ECEN720: High-Speed Links Circuits and Systems Spring 2023

Lecture 3: Time-Domain Reflectometry & S-Parameter Channel Models



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Announcements

- Lab 1 report and Prelab 2 due Feb 6
- Reference Material Posted on Website
 - TDR theory application note
 - S-parameter notes

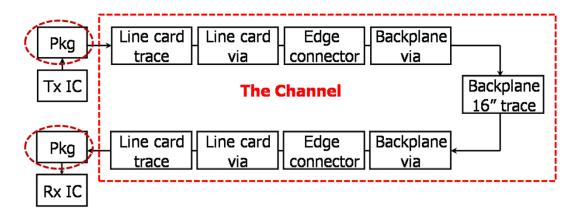
Agenda

- Interconnect measurement techniques
 - Time-domain reflectometry (TDR)
 - Network analyzer
- S-parameters
- Cascading S-parameter models
- Full S-parameter channel model
- Transient simulations
 - Impulse response generation
 - Eye diagrams
 - Inter-symbol interference

Lecture References

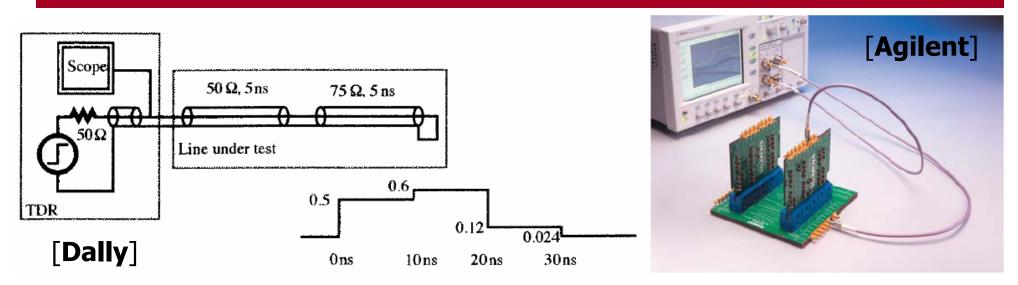
- Majority of TDR material from Dally Chapter 3.4, 3.6 - 3.7
- Majority of s-parameter material from Hall "Advanced Signal Integrity for High-Speed Digital Designs" Chapter 9

Interconnect Modeling



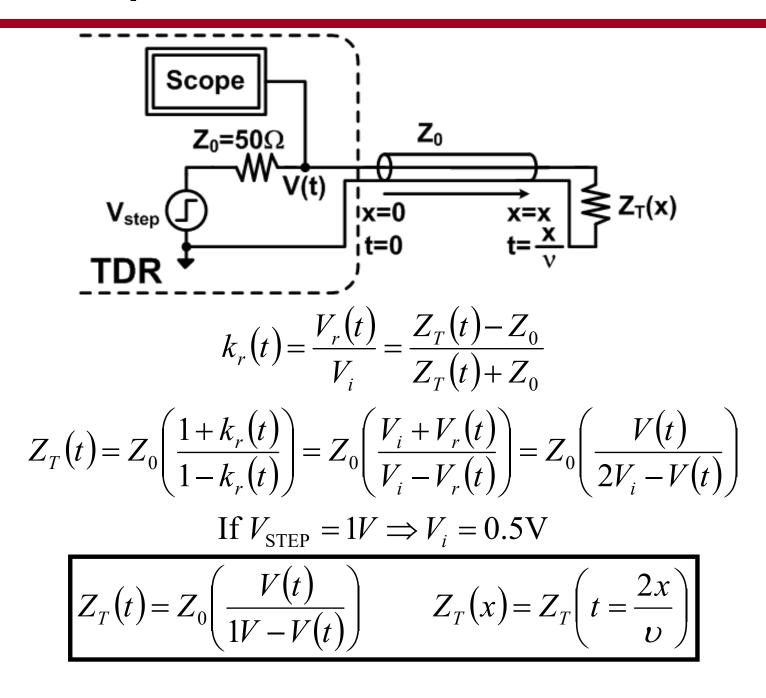
- Why do we need interconnect models?
 - Perform hand calculations and simulations (Spice, Matlab, etc...)
 - Locate performance bottlenecks and make design trade-offs
- Model generation methods
 - Electromagnetic CAD tools
 - Actual system measurements
- Measurement techniques
 - Time-Domain Reflectometer (TDR)
 - Network analyzer (frequency domain)

Time-Domain Reflectometer (TDR)

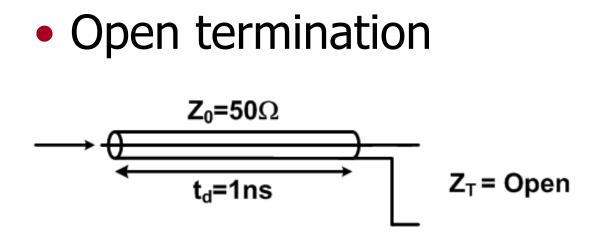


- TDR consists of a fast step generator and a high-speed oscilloscope
- TDR operation
 - Outputs fast voltage step onto channel
 - Observe voltage at source, which includes reflections
 - Voltage magnitude can be converted to impedance
 - Impedance discontinuity location can be determined by delay
- Only input port access to characterize channel

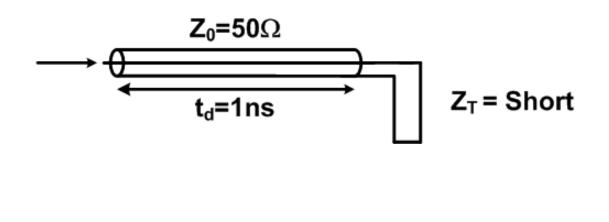
TDR Impedance Calculation

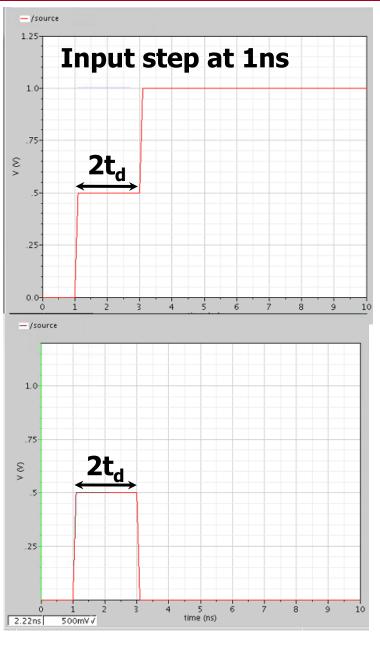


TDR Waveforms (Open & Short)



