

Astro
Sciences
Center


Report No. M-16
THE MULTIPLE OUTER PLANET MISSION (GRAND TOQRE RECEIVED Hint bum $82<29252$

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## APPROVED

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January 1969

The Multiple Outer Planet Mission (Grand Tour) is possible in the late 1970's because of an unusual alignment of the outer planets. Such an alignment will not reoccur for some one hundred seventy-nine years. From its initial conception the mission appeared potentially rewarding, but many unknowns were associated with it and there were many questions which had not been answered. Accordingly, the Astro Sciences Center of IIT Research Institute undertook a study of the major problem areas associated with the Grand Tour mission in order to further verify the mission concept and to provide a background for later Phase A study.

The specific aims of the study were:

1. To determine the guidance requirements to perform the mission,
2. To identify the scientific commonality between the planets Jupiter, Saturn, Uranus, Neptune,
3. To define "minimum" and "representative" scientific payloads, and
4. To estimate the launch vehicle requirements to perform the mission.

Trajectory opportunities for the Grand Tour exist from 1976 through 1980. The 1976 opportunity requires a high risk penetration of the Jovian radiation belts, in order to achieve adequate gravitational deflection. Since later opportunities relax this constraint, the 1976 opportunity has not been considered in detail. The 1977 and 1978 opportunities are the most acceptable in terms of planet miss distances, characteristic velocity, and time of flight. These were examined in detail and the results used as inputs to the guidance and scientific experiment analyses. The 1979 and 1980 opportunities pass very far from Jupiter (greater than 30 radii) which reduces the significance of Jupiter in the mission concept. These opportunities also have relatively high launch energy requirements and were not considered in further"detail.

The most critical planetary intercept profile is at Saturn, the miss distance being generally of the same order as the radius of its rings. A cursory study of the possible collision rates in the rings made it advisable not to permit direct penetration of the rings by the spacecraft. At each of the 1977 and 1978 opportunities, mission profiles that pass entirely outside the rings (exterior) and that pass between planet surface and the lower edge of the rings (interior) have been considered. These are designated the 1977 E , and $1977 \mathrm{I}, 1978 \mathrm{E}$, and 1978 I missions. Once a

Saturn profile had been selected, the profiles at each of the other gravity assist planets were essentially fixed. The major trajectory parameters for the selected opportunities are shown in Table S-1.

Table S-1
TRAJECTORY PARAMETERS FOR GRAND TOUR

|  | 1977 E | 1977 I | 1978 E | 1978 E |
| :--- | :---: | :---: | :---: | :---: |
| Launch Date | Sept 1977 | Sept 1977 | Oct 1978 | 0ct 1978 |
| Ideal Velocity ft/sec |  |  |  |  |
| Center of Window <br> 20 Day Launch Window | 51,900 | 54,400 | 53,200 | 56,200 |
| Time of Flight (yrs) |  | 55,200 | 54,200 | 57,100 |
| Jupiter | 1.87 | 1.40 | 1.60 | 1.28 |
| Saturn | 3.98 | 2.98 | 3.36 | 2.53 |
| Uranus | 8.40 | 6.37 | 7.53 | 5.71 |
| Neptune | 11.94 | 9.05 | 11.00 | 8.32 |
|  |  |  |  |  |

The guidance requirements were established for each of the selected trajectories. Guidance maneuvers were specified on both approach and departure at each swingby planet to correct for three major errors:
a. the $\Delta V$ execution error from the previous maneuver
b. orbit determination errors
c. planet ephemeris errors

Because each swingby effectively magnifies any error that exists on approach to a planet the guidance velocity require. ments are sensitive to the size of the error and to the planet at which it occurs. The objectives of the guidance analysis were to determine realistic estimates of spacecraft propulsion $\angle V$ requirements, the method and accuracy of orbit determination, and the trajectory selection. Two tracking modes were consider ed, one using an on-board planet tracker, as originally con. sidered for the Mariner '69, and an alternative using earth based radar tracking as is current practice.

The guidance requirements for the Grand Tour mission are nuch more severe than for current missions although they are not beyond the current state of the art. The total velow city corrections are given in Table S-2 and it can be seen that interior ring passage missions are by far the more demanding.

Table S-2
TOTAL GUIDANCE VELOCITIES FOR GRAND TOUR

1977 E 1977 I 1978 E 1977 I

| On-Board Tracking (m/sec) | 190 | 430 | 200 | 370 |
| :--- | ---: | ---: | ---: | ---: |
| Earth Radar Tracking (m/sec) | 450 | 1710 | 340 | 1010 |

The orbit determination process must extend well into the planetary approach phase at Lranus and Saturn. Thus some approach maneuvers must be made relatively close to the planet. However, from the standpoint of positional error, either tracking mode will provide accuracies within the tolerances of the scientific experiments at each target planet.

The largest $\angle V$ contribution occurs at the Lratiss encounter. The importance of this result is that if a probiem of fuel depletion occurs, it would be significant only at Uranus and hence only the Neptune encounter need be sacrificed. In the interest of minimizing tne guidance iV requirement a strong case is made for an on-board planet tracking capability.

The scientific objectives for the Grand Tour mission have been developed from the goal of understanding the outer planets of the solar system. A systematic and logical procedure was adopted to identify the parameters of interest (measurables) that should be measured at each planet, and their relative values. Potential experiments were identified for each of the measurables and the extent to which each experiment could fulfill the objectives, given the flyby profiles, was evaluated. By combining these two sets of resuits it was possible to identify the relative importance of a wide range of experiments to the goal and objectives of
exploring the outer planets. A final rating for the experiments was expressed in terms of value per pound to aid the selection of typical payloads. The major results of this evaluation are presented graphically in Figure Sol. The order in which the experiments have been plotted was determined by their relative values.

The highest priority scientific objectives were reiated to the atmospheres of the outer planets, but the filghest priority experiments were related to particles and fields. This resulted directly from the universality of these experiments throughout the mission and hence their high integrated total value. The value of the planetary experiments is approximately equal at each target for all weights. This results from the fact that all the flyby profiles are similar in terms of their viewing of the light and dark hemispheres of the planets. The major differences between the plantary profiles are in miss distance. Overall there is a clear scientific commonality between the targets. Furthermore, this commonality can be retained for both 1977 and 1978 opportunities and for the interior and exterior ring passages, although the detailed experiment design specifications will be different in each case.

Typical scientific payloads have been derived on the basis of the experiment value curves shown in Figure $\mathrm{S}-1$ and are shown in Table S-3. The "minimum" payload for which the mission is considered worthwhile utilizes the first four itt research institute

FFA
scientific value of instrument payloads


| EXPERIMENT | $\begin{gathered} \text { WEIGHT } \\ \text { LBS } \end{gathered}$ | value/Lb <br> ARB. UNITS | DATA |
| :---: | :---: | :---: | :---: |
| MICROMETEOROID DETECTOR | 2 | 124 | NOMINAL |
| MAGNETOMETER PACKAGE. | 10 | 76 | 1 bps |
| COSMIC RAY detector | 2.5 | 66 | NOMINAL |
| plasma probe | 6.5 | 48 | 3 bps |
|  | 21 | 314 | $\simeq 5 \mathrm{bps}$ |
| TRAPPED PARTiCLE DETECTOR | 5 | 41 | $10^{4} \mathrm{bpp} *$ |
| POLARIMETER - PHOTOMETER | 5 | 41 | $10^{5}$ |
| IR, WAVE RADIOMETER | 10 | 20 | $10^{4}$ |
| RF DETECTOR | 5 | 14 | $10^{4}$ |
|  | 46 | 430 | $5 \mathrm{bps}+10^{5} \mathrm{bpp}$ |
| LOW RES. TV | 10 | 12 | $2 \times 10^{8} \mathrm{bpp}$ |
| NARROW UV PHOTOMETERS | 15 | 9 | $10^{4}$ |
| OCCULTATION (DUAL FREQU.) | 20 | 6 | $10^{4}$ |
| ABSORPTION PHOTOMETERS | 28 | 5 | $10^{4}$ |
| MASS SPECTROMETER | 10 | 5 | NOMINAL |
| AIRGLOW PHOTOMETERS | 8 | 4 | $10^{3}$ |
|  | 137 | 471 | $5 \mathrm{bps}+2 \times 10^{8} \mathrm{bpp}$ |
| HIGH RES. TV | 30 | 3 | $2 \times 10^{8} \mathrm{bpp}$ |
| RADAR ( 10 cm ) | 20 | 3 | $10^{3}$ |
| HIGH RES. IR RADIOMETER | 20 | 1 | $10^{6}$ |
|  | 207 | 478 | $5 \mathrm{bps}+4 \times 10^{8} \mathrm{bpp}$ |

[^0]TABLE S. 3 SELECTED PAYLOADS FOR GRAND TOUR
particles and fields experiments. This weighs approximately 20 pounds and will acquire some 5 bits per second of data. A "small" payload includes the first 8 experiments and is able to include 4 planetary experiments with a relatively low data requirement. The total weight is approximately 50 pounds. The "medium" payload includes television which adds some $2 \times 10^{8}$ bits to the data requirement. It was aiso possible to include the next five experimencs without adding markedly to the power or data requirements. The payload weight is approximately 140 pounds. Finally a "large" payload includes all the experiments considered and weighs some 200 pounds. These selected payloads are used to define a typical range of total spacecraft weights and launch vehicle requirements.

In terms of the total spacecraft weight there are many Grand Tour mission options with different mission requirements. There are four selected trajectories, with their quite distinct midcourse correction requirements, depending on the tracking system used. There are four selected payloads each with its own weight, power, and data bulk. Rather than select a typical examp1e, a matrix of spacecraft weights is presented in Table S-4 which bound the variables of the Grand Tour missions and launch vehicle capabilities. These weight totals are based on a brief analysis of the subsystem requirements for commications, power guidance, attitude control, sequencing and storage; thermal control, and structure.

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| $\left\lvert\, \begin{aligned} & 4 \\ & \text { 彩 } \end{aligned}\right.$ | 8 |  | O- |  | 아N |  | － |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 유N |  | 暑 |  | 올 |  | 응 |  |
|  | 응 |  | 1 |  | 웅 |  | 1 |  |
|  | 욧 |  | 1 |  | 1 |  | 1 |  |
| $\begin{aligned} & \stackrel{U}{O} \\ & \frac{2}{J} \end{aligned}$ | $\begin{aligned} & \text { 요 } \\ & \underline{\circ} \end{aligned}$ | 용 | 응 | \％ | 응 | 용 | 읒 | 요융 |
|  | 응 | 8 | \％ | \％ | 을 | $\begin{aligned} & \text { O्N } \\ & \underline{\sim} \end{aligned}$ | $\stackrel{\text { 용 }}{\sim}$ | 侖 |
|  | N | 응 | $\stackrel{\sim}{8}$ | 읓 | 윤 | 응 | \％ | － |
| $\begin{aligned} & \frac{\overline{3}}{\frac{3}{2}} \\ & \frac{2}{\frac{2}{2}} \\ & \hline \end{aligned}$ | 응 | 웃 | $\stackrel{8}{\circ}$ | 숯 | 웅 | $\stackrel{\sim}{\circ}$ | 웃 | 융 |
| 은 른 존 |  |  |  | $\frac{\stackrel{\rightharpoonup}{a}}{\frac{\alpha}{\alpha}}$ |  | $\frac{\stackrel{a}{a}}{\frac{1}{\alpha}}$ |  | 旁 |
| $\begin{aligned} & \frac{7}{\frac{0}{6}} \\ & \frac{0}{2} \end{aligned}$ |  |  |  |  |  |  |  |  |

TABLE S． 4 COMPARISON OF LAUNCH VEHICLE CAPABILITY WITH SPACECRAFT WEIGHT

From a total capability standpoint the exterior ring passages are strongly recommended, and an on-board tracker is the most effective tracking system. However for the exterior passages, the differences are such that radar tracking could be used as a back up, and only the Neptune intercept would be lost if the on-board system failed. If it is important that the same spacecraft design and launch vehicle be used at both opportunities, the minimum vehicle would be a Titan III-DCentaur which has a capability for the exterior missions of 1900 lbs in 1977 and 1250 lbs in 1978. This will launch a "medium" payload with on-board tracking or a "smal1" payload with radar tracking.

The recommended missions would utilize the 1977 and 1978 opportunities, use an on-board planet tracker, have a payload in the 100 pound weight class, and reçuire a total spacecraft weight of some 1200 pounds. In the light of the apparent tractability of all the subsystem requirements for the Grand Tour mission, it is strongly recommended that conceptual spacecraft designs be developed and that the complete feasibility of the mission be verified.

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## SECTION 1

## INTRODUCTION

In the late 1970's a unique opportunity to conduct a grand tour of the outer planets will be possible utilizing gravity-assisted swingbys of Jupiter, Saturn and Uranus to achieve flyby missions of the planets and Neptune (Flandro 1966). A typical profile of this Grand Tour Mission is shown in Figure 1.1. In concept the Grand Tour offers a very significant exploration opportunity. For the investment of a single launch to Jupiter, scientific experiments are potentially possible at four outer planets. The most attractive opportunities occur in 1977 and 1978 with total mission times on the order of 9 to 12 years to Neptune. The opportunities offer a saving in trip time over direct outer planet missions but are rare in the sense that they will not reoccur until 2156 A.D.

In reality it is not obvious that the Grand Tour is practical. It is quite possible that the flyby profiles at each planet are so different as to demand different rather than common experimental payloads. One of the most critical aspects of executing the mission will be avoiding the rings of Saturn. Both interior and exterior ring flybys of Saturn have been considered (Silver 1967). It intuitively appears that a heavy guidance and control capability may be necessary to keep the spacecraft on course during the successive planet flybys.

FIGURE I.I. HELIOCENTRIC FLIGHT PATH, 1977-I GRAND TOUR.

It was in the context of this potentially rewarding mission concept, with many unknowns, that the Astro Sciences Center of IIT Research Institute performed the "Pre-Phase A" Study reported here. The specific aims of the study were:

1. To determine the guidance requirements to perform the mission.
2. To identify the scientific commonality between the planets (Jupiter, Saturn, Uranus, Neptune).
3. To define "minimum" and "representative" scientific payloads.
4. To estimate the launch vehicle requirements to perform the mission.

The flow chart for the study is shown in Figure 1.2. The trajectory selection exerts a strong influence on both the guidance and the science raquirements in that it specifically defines each flyby profile. The sensitivity of the trajectory to guidance errors, and therefore the probability of completing all swingby maneuvers, is also dependent on the particular trajectory considered. Section II of this report presents four specific trajectories and the rationale for their selection. The four trajectories are designated exterior and interior Saturn Ring passages in 1977 and 1978 (1977 E, 1977 I, 1978 E , and 1978 I ). By way of example Figure 1.3 shows the encounter profile at each of the planets for the 1977 E Grand Tour Mission.

FIGURE 1.2. STUDY FLOW CHART - GRAND TOUR


Section 3 describes the orbit determination analysis and the guidance requirements associated with each of the four selected trajectories. In defining the guidance velocity requirements both radar tracking from earth and on-board planet tracking (such as was proposed for Mariner '69) were evaluated.

Section 4 presents an evaluation of the scientific objectives for exploration of the outer planets. A method is presented which allows the relative priority of all the relevant scientific objectives to be assessed at each of the outer planets. These objectives are then considered in Section 5 together with the actual flyby profiles, and with available flyby measuring techniques, to select mission payloads. The results for each potential experiment are expressed in terms of value per pound at each target. A total of four representative payloads have been selected on the basis of this e: Iluation.

Section 6 discusses the major mission requirements which have resulted from the trajectory, guidance and payload analyses. Sample spacecraft weight breakdowns are presented as a guide to the identification of the launch vehicle requirements.

The study has provided a much better understanding of the mission requirements for the Grand Tour Mission. In particular guidance and experiment analyses had not been performed to this level prior to this study.

## SECTION 2

## TRAJECTORY ANALYSIS AND SELECTION

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The trajectory of an interpianetary spacecraft can be altered significantly if the spacecraft passes near a planetary body. This perturbation effect, due to the planet ${ }^{\mathrm{r}} \mathrm{s}$ gravitational field, is often referred to as a "gravity assist." When properly designed, a gravity assist can be used to modify the heliocentric trajectory in a desired manner. For example, the trajectory may be deflected to intercept another target planet at a later time. The technique of gravity assisted or planetary-swingby trajectories has been studied extensively during the past several years (Minovitch 1963) and (Niehoff 1965). A number of studies have shown the advantage in reduced launch energy and trip time that accrues when this technique is employed for multiplemtarget missions in solar system exploration (Niehoff 1966) and Sturms 1967). This report is concerned with the "Grand Tour" mission, i.e., the successive swingbys of the Jovian or outer planets $-\infty$ Jupiter, Saturn, and l!ranus, with Neptune being the final target.

### 2.1 Principle of Planet Swingby <br> Viewed on a heliocentric scale, the result of a gravity assist is to change the spacecraft's velocity vector between the time that the spacecraft enters and leaves the planet's sphere of influence (see Table 2.1). Since this

Table 2.1 PLANET SPHERE OF INFLUENCE*

|  | Radius | Sphere of Inf1uence |
| :--- | :---: | :---: |
| P1anet | $6,378 \mathrm{~km}$ | $0.925 \times 10^{6} \mathrm{~km}$ |
| EARTH | 71,375 | $48.1 \times 10^{6}$ |
| JUPITER | 60,500 | $54.6 \times 10^{6}$ |
| SATURN | 24,850 | $51.7 \times 10^{6}$ |
| URANUS | 25,000 | $86.1 \times 10^{6}$ |

[^1]time is relatively short compared to the interplanetary travel time, the planet's orbital velocity may be considered approximately constant. Furthermore, the spacecraft's motion with respect to the planet approximates a hyperbola. Figure 2.1 illustrates the geometry of the hyperbolic flyby.

The spacecraft approaches the planet initially along one asymptote of the hyperbola with velocity $\mathrm{V}_{\mathrm{h} 1}$. This asymptotic approach velocity is defined as the vector difference between the heliocentric velocity of the spacecraft and that of the planet,

$$
\begin{equation*}
\underline{v}_{\mathrm{h} 1}=\mathrm{v}_{1}-\underline{v}_{\mathrm{p}} \tag{2.1}
\end{equation*}
$$

both of which are assumed determined at the nominal time of encounter. The gravitational attraction causes the planetocentric trajectory to bend through a rotation $\Psi$ which is the turning angle between the approach and departure asymptotes. The asymptotic departure velocity, $\mathrm{V}_{\mathrm{h} 2}$, is equal in magnitude to $V_{\mathrm{h} 1}$ but differs in direction. With reference to heliocentric coordinates, the changed velocity is now given by the vector addition.

$$
\begin{equation*}
\underline{v}_{2}=\underline{v}_{\mathrm{p}}+\underline{\mathrm{v}}_{\mathrm{h} 2} \tag{2.2}
\end{equation*}
$$

$\mathrm{V}_{2}$ differs from $\mathrm{V}_{1}$ in both magnitude and direction, the former reflecting a change in the energy of the heliocentric trajectory. In the case of successive swingbys of the outer planets, each swingby trajectory takes place along the trailing edge of the planet's motion, i.e., behind the planet as seen from the Sun.


FIGURE 2.I HYPERBOLIC FLYBY DIAGRAM

Hence, the heliocentric energy is increased by the gravity assist. Conservation of energy is preserved, of course, since the planet looses orbital energy in the gravitational exchange. However, this point is strictly academic inasmuch as the gravitational attraction of the massive planet by the spacecraft is negligible.

For a given grdvity assist planet, the asymptotic der. parture velocity can be shown to depend on the approach veiocity and the aim point parameters. The latter is expressed by the asymptotic miss vector $\underline{B}$ which is referred to the STR coordinate system of Figure 2.1. By definition, the target plane ( $T-R$ ) passes through the planet's center and is perpendicular to the direction of the approach asymptote $S$ (a unit vector).

$$
\begin{align*}
& \underline{S}=\frac{V_{\mathrm{h} 1}}{\left|V_{\mathrm{h} 1}\right|} \text { ecliptic reference }  \tag{2.3}\\
& \underline{T}=\frac{\underline{S} \times \underline{k}}{|S \times \underline{k}|}  \tag{2.4}\\
& \underline{R}=\underline{S} \times \underline{T} \tag{2.5}
\end{align*}
$$

with $k$ being a unit vector perpendicular to the ecliptic plane, $I$ is defined as a unit vector perpendicular to $\underline{S}$, and also parallel to the ecliptic. The vector $\underline{B}$, from the planet center perpendicular to the approach asymptote, lies in the target plane with components

$$
\begin{align*}
& (\underline{B} \cdot \underline{T})=b \cos \theta  \tag{2,6}\\
& (\underline{B} \cdot \underline{R})=b \sin
\end{align*}
$$

where $b=|\underline{B}|$ is the miss distance (here, miss distance is a trajectory design parameter not to be confused with a guidance error $\Delta b$ ).

Several important conic formulas relating the swingby parameters are

Hyperbolic velocity: $\quad \mathrm{V}_{\mathrm{h}}=\left|\underline{\mathrm{v}}_{\mathrm{h} 1}\right|=\left|\underline{\mathrm{V}}_{\mathrm{h} 2}\right|$
Periapse distance: $\quad r_{p}^{2}+\frac{2 \mu}{v_{h}^{2}} r_{p}=b^{2}$
Turning (deflection) angle:

$$
\begin{equation*}
\cos \psi=\frac{b^{2} v_{h}^{4}-\mu^{2}}{b^{2} v_{h}^{4}+\mu^{2}} \tag{2.9}
\end{equation*}
$$

Departure velocity vector:

$$
\begin{equation*}
\underline{V}_{\mathrm{h} 2}=\underline{V}_{\mathrm{h} 1} \cos \psi-\left(\frac{\underline{\mathrm{V}}_{\mathrm{h}} \sin \psi}{\mathrm{~b}}\right)_{2} \tag{2.10}
\end{equation*}
$$

where $\mu$ is the planet's gravitational constant $\left(\frac{\mathrm{km}^{3}}{\mathrm{sec}^{2}}\right)$ which is proportional to the planet's mass. Several comments can be made about the general effects of the above equations.
(1) The periapse (closest approach) distance is always less than or equal to the asymptotic miss-distance. The difference between these quantities will decrease as $\mu$ decreases or as $V_{h}$ increases.

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(2) The turning angle can vary between $0^{\circ}$ and $180^{\circ}$. Turning angle will increase as $\mu$ increases, or as $b$ decreases, or as $V_{h}$ decreases.

### 2.2 Launch Opportunities

Practical launch opporturities for the Crand Tour mission are dictated by the relative orientation of the outer planets. The appropriate phase angle relationship reoccurs approximately once every 179 years. This long period is fixed largely by the synodic period $c$ : the two outermost planets considered in the combination, Uranis and Neptune have a synodic period of about 171.4 years. Once the proper phasing does occur, however, several consecutive launch years are available because of the slow motion of the outer planets. The next opportunity occurs during the period from 1976 to 1980. Launch windows in each of these years are approximately 13 months apart.

Previous trajectory analyses of the Grand Tour were helpful to the present study in that launch windows and velocity requirements were fairly well delineated (Flandro 1966) and (Silver 1967). These results allowed one to readily identify the best opportunities, and to minimize costly trajectory search computations.

The bar chart of Figure 2.2 shows the range of ideal launch velocities* and trip times to Neptune for five launch opportunities in the period 1976-1980. It is seen that ideal velocity generally increases with each successive launch year, whereas the trip time tends to decrease. In any given year, the faster trip times correspond to the higher launch velocities. Overall, the potential Grand Tour missions cover the range of velocities 51,400 to $60,700 \mathrm{ft} / \mathrm{sec}$, and the range of trip times 8.1 to 12.8 years.

Another important parameter of the Grand Tour trajectories is the pericenter of closest approach distance at each planet. In the case of Jupiter, which moves faster than the other planets, the variation of pericenter distance with the launch year is quite large. A spacecraft launched in 1976 will pass very close to Jupiter (1.02-1.50 Jupiter

[^2]where VHL is hyperbolic excess velocity in $\mathrm{ft} / \mathrm{sec}$
$$
C_{3} \text { is injection energy in }\left(\frac{\mathrm{km}}{\mathrm{sec}}\right)^{2}
$$


FIGURE 2.2 GRAND TOUR LAUNCH OPPORTUNITIES
radii). Later flights in 1979 and 1980 have very large pericenter distances (30-70 Jupiter radii). Although close flybys of Jupiter may be desirable from a science experiment standpoint, several disadvantages of the 1976 opportunity are worth noting. These are: (1) long trip times, (2) equipment shielding penalty due to Jupiter's radiation belts, (3) high guidance requirement, and (4) an earlier spacecraft development and flight program. The disadvantages of the later launch opportunities are clearly the high launch velocities required and the large passing distances at Jupiter.

On the basis of the above preliminary results and arguments, it was decided that the best launch opportunities for the Grand Tour mission occur in 1977 and 1978. Accordingly, this study was aimed at these two consecutive launch years.
2.3 Method of Trajectory Analysis
The various stages in the trajectory analysis are
described by the block diagram shown in Figure 2.3 . A
computer program based on conic trajectory approximations was
employed to generate the large amount of data representing
potential Grand Tour trajectories throughout the launch
opportunities. Trajectory selections were then made from the
data map after imposing several conditions of constraint which
define the regions of practical trajectories. The final stage
in the analysis employs an N-BODY numerical integration

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FIGURE 2.3 METHOD OF TRAJECTORY ANALYSIS
targeting program to check the validity of the conic results, and to generate the partial derivative (sensitivity) matrices needed for the guidance analysis.

### 2.3.1 Conic Analysis

Trajectory data was obtained from the Space Research Conic Program (SPARC) developed at JPL for investigations of multiple planet missions (Joseph 1965). The inputs to this program are specialed values of the Earth-launch date and injection energy $C_{3}$. Using a matched conic approach between the successive heliocentric trajectory legs, a search is made to find the appropriate Earth-Jupiter transfer which results in subsequent planetary swingbys and finally Neptune encounter. The matching process insures equal magnitude of the approach and departure hyperbolic velocities at each swingby planet. A11 heliocentric trajectory legs were restricted to Type $I$, Class I transfers* in order to achieve th. thortest possible flight times. Mean orbital elements of the jianets were used to obtain the planetary positions and velocities at the encounter times.

[^3]In operation, potential Grand Tour trajectories are obtained over a range of launch dates and injection energy (ideal velocity). For each trajectory, the computer program printout includes defining parameters of the geocentric and planetocentric hyperbolas, planet encounter dates, elements of the heliocentric transfer legs, and orientation angles of the Earth, Sun and Canopus as seen by the spacecraft at the encounter times. Trajectory data is obtained over a sufficiently fine grid of input variables to allow the use of crossplotting techniques in the trajectory selection stage of the analysis.

### 2.3.2 NBCDY Targeting Analysis

The NBODY Targeting Program indicated in Figure 2.3 was developed at IITRI as a modification of the Lewis Research Center NBODY code (Strack 1963). Because of the single precision arithmetic of this program and the high trajectory sensitivity of. the Grand Tour, it was not possible to target a concinuous trajectory from Earth to Neptune. In fact, attempts to target two legs at a ̇ime (e.g., EarthoJupiter. Saturn) were not too satisfactory, although near convergence was obtained. The method adopted in this study was to target one leg at a time working backwards from the Uranus-Neptune leg and successively matching the arrival and departure target vector at each planet. This procedure is initialized with the conic trajectory parameters obtained from the SPARC program. IIT RESEARCH INSTITUTE

It should be made clear that the procedure of targeting each individual leg separately does not yield a continuous trajectory from Earth to Neptune. The discontinuity appears as a target plane velocity difference between the approach and departure trajectories. This is due to the fact that no attempt was made to converge on velocity but only on the miss vector $B$ and the time of encounter. Generally, the conic and NBODY results are in excellent agreement for any one trajectory leg. On the basis of this result, it is expected that the conic trajectory data is sufficiently valid for preliminary mission analysis. Some results of the NBODY Targeting Program are described in the Appendix to this section of the report.

