ Theoretical study of SW in patterned MMLs with PMA using discrete dipole approximation showed that magnetic inhomogeneity along the central axis splits the magnetostatic SWs into two bands and the exchange SWs into a number of bands as a result of the underlying long- and short-range interactions, respectively.¹⁹⁴ The first experimental observation of SW dynamics in this system was done in 2014, when Pal *et al.* observed a decrease in SW frequency with increasing density of antidots, down to values well below the FMR frequency of the continuous ML, in a series of [Co(0.75 nm)/Pd(0.9 nm)]₈ ADLs with PMA.¹⁸⁹ This was modeled by assuming nanoscale rim-like shell regions surrounding the antidots created by the Ga⁺ ion bombardment during patterning using the FIB technique. The decrease of SW frequencies is found to be driven by a dynamical coupling between the localized modes within the shells, most likely by tunneling and exchange interactions. The shape of the antidots has found to play decisive roles in the in-plane domain structure and the ensuing edge-localized SW spectra, their mutual interactions, and interactions with bulk SW excitations.¹⁹⁵

It is quite fascinating that spin-polarized current or pure spin current can apply torque on the magnetization in MMLs, which can excite oscillatory magnetic modes in the nanomagnets. In a magnetic tunnel junction-based STNO, this microwave oscillation is converted to voltage from the change in magnetoresistance. In SHNO, pure spin currents drive local regions of magnetic films and nanostructures into auto-oscillation. These microwave-generating nanomagnets can act as nanoscale motors, resonators, transducers, etc. The first experimental demonstration was reported by exploiting a heterodyne mixer circuit for 130 × 170 nm² elliptical nanopillar made of Cu(80 nm)/Co(40 nm)/Cu(10 nm)/Co(3 nm)/Cu(2 nm)/Pt(30 nm) MLs.⁷⁷ The achievable power could be tuned by varying the current and magnetic field for a wide frequency range. Additionally, on tuning several factors, the dynamics entered from the linear to nonlinear regime. However, the microwave power emitted from a single STNO was found to be only 1 nW. Thus, the necessity for designing mutually phase-locked array of oscillators became crucial. The mutually synchronized oscillators showed a sudden narrowing of the signal linewidth and an increase in the power due to coherence.²⁶ This caused noise reduction and increased stability analogous to the array of Josephson junction oscillators. The output power can scale with N^2 at room temperature where N is the number of oscillators. Thus, collective dynamical response from the array of nano-oscillators can be extremely useful in powering a larger network and neuromorphic computing.¹⁹⁶

The successful generation of microwaves in ML nanomagnets can be achieved in another energy-efficient manner. The antidamping-like torque exerts a negative damping on the magnetization and can eventually overcome the intrinsic damping showing auto-oscillation around the effective magnetic field. However, suppression of the auxiliary modes showing nonlinear trends must be deliberately avoided. Demidov *et al.* demonstrated the construction of such SHNOs in specially designed ML structures and explained the intriguing mechanism for a single nanomagnet.²⁵ The same group developed a nano-notch SHE oscillator directly incorporated into a magnonic nano-waveguide for simultaneous excitation and enhancement of propagating SW in the waveguide.¹⁹⁷ It has further been demonstrated that by controlling

the PMA strength, one can suppress the nonlinear magnetic damping,¹⁰ for achieving decay-free propagation and probable amplification of SWs.¹⁹⁸

I. Dynamics of nanoscale spin textures

Spin textures are nonuniform spin configurations in magnetic materials, which are stable, resilient, and yet possess a remarkable degree of tunability and scalability. They are extremely promising for energy-efficient, dynamically reconfigurable, and reprogrammable components in spintronics and magnonics. Here, we briefly discuss the progress in magnetization dynamics of spin textures, namely, DW, vortex, and skyrmion.

1. Domain wall

Magnetic DW is a common magnetic texture with intriguing physical properties, which has attracted huge scientific interest due to its potential application in magnetic logic devices and topology-based memory applications.¹⁹⁹ Motion of the DW in response to high frequency has drawn attention since 1950.²⁰⁰ Later, current-induced dynamics and switching of domains attracted attention, and domains in adjacent cobalt layers were manipulated controllably between stable parallel and antiparallel configurations by applying spin-polarized current pulses of the appropriate sign.²⁰¹ Imaging of DW oscillation by TRSKM showed two different oscillation modes at 0.8 and 1.8 GHz to be concentrated at different parts of the DWs in a microscale magnetic element.²⁰² Subsequently, intrinsic nonlinearity in the resonant response of magnetostatically coupled transverse DWs was demonstrated.²⁰³

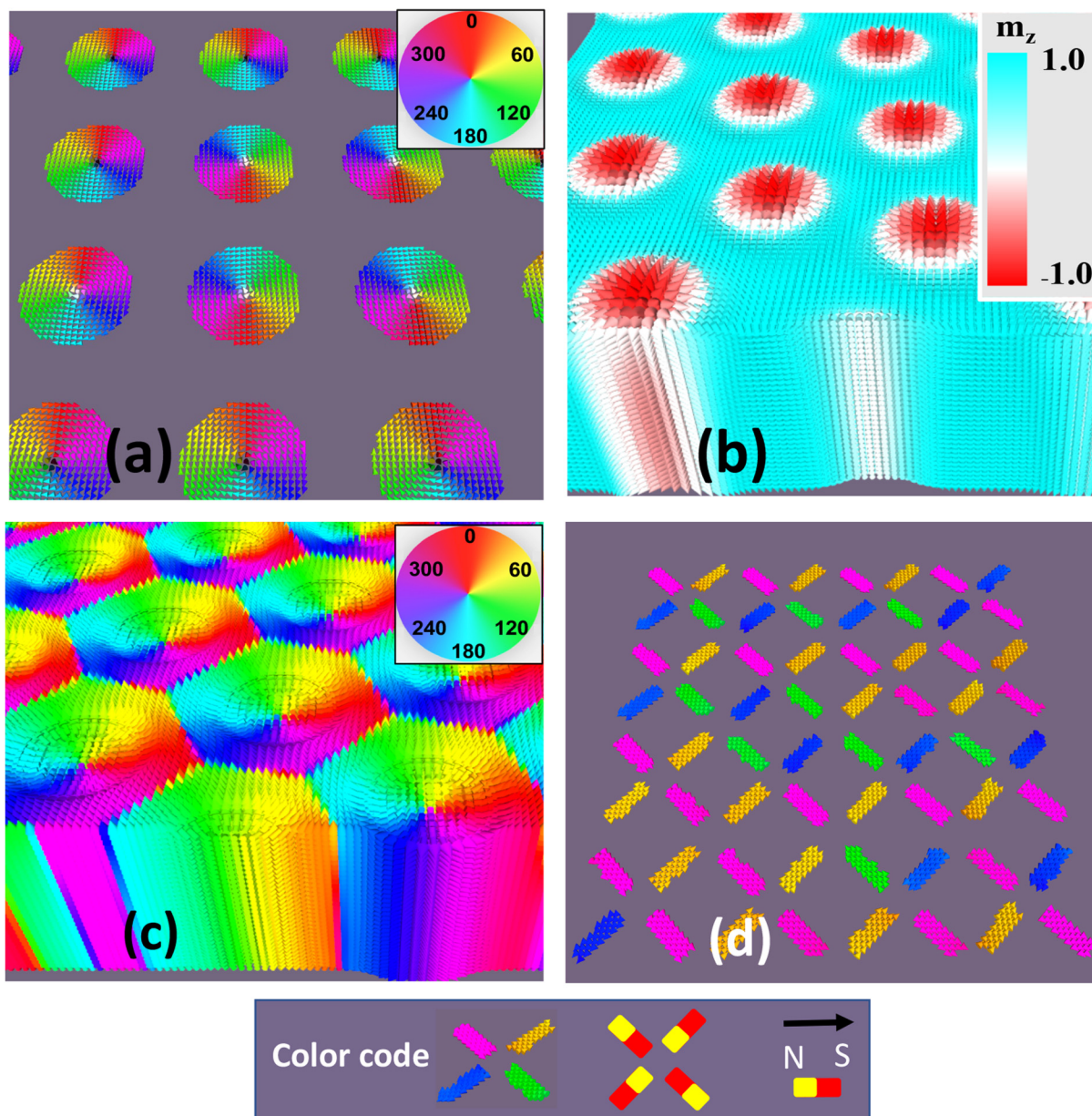
The interaction of SW with DW has also become an important topic. Hertel *et al.* numerically showed that the presence of a 360° DW causes strong attenuation of the radiating SWs due to the pronounced phase-lag between the propagating wavefronts along the two arms of a nanoring.²⁰⁴ A similar phase-shift was also predicted for the SWs colliding with 180° Bloch-DW.²⁰⁵ Kim *et al.* reported that monochromatic dipole-exchange SW undergoes a peculiar negative refraction due to collision with the 90° DW at the twin interface of a 5-nm-thick Fe film with cubic anisotropy.²⁰⁶ Using LTEM imaging, Sandweg *et al.* demonstrated the modulation of thermal SWs in the presence of asymmetric transverse DWs.²⁰⁷ Further BLS measurements revealed the annihilation of quantized SW modes near the DW and the evolution of a new mode inside the complex SW structure due to the change in the effective internal field within the DW region.²⁰⁸ The focus gradually shifted toward the investigation of DW-assisted propagating SWs to construct reconfigurable magnonic nanocircuitry. Garcia-Sanchez *et al.* reported a remarkable observation of guiding of propagating excitations localized to the wall in curved geometries while flowing in close proximity to other channels.²⁰⁹ For Néel-type walls, they show strong non-reciprocity and an analogy with the whispering gallery modes of sound waves. Woo *et al.* illustrated DWs as stationary reservoirs of exchange energy that can be generated, manipulated, and used to release on-demand SWs.²¹⁰ This can further be detected by using DWs in an all-DW device. Recent emergence of the application of DWs as reconfigurable MC and SW nanochannels has been described in Sec. III I.

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2. Magnetic vortex

In systems with negligible magnetocrystalline anisotropy, the competition between demagnetization and exchange energy may lead to the flux closure structure like magnetic vortex with in-plane curling magnetization and out-of-plane core within ferromagnetic

planar element with certain dimensions [see Fig. 12(a)].⁶³ The core polarity ($P = \pm 1$) and in-plane circulation (clockwise or counter-clockwise) can be manipulated by the magnetic field, current, or spin-torque to make these topological solitons fundamentally interesting and viable for applications.^{211,212} Vortex core gyration is a



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FIG. 12. (a) Simulated spin configuration of 2D array of magnetic vortices with different polarity and circulation combinations. Simulated skyrmion lattice: (b) in-plane (x - y) angle variation of magnetization shows a hexagonal lattice symmetry. (c) Distribution of the m_z component shows the formation of skyrmion tubes along its thickness. Color maps are presented inside the figures. (d) Simulated spin configurations of a 2D artificial spin ice (ASI) structure at the remanent state. The color code is indicated at the bottom of the figure.

relatively slower process and the gyration frequency lies in the range of sub-GHz to about 1 GHz. An initial study of time domain measurement of vortex dynamics in Py square elements with lateral dimension down to 500 nm revealed a high-frequency mode originating from the uniform precession of the magnetization, which is associated with another low frequency mode (~ 0.6 GHz for the element size of 500 nm) characteristic of the spiral gyrotropic motion of the vortex core due to magnus force.²⁰² A rigid vortex model considering the edge poles and another model avoiding the edge poles were used to describe these motions. BLS measurements and hybrid micromagnetic modeling revealed the presence of azimuthal SW modes in magnetic vortex states in Py dots with 100 nm diameter and 15 nm thickness.¹¹⁵ Further experiment revealed splitting of the azimuthal modes into doublets due to the coupling between SWs and the gyrotropic motion of the vortex core.²¹³ Dynamics of a vortex with a pinning site showed gyration of the vortex about a single pinning site at low excitation amplitude, gyration due to the magnetostatic energy of the entire vortex for high excitation amplitude, and a sharp transition between these two amplitude regimes that is due to depinning of the vortex core from a local defect.²¹⁴ In 2010, a frequency controlled magnetic vortex memory was proposed.²¹⁵

Gyration of coupled magnetic vortices turned out to be an exciting problem and was first reported by Buchanan *et al.* where two vortices were found to stabilize in a single elliptical element. Four eigenmodes were observed, which were identified as the in-phase and out-of-phase polarization-dependent core gyration.²¹⁶ A flurry of papers on coupled magnetic vortices came after a few

years using different techniques,²¹⁷ which showed that the coupled pair of vortices behave like a diatomic molecule with bonding and antibonding states, promising the possibility for designing the magnonic band structure in an array of magnetic vortex oscillators.^{218,219} Barman *et al.* numerically showed an efficient energy transfer of gyration mode in a locally excited 1D chain of physically separated nanodisks,²²⁰ which was later experimentally verified by Hasegawa *et al.*²²¹ Jung *et al.* experimentally demonstrated the logic operations based on this idea.²²²