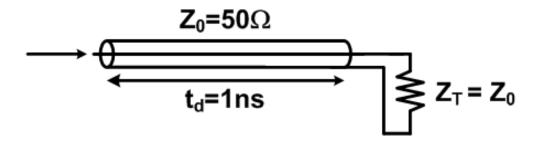
Short termination



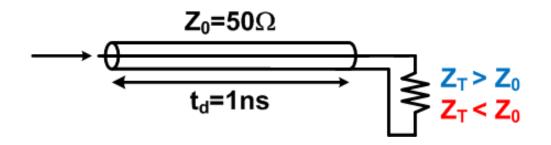


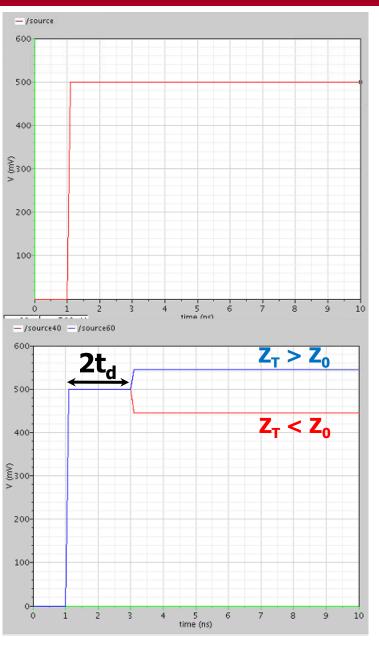
TDR Waveforms (Matched & Mismatched)

Matched termination

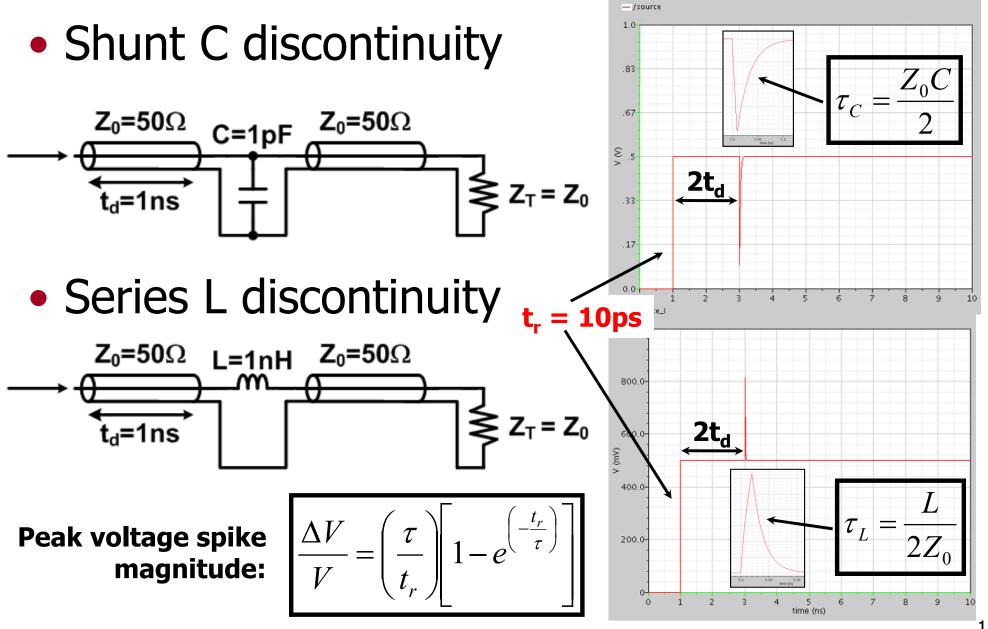


Mismatched termination





TDR Waveforms (C & L Discontinuity)



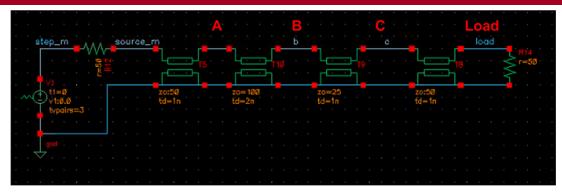
TDR Rise Time and Resolution

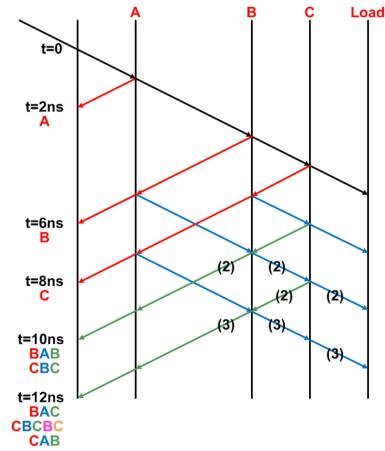
TDR spatial resolution is set by step risetime

 $\Delta x > t_r \upsilon$

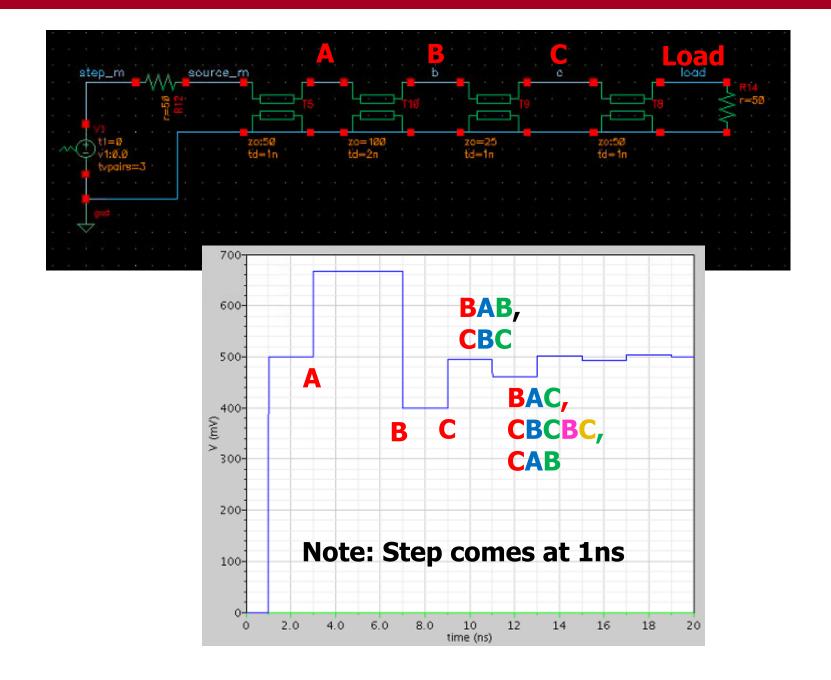
- Step risetime degrades with propagation through channel
 - Dispersion from skin-effect
 - Lump discontinuities low-pass filter the step
- Causes difficulty in estimating L & C values
- Channel filtering can actually compensate for lump discontinuity spikes ⁽³⁾

