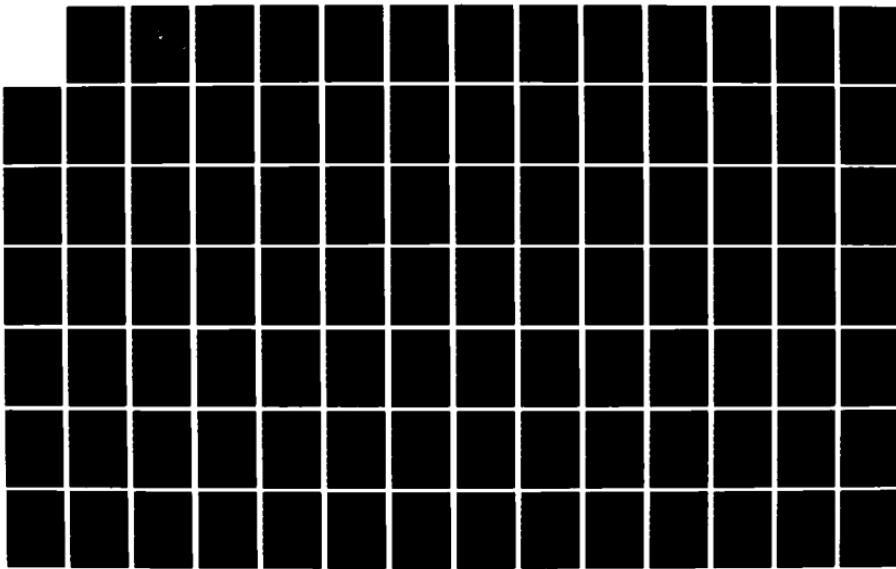


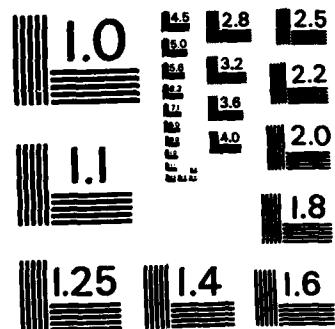
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# NAVAL POSTGRADUATE SCHOOL

## Monterey, California



# THESIS

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THE EFFECTIVENESS OF HEAT EXCHANGERS  
WITH ONE SHELL PASS AND  
THREE TUBE PASSES

by

Mark S. O'Hare

June 1985

Thesis Advisor:

Allan D. Kraus

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The Effectiveness of Heat Exchangers  
With One Shell Pass and  
Three Tube Passes.

by

Mark S. O'Hare  
Lieutenant Commander, United States Navy  
B.S., United States Naval Academy, 1976

Submitted in partial fulfillment of the  
requirements for the degree of



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from the

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June 1985

Author:

Mark S. O'Hare

Mark S. O'Hare

Approved by:

Allen D. Kraus

Allen D. Kraus, Thesis Advisor

Paul J. Marto

Paul J. Marto, Chairman,  
Department of Mechanical Engineering

John N. Dyer

John N. Dyer, Dean of Science and Engineering

## ABSTRACT

Heat exchangers with one shell pass and n tube passes are often referred to as 1-n exchangers. The heat transfer literature contains many references to studies of 1-n exchangers when n is even but apparently little work has been done with respect to the 1-n exchanger when n is odd. This thesis greatly expands the theoretical study of 1-n exchangers with n being odd. While a completely closed form solution was found to be unfeasible, a polynomial approximation has been developed that yields the effectiveness ( $\epsilon$ ) of the two possible arrangements of the 1-3 exchanger as a function of the capacity rate ratio (R) and the number of transfer units (Ntu). It is also shown that the effectiveness of the arrangement with two counterflow and one parallel flow tube side passes exceeds that of some of the 1-n exchangers with n even.

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## NOMENCLATURE

### English Letter Symbols

- A = Exchanger heat-transfer surface, sq m
- $A_m$  = Coefficient of the  $m$ th value dimensionless
- $A_0$  = Coefficient, dimensionless
- $A_1$  = 1st order coefficient to be multiplied by  $Ntu$ , dimensionless
- $A_2$  = 2nd order coefficient to be multiplied by  $Ntu^2$ , dimensionless
- $A_3$  = 3rd order coefficient to be multiplied by  $Ntu^3$ , dimensionless
- $A_4$  = 4th order coefficient to be multiplied by  $Ntu^4$ , dimensionless
- $A_5$  = 5th order coefficient to be multiplied by  $Ntu^5$ , dimensionless
- a = Exchanger heat-transfer surface, sq m/m
- C = Capacity rate, W/K. Also designates dimensionless arbitrary constant
- $c_{pc}$  = Specific heat at constant pressure of cold fluid, J/kg°K
- $c_{ph}$  = Specific heat at constant pressure of hot fluid, J/kg°K
- D = Empirical value of effectiveness (computer generated), dimensionless
- e = Error. Also used as the exponential function
- F = Logarithmic mean temperature difference correction factor, dimensionless
- L = Exchanger length, m
- N = Number of effectiveness empirical data points used to determine a curve for R, dimensionless

$n$  = Number of tube passes, dimensionless. Also number of equations, dimensionless

$n_c$  = A related  $N_{tu}$  per unit length hot side,  $m^{-1}$

$n_h$  = A related  $N_{tu}$  per unit length cold side,  $m^{-1}$

$N_{tu}$  = Number of transfer units, dimensionless

$P$  = Temperature group, dimensionless

$q$  = Total rate of heat transfer, W

$q_{max}$  = Maximum total rate of heat transfer, W

$R$  = Capacity rate ratio, dimensionless

$S$  = Temperature group, dimensionless

$S_r$  = Sum of the squares of the residuals, dimensionless

$T$  = Hot fluid temperature, °C

$T_{pi}$  = Particular integral, dimensionless

$T_1$  = Hot fluid temperature in, °C

$T_2$  = Hot fluid temperature out, °C

$t_1$  = Cold fluid temperature in, °C

$t_2$  = Cold fluid temperature out, °C

$t_a$  = Cold fluid temperature 1st pass, °C

$t_{ab}$  = Cold fluid temperature between 1st and 2nd passes

$t_b$  = Cold fluid temperature 2nd pass, °C

$t_{bc}$  = Cold fluid temperature between 2nd and 3rd passes

$t_c$  = Cold fluid temperature 3rd pass, °C

$U$  = Overall heat transfer coefficient,  $W/m^2 - ^\circ C$

$w$  = Mass flow, kg/sec. Also the product of  $w$  and  $L$ , dimensionless

$x$  = length coordinate, m. Also used to represent a constant value in a sequence

$y$  = Sum of  $m$ th degree polynomial, defined by eq. (53),  
dimensionless

$Z$  = A product of  $z$  and  $L$ , dimensionless

$z$  = A related  $N_{tu}$  per unit length, hot side,  $1/m$

#### Greek Letter Symbols

$\alpha$  = Root of auxiliary differential equation,  $1/m$

$\epsilon$  = Exchanger effectiveness, dimensionless

$\lambda$  = Combination of variables defined by equation (11),  
dimensionless

$\omega$  = A related  $N_{tu}$  per unit length, hot side,  $1/m$

$\phi$  = A combination of terms defined by eq. (38),  
dimensionless

$\Sigma$  = Summation, dimensionless

$\sigma^2$  = Variance, dimensionless

$\theta_m$  = Mean temperature difference for exchanger,  $^{\circ}C$

$\partial$  = Indicates partial derivative, dimensionless

#### Subscripts

$c$  = Cold fluid

$h$  = Hot fluid

$i, j, k$  = Values in a sequence

$m$  = Degree or order, an exponent

$1$  = inlet

$2$  = outlet

#### Special Symbols

$[A]$  = An  $m \times n$  matrix, symmetric

[K] = An m x n matrix, symmetric

[L] = A lower triangular matrix

[T] = An m x 1 vector

[0] = A null vector

#### ACKNOWLEDGEMENT

I wish to thank my wife Jayne for her support and never ending faith in me always, especially while here at NPS. Also deep appreciation of thanks to Professor Allan D. Kraus for his guidance, brilliance and friendship in completing this work. A special thanks to those in my Navy career who have encouraged me and given me the chance to prove myself. In closing, I note that I am grateful that the apple did not fall far from the tree.

## I. INTRODUCTION

### A. BACKGROUND

When analyzing the standard counterflow heat exchanger, it becomes apparent that, from a practical standpoint, it is often difficult to obtain a high velocity for one of the fluids when this fluid is constrained to flow through all of the tubes in a single pass. This leads to a possibility of a low overall heat transfer coefficient which cancels the advantage of the high logarithmic mean temperature difference which is obtainable in true counterflow.

The quest for flow arrangements for increased heat recovery has led to arrangements that yield increased tube-side velocities and higher overall heat transfer coefficients even at the expense of a departure from the ideal true counterflow arrangement. Thus, the design may be modified so that the tube side fluid is carried through fractions of the tubes consecutively.

Heat exchangers of this type with one shell pass and n tube passes are often referred to as 1-n exchangers. These exchangers, such as the one shell pass, two-tube pass (1-2) parallel-counterflow exchanger (see Figure 1.1), are configured such that all of the tube side fluid flows through the two halves of the the tubes successively. A single channel is employed with a partition to permit the

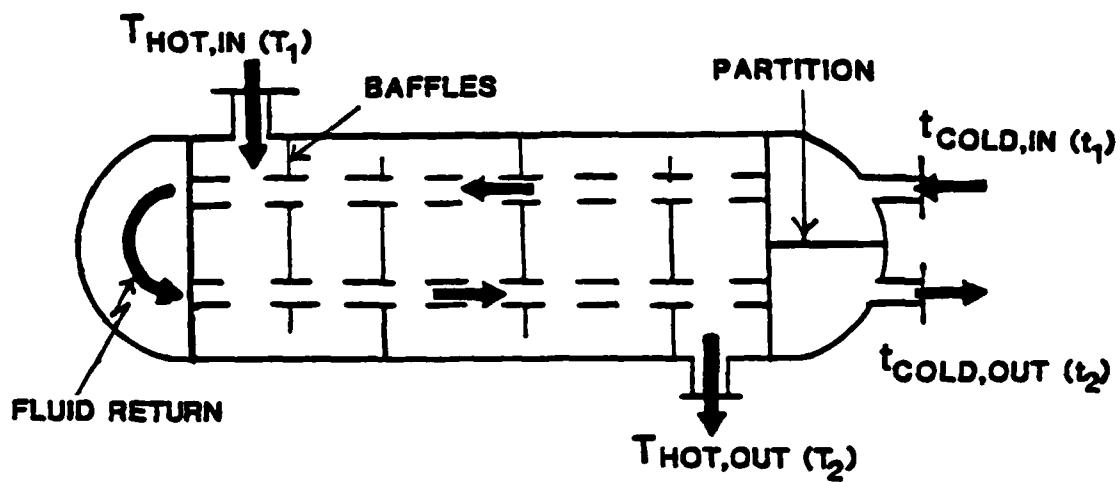


Figure 1.1 1-2 Parallel-Counterflow Exchanger

entry and exit of the tube side fluid from the same channel. Note the baffles used to induce turbulence causing the liquid to flow through the shell at right angles to the axes of the tubes thus helping to create a higher shell side velocity with higher shell side heat-transfer coefficients.

To date, much work has been done on finding the true logarithmic mean temperature difference for heat exchangers with an even number of tube passes. Little work, however, has been done with regard to heat exchangers having an odd number of passes. This is primarily due to the method employed in deriving an analytical solution to measure the overall effectiveness of a heat exchanger.

Exchangers with an even number of tube passes often present a configuration problem especially in a marine application where the inlet and outlet of the cooling fluid must

be one the same side of the exchanger header (see Figure 1.1). This particular problem could be alleviated by going to heat exchangers with an odd number of tube passes. Currently, precise mathematical expressions for the effectiveness of the 1-3 exchangers do not exist. Hence, a theoretical examination is reported on here which considers the effectiveness of the 1-3 parallel-counter flow exchanger which is shown in Figure 1.2.

Before doing this it is important to mention the work that lead to the effectiveness method and the development of work on heat exchangers with an odd number of tube passes.

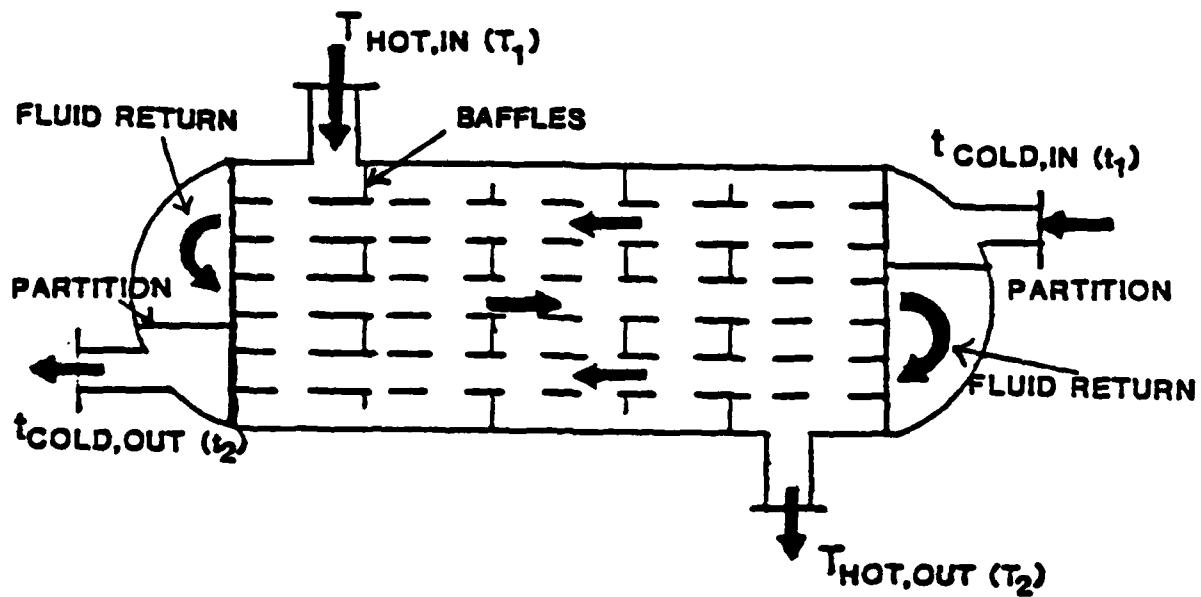


Figure 1.2 1-3 One Shell Pass Three Tube Pass Exchanger

This will be considered in Section II. Kern [Ref. 1: pp. 224-226], makes the interesting point that the optimum exchanger requires an exchanger capable of providing the optimum fluid-flow velocities on the shell as well as the tube sides. This might frequently entail the use of an odd number of tube passes or an odd tube length.

#### B. WHY EFFECTIVENESS AS A FUNCTION OF $N_{tu}$

It is also noted that Kays and London [Ref. 2: pp. 24-29] indicated that the effectiveness as a function of  $N_{tu}$  ( $\epsilon - N_{tu}$ ) method is the favored approach for evaluating a heat exchanger's performance because:

1. The effectiveness value stands alone as a dependent variable and should not appear directly in the abscissa and indirectly in the ordinate of a graphical display.
2. The log-mean difference equation misleadingly simplifies the notion of what is involved in heat exchanger design theory, since the implication is that only a rate equation is required.
3. The  $\epsilon - N_{tu}$  approach simplifies the algebra involved in predicting the performance of complex flow arrangements.
4. The more meaningful arguments are related to ease of use in design work. Two prime examples of these are:
  - a) Given the overall heat transfer coefficient,  $U$ , the two fluid capacity rates,  $C_c$  and  $C_h$ , and the terminal temperatures, determine the required surface area,  $A$ .
  - b) Given  $A$ ,  $U$ ,  $C_c$ ,  $C_h$  and the inlet temperatures of both streams, determine the outlet temperatures.

## II. THE DEVELOPMENT OF THE EFFECTIVENESS METHOD

### A. LITERATURE SURVEY

It was Nagle [Ref. 3: pp. 604-609], in 1931, who credited Davis [Ref. 4] with a simplified method for computing actual temperature differences between two heat-interchanging streams which depart from true counter or concurrent (parallel) flow. This is now the familiar "F factor" method which expresses the actual mean temperature difference  $\theta_m$  in  $q = UA\theta_m$  as a fraction F of the counterflow logarithmic mean temperature difference, LTMD,  $\theta_{mc}$  via  $\theta_m = F\theta_{mc}$ .

The example of initial interest was the 1-2 exchanger with a single shell pass and two continuous tube passes in counter and concurrent flow with it. The method involved derivation of the actual temperature difference for the flow pattern and formed the ratio  $F = \theta_m / \theta_{mc}$ . This familiar LMTD correction factor was plotted conveniently as functions of the effectiveness,  $\epsilon$ , and the capacity rate ratio R with R as a parameter. These mean temperature difference correction charts are available for many flow arrangements [Ref. 1: pp. 829-833 and Ref. 5]. The effectiveness,  $\epsilon$  (often called P or S), is always the cold fluid effectiveness and R is always the capacity rate ratio of cold fluid to hot fluid.

Nagle detailed assumptions and derivations for the 1-2, 1-4 and 1-6 exchangers. The F factors were obtained by Nagle through graphical integration and were accompanied by the comment that F factors for the 1-2 exchanger could be applied with negligible error to 1-4 and 1-6 exchangers. Underwood [Ref. 6: pp. 145-148] rederived the equations of Nagle for 1-2 and 1-4 exchangers to eliminate the need for obtaining F factors by graphical integration.

Bowman [Ref. 7: pp. 541-544 ] pointed out that for a very large or infinite number of tube passes, the F factor approached, as a limit, its value in crossflow with both fluids completely mixed. It was further stated that even at the limit, the F factors were only 1 to 2 percent lower than those for the 1-2 exchanger. A previous paper by Kraus and Kern [Ref. 8] did not confirm the generalization that 1-n exchangers differed only negligibly from the 1-2 exchanger although this lack of confirmation was obtained on an  $\epsilon = f(R, N_{tu})$  basis. Moreover, the Kraus-Kern work does not confirm the generalizations on an  $F = f(R, N_{tu}, \epsilon)$  basis.

From the standpoint of usefulness and good accuracy, it is essential that F factors, if they are to be used in preference to  $\epsilon = f(R, N_{tu}, \text{flow arrangement})$ , be obtained with precision. Plots of  $F = f(R, \epsilon, = P \text{ or } S)$  [Ref. 1: pp. 829-833 and Ref. 5] show that the curves for particular values of R approach infinite slope as F decreases. While this can be partially alleviated by restricting  $R < 1.0$  (a

constraint used in the  $\epsilon = f(R, N_{tu}, \text{flow arrangement})$  approach), it is seen that small errors in the interpolation for R or  $\epsilon = P$  or S can result in large fluctuations in the value of F.

In a comprehensive paper, Bowman, Mueller and Nagle [Ref. 9: pp. 283-294] presented graphs of F factors for shells with one through six shell passes and numbers of continuous tube passes respectively double the number of shell passes. In view of the earlier references to Nagle and Bowman, it should be noted that F factors were computed for the 1-2 exchanger in [Ref. 9: pp. 283-294] using the equations of Underwood [Ref. 6: pp. 145-158].

Ten Broeck [Ref. 10: pp. 1041-1042] prepared a graph of the dimensionless groups now known as  $\epsilon$ , R and N<sub>tu</sub> for the 1-2 exchanger. Such a graph had the added versatility of simplifying the calculation of performance in a given exchanger when operating at conditions different for those for which it was designed. Kays and London [Ref. 2: pp. 63-74] prepared similar graphs and tables of  $\epsilon = f(R, N_{tu}, \text{flow arrangement})$  for the 1-2 exchanger and for several cases of crossflow and periodic flow.

The foregoing describes the early history of the search for the so-called Logarithmic Mean Temperature Difference Correction Factor, F, with regard to heat exchangers having an even number of tube passes. It is a fact, however, that certain space economies could be realized from exchangers

having an odd number of tube passes so that the tube side fluid could enter and leave the exchanger at opposite ends of the exchanger (see Figure 1.2).

#### B. FISCHER'S WORK

With the foregoing in mind, an extensive search has been conducted to obtain  $\epsilon - N_{tu}$  data for the so called "1-3" and "1-5" exchangers. This search has uncovered a single work, that of Fischer [Ref. 11: pp. 377-383], which summarizes the historical development covered here and contains only a small section on the 1-3 exchanger. This work by Fischer develops an equation for true mean temperature difference of the 1-3 exchanger and casts the results in terms of  $F$  rather than  $\epsilon$ . Moreover, the work treats only the case where the three tube passes are arranged with two in counterflow and one in parallel flow (1-3:2C) making no mention of the one counterflow and two parallel flow (1-3:2P) case (see Figures 2.1 and 2.2). In addition, the equation developed to yield  $F$  must be solved using a trial and error solution.

The present work is aimed at continuing the Fischer investigation for several reasons:

1. A solution is needed for effectiveness,  $\epsilon$ , as a function of capacity rate ( $R$ ) and number of transfer units ( $N_{tu}$ ).
2. This solution should be in a closed form if at all possible so that it will be computationally efficient and useful in both the design and analysis frameworks.

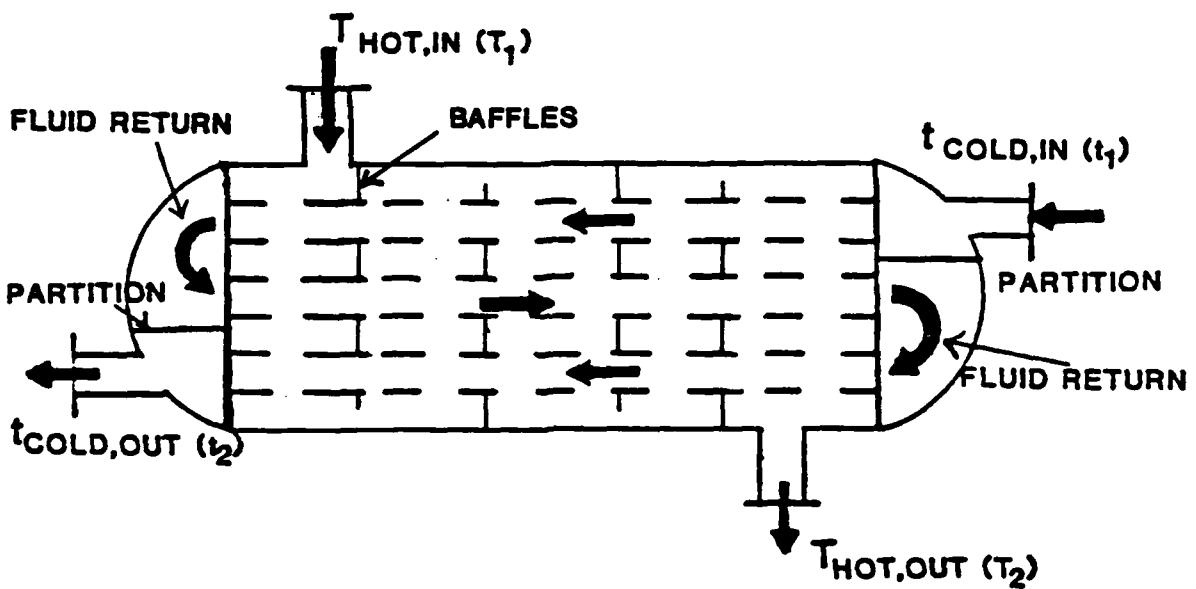


Figure 2.1 1-3:2C Three Tube Passes - Two in Counterflow

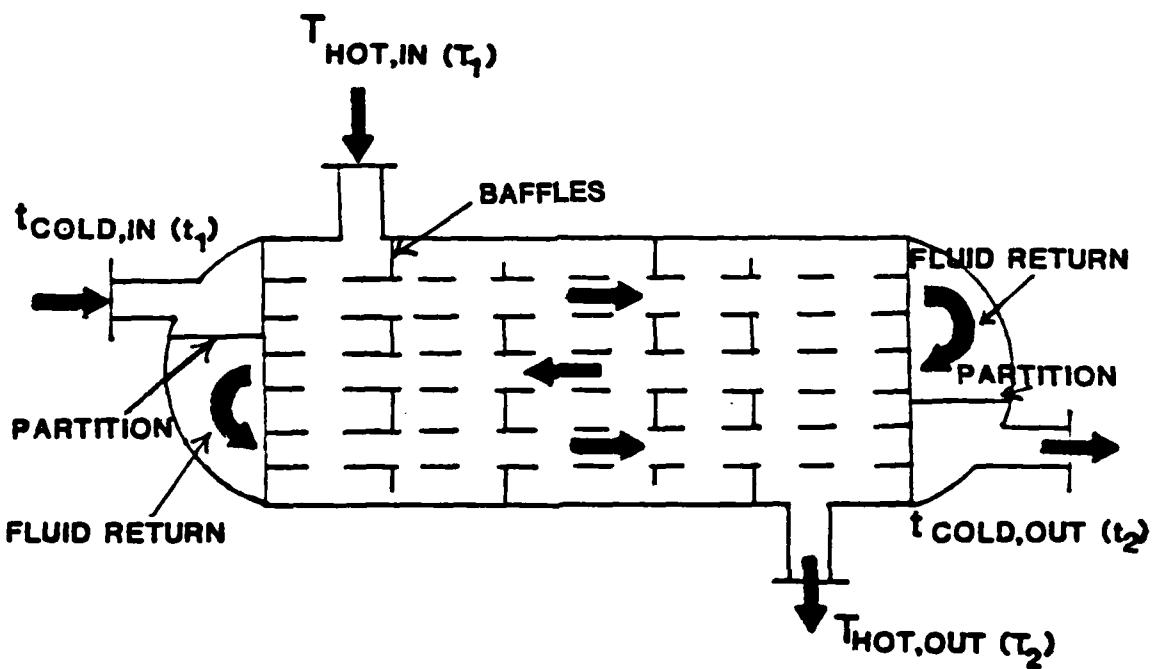


Figure 2.2 1-3:2P Three Tube Passes - Two in Parallel Flow

3. Because valid design data can evolve from a polynomial approximation. The search should not be abandoned just because a closed form solution does not result from an analytical approach.
4. Data is needed for the (1-3:2P) two parallel-one counterflow configuration.
5. A 1-3 exchanger in a marine (shipboard) application may result in a considerable space saving over its 1-n counterpart with n even. This would be evident on the outside of the exchanger where it would be immediately noted that the 1-3 exchanger has tube side inlet and outlet at opposite ends of the exchanger.

The next section confirms Fischer's result and shows that a closed form solution cannot be obtained for the effectiveness of the 1-3 exchanger. Sections IV and V demonstrate how, through numerical analysis assisted by a computer, a polynomial solution can be derived that will yield the effectiveness to engineering accuracy.

### III. AN ATTEMPT AT A CLOSED FORM SOLUTION

#### A. EFFECTIVENESS AS A FUNCTION OF CAPACITY RATES AND EXCHANGER SIZE

This section deals with an investigation into the effectiveness,  $\epsilon$ , of a one shell pass and three tube pass heat exchanger, whereby  $\epsilon$  compares the actual heat transfer rate to the thermodynamically limited, maximum possible heat transfer rate as would be realized only in a counter flow heat exchanger of infinite transfer area. This exchanger heat transfer effectiveness is given by

$$\epsilon = \frac{q}{q_{\max}} = \frac{C_h(T_{hot,in} - T_{hot,out})}{C_{\min}(T_{hot,in} - t_{cold,in})} = \frac{C_c(t_{cold,out} - t_{cold,in})}{C_{\min}(T_{hot,in} - t_{cold,in})}$$

where  $C_{\min}$  is the smaller of the  $C_h$  and  $C_c$  magnitudes. Thus,  $\epsilon$  possesses the significance of effectiveness of the heat exchanger from a thermodynamic point of view, with the magnitude of the effectiveness completely defining the heat transfer performance. In general we express  $\epsilon = f(N_{tu}, R,$  and flow arrangement) and when the flow arrangement is understood, it is said that  $\epsilon = f(N_{tu}, R)$ . [Ref. 2: pp. 14-26].

The number of heat transfer units  $N_{tu}$  is a nondimensional expression of the "heat transfer size" of the exchanger. When  $N_{tu}$  is small the exchanger effectiveness is low, and when  $N_{tu}$  is large,  $\epsilon$  approaches the limit imposed by the flow

arrangement and thermodynamic conditions asymptotically.

From inspection of the definition of  $N_{tu}$

$$N_{tu} = \frac{AU}{C_{\min}} = \frac{1}{C_{\min}} \int_0^A UdA$$

it is clear that the overall conductance and transfer area affect the costs of attaining a high value for  $N_{tu}$ , ergo high  $\epsilon$ . The capacity rate ratio,  $R$ , as defined by

$$R = \frac{C_{\min}}{C_{\max}}$$

is simply the ratio of mass flow rate times specific heat capacity for the two streams. These can be considered as flow stream thermal-capacity rates, i.e., energy storage rate in the stream per unit of temperature change. [Ref. 2: pp. 14-26]

The attempt taken in this thesis to develop a closed form solution has used the basic fundamentals of heat transfer as well as those indicated above. A closed form solution for  $\epsilon$  was sought for both 1-3 exchangers with one having two out of three tube passes in parallel flow and the other having two out of three tube passes in counterflow. The analytical approach taken, and demonstrated in this section, is for two out of three tube passes in counterflow.

## B. ANALYTICAL DEVELOPMENT

The derivation for the effectiveness,  $\epsilon$ , of the 1-3 exchanger as a function of the capacity rate ratio,  $R$ , and number of transfer units,  $N_{tu}$ , depends on several assumptions.

- (1) The overall coefficient of heat transfer,  $U$ , does not vary within the exchanger.
- (2) The specific heat of both hot side and cold side fluids does not vary.
- (3) Each fluid is thoroughly mixed, that is, the temperature of both hot and cold side fluids is uniform over any cross section.
- (4) Steady flow conditions are maintained.
- (5) Heat losses to or from the environment are negligible.
- (6) No change of phase takes place; all heat transferred is sensible heat.
- (7) There is equal heat transfer surface in each pass.

The configuration is shown in Figure 3.1 where the three tube passes are designated with subscripts a, b and c. The temperature of the hot (shell side) fluid is indicated by upper case letters. For the cold (tube side) fluid, lower case letters are used. The subscript 1 always refers to the fluid inlet and the subscript 2 always refers to the fluid outlet.

With  $W_h$  and  $C_{ph}$  designating mass flow (kg/sec) and specific heat (Joules/kg<sup>-1</sup>K) of hot fluid entering at  $T_1$  and leaving at  $T_2$  we define a capacity rate for the hot side

$$C_h = W_h C_{ph}$$

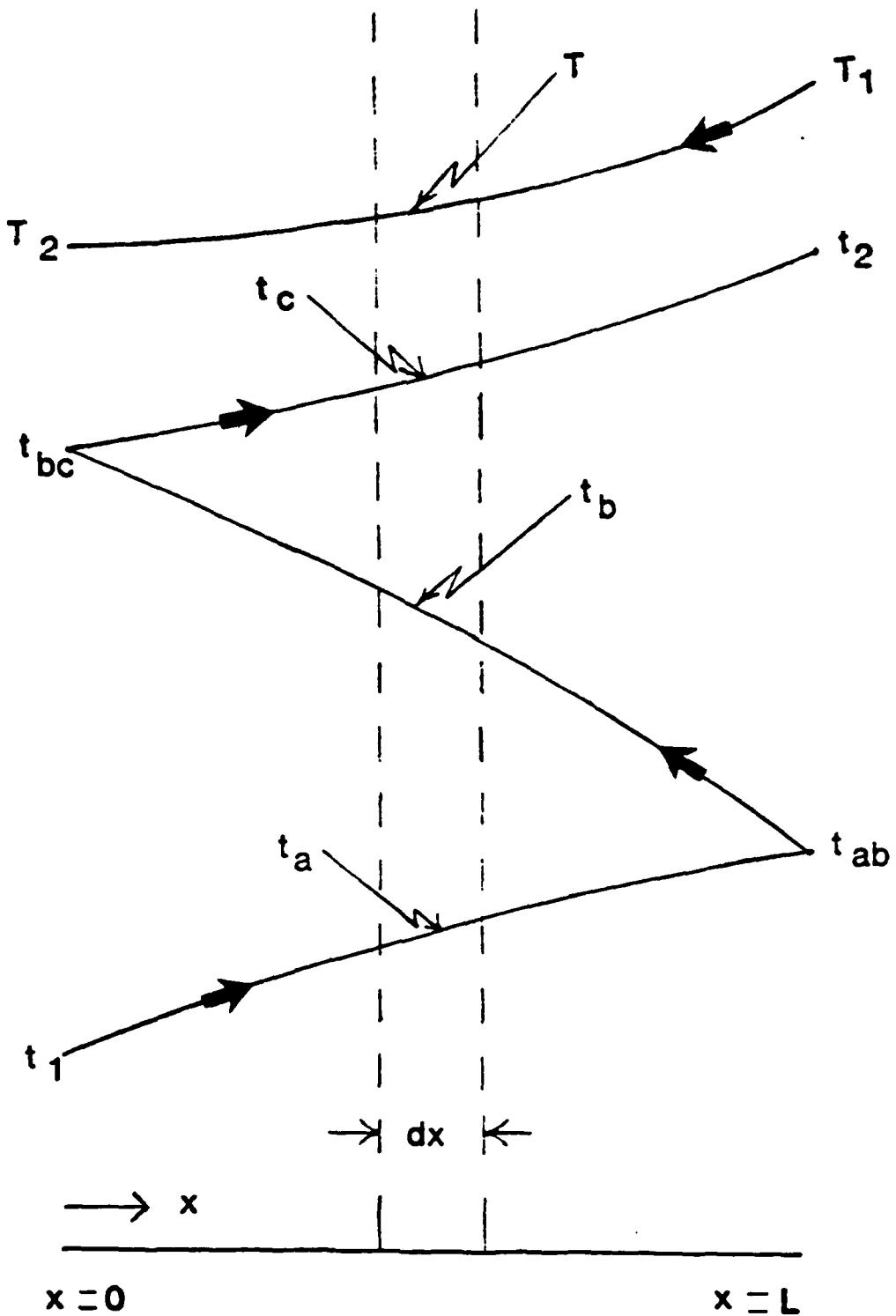


Figure 3.1 Two Counter One Parallel Configuration for Development of Effectiveness Relationship

In similar fashion for the cold side (with  $w_c$  and  $C_{pc}$ ) entering at  $t_1$  and leaving at  $t_2$ , we have

$$C_c = w_c C_{pc}$$

We then obtain an energy balance for the entire exchanger

$$C_h(T_1 - T_2) = C_c(t_2 - t_1) \quad (1)$$

Over the right hand side of the exchanger (Figure 3.1)

$$C_h(T_1 - T) = C_c(t_2 - t_c + t_b - t_a) \quad (2)$$

and a differentiation gives

$$C_h dT = C_c(dt_c - dt_b + dt_a) \quad (3)$$

Across  $dx$ , with a ( $m^2/m$ ), the surface per running meter of length of pass so that  $A = 3aL$  is the total surface in the exchanger, we may write the heat transferred to the element  $dx$  in each cold pass.

$$C_c dt_a = U a dx (T - t_a) \quad (4a)$$

$$C_c dt_b = -U a dx (T - t_b) \quad (4b)$$

$$C_c dt_c = U a dx (T - t_c) \quad (4c)$$

Here it should be observed that due cognizance has been taken of the direction of the flow in each cold fluid pass

with respect to the positive sense of the length coordinate,  $x$ , and  $U$  is the overall heat transfer coefficient ( $\text{W}/\text{m}^2 \cdot ^\circ\text{C}$ ).

With eqs. (4) in eq. (3)

$$C_h dT = U_a (3T - t_a - t_b - t_c) dx$$

or

$$\frac{dT}{dx} = n_h (3T - t_a - t_b - t_c) \quad (5)$$

where

$$n_h = \frac{U_a}{C_h}$$

is a sort of  $N_{tu}$  per unit length for the hot side.

Now differentiate eq. (5)

$$\frac{d^2 T}{dx^2} = n_h (3 \frac{dT}{dx} - \frac{dt_a}{dx} - \frac{dt_b}{dx} - \frac{dt_c}{dx})$$

and with eqs. (4) substituted

$$\frac{d^2 T}{dx^2} = 3n_h \frac{dT}{dx} - n_c n_h (T - t_a + t_b - t_c) \quad (6)$$

where

$$n_c = \frac{U_a}{C_c}$$

where again the resemblance of  $n_c$  to  $N_{tu}$  can be noted.

From eq. (2) we obtain

$$\frac{C_h}{C_c} (T_1 - T) - t_2 = t_b - t_a - t_c \quad (7)$$

and with eq. (7) put into eq. (6) we obtain

$$\frac{d^2T}{dx^2} - 3n_h \frac{dT}{dx} = - n_c n_h [T + \frac{C_h}{C_c} (T_1 - T) - t_2]$$

or

$$\frac{d^2T}{dx^2} - 3n_h \frac{dT}{dx} = -n_c n_h \frac{C_h}{C_c} [(R_c - 1)T + T_1 - R_c t_2] \quad (8)$$

where

$$R_c = C_c/C_h$$

is the capacity rate ratio for the cold side.

Notice that

$$n_c n_h \frac{C_h}{C_c} = \frac{U_a}{C_c} \cdot \frac{U_a}{C_h} \cdot \frac{C_h}{C_c} = \left(\frac{U_a}{C_c}\right)^2 = m$$

and

$$R_h = \frac{1}{R_c} = \frac{C_h}{C_c}$$

a capacity rate ratio for the hot side. Then, algebraic adjustment provides

$$\frac{d^2T}{dx^2} - 3n_h \frac{dT}{dx} + m \left( \frac{1 - R_h}{R_h} \right) T = m \left( \frac{T_2}{R_h} - T_1 \right) \quad (9)$$

which is a linear, non-homogeneous, second order differential equation with constant coefficients having a complementary function

$$T_c = C_1 e^{\alpha_1 x} + C_2 e^{\alpha_2 x} \quad (10)$$

where  $C_1$  and  $C_2$  are arbitrary constants and where

$$\alpha_1, \alpha_2 = \frac{3n_h}{2} \pm \frac{1}{2} [9n_h^2 - 4m(\frac{1 - R_h}{R_h})]^{1/2}$$

$$= \frac{3n_h}{2} \pm \frac{n_h}{2} [9 - \frac{4m}{n_h} (\frac{1 - R_h}{R_h})]^{1/2}$$

But

$$\frac{m}{n_h^2} = \frac{(Ua)^2}{(C_c)^2} \cdot \frac{(C_h)^2}{(Ua)^2} = \left( \frac{C_h}{C_c} \right)^2 = R_h^2 = \frac{1}{R_c^2}$$

so that

$$\alpha_1, \alpha_2 = \frac{3n_h}{2} \pm \frac{n_h}{2} [9 - 4R_h^2 (\frac{1 - R_h}{R_h})]^{1/2}$$

or

$$\alpha_1, \alpha_2 = \frac{n_h}{2} (3 \pm \lambda) \quad (11)$$

where

$$\lambda = [9 - 4R_h(1 - R_h)]^{1/2} \quad (12)$$

Designate the particular integral as  $T_{pi}$  and by the method of undetermined coefficients let  $T_{pi} = P$  so that in eq. (9)

$$m\left(\frac{1 - R_h}{R_h}\right) P = m\left(\frac{t_2}{R_h} - T_1\right)$$

This makes

$$T_{pi} = P = \left[ \frac{t_2}{R_h} - T_1 \right] \left[ \frac{R_h}{1 - R_h} \right]$$

so that

$$T_{pi} = \frac{t_2 - R_h T_1}{1 - R_h} \quad (13)$$

The general solution to eq. (9) is the sum of eqs. (10) and (13)

$$T(x) = C_1 e^{\alpha_1 x} + C_2 e^{\alpha_2 x} + \frac{t_2 - R_h T_1}{1 - R_h} \quad (14)$$

where the arbitrary constants,  $C_1$  and  $C_2$  are evaluated from conditions at  $x = 0$  and  $x = L$ . At  $x = 0$ ,  $T(x = 0) = T_2$  and at  $x = L$ ,  $T(x = L) = T_1$ . When these are inserted, in turn, into eq. (14), one obtains a pair of linear algebraic equations in the unknowns  $C_1$  and  $C_2$

$$T_2 = C_1 + C_2 + T_{pi}$$

$$T_1 = C_1 e^{\alpha_1 L} + C_2 e^{\alpha_2 L} + T_{pi}$$

where  $T_{pi}$  is given by eq. (13).