In 2014, a novel magnetic vortex-based transistor (MVT) operation was proposed by Kumar *et al.* There, a three-vortex sequence (material Py: diameter = 200 nm; thickness = 40 nm; separation = 50 nm) with polarity combinations (1, -1, -1) was considered an MVT, providing a gain (i.e., the amplification of core gyration amplitude from input to output vortex) of ~ 15 dB similar to an electronic bipolar junction transistor (BJT).²²³ The gain was further optimized by tuning the intervortex separation in an asymmetric three-vortex (AMVT) network.²²⁴ Furthermore, the output from this AMVT was fed into the input of two other AMVTs to perform a successful fan-out operation and nearly equal gains were achieved. Exploiting the asymmetric nature of the energy transfer mechanism by stray field antivortex solitons, a successful fan-in operation with the construction of a tri-state buffer gate was recently reported.²²⁵ Figure 13 shows the simulated magnetostatic stray field distribution of a single vortex, coupled vortices, AMVT, and AMVT-based networks arranged in fan-out and fan-in configurations. Collective modes in a 3D magnonic vortex crystal have also been observed recently.²²⁶

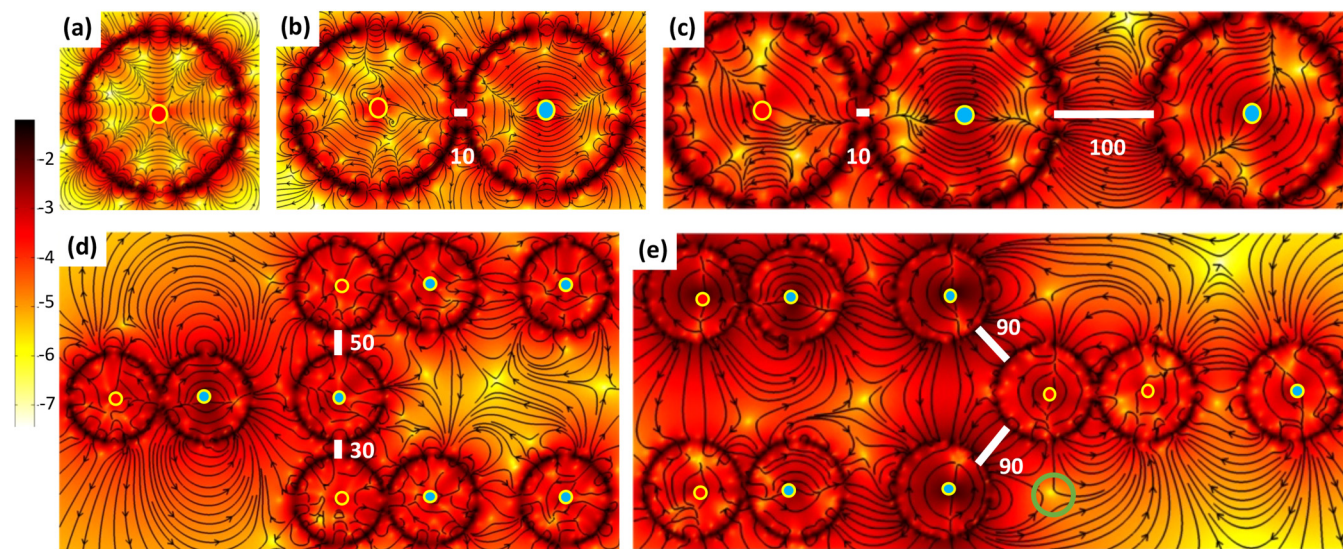


FIG. 13. Magnetic field distributions for (a) single vortex (diameter: 200 nm and thickness: 40 nm), (b) magnetostatically coupled two vortex systems with inter-disk separation = 10 nm, (c) AMVT structure with inter-disk separations 10 nm and 100 nm, (d) fan-out unit, and (e) fan-in unit. The images are obtained after 25 ns of the excitation provided at the input vortices. The excitation field of amplitude 1.5 mT is applied for all the systems. One antivortex in the stray field is marked with a green circle for representation. The color bar is shown at the left side of the figure. The contour coloring is based on the sum of squares of x and y components of the magnetic field and the color bar is in dB. The up and down polarities of the vortices are marked by red and blue dots, respectively. The important physical distances are indicated in numerical figures where the unit is nm.

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3. Magnetic skyrmions

Skyrmion is a topologically protected swirling magnetic texture with a topological charge or winding number ($S = \frac{1}{4\pi} \int \mathbf{m} \cdot (\partial_x \mathbf{m} \times \partial_y \mathbf{m}) dx dy = \pm 1$) that emerges within the bulk non-centrosymmetric compound or nanoscale MMLs with a broken inversion symmetry at the interface. These are found to be very robust under external perturbations. DMI plays a pivotal role in stabilizing the skyrmions. They are of two different types: Bloch and Néel skyrmions. After the first theoretical prediction back in 2001, skyrmions were first observed in bulk non-centrosymmetric MnSi crystals in 2009²²⁷ and Fe monolayers and PdFe bilayers on Ir (111) in 2011.²²⁸ The exploitation of spin-polarized current or pure spin current have been found to be an extremely energy-efficient way to trigger the dynamics of these solitons. The fact that skyrmions can exhibit fast longitudinal motion at an average speed of 100 m/s plays a key role in designing of skyrmion-based racetrack memory and many other magnetic devices.

Theoretical calculations showed various types of dynamical modes of skyrmions, namely, clockwise, counterclockwise, and breathing mode, and a melting of skyrmion crystal when intensely excited.²²⁹ Using microwave transmittance spectroscopy, a nonreciprocal directional dichroism effect via skyrmion resonance modes in a helimagnetic Cu_2OSeO_3 was observed.²³⁰ Furthermore, a broadband FMR study of collective spin excitations (magnetic helix and skyrmion dynamics) in the metallic, semiconducting, and insulating chiral magnets and a precise quantitative modeling across the entire magnetic phase diagrams of the systems quantified the chiral and the critical field energy.²³¹ Büttner *et al.* used time-resolved pump-probe x-ray holography to image gigahertz gyrotropic eigenmode dynamics of a single magnetic bubble whose trajectory confirmed its skyrmion topology. The trajectory further revealed a large inertial mass of the skyrmion due to its topological confinement and the energy associated with its size change.²³² The time-resolved pump-probe soft x-ray imaging technique revealed distinct dynamic excitation states of 100-nm diameter magnetic skyrmions, triggered by current-induced SOTs. The dynamics of magnetic skyrmions was found to be efficiently controlled by the SOT on the nanosecond time scale.²³³ Current-driven dynamics of frustrated skyrmions in a synthetic antiferromagnetic bilayer showed interesting results. While the in-plane current-driven bilayer skyrmion moves in a straight path, the out-of-plane current-driven bilayer skyrmion moves in a circular path with better in-plane current-driven mobility of a bilayer skyrmion than the monolayer one.²³⁴ Very recently, the exciting development of the coherent propagation of spin excitations over a distance exceeding $50 \mu\text{m}$ along skyrmion strings in the chiral-lattice magnet Cu_2OSeO_3 has been reported. The propagation is found to be directionally non-reciprocal, and the degree of non-reciprocity, group velocity, and decay length are strongly dependent on the character of the excitation modes.²³⁵ Figures 12(b) and 12(c) represent simulated skyrmion lattice exhibiting a hexagonal lattice symmetry and the formation of skyrmion tubes along the film thickness in a 90-nm-thick FeGe sample²³⁶ with DMI strength $= 1.58 \times 10^{-3} \text{ J/m}^2$. All other simulation parameters were also taken from Ref. 236.

J. Dynamics of artificial spin ice structures

Artificial spin ice (ASI) structures are engineered materials where ferromagnetic nano-islands are arranged in a predefined

geometry to manifest frustration. In such systems, there is an ambiguity to choose the magnetic ground state because of the degeneracy that gives rise to the “zero-point entropy.”²³⁷ The frustration leads to the creation of magnetic monopole defects connected through the “Dirac string” with the anti-monopole defects. The natural monopoles were first observed in a pyrochlore material ($\text{Ho}_2\text{Ti}_2\text{O}_7$)²³⁸ resembling the frustrated geometry of water ice, but those were difficult to control externally. The first report on an ASI system in 2006²³⁹ revealed experimentally that the monopole states can be stabilized in a square ASI system. This was followed by a series of studies including square and kagome ASI lattices as can be found in the literature.^{240,241} Static characterizations showed that the defects in ASI are very much sensitive to the magnetic history and applied magnetic field, which can influence the SW dynamics. Simulated spin configurations of an exemplary 2D ASI structure at the remanent state is presented in Fig. 12(d), which shows a two-in-two-out configuration. The SW dynamics with changing monopole numbers and string lengths in square ASI was first analytically reported by Gliga *et al.*²⁴² The monopoles modify the frequency of EMs and splitting of the mode signifies the monopole resonance. Later on, researchers observed these dynamics experimentally.^{243–245} Field-dependent hysteresis explored the complex behavior of the low frequency mode at a lower bias magnetic field in square ASI.²⁴³ Two different SW modes were found to coexist at zero field depending on the magnitude of the initial applied field. The occurrence of monopoles manifested a new SW mode in an interconnected kagome ASI system.²⁴⁴ The SW mode intensity increased with the increasing number of monopoles. A systematic study of static and dynamic properties of six different spin ice and anti-spin ice was reported by Zhou *et al.*²⁴⁵ where the sensitivity of SW modes to the aspect ratio of ASI systems was observed.^{246,247} Mode merging was observed with decreasing thickness of nano-islands in square ASI.²⁴⁶ The different shape anisotropies of nano-islands in Y-shaped units of the kagome lattice²⁴⁷ were found to control SW modes’ activation and deactivation depending on the applied magnetic field direction. The structural parameters in ASI clearly influence the wave-vector dispersion. A theoretical calculation of topology-controlled SW dispersion in square ASI was reported by Iacocca *et al.*²⁴⁸ The experimental demonstration of SW dispersion in ASI was reported in the literature.^{249,250} The weak intra-element coupling showed flatter dispersion.²⁴⁹ The opening of channel at 45° angle led to the dispersive SW nature in a square anti-ASI system.²⁵⁰ The extensive study of SW dispersion in the strongly coupled and interconnected ASI may open up new opportunities for constructing ASI-based magnonic devices. To realize the magnetic frustration in 3D, square spin ice geometry with vertically shifted nano-islands,²⁵¹ quasi-tetrahedral geometry of 3D inverse opal-like structures,²⁵² diamond bond-like 3D lattice mimicking the ASI structure²⁵³ have been developed. However, the SW dynamics in 3D ASI systems is yet to be realized.

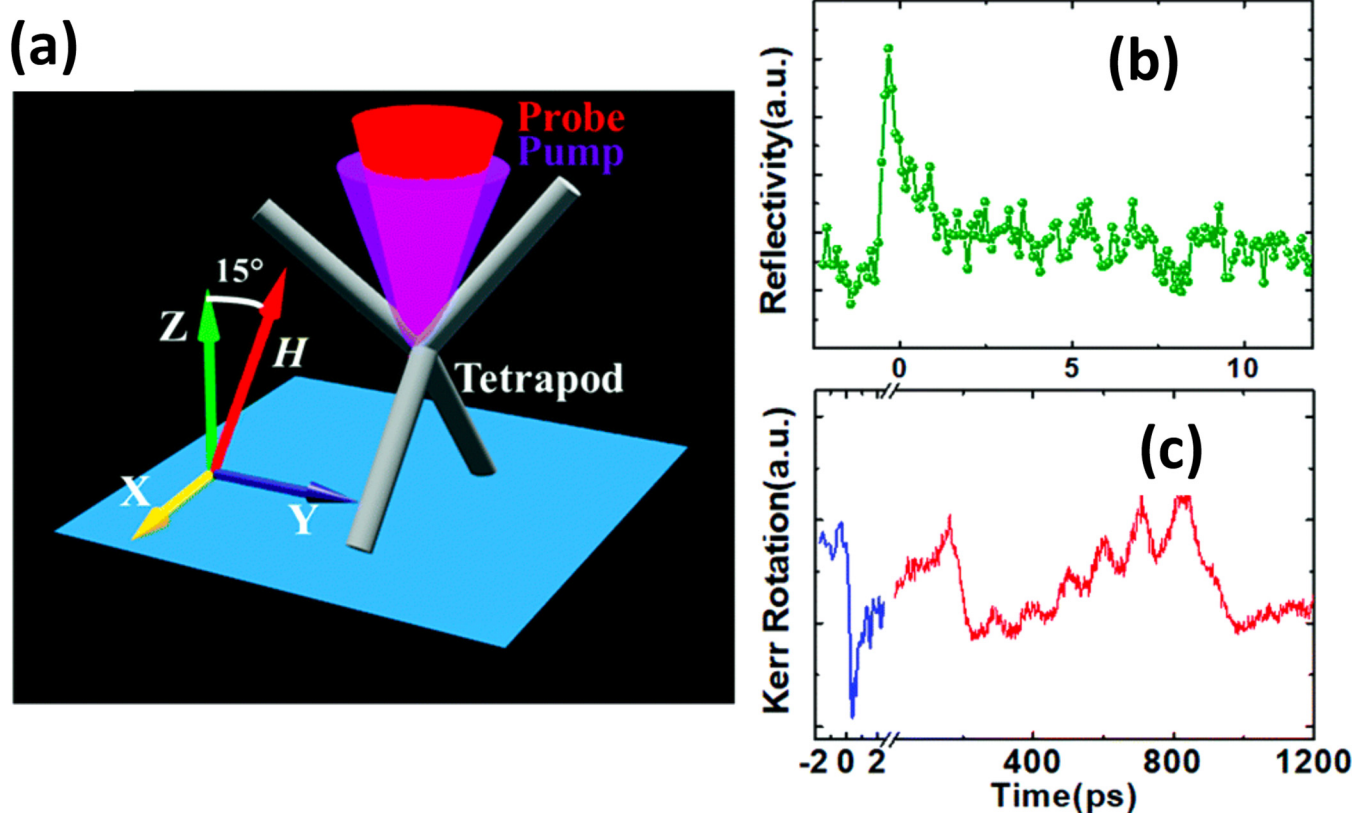
K. Dynamics of 3D magnetic nanostructures