TDR Multiple Reflections

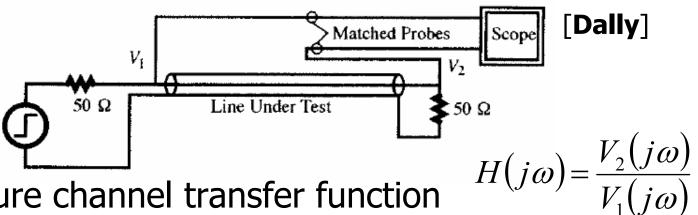




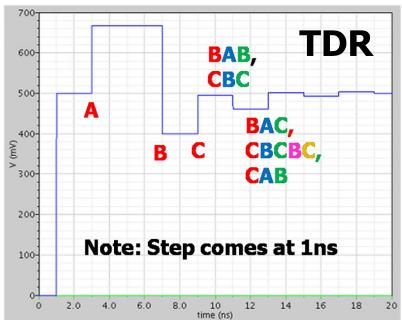
TDR Waveforms (Multiple Discontinuities)

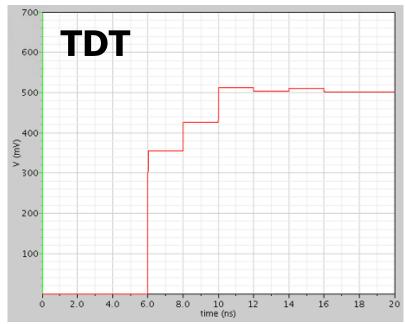


Time-Domain Transmission (TDT)

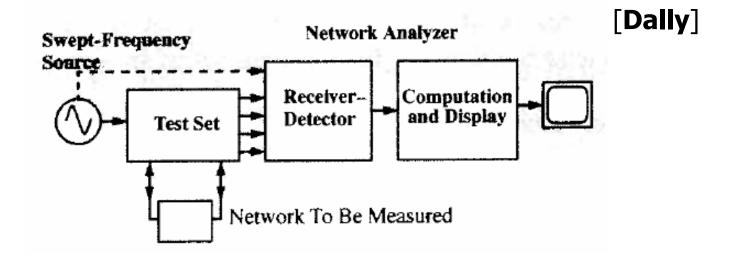


- Can measure channel transfer function
- Hard to isolate impedance discontinuities, as they are superimposed on a single rising edge



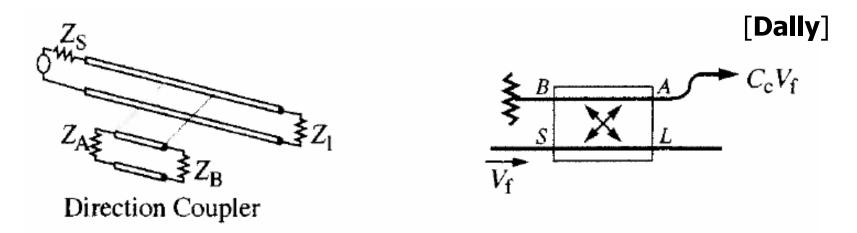


Network Analyzer



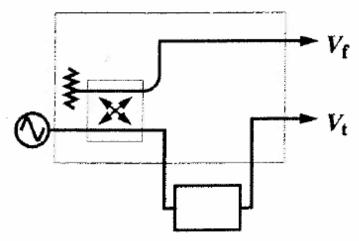
- Stimulates network with swept-frequency source
- Measures network response amplitude and phase
- Can measure transfer function, scattering matrices, impedance, ...
- Test set is configured differently for each kind of measurement to be performed

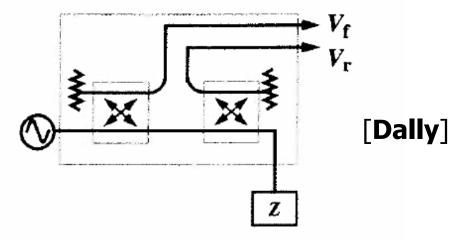
Directional Coupler



- Test sets in high-frequency network analyzers make use of directional couplers
- Directional couplers are two transmission lines coupled over a short distance
- If the short line is properly terminated, it allows for the voltage across Z_A to be proportional to the forward traveling wave and the voltage across Z_B to be proportional to any reflected wave

Transfer Function & Impedance Measurements





Test Set for Transfer Function

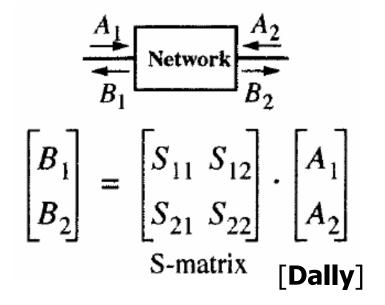
Test Set for Impedance Measurements

- Transfer function measurement
 - The input signal is from a directional coupler which samples the forward traveling wave
 - The network output serves as the output
- Impedance measurement
 - The input signal is from a directional coupler which samples the forward traveling wave
 - The reflected wave from the network is compared with this input to characterize the impedance over frequency