### 2.3.3 Conditions of Constraint

Four constraints are imposed on the trajectory selection process. Clearly, the "hard" constraint is that the point of closest approach at each swingby planet must be above the planet's surface. This applies initially to the nominal trajectory conditions, but the question of guidance accuracy must be factored in at a later stage in the analysis. Guidance accuracy is the dominant factor in selecting the nominal aim point at Neptune, which otherwise might be chosen arbitrarily since Neptune is the final target.

Another constraint is that the declination of the geocentric departure asymptote be limited to about $34^{\circ}$. Lower declinations provide launch azimuths within ETR range safety limits, thus avoiding costly dog-leg maneuvers during ascent to Earth orbit. Also, early orbit determination accuracy is enhanced if the declination is not too large.

To avoid a communications problem caused by solar activity interference, it is desirable that the planet not be behind the sun at the time of encounter. That is, the earth-Sun-planet angle at planet encounter should be somewhat removed from $180^{\circ}$ (superior conjunction). A third constraint on the trajectory selection process, then, is a set of conjunction bands of $\pm 10$ days ( $\pm 10^{\circ}$ ) for each planet encounter.

The fourth, and major, constraint is the apparent necessity of avoiding passing through the Ring of Saturn. Lying in Saturn's equatorial plane, the Rings extend from about $11,500 \mathrm{~km}$ to $76,500 \mathrm{~km}$ above Saturn's surface. The inclination of the spacecraft's swingby trajectory to the Ring plane is about $30^{\circ}$ for the Grand Tour mission. The relative velocity between the spacecraft and Ring particles is about $12 \mathrm{~km} / \mathrm{sec}$ as an average, and the component of the spacecreft's velocity normal to the Ring plane is also about $12 \mathrm{~km} / \mathrm{sec}$.

There is great uncertainity in the present knowledge of the Ring density and thickness. An estimate of the upper limit on density based on a gravitational stability analysis is $0.06 \mathrm{~g} / \mathrm{cm}^{3}$ (Cook 1965) but the actual
density may be more than an order of magnitude lower. Earlier estimates of Ring thickness have an upper limit of about 10 km . However, a more recent analysis of observations fitter to a theoretical physical model indicates that the Rings may only be 10 cm thick (Franklin 1965).

A parametric analysis was performed assuming the average particle radius ( $r_{p}$ ) to range from 0.01 cm to 100 cm , and the average particle density ( $\rho_{p}$ ) to range from $1 \mathrm{~g} / \mathrm{cm}^{3}$ to $8 \mathrm{~g} / \mathrm{cm}^{3}$. It can be shown that the number of collisions (C) and the mass encountered (M) per unit spacecraft area are given by the following equations:

$$
\left.\begin{array}{l}
C=\left(\frac{V_{R}}{V_{N}}\right)\left(\frac{\tau}{\pi r_{p}^{2}}\right) \times 10^{4} \frac{\text { collisions }}{m^{2}} \\
M=\left(\frac{V_{R}}{V_{N}}\right)\left(\frac{4}{3}\right. \tag{2.12}
\end{array} \tau_{\mathrm{p}} \rho_{\mathrm{p}} r_{p}\right) \times 10^{1} \frac{\mathrm{~kg}}{\mathrm{~m}^{2}} .
$$

where $V_{R}$ is the relative velocity between the spacecraft and the Ring particles ( $\sim 12 \mathrm{~km} / \mathrm{sec}$ ) and $\mathrm{V}_{\mathrm{N}}$ is the spacecraft's velocity component normal to the Ring plane ( $\sim 12 \mathrm{~km} / \mathrm{sec}$ ).

The normalized optical thickness of the Rings, T , is assumed to be unity which is the maximum experimentally determined value. The following table lists several values of $C$ and $M$.

|  | $1 \mathrm{~g} / \mathrm{cm}^{3}$ | $8 \mathrm{~g} / \mathrm{cm}^{3}$ |
| :---: | :---: | :---: |
| $0.01 \mathrm{~cm}$ | $\begin{aligned} & \mathrm{C}=3.2 \times 10^{7} \frac{\mathrm{coll}}{\mathrm{~m}^{2}} \\ & \mathrm{M}=0.134 \frac{\mathrm{~kg}}{\mathrm{~m}^{2}} \end{aligned}$ | $\begin{aligned} & \mathrm{C}=3.2 \times 10^{7} \frac{\mathrm{coll}}{\mathrm{~m}^{2}} \\ & \mathrm{M}=1.07 \frac{\mathrm{~kg}}{\mathrm{~m}^{2}} \end{aligned}$ |
| $100 \mathrm{~cm}$ | $\begin{aligned} & \mathrm{C}=0.32 \frac{\mathrm{col}}{\mathrm{~m}^{2}} \\ & \mathrm{M}=1340 \frac{\mathrm{~kg}}{\mathrm{~m}^{2}} \end{aligned}$ | $\begin{aligned} & C=0.32 \frac{\mathrm{coll}}{\mathrm{~m}^{2}} \\ & M=10,700 \frac{\mathrm{~kg}}{\mathrm{~m}^{2}} \end{aligned}$ |

Since the mass that would be encountered by a spacecraft is estimated to be in the range $0.1 \mathrm{~kg} / \mathrm{m}^{2}$ to $10,000 \mathrm{~kg} / \mathrm{m}^{2}$, it would appear that the Grand Tour trajectory should not pass through the Rings of Saturn.

Launch opportunities for the Grand Tour in 1977 occur over a two to three week period in August-September of that year. A similar period 13 months later occurs during September-October in 1978. In this section of the report, certain characteristic trajectory parameters obtained from the SPARC computer runs are presented for these two launch years. Consideration of constraint conditions is deferred to the next section.

Figure 2.4 shows curves of ideal launch velocity in 1977 plotted on a grid of Jupiter arrival date (Julian Date) versus Earth launch date. Every point on the grid represents a potential Grand Tour trajectory to Neptune with swingbys at Jupiter, Saturn and Uranus. In selecting the range of design trajectories throughout a launch window, it is helpful to fix the Jupiter arrival date at some specified value. Therefore, the Jupiter arrival data is a convenient independent variable for representing other key trajectory parameters. The velocity curves are actually closed contours although this is not shown in the figure. In other words, for a given launch date and velocity, there are two possible Jupiter arrival dates. The later date corresponds to a Class II trajectory which has a significantly longer flight time. It is recalled that the Class II trajectories are not

IDEAL LAUNCH VELOCITY, FT/SEC


FIGURE 2.4 TRAJECTORY SELECTION GRAPH, 1977 GRAND TOUR
considered in the study. The minimum energy trajectory (Type I) has a launch date of Sept. 51977 and a Jupiter arrival date of Oct. 241979 (2444170). The corresponding minimum ideal launch velocity is $51,500 \mathrm{ft} / \mathrm{sec}$.

Figure 2.5 shows the declination of the geocentric departure asymptote. This parameter is seen to be in the range $23^{\circ}$ - $36^{\circ}$ for the 1977 Grand Tour. The higher declinations are associated with lower values of launch velocity. The minimum flight time to Jupiter is plotted as a function of launch velocity in Figure 2.6. This curve is obtained from the minimum points of the velocity contours of Figure 2.4. Flight time to Jupiter varies from 460 to 660 days as the ideal launch velocity decreases from 56,00C to $52,000 \mathrm{ft} / \mathrm{sec}$.

Three additional descriptive parameters of the Grand Tour are the trip time, pericenter distance and hyperbolic approach velocity at each planet encounter. This data is plotted against the Jupiter arrival date in Figures 2.7 to 2.9. The curves shown are specifically for the optimum launch date, i.e., the minimum launch velocity for each value of Jupiter arrival date. Although there is a variation of the parameters with launch date, this variation is quite small for Grand Tour trajectories. Hence, when plotted against Jupiter arrival date, this form of data compression is quite representative of all trajectories throughout the launch windows.


FIGURE 2.5. DECLINATION OF GEOCENTRIC DEPAFTURE ASYMPTOTE, 1977 GRAND TOUR


FIGURE 2.6 MINIMUM FLIGHT TIME TO JUPITER, 1977 GRAND TOUR



FIGURE 28 PLANET CLOSEST APPROACH DISTANCES, 1977 GRAND TOUR


FIGURE 2.9 PLANET ARRIVAL VELOCITIES, 1977 GRAND TOUR

It is seen that the closest approach distance is largest at Jupiter and smallest at Saturn. Closest approach at Neptune is not shown since it is arbitrary and will be chosen by the selection process described later. Another important characteristic is that the closest approach at each swingby planet increases as the trip time increases (or, as the launch velocity decreases). The largest variation occurs for Jupiter (3-12 Jupiter radii), and the smallest variation for Saturn (1-2.7 Saturn radii).

Along a given trajectory, the approach velocity is found to increase at each successive planet encounter. Also, as the trip time increases, the approach velocity at each planet decreases. The velocity variation over the range of trajectories shown are $7.7-13.4 \mathrm{~km} / \mathrm{sec}$ (Jupiter), 10.5-18.2 $\mathrm{km} / \mathrm{sec}$ (Saturn), $14.5-22.8 \mathrm{~km} / \mathrm{sec}$ (Uranus), and $16.3-25.3 \mathrm{~km} / \mathrm{sec}$ (Neptune).

The above results have described the 1977 Grand Tour opportunity. Similar data is presented for the 1978 Grand Tour in Figure 2.10 to 2.14.

### 2.5 Trajectory Selections <br> The constraint conditions discussed previously

 are first applied to select trajectories for the 1977 launch opportunity. Figure 2.15 shows the constraint regions of the surface and Rings of Saturn projected onto the basic trajectory selection grid of Jupiter arrival date versus

FIGURE 2.10 TRAJECTORY SELECTION GRAPH, 1978 GRAND TOUR


FIGURE 2.II. MINIMUM FLIGHT TIME TO JUPITER, 1978 GRAND TOUR


FIGLIRE 2.12. PLANET ARRIVAL TIMES, 1978. GRAND TOUR


FIGURE 2.13. PLANET CLOSEST APPROACH DISTANCES, 1978 GRAND TOUR .


FIGURE 2.I4. PLANET ARRIVAL VELOCITY, 1978 GRAND TOUR


FIGURE 2.15 SATURN'S RINGS AND SURFACE CONSTRAINTS, 1977 GRAND TOUR

Earth launch dnte. Also shown is the constraint region corresponding to launch declinations greater than $34^{\circ}$. Saturn's surface is the governing "hard" constraint of Grand Tour trajectories in 1977 and 1978. That is, the surface constraint boundary of Jupiter and Uranus lies below that of Saturn. The Cassini Gap between Ring's A and B is about 4000 km wide and offers a pntential, but somewhat daring, trajectory selection. Some level of material density below that of the Kings proper is likely to exist in the Cassini Gap.

Figure 2.16 shows the constraint regions imposed by the $\pm 10$ day Earth-planet conjunctionbands. In cases where the conjunction bands of two planets overlap, only a single constraint region is shown. For a given planet, the real time difference between successive conjunctions is aboat one year - approximately the synodic period between Earth and the outer planets. Of course, when projected onto a grid of Jupiter arrival date, this difference contracts for Saturn, Uranus and Neptune. Also, on this grid, the frequency of conjunction is highest for the outermost planet.

Figure 2.17 combines the four constraint conditions and again shows the launch velocity contours. A launch window of about 20 days is thought to be a reasonable requirement for this mission. To minimize the launch velocity spread throughout the window it is desirable that the center


FIGURE 2.16 EARTH-PLANET CONJUNCTION CONSTRAINTS, 1977 GRAND TOUR


FIGURE 2.17 TRAJECTORY SELECTION GRAPH, 1977 GRAND TOUR
of the window lie near the optimum launch date. fearly, then, the constraint regions leave little room for $\circ$ - lecting trajectories. Two types of trajectories are selested and designated by their principal characteristics:
(1) Exterior Ring Passags - a trajectory passing through the Saturn Ring plane at a distance above the outer Ring boundary.
(2) Interior Ri:g Passage - a trajectory passing through ie Saturn Ring plane at a distance betwer: the surface and the inner Ring E. undary.
A. third trajectory selection passing through the Cassini Gap in the Rings is also indicated on the graph. Hc rever, because of the unknown material density in the Gap this trajectory could be risky. Since data for this trajectory would be bounded by the other two trajectory types, the Cassini Gap passage will not be considered further in this report.

On the question of Ring density, there is certain to be found some particulate matter outside of the visible boundaries of the Rings. For this reason it is best to choose an Exterior trajectory sufficiently above the visible boundary of Ring A. The trajectory selection shown in Figure 2.17 passes about $20,000 \mathrm{~km}$ outside of this boundary.

There remains the task of selecting the Neptune encounter conditions. The selection is made on the basis of the $3 \sigma$ guidance error dispersion ellipse such that Earth occultation is obtained but not Canopus occultation, From the guidance analysis, it is estimated that $3 \sigma_{B \cdot T} \times 3 \sigma_{B \cdot R}$ is $45,000 \times 39,000 \mathrm{~km}$ for the Exterior Ring Passage and $38,000 \times 36,000 \mathrm{~km}$ for the Interior Ring Passage. Figures 2.18 and 2.19 illustrate the nominal aim point selection for these two trajectories. The selection graphs show the occultation zones of the Earth, Sun and Canopus plotted in target plane coordinates. The occultation boundary (from the exact moment of occultation) has been specified as $0^{\circ}, 5^{\circ}$, and $20^{\circ}$ respectively, for the Earth, Sun and Canopus.

Figures 2.20 to 2.24 illustrate the selection process for the 1978 launch opportunity. Descriptive parameters of the four trajectory selections (1977-E, 1977-I, 1978-E, 1978-I) are 1 isted in Table 2.2. Interior Ring Passages are characterized by faster trip times and closer flyby distances, but require higher launch velocities than the Exterior Ring Passages and also have higher approach velocities. Launches in 1978 allow somewhat shorter trips at the expense of higher launch velocities, but pass Jupiter at much greater distances than do trajectories in 1977. The implication of these comparative characteristics will be more fully discussed in the later sections on guidance, scientific payload selection, and mission requirements. IIT RESEARCH INSTITUTE


FIGURE 2.18. OCCULTATION ZONES AND TRAJECTORY SELECTION FOR NEPTUNE ENCOUNTER, 1977-E GRAND TOUF


FIGURE 2.19 OCCULTATION ZONES AND TRAJECTORY SELECTION FOR NEPTUNE ENCOUNTER, 1977-I GRAND TOUR.


FIGURE 2.20 SATURN'S RINGS AND SURFACE CONSTRAINTS, 1978 GRAND TOUR


FIGURE 2.21 EARTH-PLANET CONJUNCTION CONSTRAINTS, 1978 GRAND TOUR


FIGURE 2.22. TRA, IECTORY SELECTION GRAPH, 1978 GRAND TOUR


FIGURE 2.23. OCCULTATION ZONES AND TRAJECTORY SELECTION FOR NEPTUNE ENCOUNTER, 1978-E GRAND TOUR.


FIGURE 2.24. OCCULTATION ZONES AND TRAJECTORY SELECTION FOR NEPTUNE ENCOUNTER, 1978-I GRAND TOUR.

Table 2.2
gRand tour trajectory selections (Continued)

| Trajectory Parameters | 1977 Grand Tours |  | 1978 Grand Tours |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { Exterior Ring } \\ \text { Passage } \\ \text { 1977-E } \end{gathered}$ | $\begin{aligned} & \text { Interior Ring } \\ & \text { Passage } \\ & \text { 1977-I } \end{aligned}$ | Exterior Ring Passage 1978-E | Interior Ring Passage 1978-I |
| Jupiter Encounter |  |  |  |  |
| Sun Occultation ( $5^{\circ}$ ) | 13.3 hrs | 2.9 hrs | 120.2 hrs | 13.6 hrs |
| Earth Occultation ( $0^{\circ}$ ) | 3.9 | 1.9 ( | 120.8 hrs | 13.6 5.0 |
| Canopus Occulcation (20 ${ }^{\circ}$ ) | 0 | 0 | 0 | 0 |
| Saturn Encounter |  |  |  |  |
| Sun Occultation | 2.1 | 1.1 | 2.1 | 1.2 |
| Earth Occultation | 1.6 | 1.0 | 1.8 | 1.1 |
| Canopus Occultation | 0 | 0 | 0 | 0 |
| Uranus Encounter |  |  |  |  |
| Sun Occultation | 3.1 | 1.1 | 3.1 | 1.2 |
| Earth Occultation | 0.1 | 0.9 | 0 | 0.8 |
| Canopres Occultation | 0 | 0 | 0 | 0 |
| Neptune Encounter |  |  |  |  |
|  | 1.7 | 0.8 |  |  |
| Earti Occultation | 1.0 | 0.6 | 1.0 | 1.3 0.9 |
| Canopus Occultation | 0 | 0 | 0 | 0.9 |

It is of interest to know the viriation of trajectory parameters throughout the 20 day launch window. Figures 2.25 and 2.26 show the launch window energy requirements for the 1977 and 1978 Grand Tour. It has been found that planet encountar parameters vary iittle over the window. This is shown, for example, by Tabie 2.3 which iists several key parameters of the 1977-E trajectory.
2.6 Planet Encounter Profiles

Several fixed parameters of the planet encounter trajectories have been given in Table 2.2. Since the Grand Tour missic: is planet oriented, the time history of certain variables of motion during the encounter phase is of general interest, and is also necessary to the proper selection of scientific payloads. In this section, the dynanical profiles of each planet encounter are illustrated for the 1977 m and 1977-I trajectories.

Profile data was obtained from a computer program (PROFYL) developed for this study. The PROFYL output is of two kinds:
(1) A summary table of the occultations of the Earth, Sun and Canopus, and the crossing of the subssatellite point over the Sun terminator line. Associated with each of these points is the time and radius of occurrence.


FIGURE 2.25 LAUNCH WINDOW ENERGY REQUIREMENTS, 1977. GRAND TOUR


FIGURE 2.26 LAUNCH WINDOW ENERGY REQUIREMENTS, 1978 GRAND TOUR
Table 2.3 PARAMETER VARIABLE ACROSS LAUNCH WINDOW

| Trajectory Parameters | Units | Launch Date (Noon) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
|  |  | 8/22 | 8/27 | 9/1 | 9/6 | 9/11 |
| Earth Departure |  |  |  |  |  |  |
| Ideal Launch Velocity | $\mathrm{ft} / \mathrm{sec}$ | 52,800 | 52,100 | 51,900 | 52,000 | 52,500 |
| Asymptote Declination | deg | 38.0 | 33.5 | 30.5 | 28.2 | 26.3 |
| Jupiter Encounter |  |  |  |  |  |  |
| Flight Time | days | 692 | 687 | 682 | 677 | 672 |
| Hyperbolic Velocity | km/ sec | 7.79 | 7.80 | 7.81 | 7.83 | 7.85 |
| Pericenter Distance | radii | 10.50 | 10.60 | 10.62 | 10.61 | 10.58 |
| Saturn Encounter |  |  |  |  |  |  |
| Fight Time | years | 4.01 | 4.00 | 3.98 | 3.97 | 3.96 |
| Hyperbolic Velocity | $\mathrm{km} / \mathrm{sec}$ | 10.66 | 10.67 | 10.69 | 10.72 | 10.74 |
| Pericenter Distance | radii | 2.60 | 2.59 | 2.58 | 2.57 | 2.56 |
| Uranus Encounter |  |  |  |  |  |  |
| Flight Time | years | 8.45 | 8.41 | 8.40 | 8.38 | 8.35 |
| Hyperbolic Velocity | km/sec | 14.71 | 14.72 | 14.74 | 14.77 | 14.80 |
| Pericanter | radii | 5.62 | 5.60 | 5.58 | 5.55 | 5.51 |
| Neptune Encounter |  |  |  |  |  |  |
| Flight Time | years | 12.00 | 11.98 | 11.94 | 11.90 | 11.87 |
| Hyperbolic Velocity | km/sec | 16.50 | 16.51 | 16.54 | 16.57 | 16.60 |
| Pericenter Distance | radii | 3.43 | 3.43 | 3.43 | 3.43 | 3.43 |

(2) Position dependent data of selected dynamic variables such as time-to-periapse, altitude, ground speed, etc. True anomaly is used as the independent position variable because of its relative uniformity over different planet encounters.

Graphical presentation of the profile data is given in Figure 2.27 to 2.39 for the $1977-E$ mission, and in Figures 2.40 to 2.52 for the $1977-$ I mission. The type of information displayed is as follows:
(1) Pictorial trajectory in plane of motion
(2) Time-to-periapse versus true anomaly
(3) Altitude versus true anomaly
(4) Sun elevation versus true anomaly
(5) Scan rate versus true anomaly
(6) Percent of "visible" hemispheric surface versus true anomaly
(7) Ground trace (1atitude, longitude) of subsatellite point.

Sun elevation refers to the angle of the Sun above the local horizontal at the subsatellite point. Scan rate is the ground speed of the spacecraft with respect to the planet's surface, and hence, includes a component of the planet's rotational velocity. The equator of the planet is the reference plane for the ground trace plots. Here, longitude is a relative coordinate since the zero longitude line is arbitrarily defined at initiation of the PROFYL data sequence.




FIGURE 2.30. NEPTUNE ENCOUNTER TRAJECTORY, 1977-E GRAND TOUR


FIGURE 2.3 i. TIME-TO-PERIAPSE VS.TRUE ANOMALY, 1977-E GRAND TOUR.

figure 2.32 altitude vs. true anomaly, 1977-e grand tour


FIGURE 2.33. SUN ELEVATION AT PLANET ENCOUNTEAS, I977-E GRAND TOUR


FIGURE 2.34. GROUND SPEED AT PLANET ENCOUNTERS, 1977-E GRAND TOUR


FIGURE 2.35. VISIBLE HEMISPHERIC AREA AT PLANET ENCOUNTERS, 1977-E GRAND TOUR


 -- SUBSATELLITE POINT IN SUNLIGHT
$h=$ TIME $\mathbb{N}$ HOURS FROM PERIAPSE $h=$ TIME $\mathbb{N}$ HOURS FROM PERIAPSE
$R=$ DIST. FROM PLANET IN RADII



$\qquad$
$\qquad$

FIGURE 2.38 GROUND TRACE OF URANUS FLYBY, I977-E GRAND TOUR

FIGURE 2.39 GROUND TRACE OF NEPTUNE FLYBY, 1977-E GRAND TOUR





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FIGURE 2.44. TIME-TO-PERIAPSE VS. TRUE ANOMALY, 1977-I GRAND TOUR
 IGURE 2.45 ALTITUDE VS. TRUE ANOMALY, 1977 -I GRAND TOUR


FIGURE 2.46. SUN ELEVATION AT PLANET ENCOUNTERS, 1977-I GRAND TOUR


FIGURE 2.47. GROUND SPEED AT PLANET ENCOUNTERS, 1977-I GRAND TOUR


FIGURE 2.48. VISIBLE HEMISPHERIC AREA AT PLANET ENCOUNTERS, 1977-I GRAND TOUR

FIGURE 2.49. GROUND TRACE OF JUPITER FLYBY, 1977-I GRAND TOUR

FIGURE 2.5I. GROUND TRACE OF URANUS FLYBY, 1977-I GR.AND TOUR.

FIGURE 2.52. GROUND TRACE OF NEPTUNE FLYBY, 1977-I GRAND TOUR
SECTION 3
GUIDANCE ANALYSIS AND REQUIREMENTS
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## 3.

GUIDANCE ANALYSIS AND REQUIREMENTS
The so-called "free" energy addition and velocity deflection available from an unpowered planetary swingby is, in reality, obtained at some expense to the spacecraft guidance (propulsion) system. Intermittent velocity corrections are required to compensate for a number of trajectory error sources. Since the trajectory error sensitivity is quite severe in the case of the multiple swingby Grand Tour, the guidance considerations are of major importance to the mission designer.

Error sensitivity of the aim points between successive target planets is shown in Table 3.1 for the two trajectory selections in 1977. It is noted that the trajectory passing inside of Saturn's Rings is about 3 to 4 times more sensitive to errors than the trajectory passing outside of the Rings. It may be expected, then, that the Interior Ring Passage Mission will incur a higher guidance $\Delta V$ penalty. For either trajectory, it is found that the Saturn-Uranus leg and the Uranus-Neptune leg have nearly the same sensitivity, but that the sensitivity of the Jupiter-Saturn leg is more than an order of magnitude smaller. Accordingly, the $\Delta V$ requirement at Jupiter encounter may be expected to have a relatively small contribution to the total $\Delta V$.

As an example of the "astronomical" error that would result if no corrective guidance maneuvers were made, consider the least sensitive of the two trajectories. IIT RESEARCH INSTITUTE

## TABLE 3.1



The error at Neptune may be estimated by multiplying together the intermediate sensitivities. Thus,

$$
\begin{aligned}
\frac{\Delta B_{\text {Neptune }}}{\Delta B_{\text {Jupiter }}} & \approx 400 \times 5600 \times 4500 \\
& \approx 10^{10} \frac{\mathrm{~km}}{\mathrm{~km}}
\end{aligned}
$$

To make matters even worse, the error at Jupiter will certainly be several orders of magnitude greater than 1 km . Clearly, multiple trajectory corrections ears te will be required to insure success of the Grand Tour Mission.

Guidance maneuvers will be specified on both the approach and departure legs of the swingby trajectory at each intermediate planet. Using the Saturn encounter as an example, Figure 3.1 illustrates the guidance policy and the factors of influence. The approach maneuver is necessary to reduce the target errors due to (1) $\Delta V$ execution error at the previous planet departure, (2) orbit determination errors at that time, and (3) planet ephemeris errors. The departure maneuver is necessary to compensate for the magnification effects of the gravitational swingby on the orbit determinecion error which exists at the time of executing the final approach maneuver. .

Objectives of the guidance analysis are (1) to obtain an understanding of the guidance problem in terms of its factors of influence, (2) to determine realistic estimates it t research institute


APPROACH MANEUVER: CORRECT SATURN MISS ERROR DUE TO
(1.) $\triangle V$ EXECUTION ERROR AT JUPITER UEPARTURE
(2.) ORBIT DETERMINATION ERROR AT JUPITER DEPARTURE
(3.) SATURN'S EPHEMERIS ERROR
departure maneuveri correct uranus miss error due to
(1.) ORBIT DETERMINATION ERROR AT FINAL SATURN APPROACH MANEUVER

APPROACH ORBIT DETERMINATION: ERROR ANALYSIS COMPARING
(1.) EARTH-BASED RADAR TRACKING (DSIF)
(2.) ON-BOARD CELESTIAL TRACKING (PLANET TRACKEP?

FIGURE 3.1 ILLUSTRATION OF GUIDANCE MANEUVERS-SATURN ENCOUNTER.
of the spacecraft propulsion system ( $\Delta V$ ) requirements, and (3) to ascertain the tradeoffs available between the $\Delta V$ requirements, the method and accuracy of orbit determination, and the trajectory selection. Standard methods of differential trajectory correction and statistical covariance analysis are employed in deriving the guidance results. A comparison is made of two instrumentation systems for planet approach orbit determination, namely, Earth-based radar tracking and on-board celestial tracking.

### 3.1 Orbit Determination Analysis

For a given trajectory selection, the guidance $\Delta V$ requirement is most deperdent upon the accuracy of orbit determination of the spacecraft relative to the swingby planets. This is so because the departure maneuvers, especially at Saturn and Uranus, are found to be the largest contributors to the total $\Delta V$. A major phrie of the present study was therefore concerned with obtaining reasonable estimaies of the orbit determination errors.

At planet approach (sphere of influence), the a priori uncertainty in the miss vector is due to the planet ephemeris error and the error remairing after tracking the spacecraft throughout the previous midcourse phase. Reduction of the a priori uncertainty can be accomplished by continued tracking during the approach phase. The
degree of reduction attainable will depend upon the type of tracking system employed and upon the instrumentation errors. Two such systems are postulated for study. The first is Earth-based radar tracking (e.g., DSIF) which is currently the only system in actual use for deep space probes. It is assumed that Earth-based tracking will be the primary or only technique used during midcourse tracking of the Grand Tour. The data type assumed is sampled doppler, or, equivalently, range-rate measurements. Any improvement in orbit determination by continued radar tracking during planet approach must rely on the inherent trajectory kinematics, i. e., the effect of gravitational bending as reflected in the doppler residuals. Generally, this effect is not very significant at large range from the planet.