3D nanomagnetism is a new avenue for future magnetism research. The inclusion of a new dimension in a 3D magnetic nanostructure (3D MNS) gives rise to different novel phenomena such as Bloch point,²⁵⁴ curvature induced anisotropy,²⁵⁵ magnetic

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monopoles and their charge conservation in 3D,²⁵⁶ topological structures,²⁵⁷ magnonic band structure,^{258,259} and others. On the other hand, 3D MNSs are the potential candidates for ultrahigh data storage capacity and processing devices,²⁶⁰ building blocks for neuromorphic computer architecture,²⁶¹ magnetic sensors and actuators,²⁶² etc. The main hindrances on the path of 3D nanomagnetism are the fabrication and characterization of 3D MNSs. To this end, some of the 2D fabrication techniques have been promoted to fabricate 3D MNS. TPL is a powerful tool to fabricate the scaffold of a 3D nanostructure. By combining TPL with various deposition techniques, complex 3D MNSs have been fabricated.^{39,253} The main issue with this technique is the accessibility of the full geometry. Focused electron beam induced deposition (FEBID), commonly known as 3D-nanoprinting, is a versatile tool for 3D nanostructure fabrication. Any arbitrary shape can be fabricated with the FEBID technique. The main issue with FEBID is that the purity of the deposited material reduces due to contamination with carbon and oxygen. High-quality nanowires were fabricated using FEBID, and static MOKE signals from them were measured.²⁶³ Chemical procedure has also been used for 3D MNS fabrication.²⁶⁴ Here, the main constraint is that the sample is deposited on a prepatterned template. The x-ray²⁶⁵ and electron²⁶⁶

tomography techniques have been used to map the magnetic induction and magnetization vector field of 3D MNS, respectively. Element specific mapping ability of magnetic circular dichroism with x rays²⁶⁷ and electron beams²⁶⁸ has also been used to study 3D MNSs. Some recent literature studies^{32,269} have made a detailed review of 3D MNS. The magnetization dynamics of 3D MNS is a necessity for understanding of SW characteristics and their applicability in spintronic and magnonic devices. Periodically patterned 3D nanostructures can form a 3D MC. A theoretical study by Mamica *et al.*²⁵⁸ revealed that the magnonic band structure in 3D MCs is extremely sensitive to saturation magnetization, Heisenberg exchange stiffness constant, and anisotropy. An alternative way of realizing 3D MC is in the form of patterned MLs, the SW dynamics of which have been discussed already in Sec. II H. Sahoo *et al.* studied the magnetization dynamics from the junction of a Co tetrapod structure using a TRMOKE microscope (see Fig. 14).²⁷⁰ With the help of micromagnetic simulations, they explained the nature of different SW modes appeared in the experimental SW spectra. However, the experimental study of collective magnetization dynamics of periodically arranged 3D MNS is still missing in the literature. Broad aspects of 3D magnonics have been discussed in Ref. 271.



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FIG. 14. (a) Schematic diagram of the cobalt tetrapod and the experimental geometry. Typical time-resolved (b) reflectivity and (c) Kerr rotation data are shown at $H = 3.92$ kOe. Reproduced with permission from Sahoo *et al.*, *Nanoscale*, **10**, 9981–9986 (2018). Copyright 2018 Royal Society of Chemistry.²⁷⁰

III. OUTLOOK OF EMERGING PHENOMENA AND FUTURE CHALLENGES

The last decade had witnessed a profusion of exciting developments in the field of nanomagnetism as discussed in the previous sections. Nonetheless, those bring along new challenges and hurdles along the path of exploring novel and intricate physical phenomena as well as elegant and demanding applications starting from imaging the ultrafast dynamics of a tiny magnet to the development of an all-magnetic computer. In this section, we will discuss about some of these emerging phenomena and challenges in the field of magnetization dynamics of magnetic nanostructures.

A. Spatiotemporal imaging of magnetization dynamics of magnetic nanostructures

The continuous development of spatiotemporal imaging techniques has made it possible to study femto- and picosecond dynamics of single nanomagnets well below the diffraction limit. However, spatial mapping of the confined modes of individual nanomagnets, collective precessional modes in arrays, short-wavelength magnons, dynamics of spin textures like vortex and skyrmions, SW caustics, bullets, ultrafast spin accumulation in nanomagnets, etc., need further development of both benchtop techniques in individual laboratories and large facility-based techniques. Various probes have been used for these measurements, which include electrical, optical, x-ray, force and, electron microscopies. The electrical techniques are easy to use and commercially viable, but lack both the required spatial and temporal resolution. Development of spatially resolved FMR²⁷² raised some hope to this end due to the exceptional versatility of the FMR techniques, but the progress have been very slow beyond that.²⁷³ TRMOKE offers unprecedented temporal resolution, and with the advent of attosecond laser, the temporal resolution can get even better. The BLS technique has its advantage of measurement of thermal magnons, and even when external excitation is used, no synchronization is needed between the optical probe and the external source. Improvement of numerical aperture of microscope objective such as solid immersion lens²⁷⁴ and lowering the wavelength of the probe laser could take the spatial resolution down to about 200 nm. The development of scanning near-field optical microscopy (SNOM) and its integration with magneto-optical measurements²⁷⁵ ushered hope to this end. However, imaging of localized edge mode in a ferromagnetic element by near-field BLS microscopy²⁷⁶ has drawn criticism.²⁷⁷ Moreover, fiber and aperture based SNOM suffers from the depolarization effect and lack of photon efficiency, as the optical transmission of apertures with sub-wavelength diameter is proportional to $(r/\lambda)^4$ where r and λ are the radius of the aperture and the wavelength of the light, respectively. The role of localized surface plasmons in enhancement of a near-field MOKE signal will be significant here. Further development of near-field atomic force microscopy probe, commercial supply of smaller aperture, and polarization preserving plasmonic antenna, such as bow-tie and cross bow-tie geometry, would be required for routine measurements with sub-100 nm spatial resolution.⁴⁵ The experimental detection of intensity and phase maps of SWs for specific SW modes in nanoscale elements are still open challenges. The techniques that require large scale facilities, such as electron or

neutron scattering with superior spatial resolution, cannot be implemented on a tabletop. Space-, time-, and phase-resolved BLSs can be very powerful in this aspect but require improvement of resolution.²⁷⁸ An important problem is to measure the wave-vector dispersion of SW frequency from nanoscale elements. However, BLS microscopy uses a microscope objective with high numerical aperture, where it is non-trivial to resolve wave-vector information. Nevertheless, using the Mach-Zehnder interferometry, the phase information can be retrieved.

Electron microscopy is a powerful technique, which can provide atomic resolution. Addition of time resolution gives rise to ultrafast electron microscopy (UEM) or dynamic transmission electron microscopy, (DTEM), which can be the strongest tool for the study of ultrafast dynamics in nanomaterials.²⁷⁹ The use of a photoactivated electron source driven by a nanosecond laser gives rise to a few nanosecond time resolution, which can potentially be improved to picosecond and further to femtosecond. Time-resolved two-photon photoemission spectroscopy²⁸⁰ is a powerful tool developed to study electron dynamics in metal and has been used to study nanostructured silver film, for example.²⁸¹ It has the potential for application in magnetic nanostructures with suitable modifications. The development of polarization determination of light emitted from nano objects by means of polarized cathodoluminescence (CL) spectroscopy with an ellipsoidal mirror in a transmission electron microscope²⁸² would be important for the measurement of time-resolved magneto-optical signals using time-resolved electron microscopy.

Polarized x-ray microscopy has revolutionized magnetic imaging. The wavelength of soft x rays is in the nm regime and for hard x rays is in the sub-nm range, promising diffraction-limited spatial resolution to the fundamental magnetic length scales. The magnetic contrast from x rays comes from XMCD for ferromagnetic material and XMLD in case of antiferromagnetic materials. The focusing of x rays are generally done by the Fresnel zone plate (FZP) as well as multilayered Laue lenses, refractive lenses, or zone-doubled diffractive optics. FZPs are concentric diffraction gratings spaced in a way that the diffracted x rays constructively interfere at the desired focus to create an image. The spatial resolution is primarily determined by the outermost zone width of the FZP, which is the thinnest one but with the largest aspect ratio,²⁸³ posing a challenge to the nanofabrication process. The two most popular FZP-based techniques, namely, magnetic full field transmission soft x-ray microscope (MTXM)²⁸⁴ and a scanning transmission soft x-ray microscope (STXM),²⁸⁵ are being widely used to study magnetic DW and vortex dynamics, while their applications to skyrmion dynamics and SW propagation have just been started. Further advantages like element specificity, interfacial sensitivity, and 3D tomographic capabilities with nm resolution can give new directions in nanomagnetism and spintronics, which are fast moving into 3D arrangements of spin structures, non-collinear spin arrangements, and SOTs in ultrathin film heterostructures and MLs. Contrary to the TXM, x-ray photoelectron microscopy (X-PEEM) can provide magnetic information down to a few nm from the sample surface.²⁸⁶ Here, the secondary electrons generated in the primary absorption process are released by a potential difference applied between the surface and the first electron lens in the electron microscopy column. This limits the probing depth to the

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escape depth of electrons, i.e., a few nm. Resonant soft x-ray ptychography offers to retrieve real space image with 10-nm resolution.²⁸⁷ In all these techniques successful integration with a femtosecond laser will lead to unprecedented spatiotemporal resolution. A soft x-ray laser with a high harmonic generation has been proven to be a viable route for strongly enhanced coherent extreme ultraviolet radiation with femtosecond pulse duration associated with a photon flux of 3×10^{11} at 32.8 nm.²⁸⁸ Such a high flux is sufficient for single-shot imaging of nano objects. Apart from time-resolved direct imaging of spin dynamics, x-ray photo correlation spectroscopy will provide a complementary access into the dynamics of spin systems in the frequency domain.²⁸⁹

Among other promising techniques, SPSTM allows us to image spin textures at nearly atomic resolution and it has recently been extended to the time domain to study fast electron spin relaxation times occurring in the ns regime.²⁹⁰ Lensless imaging of magnetic nanostructure using x-ray spectro-holography is a form of Fourier transform holography, which is transferable to a wide variety of specimens, scalable to diffraction-limited resolution, and is well suited for ultrafast single-shot imaging with coherent x-ray free-electron laser sources.²⁹¹ MRFM bridged the gap between MRI and SPM.²⁹² It operates on the principle of probe beam modulation reflected from a scanning tip with about 700 nm diameter sensing the magnetic field from the sample. On the other hand, a nano-magnetic tip attached to MRFM facilitates scanning with sub-nm spatial resolution, and in the near future, it can be employed for 3D imaging.²⁹³ We hope that further development can lead this technique to be established as a reliable microscopy in the FMR mode for studying the dynamics of nanomagnets. Nitrogen vacancy (NV) center is an atomic sized point defect in the diamond crystal providing high spatial resolution and also possessing remarkable magnetic and quantum properties with high-field sensitivity and excellent spatial coherence. NV center magnetometry²⁹⁴ is another powerful nano-magnetometric tool due to its properties and can be useful for imaging nanoscale spin dynamics, if coupled with high frequency.

B. Arrays of nanostructures with complex geometry

Like all other crystals, MC also enjoys the benefits of introducing geometrical complexity to achieve extremely rich and complex SW dynamics and magnonic band structures. This includes the introduction of varying lattice symmetry as well as complex basis structures. When added to the inherent magnetic anisotropy, non-uniform internal magnetic field, interfacial effects, etc., these can lead to almost unlimited possibilities for MCs, which make them unique among its counterparts from other artificial crystals. In Sec. II G, existing reports on SW dynamics in various forms of complex 2D arrays of nanostructures such as octagonal lattice, defective honeycomb lattice, binary nanostructures, rings, and anti-rings have been discussed. Composite antidot structures with continuously varying lattice constant^{142,152} have also been studied scarcely. Although some attempts have been made to vary the lattice symmetry as well as the basis structures,^{295,296} those form only a negligible fraction of the overall possible combination of such structures and phenomena. Therefore, systematic variation of various geometric parameters for tuning

the SW dynamics and magnonic band structures will be extensively studied in the coming years too. An example is given in Fig. 15, where triangular antidots are arranged in a honeycomb lattice with varying lattice constant. The combination of an asymmetric basis and lower lattice symmetry shows magnonic spectra, which shows excellent tunability with lattice constant. Along this line, if we introduce binary or ternary basis with antidots with different size, shape, or separation, we can further enrich the SW spectra and mode structures. They can introduce new bands or (semi)localized states in the magnonic band structure, besides modulating the MBG very efficiently. In photonics, a less symmetric structure has been found to give better self-collimation²⁹⁷ and slight modulation of the lattice symmetry or basis structure can give rise to new phenomena useful in different applications. The simulated equilibrium magnetic configurations, SW spectra and SW power maps of two exemplary complex basis nanostructures, are shown in Fig. 16.