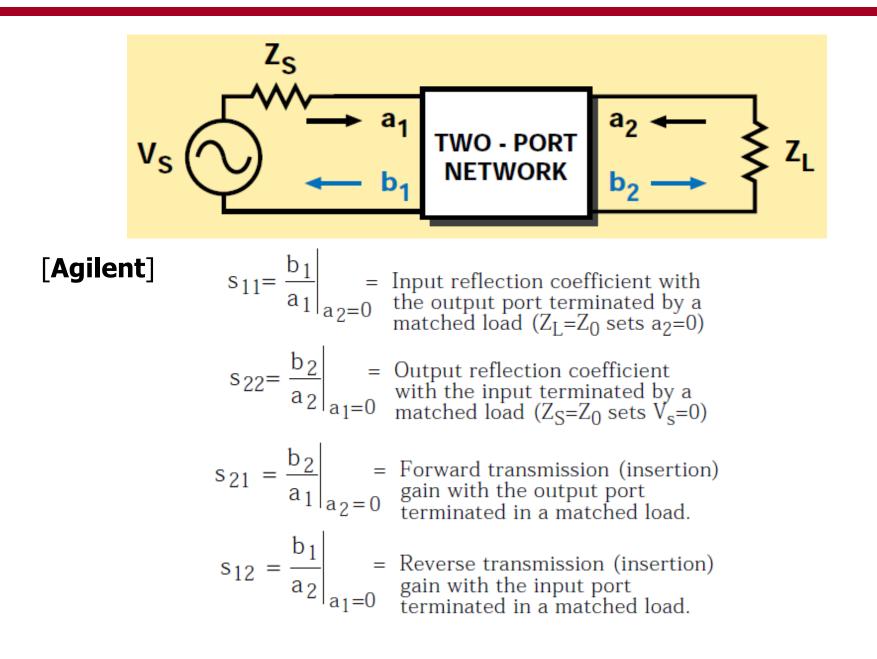
Scattering (S) Parameters

• Why S Parameters?

- Easy to measure
- Y, Z parameters need open and short conditions
- S parameters are obtained with nominal termination
- S parameters based on incident and reflected wave ratio



Formal S-Parameter Definitions

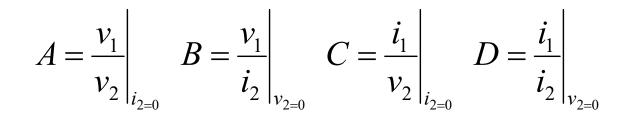


Cascading S-Parameters

- Network analysis allows cascading of independently characterized structures
- However, can't directly cascade sparameter matrices and multiply
- Must first convert to an ABCD matrix (or T matrix)

ABCD Parameters





 $\begin{vmatrix} v_1 \\ i_i \end{vmatrix} = \begin{vmatrix} A & B \\ C & D \end{vmatrix} \bullet \begin{vmatrix} v_2 \\ i_2 \end{vmatrix}$

Converting Between S & ABCD Parameters

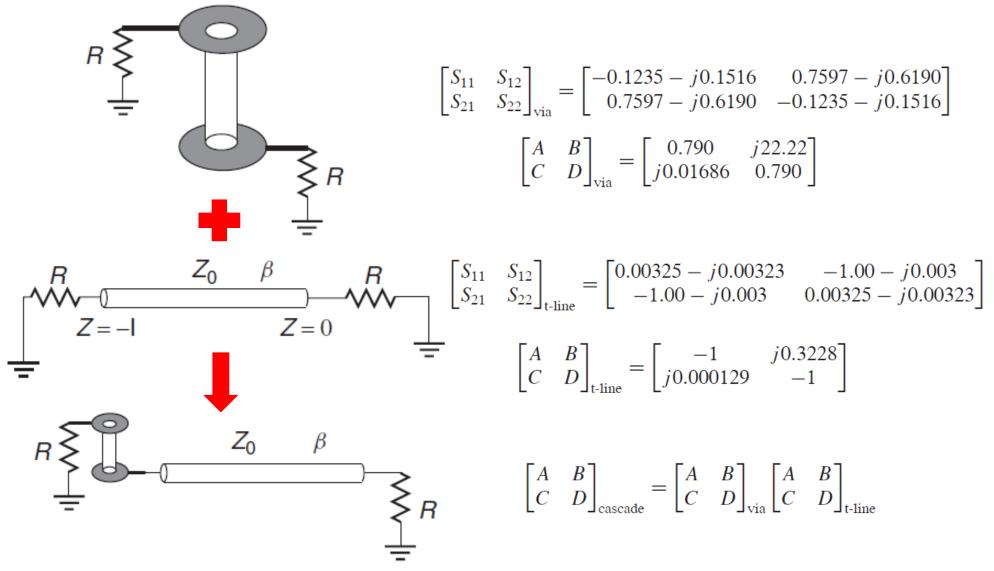


$$\begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \begin{bmatrix} \frac{B - Z_n(D - A + CZ_n)}{B + Z_n(D + A + CZ_n)} & \frac{2Z_n(AD - BC)}{B + Z_n(D + A + CZ_n)} \\ \frac{2Z_n}{B + Z_n(D + A + CZ_n)} & \frac{B - Z_n(A - D + CZ_n)}{B + Z_n(D + A + CZ_n)} \end{bmatrix}$$
$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} \frac{(1 + S_{11})(1 - S_{22}) + S_{12}S_{21}}{2S_{21}} & Z_n \frac{(1 + S_{11})(1 + S_{22}) - S_{12}S_{21}}{2S_{21}} \\ \frac{1}{Z_n} \frac{(1 - S_{11})(1 - S_{22}) - S_{12}S_{21}}{2S_{21}} & \frac{(1 - S_{11})(1 + S_{22}) + S_{12}S_{21}}{2S_{21}} \end{bmatrix}$$

 ${}^{a}Z_{n}$ is the termination impedance at the ports.

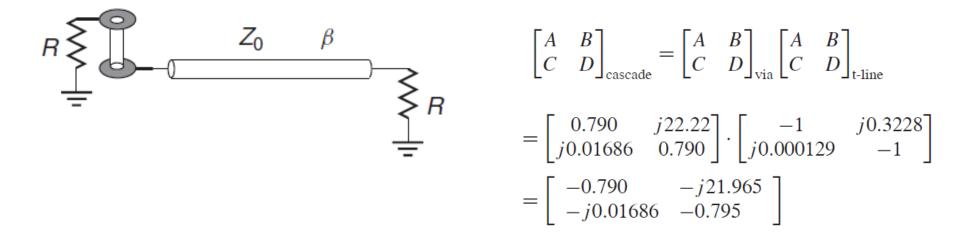
[Hall]