It is only a matter of algebra to show that

$$C_1 = \frac{(T_1 - T_{pi}) - (T_2 - T_{pi})e^{\alpha_2 L}}{e^{\alpha_1 L} - e^{\alpha_2 L}} \quad (15a)$$

and

$$C_2 = \frac{(T_2 - T_{pi})e^{\alpha_1 L} - (T_1 - T_{pi})}{e^{\alpha_1 L} - e^{\alpha_2 L}} \quad (15b)$$

It is easy to see from eq. (1) that

$$R_h = \frac{C_h}{C_c} = \frac{(t_2 - t_1)}{(T_1 - T_2)}$$

so that

$$t_2 = t_1 + R_h(T_1 - T_2)$$

Use of this in eq. (13) shows that

$$T_{pi} = \frac{t_1 + R_h(T_1 - T_2) - R_h T_1}{1 - R_h}$$

or

$$T_{pi} = \frac{t_1 - R_h T_2}{1 - R_h} \quad (16)$$

indicating two alternative forms for  $T_{pi}$  given by eqs. (13) and (16).

Insertion of eqs. (13) and (16) in eqs. (15) for  $C_1$  and  $C_2$  will yield after some algebra

$$C_1 = \frac{\left(\frac{T_1 - t_2}{1 - R_h}\right) - \left(\frac{T_2 - t_1}{1 - R_h}\right) e^{\alpha_2 L}}{e^{\alpha_1 L} - e^{\alpha_2 L}} \quad (17a)$$

and

$$C_2 = \frac{\left(\frac{T_2 - t_1}{1 - R_h}\right) e^{\alpha_1 L} - \left(\frac{T_1 - t_2}{1 - R_h}\right)}{e^{\alpha_1 L} - e^{\alpha_2 L}} \quad (17b)$$

Equation (14) is an expression for the hot side temperature at any location in the exchanger in terms of the extreme temperatures,  $t_1$ ,  $t_2$ ,  $T_1$  and  $T_2$ .

Next take eq. (5) and set it equal to the derivative of eq. (14) noting that  $C_1$ ,  $C_2$  and  $T_{pi}$  are all known constants.

$$\frac{dT}{dx} = n_h (3T - t_a - t_b - t_c) = \alpha_1 C_1 e^{\alpha_1 x} + \alpha_2 C_2 e^{\alpha_2 x} \quad (18)$$

At  $x = 0$ , where  $T = T_2$ ,  $t_a = t_1$  and  $t_b = t_c = t_{bc}$

$$\frac{dT}{dx} = n_h(3T_2 - t_1 - 2t_{bc}) = \alpha_1 C_1 + \alpha_2 C_2 \quad (19)$$

and if we subtract eq. (4a) from eq. (4c) we obtain

$$\frac{dt_a - dt_c}{t_a - t_c} = - \frac{U_a}{C_c} dx = -n_c dx$$

which can be integrated using  $C_3$  as the constant of integration.

$$t_a - t_c = C_3 e^{-n_c x}$$

and at  $x = 0$  where  $t_a = t_1$  and  $t_c = t_{bc}$

$$t_1 - t_{bc} = C_3$$

or

$$t_{bc} = t_1 - C_3$$

In addition at  $x = L$ ,  $t_a = t_{ab}$  and  $t_c = t_2$  so that

$$t_{ab} - t_2 = C_3 e^{n_c L}$$

or

$$C_3 = \frac{t_{ab} - t_2}{e^{-n_h L}} = (t_{ab} - t_2) e^{n_c L}$$

This gives a relationship between  $t_{ab}$  and  $t_{bc}$

$$t_{bc} = t_1 - (t_{ab} - t_2) e^{n_c L} \quad (20)$$

where  $N_c = n_c L$  can be considered as the total number of transfer units for the cold side.

Return now to eq. (18) and look at the conditions at  $x = L$  where  $t_a = t_b = t_{ab}$ ,  $t_c = t_2$  and  $T = T_1$ . These conditions in eq. (18) give

$$n_h(3T_1 - 2t_{ab} - t_2) = \alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L}$$

where again we remember that  $C_1$  and  $C_2$  are known constants.

Solving for  $t_{ab}$

$$2t_{ab} = -\frac{1}{n_h} (\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L}) + 3T_1 - t_2$$

and with this in eq. (20)

$$2t_{bc} = e^{N_c} \left[ \frac{1}{n_h} (\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L}) + 3t_2 - 3T_1 \right] + 2t_1$$

Then with eq. (21) in eq. (19)

$$\begin{aligned} \alpha_1 C_1 + \alpha_2 C_2 &= 3n_h [(T_2 - t_1) + e^{N_c} (T_1 - t_2)] \\ &\quad - e^{N_c} (\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L}) \end{aligned} \quad (22)$$

Equation (22) confirms Fischer's result [Ref. 12: pp. 377-383] and at this point in his development he branches off to seek an expression for the Logarithmic Mean

Temperature Difference Correction Factor, F. The attention here is focused on  $\epsilon = f(R, N_{tu})$  and the balance of this section continues in this vein.

Look at the  $\alpha_1 C_1 + \alpha_2 C_2$  term in eq. (22). Use of eq. (11) allows the representation of  $\alpha_1 C_1 + \alpha_2 C_2$

$$\frac{n_h}{2} (3 + \lambda) C_1 + \frac{n_h}{2} (3 - \lambda) C_2 \quad (23a)$$

or

$$\frac{3n_h}{2} (C_1 + C_2) + \frac{\lambda n_h}{2} (C_1 - C_2) \quad (23b)$$

Then from eqs. (17)

$$C_1 + C_2 = \frac{(T_2 - t_1)[e^{\alpha_1 L} - e^{\alpha_2 L}]}{(1 - R_h)[e^{\alpha_1 L} - e^{\alpha_2 L}]}$$

or

$$C_1 + C_2 = \frac{T_2 - t_1}{1 - R_h} \quad (24)$$

Moreover

$$C_1 - C_2 = \frac{2(T_1 - t_2) - (T_2 - t_1)[e^{\alpha_1 L} + e^{\alpha_2 L}]}{(1 - R_h)[e^{\alpha_1 L} - e^{\alpha_2 L}]} \quad (25)$$

Now let

$$\omega = \frac{3n_h}{2} \quad (26a)$$

and

$$z = \frac{\lambda n_h}{2} \quad (26b)$$

so that

$$\begin{aligned} e^{\alpha_1 L} - e^{\alpha_2 L} &= e^{(\omega+z)L} - e^{(\omega-z)L} \\ &= e^{\omega L} e^{zL} - e^{\omega L} e^{-zL} \\ &= e^{\omega L} (e^{zL} - e^{-zL}) \end{aligned}$$

or

$$e^{\alpha_1 L} - e^{\alpha_2 L} = 2e^{\omega L} \sinh zL \quad (27)$$

Moreover, it is easy to see that

$$e^{\alpha_1 L} + e^{\alpha_2 L} = 2e^{\omega L} \cosh zL \quad (28)$$

If eqs. (24) through (28) are collected and put into the expression of eq. (23b), the result is

$$\alpha_1 C_1 + \alpha_2 C_2 = \frac{3n_h}{2} (C_1 + C_2) + \frac{\lambda n_h}{2} (C_1 - C_2) \quad (23b)$$

$$= \omega \left[ \frac{T_2 - t_1}{1 - R_h} \right] + z \left[ \frac{2(T_1 - t_2) - (T_2 - t_1)2e^{\omega L} \operatorname{csch} zL}{(1 - R_h)2e^{\omega L} \sinh zL} \right]$$

or

$$\alpha_1 C_1 + \alpha_2 C_2 = \omega \left( \frac{T_2 - t_1}{1 - R_h} \right) +$$

$$z \left[ \left( \frac{T_1 - t_2}{1 - R_h} \right) e^{-\omega L} \operatorname{csch} zL - \left( \frac{T_2 - t_1}{1 - R_h} \right) \coth zL \right] \quad (29a)$$

and this could also be written as

$$\alpha_1 C_1 + \alpha_2 C_2 = \left( \frac{T_2 - t_1}{1 - R_h} \right) [\omega - z \coth zL]$$

$$+ z \left( \frac{T_1 - t_2}{1 - R_h} \right) e^{-\omega L} \operatorname{csch} zL \quad (29b)$$

The next step is to reduce the right hand side of eq. (22). Use of eq. (11) permits the representation

$$\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L} = \left( \frac{3n_h}{2} + \frac{\lambda n_h}{2} \right) C_1 e^{\alpha_1 L} + \left( \frac{3n_h}{2} - \frac{\lambda n_h}{2} \right) C_2 e^{\alpha_1 L}$$

or with eqs. (26) inserted

$$\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L} = \omega (C_1 e^{\alpha_1 L} + C_2 e^{\alpha_2 L}) + z(C_1 e^{\alpha_1 L} - C_2 e^{\alpha_2 L}) \quad (30)$$

But by eqs. (11) and (17)

$$C_1 e^{\alpha_1 L} + C_2 e^{\alpha_2 L} = \frac{(T_1 - t_2)(e^{\alpha_1 L} - e^{\alpha_2 L}) + (T_2 - t_1)[e^{(\alpha_1 + \alpha_2)L} - e^{(\alpha_1 + \alpha_2)L}]}{(1 - R_h)(e^{\alpha_1 L} - e^{\alpha_2 L})}$$

or

$$C_1 e^{\alpha_1 L} + C_2 e^{\alpha_2 L} = \frac{T_1 - t_2}{1 - R_h} \quad (31)$$

$C_1 e^{\alpha_1 L} - C_2 e^{\alpha_2 L}$  may also be simplified. Again using eqs. (11), (17a) and (17b)

$$C_1 e^{\alpha_1 L} - C_2 e^{\alpha_2 L} = \frac{(T_1 - t_2)(e^{\alpha_1 L} + e^{\alpha_2 L}) - (T_2 - t_1)[e^{(\alpha_1 + \alpha_2)L} + e^{(\alpha_1 + \alpha_2)L}]}{(1 - R_h)(e^{\alpha_1 L} - e^{\alpha_2 L})}$$

The exponential term at the far right in the numerator is really quite simple. From eq. (11)

$$\alpha_1 + \alpha_2 = \left( \frac{3n_h}{2} + \frac{\lambda n_h}{2} \right) + \left( \frac{3n_h}{2} - \frac{\lambda n_h}{2} \right) = 3n_h$$

and by eq. (26a)  $\alpha_1 + \alpha_2 = 3n_h = 2\omega$ . Thus with the combination of exponentials in the numerator and the denominator given by eqs. (27) and (28) we find that

$$C_1 e^{\alpha_1 L} - C_2 e^{\alpha_2 L} = \frac{2(T_1 - t_2)e^{\omega L} \cosh zL - (T_2 - t_1)2e^{2\omega L}}{2(1 - R_h)e^{\omega L} \sinh zL}$$

or

$$C_1 e^{\alpha_1 L} - C_2 e^{\alpha_2 L} = \frac{T_1 - t_2}{1 - R_h} \coth zL - \frac{T_2 - t_1}{1 - R_h} e^{\omega L} \operatorname{csch} zL \quad (32)$$

Now with eqs. (31) and (32) put into eq. (30) we obtain

$$\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L} = \omega \left( \frac{T_1 - t_2}{1 - R_h} \right)$$

$$+ z \left[ \left( \frac{T_1 - t_2}{1 - R_h} \right) \coth zL - \left( \frac{T_2 - t_1}{1 - R_h} \right) e^{\omega L} \operatorname{csch} zL \right]$$

or

$$\alpha_1 C_1 e^{\alpha_1 L} + \alpha_2 C_2 e^{\alpha_2 L} = \left( \frac{T_1 - t_2}{1 - R_h} \right) [\omega + z \coth zL]$$

$$- z \left( \frac{T_2 - t_1}{1 - R_h} \right) e^{\omega L} \operatorname{csch} zL \quad (33)$$

With eqs. (29b) and (33) inserted into eq. (22) we obtain

$$\begin{aligned} & \left( \frac{T_2 - t_1}{1 - R_h} \right) [\omega - z \coth zL] + z \left( \frac{T_1 - t_2}{1 - R_h} \right) e^{-\omega L} \operatorname{csch} zL = \\ & 3n_h [(T_2 - t_1) + e^{-N_c} (T_1 - t_2) - \\ & e^{-N_c} \left( \frac{T_1 - t_2}{1 - R_h} \right) (\omega + z \coth zL) - z \left( \frac{T_2 - t_1}{1 - R_h} \right) e^{\omega L} \operatorname{csch} zL] \end{aligned} \quad (34)$$

We wish to develop an expression for the exchanger effectiveness so we designate the hot side effectiveness as

$$\epsilon_h = \frac{T_1 - t_2}{T_1 - t_1} \quad (35)$$

and we begin by simplifying eq. (34) by dividing throughout by  $(T_2 - t_1)/(1 - R_h)$  to obtain

$$(w - z \coth Z) + ze^{-W} \operatorname{csch} z \left( \frac{T_1 - t_2}{T_2 - t_1} \right) = R + e^{-N_c R} \left( \frac{T_1 - t_2}{T_2 - t_1} \right)$$

$$- e^{-N_c} [(w + z \coth Z) \left( \frac{T_1 - t_2}{T_2 - t_1} \right) - ze^W \operatorname{csch} Z] \quad (36)$$

where

$$W = \omega L \quad (37a)$$

$$Z = zL \quad (37b)$$

and

$$R = 3n_h(1 - R_h) \quad (37c)$$

We can then let

$$\phi = \frac{T_1 - t_2}{T_2 - t_1}$$

and get eq. (36) to look like

$$(\omega - z \coth Z) + (ze^{-W} \operatorname{csch} Z) \phi =$$

$$R + (e^{Nc} R) \phi - [e^{-Nc} (\omega + \coth Z)] \phi - (ze^{(W-Nc)} \operatorname{csch} Z)$$

It is now a matter of algebra to solve for  $\phi$

$$\phi = \frac{R + ze^{(W-Nc)} \operatorname{csch} Z - (\omega - z \coth Z)}{ze^{-W} \operatorname{csch} Z - Re^c + e^c (\omega + z \coth Z)} \quad (38)$$

The next step is to represent  $\phi$  as a function of  $\epsilon_h$ .

This is done with some algebraic gymnastics as follows:

$$\phi = \frac{T_1 - t_2}{T_2 - t_1} = \frac{T_1 - t_2}{T_2 - T_1 + T_1 - t_1} = \frac{T_1 - t_2}{(T_1 - t_1)(\frac{T_1 - T_2}{T_1 - t_1})}$$

or

$$\phi = \frac{T_1 - t_2}{(T_1 - t_1)(1 - \epsilon_h)}$$

Moreover

$$\phi = \frac{T_1 - t_2}{(T_1 - t_1)(1 - \epsilon_h)} = \frac{T_1 - t_1 + t_1 - t_2}{(T_1 - t_1)(1 - \epsilon_h)}$$

$$= \frac{(T_1 - t_1)[1 - (\frac{t_2 - t_1}{T_1 - t_1})] (\frac{T_1 - T_2}{T_1 - t_1})}{(T_1 - t_1)(1 - \epsilon_h)}$$

$$= \frac{1 - \left( \frac{T_1 - T_2}{T_1 - t_1} \right) \left( \frac{t_2 - t_1}{T_1 - T_2} \right)}{1 - \epsilon_h}$$

But  $R_h = (t_2 - t_1)/(T_1 - T_2)$  so that

$$\phi = \frac{1 - \epsilon_h R_h}{1 - \epsilon_h}$$

or

$$\epsilon_h = \frac{\phi - 1}{\phi - R_h} \quad (39)$$

where  $\phi$  is given by eq. (38)

The neatness of the form of eq. (39) is deceptive because, unfortunately, it cannot be used to determine a unique value for  $\epsilon_h$ . The reason for this can be found in an inspection of eq. (38) which provides the value of  $\phi$  which is used in eq. (39).

Notice in eq. (38) that  $Z$ ,  $W$  and  $N_C$  are all functions of the product  $aL$ . On the other hand,  $w$ ,  $z$  and  $R$  are functions of  $a$  only. Thus, it is impossible to vary  $a$  and  $L$  independently and still achieve a unique solution.

For example, suppose  $a = 50 \text{ m}^2/\text{m}$  and  $L = 5 \text{ m}$  so that  $aL = 250$ . A value of  $\phi$  may be obtained from eq. (38) using these values. However, if  $a = 100$  and  $L = 2.5$  so that  $aL$  is still equal to 250, an entirely different value of  $\phi$  is obtained because  $a = 100$  rather than 50.

One should resist the temptation to multiply numerator and denominator of eq. (38) by L thereby creating a situation where only Z, W and  $N_c$  appear along with a new  $R' = RL$ . Such a procedure is doomed to failure because in dealing with an equation derived from n equations in  $n+1$  unknowns, one cannot create the  $n+1^{th}$  equation by multiplying one of the n equations by a constant. This makes the  $n+1^{th}$  equation so obtained linearly dependent on one of the original n equations and the entire set becomes linearly dependent.

This section represents an attempt to obtain  $\epsilon = f(R, N_{tu})$  and the attempt has not been successful. It is now time to turn to the computer and this will be done in Section IV.

#### IV. NUMERICAL AND COMPUTER ANALYSIS

With a closed form solution for  $\epsilon$  as a function of  $R$  and  $N_{tu}$  not attainable as indicated in Section III, it becomes apparent that an alternative method is needed to determine the effectiveness for the 1-3:2C and 1-3:2P heat exchangers. Kern and Kraus [Ref. 12: pp. 306-360] describe a computer code for a thermal analyzer. This code (program) makes use of node equations generated by finite differences and it employs a Cholesky LU decomposition scheme.

The Cholesky decomposition, as explained by Stewart [Ref. 13: pp. 134-144], is best used when decomposition in the presence of positive definite matrices is requested. This is the case at hand where one tries to solve numerically for the temperatures that lead to the effectiveness of the 1-3:2C and 1-3:2P heat exchangers.

##### A. THERMAL ANALYZER TVSSI

The computer program employed is Program TVSSI (Appendix A) which is an adaptation of the thermal analyzer program called TVSS2 and listed by Kern and Kraus [Ref. 12: pp. 306-360]. The adaptation consisted of changing the program so that it could perform the computations in the SI system of units and be receptive to the use of a specially created input file. Also it should be noted that TVSS2 was written

to be used in conjunction with the Honeywell H-1800 computer system. Therefore, it had to be modified to run on the Naval Postgraduate School's IBM 3033 AP system.

The program itself is a non-linear equation solver that determines the temperatures at a prescribed number of node-points or nodes from a set of node equations in almost any framework (i.e., network analysis, field plotting, or fluid flow distribution). It has certain features that make it primarily an equation solver for thermal analysis. These features include:

1. an ability to linearize radiation terms.
2. an ability to allow any of the coefficients in the node equations to vary with temperature.
3. an ability to provide constant heat input and heat input as a function of temperature at any node.
4. an ability to consider other modes of heat transfer that are non-linear such as boiling and natural convection.

As stated earlier, the program utilizes the Cholesky decomposition scheme and, because of the linearization of the radiation terms (a feature of the program that is used even though radiation does not appear in this  $\epsilon$  -  $N_{tu}$  study), the program is iterative.

Cholesky's decomposition consists of finding a lower triangular matrix [L] which is capable of reducing the original system of equations.

$$[K][T] = [Q] \quad (40)$$

or

$$[K][T] - [Q] = [0] \quad (41)$$

to the unit triangular form

$$[A][T] - [B] = [0] \quad (42)$$

so that the sought after elements of the column vector  $[T]$  can be obtained by backward substitution.

Suppose, for example, that  $[K]$  is  $3 \times 3$  and assume that the system  $[K][T] = [Q]$  has been reduced to the form  $[A][T] - [B] = [0]$ . In this event a premultiplication by  $[L]$  will return the system to its original form, that is

$$[L]([A][T] - [B]) = [K][T] - [Q] = [0]$$

This implies that

$$[L][A] = [K] \quad (43)$$

and

$$[L][B] = [Q] \quad (44)$$

These equations allow the determination of  $[L]$ ,  $[A]$ , and  $[B]$  in a very simple manner and the matrices are uniquely determined because  $[K]$  and  $[Q]$  are known, or, at least are known after each iteration because the elements of  $[K]$  are linearized. For a  $3 \times 3$  system

$$\begin{array}{c}
 [\mathbf{K}, \mathbf{Q}] \\
 \left[ \begin{array}{cccc}
 k_{11} & k_{12} & k_{13} & q_1 \\
 k_{21} & k_{22} & k_{23} & q_2 \\
 k_{31} & k_{32} & k_{33} & q_3
 \end{array} \right]
 \end{array}
 =
 \begin{array}{c}
 [\mathbf{L}] \\
 \left[ \begin{array}{ccc}
 l_{11} & 0 & 0 \\
 l_{21} & l_{22} & 0 \\
 l_{31} & l_{32} & l_{33}
 \end{array} \right]
 \end{array}
 =
 \begin{array}{c}
 [\mathbf{A}, \mathbf{B}] \\
 \left[ \begin{array}{cccc}
 1 & a_{12} & a_{13} & b_1 \\
 0 & 1 & a_{23} & b_2 \\
 0 & 0 & 1 & b_3
 \end{array} \right]
 \end{array}$$

one may obtain the following for the elements of  $[\mathbf{L}]$ ,  $[\mathbf{A}]$ , and  $[\mathbf{B}]$ .

$$k_{11} = (1)l_{11} + (0)l_{12} + (0)l_{13} = l_{11} \quad (45)$$

which shows that the first column of  $[\mathbf{L}]$  is identical to the first column of  $[\mathbf{K}]$ .

$$k_{1j} = (l_{11})a_{1j} + (0)a_{2j} + (0)a_{3j} = l_{11}a_{1j} = k_{11}a_{1j} \quad (46)$$

which shows that the first row of  $[\mathbf{A}]$  is equal to the first row of  $[\mathbf{K}]$  divided by  $[k_{11}]$  and then

$$k_{22} = l_{21}a_{12} + l_{22}(1), \quad l_{22} = k_{22} - l_{21}a_{12}$$

$$k_{23} = l_{21}a_{13} + l_{22}a_{23}, \quad a_{23} = (k_{23} - l_{21}a_{13})/l_{22}$$

$$k_{32} = l_{31}a_{12} + l_{32}(1), \quad l_{32} = k_{32} - l_{31}a_{12}$$

$$q_2 = l_{21}b_1 + l_{22}b_2, \quad b_2 = (q_2 - l_{21}b_1)/l_{22}$$

In the foregoing manner the elements of  $[\mathbf{L}]$ ,  $[\mathbf{A}]$  and  $[\mathbf{B}]$  are obtained successively in terms of previously determined elements in a progression that goes horizontally from  $l_{22}$  on. Thus the general relationship are seen to be

$$l_{ij} = k_{ij} - \sum_{r=1}^{j-1} l_{ir} k_{rj} \quad (47)$$

with

$$l_{i1} = k_{i1} \quad (48)$$

and

$$a_{ij} = \frac{1}{l_{ii}} [k_{ij} - \sum_{r=1}^{i-1} l_{ir} a_{rj}] \quad (49)$$

with

$$a_{ij} = \frac{k_{ij}}{k_{11}} \quad (50)$$

Moreover, it is observed that if  $[K]$  is symmetrical which it must be in our coupled set of equations ( $k_{ij} = k_{ji}$ ) then

$$l_{ij} = a_{j1} l_{i1} \quad (i,j = 1,2,3,\dots n-1; i \neq j) \quad (51)$$

The modification for computation in the SI system was quick and simple. It involved changing a numeral in two places (460 to 273) and some format statements ( $^{\circ}\text{F}$  to  $^{\circ}\text{C}$  and Btu/hr to Watts).

The conversion of TVSS2 to TVSSI for running on the IBM 3033 AP system (which uses the FORTVS compiler) required

a modification to the Fortran program language used in TVSS2 in order to compile the FORTVS (basically international Fortran 77) system used on the IBM 3033.

#### B. INITIAL MODELING

Initially, the model was designed to find the temperatures that would allow computation of a single effectiveness value after a detailed set of capacity rate, coefficients and surface data were entered into the program. From the scope of the problem it was realized that multiple runs of the thermal analyzer program (TVSSI) would be needed. It therefore became necessary to develop a program that given  $C_h$ ,  $C_c$ ,  $U$ ,  $A$ ,  $T_1$ , and  $t_1$ , an input file would be created for use by the modified version of the thermal analyzer (TVSSI).

The first step taken was to develop a program to create an input file for TVSSI that would yield the effectiveness for a 1-4 heat exchanger which could be compared to the existing analytical solution for the effectiveness of a 1-4 exchanger. With this accomplished and confidence established, similar programs for the 1-3:2C and 1-3:2P exchangers could be developed. This program was called NTU14 (See Appendix B) and the following parameters were used for all runs.

1. 250 nodes were used.
2. The initial temperature for the computer to begin the iterative process was set at 200°C.

3. An eventual accuracy of .05 between the final and next to last iterations was used.
4. A radiation coefficient convergence factor of 0.66667 between iterations was used.
5. The maximum number of iterations that the computer was allowed to perform was set at 12.
6. A damping factor of .8 was set as an initial damping based on the number of non-linear terms in all of the node equations.

When the values of  $C_h$ ,  $C_c$ ,  $U$ ,  $A$ ,  $T_1$  and  $t_1$  are set,  $N_{tu}$  and  $R$  are then compiled and an input file for TVSSI was generated. In this file all node equations and internode conductance values were determined. This program determined and specified the nodes that interact with each other and the methods by which the interaction takes place such as conduction, forced convection, and fluid flow.

The program, NTU14, makes use of the fact that each term in a node equation shows three things. The first is the node that is coupled for heat flow with the node in question. The second is the method of heat flow between the nodes. In this case forced convection and fluid flow are used. Finally, the node equation shows the magnitude of the internode heat flow. Here all the pieces of information are collected and presented for use by TVSSI as an input file with all items in the proper format.

A comparison of the effectiveness for the 1-4 exchanger developed by the computer to that of using the closed form analytical solution for effectiveness developed by Kraus

and Kern [Ref. 8] as shown by equation (52)

$$\epsilon = \frac{2}{1 + R + \frac{1}{2}[1 + 4R^2]^{1/2} \coth(\frac{N_{tu}[1 + 4R^2]}{4}) + 4 \tanh \frac{N_{tu}}{4}} \quad (52)$$

was then undertaken. The results of this comparison showed that over the entire range of R from .01 to 1.0 for varying values of N<sub>tu</sub> from 0 to 3.25 less than a 0.5% difference was ever realized. A small sample of these results are provided in Table 1. The conclusion to be drawn here, is that the methodology used to develop the computer program NTU14 for input to TVSSI for finding effectiveness was sound and could then be used in the development of the 1-3:2C and 1-3:2P exchanger methodology.

#### C. DEVELOPED MODELS FOR 1-3:2C AND 1-3:2P HEAT EXCHANGERS

The same technique used in developing the program NTU14 was used to generate computer programs NTU32C and NTU32P. These are listed in Appendices C and D. The departure for each of these programs from the NTU14 program is in the number of nodes; they are based on 200 node models as shown in Figures 4.1 and 4.2. An example of the output file generated from one of these programs is found at Appendix E. It is these values shown in Appendix E that are used by the thermal analyzer to determine the temperatures T<sub>2</sub> and t<sub>2</sub> for the specific set of given initial parameters C<sub>h</sub>, C<sub>c</sub>, R, A, T<sub>1</sub>, and t<sub>1</sub>.

TABLE 1  
COMPUTER TO ANALYTICAL COMPARISON  
FOR R = .5

$N_{tu}$	ANALYTICAL RESULTS	COMPUTER RESULTS	% DIFFERENCE
0.05	.0482	.0482	0.00
0.25	.2094	.2090	0.20
0.50	.3569	.3559	0.28
0.75	.4628	.4612	0.35
1.00	.5398	.5377	0.39
1.25	.5963	.5940	0.39
1.50	.6379	.6354	0.40
2.00	.6915	.6886	0.42
2.50	.7206	.7177	0.40
3.00	.7360	.7333	0.37
3.25	.7406	.7381	0.34

#### D. SCOPE OF COMPUTER ANALYSIS

At this point it is possible to let the computer solve for temperature values that yield a value for effectiveness based on a specific set of initial parameters. However, it must be realized that many computer runs are required to generate enough data to ensure confidence in the results which cover a wide range of capacity rate ratios and  $N_{tu}$  values.

To efficiently expedite the computer task, the Multiple Virtual System (MVS) with Job Entry Subsystem and Networking (JES3) was utilized. The MVS coupled with JES3 is more commonly referred to as batch processing. Based on trial and error, it was determined that in order to build a solid data base, eleven different values for effectiveness were needed to best represent a particular value of R. This was required over a range of R from R = 0.1 to 1.0 in increments of .01. In all, 200 curves for both the 1-3:2C and 1-3:2P exchangers were needed. This means that 2,200 unique values of effectiveness needed to be found, plus 100 values of effectiveness to be used for comparison with the 1-4 exchangers.

To complete this task, TVSSI was slightly modified in accordance with the appropriate guidelines of the job control language (JCL) needed to run on the batch processing system. These modifications are few and were needed only at the beginning and end of TVSSI. The modified version

of TVSSI has been called TVCOUNT with changes shown in Appendix F. It was TVCOUNT that was then used to activate TVSSI.

It also became necessary to modify the three input file programs NTU14, NTU32P and NTU32C such that they needed to be compiled only once. They were then loaded in a library file to be used when called by another program. New programs utilizing the batch system were written that could easily be loaded with the appropriate input data for a specific R value. These, which are referred to as "sister programs," were used to go from the library file to TVSSI and cause TVSSI to be executed eleven times under TVCOUNT covering the desired range of N<sub>tu</sub> for a specific R value. The revised input files called NTU14C, NTU32CC, NTU32PC and their associated "sister execution programs," NTU14L, NTU32CL, NTU32PL, are found in Appendices G through L.

The overall system flow chart of how all of the foregoing is accomplished is found in Figures 4.3, 4.4 and 4.5. It is noted from these figures that TVSSI is referred to as TVSSIA through TVSSIV. These are the same programs as TVSSI but for bookkeeping purposes by the computer they are labeled A through V.

#### E. COMPUTER RESULTS

Upon completion of all data collection from the computer output, plots of effectiveness vs. N<sub>tu</sub> for the whole range

of R were plotted and are shown in Appendices M and N. Thirty-three different plotting programs utilizing the "Display Integrated Software System and Plotting Language (DISSPLA)," were written to graph the data obtained. An example of one of these programs is provided in Appendix O.

Examination of the graphs in Figures 4.6, 4.7, and 4.8 shows that the 1-3:2C exchangers outperform the 1-3:2P, 1-2 and 1-4 exchangers. This is true in all cases, and, because of this, only a sample of the data was chosen to be shown in these figures. Furthermore, it is noted that at higher Ntu values, the effectiveness of the 1-3:2C exchanger is better than all of the others considered, while at higher capacity rate ratios, the effectiveness of 1-3:2C exchanger even begins to outperform the others at lower Ntu values. This increase in performance is easily understood because it has been proven by Kern [Ref. 1: pp. 139-137] and others that greater temperature differences result when process streams are in counterflow than parallel flow. Thus, when there is a combination of the two phenomena (counterflow and parallel flow) occurring, then it becomes apparent that the extra counterflow pass must increase the exchanger's overall performance.

As shown in the graphs in Appendices M and N, effectiveness increases as both R and Ntu increase. These curves can be used to give a graphical approximation of effectiveness

if that is all that is required. From the empirical data used to develop these curves, further investigation into the development of equations for these curves which may be used to determine an exact value of effectiveness when  $R$  and  $N_{tu}$  are known, is undertaken in Section V.