The second tracking model assumes an on-board celestial system, e.g., sun sensors, a Canopus tracker and a planet tracker. It is likely that the sun sensors and Canopus tracker will be on-board in any case for attitude control purposes through the flight. The additional instrument then is the planet tracker which would be operational only in the planetocentric region. The celestial data types are the directional angles of the planet as seen from the spacecraft. In contrast to Earth-based tracking, the on-board system need not rely on the gravitational bending effect since
direct reference is made to the planet. This offers the potential for more accurate orbit determination earlier in the approach phase.

With reference to Figure 3.2, two separate computer programs were developed to evaluate the performance of each tracking system. In each case, the trajectories are modeled as hyperbolic conics, analytical partial derivatives are derived from the conic formulas, and the motion and measurement variables are referred to the planetocentric STR coordinate frame. Since the various error sources are best described in a statistical manner, the approach taken is to compute the error covariance matrix associated with estimating the target parameters. Optimal statistical filtering of the tracking data is assumed for the analysis. Both the Kalman filter and Weighted Least-Squares algorithms (for covariance computation) are available as options to each program. It was found that each algorithm gives approximately the same results. Generally, however, the Kalman approach was used for celestial tracking, and the LeastSquares approach was used for radar tracking. Further details of the analytical basis for the two programs are given elsewhere (Friedlander 1967) and (Gates 1964).


FIGURE 3.2 METHOD OF GUIDANCE ANALYSIS

The NBODY Guidance Program illustrated in Figure 3.2 is simply a set of subroutines of the Targeting Program which compute the necessary partial derivative matrices along the nominal trajectory legs, and also the covariance matrices of the guidance maneuvers. The mapping matrix between target planes of the form $\partial \underline{m}_{2} / \partial \underline{m}_{1}$ is constructed by finite difference quotients as part of the targeting scheme, A11 other mapping matrices are obtained by integrating the first-order-variational equations of position and velocity.

The first guidance maneuver would take place several days after launch to compensate for the injection errors in position and velocity. If $\Lambda_{\text {xo }}$ denotes the $6 \times 6$ covariance matrix of injection errors, then the error covariance matrix mapped to the Jupiter target plane is

$$
\begin{equation*}
\Lambda_{m_{10}}=\left[\frac{\partial \underline{m}}{\partial \underline{x}_{0}}\right] \quad \Lambda_{x_{0}}\left[\frac{\partial \underline{m}}{\partial \underline{x}_{0}}\right]^{T} \tag{3,1}
\end{equation*}
$$

Then, for the first guidance manetiver,

$$
\begin{equation*}
\Lambda_{\Delta V_{1}}=\left[\frac{\partial \underline{m}}{\partial \underline{v}_{1}}\right]^{-1} \quad \Lambda_{m_{10}}\left[\frac{\partial \underline{\underline{m}}}{\partial \underline{v}_{1}}\right]^{-1} \tag{3.2}
\end{equation*}
$$

It should be noted that all guidance maneuvers correct the inpact parameters $\underline{\Delta} \underline{B} \cdot \underline{T}, \Delta \underline{B} \cdot \underline{R}$ and the time of encounter $\Delta \mathrm{T}_{\mathrm{e}}$. Hence, complete freedom in the magnitude and direction of the velocity correction is assumed. At this point it will be expedient to consider the general case of the approach and departure maneuvers at the $k$-th planet.

The effect of maneuver execution errors are considered important only for the planet departure maneuvers. This is because the time available to propagate these errors during planet approach is small in comparison to the midcourse times. The execution model assumed is a spherically distributed error proportional to the RMS magnitude of the maneuver. Thus, for the planet departure maneuver the execution covariance j.s

$$
\begin{align*}
\Lambda_{\varepsilon x}^{(k-1)} & =\sigma_{\varepsilon x}^{2} \overline{\Delta V}_{\text {dep }}^{2(k-1)} \cdot I  \tag{3.3}\\
\overline{\Delta V}_{\text {dep }}^{2(k-1)} & =\operatorname{Trace} \Lambda_{\Delta V, \text { dep }}^{(k-1)} \tag{3.4}
\end{align*}
$$

where $I$ is a $3 \times 3$ identity matrix. The effect of the execution errors is mapped to the next planet by

The uncertainty in determining the spacecraft velocity just prior to the departure maneuver contributes a target error covariance $\Lambda_{m, O D}^{(k)}$ which is found by mapping similar to Eq. (3.5). Now, adding the ephemeris error of the target planet, the total error to be corrected by the approach maneuver is

$$
\begin{equation*}
\Lambda_{\mathrm{m}}^{(\mathrm{k})}=\Lambda_{\mathrm{m}, \mathrm{ex}}^{(\mathrm{k})}+\Lambda_{\mathrm{m}, \mathrm{OD}}^{(\mathrm{k})}+\Lambda_{\mathrm{m}, \mathrm{eph}}^{(\mathrm{k})} \tag{3.6}
\end{equation*}
$$

The approach maneuver is evaluated at a sequence of ranges $\left\{R_{i}\right\}$ from the planet beginning at about the sphere of influence. The maneuver covariance is given by

$$
\begin{equation*}
\Lambda_{\Delta V, a p p}^{(k)}=\left[\frac { \partial \underline { m } ^ { ( k ) } } { ( k ) } \left[-1 \quad \Lambda_{m}^{(k)}\left[\frac{\partial \underline{m}_{a p p}^{(k)}}{\partial v_{a p p}}\right]\left[-1^{T}\right.\right.\right. \tag{3.7}
\end{equation*}
$$

For the same range sequence, the approach orbit determination error covariance $P_{0 D}^{(k)}$ is mapped into target errors at the next planet,

$$
\begin{equation*}
\Lambda_{m}^{(k+1)}=\left[\frac{\partial \underline{m}^{(k+1)}}{\partial \underline{m}^{(k)}}\right] \quad p_{0 D}^{(k)}\left[\frac{\partial \underline{m}^{(k+1)}}{\partial m^{(k)}}\right]^{T} \tag{3.8}
\end{equation*}
$$

and the departure maneuver covariance is computed from

$$
\begin{equation*}
\left.\Lambda_{\Delta V, \operatorname{dep}}^{(k)}=\left[\frac{\partial_{m}^{(k+1)}}{\partial \underline{v}_{\text {dep }}}\right]^{-1} \Lambda_{m}^{(k+1)}\left[\frac{\partial_{m}^{(k+1)}}{\frac{\partial v_{\text {dep }}}{(k)}}\right]^{-1}\right]^{T} \tag{3.9}
\end{equation*}
$$

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It is assumed that the departure maneuver is made at the planet's sphere of influence.

Finally, an approximate optimization of the maneuvers at each planet is accor $\sim 1$ ished by finding that $R_{i}$ which results in a minimum sum of the approach and departure velocity corrections (RMS values). The individual maneuver RMS values are then taken corresponding to the optimal $R_{i}$. If two approach maneuvers are allowed, the first is made at $\mathrm{R}_{1}$ which is about $50 \times 10^{6} \mathrm{~km}$ from the planet. Then, the second maneuver must correct the approach orbit determination error at that point i.e., $P_{0 D}^{(k)}\left(R_{1}\right)$. Substituting this new value for $\Lambda_{m}^{(k)}$ in Eq. (3.7), the second maneuver is evaluated at the ::emaining points $R_{2}, R_{3}, \ldots R_{N}$.

The previous Eqs. (3.8) and (3.9) describe how errors in the arrival conditions at one planet are propagated to the next, and determine the planet departure maneuver necessary to correct these errors. Since mere substitution of numerical values for the partial derivative matrices would contribute little to a basic understanding of the problem, it would be helpful to describe the error sensitivity by analytical expressions. Such expressions may be derived using the conic formulas of the hyperbolic encounter.

To simplify the problem, it is assumed that the departure maneuver nulls the error in the departure hyperbolic velocity vector. The encounter time error is neglected since
its effect is small in comparison to errors in $b$ and $\theta$. From Eqs. (2.3) to (2.10), the sensitivity of the departure velocity may be expressed as

$$
\begin{align*}
\frac{\partial \underline{V}_{h 2}}{\partial b}= & \frac{V_{h}^{3}(1-\cos \psi)}{\mu}[\sin \psi \underline{S}+\cos \psi \cos \theta \underline{T} \\
& +\cos \psi \sin \theta \underline{R}]  \tag{3.10}\\
\frac{\partial \underline{V}_{h 2}}{b \partial \theta}= & \frac{V_{h} \sin \psi}{b}[\sin \theta \underline{T}-\cos \theta \underline{R}] \tag{3.11}
\end{align*}
$$

Since we have assumed $\Delta V_{\mathrm{dep}}^{2} \approx \Delta \underline{\mathrm{~V}}_{\mathrm{h} 2} \cdot \Delta \underline{\mathrm{~V}}_{\mathrm{h} 2}$,

$$
\begin{aligned}
\Delta V_{\text {dep }}^{2} \approx & {\left[\frac{\partial \underline{V}_{h 2}}{\partial b} \cdot \frac{\partial \underline{V}_{h 2}}{\partial b}\right]^{2}(\Delta b)^{2} } \\
& +\left[\frac{\partial \underline{V}_{h 2}}{b \partial \theta} \cdot \frac{\partial \underline{V}_{h 2}}{b \partial \theta}\right]^{2}(b \Delta A)^{2} \\
= & {\left[\frac{V_{h}^{3}(1-\cos \psi)}{\mu}\right]^{2}(\Delta b)^{2}+\left[\frac{V_{h} \sin \psi}{b}\right]^{2}(b \Delta \theta)^{2} }
\end{aligned}
$$

Using Eq. (2.6), the bracketed terms above are found to be equal. Therefore, the departure meneuver is equally sensitive to in-plane and out-of-plane error components of $\underline{B}$ (actually, the orbit determination errors)

$$
\begin{equation*}
\Delta V_{\text {dep }} \approx\left(\frac{V_{h} \sin \psi}{b}\right)\left[(\Delta b)^{2}+(b \Delta A)^{2}\right] 1 / 2 \tag{3.12}
\end{equation*}
$$

From Table (2.1), it is seen that the parenthetical sensitivity factor in Eq. (3.12) is much larger for the Interior Ring Passage trajectories. Also, this factor is generally smallest for the Jupiter swingby and largest for the Uranus swingby. Taking the 1977-I mission as an example, the maneuver sensitivity at Jupiter, Saturn and Uranus is, respectively, 16, 113 and $165 \mathrm{~m} / \mathrm{sec}$ per 1000 km .

An approximate analytical expression for the approach maneuver may be derived quite simply. Assume that the approach maneuver is made at a range $R \gg b$, and that this maneuver nulls the two error components of $\underline{B}$ but neglects the error in encounter time. Then, for a field-free space approximation

$$
\begin{equation*}
\Delta V_{a p p} \approx \frac{V_{h}}{R}\left[(\Delta b)^{2}+(b \Delta A)^{2}\right] 1 / 2 \tag{3.13}
\end{equation*}
$$

which shows the maneuver sensitivity to be inversely proportional to range. Equations (3.12) and (3.13) are very useful in checking and interpreting the numerical results obtained from Eqs. (3.7) to (3.9).

Table 3.2 lists the various error sources considered in this study. Items 3,4 and 5 contribute directly to trajectory errors (perturbations), whereas the remaining terms contribute to trajectory uncertainty via the orbit determination process. Midcourse disturbances due to solar pressure uncertainties and attitude control gas leaks are for ad to have a relatively snall effect for this mission. The injection accuracy assumed is typical of a Cenraur upper stage launch vehicle. It is noted, however, that injection errors have a small effect on the total $\Delta V$ requirements of this mission. The maneuver execution error of $1 \%$ is perhaps somewhat conservative for a post-1975 attitude control system. Planet ephemeris errors of 0.2 sec arc in latitude and longitude are representative of the best astrometric observations from Earth. The data noise and station location errors assumed for radar tracking represent the projected improvement in the DSIF accurasy (JPL Series, SPS Vol. III). Optical sensor errors assumed for the on-board tracking mode are typical of such systems currently under development (Barone 1967). The designation "a priori" in Table 3.2 means initial values of error sources which are also being estinsated along with the miss vector. For example, the gravitational constant uncertainty is greaty reduced during the radar tracking mode. Compensation for the data bias is also effective as on-board observations are accumulated.

TABLE 3.2 ASSUMED ERROF SOURCES (RMS VALUES)

1. PLANET EPHEMERIS (A Priori)

Latitude, Longitude 0.2 sec arc
Radial Distance $\quad R_{p}$ (AU) $\times 200 \mathrm{~km}$
2. TIANET GRAVITATIONAL CONSTANT (A P:iori)
$0.1 \%$
3. MIDCOURSE DISTURBANCES

Solar Pressure $5 \%$ Uncertainty Negligible Gas Leaks $10^{-10} \mathrm{~m} / \mathrm{sec}^{2}$ Effect
4. INJECTION ACCURACY

Position
10 km
Velocity
$16 \mathrm{~m} / \mathrm{sec}$
5. MANEUVER EXECUTION ERROR

1\% Spherically Distributed
6. EARTH-BASED RADAR TRACKING

| Data Samples | 480 sec |
| :--- | :--- |
| Data Noise | $0.005 \mathrm{~m} / \mathrm{sec}$ |
| Station Location | 3 m |

7. ON-BOARD CELESTIAL TRACKING

Data Samples
2 hrs
Data Noise
Data Blas
Planet Center Finder Bias

6 sec arc
200 sec arc (A Priori)
0.3\% Planet Diameter (A Priori)

## 3.3 .1

Orbit Determination Errors
The error analysis was applied to each of the four trajectory selections. On-board planet tracking was found to be superior to Earth-based radar tracking in determining the miss components at each planet. The only exception to this is the Jupiter approach where the in-plane miss uncertainty, $\sigma_{b}$, is less in the case of radar tracking. A comparison of the two tracking modes for the 1977-I Grand Tour is shown in Figures 3.3 to 3.8. The RMS uncertainties of the in-plane and out-of-piane miss components are plotted as a function of range to the planet beginning at the initial data acquisition range of $50 \times 10^{6} \mathrm{~km}$. It is noted that celestial tracking is effective in reducing the uncertainties in both miss components, whereas radar tracking information is rather insensitive to the out-of-plane component.

Taking the Uranus encounter as a worst case comparison, it is seen that radar tracking yields little or no reduction of the initial uncertainty until the range decreases to about $2 \times 10^{6} \mathrm{~km}$. At this point the gravitational bending effect becomes more pronounced. Even then, the out-of-plane component remains poorly determined until nearer closest approach. In contrast, celestial tracking yields an early and continuing reduction of the miss uncertainty. For example, at a range of $25 \times 10^{6} \mathrm{~km}, b \sigma_{\rho}$

TRACKING CONDITIONS


FIGURE 3.3 N-PLANE MISS UNCERTAINTY FOR JUPITER APPROACH ORBIT DETERMINATION, 1977 -I GRAND TOUR
I $=$ (1000

FIGURE 3.4 OUT-OF-PLANE MISS UNCERTAINTY FOR JUPITER APPROACH ORBIT DETERMINATION, 1977-I GRAND TOUR


FIGURE 3.5 IN-PLANE MISS UNCERTAINTY FOR SATURN APPROACH ORBIT DETERMINATION, 1977-I GRAND TOUR


FIGURE 3.6 OUT-OF-PLANE MISS UNCERTAINTY FOR 1977-I GRAND TOUR


FIGURE 3.7 IN-PLANE MISS UNCERTAINTY FOR URANUS APPROACH ORBIT DETERMINATION, 1977 - I GRAND TOUR.


FIGURE 3.8 OUT-OF-PLANE MISS UNCERTAIMTY FOR URANUS APPROACH ORBIT DETERMINATION, 1977-I GRAND TOUR
is 5600 km for radar tracking but on 1 y 440 km for celestial tracking. At a range of $: 0^{6} \mathrm{~km}$, the respective uncertainties are 2800 km and 160 km .

Earth-based radar tracking gives better results in estimating the encounter time and the planet's gravitational constant. This is shown for each of the planets in Figures 3.9 and 3.10.

### 3.3.2 Scheduling of Guidance Maneuvers

As a result of the orbit determination characteristics, the $\Delta V$ cost of guidance for the Grand Tour can be quite sensitive to the times at which the planet approach maneuvers are made. The opportunity for minimizing the total $\Delta V$ requirement by appropriately scheduling the maneuvers cannot afford to be neglected. To illustrate this point, consider the Uranus swingby on the 1977-I mission. Figure 3.11 shows the approach maneuver requirements as a function of planet range. The celestial tracking mode requires a smaller $\Delta V$ for a single correction because the approach error is smaller. This simply reflects the better showing of celestial tracking at Saturn; more accurate orbit determination implies a small departure maneuver which in turn implies smaller execution errors. Figure 3.12 compares the two tracking modes for the Uranus departure maneuver. This result reflects the orbit determination accuracy of Figures 3.7 and 3.8.


FIGURE 3.9 ENCOUNTER TIME UNCERTAINTY FROM PLANET APPROACH ORBIT DETERMINATION, 1977-I GRAND TOUR


FIGURE 3.10 DETERMINATION OF GRAVITATIONAL CONSTANT (MASS) DURING PLANET SWINGBY, 1977-I GRAND TOUR


FIGURE 3.11 VELOCITY CORRECTIOH REQUIREMENT FOR URANIS DEPARTURE, 1977 - I GRAMD TCUR


FIGURE 3.12 VELOCITY CORRECTION REQUIREMENT FOR URANUS APPROACH, 1977-I GRAND TOUR

Optimization of the Uranus encounter maneuvers is illustrated in Figure 3.13. If only one approach maneuver were allowed, the minimum mean sum $\Delta V$ at Uranus encounter is $1100 \mathrm{~m} / \mathrm{sec}$ for radar tracking, but only $200 \mathrm{~m} / \mathrm{sec}$ for celestial tracking. Allowing two approach maneuvers reduces the requirement to $680 \mathrm{~m} / \mathrm{sec}$ and $110 \mathrm{~m} / \mathrm{sec}$, respectively. For the latter case with radar tracking, the best range for the final approach maneuver is about $10^{6} \mathrm{~km}$, resulting in RMS values for the Uranus maneuvers of 98,133 and $549 \mathrm{~m} / \mathrm{sec}$. For celestial tracking, the optimal range is about $10 \times 10^{6} \mathrm{~km}$, and the RMS values of the maneuvers are 61,14 and $47 \mathrm{~m} / \mathrm{sec}$.

It should be noted that the radar tracking results may be somewhat optimistic since the final approach maneuver is made only 14 hours before encounter (closest approach). The round trip communication time to Uranus is about 5.5 hours. If the maneuver computation and command were Earth-based, this time differential appears to be marginal at best. Even if this were tolerable, the second approach maneuver would increase from $133 \mathrm{~m} / \mathrm{sec}$ to about $220 \mathrm{~m} / \mathrm{sec}$ due to the decreased range over the 5.5 hour period. This fact might be kept in mind when interpreting the sumary results to be given since these results assume an instantaneous correction capability. In other words, the celestial tracking mode may be even more favorable than is apparent.


FIGURE 3.13 OPTIMIZATION OF URANUS ENCOUNTER VELOCITY CORRECTION REQUIREMENTS, 1977 - I GRAND TOUR

Tables 3.3 and 3.4 list the RMS values of the individual guidance maneuvers and the times at which they are made for each of the four trajectory selections and the two tracking modes. These results are obtained by the aforementioned method of minimizing the sum of the approach and departure maneuvers at each planet encounter. The smallest $\Delta V^{\prime}$ 's are associated with the Jupiter encounter and the largest with the Uranus encounter. Total maneuver requirements are listed in terms of a mean +3 sigma value which is based on a Rayleigh distribution matched to the individual RMS values. The Rayleigh distribution has been found to be an excellent approximation to the actual statistical distribution of $\Delta V$ magnitude (Sturms 1966).

The effect of the trajectory selection and the orbit determination tracking mode is summarized by the matrix of total $\Delta V$ requirements shown in Table 3.5. In the case of radar tracking, the total $\Delta V$ could be as small as $354 \mathrm{~m} / \mathrm{sec}$ for the 1978 -E mission or as high as $1712 \mathrm{~m} / \mathrm{sec}$ for the 1977-I mission. The large $\Delta V$ difference between the Interior Ring Passages of 1977 and 1978 is attributed to larger orbit determination (radar) errors at Saturn and Uranus for the 1977 mission. This is due to differences in planet approach geometry as viewed from the Earth. A comparison of the two tracking modes shows a very

TABLE 3.3 GRAND TOUR $\triangle V$ REQUIREMENTS FOR EARTH-BASED RADAR TRACKING

| GUIDANCE MANEUVERS | Grand Tour Trajectories |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 1977-E | 1977-I | 1978-E | 1978-I |
| Post-Earth Injection ( $\mathrm{I}+10 \mathrm{~d}$ ) | 13 . | 9 | 9 | 9 |
| Jupiter Approach | $5(E-66 d)$ | 4 (E-37d) | 3 (E-52d) | 4 (E-32d) |
| Jupiter Departure | 10 (E+64d) | 29 (E+43d) | 7 ( $\mathrm{E}+50 \mathrm{~d}$ ) | 19 ( $\mathrm{E}+38 \mathrm{~d}$ ) |
| lst Saturn Approach | 11 (E-15d) | 9 (E-34d) | 28 (E-5d) | 5. (E-34d) |
| 2nd Saturn Approach | - | 44 (E-14hr) | - | 25 (E-28hr) |
| Saturn Departure | 69 ( $\mathrm{E}+58 \mathrm{~d}$ ) | 127 ( $E+37 \mathrm{~d}$ ) | 37 (E+55d) | 86 ( $\mathrm{E}+37 \mathrm{~d}$ ) |
| lst Uranus Approach | 48 (E-39d) | 98 (E-27d) | 25 (E-38d) | 63 (E-27d) |
| 2nd Uranus Approach | 48 (E-36hr) | 133 (E-14hr) | 51 (E-36hr) | 131 (E-13hr) |
| Uranus Departure | 62 ( $\mathrm{E}+40 \mathrm{~d}$ ) | 549 (E+28d) | 56 ( $\mathrm{E}+39 \mathrm{~d}$ ) | 260 ( $\mathrm{E}+28 \mathrm{~d}$ ) |
| Uranus-Neptune Midcourse | 10 | 20 | 10 | 10 |
| TOTALS <br> (Mean +3 Sigma)* | $450 \mathrm{~m} / \mathrm{sec}$ | $1712 \mathrm{~m} / \mathrm{sec}$ | $354 \mathrm{~m} / \mathrm{sec}$ | $1010 \mathrm{~m} / \mathrm{sec}$ |

* Based on Assumed Rayleigh Distribution for $\Delta V$ Maneuvers With Full Correlation Between Approach ( $k+1$ ) Maneuver and Departure (k) Maneuver. ${ }^{*} E$ is Time of Encounter.

TABLE 3.4 GRAND TOUR $\triangle V$ REQUIREMENTS FOR ON-BOARD CELESTIAL TRACKING
$\Delta V$ (RMS) , M/SEC

| gUIDANCE MANEUVERS | Grand Tour Trajectories |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 1977-E | 1977-I | 1978-E | 1978-I |
| Post-Earth Injection (I+lod) | 13 | 9 | 9 | 9 |
| Jupiter Approach | 5 (E-66d) | 7 (E-2ld) | 5 (E-23d) | 6 (E-19d) |
| Jupiter Departure | 10 (E+64d) | $20(E+43 \mathrm{C})$ | $4(E+50 d)$ | 11 (E+38d) |
| 1st Saturn Approach | 8 (E-20d) | 22 (E-10d) | 6 (E-13d) | 14 (E-10d) |
| 2nd Satuen Approach | $\longrightarrow$ | - | - | - |
| Saturn Departure | 20 (E+58d) | $79(E+37 \mathrm{~d})$ | 27 (E+55d) | $70(E+37 d)$ |
| 1st Uranus Approach | 30 (E-20d) | 61 (E-27a) | 37 (E-14d) | 51 (E-27d) |
| 2nd Uranus Approach |  | 14 (E-5d) | - | 13 (E-5d) |
| Uranus Departure | $24(E+40 d)$ | 47 (E+28d) | 23 (E+39d) | 35 (E+28d) |
| Uranus-Neptune Midcourse | 5 | 5 | 5 | 5 |
| $\begin{gathered} \text { TOTALS } \\ (\text { Mean }+3 \text { Sigma }) * \end{gathered}$ | 190 m/sec | $428 \mathrm{~m} / \mathrm{sec}$ | $203 \mathrm{~m} / \mathrm{sec}$ | $372 \mathrm{~m} / \mathrm{sec}$ |

*Based on Assumed Rayleigh Distribution for $\Delta V$ Maneuvers With Full Correlation Between Approach ( $k+1$ ) Maneuver and Departure (k) Maneuver.
** E is Time of Encounter.

TABLE 3.5
SUMMARY OF GUIDANCE $\triangle V$ REQUIREMENTS
FOR THE GRAND TOUR MISSION
$\Delta V$ TOTAL (MEAN + 3 SIGMA)*

| TRALECTORY <br> SELECTION | ORBIT DETERMINATION TRACKING CONDITIONS |  |
| :---: | :---: | :---: |
|  | EARTH-BASED RADAR | ON-BOARD CELESTIAL |
| $1977-E$ | $450 \mathrm{M} / \mathrm{SEC}$ | $190 \mathrm{M} / \mathrm{SEC}$ |
| $1977-1$ | 1712 | 428 |
| $1978-E$ | 354 | 203 |
| $1978-1$ | 1010 | 372 |

*BASED ON ASSUMED RAYLEIGH DISTRIBUTION FOR $\triangle V$ MANEUVERS WITH PERFECT CORRELATION BETWEEN APPROACH ( $K+1$ ) MANEUVER AND DEPARTURE ( $K$ ).MANEUVER.
significant advantage to on-board celestial tracking. In this case, the Interior Ring Passages would require about $400 \mathrm{~m} / \mathrm{sec}$, and the Exterior Ring Passages would require only about $200 \mathrm{~m} / \mathrm{sec}$.

The $\Delta V$ 's listed in Table 3.5 are indicative of the total propellant loading of a spacecraft. For example, assuming a propellant specific impulse of 235 seconds, the propellant loading corresponding to $190 \mathrm{~m} / \mathrm{sec}$ is $8 \%$ of the spacecraft weight. The propellant loading corresponding to $1712 \mathrm{~m} / \mathrm{sec}$ is $53 \%$.
3.3.4 Guidance Accuracy
On the question of guidance accuracy, either tracking mode should provide adequate control of the flyby trajectories at each planet for purposes of the scientific experiments to be carried out. Approach guidance accuracy data for the 1977-I Grand Tour is 1isted in Table 3.6. Figures 3.14 to 3.17 illustrate the miss dispersions before and after the approach maneuvers. The most severe guidance accuracy requirement of any of the Grand Tour Missions occurs at Saturn on the Interior Ring Passage trajectory. Here, the spacecraft must pass between the surface and the inner Ring boundary. Figure 3.16 shows that the $3 \sigma$ miss dispersion for either tracking mode meets the accuracy requirement.

TABLE 3.6 GUIDANCE ACCURACY FOR 1977 - 1 GRAND TOUR

| $\text { JUPITER }{ }^{1}$ | EARTH-BASED RADAR |  | ON-BOARD CELESTIAL |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\sigma_{b}$ | ${ }^{\mathrm{bo}} \theta$ | $\sigma_{b}$ | $\mathrm{bo}_{\theta}$ |
|  | 260 km | 840 km | 500 km | 470 km |
| SATURN ${ }^{1}$ | 90 | 880 | 370 | 390 |
| URANUS ${ }^{1}$ | 750 | 2800 | 180 | 190 |
| neptune ${ }^{2}$ | 13,000 | 12,000 | 13,000 | 12,000 |

1. Corresponds to Errors at Final Approach Maneuver.
2. Assumes No Neptune Approach Maneuver. If necessary, this error can be reduced by a factor of 2 or 3 by making a late correction on the Uranus - Neptune trajectory leg. The $\Delta V$ cost should be under $10 \mathrm{~m} / \mathrm{sec}$.