Example: Cascaded Via & Transmission Line



• Taken from "Advanced Signal Integrity for High-Speed Digital Designs" by Hall

Example: Cascaded Via & Transmission Line



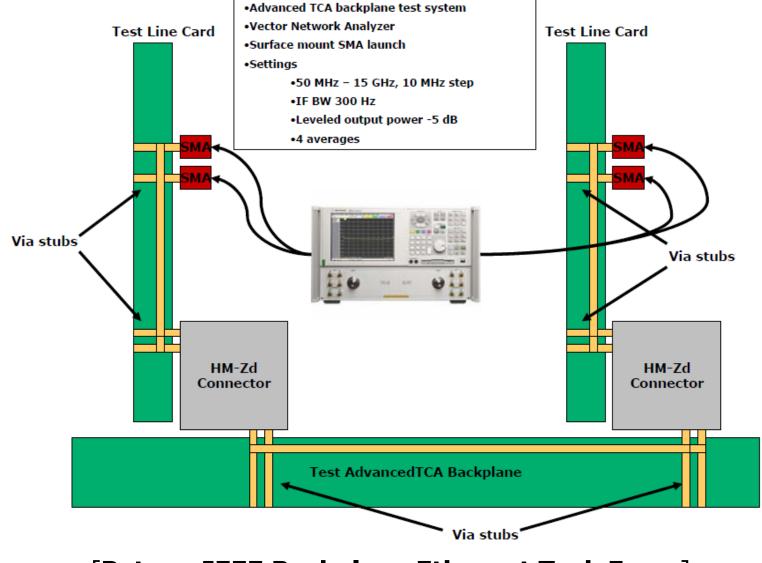
Using conversion table:

$$\begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix}_{\text{cascade}} = \begin{bmatrix} -0.1259 - j0.1553 & -0.7635 + j0.6186 \\ -0.7645 + j0.6182 & -0.1200 - j0.1565 \end{bmatrix}$$

• Can also use T matrixes to cascade

• Taken from "Advanced Signal Integrity for High-Speed Digital Designs" by Hall

S-Parameter Channel Example



[Peters, IEEE Backplane Ethernet Task Force]

S-Parameter Channel Example (4-port differential)

peters 01 0605 rzv channel thru response HZ S RT R 50 FREQ S11 S12 S13 S14 521 522 523 524 S31 S32 S33 S34 S41 S42 S43 S44 REAL. TMAG REAL. TMAG REAL TMAG REAL. TMAG 5.00000000e+007 6.279266901548e-002 -5.256007502766e-002 -1.995363973143e-001 -9.018006169275e-001 7.405252014369e-002 -1.653914717779e-002 4.694410796534e-004 2.855671737566e-003 -1.993592781969e-001 -9.017752677900e-001 6.847049395661e-002 -3.537762509466e-002 6.592975593456e-004 2.600733690373e-003 7.478976460177e-002 -1.488182269791e-002 7,438370524663e-002 -1.650568516548e-002 6.663957537997e-004 2.723661634513e-003 5.641343731365e-002 -5.693035832892e-002 -2.070369894915e-001 -8.986367167361e-001 3.380698172980e-004 2.715033111885e-003 7.497765935351e-002 -1.488546535615e-002 -2.063544808970e-001 -9.002700655374e-001 6.856095801756e-002 -3.019606086420e-002 6.00000000e+007 4.829977376755e-002 -6.288238652440e-002 -4.923832497425e-001 -7.721510464035e-001 6.298956599590e-002 -3.938489680891e-002 1.125377257145e-003 1.921732299021e-003 -4.925547500023e-001 -7.726263821707e-001 6.163450406360e-002 -4.486265928179e-002 1.299644022342e-003 1.492436402394e-003 6.462146347807e-002 -3.736630924981e-002 6.308085276969e-002 -3.947655302643e-002 1.386741613180e-003 1.653454474207e-003 4.393874455850e-002 -6.448913049207e-002 -4.992743919180e-001 -7.660808533046e-001 1.280875740087e-003 1.936760526874e-003 6.482369657086e-002 -3.743006383763e-002 -4.995203164654e-001 -7.674804458241e-001 6.284893613667e-002 -4.132139739274e-002

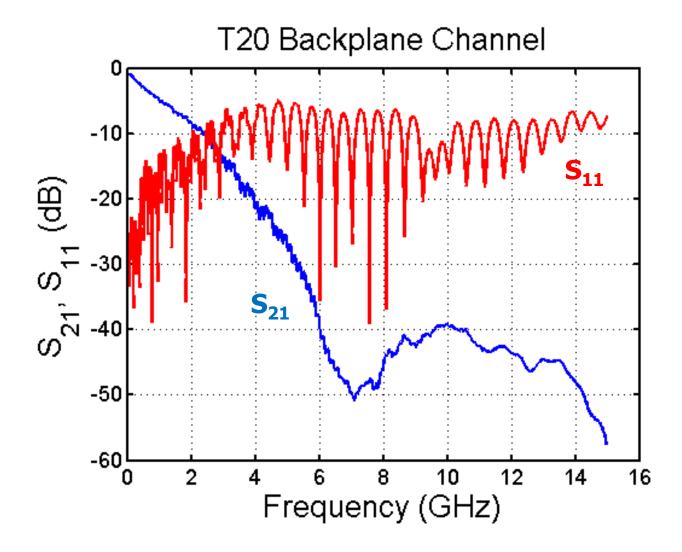
Data from 50MHz to 15GHz in 10MHz steps

1.49900000e+010 -1.884123481138	e-001 3.522933794755e-001 9.493645552321e-004	04 2.735890006358e-004 2.939002692375e-002 -8.676465491258e-003 -2.207496924854e-004 1.236065259912e-004	£
9.463443060684	e-004 3.105615146344e-004 -1.742347383703e-001	01 4.813685271232e-002 -6.152705437030e-004 1.614752661571e-003 6.774475978813e-002 9.617239585695e-003	3
2.953403838205	e-002 -8.707827389646e-003 -6.226849675423e-004	04 1.637610280621e-003 -1.595766021694e-001 3.757605914955e-001 -1.809501624148e-004 -7.061855554470e-004	4
-2.613575703191	e-004 1.368108929760e-004 6.788329666403e-002	02 9.551687705500e-003 -2.146293806886e-004 -7.363580847286e-004 -1.199804891859e-001 7.697336952293e-002	2
1.50000000e+010 -1.883176013184	e-001 3.545614742110e-001 9.524680768441e-004	04 -5.404222971799e-005 2.935126165241e-002 -1.235086132268e-002 -1.616280086909e-004 2.347368458649e-004	4
1.039250921080	e-003 -6.032017103742e-005 -1.649137634331e-001	01 4.966164587830e-002 -6.748937194262e-005 1.689652681670e-003 6.725041473699e-002 1.961009613152e-003	3
2.959693594806	e-002 -1.251203706381e-002 -2.927441863297e-005	05 1.747754847916e-003 -1.531702433245e-001 3.773014940454e-001 -3.769459376261e-004 -5.671620228005e-004	ł
-2.089293612250	e-004 2.303682313561e-004 6.740524959192e-002	02 1.672663579641e-003 -4.385850073691e-004 -5.810569604703e-004 -1.121319455376e-001 7.458173831411e-002	2