The SW mode profiles show some complex characters that are not observed in usual basis structures as described in Sec. II G. Further complexity can be added to the 2D arrays by inclusion of spatial nonuniformity of the magnetic properties within the individual nanomagnet. This can be termed as “Janus nanomagnet” analogous to Janus NPs having a symmetric shape but asymmetric surface properties²⁹⁸ [see Fig. 17(a)]. Such structural engineering may require complicated fabrication processes such as multistep lithography. However, the powerful exchange coupling within the nanomagnet itself made of two different materials can introduce a stark variation in the SW spectra and will be worth exploring in the near future.

C. Arrays of nanostructures with quasiperiodicity and defects

Quasicrystals possess long-range ordering without any periodicity and their diffraction patterns exhibit symmetry forbidden by crystallographic restrictions. Quasicrystals have been extensively studied in photonics and phononics for a long time but have only recently been introduced in nanomagnetism in the form of MQC. Appearance of a passband,²⁹⁹ allowed bulk band in place of bandgaps,³⁰⁰ modulation of magnonic gaps,³⁰¹ damping of collective SW modes,³⁰² etc., have been theoretically investigated in 1D bi-component MQCs with Fibonacci sequences. Recently, Hussain *et al.* theoretically demonstrated SW dynamics in nanowire with vertically developed multilayer designed according to a quasiperiodic Fibonacci sequence.³⁰³ Grisin *et al.* fabricated Fibonacci type structures consisting of grooves and crests made in YIG.³⁰⁴ Apart from multiple forbidden gaps, the appearance of relatively narrow passbands for the magnetostatic surface SW (MSSW) mode in their measurements led to the development of a ring resonator. Bhat and Grundler studied MQCs made of Py interconnected nanobars arranged in Penrose P2 and P3 and Ammann tiling, which exhibited distinct sets of FMR modes with characteristic angular dependencies (eightfold and tenfold rotational magnetic symmetry) for applied in-plane magnetic fields.³⁰⁵ The same research group later demonstrated that the tenfold rotational symmetry of aperiodic nanohole arrangements results in multiplexed magnonic nanochannels, inside a so-called Conway worm.³⁰⁶ Choudhury *et al.* observed characteristic magnonic

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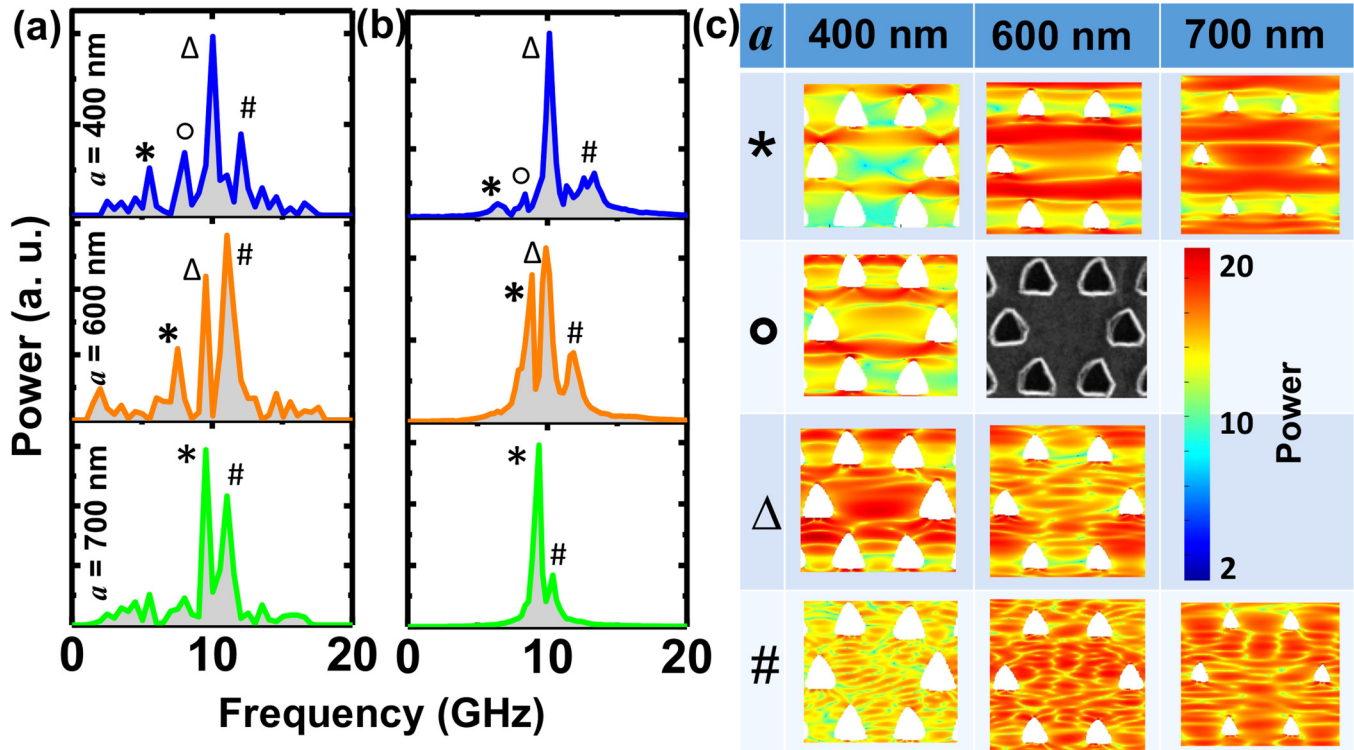


FIG. 15. (a) Experimental and (b) simulated SW power spectra of a triangular shaped antidot lattice having honeycomb symmetry with varying lattice constants (a). (c) Simulated power profiles of the observed SW modes. The color map used for the power profiles and the SEM image of the lattice with $a = 400$ nm are shown inside the figure. The number of modes and the overall bandwidth of the spectra reduce with the increase in lattice constant. The lateral width and power of the extended mode through the channels between the antidots increase, and the quantized mode also becomes more prominent with the increase in a .

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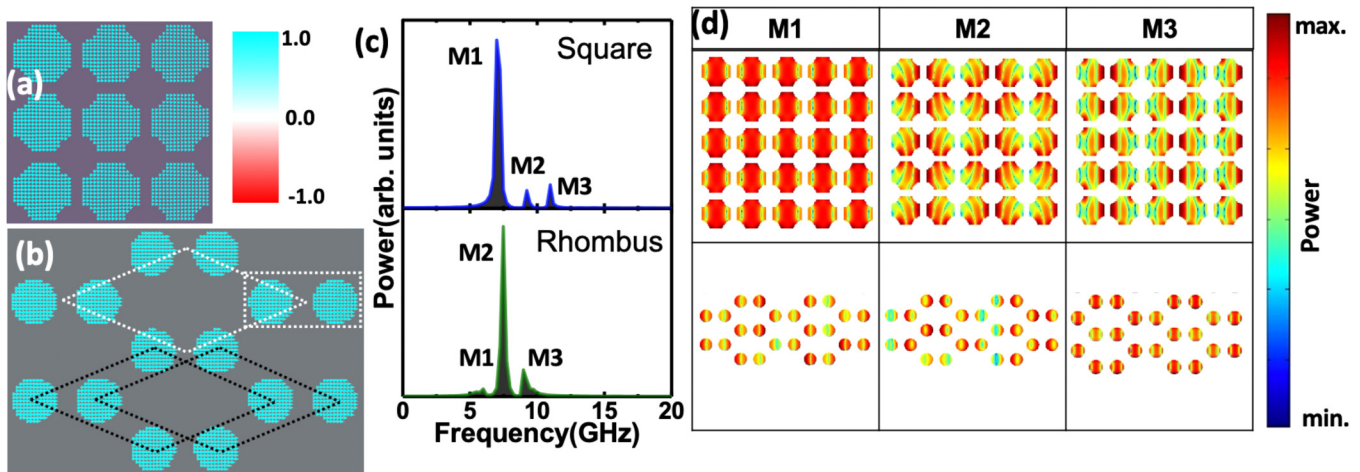
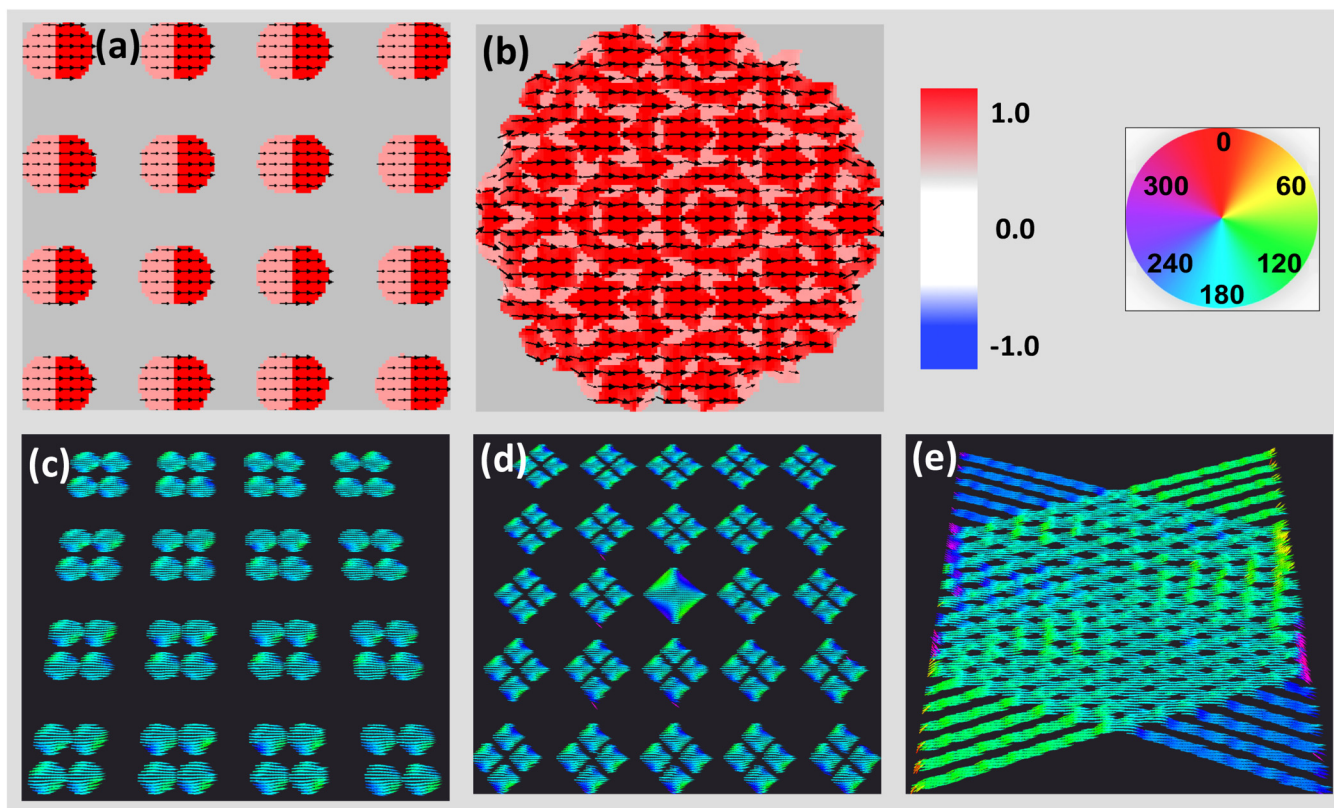


FIG. 16. Simulated static magnetization configurations of two different complex basis nanomagnet arrays at a bias magnetic field of 1 kOe: (a) square lattice with complex basis of length 125 nm and lattice constant 150 nm and (b) two-atom basis rhombus lattice with dot radius of 100 nm, interdot separation in the basis of 50 nm, and lattice constant of 300 nm (highlighted by the white dashed line) or superposition of two linearly shifted rhombus lattices (highlighted by the black dashed line). (c) Simulated SW spectra for square and rhombus lattices at a bias magnetic field 1 kOe. (d) The corresponding simulated SW power profiles are shown. The color bars are presented besides respective figures.