FIGURE $3.14 \quad 3 \sigma$ MISS ELLIPSES FOR JUPITER ENCOUNTER, 1977 I GRAND TOUR


FIGURE 3.16 SATURN APPROACH GUIDANCE ACCURACY 1977-1 GPAND TOUR


FIGURE 3.17 3 $\sigma$ MISS FOR URANUS ENCOUNTER, 1977-I GRAND TOUR

### 3.3.5 Guidance Analysis Summary

From the results of the guidance analysis, the following summary remarks may be made:

1. A1though the guidance requirements of the Grand Thur Mission are much more severe than current planetary missions, they are not beyond the capability of the present or projected state-of-the-art. Multiple guidance maneuvers are necessary to meet the mission requirements. For each planetary swingby, one or two approach maneuvers and one departure maneuver will suffice. A total of $8-10$ maneuvers would be required.
2. The orbit determination process, whether Earthbased radar or on-board celestial tracking, must extent well into the planetary approach phase at Saturn and particularly at Uranus. From the standpoint of guidance accuracy, either tracking mode should be adequate for purposes of the scientific experiments to be carried out.
3. "Interior Ring Passage" missions have a significantly higher guidance $\Delta V$ requirement than "Exterior Ring Passage" missions.
4. The largest $\Delta V$ contribution occurs at the Uranus encounter. The importance of this result is that if a problem of fuel depletion occurs at this late stage in flight, only the Neptune encounter need be sacrificed. In other words, for a multiple target mission, it is desirable that the
large $\Delta V$ corrections occur late rather than early in the flight in order to ethance the probability of mission success for a fixed fuel load.
5. In the interest of minimizing the guidance $\Delta V$ requirements, a strong case is made for having an on-board planet tracking capability. This is particularly true for the most sensitive Interior Ring Passage mission. With onboard tracking the largest total $\Delta V$ requirement is about $400 \mathrm{~m} / \mathrm{sec}$. This is to be compa.ed with $1700 \mathrm{~m} / \mathrm{sec}$ if Earthbased tracking alone were employed. However, if the 1978 Exterior Ring Passage mission were selected, the advantage of on-board tracking is reduced somewhat. In this case the $\Delta V$ requirements are about $200 \mathrm{~m} / \mathrm{sec}$ for on-board tracking and $350 \mathrm{~m} / \mathrm{sec}$ for Earth-based tracking.

## SECTION 4

EVALUATION OF THE SCIENTIFIC OBJECTIVES
Compiled ByK. L. UherkaContributorsA. B. BinderJ. C. JonesD. L. RobertsK. L. Uherka
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4.1 Methodology for Science Selection ..... 131
4.2 Evaluation of Scientific Objectives ..... 135

The detailed trajectory and guidance analyses of Sections 3 and 4 have clearly illustrated the possibility of a multiple outer planet mission which utilizes gravity assist at each target. The ultimate worth or usefulness of such a mission depends on the value of the scientific data that is obtained from measurements. Since the opportunities for a Grand Tour mission encountering all four Jovian planets are rare, occurring approximately every 179 years, it is of the utmost importance that the most effective use is made of the payload capabilities. Therefore it is highly desirable that the selection of scientific experiments for the mission payload be based on a systematic and logical methodology.

The selelection methodology, to be useful, should result in a relative "value" being placed on different scientific experiments so that they can be ranked according to their value of importance. This allows experiments and experiment packages to be selected on the basis of highest values. The worth or value of any experiment depends upon its measurement data, and the percentage contribution that these measurements make toward fulfilling the total scientific goals and objectives of exploration for the outer planets. Hence, a complete methodlogy for mission payload selection must also include a scheme for evaluation and ordering of both the basic science objectives, and the measurables that are of interest.

Section 4.1 below is devoted to the methodology that has been developed by ASC/IITRI to determine the science objectives and measurables that are relevant to the overall scientific goal of Examination of the Jovian Planets and Interplanetary Space. The evaluation scheme and logic used to obtain relative values for the scientific objectives is discussed in Section 4.2. The methodology used to determine the value and priority order of actual spacecraft instrumentation (based on their capability to fulfill the scientific objectives) is covered in Section 5, along with the selection criteria used to obtain mission payloads.

### 4.1 Methodology for Science Selection

The first step in the science evaluation is to obtain a complete listing of the scientific objectives for which measurement data is desirable. To insure completeness, the method of approach starts with a definition of the broad overall Goal of Exploration, which is then further subdivided into subgoals called Exploration Regimes. The Exploration Regimes are more specific than the Goal and also define the scope encompassed by the original goal. The scope of the Exploration Regime subgoals are then further clarified by an additional level of detail which are called Regime Categories. The Regime Categories are then defined by a natural breakdown into Category Objectives, which in turn are subdivided into

Objective Measurables. The Objective Measurables represent the final level of detail and they are directly related to measurable quantities (an example of an Objective Measurable would be "to measure the $\mathrm{NH}_{3}$ abundance in a planetary atmosphere").

Figure 4.1 illustrates the systematic breakdown of a Goal into succcessive levels of detail. It should be emphasized that each level of breakdown as a whole is entirely equivalent to its previous level. It is felt that the methodology adopted there is general in nature and its logical framework is valuable in that it reduces to a minimum any possibility of overlooking important mission science requirements.

The present study is concerned with a mission to the four outer planets, and thus the Goal of Exploration can be taken quite generally as: Examination of the Jovian Planets and the Interplanetary Medium. The detailed breakdown of this goal is shown in Figure 4.2. The first 3 levels of breakdown into Exploration Regimes, Regime Categories and Category Objectives are shown in the illustration, while the results for detailed Objective Measurables are given in the Figures of Section 4.2. The breakdown shown in the block diagram of Figure 4.2 was strongly influenced by the recommendations of the Space Science Board of the National Academy of Sciences (SSB 1966), in that the emphasis is

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figure 4.I. EVALUATION OF SCIENTIFIC OBJECTIVES


Figure 4.2 detailed development of objectives from goal
placed on those factors of scientific exploration which have a bearing on the crigin and evolution of the solar system and on life.

### 4.2 Evaluation of Science Objectives <br> The format that was developed in the previous

 section to establish the consecutive levels of detail for the exploration goal can be utilized as a basis for numerical evaluation and priority ordering of the science objectives. As mentioned previously, spacecraft instrumentation can then be evaluated and given a priority that is based on the ability of the instrument to fulfill the scientific requirements.Numerical evaluation is accomplished by assigning an arbitrary value (such as unity or 1000) to the Goal of Exploration, and then determining the appropriate percentage of this value that is contributed by each Exploration Regime. Similarly, the worth of each individual Exploration Regime can be apportioned among its Regime Categories in terms of relative percentages. Continuing in this fashion, the fractional contributions of: the Category Objectives to their individual Regime Categories can be determined. A complete rationale thus resulto in which each level of the science breakdown is evaluated in terms of the percentage value that it contributes toward fulfilling the next higher level from which it was derived.

The evaluation results corresponding to the first three levels of Figure 4.2 are shown in Figure 4.3. The percentage values shown were obtained through discussion and judgement by a group of scientists and consultants. The Exploration Regime of "Atmospheres of Jovian Planets" was judged to smiulipass $30 \%$ of the total science attributable to the Goal of Exploration because of the nature of the Jovian planets with their massive atmospheres and the fact that it is not known whether a truly definable surface even exists (Michaux, 1967). The science value of Particles and Fields was estimated to be about $22 \%$ of the overall goal because of its importance in the origin and present evoluticnary state of the outer planets. The remaining percentage contribution to the overall Goal was divided equally among the other three Exploration Regimes as shown in Figure 4.3.

The same procedure was used to estimate the percentage contribution that the Regime Categories make towards fulfilling the science requirements of the particular Exploration Regimes from which they were derived. For example, the first three Regime Categories listed in Figure 4.3 were judged to respectively contribute $42 \%, 33 \%$, and $25 \%$ of the value attributable to the Regime of Atmospheres of Jovian Planets. The higher percentage value given to Atmospheric Composition was chosen on the basis of the important role that elemental, molecular and isotopic abundances play in theories relevant


Figure 4.3 SCIENCE EVALUATION OF CATEGORIES RELATIVE TO GOAL
to the origin and evolution of the solar system (e.g., Cameron 1962). Similarly, Atmospheric Dynamics and Active Processes were judged slightly more important than Atmospheric Structure ( $33 \%$ versus $25 \%$ ) because of the importance of atmospheric circulation and weather phenomena in understanding the past and present evolutionary processes which shape a planet's history.

The breakdown and evaluation of each Regime Category of Figure 4.3 are shown in Figures 4.4 through 4.17. These figures illustrate the detailed breakdown into Category Objectives, which in turn are elucidated by their Objective Measurables as shown. The percentage contribution of each Regime Category to its Exploration Regime (see Figure 4.3) is reiterated in the first title block of each figure. The remainder of each block diagram is devoted to the science details leading to the Objective Measurables, which are then followed by estimates for relative worth. The percentages given in parenthesis under the "Relative Value" column represent the judgement value or worth of each Category Objective relative to its Regime Category. This relative value has been divided among the four outer planets in proportion to their individual importance in relation to the science data purtaining to each Category Objective and the associated Objective Measurables. This planetary portion of the relative Category Objective Value is given in the last
SCIENCE EVALUATION FOR CATEGORY OF ATMOSPHERIC COMPOSITION
The block diagram illustrates the approach used for the detailed development of in parentheses give the percentage worth that a given level contributes Thus Atmospheric Composition contributes $42 \%$ of the total worth attributable to Atmospheres of the Jovian Planets (see Figure 4.3). The Regime Category has three Category Objectives, which in turn are further subdivided into the relevant measurable quantities called Objective Measurables. The Objective Measurables shown within the brackets of Figure 4.4 are based on present estimates as to what elements, isotopes, and aspects of particulate matter are of paramount importance in understanding the composition of the Jovian planets. Thus the abundances of hydrogen,
 would be reduced for the terrestrial planets. On the basis of the importance of the defining Objectives Measurables to theories concerning the origin and evolution of the solar system, the relative worths for the Category Objectives of Elemental and Molecular Abundances and Isotopic Abundances and Ratios were judged to be approximately equal to $38 \%$ of the total R'egime Category value. Particulate Matter was judged to have a slightly lower science value (24\%) as shown. The last column of the block diagram shows how the relative percentage value for
each Category Objective was divided up or apportioned among the four outer planets. In general, Jupiter is taken to be of greatest importance because of its unique characteristics and almost star-like mass. Scientific knowledge pertaining to Saturn's composition was estimated to be intermediate in value relative to that of Jupiter and the lower worth of Uranus and Neptune. The exception to the above is Particulate Matter, where all planets were judged to contribute equally.
Planetary Portion of Relative Value


| Isotopic <br> Abundances and <br> Ratios |  |  |
| :---: | :---: | :---: |

## Figure 4.4

SCIENCE EVALUATION FOR CATEGORY OF ATMOSPHERIC COMPOSITION

| Atmospheric |
| :---: |
| Composition |
| $(42 \%)$ |


SCIENTIFIC EVALUATION FOR CATEGORY OF ATMOSPHERIC DYNAMICS AND ACTIVE PROCESSES
The block diagram of Figure 4.5 illustrates the logical division of Atmospheric
Dynamics and Active Processes into the two Category Objective subdivisions of Atmospheric Motions and Circulation, and Weather Phenomena. The first Category Objective includes all large scale and more or less permanent atmospheric activity as denoted by the Objective Measurables shown in brackets. Weather phenomena includes the more localized
and short duration processes such as precipitation, lightning and cyclone activity. The worth of each level of detail relative to its preceding level is indicated by the percentages in parenthesis. The larger relative value ( $60 \%$ ) was attributed to Atmospheric Motion and Circulation because of its greater importance to the overall dynamical activity which establishes the present evolutionary tendancies of the planet. Scientific knowledge of the short duration activity attributable to Weather Phenomena thus contributes the remaining $40 \%$ of the total worth. The portion of the relative Category Objective value that was given to each planet is shown in the last column. Jupiter was apportioned the largest share because of the observed atmospheric activity on this planet (e.g., Hide 1966), a detailed knowledge of which would contribute greatly to our knowledge of atmospheric processes and present evolutionary trends.

Figure 4.5

SCIENCE EVALUATION FOR CATEGORY OF ATMOSPHERIC STRUCTURE
The Regime Category of Atmospheric Structure was judged to be the smallest contrib-


Figure 4.6
SCIENCE EVALUATION FOR CATEGORY OF ATMOSPHERIC STRUCTURE
SCIENCE EVALUATION FOR CATEGORY OF PLANETARY FIELDS than a detailed understanding of gravity or electric fields, and thus was apportioned $75 \%$ of the worth attributable to the Category of Planetary Fields. This high relative worth was based on the importance of understanding how magnetic fields originate and evolve in planetary bodies, particularly for the rapidly rotating planetary systems under investigation. A further consideration is the role of the magnetosphere in permitting biological evolution through its shielding of energetic solar particles. Data concerning gravity fields was estimated to be of greater value than that for electric fields (i.e., $20 \%$ versus $8 \%$ relative value), since the latter is of secondary origin arising from interactions between the atmospheric motions, magnetic fields and the solar flux. Category Objective levels of Magnetic, Gravity and Electric Fields. The measurable quantities of major interest for each of these levels are specified under the Objective
Measurables column of Figure 4.7.

$$
\text { Figure } 4.7 \text { shows the logical breakdown of Planetary Fields into its relevant }
$$

> The Jovian planets were judged to contribute equal shares in fulfilling the
scientific data for each of the three Category Objectives, as shown by the final bra information in rh. -lock diagram of Figure 4.7.

## Figure 4.7

SCIENCE EVALUATION FOR CATEGORY OF PLANETARY FIELDS
SCIENCE EVALUATION FOR CATEGORY OF PLANETARY PARTICLES AND RADIATION
> adequately from \& knowledge of the solar constant and existing radiation laws.

SCIENCE EVALUATION FOR CATEGORY OF SURFACE AND INTERNAL COMPOSITION
The Exploration Regime of Interiors of Jovian Planets has Regime Categories of
to their Exploration Regime. The further development of the Surface and Internal Composition
category is given in Figure 4.9 .
As in the case for Atmospheric Composition (see Figure 4.4 ), an equally high rela-
tive science value ( $38 \%$ ) was attributed to both elemental abundances and isotopic ratios.
This judgment relates to the basic importance that elemental and isotopic variations play
in present theories regarding the origin and evolution of our solar system. The bracketed
aata in the right-hand column of Figure 4.9 shows that Jupiter and Saturn were assigned
the largest portions of the relative values attributed to Planetary Elemental Abundances and
Isotopic Ratios. This judgment was based on the massive size of these two planets, which
for Jupiter's case borders un that of a small star, and the importance of establishing the
interior composition of these two giants. This knowledge would contribute greatly to our
understanding of the origin and development of large planetary systems. Uranus and Neptune
were judged to be equal, but of less importance in the above context.
The last Category objective, Surface and Core Materials, covered in Figure 4.9 in-
cludes the relevant compositional data other than the basic elemental and isotopic abundances.
This science data is valuable in establishing the present state of the outer planets, and
the relative value was apportioned equally among them.
Planetary $\left\{\left[\begin{array}{ll}1 . & \text { Carbon } \\ 2 . & \text { Oxygen } \\ 3 . & \text { Silicon } \\ 4 . & \text { Magnesium } \\ 5 . & \text { Sulfur } \\ 6 . & \text { Iron } \\ 7 . & \text { Hand He } \\ 8 . & \text { Others }\end{array}\right]\left\{\begin{array}{l}\text { Abundances }\end{array}\right]\left\{\begin{array}{l}\text { Jupiter }-16 \% \\ \text { Saturn }-10 \% \\ \text { Uranus } \\ \text { Neptune }-6 \% \\ 6 \%\end{array}\right]\right\}$


SCIENCE EVALUATION FOR CATEGORY OF PLANETARY STRUCTURE The detailed development for the Regime Category of Planetary Structure is outlined in Figure 4.10. The four Category Objective levels include the internal distribution of thermodynamic variables (pressure, temperature, etc.), surface characteristics, relevant chemical and physical properties, and the general geometric properties. relative to understanding the overall planetary structure. This information on the internal and core regions of the planets is valuable in establishing the formation processes which led to the present state. Again, a greater portion of the $40 \%$ relative value can be attributed to Jupiter ( $13 \%$ versus $9 \%$ for each of the other Jovian planets) because of its unique status in the solar system. The Category Objectives of Surface Structure, and Chemical and Physical Properties were judged to be close in their relative values ( $28 \%$ and $20 \%$ respectively). The Category of Geometric Shape was ranked lowest in relative value since its Objective Measurables, while being of general interest, do not contribute greatly to understanding the origin and evolution of the planets. Each of the Jovian planets was judged to contribute an equal portion to the relative value of the last three Category Objectives of Figure 4.10 .

SCIENCE EVALUATION FOR CATEGORY OF PLANETARY ACTIVE PROCESSES
The breakdown of Planetary Active Processes into its sub-levels is shown in
Figure 4.11. The three Category Objective levels include internal phenomena, active surface processes and general dynamical activity. The Objective Measurables define in detail the measurable phenomena that are of interest and also illustrate the characteristics which constitute the total of each Category Objective level.
Since it is not known whether or not a definable surface even exists on the Jovian
planets, the traditional surface activity usually associated with the terrestrial planets, such as topographic changes and faulting, may not be present. For this reason, the Internal Activity objective was ranked considerably higher than Active Surface Processes in its relative value. Thus Internal Activity was judged to contribute about $64 \%$ to the overall value of the Regime Category of Planetary Active Processes. The high relative value of Internal Activity is further exemplified through the importance of interior processes in establishing the present and future evolutionary trends of planetary bodies. A larger portion of the worth for this Category Objective was attributed to Jupiter than to the other planets, because of its massive size and the associated core activity that is expected to exist (such as the core dynamo effect necessary to produce the observed magnetic field).

$$
\begin{aligned}
& \text { The relative contribution of Active Surface Processes was estimated as } 24 \% \text { of the } \\
& \text { total, in contrast to only } 12 \% \text { for Dynamics of the Planet. This judgment was based on the } \\
& \text { fact that the first of these two Category Objectives is valuable in estimating the present } \\
& \text { evolutionary trends, while additional information on the latter would not be as significant } \\
& \text { in its contribution towards understanding the origin and evolution. For these two Category } \\
& \text { Objectives, an equal fraction of the total relative value was attributed to each of the } \\
& \text { Jovian planets. }
\end{aligned}
$$

Planetary Portion
of Relative Value Value




[^4]SCIENCE EVALUATION FOR CATEGORY OF PRIMEVAL CONDITIONS

The worth for the Exploration Regime of Biology of the Jovian planets was assessed
as $37 \%$ being contributed by a knowledge of Primeval Conditions, $37 \%$ by Primordial Substances,
 judged to be the most important because exobiology of the outer planets, if it exists, is believed to be in a primitive state. The probability for finding eviden, fors belleved to be in a primitive state. The probability for finding evidence for living organisms is small, and thus the Manifestations of Life category was taken to be of slightly lower value.

Figure 4.12 shows the breakdown of Primeval Conditions into its Category Objectives, which were taken as Primitive Reducing Atmosphere, Solvents, and Energy Sources. Further elucidation is then given through their Objective Measurables. The three Category Objectives under consideration were judged to contribute equally in fulfilling the science requirements for the overall Regime Category. The reason for this is that a reducing atmosphere, solvents and suitable energy sources are all deemed necessary fos the initiation of life-producing processes.

The planetary portions of the Category Objective relative values (given by the bracketed data in the last column of Figure 4.12) were assigned with Jupiter having the highest weight, Saturn second, and with Uranus and :Teptune each having an equal but smaller contribution. The reasoning for this evaluation was based on the warmer temperature (hence, a more suitable biological environment) of the nearer of the Jovian planets, and the fact that liquid solvents and energy sources are thought to be more readily available on Jupiter and Saturn.

Figure 4.12
SCIENCE EVALUTION FOR CATEGORY OF PRIMEVAL CONDITIONS
SCIENCE EVALUATION FOR CATEGORY OF PRIMORDIAL SUBSTANCES

Primordial Substances include all biological ingredients necessary for the develop-
 phenomena are shown in the block diagram of Figure 4.13.
Since Life-Associated Substances are more indicative of biological life development

$$
\text { than are Pre-Life Molecules, the first Category Objective of Figure } 4.13 \text { was estimated }
$$

to contribute about twice the value of Pre-Life Molecules in fulfillment of the scientific knowledge necessary for understanding the Regime Category associated with Primordial

Substances. Therefore the relative values were taken to be $67 \%$ and $33 \%$ as shown.
As discussed for the previous Regime Category of Primeval Substances (see Figure
4.12), the relative values were apportioned among the planets on the basis of Jupiter having highest priority, Saturn second, and then followed by Uranus and Neptune. These results are shown in the last column of Figure 4.13.
Planetary Portion
of Relative Value

Figure 4.13
SCIENCE EVALUATION FOR CATEGORY OF PRIMORDIAL SUBSTANCES
SCIENGE EVALUATION FOR CATEGORY OF MANIFESTATIONS OF LIFE
> of Figure 4.14.

SCIENCE EVALUATION FOR CATEGORY OF INTERPLANETARY FIELDS

> The exploration science associated with the interplanetary medium has been classified according to the Regime I.tegories of: Interplanetary Fields, Interplanetary Particles, and Agglomerate Matter. The value $j \cdot 1 d g m e n t s$ pertaining to the above were given in Figure 4.3, with Interplanetary Fields being judged slightly more important than the orher two categories. This value judgment was based on the need for a better understanding of magnetic fields, their origin, and the role they played in the early history of the solar system.

> The Category Objectives for Interplanetary Fields are shown in Figure 4.15, along with the more descriptive level of Objective Measurables. As mentioned above, knowledge concerning the structure and variations of the magnetic fields in interplanetary space is of prime importance as an aid to understanding the past and present evolutionsry history of the solar system. Thus the relative value for Magnetic Fields has been set at $84 \%$ in contrsst to the $8 \%$ values for Electric and Gravity Fields.

> The planetary portion 5 the relative Category Objective values was based on the importance of the regions of interplanetary space located between the outer planets. Thus the planetary portions of the relative values that are indicated for Jupiter, Saturn, Uranus, and Neptune refer respectively to distance intervals of 1 to $5 \mathrm{AU}, 5$ to 10 AU , 10 to 20 AU , and 20 to 100 AU from the sun. As shown in the last column of figure 4.15, each of the four intervals was judged as being equally important in their fractional contributions toward fulfilling the science requirements.
Planetary Portion Planetary Portion
of Relative Value

SCIENCE EVALUATION FOR CATEGORY OF INTERPLANETARY FIELDS
SCIENCE EVALUATION FOR CATEGORY OF INTERPLANETARY PARTICLES
The science breakdown into the various levels of detail for the Regime Category of
 Objective of Solar Plasma was judged to contribute $56 \%$ to the total science value needed for an understanding of Interplanetary Particles. This value was based on the important role that the solar wind plays throughout the solar system, such as its capability to sweep any stationary particles out of the solar system and also its influence on rearranging the interplanetary magnetic field configuration.
The Category Objective of second importance is Cosmic Rays, since they offer a vital means of comparing the energy spectrum of energetic particles which have both solar and
galactic sources. The four regions of interplanetary space (as indicated in the last column of Figure 4.16) were estimated to be of equal importance in their contributions towards fulfilling the relative values associated with the objectives of Solar Plasma and Cosmic
The interplanetary elements and particles are generally considered to be in a com-
pletely ionized state. At some distance from the sun, perhaps beyond the outer-most planet, the solar radiation and plasma will not be sufficient to completely ex lite the gaseous
medium. Thus, scientific knowledge of neutral elements (particularly hydrogen) is of in-
portance in assessing the degree of interaction between the solar system plasma and the
neutral hydrogen of interstellar space. Though the exact transition region is uncertain,
a greater portion of the relative value for Neutral Particles has been attributed to the
outer regions of the solar system (ie., 10 to 100 AU as shown in Figure 4.16).

SCIENCE EVALUATION FOR CATEGORY OF INTERPLANETARY AGGLOMERATE MATTER
> assigned to the 1 to 5 AU region where the asteroid belt is located.


## Figure 4.17

SCIENCE EVALUATION FOR CATEGORY OF INTERPLANETARY AGGLOMERATE MATTER
column of the figures. The reasoning used in the value judgements is discussed on the title pages opposite to each of Figures 4.4 through 4.17 at the end of this section. While the numerical percentages that have been assigned in Figures 4.4 through 4.17 are subjective, it is felt that they are fairly representative of judgement values within the scientific community at the present time. In addition, the systematic approach used readily allows a logical mechanism for re-evaluation if new data or priorities are brought to light. It was for this reason, in order to facilitate any re-evaluation necessary, that the worth value at each level of the science breakdown was stated in terms of the percentage contribution relative to the level immediately preceding it, in contrast to having the percentage contribution at each level related directly to the original Goal of Exploration.