$$\begin{bmatrix} b_{1} \\ b_{2} \\ \vdots \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} & S_{13} & S_{14} \\ S_{21} & S_{22} & S_{23} & S_{24} \\ S_{31} & S_{32} & S_{33} & S_{34} \\ S_{41} & S_{42} & S_{43} & S_{44} \end{bmatrix} \begin{bmatrix} a_{1} \\ a_{2} \\ a_{3} \\ a_{4} \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} & S_{13} & S_{14} \\ S_{21} & S_{22} & S_{23} & S_{24} \\ S_{31} & S_{32} & S_{33} & S_{34} \\ S_{41} & S_{42} & S_{43} & S_{44} \end{bmatrix} \begin{bmatrix} a_{1} \\ a_{2} \\ a_{3} \\ a_{4} \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} & S_{13} & S_{14} \\ S_{21} & S_{22} & S_{23} & S_{24} \\ S_{31} & S_{32} & S_{33} & S_{34} \\ S_{41} & S_{42} & S_{43} & S_{44} \end{bmatrix} \begin{bmatrix} a_{1} \\ a_{2} \\ a_{3} \\ a_{4} \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} & S_{13} & S_{14} \\ S_{21} & S_{22} & S_{23} & S_{24} \\ S_{31} & S_{32} & S_{33} & S_{34} \\ S_{41} & S_{42} & S_{43} & S_{44} \end{bmatrix} \begin{bmatrix} v \\ 0 \\ -v \\ 0 \end{bmatrix}$$

$$S_{dd11} = \frac{b_{d1}}{a_{d1}} \bigg|_{a_2 = a_4 = 0} = \frac{1}{2} \left(S_{11} + S_{33} - S_{13} - S_{31} \right)$$
$$S_{dd21} = \frac{b_{d2}}{a_{d1}} \bigg|_{a_2 = a_4 = 0} = \frac{1}{2} \left(S_{21} + S_{43} - S_{23} - S_{41} \right)$$

S-Parameter Channel Example



Impulse Response

- Channel impulse responses are used in
 - Time domain simulations
 - Link analysis tools

$$X(\omega) \qquad H(\omega) \qquad Y(\omega)$$

$$h(t) \qquad Y(\omega)$$

$$Y(\omega) = H(\omega)X(\omega)$$

$$y(t) = h(t) * x(t) = \int_{-\infty}^{\infty} h(t-\tau)x(\tau)$$

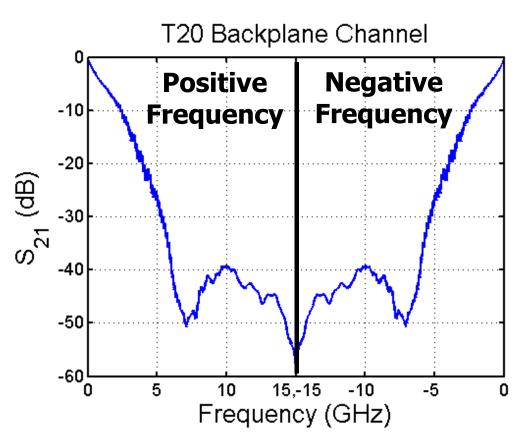
$$h(t) = F^{-1}{H(w)}$$

Generating an Impulse Response from S-Parameters

- Perform the inverse Fourier transform on the s-parameter of interest
- Step 1: For ifft, produce negative frequency values and append to sparameter data in the following manner

$$S(-f) = S(f)^*$$

 $h(t) = F^{-1}\{S(\omega)\}$



Increasing Impulse Response Resolution

 Could perform ifft now, but will get an impulse response with time resolution of

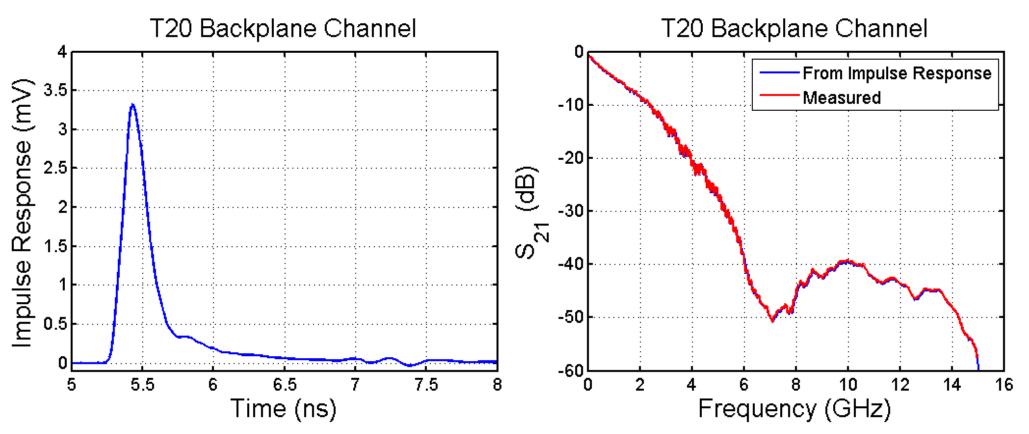
$$\frac{1}{2f_{\text{max}}} = \frac{1}{2(15\text{GHz})} = 33.3\text{ps}$$

 To improve impulse response resolution expand frequency axis and "zero pad"