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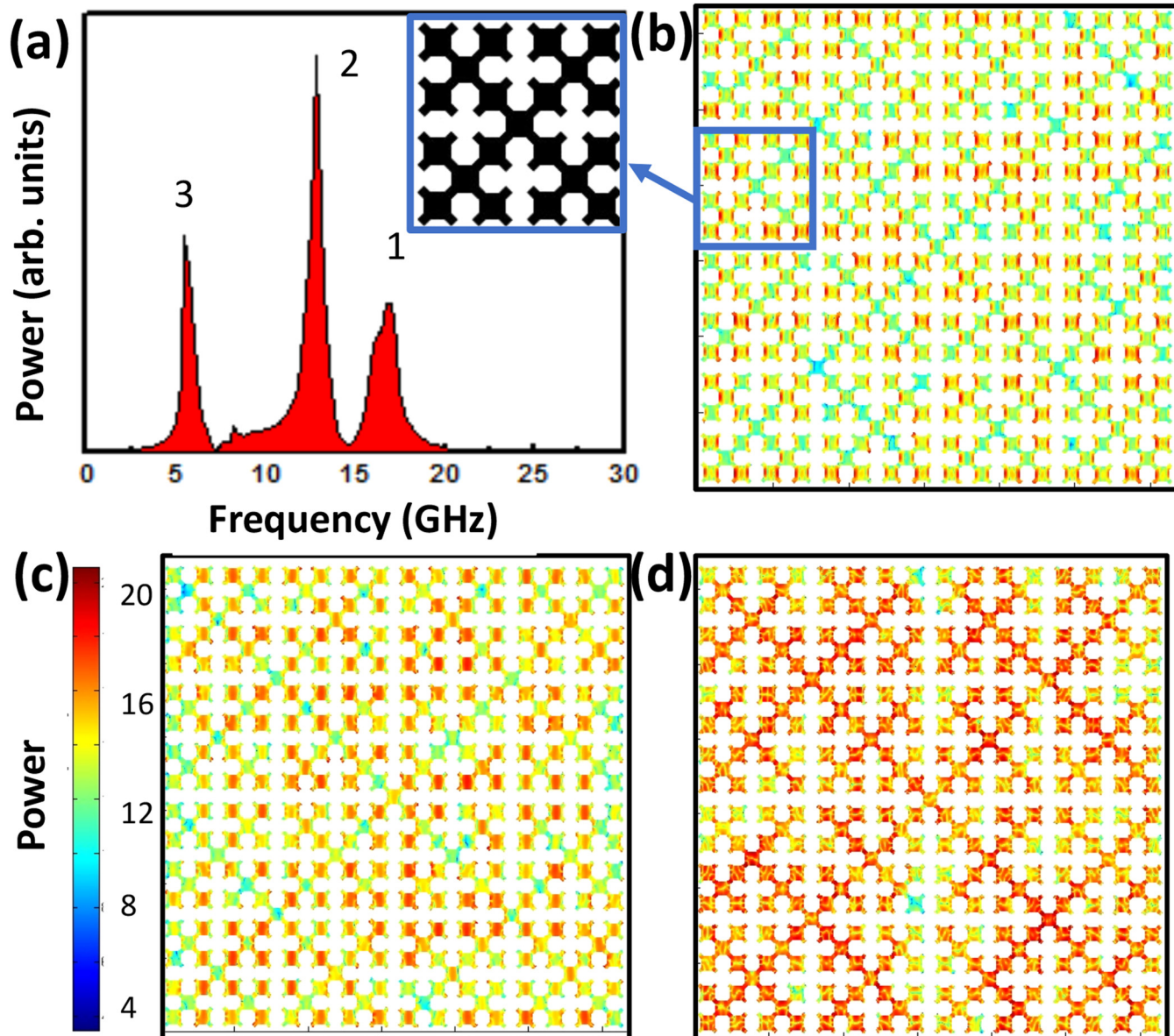
FIG. 17. Ground state spin configurations for (a) bi-component MC with Janus nanomagnets as basis, (b) bi-component MQC with the Penrose tiling arrangement, (c) MC resembling the symmetrical Delone set, (d) 2D array of diamond-shaped nanodots with a point defect, and (e) cross-weaved nanostripes: structural defect arising due to overlapping of nanostripes with moderate tilting. Color bars are presented at the top-right corner of the figure.

spectra and an eightfold rotational symmetry in a Py antidot lattice with octagonal symmetry.¹⁵⁵ Lisiecki *et al.* observed a remarkable dynamic coupling between propagating SWs through Py nanowires of two different widths arranged in a 1D Fibonacci sequence using STXM measurement.^{307,308} This field, however, remained wide open with new opportunities. For example, a crystallographic structure constrained by only two simple physical properties, “discreteness” and “homogeneity,” turns into Delone sets.³⁰⁹ Magnonic analog of these sets can be easily realized to explore intriguing SW dynamics in this unconventional structure. Another interesting polytope of MC can be “Voronoi cell”-like nanostructures, which retains the lattice symmetry but offers more independent choice of the basis.³⁰⁹ Figure 17 shows the ground state spin configurations of some of these structures. Construction of numerous types of bi-component or multi-component MQCs is possible with aperiodic geometries, such as different variants of Penrose tiling, oblique tiling, and Ammann–Beenker tiling,^{309,310} which may offer unprecedented tunability of the magnonic band structure besides a stark modulation of SW group velocity due to the lack of translational symmetry.

MCs with “fractal” geometries can now be included as a new member of the family of artificial crystals offering intriguing high-

frequency dynamics. In 1919, German topologist F. Hausdorff introduced the idea of fractional dimension, and in 1975, Mandelbrot assigned the name “fractal” to a particular class of curves.³¹⁰ Those are the curves whose paths are monodimensional; however, at the limit they occupy a 2D area. Dai *et al.* have recently reported a micromagnetic simulation study on magnetization reversal and magnetic spectra in Sierpinski triangles.³¹¹ However, experimental results are still lacking in this field. An exemplary Sierpinski’s closed peano curve in the form of a MC is shown in Fig. 18. The simulated SW spectrum spreads over a broad range between 5 and 17 GHz for moderate value of bias magnetic field. The highest frequency mode exhibits mixed azimuthal quantization within the elements and a “Fractal” like spatial distribution over the whole array. Such structures are expected to provide enormously rich SW spectra with a broad range of control parameters and exotic SW propagation properties.

The tunability of magnonic bands in MCs is the key for efficient transfer and process of information in magnonics. Introduction or intrinsic occurrence of defects or disorder reforms the local magnetic properties including magnetic potential. This may drastically reconstruct the magnonic band structure by introducing new SW modes, phase shifts, and minibands and adjusting



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FIG. 18. SW dynamics of Sierpinski's closed peano curve is simulated in the form of a MC with the material as Py and array size of $3 \times 3 \mu\text{m}^2$ discretized into $5 \times 5 \times 20 \text{ nm}^3$ cells. (a) Frequency spectra for the "fractal" structure at a bias magnetic field of 1 kOe. Mode numbers are indicated in numeric figures. A portion of the structure is shown at the inset. SW power profiles are shown for (b) mode 3, (c) mode 2 and (d) mode 1. The corresponding color bar is shown at the left of the figure.

MBG and SW group velocities due to the breaking of translational symmetry. Kruglyak *et al.* numerically showed that introduction of an isolated defect layer in a 1D MC leads to the appearance of several localized defect modes within the bandgaps.³¹² Ding *et al.* experimentally studied the correlation between FMR response (singlet or doublet) and the degree of disorder in a 1D array of a dipolar-coupled Py nanowire.³¹³ Such defect modes are often

found to be dispersionless.³¹⁴ Point defects with symmetrical shapes and moderate filling fraction embedded within 2D MC have generated multiple defects modes.³¹⁵ It can be expected that the defect with inferior or no lines of symmetry (such as rectangle, triangle, diamond, cross, and parallelogram) and superior filling fraction may offer greater tunability of magnonic bands. Morozova *et al.* showed that the length of the magnetization localization

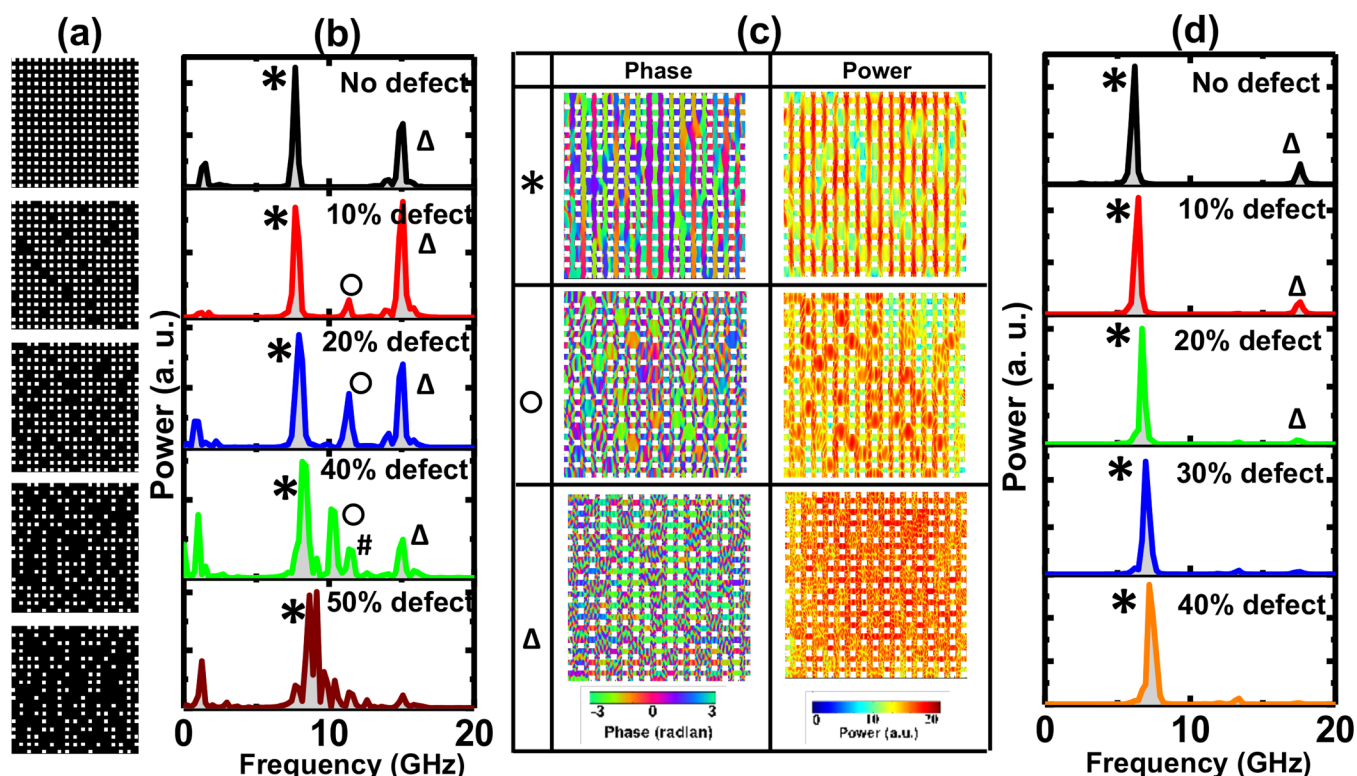


FIG. 19. (a) Images of ADLs with defects having a hole diameter of 100 nm and a separation of 100 nm. (b) Simulated SW spectra of the corresponding ADLs with defects. (c) Simulated SW phase and power maps of the same ADL with 20% defect. (d) Simulated SW spectra of the ADLs with defects having a hole diameter of 25 nm and a separation of 50 nm.

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region depends on the line defect width, which can be used for developing SW logic and multiplexing blocks.³¹⁶ The edge roughness and shape deformation that occurred due to the limitation of nanofabrication primarily affects the edge modes and localized SW modes.¹⁵⁴ Magnonic spectra of Co antidot lattice with hexagonal symmetry was found to be quite robust to the introduction of random defect.¹⁵² Further case simulations on square antidots (100 nm width) arranged on a square lattice (lattice constant = 200 nm) showed a sharp variation in SW spectra with the emergence and subsequent splitting of defect modes confined within the defect regions (see Fig. 19). Reduction of antidot size and lattice constant, when the SW transforms into the dipole-exchange mode, caused a significant variation in the pattern of defect density dependence, where only a slight blueshift in an extended mode and gradual disappearance of quantized mode occur. Defects in MC can play a significant role in magnonic bands analogous to electronic bands in semiconducting crystals and extensive research to this end is expected in the coming years.