The summary results for the science evaluation of Figures 4.3 through 4.17 are given in Table 4.1. The table shows the computed value for each level of science relative to the overall Goal of Exploration. For convenience, the total goal value was taken to be equal to 1000. The number values given represent the portion of the 1000 value that is attributable to each Exploration Regime, Regime Category, and Category Objective. As an example, the total value relative to the overall goal for the Category Objective of Cloud Structure

| GOAL OF EXPLORATIOM | value | $\underset{\substack{\text { exploration } \\ \text { regime }}}{ }$ | Value RElative TO GOAL | regine CATEGORY | value relative to coal. | CATEgORY OBJECTIVE | planetary value of category Objective relative to goal |  |  |  | total value pelative to GOAL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | JUPITER | SATURM | URANUS | NEPTUME |  |
|  | 各 | ATMOSPHERES OF soyian plamets | 300 | atmospheric composition | 126 | elemental amd molecular abundances | 20 | 12 | 8 | 8 | 48 |
|  |  |  |  |  |  | ISOTOPIC AEUMDANCE AKD RATIOS | 21 | 11 | 8 | 8 | 48 |
|  |  |  |  |  |  | PARTICULATE MATTER | 7.5 | 7.5 | 7.5 | 7.5 | 48 |
|  |  |  |  | ATMOSPHERIC DYMAMICS AND ACTIVE PROCESSES | 99 | ATMOSPHERIC MOTIOM GMD CIRCULATION | 25 | 15 | 10 | 10 | ) |
|  |  |  |  |  |  | WEATHER PHENOMEMA | 12 |  |  |  | 60 |
|  |  |  |  | ATMOSPHERIC STRUCTURE | 75 | ThERHODYYAMIC STATE |  |  | 9 | 9 | 39 |
|  |  |  |  |  |  | Cloud structure |  | 8 | 8 | 8 | 37 |
|  |  | particles AMD FIELDS | 220 | plametary FIELDS | 110 | Magmetic field | 14 | 10 | 7 | 7 | 38 |
|  |  |  |  |  |  |  | 20 | 20 | 20 | 20 | 80 |
|  |  |  |  |  |  | GRAVITY FIELD --_----.... | 5.5 | 5.5 | 5.5 | 5.5 | 22 |
|  |  |  |  |  |  | ELECTRIC FIELD | 2 | 2 | 2 | 2 | 8 |
|  |  |  |  | plametary particles amo raditition | 110 | Particles | 12 | 12 | 8 |  | 40 |
|  |  |  |  |  |  | INTERACTION WITH INTERPLAMETARY MEDIL LOM | 8 | 8 | 8 | 8 | 32 |
|  |  |  |  |  |  | Plametary radiation | 11 | 5 | 5 | 5 | 26 |
|  |  |  |  |  |  | SOLAR IMFLUX | 3 | 3 | 3 | 3 | 12 |
|  |  | IUTERIORS OF JOVIAM PLAMETS | 160 | SURFACE AND IMTERMAL COMPOSITIOA | 53 | Planetary elememtal abumdances | 9 | 6 | 3 | 3 | 21 |
|  |  |  |  |  |  | PLANETARY ISOTOPIC RATIOS | 9 | 5 | 3 | 3 | 20 |
|  |  |  |  |  |  | SURFAC: AND CORE MATERIALS | 3 | 3 | 3 | 3 |  |
|  |  |  |  | plametary STRUCTURE | 53 | IWTERMAL STRUCTURE | 6 | 5 | 5 | 5 | 21 |
|  |  |  |  |  |  | SURFACE STRUCTURE | 4 | 4 | 4 | 4 | 21 |
|  |  |  |  |  |  | Chemical and physical properties | 2.5 | 2.: | 2.5 | 2.5 | 10 |
|  |  |  |  |  |  | GEOMETRIC SHAPE | 1.5 | 1.5 | 1.5 | 1.5 | , |
|  |  |  |  | ilametary aCTIVE PROCESSES | 53 | INTERMAL ACTIVITY | 10 | 8 | 8 | 8 | 34 |
|  |  |  |  |  |  | ACTIVE SURFACE PROCESSES | 3 | 3 | 3 | 3 | 12 |
|  |  | biosogy of the JOVIAM PLAMETS |  |  |  | DYMAMICS OF THE PLAMET | 2 | 2 | 2 | 2 | 8 |
|  |  |  | 160 | primeval combitions | 59 | PRIMITIVE REDUCIMG ATMOSPHERE | 6 | 5 | 4 | 4 | 19 |
|  |  |  |  |  |  | SOLVELTS | 7 | 5 | 4 | 4 |  |
|  |  |  |  |  |  | ENERGY SOURCES | 7 | 5 | 4 | 4 | 20 |
|  |  |  |  | primardial substances | 59 | LIFE-ASSOCIATED SUASTANCES | 13 | 11 | 8 | 8 | 40 |
|  |  |  |  |  |  | PRE-LIFE MOLECULES | 6 | 5 | 4 | 4 | 19 |
|  |  |  |  | manifestations OF LIfE | 42 | DIRECT EVIDENCE OF LIFE | 9 | 6 | 4 | 4 | 23 |
|  |  |  |  |  |  | PHYSICAL EFFECTS OF LIFE | 4 | 3 | 2 | 2 | 11 |
|  |  |  |  |  |  | B10-CHENICAL PROCESSES | 3 | 2 | 1.5 | 1.5 |  |
|  |  | IMTERPLAMETGARYMEDILM | 160 | interplametaryfiel.os | 64 | MABMETIC FIELDS | 13.5 | 13.5 | 13.5 | 13.5 | 54 |
|  |  |  |  |  |  | ELECTRIC FIELDS | 1.3 | 1.3 | 1.2 | 1.2 |  |
|  |  |  |  |  |  | GRAVITY FIELOS | . 3 | 1.3 |  |  | 5 |
|  |  |  |  | IWTERPLANETARY particles | 48 | S0LAR PLASMA | 6.5 | 6.5 | 1.2 | 1.2 | 5 |
|  |  |  |  |  |  | COSMIC RAYS |  | . 5 |  |  | 26 |
|  |  |  |  |  |  | MEUTRAL PARTICLES |  |  | 4 | 4 | 16 |
|  |  |  |  | agglomeratematter | 48 | METEOROIDS | 5 | , | 2 | 2.5 | 6 |
|  |  |  |  |  |  | ASTEROIDS | 7.3 | 7.3 | 7.2 | 7.2 | 29 |
|  |  |  |  |  |  |  | 19 | 0 | 0 | 0 | 19 |

is found from the relative percentage values of Figures 4.3 and 4.6 to be given by (.50) $\times(.25) \times(.30) \times(1000)=38$. The portion of each of the total Category Objective values that is attributable to the individual planets is also tabulated in Table 4.1.

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## PAYLOAD SELECTION

The selection of actual instrumentation and the consequent payload to be used for the multiple outer planet mission could be based on a variety of criteria. Some of the relevant factors include: scientific worth of the measurements, national prestige, weight and/or power requirements $f$ the instrument packages, economic considerations, and so forth. Factors such as national prestige are difficult to assess, and as a consequence the present study will be limited to a certain extent. This limitation is self-imposed in that the purpose of this investigation is to develop a spacecraft instrument selection methodology based principally on the science requirements, in an attempt to formulate a logical scheme that can be used as a guide in determining the final payload.

Section 5.1 of this Section is devoted to the methodology used for the selection of instruments for the flyby mission to the Jovian planeis. The final selection criteria is based on the capability of a particular instrument to fulfill the science objectives discussed in the previous chapter, but subject to various constraints such as: the requirement to increase present knowledge by an order of magnitude, compatability of instruments with flyby missions, weight requirements, and trajectory profile restrictions.

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Section 5.2 is devoted to a discussion of the types of instrumentation that are considered and their role in fulfilling the science requirements. The actual worth evaluation of measurement techniques for a 1977 mission passing exterior to the rings of Saturn is covered in Section 5.3. Section 5.4 concludes the chapter with a :"esentation of the selected payloads.

### 5.1 Kethodology for Payload Selection

The basic thesis of the present study is to outline a logical framework through which spacecraft instrumentation can be selected on $t^{1 ;}$; basis of their contributions to science.
 that has been developed to evaluate spacecraft instrumentation. As a first step, values of scientific objectives and measurables relative to the overall exploration goal were established in the previous chapter. The evaluation scheme sought to place the major emphasis on those scientific objectives that contributed the most to our understanding of the origin and evolution of the solar system through examination of the Jovian planets. Using these results as the basic foundation, the next step is to determine what measurement techniques would, when operating remotely in a flyby mode, be capable of obtaining useful scientific data relative to the science requirements.


FIGURE 5.1
FLOW DIAGRAM FOR EVALUATION AND SELECTION OF SPACECRAFT EXPERIMENTS

The applicable flyby measurement techniques that were selected are shown in Table 5.1, along with a summary presentation of the Category Objectives that were developed from the original Goal of Exploration. It should be noted that the measurement techniques are those which were judged to be most effective in obtaining data relative to the Objective Measurables that were presented for each Category Objective level in Figures 4.4 through 4.17. The designation of "Not Applicable" under the right-hand column for Measurement Techniques in Table 5.1 indicates those objectives for which present remote sensing techniques were deemed inadequate to increase our present knowledge significantly. Also, it should be noted that only those techniques that were considered most appropriate for a flyby mission to the outer planets have been considered. As an example, while spectrometery is an applicable technique for the Category Objective of Atmospheric Elemental and Molecular Abundance, it was omitted because narrow band photometry provides a simpler means of measurement and can provide adequate data for the initial mission to the Jovian planets under consideration. The next generation of missions would undoubtedly require the more sophisticated techniques of spectrometry measurements. The Occulation Data technique for this same Category Objective pertains only to the determination of the mean molecular weight (See Objective Measurables Column of Figure 4.4). Similar reasoning and judgement was

| G0AL OF EXPLURATIOM | EXPLOALTIOM REGME | REGIME CATEGORY | Category obuective | APPLICABLE FLYBY MEASURFMENT TECHMI PUES FOR MULTIPLE OUTER PLAMET MISSION |
| :---: | :---: | :---: | :---: | :---: |
|  | ATMOSPHERES OF Jovian PLaMETS | ATMOSPHERIC composition | ELEMEMTAL AMD MOLECULAR ABUMDAMCES | Photometry and occul tation data |
|  |  |  | ISOTOPIC ABuMDAMCE AMD RATIOS | PMotometry |
|  |  |  | PARTICULATE MATTER | POLARIMETRY，PHOTOMETRY AND RADAR |
|  |  | ATMOSPHERIC DYMANICS AMD ACTIVE PROCESSES | ATMOSPAERIC motion ano circulation | TELEVISIOM AMD RADIOMETRY |
|  |  |  | WEATHER PHENOKEMA | RADIONETRY |
|  |  | ATMOSPHERIC structure | Therwog inhilc state | RADIOMETRY AND OCCULTATIOM DATA |
|  |  |  | CLOUD STRUCTURE | TELEVISIOM |
|  | PARTICLES and fielos | Plametary fielos | MAGETIC FIELD | MAGMETOMETER |
|  |  |  | GRavity field | trajectory data |
|  |  |  | ELECTRIC FIELD | MOT APPLICABLE |
|  |  | plametary particles and radiation | PARTICLES | $\mu$－METEORITE AMD COSNIC RAY delectors amd lon and trapped part．package |
|  |  |  | IMTERACTIOM WITM ImTERPLAMETARY MEDIUM | Plasma probe，magmetometer amd ion．Chanber and trappeo part．package |
|  |  |  | Plametary radiation | Photowetry amd radionetry |
|  |  |  | SOLAR IMFLUX | PLASMA PROBE AND COSNIC RAY detector |
|  | Ifrepicas of sovian planets | SURFACE AMD InTERMAL COMPOSITIOM | PLAMETARY ELEMENTAL ABundances | mor APPLICABLE |
|  |  |  | rlametary isotopic ratios | WJT APPLICABLE |
|  |  |  | SURFACE AMD CORE MATERIALS | MOT APPL．ICABLE |
|  |  | Plametary STRUCTURE | IMTERMAL STRUCTURE | Woi APPLICABLE |
|  |  |  | SURFACE STRUCTIIRE | 40SR |
|  |  |  | CHEM．AND PHYSICAL PROPERTIES | r－－Applicable |
|  |  |  | GEOUETRIC SHAPE | IE Evisiom and occultation data |
|  |  | plametary active processes | IMTERINAL ACTIVITY | W0\％APPLICABLE |
|  |  |  | Active Surface processes | MOT APPLICABLE |
|  |  |  | drunulics of tiee plamet | TELEVISIOM |
|  | glology of the JOVIAN PLANETS | Plimeval CoMDITIOMS | Primitive reducing atwosphere | MOT APPLICABLE |
|  |  |  | Solverts | PMOTONETRY |
|  |  |  | Emerar sources | radiometay |
|  |  | primordial． surstances | LIFE－ASSOCIATED SUBSTANCES | PMOTOMETRY |
|  |  |  | PRE－LIFE MOLECUES | PHOTOMETRY |
|  |  | MAMIFESTATIOMS OF LIFE | DIRECT EVIDEWCE OF LIFE | moi Applicable |
|  |  |  | PHYSICAL EFFECTS Of LIFE | MOT APPLICABLE |
|  |  |  | BIO－CMEWICAL PROCESSES | not APPLICABLE |
|  | imferplanetary | IMTERPLAMETARY FIELDS | MAOMETIC FIELDS | MAGMETOMETER PACKAGE |
|  |  |  | ELECTRIC FIELOS | not APPLICABLE |
|  |  |  | grivity fielos | Tracking data |
|  |  | atowic particles | SOLAR PLASMA | PLASMA PROBE |
|  |  |  | COSNIC RAY8 | COSNIC RAY DETECTOR |
|  |  |  | MEUTRAL PARTICLES | MARS SPECTROMETER |
|  |  | mgalomerate matter | WETEOROIDS | $\mu$－METEOROIO DETECTOR |
|  |  |  | ASTEROIDS | $\mu$－METEOROID DETECTOR |

Table 5．1 APPLICABLE MEASUREMENT TECHNIQUES BASED ON SCIENCE REQUIREMENTS
used to select the other measurement techniques given in Table 5.1.

The general techniques of Table 5.1 are, of course, directly associated with actual or contemplated spacecraft instrumentation. An understanding of the capabilities of these instruments is required in order to assess their ability to fulfill, either completely or partially, the desired science objectives. Thus, the measurement techniques, along with a knowledge of the remote sensing potential of the associated spacecraft instruments provide a means for evaluating the worth of a particular instrument. This worth is directly related to that portion of the Objective Measurables of a particular Category Objective (see Section 4) for which the instrument yields useful scientific data. Of course, if a particular measurement contributes data that applies to more than one Category Objective level, the overall worth of the instrument in question is increased accordingly. The ultimate value and priorty of any individual instrument will thus depend both on the magnitude of the pure science value of an Category Objective (see Table 4.1) for which it yields data and on the total number of Category Objectives for which it is applicable. This summation feature of the present evaluation scheme provides a highly desirable and logical approach for assessing the full worth of an instrument, and contributes greatly towards the effective utilization of spacecraft capabilities.

Although the general evaluation scheme appears to be more or less straight forward, there are several constraints which must be considered and accounted for. First of all, there is the fact that a certain amount of scientific data, particularly in the case of Jupiter, is presently available. Thus, for a spacecraft measurement to have full value, it should yield information which increases knc rledge beyond its present extent. As a result, an evaluation contraint was adopted which states that: "for a particular instrument to have value it must provide scientific data that is an order of magnitude better than the data which is presently available." This constraint, of course, is planet dependent and was treated as such in the evaluations. Perhaps the major evaluation variable is the influence of the trajectory prof' ${ }^{\text {les }}$ at each planet. For example, the data from an instrument such as TV which depends on factors such as ground resolution and reflected sunlight, depends critically on the spacecraft altitude during encounter as well as on the amount of time spent over the daylight hemisphere.

The methodology for the final instrument evaluation scheme which evolved is illustrated by Figure 5.2. The first step indicates the science evaluation performed in the previous chapter, in which the relative value of each science objective was determined for each planet. The next step was to select the applicable flyby measurement techniques that are best
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FIGURE 5.2 METHOD FOR EVALUATION AND SELECTION OF PAYLOAD
suited for obtaining scientific data relativ to the Category Objectives and their Objective Measurables, the results of which were shown in Figure 5.1. Using this information, along with a knowledge of the capabilities of the related spacecraft instruments that are discussed in the next section (5.2), it will be possible in Section 5.3 to estimate the maximum science value that the data of any particular instrument could yield. This step in the evaluation scheme is indicated 'y the second block of Figure 5.2, and indicates the percentage of the Category Objective values that a particular instrument could fulfill under ideal conditions (assuming an increase of present knowledge by an order of magnitude and an optimum trajectory profile).

The third step in the evaluation scheme is to assess the inflience of the various constraints due to non-optimum fly-by profiles, illumination conditions, resolution requirements, etc., for each planet. The assessment is accomplished by roundtable discussion and analysis by a qualified group of scientists and engineers. This step then, represented by the third block of Figure 5.2, effective? $y$ results in the determination of a "degradation factor" at each planet and for each trajectory opportunity under consideration (see Sections 2 and 3). Tlie final result is a new relative value for each instrument that is less than or equal to the previous optimum value for the case of ideal conditions. The detailed evaluation results for
the 1977 opportunity with an exterior passige around Saturn's outer-most ring (designated as: 1977-E) are given in Section 5.3.

The final phase in the payload selection involves priority ordering of the spacecraft instruments. This can be accomplished by introducing the weight of the spacecraft instruments as an additional factor to be used in the selection criteria. Since the total payload weight for a given space vehicle is limited due to fuel requirements, etc., it is logical that, given two instruments with the same relative value, the instrument having the least weight should have first priority on the spacecraft since this allows for the possibility of additional instruments and hence a higher total value for the final payload (for a given payload weight). Thus using the instrument specifications of Section 5.2, the value per unit weight of each individual instrument can be determined. These results along with the recommended mission payloads are presented in Section 5.4.

### 5.2 Description of Instrumentation

The following section describes briefly the types of instrumests which were tabulated in Table 5.1 as possibilities for a Grand Tour Mission. Several are very similar to existing spacecraft instruments, but some are beyond the present state-of-the-art of spacecraft technology.

In each case the mode of operation and any critical facts concerning the instrument's inclusion in a mission payload have been outlined. Also, a summary of the important specifications is presented in Table 5.2.
5.2.1 Meteoroid Detector - This instrument is of the dielectric/acoustic type similar to that flown on the Mariner spacecraft. It consists of an al:minum acoustic plate with a crystal microphone on one side, and overcoated on both sides with an evaporated dielectric capacitance. The dielectric capacitors provide directional information of impacts and in addition have a detecting threshold at least one order of magnitude below that of the microphone. A threshold detection limit of momentum $\leq 10^{-6}$ dynes -sec is desired for the dielectric capacitor and assuming particle velocities $\times 10 \mathrm{kms} / \mathrm{sec}$, this gives a mass detection threshold $\leq 10^{-12}$ gms.

A momentum spectrum is produced by pulse height analysis of the acoustic impact signals, the range being $\times 10^{-5}$ dyne-sec to $\sim 10^{-3}$ dyne sec.

The instrument could be operated continuously throughout the mission, the mean rate of data acquisition would be nominal except during passage through the Asteroid Belt and in the region of Saturn's rings. At these times the data rate required is $\sim 1$ bit/sec. Data from the detecto: consists of an accumulated count of the total number of microphone impacts, and for each impact a pulse height
Table 5.2
SUMMARY OF SPECIFICATIONS FOR APPLICABLE FLYBY INSTRUMENTATION

Table 5.2 (Continued)
SUMMARY OF SPECIFICATIONS FOR APPLICABLE FLYBY INSTRUMENTATION References:

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SUMMARY OF SPECIFICATIONS FOR APPLICABLE FLYBY INSTRUMENTATION
References (Continued)

analysis of the microphone impulse, a direction indication from the capacitance detectors, and the total number of capacitance impacts between each microphone impact.
5.2.2 Magnetometer Package - The range of the magnetic field strength to be measured during the mission extends from $\sim 1$ gamma in the interplanetary medium to $\sim 5$ gauss (1 gauss $=10^{5}$ gamma) in the vicinity of Jupiter. To cover this range two types of magnetometer are included.

For measurements of the interplanetary field, which is approximately 3 gamma, with an accuracy $\sim 0.05$ gamma, a Rubidium vapor magnetometer could be used. By subjecting the vapor cell to fields produced by a system of Helmholtz coils, both the magnitude and the direction of the interplanetary field can be measured in the range 0.05 - 100 gammas. For planetary field measurements, in the range 100 gamma - 5 gauss, a triaxial fluxgate magnetometer could be used.

The vapor magnetometer should operate throughout the mission at a measurement rate $\sim 1$ per min., corresponding to a data rate $\sim 0.2$ bits/sec. During planet encounters both instruments may be in use simultaneously, giving a data rate ~ 1 bit/sec.
5.2.3 Cosmic Ray Detector - In order to monitor the flux and the approximate energy distribution of cosmic rays a simple charged particle telescope of the type flown on IMP-1 and Mariner IV is desirable. This consists of three gold-silicon barrier layers, surface area $2 \mathrm{~cm}^{2}$, spaced by aluminum and platinum absorbers, producing an angle of acceptance of $45^{\circ}$. By a combination of coincidence counting and pulse height analysis of the signals from each barrier layer, discrimination between protons, alpha particles and electrons is obtained and the energy range of each type can be estimated. Incident protons are detected within the energy ranges $0.8-15 \mathrm{Mev}, 15-80 \mathrm{Mev}$, and $80-190 \mathrm{Mev} ; ~ a l p h a$ particles within energy ranges 3-60 Mevr, $60-280 \mathrm{Mev}$ and $\geq 280 \mathrm{Mev}$. In addition electrons with energy $>0.2 \mathrm{Mev}$ are detected by the first barrier layer only.
5.2.4 Plasma Probe - A Faraday Cup type probe was selected to measure the flux density and energy spectrum of the positive particles of the Solar plasma. The present threshold sensitivity of this type of instrument is $10^{-13}$ amp $/ \mathrm{cm}^{2}$, corresponding to fluxes $5.10^{5}$ parts $/ \mathrm{cm}^{2} / \mathrm{sec}$. This is approximately two orders of magnitude lower than the average flux at 1 AU and therefore equal to the expected flux at distances 10 AU . Thus the present threshold sensitivity must be reduced by at least an order of magnitude or the collecting area increased by an order of magnitude, to be effective at distance > 10 AU on the Grand Tour Mission. ilt research institute

The energy range of analysis available with this type of instrument is 10 eV to 10 keV , divided into 10 energy ranges. Measurements should be made in three directions as in the Mariner IV instrument, in order to find the vector of the Solar plasma. T'aking the three measurements at approximately 20 sec . intervals, yields a mean data rate 3 bits/sec which is continuous throughout the mission.
5.2.5 Ionization and Trapped Particle Package Three types of particle detectors are ncluded in this package to measure the solar cosmic rays and energetic electrons in the interplanetary medium and to determine the spatial distribution, energy spectra and particle types of any trapped radiation belts which may exist at any of the outer planets.

A total-ionization chamber, consisting of a thin wall aluminum sphere filled with argon gas and containing a quartz fiber electrometer, provides an integrated value for the total amount of ionizing radiation. The wall thickness would be designed to allow gas ionization only by electrons with energy > 1 Mev , protons with energy > 10 Mev and alpha particles with energy > 40 Mev . Further energy and particle type discrimination is achieved using Silicon diode type detectors and Geiger-Muller tubes, both of which detect individual particle impacts.

The silicon surface barrier diode is essentially insensitive to electrons and by amplitude discrimination of the output pulse, at least two levels of proton detection can be obtained. The proton energy ranges monitored can therefore be designed as $\mathrm{Mev}<\mathrm{E}<10 \mathrm{Mev}$ and $<\mathrm{E}<4 \mathrm{Mev}$ using a single detector.

The energy range of the Geiger-Muller tube is determined largely by the thickness and material of the entrance window. By suitable choice of e entrance windows of G-M tubes, electron energies $>40 \mathrm{keV}$ and proton energies $>0.5 \mathrm{Mev}$ can be divided into several regions.

The ionization chamber is essentially an omnidirectional detector except where it is shielded by the spacecraft, the angles of acceptance of G.-M. tubes and Si diode, however, are determined by the metal shielding in front of the window. Thus angular distribution information can be obtained by orientating the detecting in different directions with respect to the stabilized spacecraft. Since the detectors are inherently event counters, and will operate continuously throughout the mission, the data rate will vary over several orders of magnitude, due to solar flare events and passage through any planetary radiation zones.

### 5.2.6 Polarization and Photometry Package -

This instrument operates only at planetary encounters, viewing the solar illuminated disk. If pointed at the
planet center, it can provide albedo and polarization data for almost all phase angles from $0-180^{\circ}$. Ten wide-band wavelength regions are desired in order to cover the entire UV-IR range. In addition, the incorporation of two polaroid filters is needed to determine the polarization.

As visualized, the instrument consists of a single photo-multiplier and collecting optics giving a spatial resolution of $1 / 00$ of the planetary disk. Spectral and polarization discrimination is provided by two rotating filter wheels operated in series. One wheel carries ten wide band-pass filters and the other, two polaroid windows and an open aperture. Thus each measurement consists of 30 data points, using all combinations of filters and windows. Measurements are required at least every $5^{n}$ change in phase angle, and in order to obtain maximum possible coverage, a total of 300 measurements are required at each planet.
5.2.7 IR-Microwave Radiometer - A radiometer with a number of pass-bands in the wavelength range $2 \mu-1 \mathrm{~mm}$ can provide data on the thermal emission of the planets. The instrument operates during planet encounter, on both the light and dark sides, with a spatial resolution of $1 / 00$ of the planets disk. Five detection bands in the region $2 \mu-1 \mathrm{~mm}$ would be satisfactory, each sensitive to $1 / 10^{\circ} \mathrm{K}$ changes in the planetary emission.

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Complete thermal mapping of each planet is possible during a flyby with 300 measurements, i.e., 1500 data points, taken over a period $\leq 3$ hours. The instrument should be bore-sighted with the TV cameras for visual identification, and a facility to preprogram examination of a particular interesting area on a planet would be desirable.
5.2.8 R.F. Detector - A radio frequency noise detector operating in the wavelength range 1 - 10 meters is required to indicate the presence of electrical discharges within the planetary atmospheres. Although lightning discharges have a peak energy output at $\omega 100$ meters, other noise sources could predominant at wavelengths other than 1 - 10 meters. At Jupiter in particular, the decameter radio bursts and the absorption of an ionosphere (if present) preclude noise detection at $\lambda>10$ meters and since the energy spectrum of lightning discharges decreases rapidly with decreasing wavelength, the most useful wavelength range is 1 - 10 meters.
5.29 Low Resolution Television - The instrument envisioned here is similar to that flown on Mariner IV, consisting of a small Cassegrain reflecting telescope and an electrostatic vidicon camera. The field of view required is 1.5 deg., the number of lines per frame $=1000$, and a small nunicer of interchangeable wide band filters would add spectral information to the images. Assuming values of closest approach corresponding to the 1977 Exterior Ring

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passage, this would give spatial resolutions ranging from 500 kms to, 50 kms at Jupiter and from 50 kms to $\sim 5 \mathrm{kms}$ (at the terminator) at Saturn, Uranus and Neptune. This is a satisfactory resolution at the latter planets for a study of cloud structure and atmospheric motion. However, at Jupiter, although it is almost an order of magnitude better than present ground-based resolution, it is not sufficient for the particular measurables of concern. The instrument is therefore given a lower value at Jupiter than at Saturn, Uranus and Neptune.

Operation of the instrument begins when the whole planet occupies an appreciable fraction of the frame size, and such pictures can be used to determine the geometric shape. A minimum of 30 pictures per planet are desired, giving a data total $\sim 2.10^{8}$ bits/planet.
5.2.10 Abundance Photometers - Approximately seven photomultiplier tubes and narrow band-pass filters are needed to measure exospheric mission lines in the UVvisual and hence obtain the exospheric abundance ratios. The required field of view for each detector is $\sim 5^{\circ}$, in the direction perpendicular to the Sun-spacecraft line. The filter band-passes would each be set at an expected emission line of $\mathrm{H}, \mathrm{He}, \mathrm{O}, \mathrm{N}, \mathrm{A}$, or Ne , one further detector at a spectral position of no emission is required to differentiate between scattered and emitted radiation.

The instrument operates at a distance of $\sim 10$ planet radii before and after, and during this time $\sim 100$ data points/channel would be taken.

A further three detectors, two with very narrow band-passes filters at the spectral location of the isotopes of H and He and one as a monitor of scattered light, will provide information on the isotopic ratios of hydrogen and helium in the exosphere.
5.2.11 Occulation - Transmission of data from the spacecraft during occulation can provide a single frequency determination of the atmospheric occulation profile. However, experimental data transmitted ir this time would be lost, at least in part. Hence the method of obtaining atmospheric and ionospheric occulation profiles will be to use a multi-channel radio receiver on the spacecraft tuned to at least two frequencies in the S-band region. This will receive and record transmissions from Earth which are then partially processed and retransmitted to Earth after planet encounter. Since the atmospheres of the outer planets are very thick, large changes of frequency, phase and amplitude of the radio signals may be expected, therefore operation in a transponder mode by the spacecraft would create very complex data without any increase in scientific value.

### 5.2.12 Narrow Band Absorption Photometers -

Two photomultipliers each with a narrow band-pass filter, can be used to measure the absorption band of a particular atmosphereic neutral gas component. One filter should be positioned at the wavelength of an absorption band of the component to be detected and the other positioned in the continum adjacent to the band. Five such pairs of detectors operating in the UV to IR spectrum are required to measure absorptions in the reflected solar radiation from the planet arising from $\mathrm{CH}_{4}$, $\mathrm{NH}_{2}, \mathrm{H}_{2} \mathrm{O}, \mathrm{H}_{2}$ and He for example. A further two pairs can be included to measure absorption arising from life-associated molecules (assuming such absorptions have been identified).

The instrument should be planet-centered, with a spatial resolution $<1 / 10$ disk and operate at encounter, viewing the illuminated disk. A total of ~ $\mathbf{3 0}$ measurements are needed and the total data acquired would be $\sim 3000$ bits.

### 5.2.13 Mass Spectrometer - A neutral mass

 spectrometer uses electrostatic and magnetic deflection techniques to separate ions created by ionization (of the neutral atoms) within the instrument. The desired instrument is a simipler version of the type flown on Explorer 17 for the same purpose, when neutral density measurements were made of $\mathrm{He}, \mathrm{O}, \mathrm{N}, \mathrm{O}_{2}, \mathrm{~N}_{2}$, and $\mathrm{H}_{2} \mathrm{O}$. The instrument should operate throughout the entire mission, taking measurementsat a maximum rate of $1 / \mathrm{min}$. and thus the data rate is $\leq$ 0.1 bits/sec.
5.2.14 Airglow Photometers - Four photomultiplier tubes and narrow band-pass filters in the JV-visible region can be used to measure atmospheric airglow and auroral emission on the dark side of the planets. The instrument should be planet-centered, with a field of view $\sim 5^{\circ}$ and should operate on1y beyond the terminator. A minimum of 30 data points per detector are required to scan the planets dark side, giving at minimum 1000 bits per planet.