1-3:2C NODE MODEL

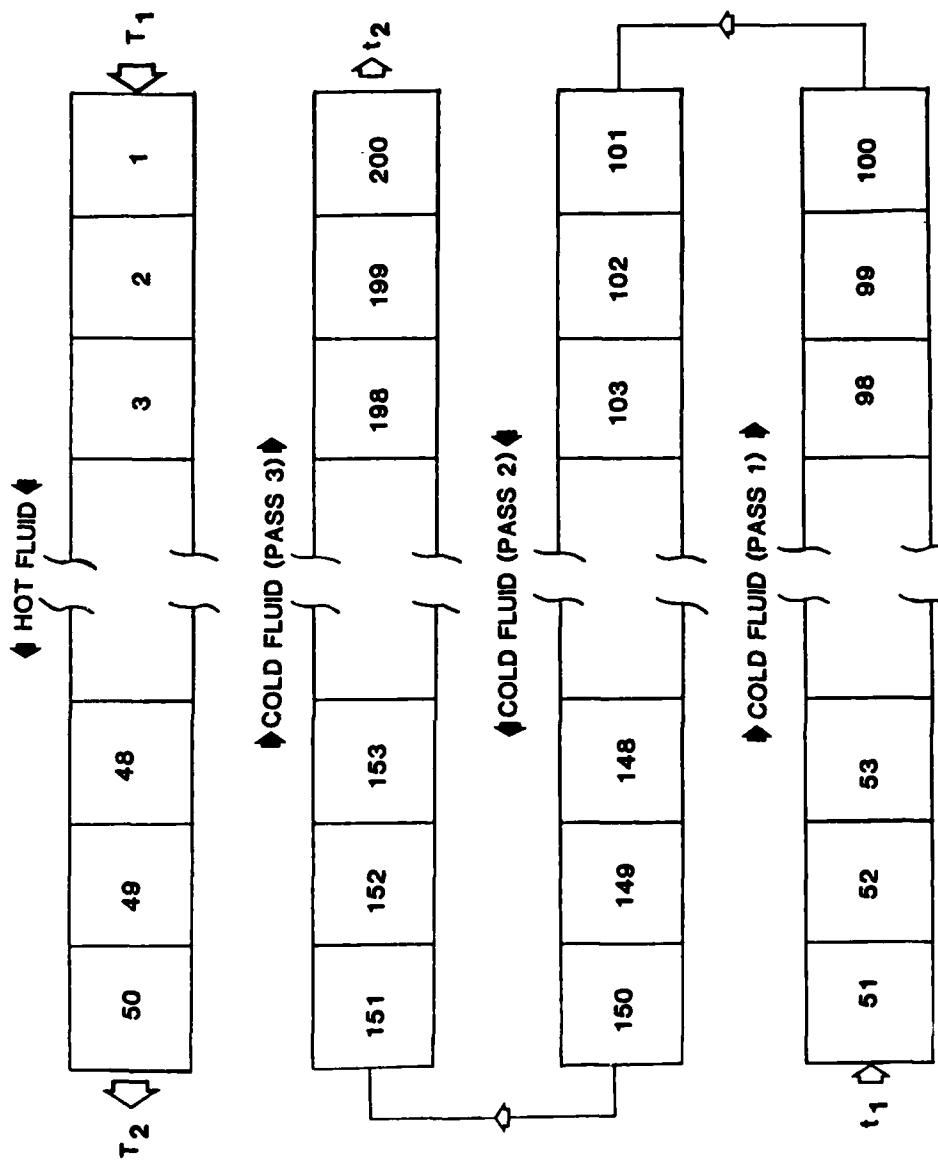


Figure 4.1 Nodal Arrangement for the 1-3:2C Exchanger

1-3:2P NODE MODEL

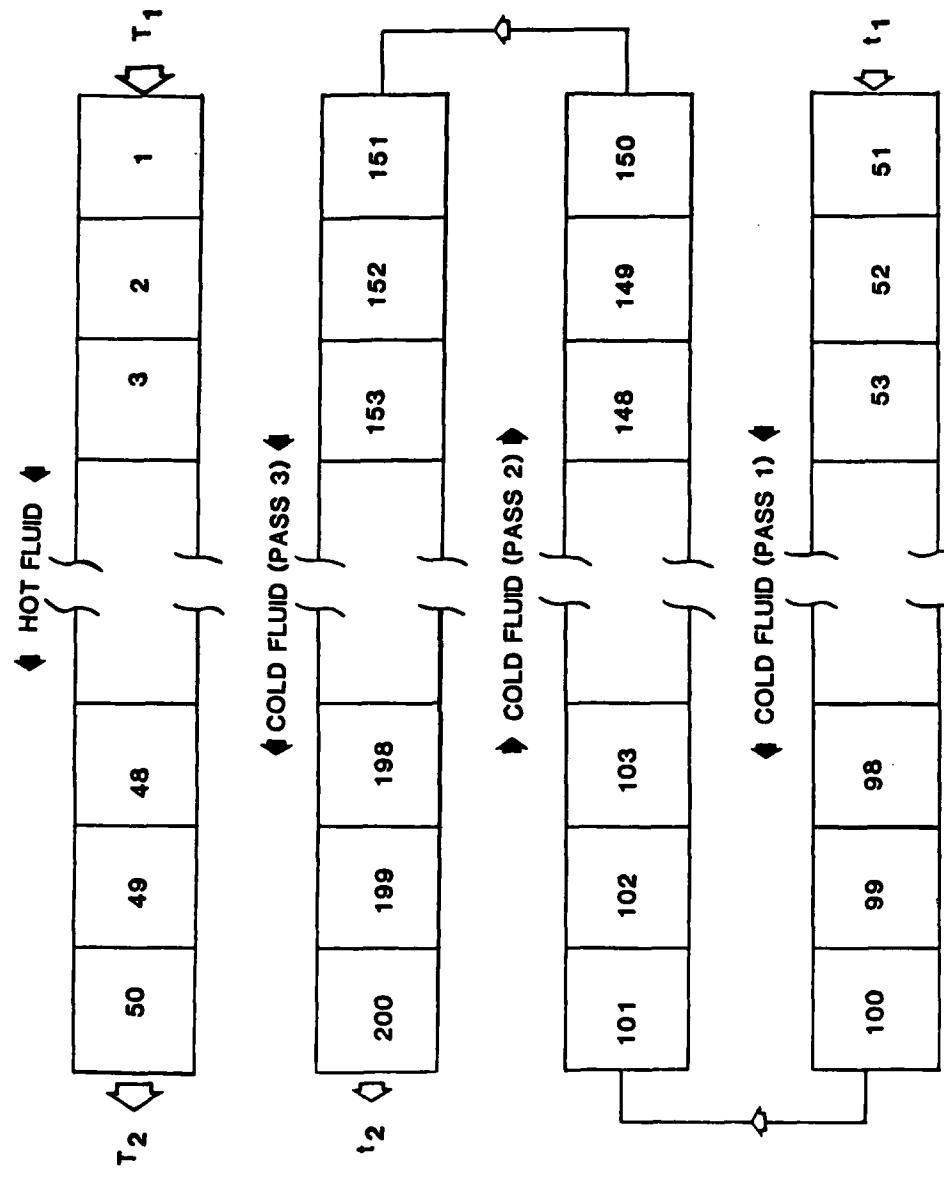


Figure 4.2 Nodal Arrangement for the 1-3:2P Exchanger

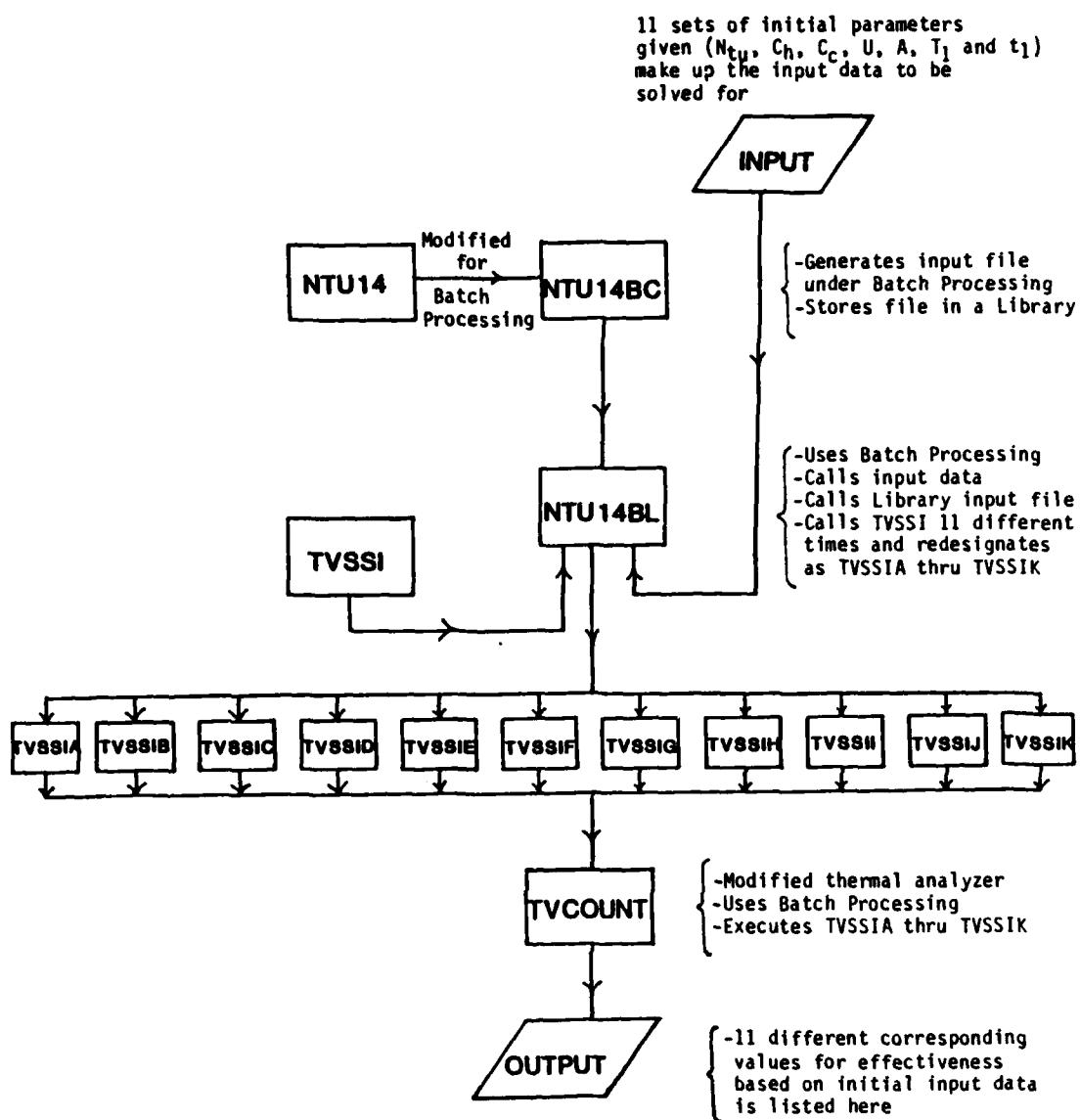


Figure 4.3 Computer Systems Flow Chart for 1-4 Exchanger Model

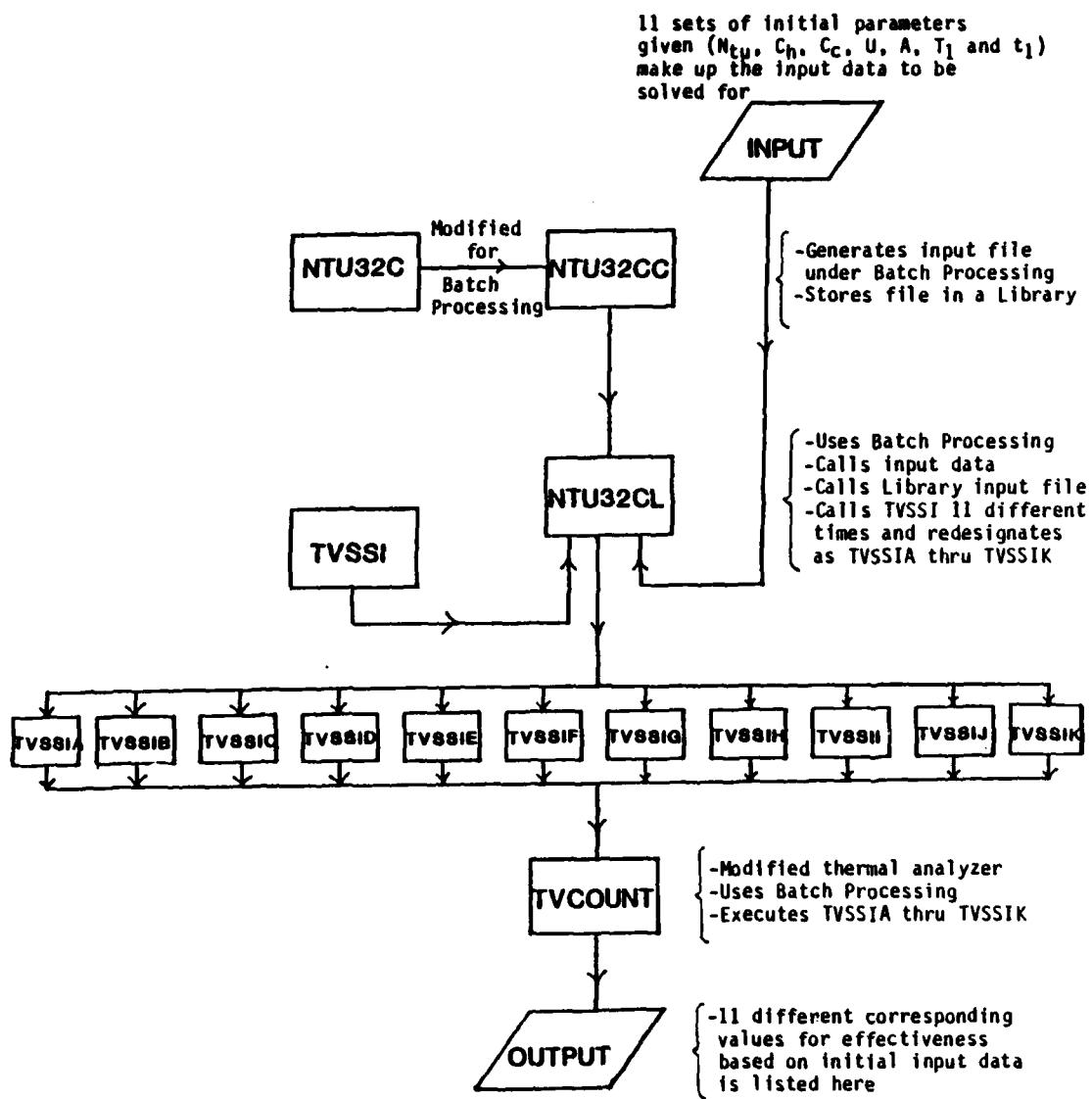


Figure 4.4 Computer Systems Flow Chart for 1-3:2C Exchanger Model

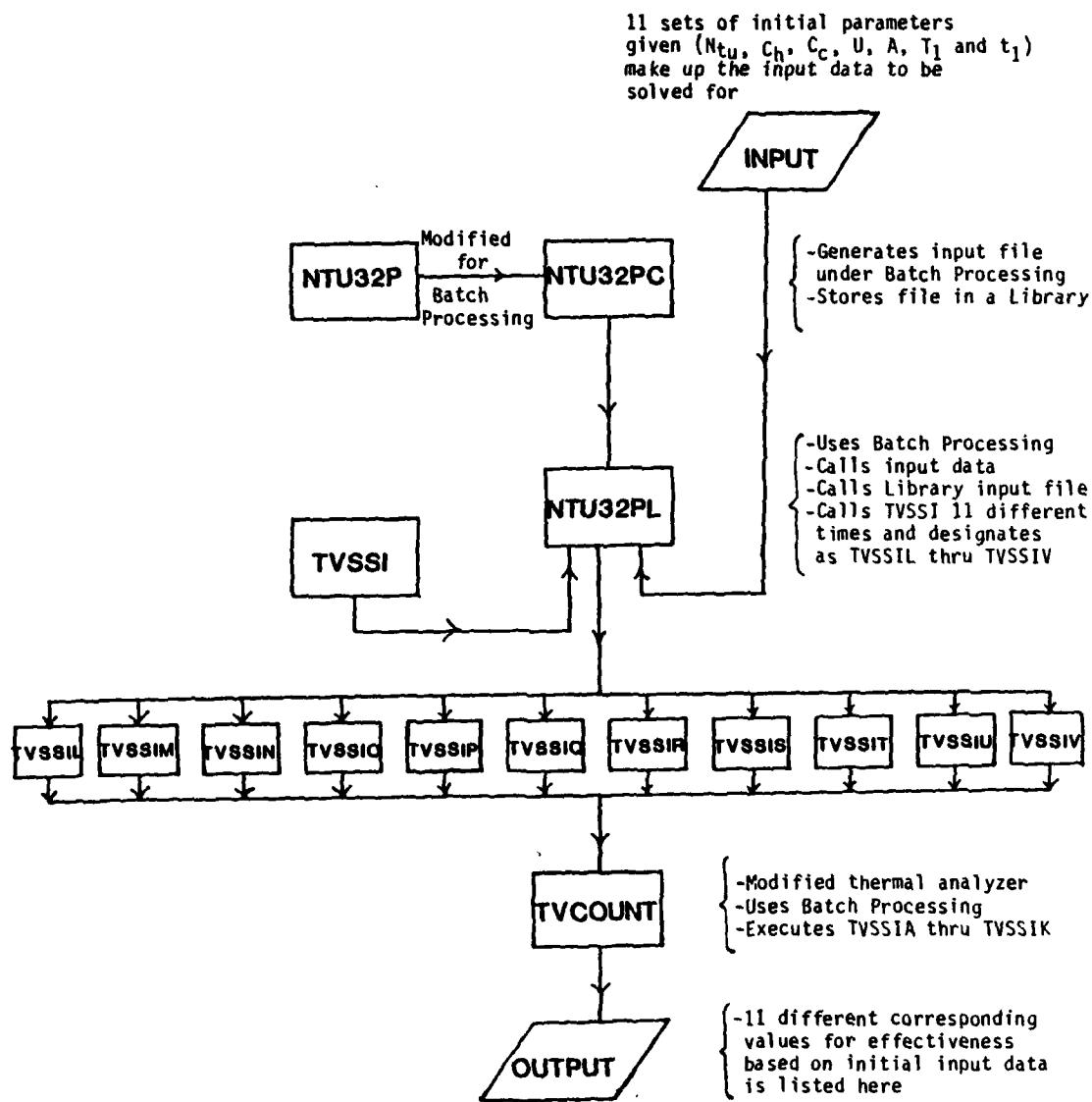


Figure 4.5 Computer Systems Flow Chart for 1-3:2P Exchanger Model

EFFECTIVENESS VS. NTU FOR R=0.2

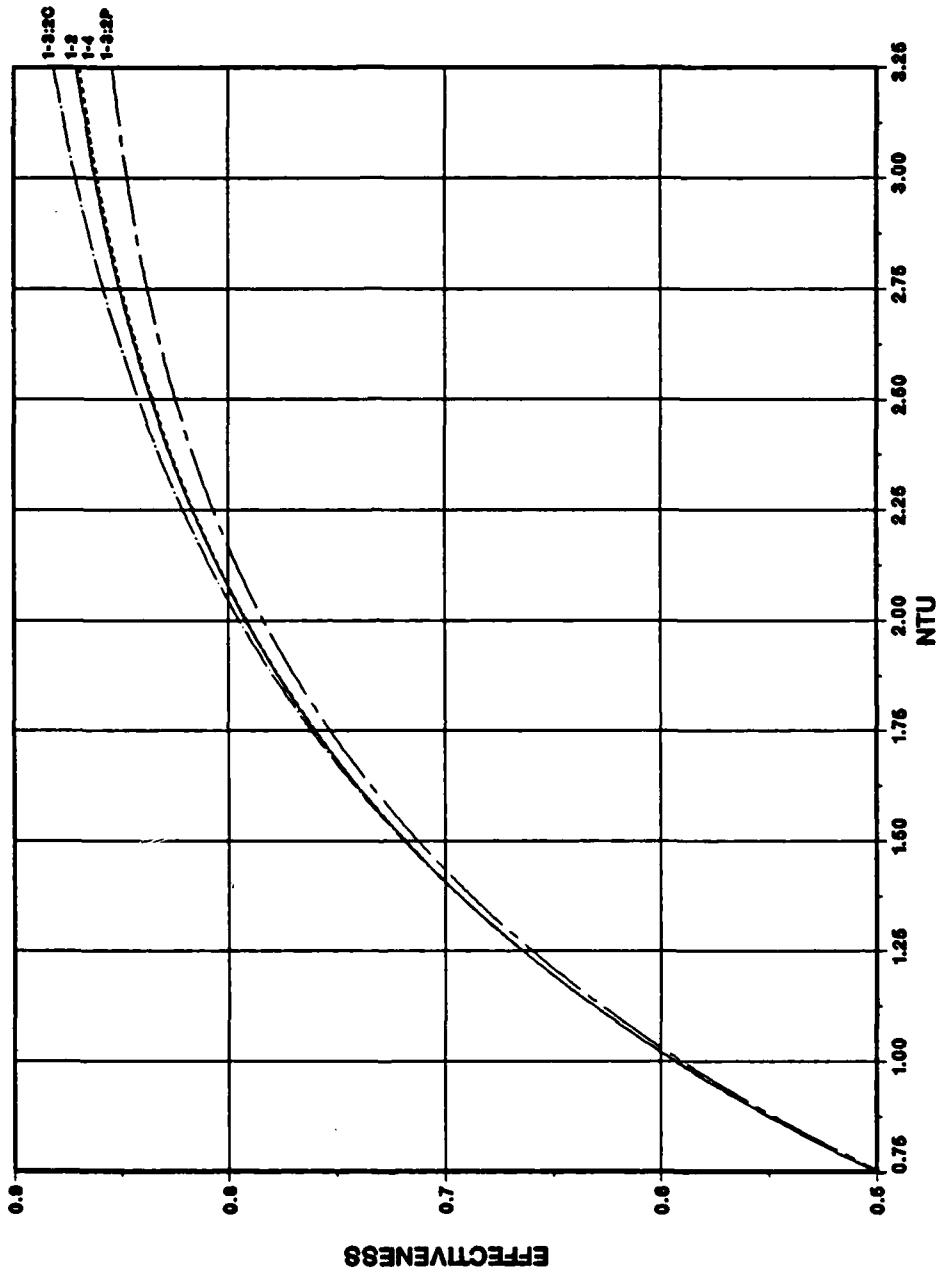


Figure 4.6 Comparison of Analytical (1-2 and 1-4) to Computer Results (1-3:2C and 1-3:2P) at  $R = .2$

### EFFECTIVENESS VS. NTU FOR R=0.5

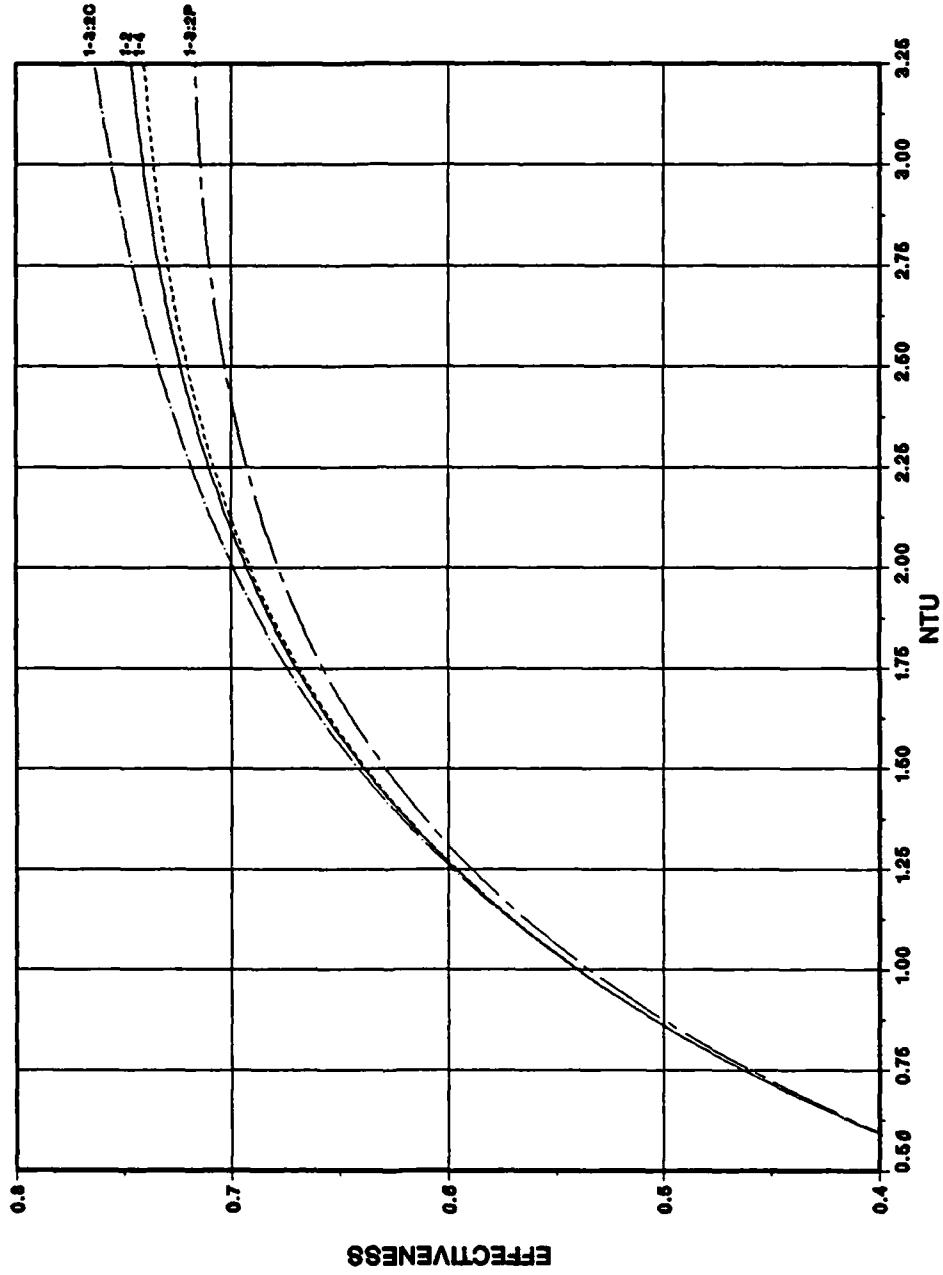


Figure 4.7 Comparison of Analytical (1-2 and 1-4) to Computer Results (1-3:2C and 1-3:2P) at  $R = .5$

### EFFECTIVENESS VS. NTU FOR R=1.0

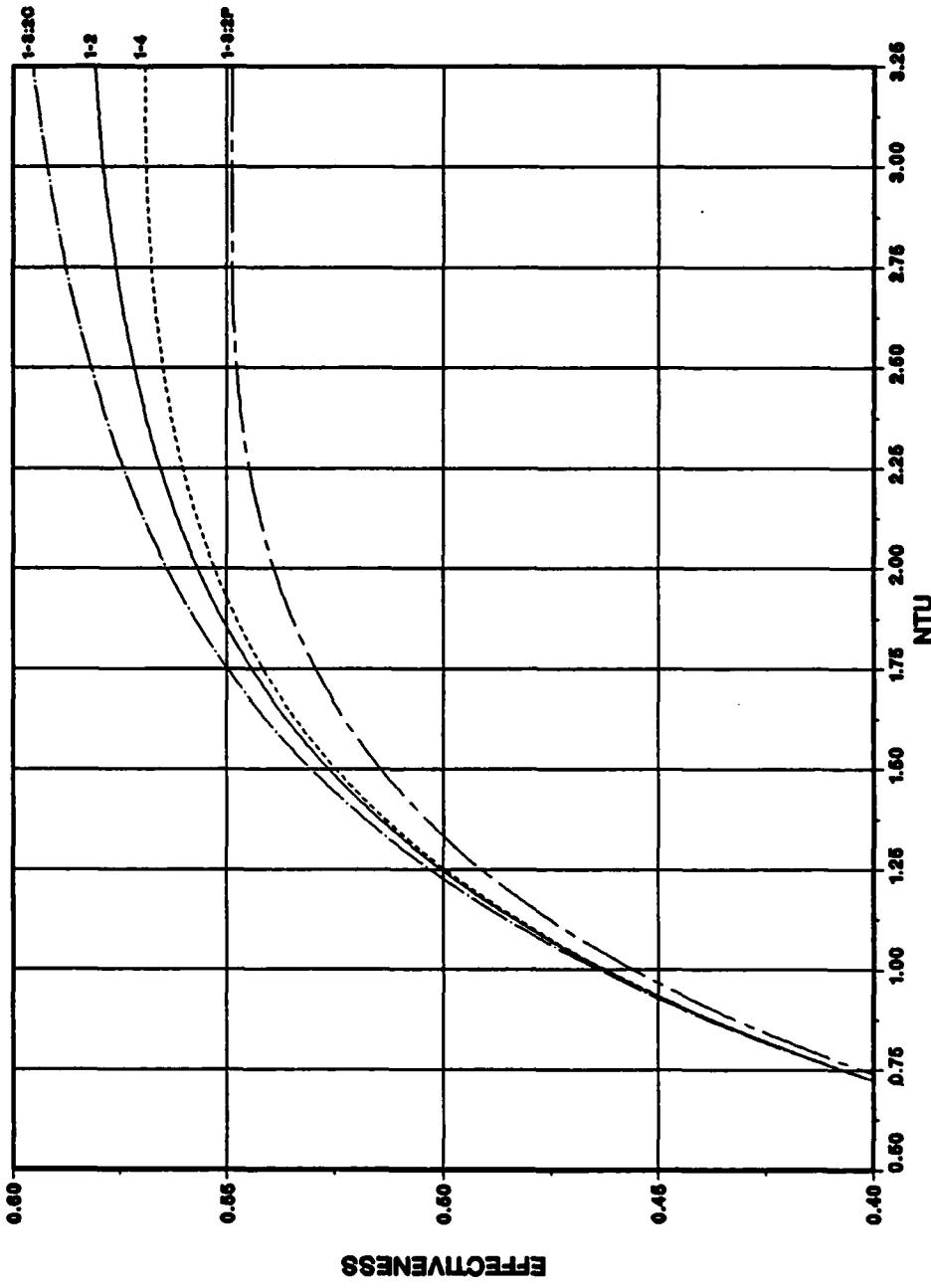


Figure 4.8 Comparison of Analytical (1-2 and 1-4) to Computer Results (1-3:2C and 1-3:2P) at  $R = 1.0$

## V. POLYNOMIAL REGRESSION

### A. DEVELOPMENT OF POLYNOMIAL EQUATIONS

The empirical data obtained for the two 1-3 heat exchangers was designed to cover an extensive range of R values varying from 0.01 to 1.0 in increments of 0.01. As discussed earlier in Section IV, the data obtained at a specific value of R is the computer evaluated result of the effectiveness, for an associated Ntu value. With this accomplished, it then becomes possible to graph separate curves for each of the different R values as shown in Appendices M and N. Through a polynomial regression technique, as discussed in this section, it is also possible to develop implicit equations for the curves with  $\epsilon = f(Ntu, R)$ . It is also apparent from an inspection of the graphical representation of the empirical data in Appendices M and N, that the curves conform to a high degree polynomial. However, further analytical investigation is needed to ascertain the exact order of the polynomial terms. This investigation will not only lead to the order of the polynomial, but to the specific equation for each curve.

By use of polynomial regression, the least-squares method can be readily extended to best fit the data to the  $m^{\text{th}}$ -degree for the polynomial

$$y = A_0 + A_1x + A_2x^2 + \dots + A_mx^m \quad (53)$$

with the error defined by

$$e_i = D_i - y_i = D_i - A_0 - A_1 x_i - A_2 x_i^2 - \dots - A_m x_i^m$$

where  $D_i$  represents the empirical data value corresponding to  $x_i$ ,  $x_i$  being free of error.

The objective is to minimize the sum of the squares of the residuals,  $S_r$ ,

$$S_r = \sum_{i=1}^m e_i^2 = \sum (D_i - A_0 - A_1 x_i - A_2 x_i^2 - \dots - A_m x_i^m)^2 \quad (54)$$

Because at a minimum, the partial derivatives  $\partial S_r / \partial A_0$ ,  $\partial S_r / \partial A_1 \dots \partial S_r / \partial A_m$  vanish, after taking the derivative of  $S_r$  with respect to each of the coefficients of the polynomial, it can be seen that

$$\frac{\partial S_r}{\partial A_0} = 0 = -2 \sum (D_i - A_0 - A_1 x_i - A_2 x_i^2 - \dots - A_m x_i^m)$$

$$\frac{\partial S_r}{\partial A_1} = 0 = -2 \sum x_i (D_i - A_0 - A_1 x_i - A_2 x_i^2 - \dots - A_m x_i^m)$$

$$\frac{\partial S_r}{\partial A_2} = 0 = -2 \sum x_i^2 (D_i - A_0 - A_1 x_i - A_2 x_i^2 - \dots - A_m x_i^m)$$

.

.

.

$$\frac{\partial S_r}{\partial A_m} = 0 = -2 \sum x_i^m (D_i - A_0 - A_1 x_i - A_2 x_i^2 - \dots - A_m x_i^m)$$

Then by dividing by -2 and rearranging we obtain

$$A_0 M + A_1 \sum x_i + A_1 x_i^2 + \dots + A_m \sum x_i^m = \sum D_i$$

$$A_0 \sum x_i + A_1 \sum x_i^2 + A_2 \sum x_i^3 + \dots + A_m \sum x_i^{m+1} = \sum x_i D_i$$

$$A_0 \sum x_i^2 + A_1 \sum x_i^3 + A_2 \sum x_i^4 + \dots + A_m \sum x_i^{m+2} = \sum x_i^2 D_i$$

$$\begin{matrix} \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \end{matrix}$$

$$A_0 \sum x_i^m + A_1 \sum x_i^{m+1} + A_2 \sum x_i^{m+2} + \dots + A_m \sum x_i^{2m} = \sum x_i^m D_i$$

where all summations are from  $i=1$  through  $n$ . All of the foregoing  $m+1$  equations are linear and have  $m+1$  unknowns:

$A_0, A_1, A_2, \dots, A_m$ . The coefficients of the unknowns can be calculated directly from the observed data. Thus, the problem of determining a least-squares polynomial of degree  $m$  is equivalent to solving a system of  $m+1$  simultaneous linear equations. Putting the equations in matrix form yields

$$\left[ \begin{array}{cccccc} N & \sum x_i & \sum x_i^2 & \sum x_i^3 & \dots & \sum x_i^m \\ \sum x_i & \sum x_i^2 & \sum x_i^3 & \sum x_i^4 & \dots & \sum x_i^{m+1} \\ \sum x_i^2 & \sum x_i^3 & \sum x_i^4 & \sum x_i^5 & \dots & \sum x_i^{m+2} \\ \cdot & \cdot & \cdot & \cdot & & \cdot \\ \cdot & \cdot & \cdot & \cdot & & \cdot \\ \cdot & \cdot & \cdot & \cdot & & \cdot \\ \sum x_i^m & \sum x_i^{m+1} & \sum x_i^{m+2} & \sum x_i^{m+3} & \dots & \sum x_i^{2m} \end{array} \right] [A] = \left[ \begin{array}{c} \sum D_i \\ \sum x_i D_i \\ \sum x_i^2 D_i \\ \cdot \\ \cdot \\ \cdot \\ \sum x_i^m D_i \end{array} \right]$$

[Ref. 15: pp. 302-309 and Ref. 16: 468-474].

From this point on, one finds that it is best to use a computer to assist in solving the simultaneous equations and this will also help alleviate any ill-conditioning that may otherwise occur. An existing "curvefit" program available through NON-IMSL [Ref. 16] and found in Appendix P was used although some modifications were made to the original program to best accommodate the goals of this work.

To determine the order of polynomial that should eventually be used, one increases the degree of the approximating polynomial as long as there is a statistically significant decrease in the variance  $\sigma^2$ , which is computed by

$$\sigma^2 = \frac{\sum e_i^2}{N - m - 1} \quad (55)$$

In otherwords, the selection of the optimum degree polynomial is contingent upon a decreasing variance and once the variance begins to increase, the degree of the polynomial becomes too high. For all cases, it was found that the  $\epsilon - N_{tu}$  developed curves are of the 5th order.

As shown in Figures 5.1 and 5.2 the computed values of effectiveness vs.  $N_{tu}$  for  $R = 0.1, 0.5$  and  $1.0$  for both flow arrangements, (1-3:2P) and (1-3:2C), have been graphed and fitted by a 5th degree polynomial. Because all computed values for effectiveness follow a predictable trend, only a sample of the data covering the whole range of

values of R have been shown. It is clear that the graphic interpretation strongly backs what is known analytically from the polynomial regression technique. Where the relationship for  $\epsilon = f(N_{tu}, R)$  is found explicitly from

$$\epsilon = A_5 N_{tu}^5 + A_4 N_{tu}^4 + A_3 N_{tu}^3 + A_2 N_{tu}^2 + A_1 N_{tu} + A_0 \quad (56)$$

while the corresponding coefficients  $A_5, A_4, A_3, A_2, A_1$ , and  $A_0$  relating to a specific value of R are found in Tables 2 and 3 for the (1-3:2P) and (1-3:2C) configurations. An example of how to use this equation in a heat exchanger problem now follows.

#### B. NUMERICAL EXAMPLE

Consider a heat exchanger containing  $400 \text{ m}^2$  of ( $A = 400 \text{ m}^2$ ) of surface and operating with an overall heat transfer coefficient of  $80 \text{ W/m}^2\text{°C}$ . Cold fluid at a capacity rate of  $10,000 \text{ W/°C}$  enters the exchanger at  $60^\circ\text{C}$ . Hot fluid at a capacity rate of  $20,000 \text{ W/°C}$  enters the exchanger at  $200^\circ\text{C}$ .

##### 1. Find

The effectiveness ( $\epsilon$ ) and compute the hot and cold fluid outlet temperatures for the (1-3:2C) shell tube pass arrangement.

##### 2. Assumptions

- 1) Negligible heat loss to surroundings and kinetic and potential energy changes.

2) Constant thermal and fluid properties for both fluids.

3. Analysis

Here  $C_c = 10,000 \text{ W}/\text{°C}$  and  $C_h = 20,000 \text{ W}/\text{°C}$  this makes  $R = C_{\min}/C_{\max} = C_c/C_h = (T_1 - T_2)/(t_2 - t_1)$   
 $10,000/20,000 = 0.5.$

and  $N_{tu} = UA/C_c$

$$= 80 (400)/(10,000) = 3.2$$

First, go to Table 2 (page 81) for the (1-3:2C) arrangement with  $R = 0.5$  and find the coefficients

$$A_0 = 0.1294 \times 10^{-2}$$

$$A_1 = 0.98120$$

$$A_2 = -0.66161$$

$$A_3 = 0.27938$$

$$A_4 = -0.66456 \times 10^{-1}$$

$$A_5 = 0.66069 \times 10^{-2}$$

Then apply equation (56) for  $N_{tu} = 3.2$

$$\epsilon = A_5 N_{tu}^5 + A_4 N_{tu}^4 + A_3 N_{tu}^3 + A_2 N_{tu}^2 + A_1 N_{tu} + A_0 \quad (56)$$

$$\epsilon = 0.769$$

Because  $C_C < C_h$

$$\epsilon = \frac{t_2 - t_1}{T_1 - t_1}$$

and with  $T_1 - t_1 = 200 - 60 = 140^\circ\text{C}$

$$\begin{aligned} t_2 - t_1 &= \epsilon(T_1 - t_1) \\ &= 0.769 (140) \\ &= 107.7^\circ\text{C} \end{aligned}$$

Finally, the outlet cold fluid temperature  $t_2$  is

$$\begin{aligned} t_2 &= 107.7 + t_1 \\ &= 107.7 + 60 \\ &= 167.7^\circ\text{C} \end{aligned}$$

and the fluid temperature,  $T_2$  is easily found

$$R = \frac{T_1 - T_2}{t_2 - t_1} = 0.5$$

$$\begin{aligned} T_2 &= T_1 - 0.5 (t_2 - t_1) \\ &= 200 - 0.5 (t_2 - t_1) \\ &= 146.1^\circ\text{C} \end{aligned}$$

#### 4. Observations

The primary observation made here is that by using the 5th order polynomial equation (56) with the appropriate coefficients found in Table 2 or 3, an accurate value for

effectiveness can be found thus allowing one to solve for many more unknown values or parameters of the heat exchanger (i.e., hot and cold outlet temperatures).

The other observation that is to be made is that when comparing the value for effectiveness computed here against the value for a 1-2 or 1-4 exchanger (0.745 and 0.740 respectively) under the same conditions, one finds that there is a significant difference in exchanger performance as a function of odd or even tube passes and that the 1-3:2C arrangement has a higher effectiveness than either the 1-2 or 1-4 arrangement. From inspection of the curves for the 1-3:2P exchanger at Figure N-1 or N-6 with  $R = 0.5$  and  $N_{tu} = 3.2$  an approximate value of  $\epsilon = .715$  is obtained. It is clear that this is also less than that of 1-3:2C arrangement. Therefore, it is evident that the 1-3:2C exchanger out-performs not only the 1-2 and 1-4 arrangement but also its counterpart the 1-3:2P exchanger by 3.1%, 3.8% and 7.0% respectfully.