D. Spin-orbit coupling in nanoscale spin dynamics

The SOC effect has emerged as a very rich and elegant effect in nanomagnetism and spintronics.³¹⁷ It enhances significantly

with reduced dimensions due to the broken inversion symmetry at the surface or interface to produce spin-split dispersion (Rashba SOC), chiral spin texture (IDMI), spin-polarized surface states with topological properties (topological insulators), and spin-momentum locking, among others. Various other intrinsic and extrinsic SOC-based properties, such as SHE, spin pumping, and PMA, exist, which have made strong inroads into present or future technologies based on spin-charge conversion, stabilization of skyrmions, STNO, SHNO, etc. Many of these strongly affect the spin dynamics starting from ultrafast demagnetization, relaxation phenomena, SW propagation, and damping. Hence, it is imperative to extend the application of single or multiple of these properties to our advantage in excitation, control, and detection of the dynamics of nanoscale spin textures and patterned nanomagnet arrays. For example, the simultaneous existence of PMA and DMI in a patterned 2D nanomagnet array can help in stabilizing topological magnetic objects like skyrmions, bubbles, or merons and in more efficient control of their dynamics. Development of 1D and 2D MCs on ferromagnet/non-magnet heterostructures along with IDMI will lead to novel magnonic band structures³¹⁸ and evolution of new bands due to the asymmetric SW dispersion in the presence of IDMI (see Fig. 20). The behavior of SW modes with increasing DMI strength is recently demonstrated in nanodots.³¹⁹ The magnitude of mode splitting is

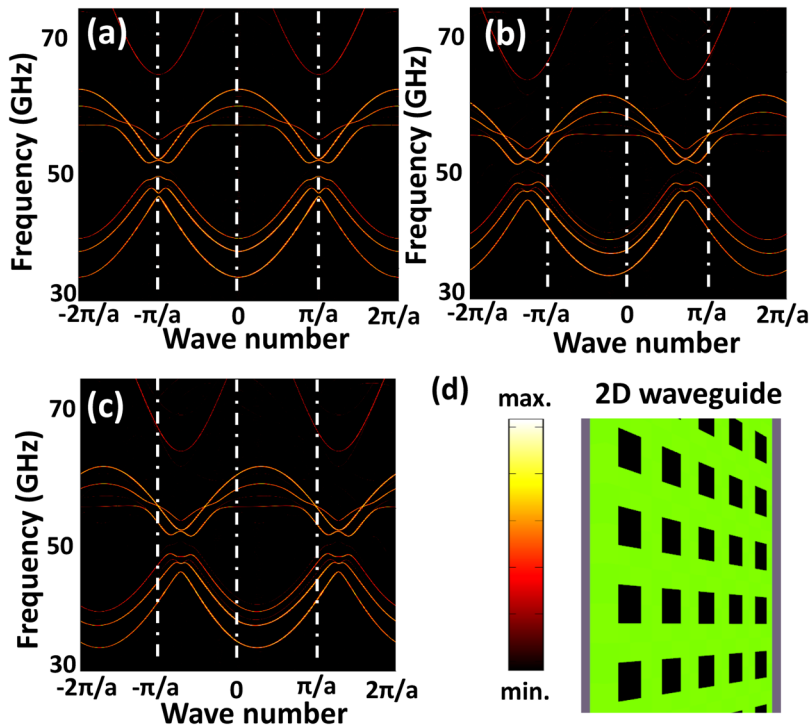


FIG. 20. Simulated SW dispersion curves of a quasi-2D antidot waveguide in the DE geometry in the presence of a bias magnetic field = 1.01 T with DMI (D) values of (a) $D=0$, (b) $D=1 \times 10^{-3} \text{ J/m}^2$, and (c) $D=-1 \times 10^{-3} \text{ J/m}^2$. (d) A schematic of antidot waveguide and color bar of SW amplitude are presented at the bottom right corner. Simulation parameters are waveguide dimension: $12 \mu\text{m} \times 120 \text{ nm} \times 3 \text{ nm}$; cell size: $6 \times 6 \times 3 \text{ nm}^3$; hole size: 12 nm; lattice constant: 24 nm; M_s : 800 emu/cc; and A_{ex} : $13 \times 10^{-12} \text{ J/m}$.

found to be larger for circular dots compared to similar sized square dots (shown in Fig. 21). The azimuthal modes showed mode splitting with increasing DMI strength, whereas slight modification in the frequency is observed for radial modes. For square dots, this

difference between azimuthal and radial modes is not clear, as a slight change in the power profiles is observed. An asymmetric mode profile is observed for the highest frequency mode of square dots [Fig. 21(b)].

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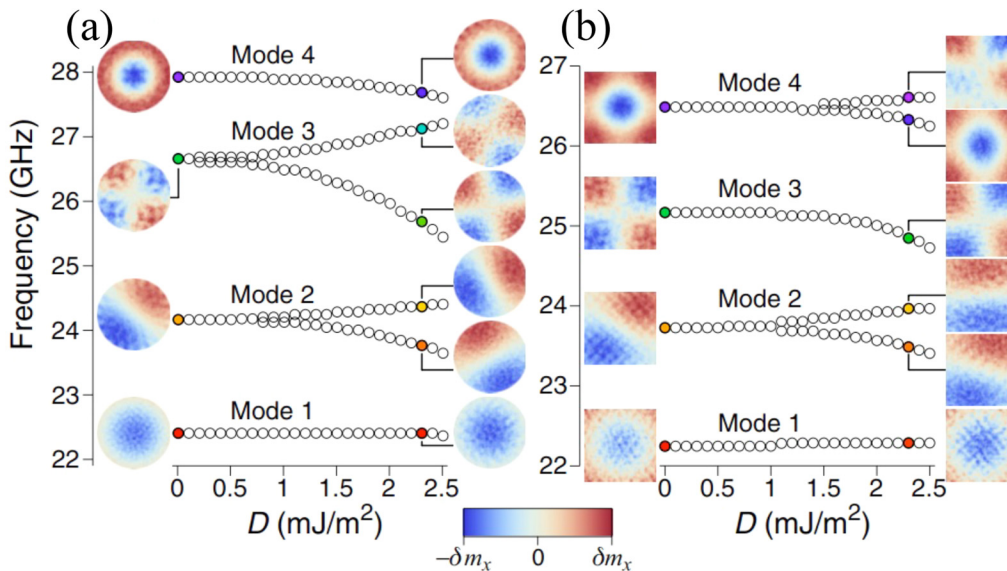


FIG. 21. Spin wave mode frequency variation as a function DMI constant (D) for (a) 100-nm-diameter circular dot and (b) 100-nm-width square dot. Selected profiles of the modes are shown for different values of D . Reproduced with permission from Garcia-Sanchez *et al.*, Phys. Rev. B **89**, 224408 (2014). Copyright 2014 American Physical Society.³¹⁹

Pure spin current-driven and controlled coherent SW in nanomagnet arrays would also be an engrossing research area. Topological insulators³²⁰ with extraordinary properties like ambipolar surface states, spin-momentum locking, protection from backscattering between states of opposite momenta with opposite spins and ensuing reduced energy dissipation, and high spin-charge conversion will lead to exotic properties and devices such as low-power electronics like topological p-n junctions,³²¹ SOT-MRAM, nano-batteries, topologically protected skyrmion states, abacus-type applications, etc. Further magnetic doping or proximity of topological insulators may break time-reversal symmetry, leading to a gap at the Dirac point and a reorientation of the low-energy spin texture, and investigation of quantum AHE³²² would be exciting prospects in this field. In graphene, SOC can be enhanced due to proximity and hybridization with an adjacent magnetic layer both due to intrinsic Rashba SOC and extrinsic defect mediated SOC. In the heterostructure of graphene with another 2D material such as transition metal dichalcogenides with larger intrinsic SOC³²³ or a topological insulator,³²⁴ the prospects of spin-charge conversion associated with larger mobility, conductivity, and longer spin lifetime of graphene would be very exciting.

Development of a hardware network that can be successfully trained by a set of STNOs to recognize spoken letters by tuning the frequency and amplitude according to the real-time learning rule with excellent scalability^{261,325} promises the construction of future artificial neural networks. A practical STNO-array based device will probably require current from a single source distributed to each oscillator through parallel or series connections. These devices will find applications as sources in nanoscale phase-locked arrays,³²⁶ which could be used in wireless chip-to-chip or intra-chip communications. SHNOs can be more advantageous due to the easy integration on Si substrates and the exploitation of pure spin current with better energy efficiency.

E. Emerging phenomena in quantum hybrid systems

Hybrid systems have rapidly emerged as strong candidates for quantum information processing³²⁷ where quantum states are coherently transferred between two media using different carriers such as superconducting qubits, spin ensembles, and optical and microwave photons and phonons. For example, microwave photons in high-quality cavities are very efficient for communicating spin information because of their long coherence length, whereas other quasiparticles such as magnon and phonons can also generate indirect interactions between tiny magnets over long distances. In the following, we discuss the recent progress and future directions in this field.

1. Magnon-phonon coupling

The coupling between magnonic and phononic degrees of freedom in the radio frequency regime was theoretically predicated long back,³²⁸ but it has attained great momentum more recently. Over the last decade, SAW in GHz regime have been implanted to excite or manipulate the SW in magnetic thin films^{329,330} and nanostructures^{80,82,331} through magnetoelastic (ME) interactions. SAW-driven ferromagnetic resonance have been studied in ferromagnetic films^{329,330} and single nanomagnets.^{323,333} In the pursuit

of understanding the complex interaction between phonons and magnons, Bas *et al.*³³⁴ studied the effects of material parameters, number of pairs of interdigital transducers, the ferromagnetic thin film deposition technique, and the presence of the Au capping layer on the ferromagnetic thin film on the SAW-driven FMR results. Yang *et al.* claimed that by investigating the field-swept dynamics of isolated Ni nanomagnets at varying SAW frequencies, the intrinsic Gilbert damping of nanostructured magnetic materials can be accurately determined.³³² The SW frequency,⁸² damping,³³⁵ and field dispersion,²³¹ can be tuned by ME coupling. A SAW-modified rich SW texture has been observed in a magnetostrictive single nanomagnet.⁸² Strong coupling between magnonic and phononic degrees of freedom have been observed in a single nanomagnet.⁸⁰ Recently, SWs with a large amplitude and a long traveling distance have been successfully generated in a Ni thin film by SAW.³³⁶ An enhancement of the amplitude of magnetic oscillation has been reported in single nanomagnets using focused ME excitation as compared to the conventional optical excitation.³³³ Selective excitation of SW modes has been demonstrated in a MC formed by Ni nanowires deposited on glass substrate using optically pumped SAWs. An unusual dependence of the ME coupling was observed, as the applied magnetic field was angle- and field-tuned relative to the wave vector of the magnetization modulation, due to the emergence of spatially inhomogeneous SW modes.^{337,338} SAW-driven dynamic MC generation based on Bragg scattering and Doppler shift has been demonstrated.³³⁹ On the other hand, strain controlled IDMI and skyrmions,³⁴⁰ elastically driven spin pumping³⁴¹ phonon mediated inverse Edelstein effect,³⁴² the mechanism of phonon-magnon coupling such as spin-rotation coupling,³⁴³ and the role of time-reversal symmetry³⁴⁴ have stirred huge interest in this field. Magnon-phonon coupling plays a key role in the spin Seebeck effect, where modification of the magnon distribution function by phonons results in a pure spin current injection from a ferromagnet to nonmagnet.³⁴⁵ In many of these phenomena, size reduction and geometric parameters will play key roles in exploring new and superior functionalities. The condensation of mixed magnon-phonon state and magnon-phonon bottleneck accumulation phenomenon³⁴⁶ are extremely rich and fundamental phenomena. Moreover, the potential of its occurrence in any multicomponent gas mixture of interacting quasiparticles having different scattering amplitudes promises the exploration of new systems in near future.

2. Magnon-photon coupling

Magnon-photon coupling or cavity magnonics has versatile applications such as hybrid quantum systems,³⁴⁷ coherent conversion between microwave and optical frequencies,³⁴⁸ quantum electrodynamics,³⁴⁹ and direct detection of dark matter.³⁵⁰ In 2014, Tabuchi *et al.* observed hybridization between ferromagnetic magnon and microwave photon in the quantum limit,³⁴⁹ thus leading the way to magnon-photon coupling. In 2015, Viennot *et al.* coherently hybridized the individual spin and charge states of a double quantum dot while preserving spin coherence up to the megahertz range at the single-spin level in a superconducting resonator.³⁵¹ To overcome the issue of limited lifetime of magnon-polariton, Zhang *et al.* created stationary magnon-polariton states

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by a dynamical balance between pumping and losses with non-Hermitian spectral degeneracies.³⁵² However, these works are predominantly based on YIG, which is non-trivial to integrate on chip and suffered from the lack of proximity between magnetic material and microwave resonator. Li *et al.* overcame this problem by fabricating an all-on-chip magnon–photon hybrid circuit with a Py thin film device directly fabricated on top of a coplanar superconductor circuit³⁵³ and obtained a coupling strength of 0.152 GHz and a cooperativity of 68. In another back-to-back article, Hou *et al.* used lithographically defined superconducting resonators to demonstrate high cooperativity between a resonator mode and Kittel mode in a Py wire with number of spins $\sim 10^{13}$. This was soon followed by another article by Wang *et al.* who showed the cooperative effect of coherent and dissipative magnon–photon couplings in an open cavity magnonic system. Their system leads to nonreciprocity, flexible controllability, and unidirectional invisibility for microwave propagation.³⁵⁴ Overall, the field of cavity magnonics is heating up, but several problems remained open. Two most important issues are downscaling of the magnetic system (number of spins) while retaining high enough cooperativity and identification and quantification of coherent and dissipative coupling origin, strength, and their competition, which will surely receive intense interest in the next few years.

3. Magnon–magnon coupling

Strong magnon–magnon coupling has set-off very recently and is still in its nascent stage. The initial study of excitation of exchange-coupled perpendicular standing SW (PSSW) in YIG from the FMR frequency of an adjacent Co layer by using strong coupling and avoided crossing has been demonstrated in 2018.³⁵⁵ Similar avoided crossing, a signature of strong coupling, was observed between the PSSW modes of the YIG film and FMR mode of the CoFeB film³⁵⁶ and that of Ni nanowires³⁵⁷ at the same time. The latter work is important as it is a way forward to overcome the issue of “coupling strength,” which can be enhanced by square root of the number of spins (N) to overcome the weaker coupling strength (g_0) between individual spins and the microwave field, i.e., $g = g_0\sqrt{N}$.³⁴⁹ Subsequently, avoided crossing for interlayer coupled atoms in the 2D antiferromagnet CrCl_3 ³⁵⁸ has been demonstrated. More recently, coherent spin pumping and large avoided crossing in YIG/Py bilayer with reduced layer thickness³⁵⁹ and magnon–magnon coupling in interlayer exchange-coupled synthetic antiferromagnets of FeCoB/Ru/FeCoB layers³⁶⁰ have been achieved. However, strong coupling between nanoscale metallic ferromagnetic elements is essential for the on-chip integration of hybrid systems. To this end, a breakthrough was obtained very recently, when a very strong magnon–magnon coupling between Py nanocross elements at moderate microwave power has been achieved where two anticrossings between magnon modes have been observed.¹³¹ Further numerical simulations demonstrated strong coupling between EM and CM in a single nanomagnet.³⁶¹ The last two works are expected to open Pandora’s box in the dynamics of nanomagnetic systems where intra- and inter-element interactions can be tailored by various material and geometric parameters of nanomagnets to engineer the strong magnon–magnon coupling.