### 5.2.15 High Resolution Television - This

instrument utilizes the same :ype of electrostatic vidicon camera as the low resolution system but will include a larger telescope, (estimated diameter $\geq 10 \mathrm{cms}$ ). The field of view required is $\simeq 0.15 \mathrm{deg}$ and the camera should be located within the frame of the low resolution system. With 1000 lines/frame, this gives a resolution at Jupiter ranging from $\sim 50 \mathrm{~km}$ to $\sim 5 \mathrm{~km}$ (at the terminator). At Saturn, Uranus and Neptune, however, the spatial resolution ranges from $\sim 5 \mathrm{~km}$ to $\sim 500 \mathrm{~km}$. This is too small for the study of cloud structure and atmospheric motion and hence the value of the instrument is reduced at these planets. A minimum of one high resolution image for each low resolution image is required; the total amount of data for this camera is then $\sim 2 \times 10^{8}$ bits per planet.
5.2.16 Radar - An active radar system comprising a transmitter and receiver on the spacecraft is required to locate particulate matter in the planetary atmosphere or a surface below the atmosphere. A minimum of two wavelengths are desirable in the range of 10 cm to 1 meter. The instrument can operate on both light and dark sides at a measurement race of $\sim 1$ pulse/min. The present state of knowledge of the Outer Planets makes this very much a search mode experiment since even the existence of planet surfaces is not proven. At the present time there does not appear to be an active radar system with reasonable power and weight specifications to perform this function.

### 5.2.17 High Resolution Radiometer - A high

 resolution radiometer operating at several wavelengths in the range $2 \mu-1 \mathrm{~mm}$ with a spatial resolution $\sim 10 \mathrm{~km}$ is judged to be capab1e of mapping local thermal cells in the planetary atmospheres. With an angular resolution $\sim 0.005$ deg., the spatial resolution at Jupiter is $\geq 100 \mathrm{kms}$ and at Saturn, Uranus and Neptune, $\geq 10 \mathrm{kms}$. Thus the value of the instrument, in achieving the required measurement, is low at Jupiter and high at the other planets.The instrument can be boresighted with the high resolution television but it should also be capable of making several spaced measurements per TV picture. Also, the radiometer will be operated on both light and dark sides of the planet, a data total $\sim 10^{6}$ bits/planet.
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## 5.3 <br> Evaluation of Measurement Techniques

The detailed worth evaluation of applicable flyby instruments is presented in this section using the evaluation m.thodology that was outlined in Section 5.1 along with the instrument specifications of Section 5.2. The relative worth of any instrument depends principally on its ability to meet measurement specifications at a given planet for a given trajectory. In order to simplify the presentation, the detailed results will be presented only for the 1977-E opportunity discussed in Sections 2 and 3. The relevance to the other mission opportunities will be briefly discussed in the next section.

The results oi the evaluation are summarized in Tables 5.3 through 5.8. The first two columns of the tables reiterate the science evaluation of Section 4 for the relevant Regime Categories and their Category Objectives. Those Category Objectives for which no applicable flyby measurement technique was indicated in Table 5.1 have been omitted from further consideration. The third column titled "Applicable Flyby Instrument" lists the instruments which were judged most appropriate for an initial mission to the Jovian planets, che selection of which was based on the discussions of the previous sections.
INSTRUMENT EVALUATION FOR THE CATEGORY OF ATMOSPHERIC COMPOSITION

$$
\text { The first two columns of Table } 5.3 \text { reiterate the science breakdown and the }
$$ value percentages that resulted from the evaluation scheme of Chapter 4 (see also Figure 4.4 and Table 5.1). The flyby instruments that are applicable for each Category Objective level are listed in the center column of the table.

The fourth column gives the value judgment for the maximum percentage value
that the scientific data of each instrument, under optimum flyby conditions, could
possibly contribute towards fulfilling the science requirements of the relevant Category Objective. These science requirements are determined by the Objective Measurables as were specified in Figure $4: 4$. For example, Emission UV Photometers were judged as capable of providing $20 \%$ of the scientific knowledge desired for Elemental and Molecular Abundances and 5\% for Isotopic Abundances as a result of narrow-band photometeric studies of airglow; auroral emission, etc. For the case of Particulate Matter, the value judgment indicated that a combined instrument package utilizing polarimetry, wideband UV-IR photometry and radar was capable as a group of providing $100 \%$ of the total value attributable to the objective, assuming optimum conditions.

$$
\text { The last four columns of Table } 5.3 \text { indicate whether or not the maximum }
$$

instrument value was attainable at the individual planets during the 1977-E opportunity. For several of the cases shown, the contributions of the instruments at the planet Jupiter were judged to be less than the maximum value because the large miss distances reduce the resolution obtainable at this planet. Also for Particulate Matter, the projected radar technology was estimated to be capable of yielding only about one-half (or 15\%) of the desired information.
INSTRUMENT EVALUATION FOR THE CATEGORIES OF ATMOSPIIERIC DYNAMICS

## AND ACTIVE PROCESSES AND ATMOSPHERI:: STRUCTURE

The science brekdown, the corresponding relative values given in Figures 4.5 and 4.6, and the applicable flyby instruments from Table 5.1 are given in the first three columns of Table 5.4. It is seen from the fourth column of the table that applicable instruments are capable of contributing only a small percentage of the total value associated with the Category Objectives of Atmospheric Motion and Weather Phenomena. These value judgments were based on the premise that a full understanding of atmospheric dynamics could only be obtained through the data of atmospheric probes and in situ measurements, in contrast to the remote sensing capabilities of flyby instruments. On the other hand, the maximum value that can be obtained from the instruments applicable for the measurables of Thermodynamic State and Cloud Structure constitutes a considerable portion of the science worth available. This conclusion follows directly from the fact that measurables such as cloud features are readily detected by remote means. The final columns of Table 5.4 give the revised instrument percentage value at each planet, after assessment of the trajectory profiles and other constraints discussed in the text. As an example, the use of television to obtain data on Atmospheric Motions and Circulation was judged to be severely hampered by the short encounter times for which sunlight was available. For the case of cloud structure, the $40 \%$ maximum value available through low resolution TV was reduced to $8 \%$ at Jupiter because the data would not be significantly better than Earth based results. For the high resolution TV system the maximum $40 \%$ value was judged to be applicable for the Jupiter profile, but was reduced for the other planets because the data would give much more detail than is desired for a satisfactory interpretation of the cloud features, at least for the case of a first mission.

## Table 5.4

instrument evaluation for tiz categories of atmospheric dynamics and active processes

|  | N゙ in \％ |  |
| :---: | :---: | :---: |
|  | N゙ in \％ | 1 侖 |
|  |  |  |
|  |  |  |
|  |  | 1 軼 |
|  |  |  |
|  |  |  |
|  |  | $\begin{gathered} \text { oxnzonazs } \\ \text { ofxaydsouzv } \\ \text { た̂t } \end{gathered}$ |

INSTRUMENT EVALUATION FOR CATEGORY OF PLANETARY PARTICLES AND RADIATION
Table 5.5 illustrates the results of the science and instrument evaluations
for the Regime Category of Planetary Particles and Radiation. The applicable flyby instruments as deduced from the results of Sections 5.1 and 5.2 are given in the third column, which is then followed by the maximum percentage value that the instrument was judged to be capable of providing. This maximum instrument value represents the percentage of the total Category Objective value that the instrument could provide under ideal conditions. The values given in Table 5.5 are a result of value judgments that were made in relation to the estimated capability of the instrument data to provide new knowledge concerning the Objective Measurables given in Figure 4.8.
 all cases been judged as equal to the maximum values that could be expected. The reason for this is the fact that the trajectory profiles at the planets have a relatively minor influence on the worth of particles and fields experiments, in contrast to the high degree of influence for many other types of experiments.
Table 5.5


| $\left\lvert\, \begin{aligned} & \text { Regime } \\ & \text { Category } \end{aligned}\right.$ | Category Objectives | Applicable Flyby Instrument | Maximum Value (\%) of Instrument Relative to |  | $\begin{aligned} & \text { tary V } \\ & \text { Relati } \\ & 1977 \end{aligned}$ |  | nstruective ory |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Jup. | Sat. | Uran. | Nept. |
| uofyefpey pus setofyded kiegourid <br> (50\%) | $\begin{gathered} \text { Particles } \\ (36 \%) \end{gathered}$ | 1. -meteorite Detector <br> 2. Cosmic Ray Detector <br> 3. Ionization Chamber and Trapped Particle Det. | 10\% | 10\% | 10\% | 10\% | 10\% |
|  |  |  | 10\% | 10\% | 10\% | 1.0\% | 10\% |
|  |  |  | 30\% | 30\% | 30\% | 30\% | 30\% |
|  | InteractionwiththeInterplanetaryMedia(28\%) | 1. Plasma <br> 2. Magnetometer Package <br> 3. Ion Chamber and Trapped Part. Det. | 25\% | 25\% | 25\% | 25\% | 25\% |
|  |  |  | 25\% | 25\% | 25\% | 25\% | 25\% |
|  |  |  | 25\% | 25\% | 25\% | 25\% | 25\% |
|  | $\begin{aligned} & \text { Planetary } \\ & \text { Radiation } \\ & \text { (24\%) } \end{aligned}$ | 1. Narrow Band UV Photometer \#3 | 15\% | 14\% | 10\% | 10\% | 10\% |
|  |  | 2. IR Radiometer <br> 3. -wave Radiometer | 20\% | 20\% | 20\% | 20\% | 20\% |
|  |  |  | 15\% | 15\% | 15\% | 15\% | 15\% |
|  | $\begin{aligned} & \text { Solar } \\ & \text { Influx } \\ & \text { (12\%) } \end{aligned}$ | 1. Plasma Probe $\left(a+p^{t}\right)$ <br> 2. Cosmic Ray Detector | 20\% | 20\% | 20\% | 20\% | 20\% |
|  |  |  | 10\% | 10\% | 10\% | 10\% | 10\% |

INSTRUMENT EVALUATION FOR THE CATEGORIES OF PLANETARY FIELDS,
PLANETARY STRUCTURE, AND PLANETARY ACTIVE PROCESSES
Table 5.6 gives the instrument evaluation results for those science objectives presented previously in Figures 4.7, 4.10, and 4.11. As before, only those
 in Table 5.1. The value judgments show that in general the applicable instruments have a small capability toward fulfilling the total science measurable requirements of their Category Objectives, with the possible exception of the magnetometer package which could yield $30 \%$ of the desired data on the planetary Magnetic Field objective.
The only two Category Objectives for which the trajectory profiles and other constraints were judged to reduce the instrument effectiveness below its maximum
capabilities were Geometric Shape and Dynamics of the Planet. The value judgments here were based on a study of the available Earth-based data, with the conclusion that some of the measurables were already known to the desired accuracy. This was particularly true for the inner-most of the Jovian planets as shown in the last four columns of Table 5.6.

Table 5.6
instrument evaluation for the categories of planetary fields, planetary structure, and planetary active processes

| $\begin{aligned} & \text { Regime } \\ & \text { Category } \end{aligned}$ | Category Objectives | Applicable Flyby Instrument | Haximum Value (\%) of Instrument Relative to Objective | Planetary Value of Instrument Relative to Objective for 1977-E Trajectory |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Jup. | Sat. | Uran. | Nept. |
|  | Magnetic Field (72\%) | 1. Magnetometer | 30\% | 30\% | 30\% | 30\% | 30\% |
|  | $\begin{aligned} & \text { Gravity } \\ & \text { Fility } \\ & (20 \%) \end{aligned}$ | 1. Trajectory Data | 10\% | 10\% | 10\% | 10\% | 10\% |
|  | $\begin{aligned} & \text { Surface } \\ & \text { Structure } \\ & (28 \%) \end{aligned}$ | 1. Radar | 10\% | 10\% | 10\% | 10\% | 10\% |
| (33\%)新 <br>  (33\%) | $\begin{aligned} & \text { Geoanetric } \\ & \text { Shape } \\ & \text { (12\%) } \end{aligned}$ | 1. TV \#1 <br> 2. Occulation Data | $\begin{array}{r} 15 \% \\ 5 \% \end{array}$ | $\begin{array}{r} 5 \% \\ 1 / 2 \% \end{array}$ | 9\% $3 \%$ | $\begin{array}{r} 15 \% \\ 5 \% \end{array}$ | $\begin{array}{r} 15 \% \\ 5 \% \end{array}$ |
|  | $\begin{gathered} \text { Dyanmics } \\ \text { of the } \\ \text { Planet } \\ \text { (12\%) } \end{gathered}$ | 1. TV \#1 | 1\% | --- | 1/20\% | 1/5\% | 2/5\% |

INSTRUMENT EVALUATION FOR CATEGORIES OF PRIMEVAL CONDITIONS
AND PRIMORDIAL SUBSTANCES The science evaluation and ar.plicable flyby instruments for the Regime Categories of Primeval Conditions and Primordial Substances are presented in the first three colums of Table 5.7. The principle instrument considered is a narrowband photometer for the purpose of studying the UV-IR absorption spectra of various molecular constituents (see the Objective Measurable listings of Figures 4.12 and 4.13).
The estimated maximum capability of the Absorption UV-IR Photometer was judged as $70 \%$ of the respective Category Objective values as shown in the fourth column of contribution of $25 \%$. One of the major difficulties is that the absorption spectra associated with Pre-Life Molecules and Life-Associated Substances are very complex, and there is considerable doubt as to whether they can be identified through the background absorption bands of the regular atmospheric constituents on the Jovian planets. The worth evaluation presented in Table 5.7 has been based on the premise that technology development can resolve this problem by the 1977-1978 time frame. In this instance, the planetary value of the instrument at Jupiter was reduced because a sufficient amount of data could be obtained from Earth-based studies on this planet.

INSTRUMENT EVALUATION FOR THE CATEGORIES OF INTERPLANETARY FIELDS,

## INTERPLANETARY PARTICLES, AND AGGLOMERATE MATTER

Table 5.8 reiterates the science evaluation results that were presented previously in Figures $4.15,4.16$, and 4.17. The applicable flyby instruments are also given along with the value judgment for the maximum percentage value that the instrument data could contribute towards fulfilling the science objectives. In all cases, except for the Asteroids, the full instrument value is available for each planetary interval. The reason for this, of course, is that the trajectory profiles at each planet have no effect on the instrument worth since the science objectives pertain only to interplanetary space. Since data is desired throughout the solar system, each of the intervals measured from the sun (i.e., 1-5 AU, 5-10 AU, 10-20 AU, and 20-100 AU) was attributed full value. The asteroid belt is located at about 2.8 AU , therefore the meteroid detection for sensing asteroid materials has value only for the 1-5 AU interval as indicated in the planetary value columns of Table 5.8.
I


In Tables 5.3 through 5.8, the column indicating the Maximum Value (\%) of Instrument Relative to Objective gives the judgment as to what percentage of the total Category Objective value that a particular instrument could possibly fulfill assuming ideal conditions with an optimum trajectory profile. It should be noted that in most cases the indicated instrument is of such a nature that its scientific data pertains only to some fraction or portion of the total number of Objective Measurables which constitute the Category Objective as listed in the second column. Thus in all cases, no one particular instrument has been judged capable of fulfilling $100 \%$ of the science requirement. In fact, in most cases, even the use of several different instruments for the purpose of obtaining data on the measurables of a particular Category Objective was not judged as sufficient to yield a $100 \%$ relative value. The reason for this is that complete fulfillment requires the use of probes and in situ measurements in addition to remote sensing data.

The final columns in the tables give the adjusted value for each instrument at each planetary target. This adjusted value corresponds to the 1977-E trajectory profiles that were presented in Section 2. For those cases in which the compatability between the instrument and the trajectory profile at a particular planet was judged to be sufficiently close to an ideal situation, the relative value of the instrument at this point was taken to be equal to the maximum
value of the instrument given in the fourth column. For those cases in which the interrelation was uut judged to be satisfactory, the instrument value was reduced accordingly to a percentage number somewhat less than the maximum attainable value.

There were many factors which entered into the value judgments associated with the last four columns of Tables 5.3 through 5.8. The trajectory profile data given in Section 2 wās perhaps the most critical (see Figures 2.27 through 2.39). The encounter trajectories for the 1977-E opportunity are given respectively for Jupiter, Saturn, Uranus and Neptune in Figures 2.27 through 2.30. These profiles provide data on the distance from the spacecraft to the planet, as well as indicating the time differential (in hours) between periapse and a given position on the trajectory path. Figure 2.31 is a plot of the time differential to periapse as a function of true anomaly for each of the Jovian planets. This data was used in assessing the degree of commonality of the various instruments in regards to the total data acquisition times available at each of the Jovian planets. A plot of altitude versus true anomaly is shown in Figure 2.32, and was used to determine the surface resolutions attainable with individual instruments. The sun elevation profiles of Figure 2.33 was useful in assessing the worth of TV systems and other instruments requiring illumination. Similarly the ground speed traces of the sub-satellite point (see Figure 2.34) were
required to determine whether or not those instruments, sensitive to relative motion, could $:$ : used at each of the outer planets. The data of Figure 2.35 gives the illuminated area that is visible, and hence the total coverage available from spacecraft TV and related instruments. Finally, the ground traces as a function of latitude and longitude (see Figures 2.36 to 2.39) give the planetary coverage available when data is obtained only at the sub-satellite point.

The profile data discussed above was used along with other information, such as the planetary black-body emission curves of Figure 5.3 and the curves for the incident solar radiation to the upper atmosphere (from which the reflected flux from the planet can be estimated by using published values for the albedo) shown in Figure 5.4, to determine the effectiveness of each instrument in relation to its capability to detect the existing radiation levels, provide adequate spatial resolution, etc.

As a further illustration, the criteria used for judging whether an instrument was capable of providing adequate spatial resolution was based on the fact that present Earthbased telescopes can provide a resolution of about $0.1^{\prime \prime}$ of arc in the $U V$ and visual wavelength regions. This corresponds to a linear resolution of approximately 300 km on Jupiter, 620 km on Saturn, 1300 km on Uranus, and 2100 km on Neptune. Thus for those instruments (operating in the UV and visual range) dependent on spatial resolution, the maximum relative


FIGURE 5.3. THEORETICAL BLACK-BOOY EMISSION FOR THE JOVIAN PLANETS.


FIGURE 5.4. INTENSITY OF SOLAR RADIATION INCIDENT TO THE UPPER
ATMOSPHERES OF TRE OUTER PLANETS
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value was permissible only if the obtainable resolution was increased by an order of magnitude (i.e., $30,60,130$, and 210 km resolution respectively for Jupiter, Saturn, Uranus, and Neptune). For the IR and $\mu$-wave regions, the desired resolutions were taken to be about a factor of 10 greater than the limits given above.

The reasoning used in the judgments for the planetary value of the instruments is discussed briefly on the title pages accompanying each of Tables 5.3 through 5.8. It should be emphasized that the percentage value assigned to each instrument is relative to the Category Objective value as was apportioned to the individual planet in Table 4.1.

### 5.4 Instrument Values

The instrument evaluation results of the previous sections are summarized in Table 5.9. The first column lists the flyby instruments that were considered in Tables 5.3 through 5.8. These instruments are ordered according to their "value per unit weight." The second and third columns of Table 5.9 give respectively a brief description of each instrument and its weight. This data was drawn from Section 5.2 as well as from published literature concerning spacecraft instrumentation.

The "Values" columns of Table 5.9 represent the total value (in arbitrary units) of each instrument at each planet

relative to the overall goal of Examination of the Jovian Planets and Interplanetary Space. The values given under each planetary heading indicate the additive worth of each particular instrument at that planet. In other words, the worth values are obtained by summing the individual contributions of an instrument over all of the Category Objectives to which that particular instrument contributed scientific data. Thus for example, at Jupiter, the meteoroid detector had an estimated capability of fulfilling $10 \%$ of the total worth attributable to the Category Objective of (planetary) Particles (see Table 5.5), $75 \%$ of the worth attributable to Meteoroids and $10 \%$ of the worth attributable to Asteroids (see Table 5.8). From the basic science evaluation that was summarized in Table 4.1, it is seen that these Category Objectives had values relative to the overall goal of 12 , 7.3 and 19 respectively at Jupiter. The additive worth of the meteoroid detector is thus given by

$$
(.1)(12)+(.75)(7.3)+(.1)(19) \simeq 8.6
$$

which when multiplied by a factor of 10 (for convenience, all worth values in Table 5.9 have been multiplied by a factor of 10 ) corresponds to the tabulated result.

It might be noted that, since the original goal
was arbitrarily based on a value of 1000 and also the values in Table 5.9 have been multiplied by the factor 10 , the worth values given in Table 5.9 are uniformly a factor of 100 .
greater than their actual numerical percentage contribution toward the overall Goal of Exploration. The last "Value" column of Table 5.9 gives the total instrument value when summed over all planets. Thus, for example, it is seen that a meteoroid detector is capable of yielding scientific data which contributes about $2.8 \%$ of the total knowledge that is desired about the outer portions of the solar system. A magnetometer package, on the other hand, could yie1d 7.6\% of all desired data if operative during the complete mission. The corresponding percentages for the other instruments are evident from Table 5.9.

As indicated in the previous sections, the economics of spaceflight and the usual restrictions on the total permissible payload weight indicate that it is desirable to include instrument weights as a factor in making payload selections. For this reason, the value per unit weight of each instrument type has been calculated using the "total value" and the "weight" indicated in the third column. These results are given in the value/weight column of Table 5.9, and the order of the instrument listing in the table have been based on these ratios. The final column of Table 5.9 is a tabulation of the Category Objectives to which instruments contributed scientific data (see also Tables 5.3 through 5.6). An exception to the above should be noted, in that the value contributions of the Absorption UV-IR Photometer to the Sategory Objectives of Pre-Life Molecules
and Life Associated Substances (see Table 5.7) have been omitted from the computations leading to Table 5.9. The reason for this omission was based on the fact that there are no presently known absorption lines from which measurables such as proteins, amino acids and other complex organic molecules could definitely be identified. If future research provides a means of interpretating these complex spectra when superimposed with the other absorption spectra of the atmospheric contituents, the estimated worth of the absorption photometer would have to be reevaluated.

The major results of the instrument evaluation can be presented in graphical form as shown in Figure 5.5. This graph represents the accumulative scientific value, that is obtained by adding successive instruments to the overall payload, as a function of payload weight. The order for addiag each ac'ditional instrument was based on the priority selection in accordance with the highest value/weight as given in Table 5.9. Since the slope of each segment of the curve is equal to the value per unit weight of the indicated instruments, the greatest increase in the payload science value occurs for those initial instruments of highest value per unit weight.

Also shown in Figure 5.5 are the payload values for hypothetical missions which terminate first at Jupiter, then Satuin, and also the case for the first three Jovian planets. These curves illustrate clearly the added science

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value between successive encounters is approximately equal. This results from the iigh degree of commonality between the selected flyby instruments, i.e., the majority of the instruments are of comparative importance at each target planet.

It is clear from Figure 5.5. that, given a fixed payload weight, the instrument package can be readily selected which yields the highest scientific value. Thus for example, for an optimum 26 lb payload would contain only particles and fields experiments (i.e., meteoroid detector, magnetometer package, cosmic ray detector, plasma probe, and the ion and trapped particle package). An optimum 60 lb payload would permit inclusion of a low resolution TV system as a part of its priority instruments. Further discussion associated with payload selections will be covered in Section 6.

The results presented above pertain specifically to the 1977-E mission opportunity to the Jovian planets. It is appropriate at this stage to discuss the evaluation results for the other opportunities that were analyzed in Section 2. Changes in the mission opportunities affect only the final stage of the evaluation scheme in which the influence of the trajectory profiles at each planet was analyzed. Thus, reevaluation for the 1977-I (where " $I$ " denotes passage interior to Saturn's rings), 1978-I, and 1978-E opportunities involves only the planetary instrument percentage values in the last four column of Tables 5.3 through 5.8. A re-assessment of the instrument weights given in Table 5.9 is also required
in some cases in order to compensate for such things as telescopic lens that are necessary to meet the desired constraints on spatial resolution.

A comparison of the 1977-I and 1978-I trajectory profiles showed that the major difference is that the miss distances are almost uniformly greater at each planet for the 1978 opportunity than they were for 1977. Thus the relative instrument value judgements are approximately the same for both cases, although the weights of some instruments (such as TV) must be increased to obtain adequate resolution. On the other hand, a comparison of the 1977-I and 1977-E opportunities showed that the approach distances to the planets are less at each target for the case of the interior ring passage. This change is not particularly significant, except for the case of Saturn, as can be seen from Figures 5.6 and 5.7. It should be noted that it is only on the nightside of Saturn that a very close approach to the surface occurs. Since most of the instruments (whose data and resolution are dependent on spacecraft altitude) operate principally on the sunlit side, the trajectory profiles for Saturn, Uranus, al.d Neptune in Figure 5.7 are approximately equivalent for the purposes of instrument evaluation. Therefore the relative changes in the spacecraft profiles, between the 1977-E and 1977-I opportunities, are of the same order of magnitude for all of the outer planets. Also the corresponding instrument

! denotes sun terminator


FIGURE 5.6. ALTITUDE VS. TRUE ANOMALY, 1977-E GRAND TOUR


FIGURE 5.7. ALTITUDE VS. TRUE ANOMALY, 1977-I GRAND TOUR.
weights are altered only by a small percentage factor between the 1977-E and 1977-I opportunities.

The net result is that the evaluation results presented for the 1977-E opportunity are also essentially valid for the 1977 -I passage. Although the instrument evaluation numbers and the weights are altered slightly in some cases, the general trends and priority orders that were given in Table 5.3 and Figure 5.5 are still valid. The same conclusions apply for a comparison between the $1978-\mathrm{E}$ and 1978-I opportunities. A comparison between a 1977 and 1978 opportunity results in higher weights for many of the instruments in the 1978 mission. However, the general priority trends remain relatively unchanged, in particular the particles and fields instruments retain their highest rank. The remaining possibility involves a trajectory passing through the Cassini gap in Saturn's rings. The evaluation results for this case were intermediate between those for the interior and exterior ring passages. However, this particular mission opportunity was not seriously considered bacause of the uncertain density of particulates within the gap and their effect on spacecraft survival.

A capsule summary of the accomplishments and conclusions obtained in Sections 4 and 5 can be stated as follows:

1. An effective methodology was developed which resulted in a logical evaluation IIT RESEARCH INSTITUTE
scheme for both the pure science objectives and the instrument payloads.
2. The evaluation of the science objectives resulted in the highest priority values being attributed to objectives associated with the atmospheres of the Jovian planets.
3. 

In contrast, the worth evaluation of applicable flyby instruments gave the highest values to particles and fields experiments. This conclusion was a direct result of the commonality feature of these instruments, in that they contribute knowledge toward i Planetary Particles \& Fields, as well as to Interplanetary Medium objectives.
4. The scientific value of the instrument payloads per planet are of approximately equal worth. In other words, the additional increment of science value gained as each target is encountered during the outer planet mission is roughly the same for each of the planets. This is true for all payload weights.
5. The exterior and interior Saturn ring passage opportunities for a given year yield trajectory profiles that have nearly equal payload values. Therefore, a choice between the 1977-I and 1977-E opportunities will depend principally on a tradeoff between guidance requirements and spacecraft survival probabilities.
6. The relative instrument values are approximately the same for 1978 opportunities as in 1977, although the instrument weights tend to be slightly higher in 1978. Thus the 1977 opportunities may be favored to those in 1978.

## SECTION 6

## MISSION REQUIREMENTS FOR THE GRAND TOUR

by
D. L. Roberts

Page
Payload Selection
Typical Spacecraft Weights $\quad \begin{aligned} & 228 \\ & 232\end{aligned}$

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## 6. Mission Requirements for the Grand Tour

The previous sections have dealt with the three most important problem areas of the Grand Tour Mission, namely trajectory selection, guidance, and experiment evaluation. This section of the report will combine the results of these analyses together with considerations of other, less critical, subsystems, into an assessment of the overall spacecraft weight and the launch vehicle requirements for the mission.