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
DATA POINTS FIT BY 6TH ORDER POLYNOMIAL

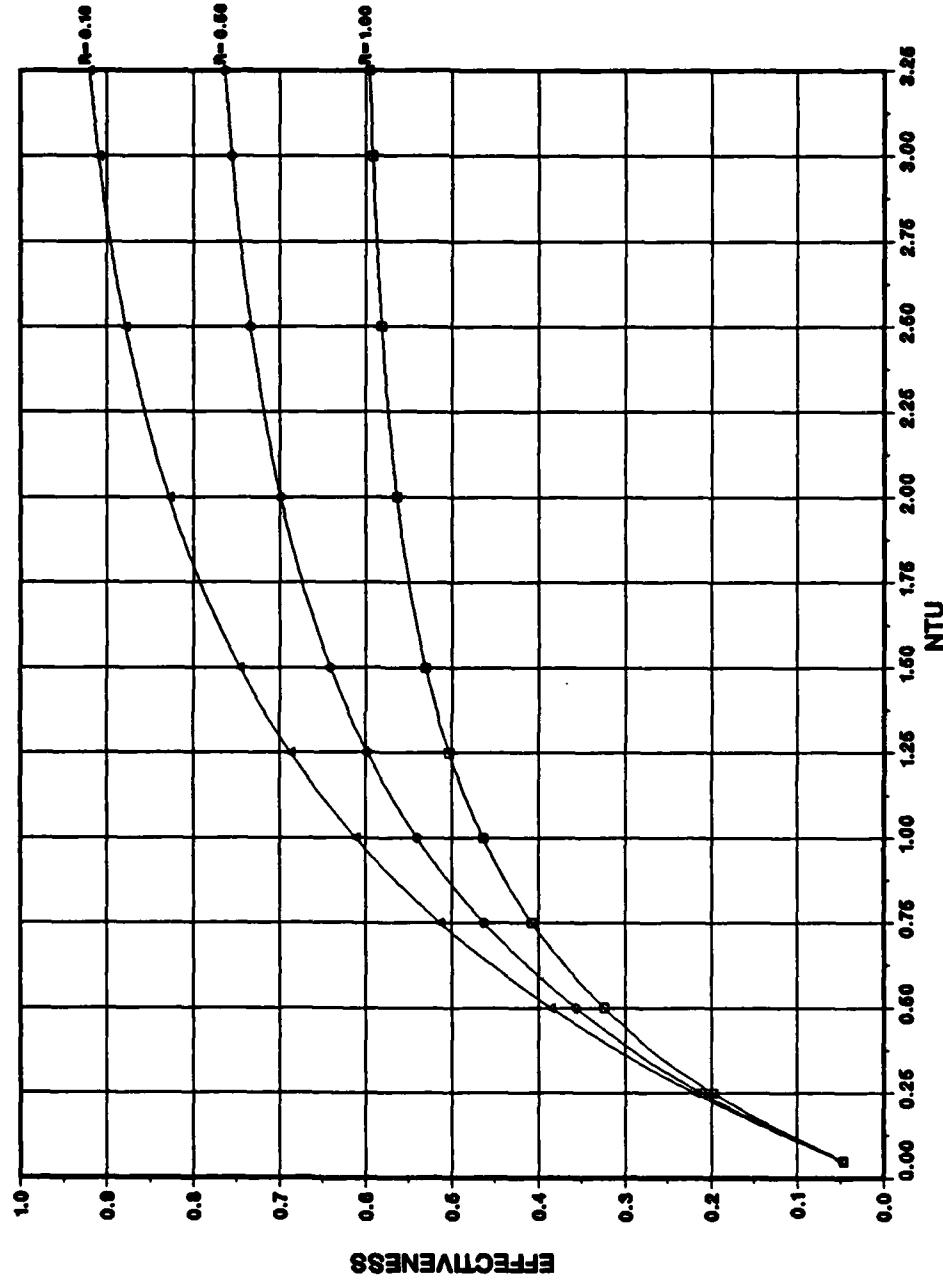


Figure 5.1 1-3:2C Data Fit by a 5th Order Polynomial

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
DATA POINTS FIT BY 6TH ORDER POLYNOMIAL

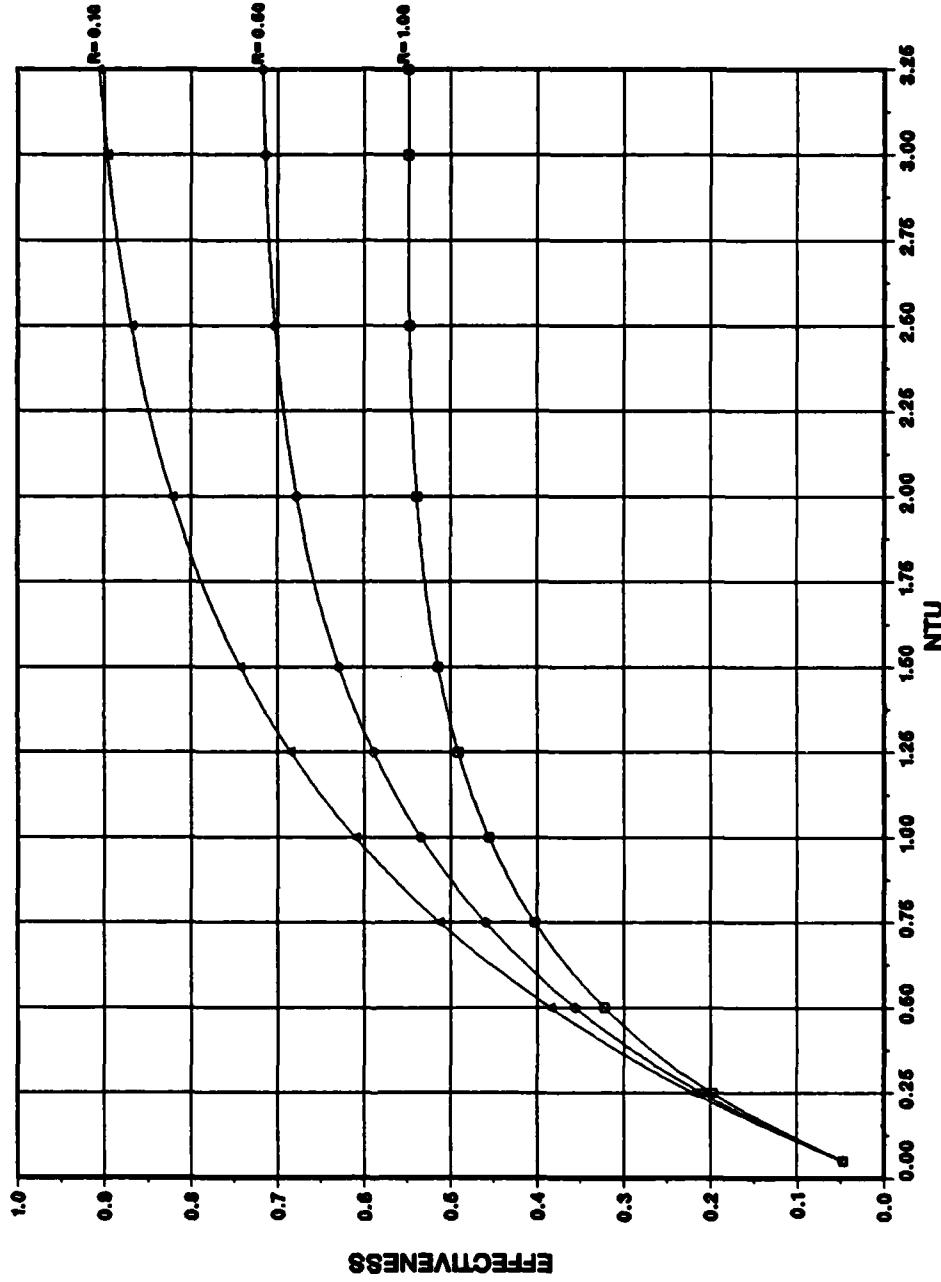


Figure 5.2 1-3:2P Data Fit by a 5th Order Polynomial

TABLE 2  
1-3:2C COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.01	-1.54650	1.00630	-0.51115	0.16418	-0.31787	0.27562
.02	1.09620	0.98977	-0.48530	0.14498	-0.25435	0.19915
.03	0.23928	0.99515	-0.49950	0.15565	-0.28857	0.23943
.04	-0.23948	0.99772	-0.50794	0.16165	-0.30646	0.25908
.05	0.70811	0.99188	-0.50226	0.15792	-0.29488	0.24608
.06	0.36469	0.99329	-0.50845	0.16207	-0.30594	0.25657
.07	0.17636	0.99546	-0.51698	0.16867	-0.32725	0.28161
.08	0.62843	0.99167	-0.51309	0.16524	-0.31420	0.26475
.09	0.41140	0.99354	-0.52158	0.17208	-0.33695	0.29217
.10	0.47085	0.99198	-0.52163	0.17131	-0.33137	0.28264
.11	0.68979	0.99116	-0.52589	0.17555	-0.34744	0.30429
.12	0.53544	0.99173	-0.53101	0.17938	-0.35920	0.31765
.13	0.38892	0.99173	-0.53462	0.18182	-0.36561	0.32373
.14	0.76975	0.98852	-0.53226	0.17971	-0.35696	0.31186
.15	0.60634	0.98885	-0.53636	0.18229	-0.36288	0.31623
.16	0.40649	0.98999	-0.54245	0.18673	-0.37606	0.33043
.17	0.73099	0.98713	-0.54081	0.18557	-0.37211	0.32587
.18	0.46417	0.98875	-0.54820	0.19109	-0.38883	0.34412
.19	0.90075	0.98061	-0.52634	0.16874	-0.30036	0.22473

TABLE 2 (cont'd)  
1-3:2C COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.20	0.711140	0.98703	-0.55346	0.19530	-0.40158	0.35808
.21	0.64893	0.98700	-0.5575	0.19879	-0.41317	0.37222
.22	0.56702	0.98762	-0.56291	0.20258	-0.42439	0.38422
.23	0.71515	0.98611	-0.56423	0.20381	-0.42850	0.38931
.24	0.61725	0.98692	-0.56969	0.20786	-0.44087	0.40315
.25	0.57119	0.98653	-0.57241	0.20960	-0.44493	0.40637
.26	0.79180	0.98547	-0.57511	0.21210	-0.45381	0.41785
.27	0.69607	0.98591	-0.58041	0.21654	-0.46901	0.43663
.28	0.62722	0.98553	-0.58350	0.21893	-0.47655	0.44549
.29	0.79437	0.98544	-0.58911	0.22410	-0.49504	0.46888
.30	0.67158	0.98625	-0.59584	0.23115	-0.52608	0.51644
.31	0.74865	0.98380	-0.59141	0.22464	-0.49281	0.46289
.32	0.92219	0.98226	-0.59256	0.22572	-0.49644	0.46752
.33	0.82224	0.98264	-0.59730	0.22942	-0.50820	0.48114
.34	0.88180	0.98243	-0.60118	0.23262	-0.51887	0.49414
.35	0.10262	0.98083	-0.60162	0.23267	-0.51751	0.49105
.36	0.99038	0.98036	-0.60424	0.23460	-0.52330	0.49765
.37	0.91970	0.98036	-0.60770	0.23702	-0.53023	0.50506
.38	1.08830	0.97884	-0.60875	0.23792	-0.53284	0.50798
.39	1.11470	0.97855	-0.61207	0.24047	-0.54058	0.51644

TABLE 2 (cont'd)  
1-3:2C COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.40	1.17740	0.97771	-0.61372	0.24125	-0.54130	0.51566
.41	1.21820	0.97688	-0.61606	0.24330	-0.54828	0.52441
.42	1.13560	0.97705	-0.61993	0.24606	-0.55618	0.53262
.43	1.17390	0.97657	-0.62278	0.24826	-0.56290	0.54017
.44	1.25770	0.97508	-0.62296	0.24798	-0.56028	0.53543
.45	1.30410	0.97449	-0.62533	0.24946	-0.56329	0.53694
.46	1.20250	0.97496	-0.63022	0.25345	-0.57673	0.55343
.47	1.39770	0.97310	-0.63045	0.25368	-0.57704	0.55347
.48	1.45510	0.97221	-0.63176	0.25421	-0.57681	0.55130
.49	2.63160	0.94641	-0.77159	0.35867	-0.89176	0.90142
.50	1.29400	0.98102	-0.66161	0.27938	-0.66456	0.66069
.51	1.46920	0.97076	-0.63972	0.26012	-0.59397	0.56948
.52	1.50140	0.97079	-0.64398	0.26376	-0.60667	0.58553
.53	1.54710	0.96986	-0.64538	0.26447	-0.60718	0.58416
.54	1.56460	0.96971	-0.64922	0.26778	-0.61866	0.59853
.55	1.46430	0.97013	-0.65396	0.27164	-0.63151	0.61405
.56	1.65860	0.96803	-0.65281	0.27025	-0.62482	0.60403
.57	1.68550	0.96775	-0.65632	0.27325	-0.63507	0.61674
.58	1.63300	0.96751	-0.65932	0.27553	-0.64200	0.62444

TABLE 2 (cont'd)  
1-3:2C COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.59	1.77010	0.96636	-0.66068	0.27651	-0.64435	0.62630
.60	1.85570	0.96466	-0.66124	0.27649	-0.64120	0.61866
.61	1.76480	0.96543	-0.66567	0.28014	-0.65464	0.63700
.62	1.74620	0.96535	-0.66936	0.28319	-0.66476	0.64910
.63	1.80880	0.96455	-0.67135	0.28478	-0.66975	0.65496
.64	1.72290	0.96471	-0.67523	0.28786	-0.67963	0.66649
.65	1.85600	0.96393	-0.67750	0.28960	-0.68455	0.67144
.66	1.81240	0.96311	-0.67878	0.29033	-0.68584	0.67199
.67	1.82510	0.96293	-0.68231	0.29330	-0.69586	0.68424
.68	1.87880	0.96231	-0.68466	0.29518	-0.70174	0.69110
.69	1.88370	0.96227	-0.68863	0.29860	-0.71344	0.70539
.70	1.96850	0.96109	-0.68955	0.29922	-0.71473	0.70618
.71	1.98700	0.96047	-0.69161	0.30065	-0.71834	0.70940
.72	2.00210	0.96018	-0.69436	0.30265	-0.72405	0.71533
.73	1.95690	0.95987	-0.69723	0.30501	-0.73180	0.72461
.74	2.08210	0.95882	-0.69884	0.30640	-0.73620	0.72971
.75	2.00140	0.95886	-0.70230	0.30908	-0.74462	0.73945
.76	2.07320	0.95796	-0.70372	0.31004	-0.74680	0.74106
.77	2.14030	0.95700	-0.70520	0.31115	-0.74972	0.74373
.78	2.10090	0.95754	-0.71036	0.31567	-0.76577	0.76409

TABLE 2 (cont'd)  
1-3;2C COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.79	2.17470	0.95647	-0.71149	0.31638	-0.76691	0.76409
.80	2.22410	0.95612	-0.71500	0.31955	-0.77811	0.77833
.81	2.29050	0.95454	-0.71442	0.31881	-0.77439	0.77261
.82	2.17700	0.95505	-0.71882	0.32224	-0.78513	0.78474
.83	2.36540	0.95352	-0.71902	0.32235	-0.78494	0.78416
.84	2.25330	0.95366	-0.72313	0.32610	-0.79853	0.80160
.85	2.31490	0.95324	-0.72564	0.32788	-0.80318	0.80576
.86	2.33970	0.95252	-0.72764	0.32960	-0.80894	0.81289
.87	2.42210	0.95135	-0.72849	0.33023	-0.81036	0.81397
.88	2.46190	0.95078	-0.73069	0.33197	-0.81554	0.81943
.89	2.50950	0.94972	-0.73156	0.33251	-0.81640	0.81960
.90	2.55370	0.94902	-0.73371	0.33440	-0.82268	0.82712
.91	2.48350	0.94906	-0.73726	0.33739	-0.83276	0.83937
.92	2.62780	0.94803	-0.73861	0.33847	-0.83576	0.84233
.93	2.53660	0.94826	-0.74226	0.34133	-0.84485	0.85293
.94	2.62050	0.94709	-0.74336	0.34240	-0.84835	0.85688
.95	2.63490	0.94638	-0.74494	0.34352	-0.85120	0.85945
.96	2.70740	0.94547	-0.74656	0.34495	-0.85586	0.86503
.97	2.72560	0.94513	-0.74924	0.34722	-0.86335	0.87396

TABLE 2 (cont'd)  
1-3:2C COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.98	2.75280	0.94473	-0.75178	0.34931	-0.86995	0.88147
.99	2.79380	0.94417	-0.75421	0.35148	-0.87737	0.89055
1.0	2.77220	0.94336	-0.75536	0.35222	-0.87876	0.89109

TABLE 3  
1-3:2P COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.01	-1.53750	1.00620	-0.51077	0.16346	-0.31456	0.27066
.02	1.11580	0.98955	-0.48504	0.14443	-0.25245	0.19708
.03	0.26058	0.99459	-0.49839	0.15419	-0.28333	0.23299
.04	-0.14339	0.99665	-0.50600	0.15936	-0.29827	0.24901
.05	0.71311	0.99151	-0.50132	0.15581	-0.28564	0.23286
.06	-0.76150	0.99957	-0.51965	0.16930	-0.32915	0.28450
.07	0.00791	0.99690	-0.52063	0.17043	-0.33265	0.28805
.08	0.53649	0.99321	-0.51784	0.16820	-0.32501	0.27915
.09	0.45711	0.99282	-0.52061	0.16963	-0.32731	0.27957
.10	0.32341	0.99298	-0.52472	0.17231	-0.33459	0.28716
.11	0.63371	0.99174	-0.52796	0.17532	-0.34560	0.30175
.12	0.44811	0.99423	-0.53763	0.18264	-0.36872	0.32827
.13	0.40379	0.99141	-0.53466	0.17935	-0.35466	0.30842
.14	0.80291	0.98808	-0.53222	0.17711	-0.34561	0.29604
.15	0.55870	0.98956	-0.53929	0.18226	-0.36119	0.31312
.16	0.39008	0.99034	-0.54496	0.18651	-0.37453	0.32851
.17	0.61833	0.98887	-0.54674	0.18791	-0.37882	0.33344
.18	0.37408	0.99011	-0.55323	0.19272	-0.39372	0.35028
.19	0.44322	0.98934	-0.55579	0.19446	-0.39841	0.35493

TABLE 3 (cont'd)  
1-3:2P COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.20	0.65879	0.98800	-0.55782	0.19608	-0.40326	0.36012
.21	0.62161	0.98815	-0.56240	0.19955	-0.41423	0.37300
.22	0.52051	0.98852	-0.56700	0.20282	-0.42390	0.38353
.23	0.70119	0.98663	-0.56742	0.20307	-0.42417	0.38350
.24	0.55381	0.98769	-0.57404	0.20845	-0.44276	0.40697
.25	0.50155	0.98755	-0.57772	0.21100	-0.44987	0.41422
.26	0.75200	0.98606	-0.57918	0.21217	-0.45355	0.41867
.27	0.67777	0.98627	-0.58389	0.21587	-0.46579	0.43366
.28	0.64963	0.98566	-0.58598	0.21689	-0.46711	0.43334
.29	0.89133	0.98422	-0.58768	0.21821	-0.47081	0.43704
.30	0.83692	0.98406	-0.59124	0.22081	-0.47884	0.44648
.31	0.72206	0.98469	-0.59633	0.22452	-0.49011	0.45909
.32	0.88562	0.98325	-0.59765	0.22550	-0.49292	0.46229
.33	0.81793	0.98323	-0.60125	0.22803	-0.50028	0.47027
.34	0.93507	0.98177	-0.60195	0.22811	-0.49868	0.46646
.35	1.02360	0.98140	-0.60574	0.23118	-0.50876	0.47864
.36	1.00020	0.98080	-0.60808	0.23263	-0.51221	0.48161
.37	0.93995	0.98064	-0.61149	0.23506	-0.51930	0.48934
.38	1.03810	0.98003	-0.61416	0.23693	-0.52453	0.49483
.39	1.12760	0.97855	-0.61487	0.23720	-0.52419	0.49327

TABLE 3 (cont'd)  
1-3:2P COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.40	1.11050	0.97929	-0.62069	0.24148	-0.53686	0.50692
.41	1.21970	0.97718	-0.61982	0.24070	-0.53399	0.50348
.42	0.13290	0.97741	-0.62437	0.24433	-0.54598	0.51805
.43	1.23020	0.97606	-0.62536	0.24480	-0.54612	0.51682
.44	1.19100	0.97648	-0.63029	0.24865	-0.55858	0.53160
.45	1.25920	0.97568	-0.63244	0.25010	-0.56229	0.53512
.46	1.16020	0.97599	-0.63644	0.25277	-0.56938	0.54187
.47	1.29110	0.97531	-0.63939	0.25522	-0.57754	0.55186
.48	1.22590	0.97482	-0.64198	0.25705	-0.58269	0.55729
.49	1.26780	0.97436	-0.64490	0.25916	-0.58859	0.56316
.50	0.88037	0.98069	-0.66207	0.27237	-0.63149	0.61370
.51	1.35630	0.97298	-0.64974	0.26273	-0.59899	0.57445
.52	1.39390	0.97251	-0.65249	0.26428	-0.60437	0.57989
.53	1.56550	0.97061	-0.65450	0.26750	-0.61662	0.59746
.54	1.45620	0.97180	-0.65881	0.26958	-0.61975	0.59779
.55	1.39610	0.97129	-0.66116	0.27113	-0.62353	0.60093
.56	1.52440	0.97070	-0.66454	0.27418	-0.63438	0.61487
.57	1.45420	0.97074	-0.66822	0.27690	-0.64250	0.62372
.58	1.51230	0.96951	-0.66891	0.27699	-0.64102	0.62022

TABLE 3 (cont'd)  
1-3:2P COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.59	1.54580	0.96909	-0.67179	0.27925	-0.64826	0.62890
.60	1.29670	0.97304	-0.68701	0.29329	-0.70007	0.69564
.61	1.58550	0.96830	-0.67761	0.28351	-0.66030	0.64118
.62	1.64580	0.96764	-0.68023	0.28565	-0.66713	0.64908
.63	1.69090	0.96705	-0.68272	0.28752	-0.67259	0.65501
.64	1.58780	0.96755	-0.68781	0.29187	-0.68781	0.67424
.65	1.78040	0.96555	-0.68713	0.29094	-0.68275	0.66610
.66	1.69280	0.96574	-0.69099	0.29381	-0.69143	0.67579
.67	1.72500	0.96543	-0.69417	0.29643	-0.70005	0.68609
.68	1.76970	0.96457	-0.69611	0.29800	-0.70500	0.69188
.69	1.78510	0.96428	-0.69931	0.30047	-0.71240	0.69995
.70	1.87300	0.96317	-0.70067	0.30149	-0.71503	0.70233
.71	1.89020	0.96250	-0.70246	0.30255	-0.71702	0.70328
.72	1.92640	0.96210	-0.70572	0.30541	-0.72691	0.71559
.73	1.85070	0.96211	-0.70916	0.30803	-0.73490	0.72452
.74	2.01410	0.96106	-0.71106	0.30976	-0.74079	0.73176
.75	1.91680	0.96092	-0.71407	0.31201	-0.74750	0.73913
.76	1.98610	0.95993	-0.71534	0.31279	-0.74887	0.73960
.77	2.00770	0.95981	-0.71914	0.31610	-0.76034	0.75395
.78	2.05850	0.95917	-0.72159	0.31810	-0.76647	0.76062

TABLE 3 (cont'd)  
1-3:2P COEFFICIENTS

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.79	2.14880	0.95793	-0.72227	0.31840	-0.76612	0.75884
.80	2.14320	0.95825	-0.72763	0.32334	-0.78412	0.78210
.81	2.15380	0.95746	-0.72853	0.32352	-0.78281	0.77874
.82	2.11630	0.95704	-0.73116	0.32558	-0.78896	0.78526
.83	2.27160	0.95557	-0.73167	0.32598	-0.78968	0.78567
.84	2.19230	0.95559	-0.73515	0.32875	-0.79851	0.79585
.85	2.25020	0.95480	-0.73710	0.33036	-0.80345	0.80142
.86	2.28490	0.95444	-0.74010	0.33290	-0.81186	0.81156
.87	2.31220	0.95411	-0.74307	0.33537	-0.81990	0.82103
.88	2.39540	0.95293	-0.74399	0.33602	-0.82109	0.82142
.89	2.36970	0.95284	-0.74728	0.33869	-0.82970	0.83153
.90	2.47650	0.95131	-0.74725	0.33850	-0.82797	0.82834
.91	2.39460	0.95151	-0.75112	0.34167	-0.83821	0.84022
.92	2.53450	0.95060	-0.75308	0.34342	-0.84404	0.84728
.93	2.42020	0.95072	-0.75683	0.34662	-0.85500	0.86088
.94	2.49640	0.94967	-0.75778	0.34718	-0.85550	0.85991
.95	2.55890	0.94885	-0.75948	0.34854	-0.85936	0.86383
.96	2.54640	0.94891	-0.76309	0.35153	-0.86925	0.87578
.97	2.63240	0.94781	-0.76451	0.35284	-0.87333	0.88020

TABLE 3 (cont'd)  
1-3:2P COEFFICIENTS.

R	$A_0 \times 10^3$	$A_1$	$A_2$	$A_3$	$A_4 \times 10^1$	$A_5 \times 10^2$
.98	2.68180	0.94678	-0.76580	0.35409	-0.87773	0.88592
.99	2.69800	0.94670	-0.76845	0.35619	-0.88404	0.89273
1.0	2.63160	0.94641	-0.77159	0.35867	-0.89176	0.90142

## VI. CONCLUSIONS AND RECOMMENDATIONS

### A. CONCLUSIONS

Effectiveness values, though not analytically derived, can be determined for the 1-3:2C and 1-3:2P heat exchangers by utilizing a 5th order polynomial approximation.

Sufficient data now exists to cover a complete range of capacity rate ratios for values of  $N_{tu}$  from 0.0 to 3.25.

From the knowledge of a particular three tube pass heat exchanger arrangement and dimensions, fluid flow rates and temperature extremes,  $N_{tu}$  and  $R$  values may be computed.

Then the effectiveness may be determined using the appropriate coefficients from the tables provided herein.

After the effectiveness is obtained, there are two choices.

- 1) From a knowledge of  $q_{max}$  (see Section III), it is a simple matter to determine the actual heat transfer rate from the postulation that  $q = \epsilon q_{max}$ .
- 2) Both fluid outlet temperatures may be computed since  $q = \omega_c C_{ph}(t_2 - t_1)$ .

It is also apparent from the work done here that the 1-3:2C exchanger effectiveness outperforms that of the 1-2, 1-4 and its counter part, the 1-3:2P exchanger, as  $N_{tu}$  increases. This is true for any and all values of  $R$ . Therefore, because it is possible to determine the effectiveness of a 1-3 exchanger which has a higher effectiveness (the 1-3:2C arrangement) than that of the 1-2, 1-4 and

1-3:2P exchanger particularly at high  $N_{tu}$  levels, the 1-3 exchanger can now be given full consideration in heat exchanger design. This would be especially helpful where three tube passes could alleviate a configuration problem.

#### B. RECOMMENDATIONS

The following recommendations are provided for possible follow-on projects of a similar nature.

- Continue study of the  $\epsilon - N_{tu}$  method for the 1-5 heat exchangers.
- Investigate the possibility of using a linear approximation from the 1-3 data to find a periodicity of R values at which to develop a 1-5 data base.
- Develop interactive software to be used on a microcomputer that contains both the 1-3 and 1-5 polynomial approximation coefficients. The procedure of entering the values for  $N_{tu}$ , R, and the type of heat exchanger when asked to do so in a menu-driven fashion so that effectiveness values can be readily obtained is self-evident.
- After results of 1-5 exchanger analyses are complete, investigate the effectiveness for both the 1-3 and 1-5 heat exchangers experimentally to confirm or refute the theoretical work done here.

## APPENDIX A

```

READ(4,501) NONODS,NOCT,NOHTR,INPTAG
READ(4,505) ERRALPHA,MNITS,BETA(I),TOLD(1)
MAXNT = TABS(MNITS)
NIT = 0
IF(BETA(1) .NE. 0.) GO TO 1010
READ(4,502) (BETA(I),I=1,N)
GO TO 1030
1010 DO 1020 I=2,N
1020 BETA(I) = BETA(I-1)

C 1030 DO 15 I=1,10
INI = INPTAG(I)
IF(INI .EQ. 17) 6,18,1
6 GO TO 10 2,3,7,16
NTCIN = 18*NTCOF
1 READ(4,502) (TCOEF(K), K=1,NTCIN)
GO TO 15
2 READ(4,502) (CONTMP(K), K=1,NCT)
GO TO 15
3 READ(4,501) NOCONT
3 READ(4,502) (HTR(K), K=1,36)
GO TO 15
7 DO 9 L= 1,N
ITAG(1,0) = 0
READ(4,504) (TCOEF(M), M=1, 9) K=1,9)
READ(4,502) (COEF(8),7,10)
IF(NT-9 .GT. 15) 7,10,9
710 DO 715 K=10,NT,9
ITAG(K+9) = 0
KE = K+8
READ(4,503) (ITAG(M), M=K ,KE)
715 READ(4,502) (COEF(M) , M=K ,KE)
8 WRITE(3,556)(ITAG(KK),KK=1,30)
9 CONTINUE
ENDFILE 1
REWIND 1
GO TO 15
10 READ(4,502) EX
10 GO TO 15
12 IF(TOLD(1) .NE. 0.) (TOLD(K), K=1,N)
12 READ(4,502) (TOLD(K), K=1,N)
GO TO 15
1201 DO 1202 L=2,N
1202 TOLD(L) = TOLD(L-1)
14 K2 = 18*NTMPHT
READ(4,502) (TMPHT(K), K=1,K2)

```

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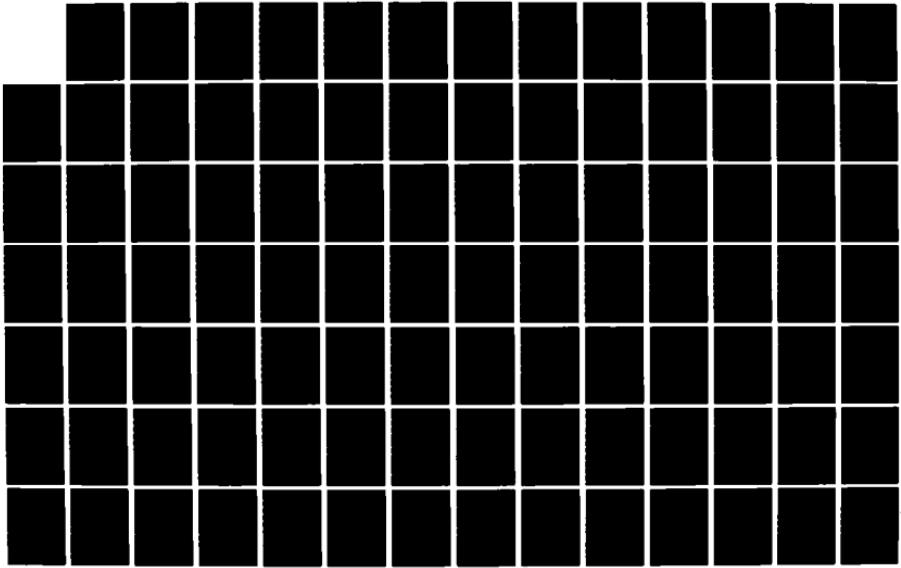
808   GO TO 15      BTUCRV
     GO TO 15      BTUCRV
809   READ(4,502)  TMPCRV
     GO TO 15      TMPCRV
810   WRITE(8,533) INI
     STOP
811   READ(4,502)  TIMCO
15    CONTINUE
17    CALL TVPAGE(0,TITLE)
     CALL TVSOUT(N,1,TOLD,TITLE)
C
     WRITE(3,551) TITLE
     WRITE(3,552) N,NCT,NOHTRS,NOEXP,NOCASE,NTCOEF,NODCFH,NTMPHT,NONODS,
1     NOCT,NOHTR,MNITS
     WRITE(3,553) INPTAG,ERR,ALPHA
     WRITE(3,554) N,HEAD,(BETA(I),I=1,N)
     HEAD=HEAD1
     WRITE(3,554) N,HEAD,(TOLD(I),I=1,N)
     WRITE(3,555) CONTMP(I),I=1,NCT}
20    IF(NOHTRS) 24,24,21
21    CALL TVSHTR(NOHTRS,HTR,CASBTU,NOCONT,TOLD,NODCFH)
24    DO 107 NOD=N
     DO 25 I=1,NPI
25    A(I)=0
     READ(1) ITAG, COEF
     DO 100 IWD=1,99
     IF(ITAG(IWD).EQ.0) GO TO 105
     NODEI=ITAG(IWD),0
     METHI=MODD(ITAG(IWD),10)
     NTTI=NODEI-NODS
     IF(NTTI.LE.0) GO TO 55
     IF(NODEI.EQ.99) GO TO 50
     NNODE=NTTH
     NTTI=NTTH-NOCT
     IF(NTTH.LE.0) GO TO 60
     NNODE=NTTH
     NTTI=NTTH-NOHTR
     IF(NTTH.LE.0) GO TO 49
     IF(NTTH.GT.5) GO TO 820
     IF(NTTH.LE.NTAG8) GO TO 815
     WRITE(9,610) NOD,NODEI,NTAG8
     LER=1
     GO TO 100
815  A(NPI)=A(NP1) - BTUCRV(NTTH)*COEF(IWD)
     GO TO 100
820  NTTI=NTTH-5
     IF(NTTH.GT.5) GO TO 830

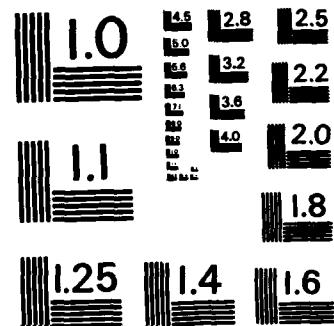
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RD-A159 706 THE EFFECTIVENESS OF HEAT EXCHANGERS WITH ONE SHELL  
PASS AND THREE TUBE PASSES(U) NAVAL POSTGRADUATE SCHOOL 2/3  
MONTEREY CA M S O'HARE JUN 85

UNCLASSIFIED

F/G 20/13 NL





MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS -1963-A

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IF ( NTTH.LE. NTAG9 ) GO TO 825
WRITE( 9,620 ) NOD, NODEI, NTAG9
IER = 1
GO TO 100
T1 = TMPCRV(NTTH)
825   GO TO 65
830   NTTH = NTTH - 5
      IF ( NTTH.LE. 5 ) GO TO 48
      WRITE( 9,570 ) NOD, NODEI
IER = 1
GO TO 100
48   IF ( NTTH.LE. NTMPHT ) GO TO 480
      WRITE( 9,630 ) NOD, NODEI, NTMPHT
IER = 1
GO TO 100
480   WCOEF = NTTH + 1100
      CALL TVFTMP( WCOEF, TOLD(NOD), TMPHT )
      A(NP1) = A(NP1) - WCOEF * COEF(IWD)
      TMPHTV(NTTH) = WCOEF
      GO TO 100
49   IF ( MNODE.LE. NOHTRS ) GO TO 490
      WRITE( 9,600 ) NOD, NODEI, NOHTRS
IER = 1
GO TO 100
490   LOCH = 36 + NNODE
      A(NP1) = A(NP1) - HTR(LOCH) * COEF(IWD)
      GO TO 100
      A(NP1) = A(NP1) - COEF(IWD)
      GO TO 100
      T1 = TOLD(NODEI)
      GO TO 65
60   IF ( MNODE.LE. NCT ) GO TO 61
      WRITE( 9,590 ) NOD, NODEI, NCT
IER = 1
GO TO 100
61   T1 = CONTMP( NNODE )
65   T2 = TOLD(NOD)
      WCOEF = COEF(IWD)
C * *
C * * ASSUMING THE USER HAS RUN PROGRAM CHECK AND FIXED ANY WCOEFS
C * * THAT MIGHT HAVE BEEN IN ERROR. TVSS1 THEREFORE WILL NOT
C * * CHECK AGAIN FOR A WCOEF > 100. NO WARNING IS PRINTED.
C * *
      IF ( WCOEF.LE. 1000 ) GO TO 73
      IF ( WCOEF.LE. 1005 ) GO TO 850
      IF ( WCOEF.LE. 1100 ) GO TO 73
      IF ( WCOEF.GT. 1105 ) GO TO 73
      ATEMP = ( T1+T2 ) / 2.

```

```

LC = WCOEF - 1099.99      GO TO 840
IF ( LC.LE NTCOEF )      GO TO 840
WRITE ( 9,640 ) NOD,NODEI,WCOEF,NTCOEF
IER = 1
GO TO 100
840 CALL TYFTMP (WCOEF, ATEMP, TCOEF)
TCO(LC) = WCOEF
GO TO 730
850 LC = WCOEF - 999.99      GO TO 855
IF ( LC.LE NTAG11 )      GO TO 855
WRITE ( 9,650 ) NOD,NODEI,WCOEF,NTAG11
IER = 1
GO TO 100
855 WCOEF = TIMCO (LC)
C * THE FOLLOWING COMPUTED GO TO WILL FALL THROUGH TO THE NEXT
C * STATEMENT FOR METHOD 6,7,8,& 9
C * * * * *
730 TD = T1 - T2
IF ( TD.NE.0. ) GO TO 731
WCOEF = 0.
GO TO 80
731 IF { ABS(TD).LT.1E-05 } TD = SIGN( 1E-05,TD )
ABSTD = ABS{TD}
GO TO (80/74,75,80,80), METHI
LC = METHI - .5
IF ( LC.LE NOEXP ) GO TO 77
WRITE ( 9,660 ) NOD,NODEI,METHI,NOEXP
IER = 1
GO TO 100
77 T3 = EX (LC)
C * THE FOLLOWING STATEMENT EQUATES TO
C * WCOEF = WCOEF * (ABSTD * T3)/ABSTD
C * * * * *
C * WCOEF = WCOEF * ABSTD ** (T3-1. )
GO TO 80
C * * * * *
C * THE FOLLOWING STATEMENT EQUATES TO
C * WCOEF = WCOEF * (ABSTD * 1.25)/ABSTD
C * 74 WCOEF = WCOEF * ABSTD ** .25
GO TO 80
75 T3 = (T1+273.) / 100.
T4 = (T2+273.) / 100.
WCOEF = WCOEF * (T3**4 - T4**4) / TD
80 IF(NODEI - NONODS( 85,85,90 ) / TD )

```

```

85 A(NODEI) = A(NODEI) + WCOEF
90 GO TO 95
95 A(NP1) = A(NP1) - WCOEF*T1
100 CONTINUE
105 IF(NOD-NOCASE) 107 106,107
106 A(NP1) = A(NP1) - CASBT0
107 WRITE (2)(A(K),K=1,NP1)

C * * * IF IER.NE.0 AT THIS POINT IT MEANS THERE ARE ERRORS IN THE
C * * * INPUT. TVSSI WILL SKIP THE CALCULATIONS AND RETURN TO
C * * * STATEMENT 1000 FOR ANOTHER PROBLEM.

C IF (IER.EQ.0) GO TO 110
C WRITE (9,670)
C GO TO 1000

C 110 ENDFILE 2
REWIND 1
REWIND 2
CALL CHOST (N, NPL, H)
ERRTAG = 0.
NIT = NIT + 1
IF (NIT.LT.13) GO TO 120
CALL CBETA (N, ALPHA, BETA, TOLD, TOLD1, TOLD2, ERR)
DO 130 I=1,N
IF (NIT.EQ.1) TOLD1(I) = 0.0
TOLD2(I) = TOLD(I)
TOLD(I) = TOLD(I) + BETA(I) * ( H(I) - TOLD(I))
A(I) = TOLD(I) - TOLD1(I)
IF (ABS(A(I)).GT. ERR) ERTAG = 1.
CALL TVSOUT (N,TOLD,A, TITLE)
IF (NOHTRS) 140,135
LOCH = 36 + NOHTRS
CALL TYPAGE (3,TITLE)
WRITE (8,525) HTR(K), K=37,LOCH)
135 CALL TYPAGE (3,TITLE)
WRITE (8,526) CASBT0
IF (NTCOEF) 140,145
140 CALL TYPAGE (2,TITLE)
WRITE (8,528) TCO(K), K = 1,NTCOEF)
145 CALL TYPAGE (2,TITLE)
150 IF (NTMPHT) 160,160
155 CALL TYPAGE (2,TITLE)
160 WRITE (8,529) (TMPHT(K), K=1,NTMPHT)
IF (NIT.GE. MAXNIT .AND. MAXNIT .GT. 0) GO TO 175
IF (ERTAG.GT.0.) GO TO 20

```

```

      WRITE (10,500) TITLE
      WRITE (10,501) (TOLD(I), I=1,N)
      GO TO 1000
      DO 180 I=1,N
      IF (BETA(I) .LT. .0001) BETA(I)=.0001
      WRITE (8,50) MAINIT, (BETA(I), I=1,N)
      GO TO 1000
C      500 FORMAT (20A4)
      501 FORMAT (18I4)
      502 FORMAT (9I8)
      503 FORMAT (12I6,8I8)
      504 FORMAT (12I6,8I8,2G8.0)
      505 FORMAT (12H CASE WATTS , 6G12.5)
      506 FORMAT (12H CASE COEFS , 6G12.5)
      507 FORMAT (12H TEMP HEAT , 6G12.5)
      508 FORMAT (12H OVER , T5 ITERATIONS, // ' BETAS' AND (20F6.4) )
      509 FORMAT (12H SET T5, T1 IS NOT ACCEPTABLE. / FIX DECK AND RESUBMIT )
      510 FORMAT (1H , 20A4)
      511 FORMAT (1H , 20A4)
      512 FORMAT (1H , N NCT NOHTRS NOEXP NOCASE NTCOEF NODCFH NTMPHT NONO
      513 1DS NOCT , NOHTR MNITS/12I6,/10
      514 FORMAT (1H , ERR ALPHA , 10I7,2(1X,F11.4))
      515 FORMAT (1H , 14,A4,1S,10I7,2(1X,F8.2))
      516 FORMAT (15I8)
      517 FORMAT (1X '* IMPOSSIBLE NODE NUMBER - YOU SPECIFIED AN ',1
      518 1INTERACTION FROM NODE I5 TO A NODE - YOU SPECIFIED AN ',1
      519 1FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      520 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      521 2'BUT THERE ARE ONLY I4, CONSTANT TEMPERATURES ')
      522 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      523 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      524 2'BUT THERE ARE ONLY I3, INVALID NODE - YOU SPECIFIED AN ',1
      525 1FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      526 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      527 2'BUT THERE ARE ONLY I3, WATT CURVES (TAG 8) '
      528 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      529 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      530 2'BUT THERE ARE ONLY I4, TEMPERATURE CURVES (SET 9) ')
      531 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      532 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      533 2'BUT THERE ARE ONLY I4, TEMP-DEPENDENT WATT CURVES (SER 7) ')
      534 FORMAT (1H , 10I7,2(1X,F11.4))
      535 1FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      536 1FORMAT (15I8)
      537 1FORMAT (1X '* IMPOSSIBLE NODE NUMBER - YOU SPECIFIED AN ',1
      538 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      539 1FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      540 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      541 2'BUT THERE ARE ONLY I4, CONSTANT TEMPERATURES ')
      542 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      543 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      544 2'BUT THERE ARE ONLY I3, INVALID NODE - YOU SPECIFIED AN ',1
      545 1FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      546 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      547 2'BUT THERE ARE ONLY I3, WATT CURVES (TAG 8) '
      548 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      549 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      550 2'BUT THERE ARE ONLY I4, TEMPERATURE CURVES (SET 9) ')
      551 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      552 1INTERACTION FROM NODE I5,5X TO A NODE I5/15X ',1
      553 2'BUT THERE ARE ONLY I4, TEMP-DEPENDENT WATT CURVES (SER 7) ')
      554 2FORMAT (1X,* INVALID NODE - YOU SPECIFIED AN ',1
      555 1TO NODE I5,5X, YOU SPECIFIED A CONDUCTANCE OF ,F7.1,/15X,

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2 'BUT THERE ARE ONLY ', I3, ' TEMP-DEPENDENT ',
3 'COEFF CURVES (SET 1), ' NODE'15.5X,
650 FORMAT (/1X 15.5X, 'INVALID CONDUCTANCE - NODE', I5.5X,
1 TO NODE', I11 ), /15X,
2 'BUT THERE ARE ONLY ', I3, 'SPECIFIED TIME COEFFS (SET 11),
660 FORMAT (/1X, 'ONLY', I3, 'INVALID METHOD ', - NODE', I5.5X, 'TO NODE',
1 I5.5X, 'YOU SPECIFIED A METHOD OF ', I3, '/15X, 'BUT THERE ARE ONLY ',
2 I3, 'UNIQUE EXPONENTS (SET 5) ', I3, '/15X, 'THERE ARE ERRORS IN YOUR INPUT FOR THIS PROBLEM',
670 FORMAT (/1X, 'THERE ARE ERRORS IN YOUR INPUT FOR THIS PROBLEM',
1 //10X, 'THERE ARE ERRORS IN YOUR INPUT FOR THIS PROBLEM',
2 //10X, 'THERE ARE ERRORS IN YOUR INPUT FOR THIS PROBLEM',
680 FORMAT(4/9F8.2)
999 CONTINUE
STOP
END