F. Emergence of nanomagnet antenna

Antennas act as an essential component in smart phones, tablets, biologically implanted devices, radio frequency identification systems, radars, etc. They are an array of conductors that can generate the oscillating electric field and magnetic field through oscillating electric currents, which are required to ensure a high radiation altitude. Conventional antennas rely on electromagnetic wave resonance that leads to antenna sizes comparable to the wavelength λ . Further miniaturization of the antenna size has been one of the fundamental challenges for years, as antennas substantially smaller than the wavelength of an electromagnetic wave exhibit decreased radiation resistance, large electrical Q-factors, and decreased radiation efficiency due to additional losses such as Ohmic dissipation.^{362,363} These limitations have made it extremely challenging to achieve miniaturized compact antennas at very high frequencies (VHF, 30–300 MHz) and ultrahigh frequencies (UHF, 0.3–3 GHz), putting severe obstacles on the wireless communication systems. Thus, new antenna concepts need to be investigated with mechanisms for the miniaturization of antenna size.

An alternative avenue to reduce antenna size is to excite an electromagnetic antenna at acoustic resonance instead of electromagnetic resonance. Strong strain-mediated magnetoelectric coupling in ferromagnetic/piezoelectric heterostructures enables efficient energy transfer between magnetism and electricity.³⁶⁴ This concept has recently been adopted by Nan *et al.* to design acoustically actuated nanomechanical magnetoelectric antennas with such a ferromagnetic/piezoelectric thin film heterostructure, which receive and transmit electromagnetic waves through the magnetoelectric effect at their acoustic resonance frequencies.³⁶⁵ Since the acoustic wave velocity is roughly five orders of magnitude smaller than the velocity of light, consequently, the acoustic wavelength is five orders of magnitude smaller than the electromagnetic wavelength at the same frequency. Hence, the radiation efficiency (A/λ^2 , where A is the emitting area and λ is the emitted wavelength) of such antennas are several orders of magnitude larger than the electromagnetic antenna, which allows a drastic miniaturization of the communication systems. A few reports on antenna miniaturization mechanisms using this concept have been made.^{366,367} Another antenna miniaturization concept using unique fractal geometry has been proposed.³⁶⁸ More recently, an antenna implemented with a closely packed array of magnetostrictive nanomagnets deposited on a piezoelectric substrate has been developed,³⁶⁹ where a SAW launched on the substrate with an alternating electrical voltage can periodically strain the nanomagnets and rotate their magnetizations owing to the Villari effect [Fig. 22(a)]. The oscillating magnetizations of the nanomagnets emit electromagnetic waves at the frequency of the applied SAW. Clearly, such miniaturized antennas can drastically enhance antenna gain at a small size, allowing dramatic downscaling. This is expected to have great impacts on future communication systems. However, tuning the geometrical and structural parameters and excitation methods can play important roles in exploring better functionalities of such nanomagnet antennas. Thorough experimental and theoretical investigations are thus highly demanded in the future to overcome several open challenges of miniaturized nanomagnet antennas with better prospects.

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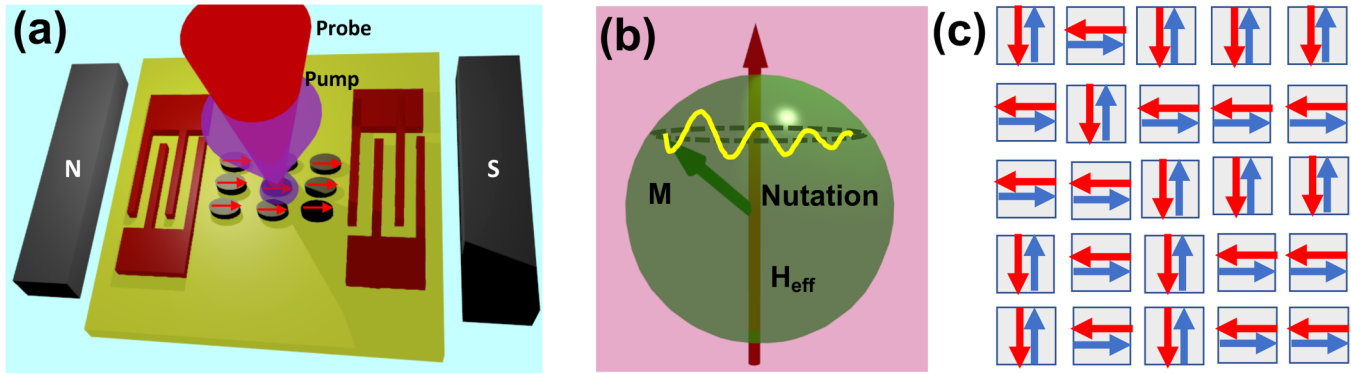


FIG. 22. (a) Schematic of the optical pump–probe technique with a nanomagnet array fabricated in between two interdigitated switches in the presence of magnetic poles. (b) Schematic of nutation dynamics of a nanomagnet. (c) Array of antiferromagnetic nanomagnets.

G. Nutation dynamics in nanomagnets

Magnetization dynamics has similarity with gyroscope dynamics. Hence, it is expected to observe a high-frequency motion along with the precessional dynamics in ferromagnetic nanostructures commonly known as “nutation.” The familiar classical analog is a spinning top. If an external field suddenly transfers angular momentum, the moments get diverted from the angular momentum axis and start to nutate on a fs time scale, followed by the ps precession [Fig. 22(b)]. This is a consequence of the Heisenberg exchange interaction. The former effect is non-trivial to detect experimentally for having shorter amplitude and time scale. It is worth mentioning that nutation dynamics has been reported in various other systems such as superconducting Josephson junction³⁷⁰ and matter-wave vortices³⁷¹. However, most of the available reports are based on the theory and simulations including those in nanomagnetic systems. Thus, this field is wide open offering scopes for extensive experimental research. Böttcher and Henk demonstrated this intriguing physics theoretically for individual magnetic moments, a chain of Fe atoms, and Co islands on Cu (111).³⁷² There is a trade-off between the nutation effect and inertia of the systems determined by an additional term in the atomic LLG equation. The nutation effect is very significant on the fs time scale with a typical damping constant of 0.01–0.1 in a single magnetic moment. In a chain of Fe atoms, the amplitude of the nutation depends on the number of interacting neighbors and with increasing damping both lifetime and magnitude of nutation decrease.

Numerical simulations by Olive *et al.* showed a scaling function with respect to $\alpha\gamma H$ for the nutation angular frequency, which is also valid for the precession angular frequency when $\alpha\gamma H \gg 1$. Here, τ is the inertial dynamics characteristic time, α is the dimensionless damping, γ is the gyromagnetic ratio, and H is the static magnetic field.³⁷³ This trembling of spins induced by inertial dynamics has been theoretically studied by various other groups.^{374,375} A later report by the atomistic approach revealed that the nutation dynamics can be induced by the nonuniform local fields originated from surface anisotropy in ferromagnetic NPs.³⁷⁶ A very recent experimental report revealed that a single YIG nanodisk (diameter: 700 nm) subjected to deep nonlinearity

can accommodate stable quantized modes that do not transfer energy within themselves and thus are very energy efficient.²⁹² The spatial confinement of the nanomagnet helps avoid any additional instability. A two-tone spectroscopic measurement was conducted where a strong continuous excitation along with a weak microwave field pulse modulated at the frequency of a cantilever tip were used in the MRFM technique to probe the nutation on top of the steady state precession.

The experiments are still at an evolving stage and the scope is very vast, where nutation dynamics can be induced in single nanomagnets of varying magnetic potential as well as arrays of interacting nanomagnets of different geometric architectures. The excitation fields can vary from pulsed magnetic field, spin-torque to acoustic excitations, and very complex nutations consisting of multiple frequencies can be potentially obtained. The competition between inertial damping and Gilbert damping along with SOT-induced antidamping can be very exciting to follow in nanomagnetic systems. Analytical and numerical methods also need to progress hand in hand to capture such complex and fundamental dynamical processes.

H. Emergence of antiferromagnetic nanostructures

The experimental study of SWs in antiferromagnets³⁷⁷ as well as the theory of antiferromagnetic resonance³⁷⁸ and linear SW theory³⁷⁹ have been known since 1950s. However, they have received great impact in recent times in spintronics and magnonics due to their various advantages over their ferromagnetic and ferrimagnetic counterparts. They do not have macroscopic magnetization and, hence, no stray field but can interact with spin-polarized current³⁸⁰ and give rise to STT and skyrmion textures.³⁸¹ Due to their strong sublattice exchange field, they can show huge resonance frequency in the THz range.³⁸² They are readily observed even in semiconductors and, therefore, are easy to integrate in hybrid devices using both charge and spin degrees of freedom. Due to these advantages, it is natural to develop and study patterned antiferromagnetic nanostructures both from fundamental interest and from device fabrication perspective. However, this field is still in its infancy. The recent discovery of long-distance spin transport

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through antiferromagnetic insulating materials opens up huge opportunities for emerging spintronics applications.³⁸³ We envisage a versatile application and a fundamental study in patterned antiferromagnetic structures starting from the magnetic tunnel junction elements and MC to THz emitters. A recent theoretical study proposes the development of antiferromagnetic MCs by using two complementary methods for achieving control over the magnonic degrees of freedom: (a) by controlling the anisotropy properties of the SW system and (b) by exposing the antiferromagnet to a tailored magnetic field. Formation of a band-like structure of allowed and forbidden bands, which can be adjusted by tuning the parameters of the MC, raises hopes for designing new types of MCs complementary to ferromagnet-based MC.³⁸⁴ This issue of avoiding spurious “crosstalk” even with high packing density is schematically shown in Fig. 22(c). For an array of antiferromagnetic nanomagnet, the 180° switching of spins will not result in any change in the net magnetization, but 90° rotation [along the y axis in Fig. 22(c)] of the Néel vector within the individual nanoelements can be considered as “0” or “1.” If these types of arrays are designed, the packing density of bits can be much larger than the ferromagnetic systems. However, the writing and reading of information within compensated antiferromagnetic nanomagnets in time scales of ps or less will be far more challenging. Researchers are currently developing various methods involving charge current and spin current for deterministic control of the ultrafast switching dynamics in antiferromagnetic systems.^{385,386} However, no such attempt has been made for patterned array of antiferromagnetic nanomagnets yet. Determination of damping of antiferromagnetic system is another challenge. This field is clearly brimming with many unsolved problems, which need to be addressed in the upcoming years.

I. Future direction in dynamics of spin textures

As mentioned earlier, nanoscale spin textures will play an important role in future reconfigurable and reprogrammable magnonic and spintronic devices. To this end, controlled preparation of magnetic DWs, vortex, skyrmions, bubbles, and other spin textures, interconversion between them, their dynamics, and interaction of them with spin current and magnon current will dominate the magnonics and spintronics research in the future.

Magnetic domains and DWs have shown great promises in racetrack memory, logic devices, and SHNOs, and huge efforts have been made in studying the DW propagation, expansion, pinning, and depinning by magnetic field, charge, and spin current.³⁸⁷ This field will continue to grow with the introduction of various SOC effects as described in Sec. III D. The interaction of SW with DW has been less studied,^{204,388,389} but the interest is shifting toward this more recently. Recently, DW has been proposed as a reconfigurable MC due to scattering of surface SW at cork-screw type DW of aligned stripe domains in a Co/Pd ML with PMA.³⁹⁰ They have also been used as SW nanochannels in a 180° Néel wall³⁹¹ and antiparallel coupled domain³⁹² arrangements. These areas will continue to grow with the introduction of various ML systems with PMA and synthetic antiferromagnets,^{393,394} where competition between Zeeman, PMA, demagnetizing and antiferromagnetic energies, and external perturbations can lead to easy tunability of domain structures.

Magnetic vortex dynamics in single vortex and coupled vortices have led to many interesting fundamental physics and application proposals as discussed in Sec. II I. Research in this area has gained further momentum more recently with the interesting reports of whispering gallery magnons in vortex,³⁹⁵ chaos in incommensurate states of spin-torque-driven vortex oscillations, MVTs,²²³ etc. Fundamental studies on the interaction of vortex with magnon,³⁹⁶ spin current, and acoustic waves will continue to increase in the coming years. Numerical studies of coupled vortices demonstrated energy transfer, amplification, fan-in, fan-out, tri-state buffer switch operation, and energy transfer by antivortex solitons.^{223–225} Experimental realization of these effects by electrical and optical techniques will be important for further progress in this field. Moreover, dispersion of gyration modes and SW in 1D, 2D, and 3D arrays of magnetic vortices (magnonic vortex crystal) will be a topic of intense interest. Local control of the core-polarization and circulation of individual vortex in an array may lead to huge set of patterned vortex crystals. Spin-torque vortex oscillator³⁹⁷ will be another field of interest, and research on the stabilization and dynamics of phase-locked vortex oscillators is expected to advance significantly.