### 6.1 Payload Selections

The evaluation of scientific experiments, and their ordering in terms of value per pound, as discussed in Section 5, allows scientific payloads to be selected on the basis of their contribution to the mission. It can be noted from the experimental value curves of Figure 5.5 (page 5 ) that the scientific experiments fall into two major categories. There are a group of particles and field experiments, with high value per 1 lb , which constitute the "steep" part of the curve and there is the "plateau" region of the curve where little value is added per additional pound of experiments. It is the first group of experiments which has been used to define the "minimum" payload for the Grand Tour Mission.

Table 6.1 shows the division of the experiments into four payloads. The term "minimum" is used in the sense that it is felt that any liesser investment in experiments would


[^5]TABLE 6.1 SELECTED SCIENCE PAYLOADS (ACCUMULATIVE)
render the mission not worthwhile. A nominal bit rate of five bit per second will be adequate to transmit all the data from these experiments. This payload derives much of its value from the interplanetary phase of the mission. This is shown in Figure 6.1 where there is only a small step increase in value as each planet is intercepted. In truth, this minimum payload would barely justify the complexity of the Grand Tour Mission.

By the ac tion of the next four experiments a "small" payload is derived. These four experiments are all planetary oriented and will provide much useful data on each of the outer planets. The position at which to draw the line between one payload and another is never quite clear and has been guided here by consideration of the required data bit rate. Without a TV system, the small payload achieves considerable value as seen in Figure 6.1 but its data requirement is still relatively nominal, i.e., five bits per second throughout the mission and a total of $10^{5}$ bits for the planetary intercepts. The experiment next in importance is indeed the TV system and it adds some $2 \times 10^{8}$ bics at each planetary encounter. However it is also possible to include the next five experiments as well, without adding markedly to the power requirements or bit rate. Therefore the "medium" payload contains the first fourteen experiments and stops just short of the high resolution TV system. The "large" payload contains all the experiments considered in this study. In power and data, it has


FIGURE 6. I. INTEGRATED SCIENCE VALUE OF PAYLOADS.
approximately twice the requirements of the medium payload. It is heavily planet oriented and from Figure 6.1 it can be seen to make a major scientific contribution at each target.

### 6.2 Typical Spacecraft Weights

On the basis of selected payloads and the overall guidance requirements, an attempt has been made to estimate the total spacecraft weight to perform the Grand Tour Mission. This leads directly to an estimate of the launch vehicle requirements for the mission. The weight estimates which follow are not based on any specific spacecraft design, conceptual or otherwise. They are extrapolations, on a subsystem weight basis, from other more detailed engineering studies (Goddard 1967, General Dynamics 1966, TRW 1966) and using the Mariner ' 67 as the technclogy base.

There are a range of Grand Tour Mission which have different requirements and hence different spacecraft weights. There are four selected trajectories with their associated, and quite distinct, midcourse velocity requirements depending on whether a planet seeker or radar tracking is used. There are four selected payloads each with its own power and data requirements. Rather than select a typical example, a matrix of information is presented which will bound all the variables of the Grand Tour Mission. Table 6.2 shous the way in which the spacecraft weight totals have been built up. This applies to the 1977 E opportunity and includes minimum and medium

| SUB SYSTEM | MINIMUM PAYLOAD |  |  | MEDIUM PAYLOAD |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | TRACKER | RADAR |  | TRACKER | RADAR |
| Science | MINIMUM | 21 LBS | 21 LBS | MEDIUM | 137 LBS | 137 LBS |
| COMMUNICATIOMS | 20 bps Jup. |  |  | 400 bps JUP. |  |  |
| 10/20 WATT | 24 SAT. |  |  | 150 SAT. |  |  |
| 8' ANTENMA | 13 UR. | 50 | 50 | 40 UR. | 100 | 100 |
|  | 5 NEP. |  |  | 15 NEP. |  |  |
| POWER | 125 WATTS | 125 | 125 | 250 WATTS | 250 | 250 |
| guidance | Including tracking | 110 | 230 | InCLUDING TRACKING | 180 | 410 |
| ATtitude control | 3-AXIS | 60 | 80 | 3-AxIS | 120 | 160 |
| data and sequencing | $5 \times 10^{4}$ BITS STORE | 100 | 100 | $2 \times 10^{8} \mathrm{BITS}$ STORE | 150 | 150 |
| THERMAL CONTROL |  | 40 | 40 |  | 60 | 60 |
| STRUCTURE AND MISC. | 20\% | 100 | 110 | 20\% | 190 | 240 |
| Estimated total weie |  | 605 LBS | 760 LBS |  | 1180 LBS | 1500 LBS |

TABLE 6.2 SUB-SYSTEM WEIGHT ESTIMATES (I977E)
payloads with either a planet tracker or radar tracking for guidance. The science payload weights are taken directly from Table 6.1.

The communications requirements are calculated somewhat as a compromise. In all cases it is necessary to accommodate the minimum data rate from the furthest target (Neptune) plus sufficient in excess to transmit the planetary data after intercept within a reasonable time. For the "minimum" payload, rates of $20,24,13$, and 5 bits per second, at the respective planets, are achieved by utilizing an 8 foot diameter spacecraft antenna and a $10 / 20$ watt transmitter. The system uses 20 watts and the $85^{\prime}$ DSIF combination out to Jupiter, 10 watts and the $210^{\prime}$ DSIF out to Saturn, and 20 watts'and the $210^{\prime}$ DSIF beyond Saturn. The excess capability at Jupiter, Uranus, and Saturn would make this same communication system suitable for the "small" payload as well. It would then on1y take approximately 2 hours to transmit the $10^{5}$ bits of planetary data at Jupiter and Saturn, about four hours at Uranus, and about eight hours at Neptune.

The "medium" payload requires a larger communications capability and uses a $20 / 50$ watt transmitter with an 8 foot diameter spacecraft antenna. The $210^{\prime}$ DSIF dish and the full 50 watts of power will be required for the data at each intercept, yielding rates of $500,125,30$, and 13 bits per second, respectively. After intercept with Neptune, it would take some two months to transmit all the data at the rate of

13 bits per second. This is probably inadequate and consideration should be given to increasing the spacecraft antenna diameter beyond 8 feet or to increasing the spacecraft transmitter power. For the interplanetary data the 20 watt transmitter can be used with the $85^{\prime}$ DSIF as far as 7 Au and the 50 watt transmitter can be used with the $85^{\prime}$ DSIF as far as Saturn. This same transmitting system can be used for the large payload as well but will require about twice the time to transmit all the data after each planetary intercept.

The power sequirements for the spacecraft have been assumed as 125 and 250 watts respectively in Table 6.1. These should be adequate to supply all the experimental requirements, the communications system, and the engineering functions of the spacecraft. Slightly larger powers will probably be required for the small and large payloads and values of 150 and 3,00 watts respectively have been used. In all cases a R.T.G. system was assumed as the sole power supply and specific weights of one pound per watt were used to represent the total subsystem weight including shielding and power conditioning.

The guidance requirements are different for each opportunity, for each payload weight, and for each tracking system. Table 6.3 shows the total guidance subsystem weight estimates for all mission options. In all cases the majority of the weight is invested in the propulsion system. An $I_{s p}$ of 235 seconds has been used in all the calculations and the propulsive mass fractions have been taken from Section IV-F-3

| TRAJECTORY | TRACKIMASYSTEM | $\begin{gathered} \text { MIDCOURSE } \\ \text { DV } \end{gathered}$ | SUB-SYSTEM WEIGHT |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \text { MINIMLMM } \\ & \text { PAYLOAD } \end{aligned}$ | $\begin{aligned} & \text { SMALL } \\ & \text { PAYLOAD } \end{aligned}$ | MEDIUM PAYLOAD | $\begin{aligned} & \text { LARGE } \\ & \text { PAYLOAD } \end{aligned}$ |
| 1977E | OM-BOARD | $190 \mathrm{M} / \mathrm{SEC}$ | 110 LBS | 120 LBS | 180 LBS | 210 LBS |
|  | radar | 450 | 230 | 260 | 410 | 540 |
| 19771 | OM-BOARD | 430 | 230 | 255 | 390 | 510 |
|  | RADAR | 1710 | 1300 | 1600 | 2300 | 2700 |
| 1978E | OH-BOARD | 200 | 115 | 125 | 190 | 220 |
|  | radar | 350 | 155 | 170 | 280 | 330 |
| 1978I | On-B0aRD | 375 | 180 | 195 | 315 | 370 |
|  | radar | 1010 | 550 | 600 | 1000 | 1200 |

TABLE 6.3 SUBSYSTEM WEIGHT FOR MIDCOURSE GUIDANCE (INCLUDING PROPULSION)
of the Launch Vehicle Estimating Factors (1968). A tracking subsystem weight of 30 pounds was assumed for the planet tracker system and of 10 pounds for the earth based radar tracking system and are included in the table. The overall weight penalty with radar tracking particularly for the inner ring passage missions, is clearly demonstrated in Table 6.3. The attitude control system weights are a function of the moment of inertia of the spacecraft and hence of its mass and size. Table 6.4 shows the total attitude control subsystem weight estimates (including propellant) for each of the mission options. They are all based on a mission daration of 10 years using nitrogen cold gas in a hard limit cycle, three axis system. The weight estimates are based on the Mariner IV technology. No special contingency has been allowed for passage through the asteroid belt.

The data storage and sequencer subsystem weights are again based on Mariner technology. The subsystem weight for the minimum payload has been estimated at 100 pounds. This has been increased for the larger payloads because of the increased storage requirement and because of the added complexity of the experimental sequences. Weights of 120 , 150 , and 200 pounds have been allowed for the "small", "medium" and "large" payloads respectively.

The thermal control subsystem has been assumed to be largely passive. Since an RTG system is included, it is assumed that it will be possible to pipe its excess heat

| TRAJECTORY | TRACKIMGSYSTEM | SUBSYSTEM WEIGht |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | MIMIMLY PAYLOAD | $\begin{aligned} & \text { SMALL } \\ & \text { PAYLOAD } \end{aligned}$ | MEDILMM <br> PAYLOAD | $\begin{aligned} & \text { LARGE } \\ & \text { PAYLOAD } \end{aligned}$ |
| 1977E | OM-BOARD | 60 LBS | 65 LBS | 120 LBS | 160 LBS |
|  | radar | 80 | 100 | 160 | 200 |
| 19771 | On-B0ard | 80 | 100 | 155 | 190 |
|  | radar | 250 | 275 | 400 | 500 |
| 1978E | OM-BOARD | 60 | 65 | 120 | 160 |
|  | radar | 70 | 85 | 140 | 180 |
| 1978I | OM-BOARD | 75 | 90 | 140 | 180 |
|  | Radar | 150 | 160 | 250 | 300 |

TABLE 6.4 SUBSYSTEM WEIGHT FOR ATTITUDE CONTROL (INCLUDING PROPELLANT)
output to most parts of the spacecraft. Nominal weight allowances of $40,50,60$, and 80 pounds have been allowed for the thermal control subsystem weight for the four payloads considered. These weights have been assumed not to vary with the opportunity.

The spacecraft's structure has been assumed to absorb $10 \%$ of the spacecraft weight. In addition $10 \%$ has been added for miscellaneous contigencies which must include redundancy to permit adequate reliability for the 10 year mission duration.

The total spacecraft weight estimates are given in Table 6.5 for all the mission options. They range from 605 lbs for a "minimum" payload mission using the 1977 E opportunity with an onboard planet tracker, to 4900 lbs for the "large" payload mission using the 1977 I opportunity with radar, tracking. Table 6.5 also shows the capabilities of four launch vehicles for comparison with the estimated total spacecraft weights. The SLV3X-Center-TE364 can be used only for the 1977 E mission and then its 750 lb capability will only deliver the "minimum" and "small" payloads, with onboard tracking. A 5 segment Titan III D-Centaur is not adequate for the incerior ring passage missions. It can be used for all the 1977 exterior opportunities with onboard tracking, and for "medium" payloads with radar tracking. For the 1978 exterior missions, only "medium" and "small" payloads are possible for onboard and radar tracking respectively. The

|  |  | SPACECRAFT WEIGHT |  |  |  | LaUNCH VEHICLE CAPABILITY |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| MISSIOM | TRACKING | MINIMUM | SMALL | MEDIUM | Large | $\begin{aligned} & \hline \text { SLV } 3 \mathrm{X} \\ & \text {-CENT-364 } \end{aligned}$ | $\begin{aligned} & \text { T1IID } \\ & - \text { CENT } \end{aligned}$ | $\begin{aligned} & \text { TIIID } \\ & \text {-CENT-BII } \end{aligned}$ | $\begin{aligned} & \text { T111F } \\ & \text {-CENT } \end{aligned}$ |
| $1977 E$ | OM board | 605 | 725 | 1180 | 1560 | 750 | 1900 | 2200 | 3300 |
|  | RADAR | 760 | 930 | 1500 | 1950 |  |  |  |  |
| 19771 | OM BOARD | 760 | 925 | 1480 | 1900 | - | - | 1450 | 2000 |
|  | RADAR | 2270 | 2750 | 4060 | 4900 |  |  |  |  |
| 1978E | ON BOARD | 620 | 730 | 1190 | 1510 | - | 1250 | 1700 | 2500 |
|  | RADAR | 675 | 810 | 1330 | 1650 |  |  |  |  |
| 1978I | ON BOARD | 720 | 850 | 1365 | 1710 | - | - | 1000 | 1200 |
|  | radar | 1250 | 1300 | 2330 | 2850 |  |  |  |  |

TABLE 6.G COMPARISON OF LAUNCH VEHICLE CAPABILITY WITH SPACECRAFT WEIGHT
addition of a burner II stage makes the Titan III D-CentaurBurner II launch vehicle adequate for all exterior ring passages. It can also support interior missions in 1977 and 1978 with "small" payloads provided onboard tracking is used. Finally for comparison a seven segment Titan III FCentaur launch vehicle capability is included but it offers 1ittle advantage over the Titan III D-Centaur-Burner II. If it is contemplated that missions will be attempted at both the 1977 and 1978 opportunities with a common spacecraft design and launch vehicle, then the possiole options are quite restricted. These are shown in Table 6.6. The smallesi acceptable launch vehicle is a Titan III-Centaur and this will only launch a "medium" payload with onboard tracking, or a "small" payload using radar. The Titan III-D Centaur-Burner II will launch all exterior missions and "small" interior missions with onboard tracking. It should however be re-emphasized that these conclusions are based on weight estimates that are indeed just estimates and have not been derived from a specific spacecraft conceptual design study.

table 6.6 Launch vehicle capability for common 1977-78 missions

In advance of a discussion of the conclusions of this study, it is important to reiterate the purpose of the study, which was to provide preliminary data on the major problem areas associated with the Grand Tour Mission concept. The study has therefore concentrated on two major problem areas, guidance and scientific compatability. In both instances it has been shown that the requirements are tractable and that the mission warrants detailed definition and conceptual design effort.

The recommended launch years for the Grand Tour Mission are 1977 and 1978. The alignment of the planets will make five launch years possible (1976 to 1980), and at each opportunity it is possible to go inside or outside the rings of Saturn. A brief analysis has shown a potentially high collision rate if the spacecraft penetrates the rings of Saturn. The 1976 opportunity has been rejected from detailed consideration because it involves a close passage of Jupiter with penetration of the radiation belts. The 1979 and 1980 opportunities have been rejected because of the high launch energy and the exceedingly large miss distance at Jupiter.

The guidance velocity requirements depend critically on the spacecraft tracking system which is used, on the closeness of passing Saturn, and on the launch opportunity. The exterior ring passages are less demanding than the interior
passages by a factor of three for radar tracking and a factor of two for on-board planet tracking. From a guidance standpoint the 1977 and 1978 exterior missions are recommended. Using an on-board tracker the total velocity requirements, for the 8 midcourse corrections are 190 meters per second and 203 meters per second respectively.

The study has ciemonstrated the scientific compatability of all four outer planets. There is a clear need for knowledge of all four targets. Payloads have been assembled, which will contribute significant data on each of the target planets. The minimum useful payload which ....s. been derived obtains its value from particles and fields measurements mainly in interplanetary space but also to some extent at each target. Its weight is about 20 pounds. . Three other typical payloads are developed and all are able to contribute at Jupiter, Saturn, Uranus and Neptune approximately equally, and each can be designed to retain their value and compatability for either interior or exterior passages. The television system has been found to act as a breakpoint in the payload selection. Its very high data requirements mean that it essentially controls the communications subsystem requirements and therefore to some extent also the power, guidance, and attitude control subsystem weights. Its inclusion in the payload means that many, less demanding experiments can also be included without a significant impact on the overall subsystem
requirements. "Medium" payload weights in the range of 60 to 130 pounds are recommended.

The total spacecraft weights required for all mission options are in the range from 600 to 4000 lbs. The exterior ring passages are strongly recommended and the appropriate weight range for these is reduced to 600 to 2000 lbs for science payload weights between 20 and 200 lbs. An on-board planet tracker is recommended as the most effective tracking system, further reducing the upper limit of the weight range to 1500 1bs. However, for the exterior passages the differences are such that radar could be used as a backup and only the Neptune intercept would be lost if the on-board system failed.

If it is important that the same spacecraft design and launch vehicle be possible at both opportunities, the minimum vehicle is a Titan III-D-Centaur which has a capability of 1900 lbs in 1977 and 1250 lbs in 1978 for the exterior ring passages.

The recommended missions would utilize the 1977 and 1978 opportunities, use an on-board planet tracker, have a payload in the region of 100 lbs weight, and require a total spacecraft weight of some 1200 lbs . In the light of the apparent tractability of all the subsystem requirements for the Grand Tour Mission, it is strongly recommended that conceptual spacecraft deiigns be developed and that the complete feasibility of the mission be verified.

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## APPENDIX A

TARGETING OF INTEGRATED TRAJECTORIES
FOR THE MULTIPLE OUTER PLANET MISSION STUDY USING THE N-BODY CODE

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APPENDIX A<br>TARGETIN: OF INTEGRATED TRAJECTORIES<br>FOR THE MULI'TPLE OUTER PLANET MISSION STUDY USIHC THE N.-BODY CODE

The purpose of this appendix is to expand upon the description of the n-body targeting analysis presented in the text of the report and to present some of the results of the $n$-body targeting program.

The n-body targeting code is used to generate integrated trajectories between Earth and a specifiec target planet. For the multiple outer planet mission study the target planet was Neptune with the trajectory passing close to Jupiter, Saturn and Uranus. An integrated trajectory serves two purposes, 1) to generate sensitivity matrices for the guidance analysis and 2) to check the accuracy of conic approximations to the trajectory.

Targeting is basically the solution of a two point boundary value problem, where desired final conditions and approximate initial conditions are obtained from the computer program SPARC which provides conic interplanetary and planetary flyby trajectories. The program used for the numerical integration of the equations of motion was the Lewis Research Center's $N$-Body code, modified to do both the targeting and the guidance analysis.

The following preliminary material will be presented before the actual method of targeting is discussed:

1. The coordinate systems used at Earth ind at the other planets.
2. The targeting variables used at Earth and at the other planets.
3. The constraints placed upon the targeting variables.

At Earth the reference plane and axis are the mean equator and equinox of date. The center of the coordinate system is at the Earth's center.

At the other planets, the RST coordinate system is used. In this system, the center of the system is at the center of the planet in question. Unit vectors $R, S, T$, are defined as follows: The vector $S$ is a vector parallel to the incoming hyperbolic velocity vector. $T$ is a vector normal to $S$ and parallel to the ecliptic plane. Its direction is determined such that the third vector $R(R=S \times T)$ in the right-handed system points in the direction of the south pole of the ecliptic. The R-T plane is called the target plane.

In order to perform the integration, a starting time and initial values for the variables $x, y, z, \dot{x}, \dot{y}$, and $\dot{z}$ are needed. At Earth these quantities are computed from the
magnitude (VHL) and the direction ( ${ }^{(1)-d e c l i n a t i o n, ~ ©-r i g h t ~}$ ascension) of the outgoing hyperbolic excess velocity vector under the following constraints:

1. The day of launch is taken as the launch date of the SPARC conic approximation to the trajectory.
2. The declination of the launch site is constant at $28.3106^{\circ}$, the declination of Cape Kennedy.
3. The launch azimuth, $\Sigma_{L}$, satisfies the following conditions:
a. $\Sigma_{L}=90^{\circ}$ when $\leq 28.3106^{\circ}$
b. $\quad \Sigma_{L}-90^{\circ}=$ minimum when $>28.3106^{\circ}$
4. Injection is at perigee at an altitude of 100 nautical miles.
5. The parking time, in a circular parking orbit, is the minimum allowable time greater than 2 minutes.

The variables VHL, $\$$ and $\otimes$ are the variables used for targeting at Earth.

At all other planets, the quantities $x, y, z, \dot{x}, \dot{y}, \dot{z}$ and time are computed at the target plane from:

VHP - magnitude of the incoming hyperbolic excess velocity
\$ - declination of the incoming asymptote of the urrival hyperbola
(4) - right ascension of the incoming asymptote of the arrival isyperbola
$B \cdot T$ - the component of $B$ along the $T$-axis where $B$ is the hyperbolic miss parameter, i.e., the vector in the target plane from the center of the planet to the incoming asymptote of the arrival hyperbola.
$B \cdot R$ - the component of $B$ along the $R$-axis
t - the time at which the spacecraft pierces the target plane.

The three variables used for targeting at all planets except Earth are B.T, B.R, and $t$.

The basic procedure in the targeting of any one leg of the trajectory is the determination of the sensitivity of the target variables at any planet to changes in the target variables at the preceeding planet. This is accomplished by computing a matrix of approximate partial derivatives of each of the 3 target variables at the target planet with respect to each of the 3 target variables at the departure planet. The method used to obtain the matrix. is that of finite-difference. With the inverse of this
matrix it is possible to predict corrections to the values of the target variables at the departure planet which will cancel (or decrease) the error in the values of the target variables at the arrival planet.

It was not known initially how great these sensitivities would be, and hence over how many legs it would be possible to target a trajectory. It turned out that the sensitivities were so great that it was possible to target only one leg at a time. For example, in general to come within 100 km of the aiming point in $B \cdot T, B \cdot R$ in the target plane, it was necessary to make changes in the departure conditions which were in the tenths, hundreths or even thousandths of a kilcmeter. However, in most cases, it was only necessary to compute one sensitivity matrix to target one leg and it was never necessary to compute more than two matrices. Even though the actual integration is performed in double precision, the targeting subroutines were written in single precision. Because of this, in trying to target two legs at a time, after the first few corrections, the changes in the departure conditions became so small that they could not be handled by the eight place accuracy of single precision arithmetic. For this reason it was not possible to target more than one leg at a time.

In targeting one leg at a time, targeting was started on the Uranus-Neptune leg. An aiming point was selected at Neptune, and the trajectory was integrated from Uranus to
to Neptune starting with the SPARC arrival conditions at Uranus as initial conditions. The error in the arrival conditions at Neptune was noted and a sensitivity matrix computed by integrating the Uranus-Neptune leg of the trajectory three more times. Then using the inverse of the sensitivity matrix to predict corrections to the initial conditions, the initial conditions were corrected on successive integrations of the trajectory until convergence was obtained at Neptune. The arrival conditions at Neptune for the converged trajectory were called the n-body converged conditions. The Uranus departure conditions for the converged trajectory became the aiming point at Uranus for the integration of the SaturnUranus leg. These departure conditions were called the 'aiming point from n-body convergence.' Targeting was continued in this manner on successive legs until convergence was obtained on the final (Earth-Jupiter) leg. At that time the entire trajectory was considered to be converged.

Because targeting was done using only the three variables, $B \cdot T, B \cdot R$, and time, there was nut complete agreement between the values of VHP, $\mathbf{I}^{\text {, }}$ and (1) for the converged trajectory and the values of VHP, $\Phi$, and * at the aiming point. See the last two columns of Tables 1 through 4 for the discrepancies in these values.

Tables 1 through 4 give the convergence histories of the four trajectories studied. On each of these tables are given 1) the values from SPARC of all the pertinent parameters

Table 1

CONVERGENCE HISTORY OF 1977 E TRAJECTORY

| Planet | Parameter | SPARC Conditions ${ }^{1}$ | Aiming Point from N -Body Convergence ${ }^{2}$ | N-Body <br> Converged Conditions |
| :---: | :---: | :---: | :---: | :---: |
| NEPTUNE | $\begin{aligned} & \mathrm{B} \cdot \mathrm{~T} \text { (KM) } \\ & \mathrm{B} \cdot \mathrm{R} \text { (KM) } \\ & \text { TIME } \\ & \text { E.F. }{ }^{3} \end{aligned}$ | $\begin{aligned} & 8.88 \times 10^{4} \\ & 0.0 \\ & 24477+6.85759735 \end{aligned}$ |  | $\begin{aligned} & 8.8725776 \times 10^{4} \\ & -2.1122848 \times 10^{1} \\ & 2447746.869920335 \\ & 0.1018 \end{aligned}$ |
| URANUS | $\begin{aligned} & \text { B.T (KM) } \\ & \text { B•R (KM) } \\ & \text { VHP (KPS) } \\ & \emptyset \text { (DEG) } \\ & \text { Q (DEG) } \\ & \text { TIME } \\ & \text { E.P. } \end{aligned}$ | $\begin{aligned} & 1.581993 \times 10^{5} \\ & 4.09231 \times 10^{4} \\ & 14.7435 \\ & -1.5304 \\ & 271.1280 \\ & 2446455.72521209 \end{aligned}$ | $\begin{aligned} & 1.5896784 \times 10^{5} \\ & 4.1320698 \times 10^{4} \\ & 14.7435 \\ & -1.5304 \\ & 271.1280 \\ & 2446456.33905181 \end{aligned}$ | $\begin{aligned} & 1.5891677 \times 10^{5} \\ & 4.1369825 \times 10^{4} \\ & 14.721352 \\ & -1.5395862 \\ & 271.143578 \\ & 2446456.338873088 \\ & 0.0712 \end{aligned}$ |
| SATURN | $\begin{aligned} & \text { B•T (KM) } \\ & \text { B•R (KM } \\ & \text { VHP (KPS) } \\ & 0 \text { (DEG) } \\ & \text { (DEG) } \\ & \text { TIME } \\ & \text { E.P. } \end{aligned}$ | $\begin{aligned} & 3.572481 \times 10^{5} \\ & -1.7228 \times 10^{4} \\ & 10.6937 \\ & 2.7472 \\ & 195.3260 \\ & 2444842.59416961 \end{aligned}$ | $\begin{aligned} & 3.5841535 \times 10^{5} \\ & -1.7359508 \times 10^{4} \\ & 10.6937 \\ & 2.7472 \\ & 195.3260 \\ & 2444846.6852323 \end{aligned}$ | $\begin{aligned} & 3.5873812 \times 10^{5} \\ & -1.7746249 \times 10^{4} \\ & 10.669641 \\ & 2.7797137 \\ & 195.4885 \\ & 2444846.684265613 \\ & 0.5057 \end{aligned}$ |
| JUPITER | $\begin{aligned} & B \cdot T \text { (KM) } \\ & \text { B•R (KM) } \\ & \text { VHP (KPS) } \\ & \emptyset \text { (DEG) } \\ & \text { O (DEG) } \\ & \text { TIME } \\ & \text { E.P. } \end{aligned}$ | $\begin{aligned} & 1.9246066 \times 10^{6} \\ & 1.510661 \times 10^{5} \\ & 7.8118 \\ & -3.0377 \\ & 94.3800 \\ & 2444070.0 \end{aligned}$ | $\begin{aligned} & 1.9387916 \times 10^{6} \\ & 1 .: 292970 \times 10^{5} \\ & 7.31180 \\ & -3.0377 \\ & 94.379999 \\ & 2444090.496979 \end{aligned}$ | $\begin{aligned} & 1.9385371 \times 10^{6} \\ & 1.5287049 \times 10^{5} \\ & 7.2031271 \\ & -3.6468103 \\ & 92.817464 \\ & 2444090.496978998 \\ & 0.35348753 \end{aligned}$ |
| EARTH | VHL (KPS) <br> $\emptyset$ (DEG) <br> (B) (DRG) <br> TIME | $\begin{aligned} & 9.5426 \\ & 30.5118 \\ & 64.6384 \\ & 2443388.0 \end{aligned}$ | $\begin{aligned} & 9.4 \cdot 577468 \\ & 32.061232 \\ & 63.501112 \\ & 2443388.039231494 \end{aligned}$ |  |