C   SUBROUTINE CBETA (N, ALPHA, BETA, TN, TNM1, TNM2, ERR )
      IMPLICIT REAL*4 (A-H,O-Z)
      DIMENSION TN(315), TNM1(315), TNM2(315), BETA(315)
      DO 50 I=1,N
      TMTM1 = TN(I) - TNM1(I)
      T12 = ABS(TNM1(I) - TNM2(I))
      IF (ABS(T12).LT.1E-06) T12 = SIGN( 1E-06, T12 )
      GAMMA = TMTM1/TI2
      IF (GAMMA.GT.0.) GO TO 10
      IF (ABS(TMTM1).LE.ERR) BETA(I) = -BETA(I)*ALPHA/GAMMA
      IF (GAMMA.LT. -ALPHA) BETA(I) = -BETA(I)*ALPHA/GAMMA
      GO TO 50
10   IF (GAMMA.GT. 1.) GO TO 50
      BETA(I) = BETA(I) / ALPHA
50   IF (BETA(I).GT. 1.) BETA(I) = 1.
      RETURN
END

C   SUBROUTINE CHOST (N, NP1, EL)
      IMPLICIT REAL*4 (A-H,O-Z)
      DIMENSION EL(316), LOCS(316), SAVE(49770)
      LOCS(1) = 1
      NM1 = N - 1
      I = 0

C   10  I = I + 1
      READ(2,EL(K),K=1,NP1)
      IP1 = I + 1
      IF (I.EQ.1) GO TO 50
      DO 45 J=2,I
      LR = LOCS(J-1)
      IF (EL(J-1).EQ. 0.) GO TO 45

```

```

DO 40 JR=J,NP1
EL(JR)=EL(JR);EQ.0.-EL(J-1)*SAVE(LR)
40 LR=LR+1
45 CONTINUE
50 DO 60 K=IP1,NP1
EL(K)=EL(K)/EL(I) GO TO 60
51 IF(EL(K)=EL(K)) GO TO 60
50 CONTINUE
60 IF(I>NP1) GO TO 80
IF(I>NP1) LS=LOC(I) GO TO 80
LS=LOC(I+1)=LS+NP1-I
DO 72 K=IP1,NP1-I
SAVE(LS)=EL(K)
72 LS=LS+1
GO TO 10
C 80 REWIND 2
EL(N)=EL(NP1)
DO 90 I=1,NM1
II=NPI-I
LF=I-N
LR=LOC(LF)=SAVE(LR)
EL(I-1)=I-N
DO 90 K=I,N
LR=LOC(LF)+K-1 GO TO 90
LF(SAVE(LR)+K-1)=SAVE(LR)
EL(I-1)=EL(I-1)*EL(K)
90 CONTINUE
RETURN
END
C SUBROUTINE TVFTMP REAL*4 (CO-A-H,T-z,TCOEF)
DIMENSION TCOEF(90)
NC=CO-1099
NB=18*NC-17
IF(T-TCOEF(NB)) 2,2,6
2 CO=TCOEF(NB+1)
2 GO TO 60
6 NE=NB+16
NB=NB+2
DO 10 K=NB,NE
IF(T-TCOEF(K)) 10,20,50
10 TCM2=TCOEF(K-2)
TCM1=TCOEF(K-1)

```

```

TCP1 = TCOEF(K+1)
TCC = TC - TCM2
IF ( ABS(TC-TCM2) .LT. 1E-06 ) * {TCC = SIGN(1)E-06 TCC }

20 CO = TO 60
GO TO 60
CO = TCOEF (K+1)
50 CONTINUE
CO = TCOEF(NE+1)
60 RETURN
END

C   SUBROUTINE TVSOUT(N,NA,T1,T2,TITLE)
      IMPLICIT REAL*4(A-H,O-Z),T1(315),T2(315),ID(12),TITLE(20)
C
      CALL TVPAGE (2,TITLE)
      WRITE(8,500)
      NL = NA+2
      DO 50 I=1,N,12
      CALL TVPAGE (NL,TITLE)
      IFLY TYPAGE 5,5,10
      N5=12
      5 GO TO 15
      10 N5=N-I+1
      15 DO 20 K=1,N5
      20 ID(K) = I+K-1
      WRITE(8,501) (ID(K), K=1,N5)
      N1 = I + N5 - 1
      IF (NA-1) 25,25,30
      25 WRITE(8,504) (T1(K), K= I,N1)
      GO TO 30
      30 WRITE(8,503) {T1(K), K= I,N1}
      50 CONTINUE
      RETURN

C   500 FORMAT (1HO)
      501 FORMAT (/10H NODE NO. :12I9)
      502 FORMAT (12H NEW TEMPS :12F9.2)
      503 FORMAT (12H NEW - OLD :12F9.2)
      504 FORMAT (12H ORIG TEMPS :12F9.2)
END

C   SUBROUTINE TVSHTR (NOHTRS,HTR,CASBTU,NOCONT,TOLD,NODCFH)
      IMPLICIT REAL*4(A-H,O-Z),HTR(42),NOCONT(6),TOLD(315)
      CASBTU = 0.

```

```

DO 25 K=1 NOHTRS
LOK = 36+K
IF (NOCONT(K)) 24, 24, 43
43 LOK1 = NOCONT(K)
TEMP = TOLD(LOK1)
IF (K-3) 45, 45, 30
45 LOK2 = 0
GO TO 55
50 LOK2 = 18
55 IF (NODCFH) 3, 3, 60
60 IF (TEMP-HTR(2)) 65, 65, 70
65 HTR(LOK) = HTR(LOK2+1)
CASBTU = CASBTU + HTR(LOK2+3)
GO TO 25
70 NODCFH = 0
IF (TEMP - HTR(LOK2+4)) 5, 5, 15
5 HTR(LOK) = HTR(LOK2+9)
CASBTU = CASBTU + HTR(LOK2+14)
GO TO 25
15 DO 16 K1=5 8
LOK3 = LOK2+K1
IF (TEMP - HTR(LOK3)) 17, 17, 16
16 CONTINUE
HTR(LOK) = HTR(LOK2+13)
CASBTU = CASBTU + HTR(LOK2+18)
GO TO 25
17 HTR3 = HTR(LOK3) - HTR(LOK3-1)
IF (ABS(HTRL3)*1E-06) HTRL3 = SIGN( 1E-06 , HTRL3 )
FRAC = TEMP - HTR(LOK3-1) / HTRL3
HTR(LOK) = (HTR(LOK3+5) - HTR(LOK3+4)) * FRAC + HTR(LOK3+9)
CASBTU = CASBTU + (HTR(LOK3+10) - HTR(LOK3+9)) * FRAC + HTR(LOK3+9)
GO TO 25
24 HTR(LOK) = 0.
CONTINUE
25 RETURN
END

C
SUBROUTINE TYPAGE*4 (NL, FNAME)
IMPLICIT REAL*4 (A-H,O-Z)
DIMENSION FNAME(20)
IF (NL) 10, 10, 20
10 NPAGE = 0
LINCNT = 75
20 LINCNT = LINCNT + NL
IF (LINCNT - 56) 40, 40, 30
30 NPAGE = NPAGE + 1
WRITE (8,50) FNAME, NPAGE
LINCNT = NL

```

```
40 RETURN
50 FORMAT (1H1,20X,20A4,8X,9HPAGE NO. ,13/ )
END
/*
//GO.FT01F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT0F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=DUMMY
//GO.FT03F001 DD DISP=SHR,DSN=MSS,S2323.TVSSIV
//GO.FT04F001 DD
//GO.FT08F001 DD SYSSOUT=A,DCB=RECFM=FBA
```

APPENDIX B  
NTU14 COMPUTER GENERATED INPUT ANALYZER PROGRAM

```
//SHARE   JOB (2323,0267) 'NTU14' , CLASS=B
//MAIN    ORG=NPGVM1 2323P
//EXEC    FORTVCL,PARM.LKED='LIST,MAP'
//FORT.SYSIN DD* THIS IS PROGRAM NTU14
C
C IT GENERATES AN INPUT FILE FOR THERMAL ANALYZER TO VERIFY
C 1-4 EFFECTIVENESS-NTU RELATIONSHIP THAT IS AVAILABLE IN
C OPEN LITERATURE.
C
C DIMENSION COEF(250,5),KCON(250,5),L1(8),L2(3),L3(6),SET2(2),FL4(4)
C
C CHARACTER *79 TITLE
C CHARACTER *12 FNAME
C
C DATA IOT,IN,IPR,IWR/6,5,4,8/
C
C OPEN PRINTER OUTPUT FILE
C
C OPEN(IPR,FILE='PRN',STATUS='NEW',FORM='FORMATTED',IOSTAT=ICK)
C IF(ICK<NE_0) WRITE(IOT,920)
C 920 FORMAT(' Trouble opening printer output file' )
C
C WRITE(IOT,917)
C 917 FORMAT(' / Input the title, of this study - 79 columns only ',
C & ' This title will appear, /, at the top of every printed page',
C & ' of output: ')
C READ(IN,918) TITLE
C 918 FORMAT(A79)
C
C WRITE(IOT,901)
C 901 FORMAT(' / INPUT HOT SIDE CAPACITY RATE: ')
C READ(IN,902) CHOT
C 902 FORMAT(BN,F10.0)
C
C WRITE(IOT,903)
C 903 FORMAT(' / INPUT COLD SIDE CAPACITY RATE: ')
C READ(IN,904) CCOLD
C WRITE(IOT,904)
```

```

904 FORMAT('INPUT OVERALL HEAT TRANSFER COEFFICIENT: ')
C   READ(IN,902) U
C   WRITE(IOT,905)
905 FORMAT('INPUT TOTAL HEAT TRANSFER SURFACE: ')
C   READ(IN,902) SURFTO
C   WRITE(IOT,906)
906 FORMAT('INPUT HOT SIDE INLET TEMPERATURE: ')
C   READ(IN,902) THOTIN
C   WRITE(IOT,907)
907 FORMAT('INPUT COLD SIDE INLET TEMPERATURE: ')
C   READ(IN,902) TCOLDIN
C   VALK1 = CHOT
VALK2 = CCOLD
60   TINIT = 100.
C   C   FRONT END
C   C   L1{1} = 250
L1{2} = 2
DO 10 I=3,8
10  L1{I} = 0
C   20 DO 20 I=1,3
20  L2{I} = 0
C   C   L3{1} = 300
L3{2} = 50
L3{3} = 6
L3{4} = 2
L3{5} = 4
L3{6} = 6
C   C   FL4{1} = .05
FL4{2} = .66667
FL4{3} = .8
FL4{4} = TINIT
L4 = 12
C   C   CONSTANT TEMPERATURES
SET2{1} = THOTIN
SET2{2} = TCOLDIN
C

```

```

C READY FOR INPUT SET 4
C NODE 1
C   KCON{1,1} = 514
C   KCON{1,2} = 1504
C   KCON{1,3} = 1514
C   KCON{1,4} = 2504
C   KCON{1,5} = 3015
C   COEF{1,5} = VALK1
C   DO 50 I = 1,4
C   50 COEF(1,I) = VALK3
C NODES 2 TO 50
C   DO 75 I = 2,50
C     J = I+50
C     K = 151-I
C     L = 150+I
C     M = 251-I
C     N = I-1
C     KCON{I,1} = 10*N + 5
C     KCON{I,2} = 10*N + 4
C     KCON{I,3} = 10*N + 4
C     KCON{I,4} = 10*L + 4
C     KCON{I,5} = 10*M + 4
C     COEF{I,1} = VALK1
C     DO 80 I = 2,5
C     COEF(I,I) = VALK3
C   80 CONTINUE
C   75 CONTINUE
C NODE 51
C   KCON{51,1} = 3025
C   KCON{51,2} = 14
C   COEF{51,1} = VALK2
C   COEF{51,2} = VALK3
C NODES 52 TO 250
C   DO 120 I = 52,250
C     K = I-1
C     IF(I.GT.100) GO TO 122
C     J = I-50
C     GO TO 135
C   122 IF(I.GT.150) GO TO 124
C     L = I-100

```

```

M = 2*L - 1
N = M + 50
J = TO - 135
GO TO 135 GO TO 135
124 IF(I .GT. 200) GO TO 126
J = I - 150
GO TO 135
126 CONTINUE
L = I - 200
M = 2*L - 1
N = M + 150
J = I - N
135 KCON{I,1} = 10*j + 4
KCON{I,2} = 10*k + 5
COEF{I,1} = VALK3
COEF{I,2} = VALK2
C END OF DATA SETUP FOR ANALYZER
C NOW CREATE INPUT FILE
C
      WRITE(IOT,922)
      WRITE(IWR,919) STATUS='NEW', FORM='FORMATTED', IOSTAT=ICK)
      IF(ICK .GT. 0) WRITE(IOT,924)
      FORMAT(/, 'Trouble opening input file' )
      & DESIGNATION: FNAME
      READ(IN923) FNAME
      923 FORMAT(A12)
C OPEN INPUT FILE
C
      OPEN(IWR,FILE=FNAME,STATUS='NEW', FORM='FORMATTED', IOSTAT=ICK)
      924 FORMAT(/, 'Trouble opening input file' )
      & DESIGNATION: FNAME
      WRITE(IOT,925) FNAME
      925 FORMAT(I7,1X,A14)
      WRITE(IWR,919) TITLE
      919 FORMAT(1X,A79)
      WRITE(IWR,908) (L1(I), I=1,8)
      908 FORMAT(19I4)
      WRITE(IWR,908) (L2(I), I=1,3)
      909 FORMAT(19I4)
      WRITE(IWR,908) (L3(I), I=1,6)
      910 FORMAT(19I4)
      WRITE(IWR,911) (FL4(I), I=1,4)
      911 FORMAT(F8.3,F8.5,F8.1)
      WRITE(IWR,912) SET2(1),SET2(2)
      912 FORMAT(2F8.0)
      C DO 200 I = 1,50
      200 WRITE(IWR,913)(KCON(I,J), J=1,5)
      913 FORMAT(9I8)

```

```
      WRITE(IWR,914)(COEF(I,J),J=1,5)
914  FORMAT(5F8.4)
      200  CONTINUE
C      DO 250 I=51,250
      WRITE(IWR,913) KCON(I,1),KCON(I,2)
      WRITE(IWR,914) COEF(I,1),COEF(I,2)
      250  CONTINUE
C      7  CONTINUE
      STOP
      END
/*
//LKED.SYSLMOND DD DISP=SHR,DSNAME=MSS.S2323.LOAD
//LKED.SYSIN DD NAME=NTU14(R)
/*
//
```

## APPENDIX C

### NTU32C COMPUTER GENERATED INPUT ANALYZER PROGRAM

THIS IS PROGRAM NTU32C

```

THIS IS PROGRAM NTU32C

IT GENERATES AN INPUT FILE FOR THERMAL ANALYZER TO OBTAIN
1-3 EFFECTIVENESS-NTU RELATIONSHIP THAT IS NOT AVAILABLE IN
OPEN LITERATURE (2C MEANING ONE PARALLEL PASS AND TWO
COUNTERFLOW PASSES) .

DIMENSION COEF(200,5),KCON(200,5),L1(8),L2(3),L3(6),SET2(2),FL4(4)

C CHARACTER *79 TITLE
C CHARACTER *12 FNAME

C DATA IOT,IN,IPR,IWR/6,5,4,8/

C OPEN PRINTER OUTPUT FILE

C OPEN(IPR,FILE='PRN',STATUS='NEW',FORM='FORMATTED',IOSTAT=ICK)
IF(ICK.NE.0)WRITE(IOT,920)
920 FORMAT('Trouble opening printer output file')

C WRITE(IOT,917)
FORMAT('
This title will appear,/, at the top of every printed page',
     & ' of output:')

C READ(IN,918) TITLE
918 FORMAT(A79)

C WRITE(IOT,901)
FORMAT('/',INPUT HOT SIDE CAPACITY RATE: ')
READ(IN,902) CHOT
902 FORMAT(BN,F10.0)

C WRITE(IOT,903)
FORMAT('/',INPUT COLD SIDE CAPACITY RATE: ')
READ(IN,902) CCLD
903 FORMAT(BN,F10.0)

C WRITE(IOT,904)
FORMAT('/',INPUT OVERALL HEAT TRANSFER COEFFICIENT: ')
READ(IN,902) U

```

```

905 WRITE(IOT,905)
      FORMAT(/,INPUT TOTAL HEAT TRANSFER SURFACE: ')
C   READ(IN,902) SURFTO
C   WRITE(IOT,906)
      FORMAT(/,INPUT HOT SIDE INLET TEMPERATURE: ')
C   READ(IN,902) THOTIN
C   WRITE(IOT,907)
      FORMAT(/,INPUT COLD SIDE INLET TEMPERATURE: ')
C   READ(IN,902) TCLDDIN
C   VALK1 = CHOT
C   VALK2 = CCOLD
C   VALK3 = USURFTO/150.
C   TINIT = 125.

C   C          FRONT END
C   L1{1} = 200
C   L1{2} = 2
C   D0{1} = I=3,8
C   10 L1(I) = 0
C   20 DO 20 I=1,3
C   20 L2(I) = 0
C   L3{1} = 300
C   L3{2} = 50
C   L3{3} = 6
C   L3{4} = 4
C   L3{5} = 6
C   L3{6} = 6
C   PL4{1} = .05
C   PL4{2} = .66667
C   PL4{3} = .8
C   PL4{4} = .1INIT
C   L4 = 12

C   CONSTANT TEMPERATURES
C   SET2{1} = THOTIN
C   SET2{2} = TCLDDIN
C   READY FOR INPUT SET 4
C   NODE 1

```

```

C   KCON(1,1) = 1004
C   KCON(1,2) = 1014
C   KCON(1,3) = 2004
C   KCON(1,4) = 3015
C   COEF(1,1) = VALK1
C   DO 50 COEF(1,1) = VALK3
50  NODES 2 TO 50
C   DO 75 I = 2,50
J = 101 - I
K = 100 + I
L = 201 - I
N = 1 - I
KCON(1,1) = 10*N + 5
KCON(1,2) = 10*J + 4
KCON(1,3) = 10*K + 4
KCON(1,4) = 10*L + 4
DO 80 COEF(I,I) = VALK1
80  COEF(1,1) = 24
CONTINUE
75  CONTINUE
C   NODE 51
C   KCON(51,1) = 3025
C   KCON(51,2) = 504
C   COEF(51,1) = VALK2
C   COEF(51,2) = VALK3
C   NODES 52 TO 200
C   DO 120 I = 52,200
K = I - 1
IF(I.GT.100) GO TO 122
L = I - 50
M = 2*L - 1
J = I - M
GO TO 135
122 IF(I.GT.150) GO TO 124
J = I - 100
GO TO 135
124 L = I - 150
M = 2*L - 1

```

```

135 KCON(I,1) = 10*j + 4
      KCON(I,2) = 10*k + 5
      COEF(I,1) = VALK3
      COEF(I,2) = VALK2

C END OF DATA SETUP
C NOW CREATE INPUT FOR ANALYZER

      WRITE(IOT,922)
      FORMAT(IOT,ENTER NAME OF INPUT FILE, INCLUDING DRIVE',
      & DESIGNATION:)
      READ(IN923) FNAME
      923 FORMAT(A12)

C OPEN INPUT FILE

      OPEN(IWR,FILE='TVSSI',STATUS='NEW',FORM='FORMATTED', IOSTAT=ICK)
      IF(ICK.GT.0)WRITE(IOT,924)
      924 FORMAT('/','Trouble opening input file')

C      WRITE(IOT,925) FNAME
      WRITE(IOT,925)
      FORMAT(IOT,' WRITING FILE : ',A14)
      FORMAT(IOT,' WRITING FILE : ',VSS1)
      925 FORMAT(IWR,919) TITLE
      919 FORMAT(IWR,A79)
      WRITE(IWR,908)(L1(I),I=1,8)
      908 FORMAT(IWR,914)
      WRITE(IWR,908)(L2(I),'I=1,3')
      WRITE(IWR,908){L3(I)}{'I=1,6}
      WRITE(IWR,911){L4(I)}FL4{2},L4,FL4(3),FL4(4)
      911 FORMAT(IWR,F8.3)F8.1
      WRITE(IWR,912){F8.1}SET2(1),SET2(2)
      912 FORMAT(2F8.0)

C      DO 200 I=1,50
      WRITE(IWR,913)(KCON(I,J),J=1,4)
      913 FORMAT(IWR,918)
      WRITE(IWR,914)(COEF(I,J),J=1,4)
      914 FORMAT(4F8.4)
      200 CONTINUE

C      DO 250 I=51,200
      WRITE(IWR,913) KCON(I,1),KCON(I,2)
      WRITE(IWR,914) COEF(I,1),COEF(I,2)
      250 CONTINUE

C      CLOSE(IWR,IOSTAT=ICK)

```

```
921 IF(ICK,NE,0) WRITE(IOT,921)EX
      FORMAT('closing printer output file')
C      STOP
      END
```

APPENDIX D  
NTU32P COMPUTER GENERATED INPUT ANALYZER PROGRAM

THIS IS PROGRAM NTU32P

```
C IT GENERATES AN INPUT FILE FOR THERMAL ANALYZER TO OBTAIN  
C 1-3 EFFECTIVENESS-NTU RELATIONSHIP THAT IS NOT AVAILABLE IN  
C OPEN LITERATURE {2P MEANING TWO PARALLEL PASSES AND ONE  
C COUNTERFLOW PASS} .  
C  
C DIMENSION COEF(200,5),KCON(200,5),L1(8),L2(3),L3(6),SET2(2),FL4(4)  
C  
C CHARACTER *79 TITLE  
C CHARACTER *12 FNAME  
C  
C DATA IOT,IN,IPR,IWR/6,5,4,8/  
C  
C OPEN PRINTER OUTPUT FILE  
C  
C OPEN(IPR,FILE='PRN',STATUS='NEW',FORM='FORMATTED',IOSTAT=ICK)  
C IF(ICK.NE.0) WRITE(IOT,920)  
C 920 FORMAT('Trouble opening printer output file')  
C  
C  
C 917 WRITE(IOT,917)  
C & This title will appear /, at the top of every printed page ,  
C & of output :}  
C READ(IN,918) TITLE  
C 918 FORMAT(A79)  
C  
C  
C 901 WRITE(IOT,901)  
C 901 FORMAT(/,INPUT HOT SIDE CAPACITY RATE: ')  
C 902 READ(IN,902) CHOT  
C 902 FORMAT(BN,F10.0)  
C  
C 903 WRITE(IOT,903)  
C 903 FORMAT(/,INPUT COLD SIDE CAPACITY RATE: ')  
C READ(IN,902) CCOLD  
C  
C 904 WRITE(IOT,904)  
C 904 FORMAT(/,INPUT OVERALL HEAT TRANSFER COEFFICIENT: ')  
C READ(IN,902) U
```

```

      WRITE(IOT,905)
      FORMAT(1/9T,902) SURFT0
      READ(INN,902) SURFT0
C      WRITE(1/9T,906)
      FORMAT(1/9T,INPUT HOT SIDE INLET TEMPERATURE: )
      READ(INN,902) THOTIN
C      WRITE(1/9T,907)
      FORMAT(1/9T,INPUT COLD SIDE INLET TEMPERATURE: )
      READ(INN,902) TCOLDIN
C      VALK1 = CHOT
C      VALK2 = CCLD
C      VALK3 = U*SURFT0/150.
C      TINIT = 125.

C      CC      FRONT END
C      L1{1} = 200
C      L1{2} = 2
C      D0{1} = I=3,8
C      10 L1(I) = 0
C      20 D0{2} = I=1,3
C      20 L2(I) = 0
C      L3{1} = 300
C      L3{2} = 50
C      L3{3} = 6
C      L3{4} = 2
C      L3{5} = 4
C      L3{6} = 6
C      FL4{1} = .05
C      FL4{2} = .66667
C      FL4{3} = .8
C      FL4{4} = TINIT
C      L4 = L2

C      CONSTANT TEMPERATURES
C      SET2{1} = THOTIN
C      SET2{2} = TCOLDIN
C      READY FOR INPUT SET 4
C      NODE 1

```

```

C      KCON(1,1) = 514
C      KCON(1,2) = 1504
C      KCON(1,3) = 1514
C      KCON(1,4) = 3015
C      COEF(1,1) = VALK1
C      DO 50 COEF(1,1) = VALK3
C      NODES 2 TO 50
C      DO 75 I = 2,50
C      J = I + 50
C      K = 151 - I
C      L = 150 + I
C      N = I - 1
C      KCON(I,1) = 10*N + 5
C      KCON(I,2) = 10*J + 4
C      KCON(I,3) = 10*K + 4
C      KCON(I,4) = 10*L + 4
C      COEF(I,1) = VALK1
C      DO 80 COEF(I,1) = VALK3
C      COEF(I,2) = 24
C      COEF(I,3) = 24
C      COEF(I,4) = 24
C      80 CONTINUE
C      75 CONTINUE
C      NODE 51
C      KCON(51,1) = 3025
C      KCON(51,2) = 14
C      COEF(51,1) = VALK3
C      COEF(51,2) = VALK3
C      NODES 52 TO 200
C      DO 120 I = 52,200
C      K = I - 1
C      IF(I.GT.100) GO TO 122
C      J = I - 50
C      GO TO 135
C      122 IF(I.GT.150) GO TO 124
C      L = I - 100
C      M = 2*L - 1
C      N = M + 50
C      GO TO 135
C      124 J = I - 150
C      135 KCON(I,1) = 10*J + 4

```

```

      KCON(1,2) = 10*K3 + 5
      COEF(1,1) = VALK3
120  COEF(1,2) = VALK2
C   END OF DATA SETUP
C   NOW CREATE INPUT FOR ANALYZER
C
C   WRITE(IOT,922)
922  FORMAT(/'Enter name of input file, including drive',
&           DESIGNATION: )
      READ(IN923) FNAME
923  FORMAT(A12)
C
C   OPEN INPUT FILE
C
OPEN(IWR,FILE=FNAME,STATUS='NEW',FORM='FORMATTED',IOSTAT=ICK)
IF(ICK.GT.0)WRITE(IOT,924)
      Trouble(IOT,ICK)
924  FORMAT('/',Trouble opening input file')
C
C   WRITE(IOT,925)
925  FORMAT(/'Writing file : ',A14)
      WRITE(IWR,919) TITLE
919  FORMAT(I1X,A79)
      WRITE(IWR,908) (L1(I),I=1,8)
908  FORMAT(I9I4)
      WRITE(IWR,908) (L2(I),I=1,3)
      WRITE(IWR,908) (L3(I),I=1,6)
      WRITE(IWR,911) (FL4(1),I=1,4)
      WRITE(IWR,911) (FL4(2),I=1,4)
      WRITE(IWR,911) (FL4(3),I=1,4)
      WRITE(IWR,911) (FL4(4),I=1,4)
911  FORMAT(F8.3,F8.5,F8.2)
      WRITE(IWR,912) SET2(1),SET2(2)
912  FORMAT(2F8.0)
C
      DO 200 I=1,50
      WRITE(IWR,913) (KCON(I,J),J=1,4)
913  FORMAT(9I8)
      WRITE(IWR,914) (COEF(I,J),J=1,4)
914  FORMAT(4F8.4)
200  CONTINUE
C
      DO 250 I=51,200
      WRITE(IWR,913) KCON(I,1),KCON(I,2)
      WRITE(IWR,914) COEF(I,1),COEF(I,2)
250  CONTINUE
C
      CLOSE(IWR,IOSTAT=ICK)
IF(ICK.NE.0)WRITE(IOT,921)EX
      921 FORMAT('Trouble closing printer output file' )
C

```

STOP  
END

## APPENDIX E

### SAMPLE OUTPUT FROM NT14 COMPUTER INPUT ANALYZER PROGRAM

NTU=0.05	R=0.15	COUNTER	0	0
200	0	0	0	0
300	500	0.6667	2	0
400	1000	0.6667	4	0
500	1500	0.6667	6	0
600	2000	0.6667	8	0
700	2500	0.6667	10	0
800	3000	0.6667	12	0
900	3500	0.6667	14	0
1000	4000	0.6667	16	0
1100	4500	0.6667	18	0
1200	5000	0.6667	20	0
1300	5500	0.6667	22	0
1400	6000	0.6667	24	0
1500	6500	0.6667	26	0
1600	7000	0.6667	28	0
1700	7500	0.6667	30	0
1800	8000	0.6667	32	0
1900	8500	0.6667	34	0
2000	9000	0.6667	36	0
2100	9500	0.6667	38	0
2200	10000	0.6667	40	0
2300	10500	0.6667	42	0
2400	11000	0.6667	44	0
2500	11500	0.6667	46	0
2600	12000	0.6667	48	0
2700	12500	0.6667	50	0
2800	13000	0.6667	52	0
2900	13500	0.6667	54	0
3000	14000	0.6667	56	0
3100	14500	0.6667	58	0
3200	15000	0.6667	60	0
3300	15500	0.6667	62	0
3400	16000	0.6667	64	0
3500	16500	0.6667	66	0
3600	17000	0.6667	68	0
3700	17500	0.6667	70	0
3800	18000	0.6667	72	0
3900	18500	0.6667	74	0
4000	19000	0.6667	76	0
4100	19500	0.6667	78	0
4200	20000	0.6667	80	0
4300	20500	0.6667	82	0
4400	21000	0.6667	84	0
4500	21500	0.6667	86	0
4600	22000	0.6667	88	0
4700	22500	0.6667	90	0
4800	23000	0.6667	92	0
4900	23500	0.6667	94	0
5000	24000	0.6667	96	0
5100	24500	0.6667	98	0
5200	25000	0.6667	100	0
5300	25500	0.6667	102	0
5400	26000	0.6667	104	0
5500	26500	0.6667	106	0
5600	27000	0.6667	108	0
5700	27500	0.6667	110	0
5800	28000	0.6667	112	0
5900	28500	0.6667	114	0
6000	29000	0.6667	116	0
6100	29500	0.6667	118	0
6200	30000	0.6667	120	0
6300	30500	0.6667	122	0
6400	31000	0.6667	124	0
6500	31500	0.6667	126	0
6600	32000	0.6667	128	0
6700	32500	0.6667	130	0
6800	33000	0.6667	132	0
6900	33500	0.6667	134	0
7000	34000	0.6667	136	0
7100	34500	0.6667	138	0
7200	35000	0.6667	140	0
7300	35500	0.6667	142	0
7400	36000	0.6667	144	0
7500	36500	0.6667	146	0
7600	37000	0.6667	148	0
7700	37500	0.6667	150	0
7800	38000	0.6667	152	0
7900	38500	0.6667	154	0
8000	39000	0.6667	156	0
8100	39500	0.6667	158	0
8200	40000	0.6667	160	0
8300	40500	0.6667	162	0
8400	41000	0.6667	164	0
8500	41500	0.6667	166	0
8600	42000	0.6667	168	0
8700	42500	0.6667	170	0
8800	43000	0.6667	172	0
8900	43500	0.6667	174	0
9000	44000	0.6667	176	0
9100	44500	0.6667	178	0
9200	45000	0.6667	180	0
9300	45500	0.6667	182	0
9400	46000	0.6667	184	0
9500	46500	0.6667	186	0
9600	47000	0.6667	188	0
9700	47500	0.6667	190	0
9800	48000	0.6667	192	0
9900	48500	0.6667	194	0
10000	49000	0.6667	196	0
10100	49500	0.6667	198	0
10200	50000	0.6667	200	0
10300	50500	0.6667	202	0
10400	51000	0.6667	204	0
10500	51500	0.6667	206	0
10600	52000	0.6667	208	0
10700	52500	0.6667	210	0
10800	53000	0.6667	212	0
10900	53500	0.6667	214	0
11000	54000	0.6667	216	0
11100	54500	0.6667	218	0
11200	55000	0.6667	220	0
11300	55500	0.6667	222	0
11400	56000	0.6667	224	0
11500	56500	0.6667	226	0
11600	57000	0.6667	228	0
11700	57500	0.6667	230	0
11800	58000	0.6667	232	0
11900	58500	0.6667	234	0
12000	59000	0.6667	236	0
12100	59500	0.6667	238	0
12200	60000	0.6667	240	0
12300	60500	0.6667	242	0
12400	61000	0.6667	244	0
12500	61500	0.6667	246	0
12600	62000	0.6667	248	0
12700	62500	0.6667	250	0
12800	63000	0.6667	252	0
12900	63500	0.6667	254	0
13000	64000	0.6667	256	0
13100	64500	0.6667	258	0
13200	65000	0.6667	260	0
13300	65500	0.6667	262	0
13400	66000	0.6667	264	0
13500	66500	0.6667	266	0
13600	67000	0.6667	268	0
13700	67500	0.6667	270	0
13800	68000	0.6667	272	0
13900	68500	0.6667	274	0
14000	69000	0.6667	276	0
14100	69500	0.6667	278	0
14200	70000	0.6667	280	0
14300	70500	0.6667	282	0
14400	71000	0.6667	284	0
14500	71500	0.6667	286	0
14600	72000	0.6667	288	0
14700	72500	0.6667	290	0
14800	73000	0.6667	292	0
14900	73500	0.6667	294	0
15000	74000	0.6667	296	0
15100	74500	0.6667	298	0
15200	75000	0.6667	300	0
15300	75500	0.6667	302	0
15400	76000	0.6667	304	0
15500	76500	0.6667	306	0
15600	77000	0.6667	308	0
15700	77500	0.6667	310	0
15800	78000	0.6667	312	0
15900	78500	0.6667	314	0
16000	79000	0.6667	316	0
16100	79500	0.6667	318	0
16200	80000	0.6667	320	0
16300	80500	0.6667	322	0
16400	81000	0.6667	324	0
16500	81500	0.6667	326	0
16600	82000	0.6667	328	0
16700	82500	0.6667	330	0
16800	83000	0.6667	332	0
16900	83500	0.6667	334	0
17000	84000	0.6667	336	0
17100	84500	0.6667	338	0
17200	85000	0.6667	340	0
17300	85500	0.6667	342	0
17400	86000	0.6667	344	0
17500	86500	0.6667	346	0
17600	87000	0.6667	348	0
17700	87500	0.6667	350	0
17800	88000	0.6667	352	0
17900	88500	0.6667	354	0
18000	89000	0.6667	356	0
18100	89500	0.6667	358	0
18200	90000	0.6667	360	0
18300	90500	0.6667	362	0
18400	91000	0.6667	364	0
18500	91500	0.6667	366	0
18600	92000	0.6667	368	0
18700	92500	0.6667	370	0
18800	93000	0.6667	372	0
18900	93500	0.6667	374	0
19000	94000	0.6667	376	0
19100	94500	0.6667	378	0
19200	95000	0.6667	380	0
19300	95500	0.6667	382	0
19400	96000	0.6667	384	0
19500	96500	0.6667	386	0
19600	97000	0.6667	388	0
19700	97500	0.6667	390	0
19800	98000	0.6667	392	0
19900	98500	0.6667	394	0
20000	99000	0.6667	396	0
20100	99500	0.6667	398	0
20200	100000	0.6667	400	0
20300	100500	0.6667	402	0
20400	101000	0.6667	404	0
20500	101500	0.6667	406	0
20600	102000	0.6667	408	0
20700	102500	0.6667	410	0
20800	103000	0.6667	412	0
20900	103500	0.6667	414	0
21000	104000	0.6667	416	0
21100	104500	0.6667	418	0
21200	105000	0.6667	420	0
21300	105500	0.6667	422	0
21400	106000	0.6667	424	0
21500	106500	0.6667	426	0
21600	107000	0.6667	428	0
21700	107500	0.6667	430	0
21800	108000	0.6667	432	0
21900	108500	0.6667	434	0
22000	109000	0.6667	436	0
22100	109500	0.6667	438	0
22200	110000	0.6667	440	0
22300	110500	0.6667	442	0
22400	111000	0.6667	444	0
22500	111500	0.6667	446	0
22600	112000	0.6667	448	0
22700	112500	0.6667	450	0
22800	113000	0.6667	452	0
22900	113500	0.6667	454	0
23000	114000	0.6667	456	0
23100	114500	0.6667	458	0
23200	115000	0.6667	460	0
23300	115500	0.6667	462	0
23400	116000	0.6667	464	0
23500	116500	0.6667	466	0
23600	117000	0.6667	468	0
23700	117500	0.6667	470	0
23800	118000	0.6667	472	0
23900	118500	0.6667	474	0
24000	119000	0.6667	476	0
24100	119500	0.6667	478	0
24200	120000	0.6667	480	0
24300	120500	0.6667	482	0
24400	121000	0.6667	484	0
24500	121500	0.6667	486	0
24600	122000	0.6667	488	0
24700	122500	0.6667	490	0
24800	123000	0.6667	492	0
24900	123500	0.6667	494	0
25000	124000	0.6667	496	0





344      0.0125      37.5665  
      0.01325      37.5600  
      0.01324      37.5608  
      0.01325      37.5600  
      0.01324      37.5609  
      0.01325      37.5600  
      0.01324      37.5600  
      0.01325      37.5600  
      0.01324      37.5600  
      0.01294      37.5700  
      0.01294      37.5715  
      0.01294      37.5700  
      0.01284      37.5720  
      0.01284      37.5700  
      0.01274      37.5730  
      0.01274      37.5700  
      0.01264      37.5740  
      0.01264      37.5700  
      0.01254      37.5750  
      0.01254      37.5700  
      0.01244      37.5760  
      0.01244      37.5700  
      0.01234      37.5770  
      0.01234      37.5700  
      0.01224      37.5780  
      0.01224      37.5700  
      0.01214      37.5790  
      0.01214      37.5700  
      0.01204      37.5800  
      0.01204      37.5800  
      0.01194      37.5810  
      0.01194      37.5800  
      0.01184      37.5820  
      0.01184      37.5800  
      0.01174      37.5830  
      0.01174      37.5800  
      0.01164      37.5840  
      0.01164      37.5800  
      0.01154      37.5850  
      0.01154      37.5800  
      0.01144      37.5860  
      0.01144      37.5800  
      0.01134      37.5870  
      0.01134      37.5800  
      0.01124      37.5880  
      0.01124      37.5800  
      0.01114      37.5890  
      0.01114      37.5800





394      37 .  
0.0125      37 .  
0.0414      37 .  
0.0125      37 .  
0.0424      37 .  
0.0125      37 .  
0.0434      37 .  
0.0125      37 .  
0.0444      37 .  
0.0125      37 .  
0.0454      37 .  
0.0125      37 .  
0.0464      37 .  
0.0125      37 .  
0.0474      37 .  
0.0125      37 .  
0.0484      37 .  
0.0125      37 .  
0.0494      37 .  
0.0125      37 .  
0.0504      37 .  
0.0125      37 .  
0.0514      37 .  
0.0125      37 .  
0.0524      37 .  
0.0125      37 .  
0.0534      37 .  
0.0125      37 .  
0.0544      37 .  
0.0125      37 .  
0.0554      37 .  
0.0125      37 .  
0.0564      37 .  
0.0125      37 .  
0.0574      37 .  
0.0125      37 .  
0.0584      37 .  
0.0125      37 .  
0.0594      37 .  
0.0125      37 .  
0.0500      37 .





## APPENDIX F