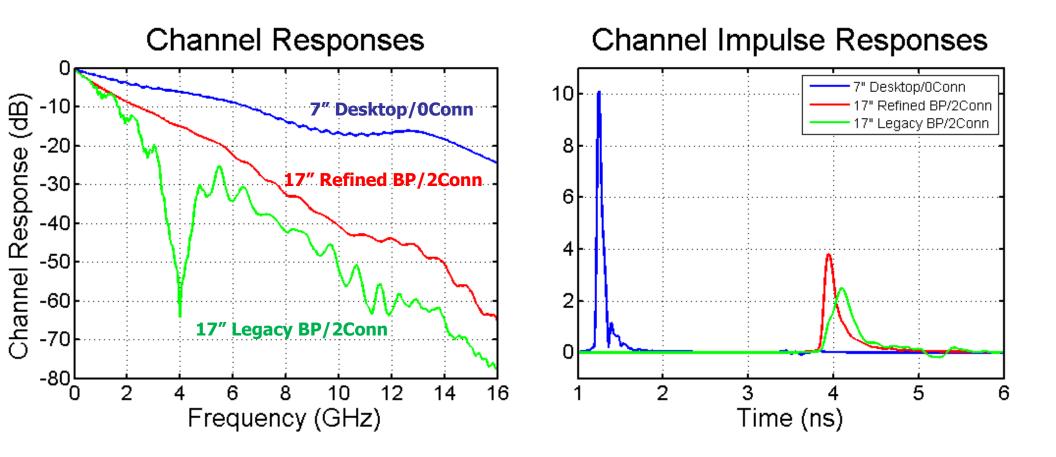
For 1ps resolution: zero pad to +/-500GHz T20 Backplane Channel 0.8 0.6 zero padding S 21 0.4 0.2 0 500.-500 250 -250'n Frequency (GHz)

Channel Impulse Response

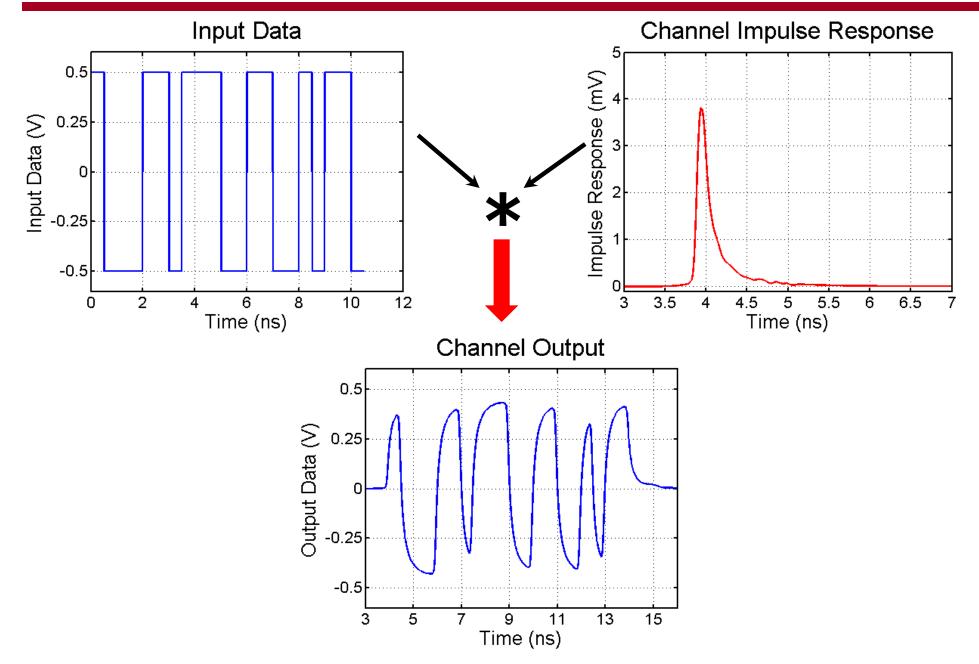
- Now perform ifft to produce impulse response
- Can sanity check by doing an fft on impulse response and comparing to measured data