1. Starting conditions for first n-body convergence run on any leg.
2. Departure conditions corresponding to converged i-body run on any leg.
3. E.P. $=[\text { (error in B.T (KM) })^{2}+{ }^{\text {(error in } B \cdot R ~(K M)) ~}{ }^{2} / 1000+$ error in time (days)/.5]

Table 2
CONVERGENCE HISTORY OF 1977 I TRAJECTORY

| Planet | Parameter | SPARC Conditions ${ }^{1}$ | Aiming Point from N Body Convergence ${ }^{2}$ | N-Body Converged Conditions |
| :---: | :---: | :---: | :---: | :---: |
| NEPTUNE | $\begin{aligned} & \text { B.T (KM) } \\ & \text { B.R (KM) } \\ & \text { TIME } \\ & \text { E.P. }{ }^{3} \end{aligned}$ | $\begin{aligned} & 8.88 \times 10^{4} \\ & 0.0 \\ & 2446702.24283599 \end{aligned}$ |  | $\begin{aligned} & 8.8728759 \times 10^{4} \\ & 4.6033367 \times 10^{1} \\ & 2446702.252454042 \\ & 0.86743 \end{aligned}$ |
| URANUS | $\begin{aligned} & \text { B•T (KM) } \\ & \text { B•R (KMD) } \\ & \text { VHP (KPS) } \\ & \text { (DEG) } \\ & \text { O (DEG) } \\ & \text { TIME } \\ & \text { E.P. } \end{aligned}$ | $\begin{aligned} & 5.54577 \times 10^{4} \\ & 8.9765 \times 10^{3} \\ & 21.2169 \\ & -1.1496 \\ & 266.1723 \\ & 2445717.68746185 \end{aligned}$ | $\begin{aligned} & 5.568189 \times 10^{4} \\ & 9.03539\urcorner 1 \times 10^{3} \\ & 21.2169 \\ & -1.1496 \\ & 266.1723 \\ & 2445717.93804669 \end{aligned}$ | $\begin{aligned} & 5.5598592 \times 10^{4} \\ & 9.0210702 \times 10^{3} \\ & 21.201689 \\ & -1.1556599 \\ & 266.703849 \\ & 2445717.94891575 \\ & 0.63469172 \end{aligned}$ |
| SATURN | B.T (KM) <br> B•R (KM) <br> VHP (KPS) <br> 0 (DEG) <br> $\theta$ (DEG) <br> TINE <br> E, P. | $\begin{aligned} & 1.464489 \times 10^{5} \\ & -5.8615 \times 10^{3} \\ & 16.6908 \\ & 2.3789 \\ & 192.0425 \\ & 2444477.21163177 \end{aligned}$ | $\begin{aligned} & 1.4674225 \times 10^{5} \\ & -5.8921 .234 \times 10^{3} \\ & 16.6908 \\ & 2.3789 \\ & 192.0425 \\ & 2444478.9283927 \end{aligned}$ | $\begin{aligned} & 1.4681419 \times 10^{5} \\ & -5.9170313 \times 10^{3} \\ & 16.693921 \\ & 2.3890921 \\ & 192.1512 \\ & 2444478.950747013 \\ & 0.80600794 \end{aligned}$ |
| JUPITER | B.T (KM) <br> B.R (KN) <br> VHP (KPS) <br> - (DBG) <br> 0 (DRG) <br> TIME <br> E.P. | $\begin{aligned} & 7.537491 \times 10^{5} \\ & 4.74979 \times 10^{4} \\ & 12.1601 \\ & -1.2147 \\ & 99.1286 \\ & 2443902.0 \\ & 2443902.0 \end{aligned}$ | $\begin{aligned} & 7.5512495 \times 10^{5} \\ & 4.7697880 \times 10^{4} \\ & 12.1601 \\ & -1.2147 \\ & 99.1286 \\ & 2443910.3168511 \\ & 2443910.3168511 \end{aligned}$ | $\begin{aligned} & 7.5519466 \times 10^{5} \\ & 4.7049485 \times 10^{4} \\ & 11.683219 \\ & -1.2812889 \\ & 98.958305 \\ & 2443910.350936017 \\ & 0.91673776 \end{aligned}$ |
| EARTH | VHL (KPS) <br> - (DEG) <br> 0 (DEG) <br> TIME | $\begin{aligned} & 10.6865 \\ & 25.5477 \\ & 70.4962 \\ & 2443391.0 \end{aligned}$ | $\begin{aligned} & 10.534982 \\ & 25.614623 \\ & 69.296594 \\ & 2443391.037413678 \end{aligned}$ |  |

1. Starting conditions for first n-bady convergence run on any leg.
2. Departure conditions corresponding to converged n-body run an any leg.
3. E.R. $=[\text { (error in B.T (ROM) })^{2}+(\text { error in B.R (NOO) })^{2} / 100+$ error in time (days)/.5]

Table 3
CONVERGENCE HISTORY OF 1978 E TRAJECTORY

| Planet | Parameter | SPARC Conditions ${ }^{1}$ | Aiming Point from N -Body Convergence ${ }^{2}$ | $\begin{gathered} \text { N-Body } \\ \text { Converged Conditions } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| NEPTUNE | $\begin{aligned} & \mathrm{B} \cdot \mathrm{~T} \text { (KM) } \\ & \mathrm{B} \cdot \mathrm{R}(\mathrm{KM}) \\ & \text { TIME } \\ & \text { E.P. } \end{aligned}$ | $\begin{aligned} & 8.88 \times 10^{4} \\ & 0.0 \\ & 2447795.03485107 \end{aligned}$ |  | $\begin{aligned} & 8.8787349 \times 10^{4} \\ & -.53713876 \\ & 2447795.046940632 \\ & .03684153 \end{aligned}$ |
| URANUS | B•T (KM) <br> $B \cdot R$ (KM) <br> VHP (KPS) <br> (DEG) <br> - (DEG) <br> TIME <br> EP. | $\begin{aligned} & 1.624708 \times 10^{5} \\ & 4.6898 \times 10^{4} \\ & 15.0754 \\ & -1.6495 \\ & 272.3912 \\ & 2446535.58604431 \end{aligned}$ | $\begin{aligned} & 1.6 ? \quad 99 \times 10^{5} \\ & 4.7363698 \times 10^{4} \\ & 15.075400 \\ & -1.6495 \\ & 272.3912 \\ & 2446536.28276522 \end{aligned}$ | $\begin{aligned} & 1.6354962 \times 10^{5} \\ & 4.7173301 \times 10^{4} \\ & 15.052522 \\ & -1.6585941 \\ & 272.392575 \\ & 2446536.299654782 \\ & 0.37185594 \end{aligned}$ |
| SATURN | $\begin{aligned} & B \cdot T \text { (KM) } \\ & \text { B•R (KM) } \\ & \text { VHP (KPS) } \\ & 0 \text { (DEG) } \\ & \text { (DEG) } \\ & \text { TIME } \\ & \text { E.P. } \end{aligned}$ | $\begin{aligned} & 3.277183 \times 10^{5} \\ & -1.54493 \times 10^{4} \\ & 11.0191 \\ & 3.4277 \\ & 193.0302 \\ & 2445014.45593261 \end{aligned}$ | $\begin{aligned} & 3.2866481 \times 10^{5} \\ & -1.5571016 \times 10^{4} \\ & 11.0191 \\ & 3.4277 \\ & 193.0302 \\ & 2445018.1242855 \end{aligned}$ | $\begin{aligned} & 3.2933279 \times 10^{5} \\ & -1.5028893 \times 10^{4} \\ & 10.976001 \\ & 3.4624565 \\ & 193.14326 \\ & 2445018.126545787 \\ & 0.86480821 \end{aligned}$ |
| JUPITER | B.T (KM) <br> B.R (KM) <br> VHP (KPS) <br> 0 (DEG) <br> 8 (DEG) <br> TIIE <br> E.P. | $\begin{aligned} & 2.5733328 \times 10^{6} \\ & 3.072777 \times 10^{5} \\ & 10.4459 \\ & -1.0682 \\ & 131.3308 \\ & 2444370.0 \end{aligned}$ | $\begin{aligned} & 2.576358 \times 10^{6} \\ & 3.0856215 \times 10^{5} \\ & 10.4459 \\ & -1.0682 \\ & 131.3308 \\ & 2444379.1380357 \end{aligned}$ | $\begin{aligned} & 2.5767222 \times 10^{6} \\ & 3.0800495 \times 10^{5} \\ & 9.99934091 \\ & -1.1806979 \\ & 130.92092 \\ & 2444379.181606578 \end{aligned}$ |
| EARTH | VHL (KPS) <br> - (DEG) <br> 0 (DEG) <br> TINE | $\begin{aligned} & 10.1703 \\ & 31.4611 \\ & 102.5632 \\ & 2443788.0 \end{aligned}$ | $\begin{aligned} & 10.051029 \\ & 31.803824 \\ & 101.07521 \\ & 2443788.045681285 \end{aligned}$ |  |

1. Starting conditions for first n-body convergence run on any leg.
2. Departure conditions corresponding to converged n-body run on any leg.
3. E.P. $=[\text { (error in } B \cdot T(K M))^{2}+(\text { error in } B \cdot R(X R y))^{2} / 100+$ error in time (days)/.5]

## CONVERGENCE HISTORY OF 1978 I TRAJECTORY

| Planet | Parameter | SPARC Conditions ${ }^{1}$ | Aiming Point from $N$-Body Convergence ${ }^{2}$ | $\begin{gathered} \mathrm{N}-\mathrm{Body} \\ \text { Converged Conditions } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| neptune | B.T (KM) | 88,800.0 | - | 88,813.824 |
|  | B.R (KM) | 0.0 | - | 7.2100276 |
|  | TIME | 2446869.64882278 | - | 2446869.658390037 |
|  | E.P. ${ }^{3}$ |  |  | . 17504714 |
| URANUS | B.T (KM) | 62,403.537 | 62.399 .409 | 62,381.158 |
|  | B•R (KM) | 12,092.542 | 12,078.476 | 12,066.347 |
|  | VHP (KPS) | 21,2430 | 21.2430 | 21.225333 |
|  | 0 (DEG) | -1.3550 | -1.3550 | -1.3611881 |
|  | - (DEG) | 268.8005 | 268.8005 | 268.821909 |
|  | TIME | 2445902.36242700 | 2445902.30991744 | 2445902.36 390082 |
|  | E.P. |  |  | . 21916502 |
| SATURN | B.T (KM) | 149,578.26 | 149,880.85 | 149,842.04 |
|  | B•R (KM) | -6,561.51 | -6,598.2403 | -6,560.6399 |
|  | VHP (KPS) | 16.6754 | 16.6754 | 16.661244 |
|  | $\emptyset$ (DEG) | 3.1370 | 3.1370 | 3.1495592 |
|  | - (DEG) | 193.7356 | 193.7356 | 193.80042 |
|  | TIME | 2444729.30791854 | 2444730.7871652 | 2444730.80984527 |
|  | E.P. |  |  | . 58567327 |
| JUPITER | B.T (KM) | 1,212,719.8 | 1,213,580.0 | 1,213,546.3 |
|  | B-R (KM) | 112,404.55 | 112,727.92 | 112,732.28 |
|  | VHP (RPS) | 14.2022 | 14.2022 | 13.860628 |
|  | - (DEG) | -. 3391 | -. 3391 | -. 35889586 |
|  | 0 (DEG) | 132.5223 | 132.52230 | 132.45347 |
|  | TIIE | 2444265.50000000 | 2444270.2575305 | 2444270.29616476 |
|  | E P. |  |  |  |
| EARTH | VHL (KPS) | 11.237559 | 11.243561 | - |
|  | - (DEG) | 28.186442 | 28.155887 | - |
|  | 0 (DEC) | 108.03907 | 107.30312 | - |
|  | TIMS | 2443790.50000000 | 2443790.991008502 | - |

1. Starting conditions for first n-body convergence zun on any leg.
2. Departure conditions corresponding to converged n-body run on any leg.
3. B.R. $=\left[(\text { error in B.T (KM) })^{2}+\cdots(\text { error in B.R (KM) })^{2} / 100++\right.$ error in time (days)/.5]
at all the planets and 2) the initial (aiming point from n -body convergence) and final ( n -body converged conditions) conditions from each leg of the converged n-body trajectories. On any one leg there is good agreement between the conic and integrated trajectories with the exception of the time of flight.
Table 5 gives the complete convergence history of the Jupiter-Saturn leg of the trajectory for the 1977 exterior ring passage. The initial and final conditions, as well as the corrections to the initial conditions, are given for each successive integration of the trajectory. In this case only one sensitivity matrix was used to obtain convergence: A1so, for most of the other legs, fewer corrections were needed to obtain convergence.
Tables 6 and 7 give the sensitivity matrices generated during convergence for all legs of the trajectories corresponding to the 1977 exterior ring passage, and the 1977 interior ring passage. A comparison of the sensitivity matrices in Tables 6 and 7. shows that the sensitivities are greater for the interior ring passage (Table 7) than the exterior ring passage (Table 6). For the trajectory corresponding to the 1977 interior ring passage it was necessary to generate two sensitivity matrices for the Earth-Jupiter and Jupiter-Saturn legs in order to obtain convergence. The sensitivity matrices were retained upon convergence for the midcourse guidance analysis.
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Table 5

|  | Parameter | SPARC Initial Conditions | First Run | Corrections | Second Run | Corrections | $\begin{aligned} & \text { Tr.ird } \\ & \text { Kun } \end{aligned}$ | Corrections |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 鬼 | B.T (KM) <br> B-R (ROM) <br> VHP (KPS) <br> - (DEG) <br> © (DEG) <br> TIIR | $\begin{gathered} 1,924,606.6 \\ 151,066.10 \\ 7.8118 \\ -3.0377 \\ 94.3799 \\ 2444070 . \\ 00000000 \end{gathered}$ | $\begin{gathered} 1,924,606.6 \\ 151,066.10 \\ 7.8118 \\ -3.0377 \\ 94.3799 \\ 2444070 . \\ 00000000 \end{gathered}$ | $\begin{aligned} & 16,497.6 \\ & 1226.26 \end{aligned}$ $21.561264$ | $\begin{aligned} & 1,941,104.2 \\ & 152,292.36 \\ & 7.8118 \\ & -3.0377 \\ & 94.3799 \\ & 2444091 . \\ & 561264 \end{aligned}$ | $\begin{aligned} & -2886.6 \\ & 648.63 \\ & -1.2584095 \end{aligned}$ | $\begin{aligned} & 1,938,217.6 \\ & 152,940.98 \\ & 7.8 i 18 \\ & -3.0377 \\ & 94.3799 \\ & 2444090 . \\ & 302854 \end{aligned}$ | $\begin{array}{r} 777.6 \\ -22.72 \end{array}$ $.29456893$ |
|  |  | N-Body Aiming Point |  |  |  |  |  |  |
| 彮 |  | $358,415.35$ $-17,359.508$ 10.6937 2.7472 195.3260 2444846. 61852323 | $\begin{aligned} & \text { 4,998,310.8 } \\ & -173,760.34 \\ & 10.822137 \\ & 2.7430736 \\ & 195.04878 \\ & 2444826 . \\ & 85295868 \\ & 4,642,530.6 \\ & 19.832273 \\ & 4682.1951 \end{aligned}$ |  | $\begin{aligned} & 496,732.79 \\ & 216.031 .72 \\ & 10.661842 \\ & 2.7654006 \\ & 194.48274 \\ & 2444847 . \\ & 77484107 \\ & 271,299.06 \\ & -1.0896087 \\ & 273.47827 \end{aligned}$ |  | $\begin{aligned} & 291,326.92 \\ & -39,355.652 \\ & 10.671063 \\ & 2.7808117 \\ & 195.49266 \\ & 2444846 . \\ & 435048818 \\ & 70,602.32 \\ & .250183 \\ & 71.102682 \end{aligned}$ |  |

1) BIMISS = (error in B.T (KOM) $)^{2}+$ error in B.R (RM) $)^{2}$
2) EP. $=\left[(\text { error in } B \cdot T(K M))^{2}+(\text { error in } B \cdot R(K M))^{2} / 1000+\right.$ error in time (days)/.5]

CONVERGENCE HISTORY OF JUPITER-SATURN LEG FOR 1977 E TRAJECTORY

| Parameter | Fourth Run | Corrections | $\begin{aligned} & \text { Fifth } \\ & \text { Run } \end{aligned}$ | Corrections | $\begin{gathered} \text { Sixth } \\ \text { Run } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| B.T (KM) <br> B.R (KIM) <br> VHP (KPS) <br> 0 (DEG) <br> - (DEG) <br> TIME | $\begin{aligned} & 1,938,995.2 \\ & 152,918.26 \\ & 7.8118 \\ & -3.0377 \\ & 94.3799 \\ & 597423 \end{aligned}$ | $\begin{array}{r} -187.4 \\ 20.5 \end{array}$ <br> -. 0808015 | $\begin{aligned} & 1,938,807.8 \\ & 152,938.74 \\ & 7.8118 \\ & -3.0377 \\ & 94.3799 \\ & 2444090 . \\ & 5116621 \end{aligned}$ | $\begin{aligned} & -16.1 \\ & -9.03 \\ & -.01964204 \end{aligned}$ | $\begin{aligned} & 1,938,791.6 \\ & 152,929.7 \\ & 7.8118 \\ & -3.0377 \\ & 94.3799 \\ & 2444090 . \\ & 496979 \end{aligned}$ |
|  | N-Body Aiming Point |  |  |  |  |
| B.T (KM) <br> B.R (KM) <br> VIP (KPS) <br> 0 (DEG) <br> 0 (DEG) <br> TIME <br> BIMISS (KM). <br> ETxit (Days) <br> E.P. | $\begin{gathered} 369,447.43 \\ -79,728.391 \\ 10.668896 \\ 2.7792466 \\ 195.48814 \\ 2444846 . \\ 7549548 \\ 14,485.038 \\ -.069722 \\ 14.624483 \end{gathered}$ |  | $\begin{gathered} 355,063.52 \\ -19,304.993 \\ 10.669496 \\ 2.7798719 \\ 195.48886 \\ 2444846 . \\ 70319819 \\ 3875.5 \\ -.017965 \\ 3.911453 \end{gathered}$ |  | $\begin{gathered} 358,738.12 \\ -17,746.25 \\ 10.669641 \\ 2.7797137 \\ 195.4885 \\ 2444846 . \\ 68426561 \\ 503.739 \\ -.0009667 \\ .50567 \end{gathered}$ |

Table 6

SENSITIVITY MATRICES
1977 E TRAJECTORY

|  |  | $B \cdot \mathrm{~T}_{\mathrm{F}}{ }^{*}$ | $B \cdot R_{F}$ | Time $_{F}$ |
| :---: | :---: | :---: | :---: | :---: |
| EARTHJUPITER | VHL <br> © | $\begin{gathered} 1.4524449 \times 10^{10} \\ -1.3078390 \times 10^{9} \\ -4.6717345 \times 10^{9} \\ B \cdot T_{F} \end{gathered}$ | $\begin{gathered} -1.7320846 \times 10^{10} \\ -8.0286081 \times 10^{8} \\ 5.7470956 \times 10^{8} \\ \text { B.R } \end{gathered}$ | $\begin{array}{r} -257.02057 \\ 6.8216719 \\ 6.3153312 \\ \text { Time }_{F} \end{array}$ |
| JUPITERSATURN | $\left\lvert\, \begin{aligned} & \mathrm{B} \cdot \mathrm{~T}_{\mathrm{I}}{ }^{*} \\ & \mathrm{~B} \cdot \mathrm{R}_{\mathrm{I}} \\ & \mathrm{Time}_{\mathrm{I}} \end{aligned}\right.$ | $\begin{array}{r} 241.85600 \\ 77.952000 \\ -404685180 \\ B \cdot T_{F} \end{array}$ | $\begin{array}{r} 16.936000 \\ -266.15400 \\ 9432296.0 \\ B \cdot R_{F} \end{array}$ | $\begin{aligned} & -.38146972 \times 10^{-7} \\ & -.76293944 \times 10^{-8} \\ & .94943237 \\ & \\ & \text { Time }_{F} \end{aligned}$ |
| SATURNURANUS | $\left\lvert\, \begin{aligned} & \mathrm{B} \cdot \mathrm{~T}_{\mathrm{I}} \\ & \mathrm{~B} \cdot \mathrm{R}_{\mathrm{I}} \\ & \mathrm{Time}_{\mathrm{I}} \end{aligned}\right.$ | $\begin{array}{r} 3963.5840 \\ -736.0000 \\ -85910912 \\ \text { B.T } T_{F} \end{array}$ | $\begin{array}{r} -435.8500 \\ -3854.8930 \\ -167873.00 \\ B \cdot R_{F} \end{array}$ | $\begin{gathered} -.85449219 \times 10^{-6} \\ .10681152 \times 10^{-6} \\ .66708374 \end{gathered}$ $\mathrm{Time}_{\mathbf{F}}$ |
| URANUS NEPTUNE | $\left\lvert\, \begin{aligned} & B \cdot T_{I} \\ & B \cdot R_{I} \\ & \text { Time }_{I} \end{aligned}\right.$ | $\begin{array}{r} 2814.7200 \\ 1629.7280 \\ -916262.40 \end{array}$ | $\begin{array}{r} 1540.5820 \\ -2798.2185 \\ 1309212.0 \end{array}$ | $\begin{aligned} & .76293944 \times 10^{-7} \\ & .30517578 \times 10^{-7} \\ & .91964722 \end{aligned}$ |

*The subscripts $F$ and I refer to the target variables at the
arrival (final) and departure (initial) planets respectively.

Table: 7

SENSITIVITY MATRICES
1977 I TRAJECTORY

| B. $\mathrm{T}_{\mathrm{F}}$ |  |  | $B \cdot \mathrm{R}_{\mathrm{F}}$ | Time $_{F}$ |
| :---: | :---: | :---: | :---: | :---: |
| EARTH- <br> JUPITER <br> MATRIX 非1 | $\begin{gathered} \text { VHL } \\ \vdots \\ \text { © } \end{gathered}$ | $\begin{gathered} .39089154 \times 10^{11} \\ -.11769157 \times 10^{10} \\ -.61185418 \times 10^{10} \\ B \cdot T_{F} \end{gathered}$ | $\begin{gathered} -.44512973 \times 10^{10} \\ -.21622508 \times 10^{10} \\ .41952192 \times 10^{9} \\ \mathrm{~B} \cdot \mathrm{R}_{\mathrm{F}} \end{gathered}$ | $\begin{array}{r} -101.97067 \\ 1.5725325 \\ 4.1982886 \\ \\ \text { Time }_{F} \end{array}$ |
| EARTH- <br> JUPITE? <br> MATRIX \#2 | $\begin{gathered} \text { VHL } \\ \$ \\ \$ \end{gathered}$ | $\begin{gathered} .39388928 \times 10^{11} \\ -.12265990 \times 10^{10} \\ -.59155179 \times 10^{10} \\ B \cdot T_{F} \end{gathered}$ | $\begin{gathered} -.49738721 \times 10^{10} \\ -.20714486 \times 10^{10} \\ .4283892 \times 10^{9} \end{gathered}$ $B \cdot R_{F}$ | $\begin{gathered} -98.93036 \\ 1.1833571 \\ 2.1417473 \\ \\ \text { Time }_{F} \end{gathered}$ |
| JUPITERSATURN | $\begin{aligned} & B \cdot T_{I} \\ & B \cdot R_{I} \\ & \text { Time }_{I} \end{aligned}$ | $\begin{gathered} 834.91199 \\ 113.28000 \\ -.20933776 \times 10^{9} \\ B \cdot T_{F} \end{gathered}$ | $\begin{gathered} 77.974000 \\ -745.13599 \\ .17943218 \times 10^{8} \\ \\ B \cdot R_{F} \end{gathered}$ | $\begin{gathered} -.38146972 \times 10^{-7} \\ -.22888184 \times 10^{-7} \\ .74314630 \\ \\ \text { Time }_{F} \end{gathered}$ |
| SATURN- <br> URANUS <br> MATRIX \#1 | $\begin{aligned} & \mathbf{B} \cdot \mathbf{T}_{\mathbf{I}} \\ & \mathrm{B} \cdot \mathrm{R}_{\mathbf{I}} \\ & \text { Time }_{\mathbf{I}} \end{aligned}$ | $\begin{aligned} & 12732.416 \\ & -676.16000 \\ & .99752256 \times 10^{8} \end{aligned}$ | $\begin{aligned} & -1328.3794 \\ & -11670.457 \\ & .13437109 y ? 0^{8} \end{aligned}$ | $\begin{aligned} & -.19531250 \times 10^{-5} \\ & -.12207031 \times 10^{-6} \\ & .70349120 \end{aligned}$ |

Table 7 (Cont.)
SENSITIVITY MATRICES
1977 I TRA.JECTORY

| SATURNURANUS MATRIX \#2 | $\begin{aligned} & \mathrm{B} \cdot \mathbf{T}_{\mathbf{I}} \\ & \mathbf{B} \cdot \mathbf{R}_{\mathbf{I}} \\ & \mathrm{Time}_{\mathbf{I}} \end{aligned}$ | $\begin{aligned} & 12400.823 \\ & -1027.5015 \\ & .97545045 \times 10^{8} \end{aligned}$ | $\begin{aligned} & -1009.7776 \\ & -11470.189 \\ & -.13392877 \times 10^{8} \end{aligned}$ | $\begin{aligned} & .97961425 \times 10^{-5} \\ & .10467529 \times 10^{-4} \\ & .73211670 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| URANUSNEPTUNE | $\begin{aligned} & \mathbf{B} \cdot \mathbf{I}_{\mathbf{I}} \\ & \mathbf{B} \cdot \mathbf{R}_{\mathbf{I}} \\ & \mathbf{T i m e}_{\mathbf{I}} \end{aligned}$ | $\begin{aligned} & 13253.760 \\ & 10267.904 \\ & -.35868352 \times 10^{8} \end{aligned}$ | $\begin{aligned} & 4330.6870 \\ & -12880.946 \\ & .59646740 \times 10^{7} \end{aligned}$ | $\begin{aligned} & .53405762 \times 10^{-7} \\ & -.44403076 \times 10^{-5} \\ & .90330505 \end{aligned}$ |


[^0]:    * bpp = bits per planet

[^1]:    ${ }^{\text {* }}$ Sphere of influence is defined as that distance from the planet where the perturbative forces due to the Sun and the planet are equal:
    $R_{\text {sphere }}=\left(\frac{\text { mass of planet }}{\text { mass of } \frac{\text { Sun }}{}}\right)^{2 / 5} \times\binom{$ mean distance of }{ planet from Sun }
    1.
    !

[^2]:    *Ideal velocity (in $\mathrm{ft} / \mathrm{sec}$ ) is that velocity required by a launch vehicle to achieve a given hyperbolic excess velocity (VHL) beyond Earth escape from a 100 n . mile parking orbit, assuming gravitational and frictional losses of $4000 \mathrm{ft} / \mathrm{sec}$.

    $$
    \begin{aligned}
    \mathrm{V}_{\mathrm{I}} & =\left[(\mathrm{VHL})^{2}+(36,178)^{2}\right]^{1 / 2}+4000 \mathrm{ft} / \mathrm{sec} \\
    & =3280.8\left[\mathrm{C}_{3}+121.5964\right]^{1 / 2}+4000 \mathrm{ft} / \mathrm{sec}
    \end{aligned}
    $$

[^3]:    Type I trajectories have a heliocentric transfer angle less than $180^{\circ}$, whereas Type II trajectories traverse more than $180^{\circ}$. For either Type I or Type II, Class I trajectories have a smaller heliocentric transfer angle than Class II trajectories.

[^4]:    Figure 4.11
    SCIENCE EVALUATION FOR CATEGORY OF PLANETARY ACTIVE PROCESSES

[^5]:    *bpp = BITS PER PLANET