```

REWIND 1
REWIND 2
READ(4,501) N,NCT,NOHTRS,NOEXP,NOCASE,NTCOEF,NODCFH,NTMPHT
NPL=N+1
READ(4,501) NTAG8 NTAG9 NTAG11
READ(4,501) NONODS NOCT NOHTR INPTAG
READ(4,505) ERR,ALPHA,MNITS,BETA(1),TOLD(1)
MAXNIT=1
NIT=0
IF(BETA(1)) NE 0 GO TO 1010
READ(4,502) (BETA(I),I=1,N)
GO TO 1030
1010 DO 1020 I=2,N
1020 BETA(I)=BETA(I-1)
C 1030 DO 15 I=1,10
INI=INPTAG(I)
IF(INI)17,17,18
17 GO TO 1,18*NTCIN
18 READ(4,502) (TCOEF(K), K=1,NTCIN)
19 GO TO 15
20 READ(4,502) (CONTMP(K), K=1,NCT)
21 READ(4,502) (COEF(M), M=1,9)
22 READ(4,502) (HTR(K), K=1,36)
23 GO TO 15
24 DO 9 L=1,N
25 ITAG(1,0)=0
26 READ(4,504) NTAG(K)
27 READ(4,502) (COEF(M), M=1,9)
28 IF(NT-9)715,K=10,NT,9
29 ITAG(K+9)=0
30 KE=K+8
31 READ(4,503) (ITAG(M), M=K ,KE)
32 READ(4,502) (COEF(M), M=K ,KE)
33 WRITE(3,556)(TAG(COEF(KK),KK=1,30)
34 CONTINUE
35 ENDFILE 1
36 REWIND 1
37 GO TO 15
38 READ(4,502) EX
39 GO TO 15
40 IF(TOLD(1)) NE 0 GO TO 1201
41 READ(4,502) (TOLD(K), K=1,N)
42 GO TO 15

```

```

1201 DO 1202 L=2 N
1202 TOLD(L) = TOLD(L-1)
14 K2 = 18 NTPMHT
15 READ(4,502) TMPMHT(K), K=1,K2)
16 GO TO 15
17 READ(4,502) BTUCRV
18 GO TO 15
19 READ(4,502) TMPCRV
20 GO TO 15
21 WRITE(8,533)INI
22 STOP(4,502) TIMCO
23 CONTINUE
24 CALL TVPAGE(0,TITLE)
25 CALL TVSOUT(N,1,TOLD,TOLD,TITLE)

C
26 WRITE(3,551)TITLE
27 WRITE(3,552)N,NCTS,NOHTRS,NOEXP,NOCASE,NTCOEF,NODCFH,NTMPHT,MONODS,
28 1 NOCT,NOHTR,MNITS,INPTAG,ERR,ALPHA
29 WRITE(3,553)IN,HEAD,(BETA(I),I=1,N)
30 WRITE(3,554)N,HEAD,(BETA(I),I=1,N)
31 HEAD=HEAD+1
32 WRITE(3,555)N,HEAD(TOLD(I),I=1,N)
33 WRITE(3,556)(CONTMP(I),I=1,NCT)
34 WRITE(3,557)24,24,21
35 IF(NOTHRS)24,24,21
36 CALL TVSHTR(NOTHRS,HTR,CASBTU,NOCONT,TOLD,NODCFH)
37 DO 107 NOD=1,N
38 107 DO 25 I=1,NP1
39 25 A(I)=0
40 READ(1)ITAG,COEF
41 DO 100 IWD=1,99
42 IF(ITAG(IWD)EQ.0) GO TO 105
43 NODEI=ITAG(IWD)
44 METHI=MOD(ITAG(IWD),10)
45 NTTH=NODEI-NONODS
46 IF(NTTH.LE.0) GO TO 55
47 NODEI=EQ.999 GO TO 50
48 NNODE=NTTH
49 NTTH=NTTH-NOCT
50 IF(NNODE=NTTH.LE.0) GO TO 60
51 NNODE=NTTH
52 NTTH=NTTH-NOHTR
53 IF(NTTH.LE.0) GO TO 49
54 IF(NTTH.GT.5) GO TO 820
55 IF(NTTH.LE.NTAG8) GO TO 815
56 WRITE(9,610) NOD, NODEI, NTAG8
57 IER=1

```

```

815 GO TO 100
     A(NP1) = A(NP1) - BTUCRV(NTTH)*COEF(IWD)
820 NTTH = NTTH - 5
     IF { NTTH.GT.5 } GO TO 830
     IF { NTTH.LE.NTAG9 } GO TO 825
     WRITE { 9,620 } NOD,NODEI,NTAG9
     IER =
     GO TO 100
825 T1 = TMPCRV(NTTH)
     GO TO 65
830 NTTH = NTTH - 5
     IF { NTTH.LE.5 } GO TO 48
     WRITE { 9,570 } NOD,NODEI
     IER =
     GO TO 100
48 IF { NTTH.LE.NTMPTH } GO TO 480
     WRITE { 9,630 } NOD,NODEI,NTMPHT
     IER =
     GO TO 100
480 WCOEF = NTTH + 1100
     CALL TVFTMP (WCOEF,TOLD(NOD),TMFHT)
     A(NP1) = A(NP1)-WCOEF*COEF(IWD)
     TMFHTV (NTTH) = WCOEF
     GO TO 100
49 IF { NNODE.LE.NOHTRS } GO TO 490
     WRITE { 9,600 } NOD,NODEI,NOHTRS
     IER =
     GO TO 100
490 LOCH = 36 + NNODE
     A(NP1) = A(NP1) - HTR(LOCH) * COEF(IWD)
     GO TO 100
50 A(NP1) = A(NP1) - COEF(IWD)
     GO TO 100
55 T1 = TOLD(NODEI)
     GO TO 65
60 IF { NNODE.LE.NCT } GO TO 61
     WRITE { 9,590 } NOD,NODEI,NCT
     IER =
     GO TO 100
61 T1 = CONTMP(NNODE)
65 T2 = TOLD(NOD)
     WCOEF = COEF(IWD)
C * *
C * * ASSUMING THE USER HAS RUN PROGRAM CHECK AND FIXED ANY WCOEFS
C * * THAT MIGHT HAVE BEEN IN ERROR. TVSSI THEREFORE WILL NOT
C * * CHECK AGAIN FOR A WCOEF > 100. NO WARNING IS PRINTED.
C * *

```

```

IF { WCOEF.LE.1000. } GO TO 73
IF { WCOEF.LE.1005. } GO TO 850
IF { WCOEF.GT.1105. } GO TO 73
ATEMP = (T1+T2)/2
LC = WCOEF - 1096.99
IF { LC.LE.NTCOEF } GO TO 840
WRITE { 9,640 } NOD,NODEI,WCOEF,NTCOEF
IER = 1
GO TO 100
840 CALL TVFTMP (WCOEF, ATEMP, TCOEF)
TCO(LC) = WCOEF
GO TO 73
850 LC = WCOEF - 999.99
IF { LC.LE.NTAG11 } GO TO 855
WRITE { 9,650 } NOD,NODEI,WCOEF,NTAG11
IER = 1
GO TO 100
855 WCOEF = TIMCO(LC)
C * THE FOLLOWING COMPUTED GO TO WILL FALL THROUGH TO THE NEXT
C * STATEMENT FOR METHODS 6,7,8,&9
C * 73 GO TO (80,730,730,80,80), METHI
730 TD = T1-T2
IF { TD.NE.0. } GO TO 731
WCOEF = 0.
GO TO 80
731 IF { ABS(TD).LT.1E-05 } TD = SIGN( 1E-05,TD )
ABSTD = ABS(TD)
GO TO (80,74,75,80,80), METHI
LC = METHI - 5
IF { LC.LE.NOEXP } GO TO 77
WRITE { 9,660 } NOD,NODEI,METHI,NOEXP
IER = 1
GO TO 100
77 T3 = EX (LC)
C * THE FOLLOWING STATEMENT EQUATES TO
C * WCOEF = WCOEF *(ABSTD * T3)/ABSTD)
C * WCOEF = WCOEF ** (T3-1.)
C * THE FOLLOWING STATEMENT EQUATES TO
C * WCOEF = WCOEF *(ABSTD * 1.25)/ABSTD
C * 74 WCOEF = WCOEF ** ABSTD ** .25

```

```

    GO TO 80
75   T3 = (T2+273.) / 100.
      WCOEF = WC0EF * ((T3**4 - T4**4) / TD )
80   IF(NODE1 - NONODS) 85,85,90
     A(NODE1) = A(NODE1) + WC0EF
     GO TO 95
90   A(NP1) = A(NP1) - WC0EF*T1
95   A(NOD) = A(NOD) - WC0EF
100  CONTINUE
105  IF(NOD-NOCASE) 107,106,107
106  A(NP1) = A(NP1) - CASBTU
107  WRITE(2)(A(K),K=1,NP1)

C * * * IF IER.NE.0 AT THIS POINT IT MEANS THERE ARE ERRORS IN THE
C * * * INPUT.TVSSI WILL SKIP THE CALCULATIONS AND RETURN TO
C * * * STATEMENT 1000 FOR ANOTHER PROBLEM.

C
C IF (IER.EQ.0) GO TO 110
C WRITE(9,670)
C GO TO 1000

C 110 ENDFILE 2
REWIND 1
REWIND 2
CALL GHOST (N, NP1, H)
ERRTAG = 0
NIT = NIT + 1
IF (NIT.LT.1) GO TO 120
CALL CBETA (N, ALPHA, BETA)
DO 130 I=1,N
IF (NIT.EQ.'1') TOLD1(I) = 0.0
TOLD2(I) = TOLD1(I)
TOLD1(I) = TOLD1(I) + BETA(I) * (H(I) - TOLD(I))
A(I) = TOLD(I) - TOLD1(I)
130 IF (ABS(A(I)) .GT. ERR) ERTAG = 1.
IF (NOHTRS) 140,140,135
CALL TVSOUP(N2,TOLD,A,TITLE)
135 LOCH = 36 + NOHTRS
CALL TVPAGE(3,TITLE)
WRITE(8,525) HTR(K), K=37,LOCH)
      526} CASBTU
140 IF (NTCOEF) 150,150,145
145 CALL TVPAGE(2,TITLE)
      528} TCO(K), K= 1,NTCOEF)

```

```

150 IF (NTMPHT) 160 160 155
155 CALL TVPAGE (2 TITLE)
      WRITE (8,529) (TMPHTV(K), K=1,NTMPHT)
      IF (NLT .GE. MAXNIT .AND. MAXNIT .GT. 0) GO TO 175
      IF (ERRTAG .GT. 0) GO TO 20
      WRITE (10,500) TITLE
      WRITE (10,501) N
      WRITE (10,680) (TOLD(I), I=1,N)
      GO TO 1000
175 DO 180 I=1,N
180 IF (BETA(I) LT .0001) BETA(I)=0.0001
      WRITE (8,530) MAXNIT, (BETA(I), I=1,N)
      GO TO 1000

C      500 FORMAT (20A4)
      501 FORMAT (18I4)
      502 FORMAT (9I8;0)
      503 FORMAT (12I16,8I8)
      504 FORMAT (12G8.0,18) 2G8.0)
      505 FORMAT (/12H HTRS WATTS , 6G12.5)
      525 FORMAT (/12H CASE WATTS , G12.5)
      526 FORMAT (/12H TEMP COEFS , 6G12.5)
      528 FORMAT (/12H TEMP HEAT , 6G12.5)
      529 FORMAT (/12H OVER , 15) 'ITERATIONS' // 'BETAS'
      530 FORMAT (0,15,15) 'SET 15, IT IS NOT ACCEPTABLE. FIX DECK AND RESUBMIT')
      533 FORMAT (1H , 20A4)
      551 FORMAT (//,N) NCT NOHTRS NOEXP NOCASE NTCOEF NODCFH NTMPHT NONO
      552 FORMAT (//,N) NCT NOHTRS MNITS /1216,/
      553 FORMAT (/,N) INPFLAG 1-10
      554 FORMAT (4,14) ERR, ALPHA, /,1017 2(1X,F11.4))
      555 FORMAT (4,14) CONTMP(I), I=1,NCT) , (/,1X,16G8.2))
      556 FORMAT (15I8) /1X,* IMPOSSIBLE NODE NUMBER - YOU SPECIFIED AN ', '
      570 FORMAT (1X,* INTERACTION FROM NODE,15 TO A NODE - 15/),
      590 FORMAT (1X,* INVALID NODE,- YOU SPECIFIED AN ', '
      1 'INTERACTION FROM NODE,15,5X,TO A NODE 15/15X,
      1 'BUT THERE ARE ONLY 14 CONSTANT TEMPERATURES')
      2 'BUT THERE ARE ONLY 15,5X,TO A NODE 15/15X,
      600 FORMAT (1X,* INVALID NODE,- YOU SPECIFIED AN ', '
      1 'INTERACTION FROM NODE,15,5X,TO A NODE 15/15X,
      2 'BUT THERE ARE ONLY 13,5X,HEATERS')
      610 FORMAT (1X,* INVALID NODE,- YOU SPECIFIED AN ', '
      1 'INTERACTION FROM NODE,15,5X,TO A NODE 15/15X,
      2 'BUT THERE ARE ONLY 13,5X,WATT CURVES (TAG 8)
      620 FORMAT (1X,* INVALID NODE,- YOU SPECIFIED AN ', '
      1 'INTERACTION FROM NODE,15,5X,TO A NODE 15/15X,
      2 'BUT THERE ARE ONLY 14, TEMPERATURE CURVES (SET 9)')

```

```

630 FORMAT ('* * * INVALID NODE, - YOU SPECIFIED AN ',
1     'INTERACTION FROM NODE', F5.5X, 'TO A NODE', F5.5X,
1     'BUT THERE ARE ONLY 4 * * * INVALID TEMP-DEPENDENT CURVES (SET 7)')
640 FORMAT ('/1X', F5.5X, 'TEMP-DEPENDENT CONDUCTANCE - NODE', F5.5X,
1     'TO NODE', F5.5X, 'YOU SPECIFIED A CONDUCTANCE OF ', F7.1, '/15X,
2     'BUT THERE ARE ONLY 3 * * * COEFF CURVES (SET 1) ')
3     COEFF CURVES (SET 1)
650 FORMAT ('/1X', F5.5X, 'INVALID CONDUCTANCE - NODE', F5.5X,
1     'TO NODE', F5.5X, 'YOU SPECIFIED A CONDUCTANCE OF ', F7.1, '/15X,
2     'BUT THERE ARE ONLY 3 * * * INVALID TIME COEFFS (SET 11) ')
660 FORMAT ('/1X', F5.5X, 'INVALID METHOD - NODE', F5.5X, 'TO NODE',
1     '15.5X, YOU SPECIFIED A METHOD OF ', I3, '/15X, BUT THERE ARE ONLY ',
2     '13.5X, UNIQUE EXPONENTS (SET 5) ')
670 FORMAT ('/1X', F5.5X, 'THERE ARE ERRORS IN YOUR INPUT FOR THIS PROBLEM',
1     '2 /10X')
2     //11)
680 FORMAT (9F8.2)
999 CONTINUE
STOP
END

```

```

C
SUBROUTINE CBETA (N, ALPHA, BETA, TN, TNM1, TNM2, ERR )
IMPLICIT REAL*4 (A-H0-Z)
DIMENSION TN(315), TNM1(315), TNM2(315), BETA(315)
DO 50 I=1,N
TM1 = TN(I) - TNM1(I)
T12 = TNM1(I) - TNM2(I)
IF ( ABS(T12) .LT. 1E-06 ) T12 = SIGN( 1E-06, T12 )
GAMMA = TM1/I
IF ( GAMMA .GT. 0. ) GO TO 10
IF ( ABS(TM1) .LE. ERR ) BETA(I) = 50
IF ( GAMMA .LT. -ALPHA ) BETA(I) = -BETA(I)*ALPHA/GAMMA
GO TO 50
10 IF ( GAMMA .GT. 1. ) GO TO 50
IF ( BETA(I) .GT. 1. ) BETA(I) = 1.
RETURN
END

C
SUBROUTINE CHOST (N, NPL, EL)
IMPLICIT REAL*4 (A-H0-Z)
LOCN(1) = 1
NM1 = N - 1
I = 0
50 READ (I+1) (EL(K), K=1, NPL)
C
10 I = I + 1

```

```

IP1 = I + 1
IF (I, J=2) EQ. 1 ) GO TO 50
DO 45 LR = LOC'S(J-1)
IF (EL(J-1) EQ. 0. ) GO TO 45
DO 40 JR = JNP1
IF (SAVE(LR) EQ. 0 ) GO TO 40
EL(JR) = EL(LR) - EL(J-1)*SAVE(LR)
40 LR = LR+1
45 CONTINUE
50 CONTINUE
51 DO 60 K = IP1 NPI
51 IF (EL(K) EQ. 0 ) / EL(I) GO TO 60
60 CON'TINUE
60 CON'TEQ(N) GO TO 80
LS = LOC'S(I)
DO 72 K = LS+NPI-1
SAVE(LS) = EL(K)
72 LS = LS + 1
GO TO 10
C   80 REWIND 2
EL(N) = EL(NPI)
DO 90 I=1,NMI
II = NP1-I
LF = N-I
LR = LOC'S(LF)+I
EL(II-1) = LSAVE(LR)
DO 90 K = II N
LR = LOC'S(LF)+K-1
IF (SAVE(LR) EQ. 0 ) II GO TO 90
EL(II-1) = EL(II-1) - SAVE(LR)*EL(K)
90 CONTINUE
RETURN
END
C   SUBROUTINE TVFTMP (COEF, T, Z)
IMPLICIT REAL*4 (A-H,O-Z) COEF)
DIMENSION TCOEF(90)
NC = CO - 1099/9
NB = 18*NC - 17
IF (T - TCOEF(NB)) 2,2,6
2 CO = TCOEF(NB+1)
6 GO TO 60
NE = NB + 16
NB = NB+2

```

```

DO 50 K=NB,NE,2      10,20,50
10 TCM2 = TCOEF(K)
      TCM1 = TCOEF(K-1)
      TCP1 = TCOEF(K+1)
      TCC = TC(TCM2)
      IC0 = ABS((TC - TCM2) * TCC) * (TCC - SIGN(1E-06 TCC))
      GO TO 60
      CO = TCOEF(K+1)
      20 CO = TCOEF(K)
      GO TO 60
      50 CONTINUE
      CO = TCOEF(NE+1)
      60 RETURN
END

C   SUBROUTINE TVSOUT(N,NA,T1,T2,TITLE)
      IMPLICIT REAL*4(A-H,O-Z),ID(12),TITLE(20)
      DIMENSION T1(315),T2(315),ID(12),TITLE(20)

      CALL TYPAGE(2,TITLE)
      WRITE(8,500)
      NL = NA+2
      DO 50 I=1,N,12
      CALL TYPAGE(1,I,NL,TITLE)
      IF(I>11-N) N5=5
      5 N5=12
      GO TO 15
      10 N5=N-I+1
      15 DO 20 K=1,N5
      20 ID(K) = I+K-1
      WRITE(8,501) ID(K), K=1,N5
      N1 = I+1
      IF(NA-1) 25,25,30
      25 WRITE(8,502) I1(K), K= I,N1
      GO TO 50
      30 WRITE(8,503) T1(K); K= I,N1
      50 WRITE(8,503) T2(K); K= I,N1
      50 CONTINUE
      RETURN

C   500 FORMAT(1HO)
      501 FORMAT(1HO NODE NO.,12I9)
      502 FORMAT(12H NEW TEMPS,12F9.2)
      503 FORMAT(12H NEW - OLD,12F9.2)
      504 FORMAT(12H ORIG TEMPS,12F9.2)
END

```

```

C      SUBROUTINE TVSHTR (NOHTRS, HTR, CASBTU, NOCONT, TOLD, NODCFH)
      IMPLICIT REAL*4 (A-H,0-Z) , NOCONT(6) , TOLD(315)
      DIMENSION HTR(42) , NOCONT(6) , TOLD(315)
      CASBTU = 0
      DO 25 K=1, NOHTRS
      LOK = 36+K
      IF (NOCONT(K)) 24, 24, 43
      43   LOK1 = NOCONT(K)
      TEMP = TOLD(LOK1)
      IF (K-3) 45, 45, 50
      45   LOK2 = 0
      GO TO 55
      50   LOK2 = 18
      55   IF (NODCFH) 3, 60
      60   IF (TEMP-HTR(2)) 65, 65, 70
      65   HTR(LOK) = HTR(LOK2+1)
      CASBTU = CASBTU + HTR(LOK2+3)
      GO TO 25
      70   NODCFH = 0
      73   IF (TEMP - HTR(LOK2+4)) 5, 5, 15
      5    HTR(LOK) = HTR(LOK2+9)
      CASBTU = CASBTU + HTR(LOK2+14)
      GO TO 25
      15   DO 16 K1=5, 8
      LOK3 = LOK2+K1
      IF (TEMP - HTR(LOK3)) 17, 17, 16
      16   CONTINUE
      HTR(LOK) = HTR(LOK2+13)
      CASBTU = CASBTU + HTR(LOK2+18)
      GO TO 25
      17   HTRL3 = HTR(LOK3) - HTR(LOK3-1)
      IF (ABS(HTRL3).LT.1E-06) HTRL3 = SIGN( 1E-06, HTRL3 )
      FRAC = (TEMP - HTR(LOK3-1))/HTRL3
      HTR(LOK) = (HTR(LOK3+5) - HTR(LOK3+4))*FRAC + HTR(LOK3+4)
      CASBTU = CASBTU + (HTR(LOK3+10) - HTR(LOK3+9))*FRAC + HTR(LOK3+9)
      GO TO 25
      24   HTR(LOK) = 0.
      25   CONTINUE
      RETURN
      END

C      SUBROUTINE TVPAGE (NL, FNAME)
      IMPLICIT REAL*4 (A-H,0-Z)
      DIMENSION FNAME(20)
      IF (NL) 10, 10, 20
      10  NPAGE = 0
      LINCNT = 75

```

```
20 LINCNT = LINCNT + NL
30 IF (LINCNT - 56) = 40,40,30
30 NPAGE = NPAGE + 1
      WRITE (8,50) FNAME, NPAGE
      LINCNT = NL
40 RETURN
50 FORMAT (1H1,20X,20A4,8X,9HPAGE NO. ,I3/)
END
/*
//LKED. SYSMOD DD DISP=SHR,DSNAME=MSS.S2323.LOADLIB
//LKED. SYSIN DD NAME TVCOUNT(R)
/*
//
```

APPENDIX G  
MODIFIED NTU14 PROGRAM NTU14BC USED TO RUN ON BATCH SYSTEM

```
//Oshare JOB (2323,0267)'NTU14BC', CLASS=B  
//      ORG=NPGVM1 2323P  
//      EXEC FORTYCL,PARM=LKED='LIST,MAP'  
//      FORT.SYSIN DD *  
C THIS IS PROGRAM NTU14  
  
C IT GENERATES AN INPUT FILE FOR THERMAL ANALYZER TO VERIFY  
C 1-4 EFFECTIVENESS-NTU RELATIONSHIP THAT IS AVAILABLE IN  
C OPEN LITERATURE.  
  
C      INTEGER O,P  
C      DIMENSION COEF(250,5) KCON(250,5) L1(8) L2(3,22) L3(6) SET(2,2,2)  
C      DCHOT(22,22) CCLD(22,22) U(22,22) SURF(22,22) THOTIN(22,22),FL4(4)  
C      2+CLDIN(22,22),TITLE(22,22),FNAME(22,22)  
  
C      CHARACTER *25 TITLE  
C      CHARACTER *25 FNAME  
  
C      DO 7 O=1,21,2  
C      P=0+1  
C      READ(1,900) CHOT(O,1),CCLD(O,2),U(O,3),SURFTO(O,4),THOTIN(O,5),TCL  
C      1DIN(O,6)  
C      900 FORMAT(2F10.0,F10.5,3F10.0)  
C      READ(1,918) TITLE(P,1),FNAME(P,2)  
C      918 FORMAT(2A2)  
  
C      OPEN OUTPUT FILE  
C      OPEN(2,FILE=FNAME(P,2),FORM='FORMATTED')  
  
C      VALK1 = CHOT(0,1)  
C      VALK2 = CCLD(0,2)  
C      VALK3 = U(0,3)*SURFTO(0,4)/200.  
C      TINIT = 12.5.  
C      FRONT END  
  
C      L1(1) = 250  
C      L1(2) = 2  
C      DO 10 L1(1) = 1-3,8  
C      10 L1(1) = 0
```

```

C      DO 20 I=1,3
C      L3(1) = 300
C      L3(2) = 50
C      L3(3) = 6
C      L3(4) = 4
C      L3(5) = 6
C      L3(6) = 6
C
C      FL4(1) = .05
C      FL4(2) = .66667
C      FL4(3) = .8
C      FL4(4) = .12
C      L4 = 12
C
C      CONSTANT TEMPERATURES
C      SET2(1) = THOTIN(0,5)
C      SET2(2) = TCOLDIN(0,6)
C
C      READY FOR INPUT SET 4
C      NODE 1
C
C      KCON(1,1) = 514
C      KCON(1,2) = 1504
C      KCON(1,3) = 1514
C      KCON(1,4) = 2504
C      KCON(1,5) = 3015
C      COEF(1,1) = YALK1
C      DO 50 I=1,4
C      COEF(I,1) = VALK3
C
C      NODES 2 TO 50
C      DO 75 I = 2,50
C      J = I+50
C      K = 151-I
C      L = 150+I
C      M = 251-I
C      N = I-1
C
C      KCON(1,1) = 10*N+5
C      KCON(1,2) = 10*J+4
C      KCON(1,3) = 10*K+4
C      KCON(1,4) = 10*L+4
C      KCON(1,5) = 10*M+4

```

```

COEF{I,1} = VALK1
DO 80 I=1,1
COEF(I,I) = VALK3
80 CONTINUE
75 CONTINUE

C NODE 51
C KCON{51,1} = 3025
C KCON{51,2} = 14
C COEF{51,1} = VALK2
C COEF{51,2} = VALK3
C NODES 52 TO 250
C DO 120 I = 52,250
C   K=I-1
C   IF(I>100) GO TO 122
C   J=I-50
C   GO TO 135
C 122 IF(I>150) GO TO 124
C   L=I-100
C   M=M+50
C   J=I-50
C   GO TO 135
C 124 IF(I>200) GO TO 126
C   J=I-150
C   GO TO 135
C 126 CONTINUE
C   L=I-200
C   M=M+150
C   J=I-N
C   KCON{I,1} = 10*j + 4
C   KCON{I,2} = 10*k + 5
C   COEF{I,1} = VALK3
C   COEF{I,2} = VALK2
C 120
C END OF DATA SETUP
C NOW CREATE INPUT FOR ANALYZER
C   WRITE(2,919) TITLE(P,1)
919  FORMAT(2,1X,4)5
C   WRITE(2,908){L1(I), I=1,8)
908  FORMAT(2,914){L2(I), I=1,3)
C   WRITE(2,908){L3(I), I=1,6}

```

```

      WRITE(2,911) FL4(1),FL4(2),L4,FL4(3),FL4(4)
911   FORMAT(2,F8.3,F8.5,F8.1,2F8.1,2F8.1)
      WRITE(2,912) SET2(1),SET2(2)
912   FORMAT(2F8.0)
C     DO 200 I=50
      WRITE(2,913) KCON(I,J),J=1,5
913   FORMAT(2,913)
      WRITE(2,914) COEF(I,J),J=1,5
914   FORMAT(5F8.4)
200   CONTINUE
C     DO 250 I=51,250
      WRITE(2,913) KCON(I,1),KCON(I,2)
      WRITE(2,914) COEF(I,1),COEF(I,2)
250   CONTINUE
C     7  CONTINUE
      STOP
END
/*
//LKED.SYSLMOD DD DISP=SHR,DSNAME=MSS.S2323.LOAD
//NAME NTU14(R)
/*
//
```

## APPENDIX H

### NTNU LIBRARY BATCH PROGRAM

```

NTU=0.250 R=0.10 25.04 0.833333 15. 200. 100.
NTU=0.250 R=0.10 25.04 1.TVSSDA,SPACED 15. 200. 100.
NTU=0.750 R=0.10 NTU14 1.TVSSDA,SPACED 15. 200. 100.
NTU=1.000 R=0.10 NTU14 1.66667 15. 200. 100.
NTU=1.250 R=0.10 NTU14 2.08333E 15. 200. 100.
NTU=1.250 R=0.10 NTU14 2.TVSSDA,SPACED 15. 200. 100.
NTU=1.500 R=0.10 NTU14 2.50000 15. 200. 100.
NTU=1.500 R=0.10 NTU14 3.33333 15. 200. 100.
NTU=2.000 R=0.10 NTU14 4.TVSSDA,SPACED 15. 200. 100.
NTU=2.000 R=0.10 NTU14 4.16667 15. 200. 100.
NTU=2.500 R=0.10 NTU14 5.TVSSDA,SPACED 15. 200. 100.
NTU=2.500 R=0.10 NTU14 5.00000 15. 200. 100.
NTU=3.000 R=0.10 NTU14 5.TVSSDA,SPACED 15. 200. 100.
NTU=3.25 R=0.10 NTU14 5.41667 15. 200. 100.

//STEPA EXEC FORTVG PROG=TVCOUNT, LIB='MSS;S2323.LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT03F001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSSIA
//GO.FT04F001 DD SYSDOUT=A,DCB=RECFM=FBA
//GO.FT08F001 DD FORTVG PROG=TVCOUNT,LIB='MSS;S2323.LOADLIB'
STE.PB EXEC STE.PC
//GO.FT01F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT03F001 DD DUMMY
//GO.FT04F001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSSIB
//GO.FT08F001 DD SYSDOUT=A,DCB=RECFM=FBA
STE.PC EXEC STE.PD
//GO.FT01F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT10F001 DD DUMMY
//GO.FT03F001 DD DUMMY
//GO.FT04F001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSSIC
//GO.FT08F001 DD SYSDOUT=A,DCB=RECFM=FBA
STE.PD EXEC STE.PC
//GO.FT01F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT10F001 DD DUMMY
//GO.FT04F001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSSIC
//GO.FT08F001 DD SYSDOUT=A,DCB=RECFM=FBA
STE.PC EXEC STE.PD
//GO.FT01F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA,SPACE=(CYL,(1,1))
//GO.FT10F001 DD DUMMY

```

```

// GO .FT03FO01 DD DUMMY
// GO .FT04FO01 DD DISP=(OLD,DELETE) UNIT=SYSDA, DSN=&TVSSID
// GO .FT08FO01 DD SYSOUT=A,DCB=RECFM=FBA, LIB='MSS S2323 .LOADLIB'
// GO .STEPE EXEC FORTVG PROG=TVCOUNT,UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT01FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT02FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT09FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT10FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT03FO01 DD DUMMY
// GO .FT04FO01 DD DISP=(OLD,DELETE) UNIT=SYSDA, DSN=&TVSSIE
// GO .FT08FO01 DD SYSOUT=A,DCB=RECFM=FBA, LIB='MSS S2323 .LOADLIB'
// GO .STEPE EXEC FORTVG PROG=TVCOUNT,UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT01FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT02FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT09FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT10FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT03FO01 DD DUMMY
// GO .FT04FO01 DD DISP=(OLD,DELETE) UNIT=SYSDA, DSN=&TVSSIF
// GO .FT08FO01 DD SYSOUT=A,DCB=RECFM=FBA, LIB='MSS S2323 .LOADLIB'
// GO .STEPE EXEC FORTVG PROG=TVCOUNT,UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT01FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT02FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT09FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT10FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT03FO01 DD DUMMY
// GO .FT04FO01 DD DISP=(OLD,DELETE) UNIT=SYSDA, DSN=&TVSSIG
// GO .FT08FO01 DD SYSOUT=A,DCB=RECFM=FBA, LIB='MSS S2323 .LOADLIB'
// GO .STEPE EXEC FORTVG PROG=TVCOUNT,UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT01FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT02FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT09FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT10FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT03FO01 DD DUMMY
// GO .FT04FO01 DD DISP=(OLD,DELETE) UNIT=SYSDA, DSN=&TVSSIH
// GO .FT08FO01 DD SYSOUT=A,DCB=RECFM=FBA, LIB='MSS S2323 .LOADLIB'
// GO .STEPE EXEC FORTVG PROG=TVCOUNT,UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT01FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT02FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT09FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT10FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT03FO01 DD DUMMY
// GO .FT04FO01 DD DISP=(OLD,DELETE) UNIT=SYSDA, DSN=&TVSSII
// GO .FT08FO01 DD SYSOUT=A,DCB=RECFM=FBA, LIB='MSS S2323 .LOADLIB'
// GO .STEPE EXEC FORTVG PROG=TVCOUNT,UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT01FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT02FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT09FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
// GO .FT10FO01 DD UNIT=SYSDA,SPACE={CYL,{1,1}}

```

```
//GO .FT03F001 DD DUMMY  
//GO .FT04F001 DD DISP=(OLD,DELETE) UNIT=SYSDA,DSN=&TVSSIJ  
//GO .FT08F001 DD SYSPUT=A,DCB=RECFM=M=FBA,  
//STEPK EXEC FORTYG PROG=TVCOUNT,LIB=MSS,S2323,LOADLIB,  
//GO .FT01F001 DD UNIT=SYSDA,SPACE=(CYL,{1,1})  
//GO .FT02F001 DD UNIT=SYSDA,SPACE=(CYL,{1,1})  
//GO .FT09F001 DD UNIT=SYSDA,SPACE=(CYL,{1,1})  
//GO .FT10F001 DD UNIT=SYSDA,SPACE=(CYL,{1,1})  
//GO .FT03F001 DD DUMMY  
//GO .FT02F001 DD DUMMY  
//GO .FT04F001 DD DISP=(OLD,DELETE) UNIT=SYSDA,DSN=&TVSSIK  
//GO .FT08F001 DD SYSPUT=A,DCB=RECFM=M=FBA
```

APPENDIX I  
 MODIFIED NTU32C PROGRAM NTU32CC USED TO RUN ON BATCH SYSTEM

```

//<OHARE JOB (2323 0267)'NTU32CC' CLASS=G
//<MAIN ORG=NPGVM1 2323P SYSTEM=SY2
//<EXEC FORTVCL PARM=LKD LIST.MAP
//<FORT.SYSIN DD * THIS IS PROGRAM NTU32C

C C IT GENERATES AN INPUT FILE FOR THERMAL ANALYZER TO OBTAIN
C C 1-3 EFFECTIVENESS-NTU RELATIONSHIP THAT IS NOT AVAILABLE IN
C C OPEN LITERATURE (2C MEANING ONE PARALLEL PASS AND TWO
C C COUNTERFLOW PASSES).

C C INTEGER O,P
C C DIMENSION COEF(200 5) KCON(200 5) L1(8)
C C 1 CHOT(22 22) CCLD(22 22) U(22 22) L2(3) L3(6)
C C 2 fCLDIN(22,22),TITLE(22,22),FNAME{22,22},THOTIN{22,22}FL4(4)

C C CHARACTER *25 TITLE
C C CHARACTER *25 FNAME

C C DO 7 O=1,21,2
C C P=O+1
C C READ(1 900) CHOT(O,1),CCLD(O,2),U(O,3),SURFTO(O,4),THOTIN(O,5),TCL
C C 1 DIN(O 6)
C C 900 FORMAT(2F10.0 F10.5,3F10.0)
C C READ(1 918) TITLE(P,1),FNAME(P,2)
C C 918 FORMAT(2A25)

C C OPEN OUTPUT FILE
C C OPEN(2,FILE=FNAME(P,2),FORM='FORMATTED')

C C VALK1 = CHOT(O,1)
C C VALK2 = CCLD(O,2)
C C VALK3 = U(O,3)*SURFTO(O,4)/150.
C C TINIT = 125.