Despite having a sizable effort, skyrmion dynamics and related effects will continue to emerge in the future. A strong motivation in skyrmion dynamics is to achieve large skyrmion velocity in a magnetic track without appreciable drift along the transverse direction during the motion. Observation of clockwise, anticlockwise, and breathing modes in single skyrmions of different sizes and skyrmion crystals of varying geometries are expected to receive much attention. Furthermore, hybridization of skyrmion modes with different magnon modes will also be imperative. The skew scattering of magnons from skyrmions gives rise to the topological magnon Hall effect (MHE), while the topological magnus force leads to the skyrmion Hall effect (SKHE). A combination of MHE and SKHE may lead to a competition between thermally driven radial magnon current, transverse magnon current, and electron flow. By designing a magnetic track with in-plane anisotropy without DMI at the edges and out-of-plane anisotropy at the middle, SKHE can be reduced.³⁹⁸ SKHE can also be suppressed in antiferromagnetically exchange-coupled skyrmions due to the absence of net topological charge and, hence, extensive research needs to be carried out with ferrimagnetic and antiferromagnetic nanostructures. The annihilation and creation of skyrmions on the application of electric field has also been proposed. Room temperature devices such as magnetic racetrack memory, skyrmion MCs, skyrmionic logic devices, and skyrmion-based radio frequency devices are few of those examples, which will lead this field to its pinnacle in next few years.³⁹⁹ Numerical calculation reveals that a chain of skyrmions exhibit a rich SW band structure with their frequencies ranging from 50 to 100 GHz,⁴⁰⁰ which is much higher than the conventional FMR frequency. Field-controlled skyrmion crystals may act as reconfigurable and yet stable MCs.⁴⁰¹ Inertial mass originates from the ability of a system to store energy internally during its motion and due to its additional topological source of inertia skyrmions can show very large inertial mass.²³² Observation of characteristic eigenmodes of inertia and determination of inertial mass of skyrmions in various systems would be an important fundamental problem.

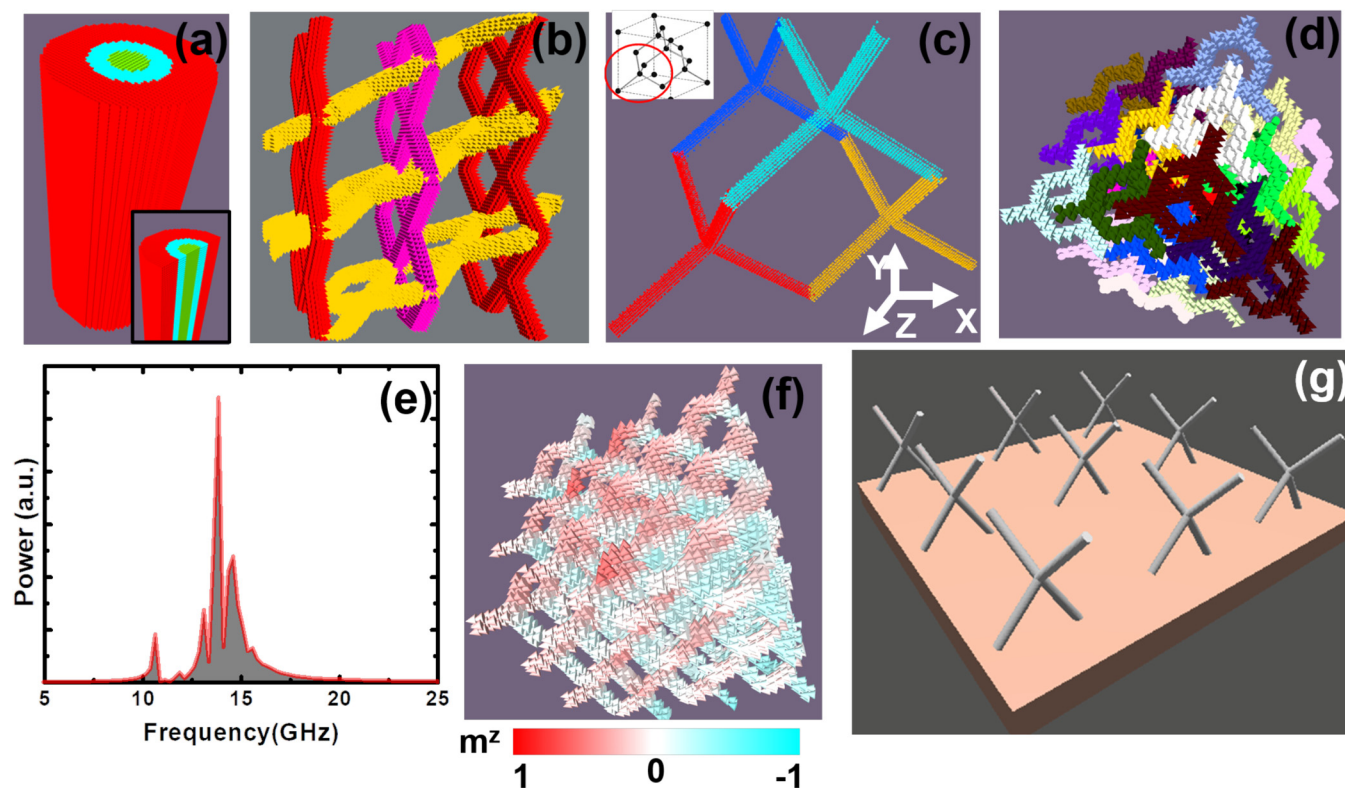
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It is relevant to mention here that not only skyrmion but also half-skyrmion, antiskyrmion, skyrmionium, meron, and other topological solitons are gaining huge attention.^{402–404} For example, the recent discovery of meron lattice in the chiral magnet $\text{Co}_8\text{Zn}_9\text{Mn}_3$ ⁴⁰⁵ raises the immediate challenge of the creation and stabilization of a single meron pair, which is the most fundamental topological structure in any 2D meron system, in a continuous ferromagnetic film, and to study its dynamics. Finally, stabilization of skyrmions in unconventional systems like ferromagnetic thin films adjacent to 2D materials, topological insulators, or heavy metals with weaker IDMI and excitation and control of their dynamics would be open problems.

J. Progress with artificial spin ice

The existence of emergent magnetic monopoles in ASI systems is one of the fascinating phenomena in magnetism. The back and forth movement of monopoles through the Dirac string can be very beneficial for “magnetronic” devices. So far, the monopoles have been mainly observed in connected and disconnected

ASI. However, the investigation of static and dynamic magnetic properties of a large variation of ASI structures both in 2D and 3D are foreseen in the near future.²⁴⁰ For SW propagation, connected ASI can be useful, but the possibility of trapped DWs or even nonuniform spin textures at the junctions can pose hindrances to the propagating SW. The interaction of the propagating SW with the monopoles will be an exciting phenomenon to explore. In addition to tunability of the magnon band structure, possible scattering of magnons by magnetic monopoles may give rise to new type of topological Hall effect. In the presence of additional stimulation, such as magnetoelasticity, spin-torque, chiral spin texture, and other spin-orbit effects, the monopoles can lead to exotic properties of SW propagation. The ASI structures can also act as complex MCs. The magnetization configuration of ASI structures is highly sensitive to an external applied field, leading toward exceptional tunability of SWs in such systems and the formation of a new class of reprogrammable magnonic devices. The exploration of frustration in 3D^{240,253} is promising both from fundamental physics as well as for extremely versatile tunable 3D MCs that can be useful for magnetic devices harnessing the variation of spin textures along the third dimension as well.



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FIG. 23. Simulated 3D magnetic nanostructures. (a) Core-shell cylindrical nanowire with three different layers and (b) interconnected zigzag nanowires. (c) Simulated unit cell of a diamond bond lattice. Different colors are assigned to four different units for better visualization. The unit cell of the diamond lattice is shown in the inset [From Kittel, *Introduction to Solid State Physics*, 18th ed. Copyright 2014 Wiley.⁴¹¹ Adapted with permission from Wiley]. (d) $3 \times 3 \times 3$ array of diamond bond lattice is shown, where each cube is assigned to a different color for better visualization. (e) FFT power spectrum of simulated time-resolved magnetization at an applied bias field of 4 kOe along the x direction. (f) The phase profile (m_z component) of the highest intense mode is shown. (g) Schematic of 3D tetrapod structures arranged in a square lattice symmetry.

K. Advancement in the dynamics of 3D magnetic nanostructures

Despite its initial progress, the fabrication of high-quality and versatile 3D MNS in sub-100 nanometer scale is yet to be achieved.^{32,253} FEBID is a powerful technique to fabricate 3D complex nanostructures in the nanoscale, but the purity of magnetic materials needs substantial improvement. The combination of TPL with electrodeposition or thermal evaporation can improve the material purity in 3D MNS but hitting the sub-hundred nanometer scale remained elusive so far. Modification of the existing fabrication techniques and development of new techniques are pre-requisites for fabrication of high-quality 3D MNS in the deep nanometer regime for the fabrication of compact 3D MNS-based magnetic devices. The ground state of 3D MNS may possess fascinating spin configurations such as hopfions.²⁵⁷ X-ray tomography⁴⁰⁶ is capable of mapping the magnetization vector in 3D. The phase contrast imaging is possible with coherent x rays.⁴⁰⁷ The measurements in these high-end instruments depend on the availability of the techniques. New methods are required for faster measurements and laboratory-based characterization of 3D MNS. The SW in 3D MNS can be measured using bench-top techniques as discussed in Secs. II C, II K, and III A. Most of the available techniques are capable of measuring the SW dynamics from the surface of 3D MNS. To study the static and dynamic magnetic properties from the complex and angled 3D MNS, new techniques such as diffraction-based MOKE in off-specular geometry⁴⁰⁸ or dark-field MOKE magnetometry based on specular reflection⁴⁰⁹ need to be further developed and integrated with time-resolved magnetometry. The experimental measurements of collective SW dynamics and magnon band structure in arrays of 3D MNS are still absent in the literature. New fabrication, experiment, and analysis tools are pre-requisites to realize fascinating spin textures and SW dynamics in 3D MNS and the development of practical devices based on them.

Simulated static spin configurations of two different types of 3D MNSs are presented in Figs. 23(a) and 23(b). Furthermore, an exemplary numerical simulation study of SW dynamics in a periodic 3D diamond bond lattice (DBL) constituted of square cross-sectional nanowires with 10 nm width and 25 nm length has been performed by using mumax³.⁴¹⁰ The unit cell of the DBL is shown in Fig. 23(c), which consists of four tetrapods, each of which is made of four wires as shown in the inset of Fig. 23(c). Each tetrapod has a common junction where four nanowires are connected. An array of $3 \times 3 \times 3$ DBL is shown in Fig. 23(d). Each unit cell⁴¹¹ has been assigned different colors for clear viewing. The simulated SW spectrum is shown in Fig. 23(e), which unraveled four clear SW modes. The phase profile of the highest power mode is shown in Fig. 23(f). Within the individual nanowire, the spins precess in the same phase, while the spins precess out-of-phase between the adjacent nanowires having an overlap at the junctions. A schematic of the 3D tetrapod structures arranged in a square lattice symmetry is shown in Fig. 23(g). Such complex structures and their spin dynamics need to be further studied experimentally and numerically to gain deeper insights into this burgeoning research field.

IV. CONCLUSION

Magnetization dynamics of magnetic nanostructures have been studied extensively for several decades, and during the last

two decades, nanomagnetism has now grown remarkably to deliver a diverse range of technological applications. Starting from the development of sophisticated fabrication processes and state-of-the-art characterization techniques to the construction of broad range of devices, the ceaseless progress in this field has spread its root deep into science and the society. Achieving the feature size down to the atomic scale limit and probing ultrafast phenomena in the femtosecond time scale are no longer impossible. Besides the immense growth in 1D and 2D nanomagnetism, recent advancements and the introduction of unconventional architectures, 3D magnetic nanostructures, magnon-spintronics, spin-orbitronics, and topological spin textures in magnetic nanostructures have widened our horizon. To this end, the focus has recently been drawn more toward entangling multiple sub-fields together, which may lead to intriguing hybrid phenomena. VCMA, the combination of spin transport with magnon dynamics, strong coupling in nanostructures, and spin texture driven SWs are few of those examples. Very recently, the development of voltage controlled on-demand magnonic nanochannels by periodically modulating VCMA using 1D stripe like indium tin oxide electrodes have been demonstrated. Controlled propagation of SWs confined through these nanochannels lead to an avoided crossing due to the strong magnon-magnon coupling of the SW modes propagating through adjacent nanochannels.⁴¹²

Despite showing substantial promises, this field still offers an abundance of new potentials and faces stern challenges in reaching some of the overriding goals, like all-magnetic computing, neuromorphic and quantum computing, and on-chip communication. The integration of the magnetic components on-chip within an atomically small area and minimization of power consumption are still massive challenges. Furthermore, fundamental areas like imaging of spin dynamics in nanomagnets, short-wavelength exchange SWs, spin accumulation, nutation, and inertial dynamics need in-depth exploration. A combined theoretical and experimental groundwork are necessary in this sector. With a steep upsurge of consumer electronics in the coming years, there will be a formidable competition between charge-based and spin-based devices. Only time will tell if nanomagnetism, along with its exceptional scalability of length and time, extraordinary diversity and flexibility of properties, and low-power consumption, is ready to become a leader in the “post-Moore era.”

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DATA AVAILABILITY

The data that support the findings of this study are available within the article.

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