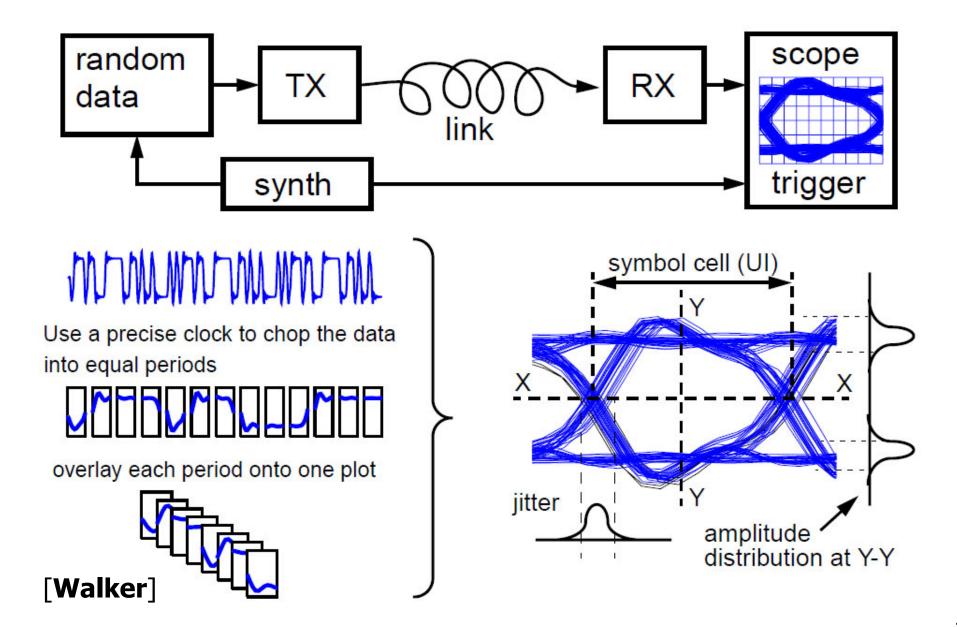
Impulse Response of Different Channels



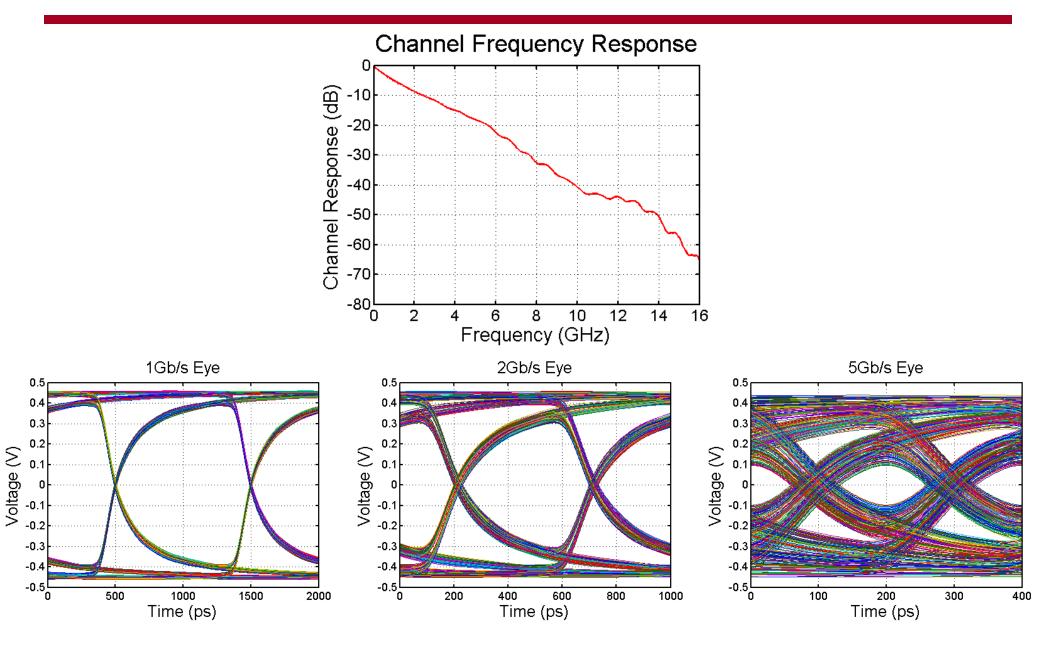
Channel Transient Response



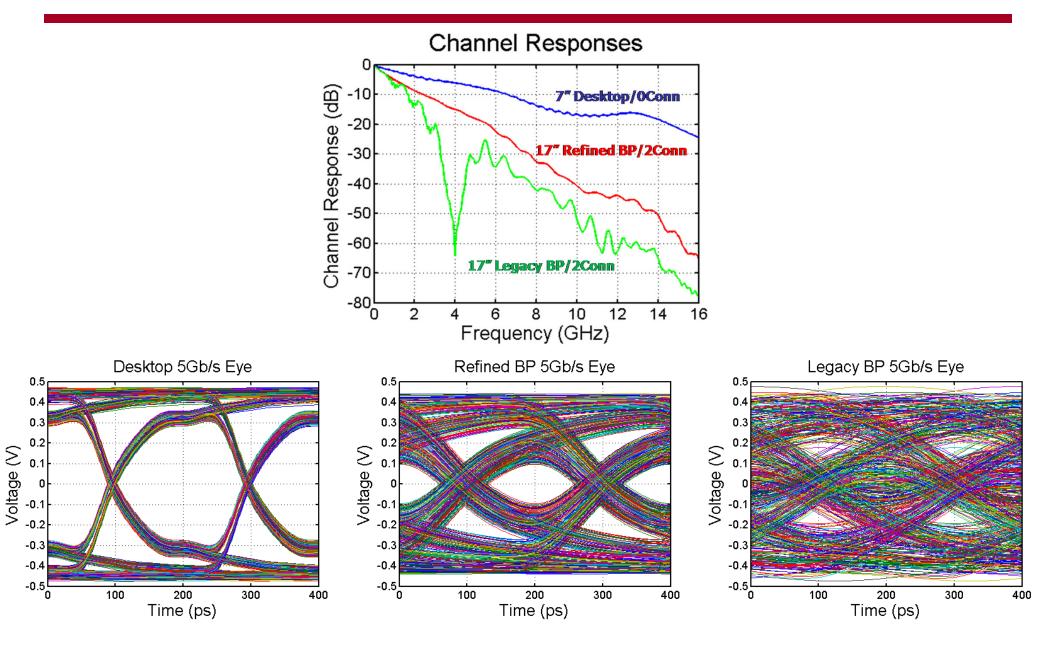
Eye Diagrams



Eye Diagrams vs Data Rate

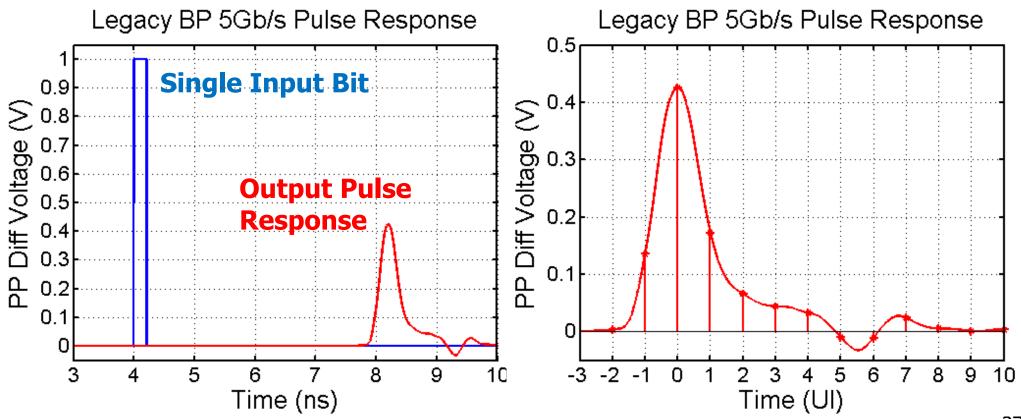


Eye Diagrams vs Channel



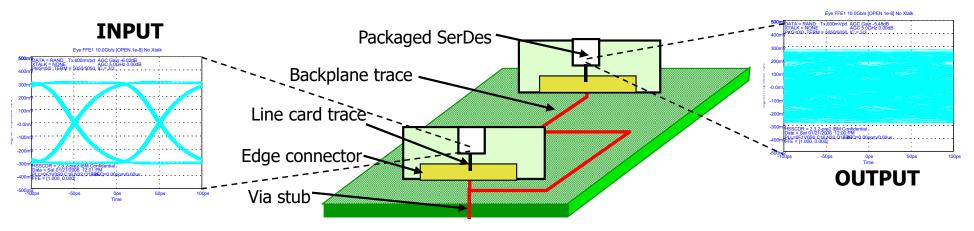
Inter-Symbol Interference (ISI)

- Previous bits residual state can distort the current bit, resulting in inter-symbol interference (ISI)
- ISI is caused by
 - Reflections, Channel resonances, Channel loss (dispersion)



ISI Impact

- At channel input (TX output), eye diagram is wide open
- As data pulses propagate through channel, they experience dispersion and have significant ISI
 - Result is a closed eye at channel output (RX input)



[[]Meghelli (IBM) ISSCC 2006]

Next Time

- Channel pulse response model
- Modulation schemes