C C FRONT END

C C L1(1) = 200
C C L1(2) = 2
C C DO 10 I=3,8

```

```

      10 L1(I) = 0
C      DO 20 L2(I) = 0
C      L3{1} = 300
C      L3{2} = 50
C      L3{3} = 6
C      L3{4} = 2
C      L3{5} = 4
C      L3{6} = 6
C      FL4{1} = .05
C      FL4{2} = .66667
C      FL4{3} = .8
C      FL4{4} = tINIT
C      L4 = 12
C
C      CONSTANT TEMPERATURES
C      SET2{1} = THOTIN(0,5)
C      SET2{2} = TCOLDIN(0,6)
C
C      READY FOR INPUT SET 4
C      NODE 1
C      KCON{1,1} = 1004
C      KCON{1,2} = 1014
C      KCON{1,3} = 2004
C      KCON{1,4} = 3015
C      COEF{1,4} = VALK1
C      DO 50 I = 1,3
C      COEF(I,I) = VALK3
C
C      NODES 2 TO 50
C      DO 75 I = 2,50
C      J = 101 - I
C      K = 100 + I
C      L = 201 - I
C      N = I - 1
C      KCON{I,1} = 10*N + 5
C      KCON{I,2} = 10*J + 4
C      KCON{I,3} = 10*K + 4
C      KCON{I,4} = 10*L + 4
C      COEF{I,1} = VALK1
C      DO 80 I = 2,4

```

```

      COEF(I,I,I) = VALK3
      80 CONTINUE
      C NODE 51
      C   KCON(51,1) = 3025
      C   KCON(51,2) = 504
      C   COEF(51,1) = VALK2
      C   COEF(51,2) = VALK3
      C   NODES 52 TO 200
      C   DO 120 I = 52,200
      C   K=I-L
      C   IF(I.GT.100) GO TO 122
      C   L=I-50
      C   M=2*L-1
      C   J=I-M
      C   GO TO 135
      C   122 IF(I.GT.150) GO TO 124
      C   J=I-100
      C   GO TO 135
      C   124 L=I-150
      C   M=2*L-1
      C   J=I-M-100
      C   135 KCON(I,1) = 100J + 4
      C   KCON(I,2) = 100J + 5
      C   COEF(I,1) = VALK3
      C   COEF(I,2) = VALK2
      C   120
      C   END OF DATA SETUP
      C   NOW CREATE INPUT FOR ANALYZER
      C   919 WRITE(2,919) TITLE(P,1)
      C   908 FORMAT(1X,A)5
      C   908 WRITE(2,908)(L1(I),I=1,8)
      C   908 FORMAT(2,908){L2{I},I=1,3}
      C   908 WRITE(2,908){L3{I},I=1,6}
      C   908 WRITE(2,908){L4{I},I=1,2}
      C   911 FORMAT(2,F8.3,F8.5,F8.2,F8.4) FL4(3),FL4(4)
      C   911 WRITE(2,911){SET2(1),SET2(2)}
      C   912 FORMAT(2F8.0)
      C   913 DO 200 I=1,50
      C   913 WRITE(2,913)(KCON(I,J),J=1,4)

```

```
914  WRITE(2,914){COEF(I,J),J=1,4)
200  CONTINUE
C   DO 250 I=51 200
      WRITE(2,913) KCON{I,1},KCON{I,2}
      WRITE(2,914) COEF{I,1},COEF{I,2}
250  CONTINUE
C   7  CONTINUE
      STOP
      END
/*
//LKED.SYSLMOD DD* DISP=SHR,DSNAME=MSS . S2323 . LOADLIB
//LKED.SYSIN DD*
      NAME COUNTER(R)
/*
//
```

## APPENDIX J

### NTU32CL LIBRARY BATCH PROGRAM

```

100. 250. R=0.40 COUNTER 100.0 3. 333333 C
NTU=0. 250. R=0.40 COUNTER 100.0 5. 00000 D
NTU=0. 250. R=0.40 COUNTER 100.0 6. 66667 D
NTU=1. 250. R=0.40 COUNTER 100.0 6. 66667 E
NTU=1. 250. R=0.40 COUNTER 100.0 8. 33333 E
NTU=1. 250. R=0.40 COUNTER 100.0 10. 00000 F
NTU=1. 250. R=0.40 COUNTER 100.0 10. 00000 G
NTU=1. 250. R=0.40 COUNTER 100.0 13. 33333 G
NTU=2. 250. R=0.40 COUNTER 100.0 13. 33333 H
NTU=2. 250. R=0.40 COUNTER 100.0 16. 66666 H
NTU=2. 250. R=0.40 COUNTER 100.0 20. 00000 I
NTU=2. 250. R=0.40 COUNTER 100.0 21. 66666 J
NTU=3. 250. R=0.40 COUNTER 100.0 21. 66666 K
NTU=3. 250. R=0.40 COUNTER 100.0 21. TYSSTIK

//STEPA EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323 . LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD DISPP=(OLD, DELETE) UNIT=SYSDA, DSN=&TVSSIA
//GO.FT04F001 DD SYSSOUT=A, DCB=RECFM=FBA
//GO.FT08F001 DD FORTVG PROG=TVCOUNT, LIB='MSS S2323 . LOADLIB'
//STEPB EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323 . LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD DISPP=(OLD, DELETE) UNIT=SYSDA, DSN=&TVSSIB
//GO.FT04F001 DD SYSSOUT=A, DCB=RECFM=FBA
//STEPD EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323 . LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD DISPP=(OLD, DELETE) UNIT=SYSDA, DSN=&TVSSIC
//GO.FT04F001 DD SYSSOUT=A, DCB=RECFM=FBA
//STEPF EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323 . LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))

```



```
//GO.FT03F001 DD DUMMY  
//GO.FT04F001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSSIJ  
//GO.FT08F001 DD DCB=RECFM=FBA  
//STEPK EXEC PGM=TVG  
//STEPK F01F001 PROG=TCOUNT,LIB=MSS:S2323.LOADLIB  
//STEPK F01F001 UNIT=SYSDA,SPACE=(CYL,{1,1})  
//STEPK F02F001 UNIT=SYSDA,SPACE=(CYL,{1,1})  
//STEPK F03F001 UNIT=SYSDA,SPACE=(CYL,{1,1})  
//STEPK F04F001 UNIT=SYSDA,SPACE=(CYL,{1,1})  
//STEPK F05F001 DD DUMMY  
//STEPK F06F001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSSIK  
//STEPK F07F001 DD SYSSOUT=A,DCB=RECFM=FBA  
//STEPK F08F001 DD
```

## APPENDIX K

MODIFIED NTU32P PROGRAM NTU32PC USEB TO RUN ON BATCH SYSTEM

```

//OH32PC JOB (2323,0267) 'NTU32PC' CLASS=G
//MAIN   ORG=NPGVM1 2323 P SYSTEM=SY2
//EXEC FORTVCL PARM=LKD=LIST,MAP,
//FORT.SYSIN DD * THIS IS PROGRAM NTU32P

C IT GENERATES AN INPUT FILE FOR THERMAL ANALYZER TO OBTAIN
C 1-3 EFFECTIVENESS-NTU RELATIONSHIP THAT IS NOT AVAILABLE IN
C OPEN LITERATURE {2P MEANING TWO PARALLEL PASSES AND ONE
C COUNTERFLOW PASS} .
C
C INTEGER 0,P
C DIMENSION COEF(200,5) KCON(200,5) L1(8) L2(3,22) L3(6) SET2(2,22),FL4(4)
C 1,CHOT(22,22) CCLD(22,22) U(22,22) SURF(22,22),THOTIN(0,5),TCL
C 2,TCLDIN(22,22),TITLE(22,22),FNAME(22,22)
C
C CHARACTER *25 TITLE
C CHARACTER *25 FNAME
C
C DO 7 0=1,21,2
C P=0+1
C READ(1,900) CHOT(0,1),CCLD(0,2),U(0,3),SURFTO(0,4),THOTIN(0,5),TCL
C 1,DIN(0,6)
C 900 FORMAT(2F10.0,F10.5,3F10.0)
C READ(1,918) TITLE(P,1),FNAME(P,2)
C 918 FORMAT(1A25)
C
C OPEN OUTPUT FILE
C
C OPEN(2,FILE=FNAME(P,2),FORM='FORMATTED')
C
C VALK1 = CHOT(0,1)
C VALK2 = CCLD(0,2)
C VALK3 = U(0,3)*SURFTO(0,4)/150.
C TINIT = 125.
C
C FRONT END
C
C L1(1) = 200
C L1(2) = 2
C DO 10 I=3,8

```

```

      10 L1(I) = 0
C     DO 20 L2(I) = 1-1,3
C     C   L3{1} = 300
C   L3{2} = 50
C   L3{3} = 6
C   L3{4} = 2
C   L3{5} = 4
C   L3{6} = 6
C
C   FL4{1} = .05
C   FL4{2} = .66667
C   FL4{3} = .8
C   FL4{4} = TINIT
C   L4 = 12
C
C   CONSTANT TEMPERATURES
C   SET2{1} = THOTIN{0,5}
C   SET2{2} = TCOLDIN{0,6}
C
C   READY FOR INPUT SET 4
NODE 1
KCON{1,1} = 514
KCON{1,2} = 1504
KCON{1,3} = 1514
KCON{1,4} = 3015
COEF{1,4} = VALK1
DO 50 I=1,3
  COEF{1,I} = VALK3
  NODES 2 TO 50
  DO 75 I = 2,50
    J = I + 50
    K = 151 - I
    L = 150 + I
    N = I - 1
    KCON{I,1} = 10*N + 5
    KCON{I,2} = 10*J + 4
    KCON{I,3} = 10*K + 4
    KCON{I,4} = 10*L + 4
    COEF{I,1} = VALK1
    DO 80 I = 2,4

```

```

      COEF(I,I) = VALK3
80  CONTINUE
C   NODE 51
C     KCON(51,1) = 3025
C     KCON(51,2) = 14
C     COEF(51,1) = VALK2
C     COEF(51,2) = VALK3
C   NODES 52 TO 200
      DO 120 I = 52,200
      K = I - 1
      IF(I.GT.100) GO TO 122
      J = I - 50
      GO TO 135
122  IF(I.GT.150) GO TO 124
      L = I - 100
      M = 2*L - 1
      N = M + 50
      J = I - N
      GO TO 135
124  J = I - 150
135  KCON(I,1) = 10*j + 4
      KCON(I,2) = 10*k + 5
      COEF(I,1) = VALK3
      COEF(I,2) = VALK2
C   END OF DATA SETUP
C   NOW CREATE INPUT FOR ANALYZER
      WRITE(2,919) TITLE(P,1)
919  FORMA(1,XA5)(L1(I),I=1,8)
      WRITE(2,908)(L2(I),I=1,3)
908  FORMA(2,914)(L3(I),I=1,6)
      WRITE(2,908)(L4(I),I=1,2)
      FORMA(2,911)(F85,F85,L4(2),FL4(3),FL4(4))
      WRITE(2,912)(F83,F83,SET2(1),SET2(2))
911  FORMAT(2,912)
912  FORMAT(2,918,0)
      DO 200 I = 1,50
      WRITE(2,913)(KCON(I,J),J=1,4)
913  FORMA(2,918)(COEF(I,J),J=1,4)
      WRITE(2,914)(COEF(I,J),J=1,4)

```

```
914 FORMAT(4F8.4)
200 CONTINUE
C      DO 250 I=51   200
      WRITE(2,913) KCON(I,1),KCON(I,2)
      WRITE(2,914) COEF(I,1),COEF(I,2)
250 CONTINUE
C      CONTINUE
      STOP
      END
      /*
//LKED.SYSLMOD DD DISP=SHR,DSNAME=MSS.S2323.LOADLIB
//LKED.SYSIN  DD NAME=PARALLEL(R)
/*
//
```

APPENDIX L  
**NTU32PL LIBRARY BATCH PROGRAM**

```

//QH2PL JOB (2323,0267) 'NTU32PL', CLASS=P
//*MAIN ORG=NPGVM1:2323 J3P
//*FORMAT PR DDNAME= DEST=LOCAL
//*EXEC FORIVG PROG='PARALLEL LIB= 'MSS.S2323.LOADLIB'
//GO.TVSSIL
//DD DISP=(NEW,PASS) DSN=&TVSSIL,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIM,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIN,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSI0,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSI1P,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIQ,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSR,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIS,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIT,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIU,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//DD DISP=(NEW,PASS) DSN=&TVSSIV,
//UNIT=SYSDA,SPACE=(CYL,(2,2))ZER=6160)
//DCB=(RECFM=FB,LRECL=80,BLKSIZE=6160)
//GO.FT01F001 DD *
//250 150 0 0.50000 15. 200.
//NTU=0.05 R=0.60 COUNTER TVSSIA
//250 150 0 2.50000 15. 200.
//NTU=0.25 R=0.60 COUNTER TVSSIB
//100. 100.

```

```

NTU=0 250 R=0 .60 COUNTER 150.0 5.00000 15. 200. 100.
NTU=0 250 R=0 .60 COUNTER 150.0 5.00000 15. 200. 100.
NTU=0 250 R=0 .60 COUNTER 150.0 10.00000 15. 200. 100.
NTU=1 250 R=0 .60 COUNTER 150.0 12.50000 15. 200. 100.
NTU=1 250 R=0 .60 COUNTER 150.0 15.00000 15. 200. 100.
NTU=1 250 R=0 .60 COUNTER 150.0 20.00000 15. 200. 100.
NTU=2 250 R=0 .60 COUNTER 150.0 25.00000 15. 200. 100.
NTU=2 250 R=0 .60 COUNTER 150.0 30.00000 15. 200. 100.
NTU=3 250 R=0 .60 COUNTER 150.0 32.50000 15. 200. 100.
NTU=3 250 R=0 .60 COUNTER 150.0 35.00000 15. 200. 100.

//STEP1 EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323.LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT04F001 DD DISP=(OLD,DELETE), UNIT=SYSDA, DSN=&TVSSIL
//GO.FT05F001 DD SYSOUT=A, DCB=RECFM=FBA, LIB='MSS S2323.LOADLIB'
STEP1 EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323.LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT04F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT05F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT06F001 DD DISP=(OLD,DELETE), UNIT=SYSDA, DSN=&TVSSIM
//GO.FT07F001 DD SYSOUT=A, DCB=RECFM=FBA, LIB='MSS S2323.LOADLIB'
STEPN EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323.LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT04F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT05F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT06F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT07F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT08F001 DD DISP=(OLD,DELETE), UNIT=SYSDA, DSN=&TVSSIN
//GO.FT09F001 DD SYSOUT=A, DCB=RECFM=FBA, LIB='MSS S2323.LOADLIB'
STEP0 EXEC FORTVG PROG=TVCOUNT, LIB='MSS S2323.LOADLIB'
//GO.FT01F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT02F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT03F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT04F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT05F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT06F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT07F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT08F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT09F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))
//GO.FT10F001 DD UNIT=SYSDA, SPACE=(CYL,(1,1))

```

```

//GO.FT03F0001 DD DUMMY
//GO.FT04F0001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSS10
//GO.FT08F0001 DD SYSCNT,LIB=MSS,S2323.LOADLIB'
//STE.PP EXEC FORTVG PROG=SYSDA,SPACE={CYL,{1,1}}
//GO.FT01F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT02F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT09F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT10F0001 DD DUMMY
//GO.FT03F0001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSS10
//GO.FT04F0001 DD SYSCNT,LIB=FBA
//GO.FT08F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//STE.PC EXEC FORTVG PROG=SYSDA,SPACE={CYL,{1,1}}
//GO.FT01F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT02F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT09F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT10F0001 DD DUMMY
//GO.FT03F0001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSS10
//GO.FT04F0001 DD SYSCNT,LIB=FBA
//GO.FT08F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//STE.PR EXEC FORTVG PROG=SYSDA,SPACE={CYL,{1,1}}
//GO.FT01F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT02F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT09F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT10F0001 DD DUMMY
//GO.FT03F0001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSS10
//GO.FT04F0001 DD SYSCNT,LIB=FBA
//GO.FT08F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//STE.PR EXEC FORTVG PROG=SYSDA,SPACE={CYL,{1,1}}
//GO.FT01F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT02F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT09F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT10F0001 DD DUMMY
//GO.FT03F0001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSS10
//GO.FT04F0001 DD SYSCNT,LIB=FBA
//GO.FT08F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//STE.PT EXEC FORTVG PROG=SYSDA,SPACE={CYL,{1,1}}
//GO.FT01F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT02F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT09F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT10F0001 DD DUMMY
//GO.FT03F0001 DD DISP=(OLD,DELETE),UNIT=SYSDA,DSN=&TVSS10
//GO.FT04F0001 DD SYSCNT,LIB=FBA
//GO.FT08F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//STE.PU EXEC FORTVG PROG=SYSDA,SPACE={CYL,{1,1}}
//GO.FT01F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT02F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT09F0001 DD UNIT=SYSDA,SPACE={CYL,{1,1}}
//GO.FT10F0001 DD DUMMY

```

```
//GO . FT03F001 DD DUMMY  
//GO . FT04F001 DD DISP=(OLD, DELETE), UNIT=SYSDA, DSN=&TVSSIU  
//GO . FT08F001 DD SYSPUT=A, DCB=RECFM=FBA  
//STE.PV EXEC FORTVG PROG='TVCOUNT', LIB='MSS.S2323.LOADLIB'  
//GO . FT01F001 DD UNIT=SYSDA, SPACE={CYL,{1,1}}  
//GO . FT02F001 DD UNIT=SYSDA, SPACE={CYL,{1,1}}  
//GO . FT09F001 DD UNIT=SYSDA, SPACE={CYL,{1,1}}  
//GO . FT10F001 DD UNIT=SYSDA, SPACE={CYL,{1,1}}  
//GO . FT03F001 DD DUMMY  
//GO . FT04F001 DD DISP=(OLD, DELETE), UNIT=SYSDA, DSN=&TVSSIV  
//GO . FT08F001 DD SYSPUT=A, DCB=RECFM=FBA
```

APPENDIX M

1-3:2C EFFECTIVENESS VS.  $N_{tu}$  GRAPHS AT VARIOUS R VALUES

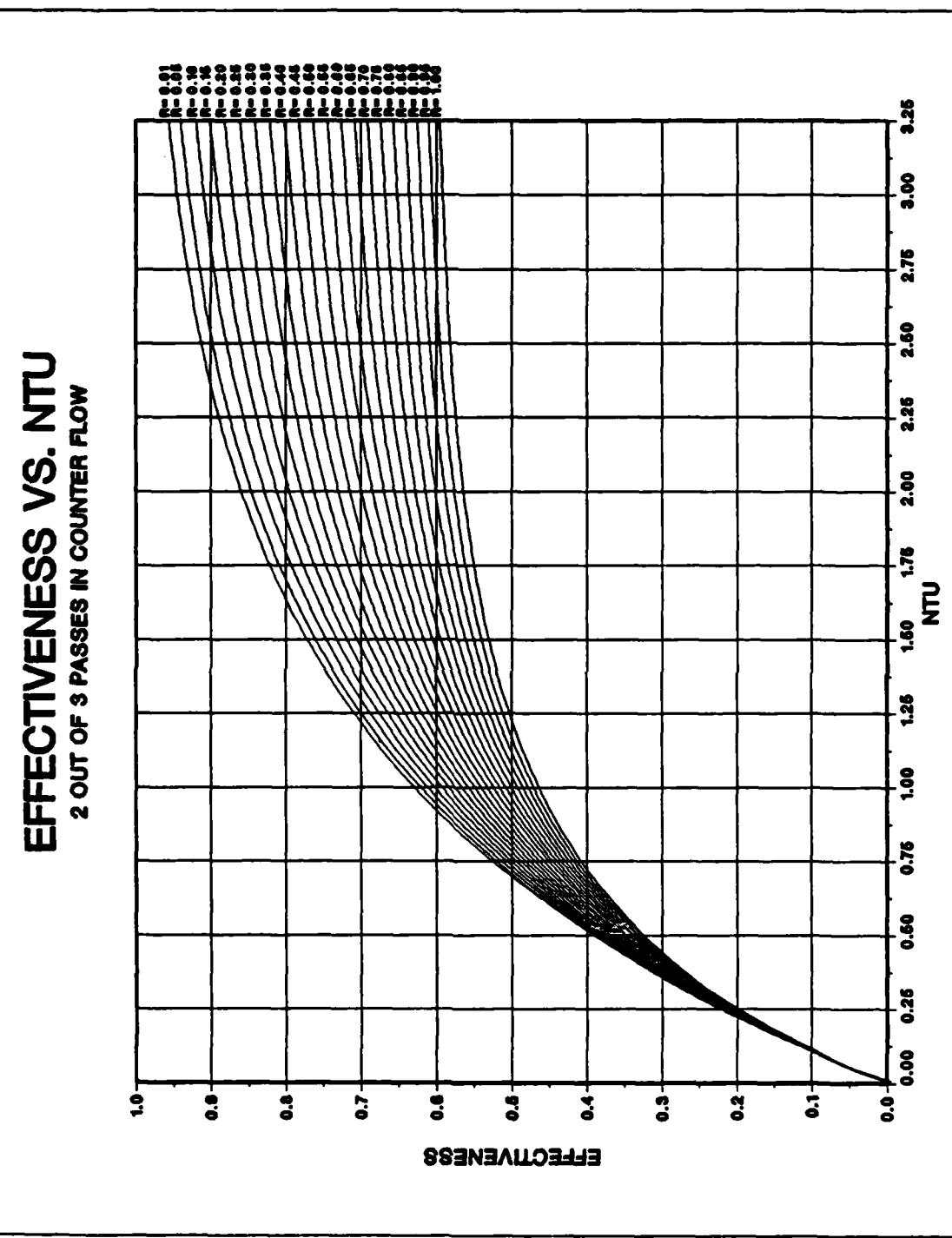


Figure M.1 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of  $R$  from 0.01 to 1.0

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .01 TO 0.1

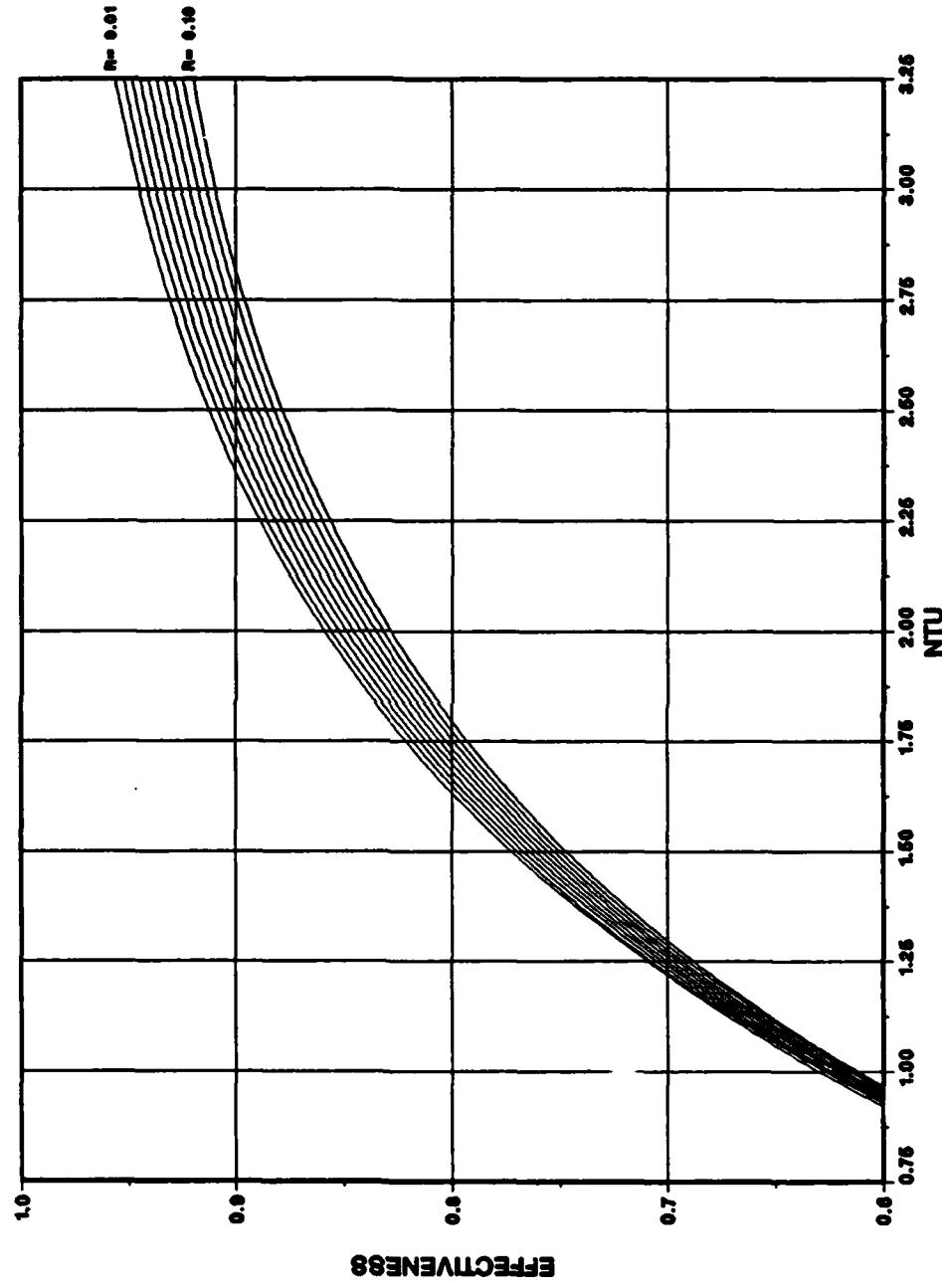


Figure M.2 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.01 to 0.10

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .11 TO 0.2

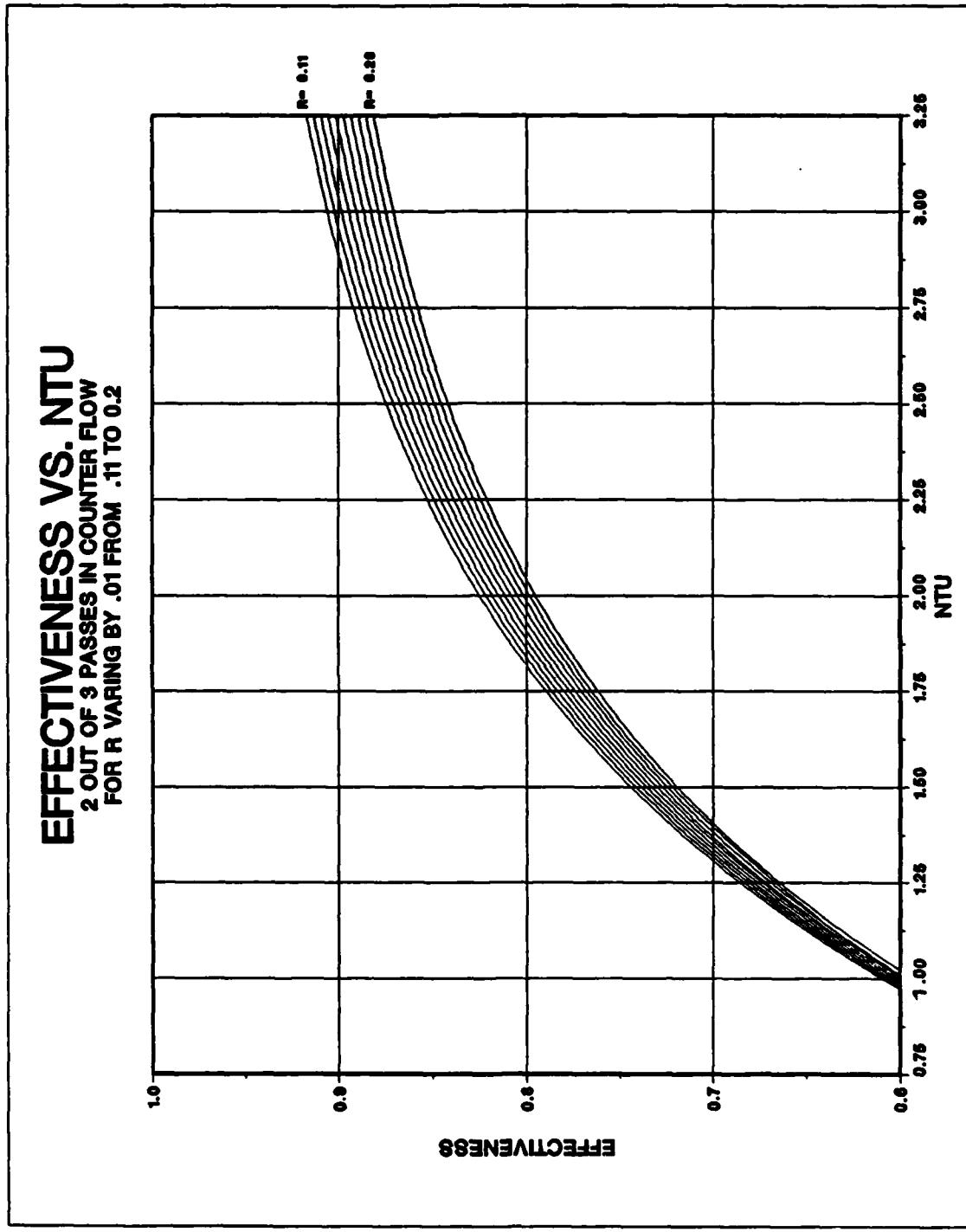


Figure M.3 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.11 to 0.2

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .21 TO 0.3

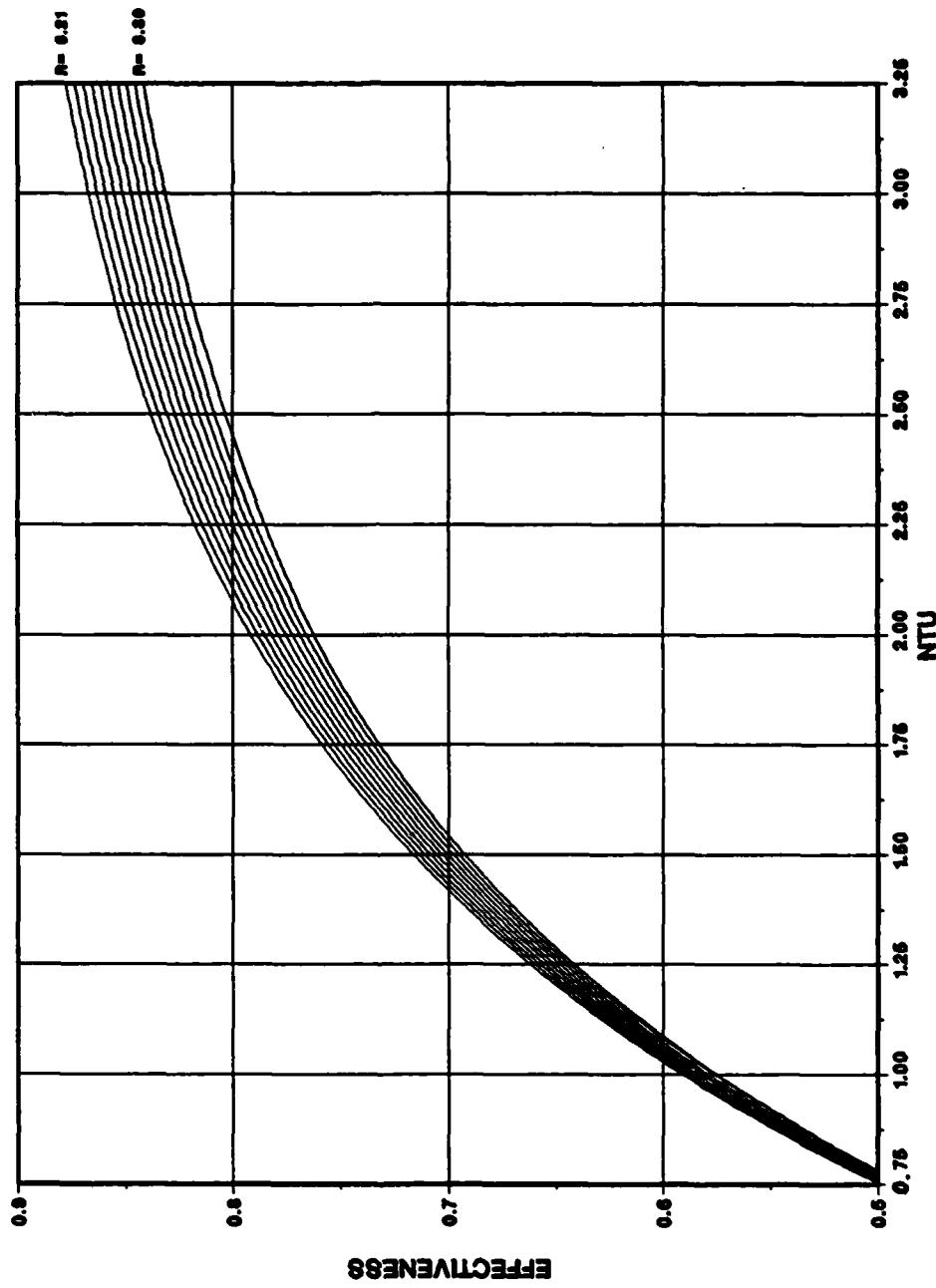


Figure M.4 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.21 to 0.3

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .31 TO 0.4

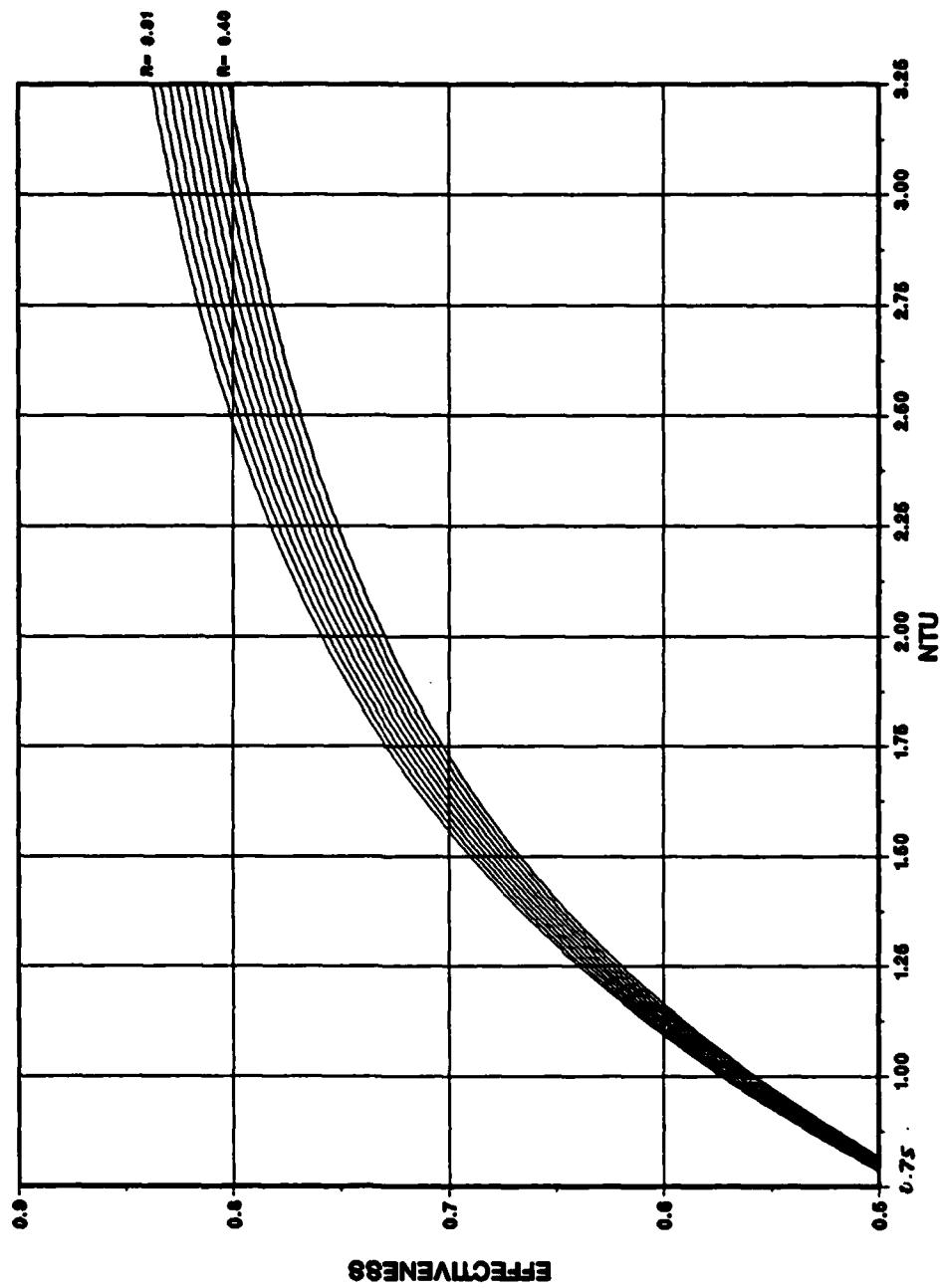


Figure M.5 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.31 to 0.4

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .41 TO 0.5

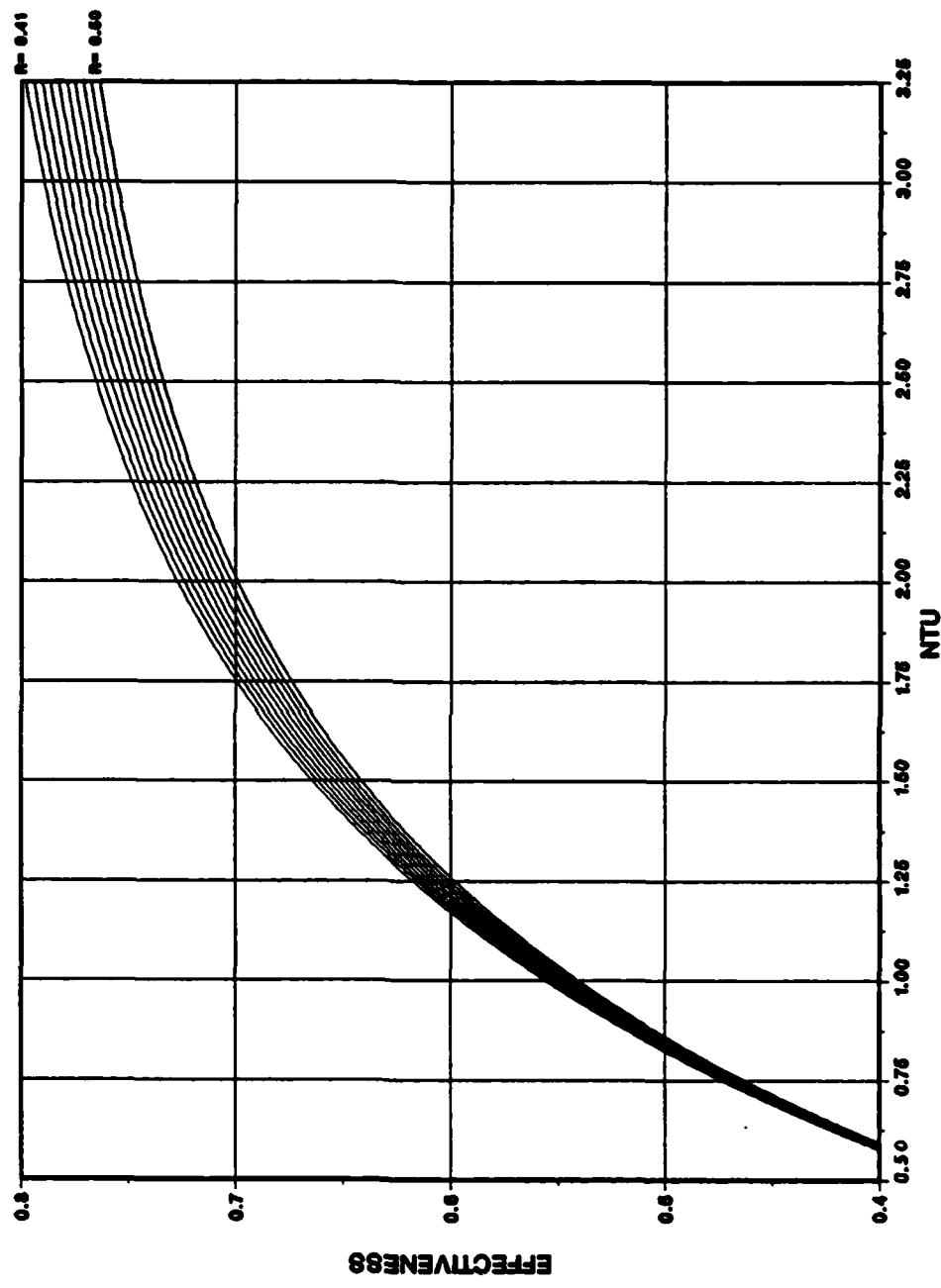


Figure M.6 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.41 to 0.5

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .51 TO 0.6

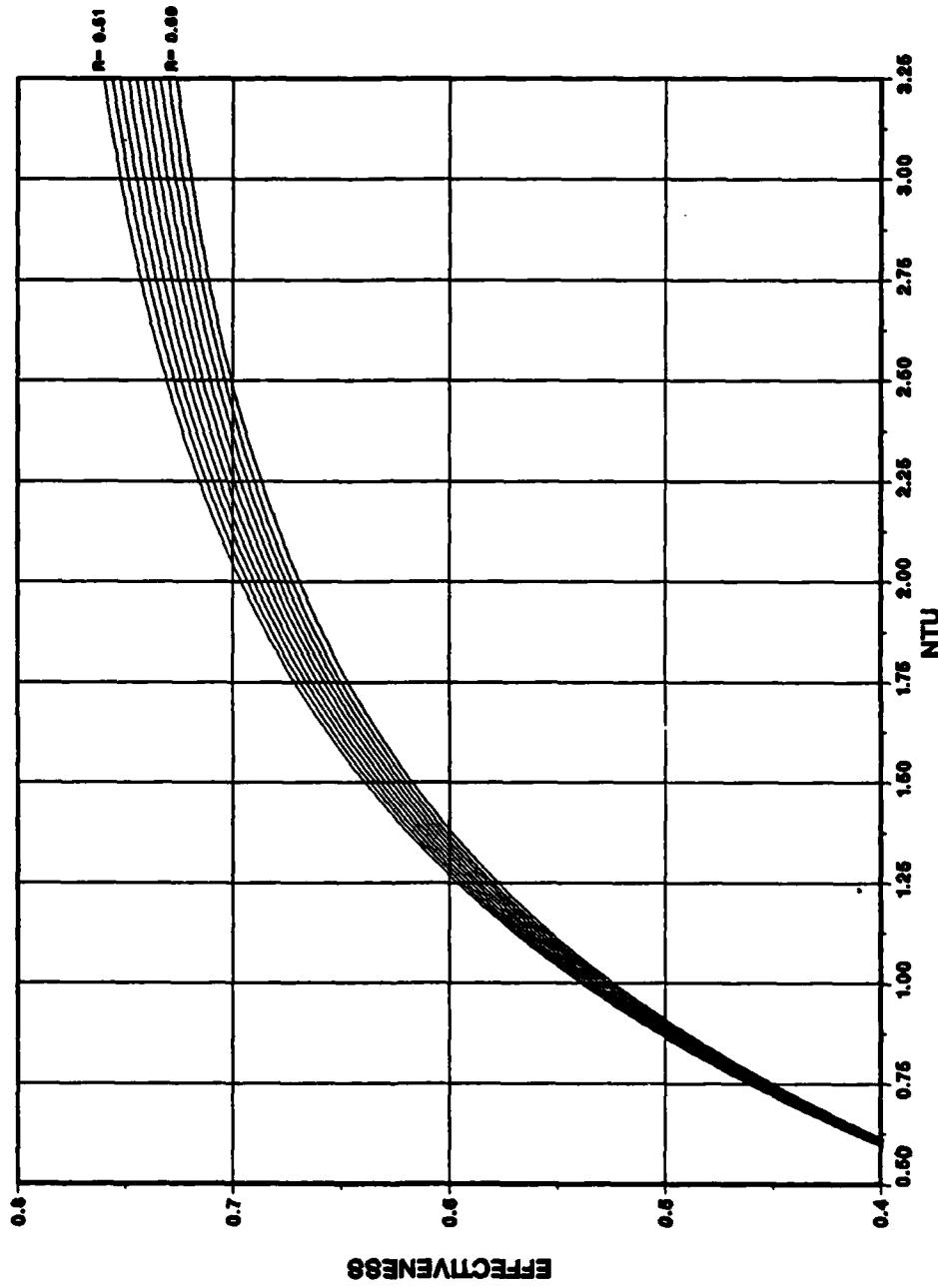


Figure M.7 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of  $R$  from 0.51 to 0.6

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .61 TO 0.7

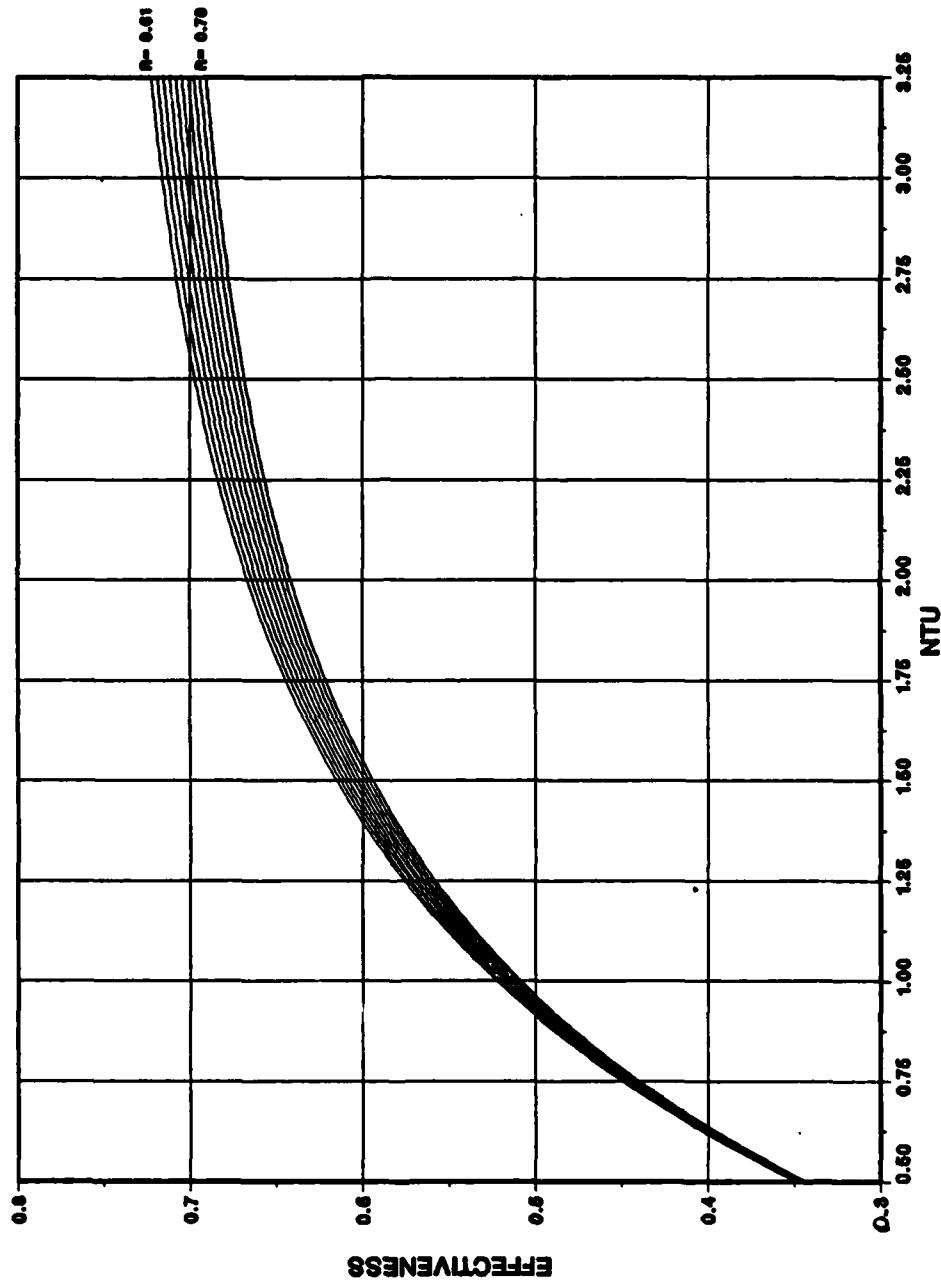


Figure M.8 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.61 to 0.7

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARING BY .01 FROM .71 TO 0.8

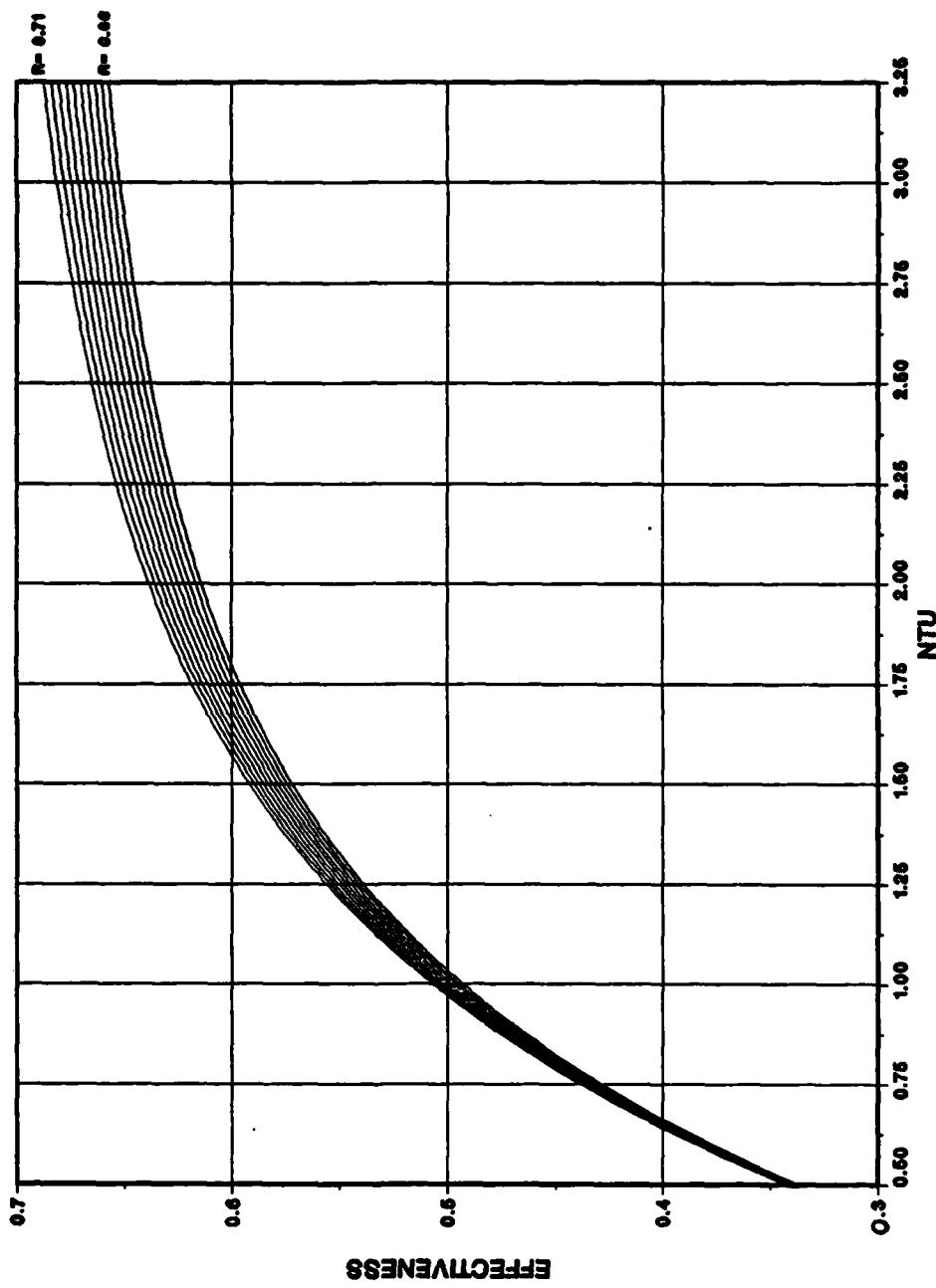


Figure M.9 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.71 to 0.8

EFFECTIVENESS VS. NTU  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM .81 TO 0.9

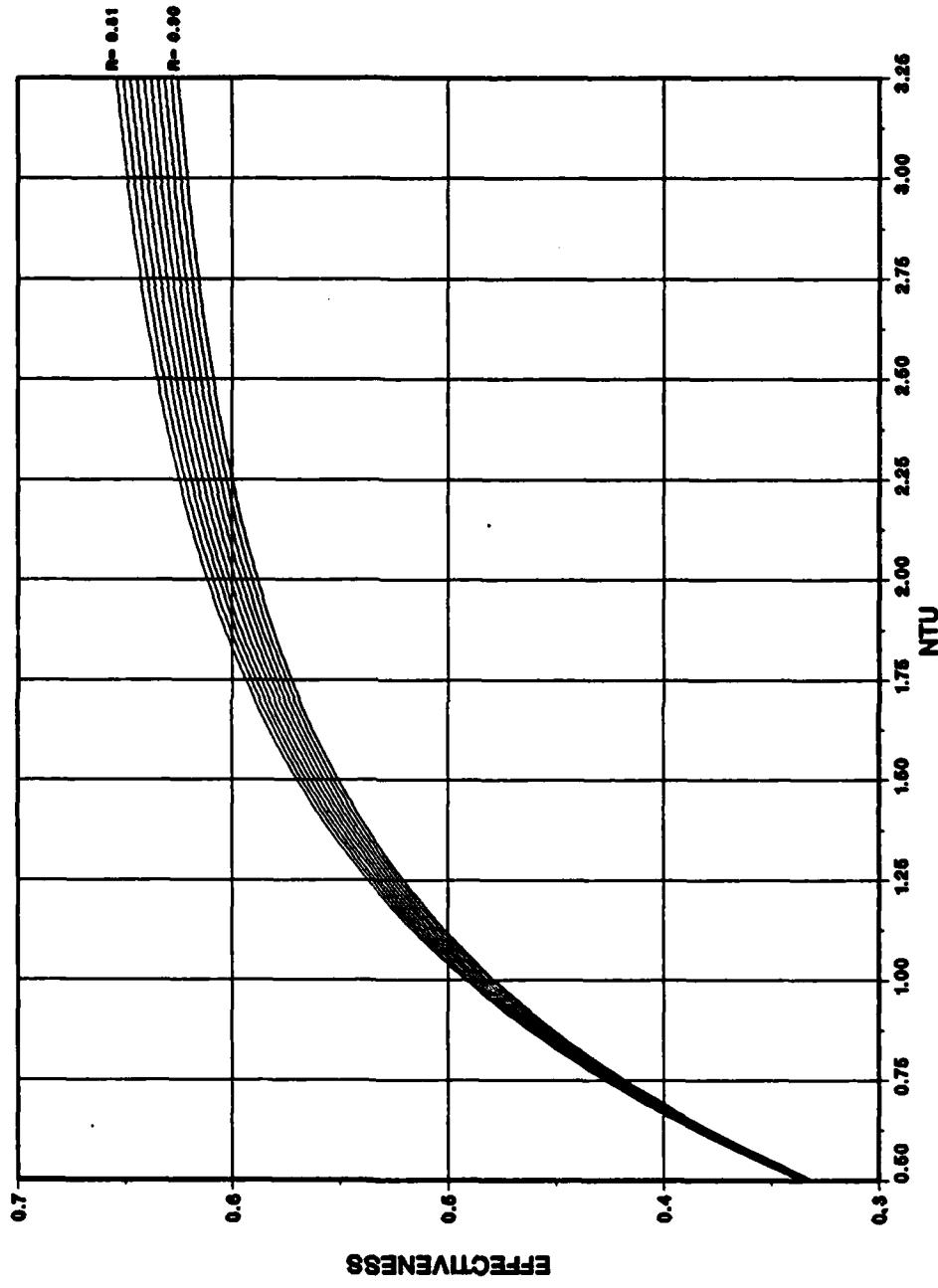


Figure M.10 1-3:2C Effectiveness vs. Ntu over Range of R from 0.81 to 0.9

EFFECTIVENESS VS. NTU  
2 OUT OF 3 PASSES IN COUNTER FLOW  
FOR R VARYING BY .01 FROM 0.9 TO 1.0

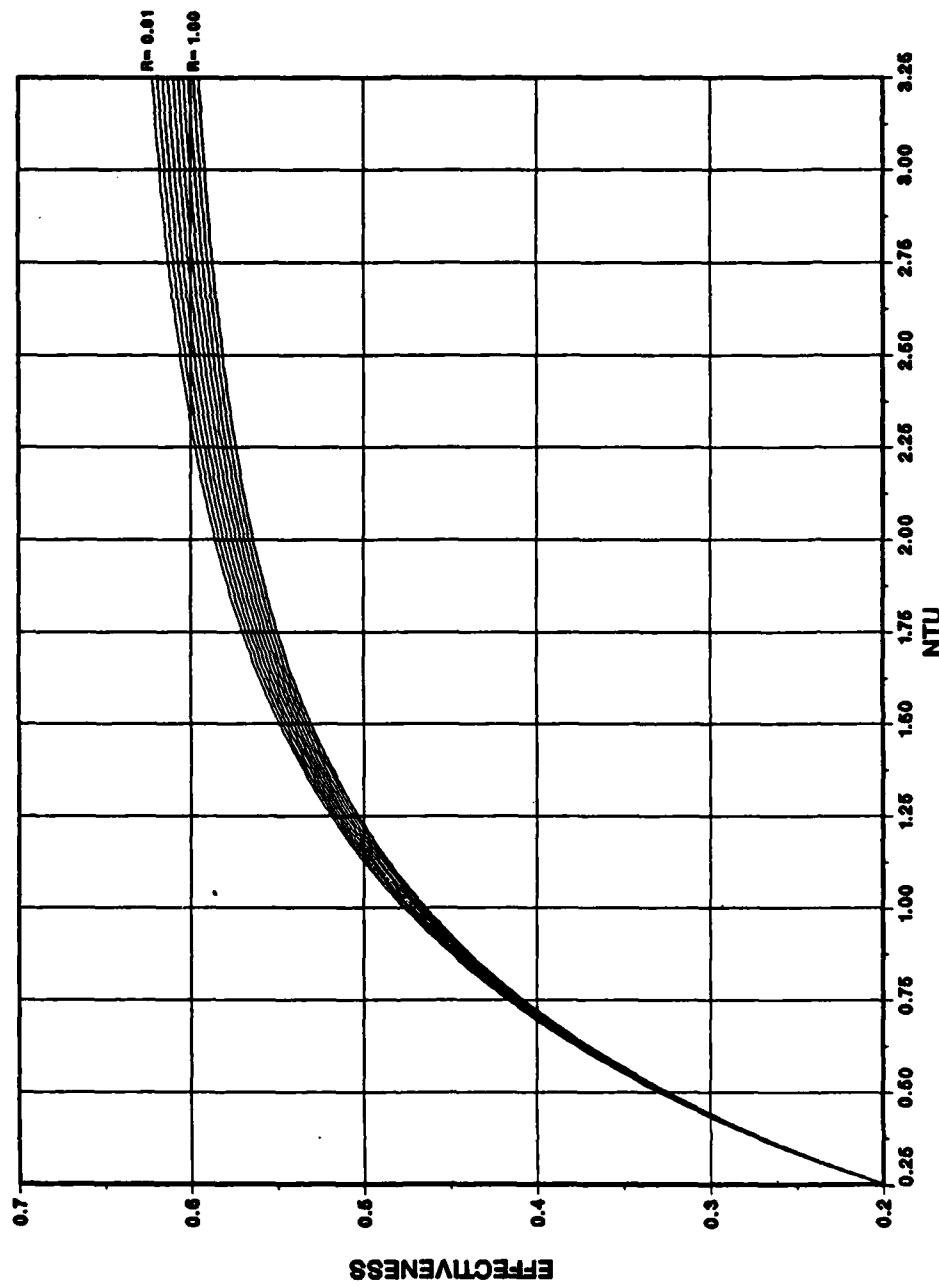


Figure M.11 1-3:2C Effectiveness vs.  $N_{tu}$  over Range of R from 0.9 to 1.0

APPENDIX N

1-3:2P EFFECTIVENESS VS.  $N_{tu}$  GRAPHS AT VARIOUS R VALUES

EFFECTIVENESS VS. NTU  
2 OUT OF 3 PASSES IN PARALLEL FLOW

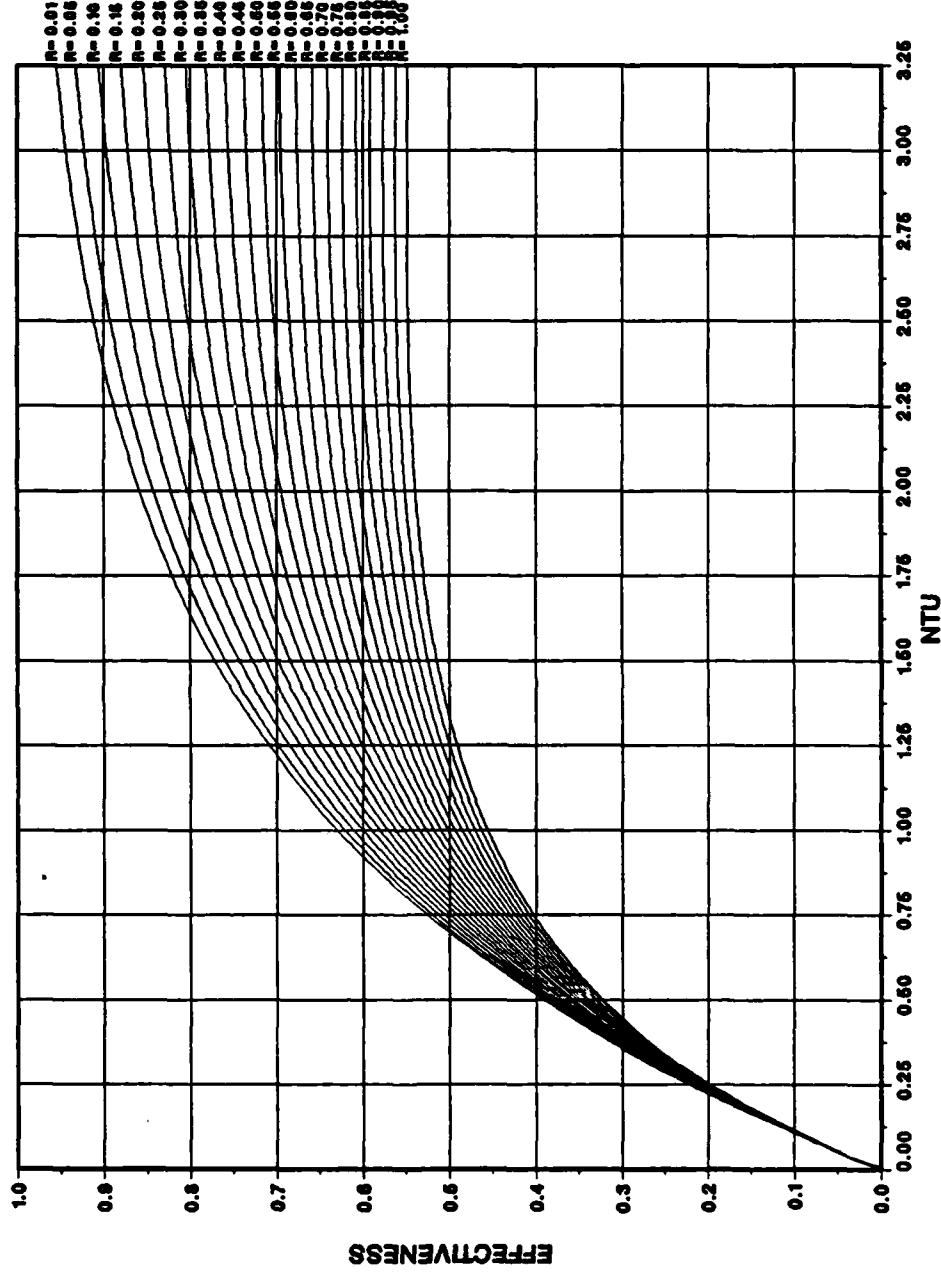


Figure N.1 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.01 to 1.0

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARING FROM .01 to 0.1

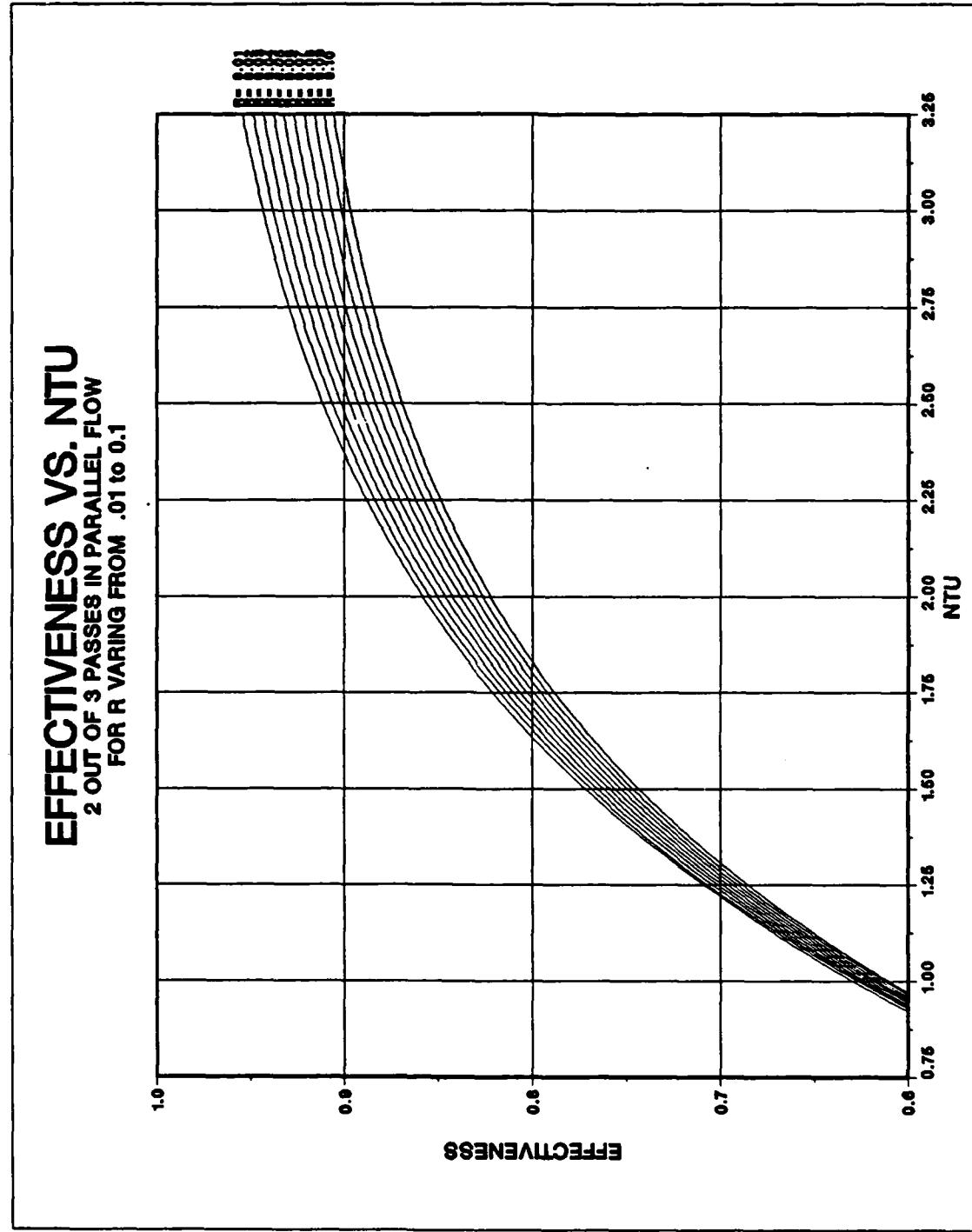


Figure N.2 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.01 to 0.1

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARING FROM .11 to 0.2

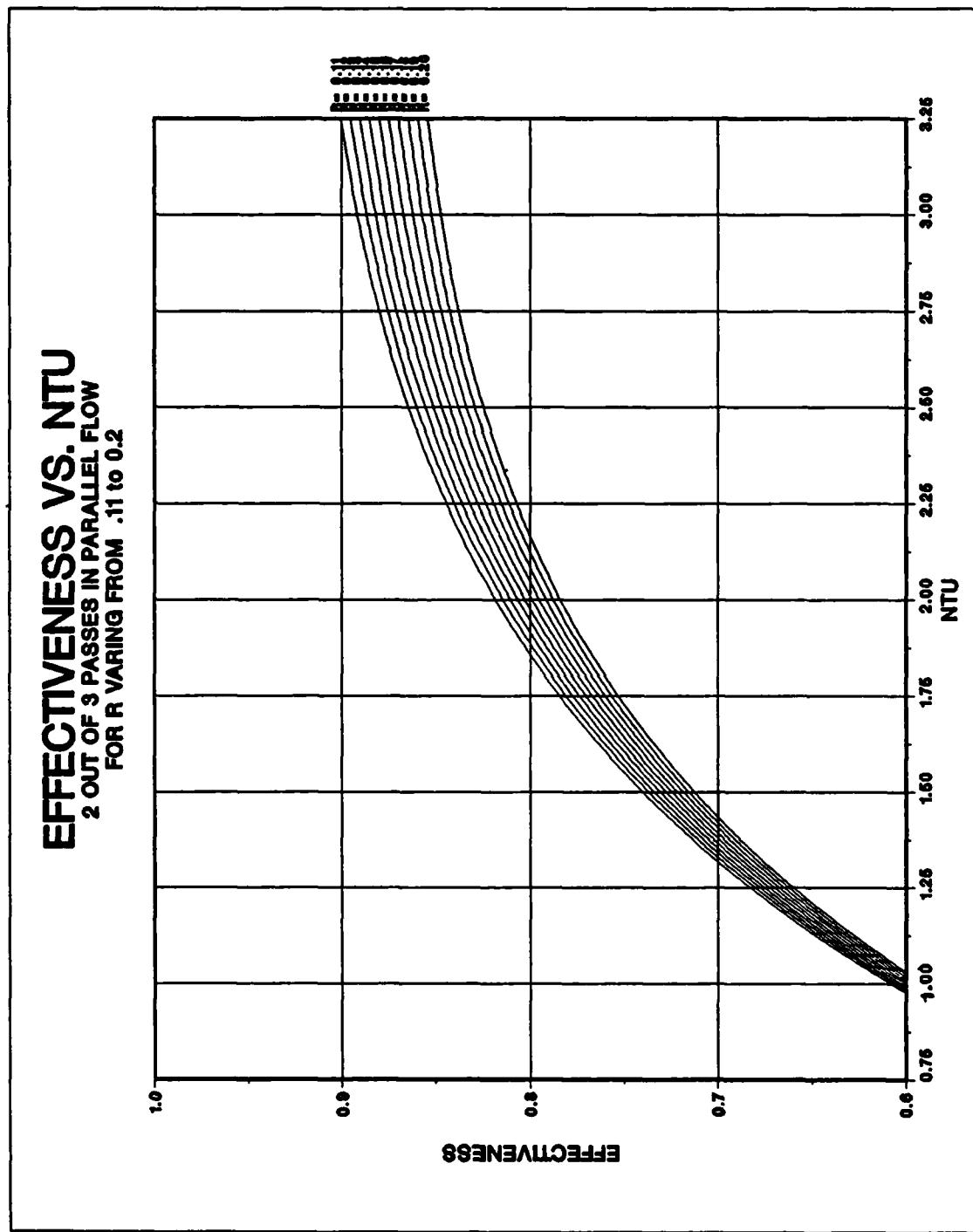


Figure N.3 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.11 to 0.2

EFFECTIVENESS VS. NTU  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING FROM .21 to 0.3

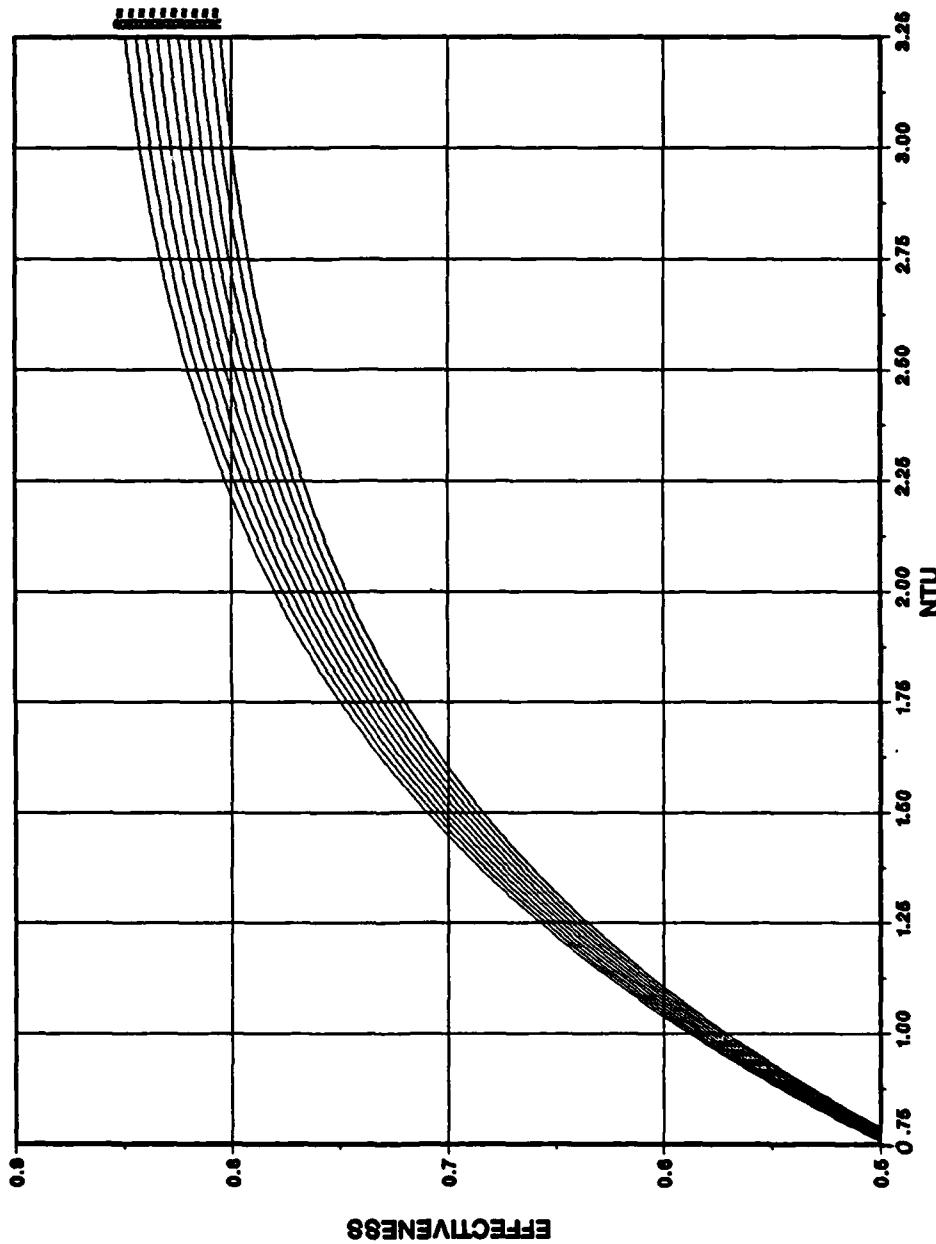


Figure N.4 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.21 to 0.3

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING FROM .31 TO 0.4

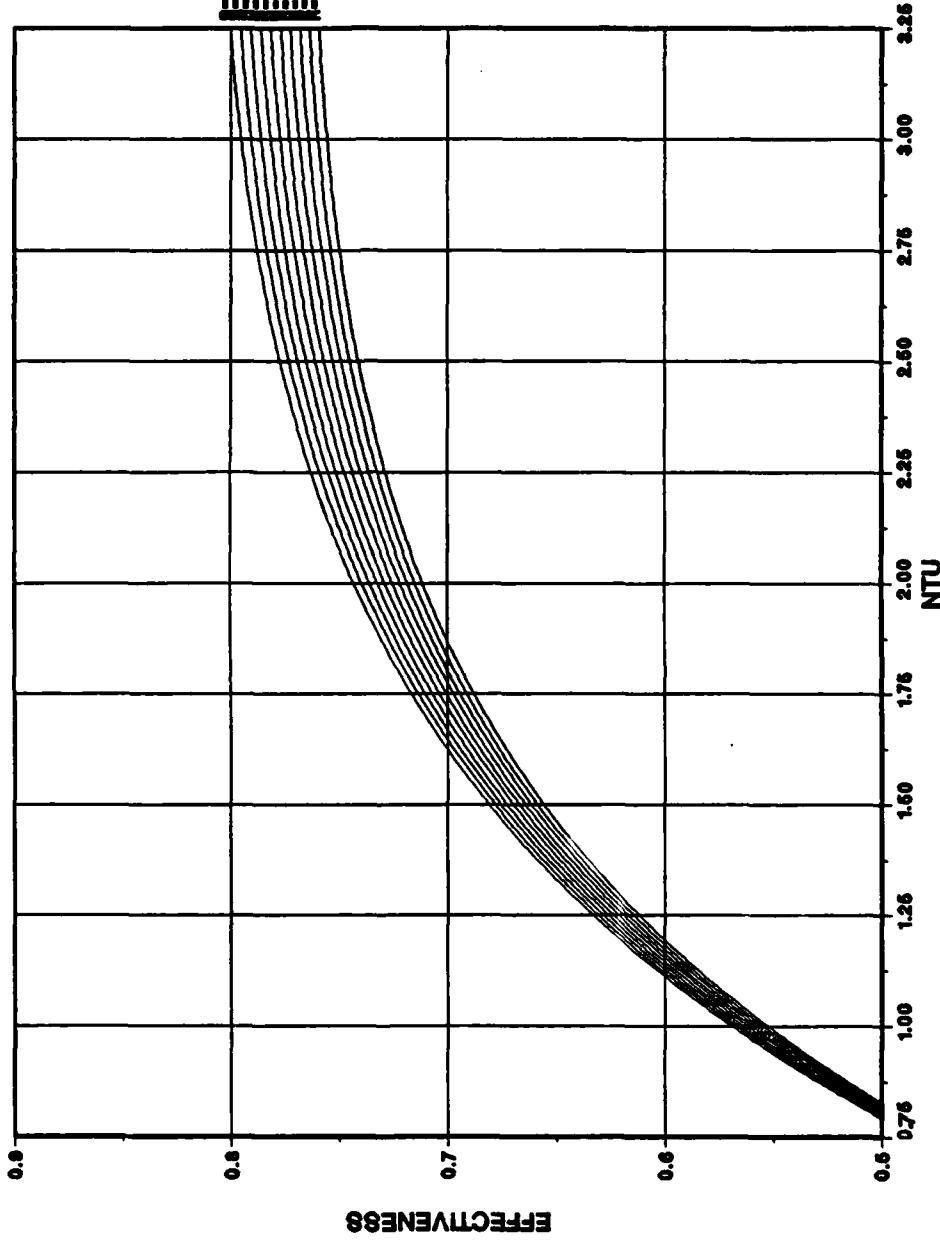


Figure N.5 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.31 to 0.4

EFFECTIVENESS VS. NTU  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING FROM .41 to 0.5

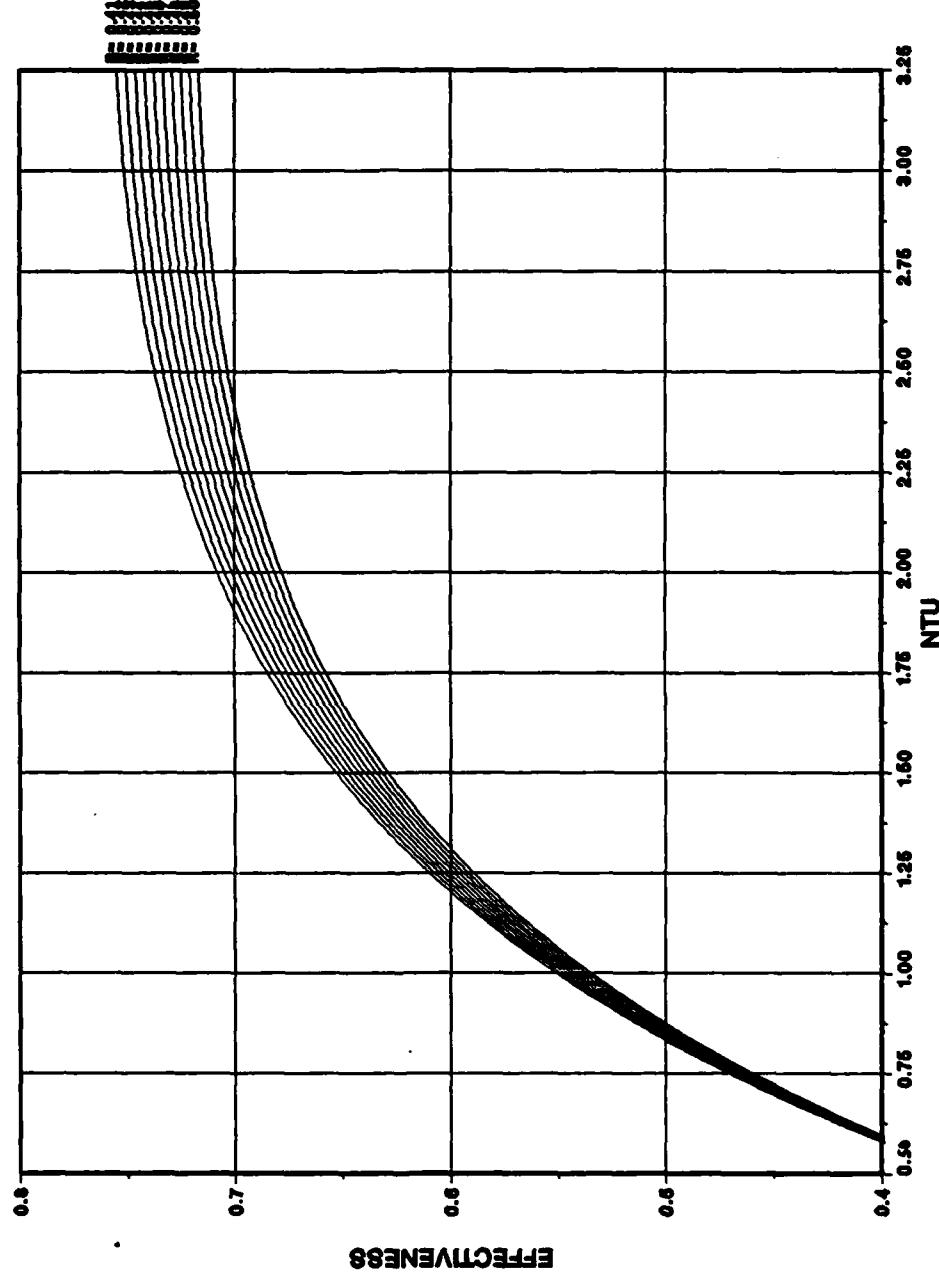


Figure N.6 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.41 to 0.5

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING FROM .51 TO 0.6

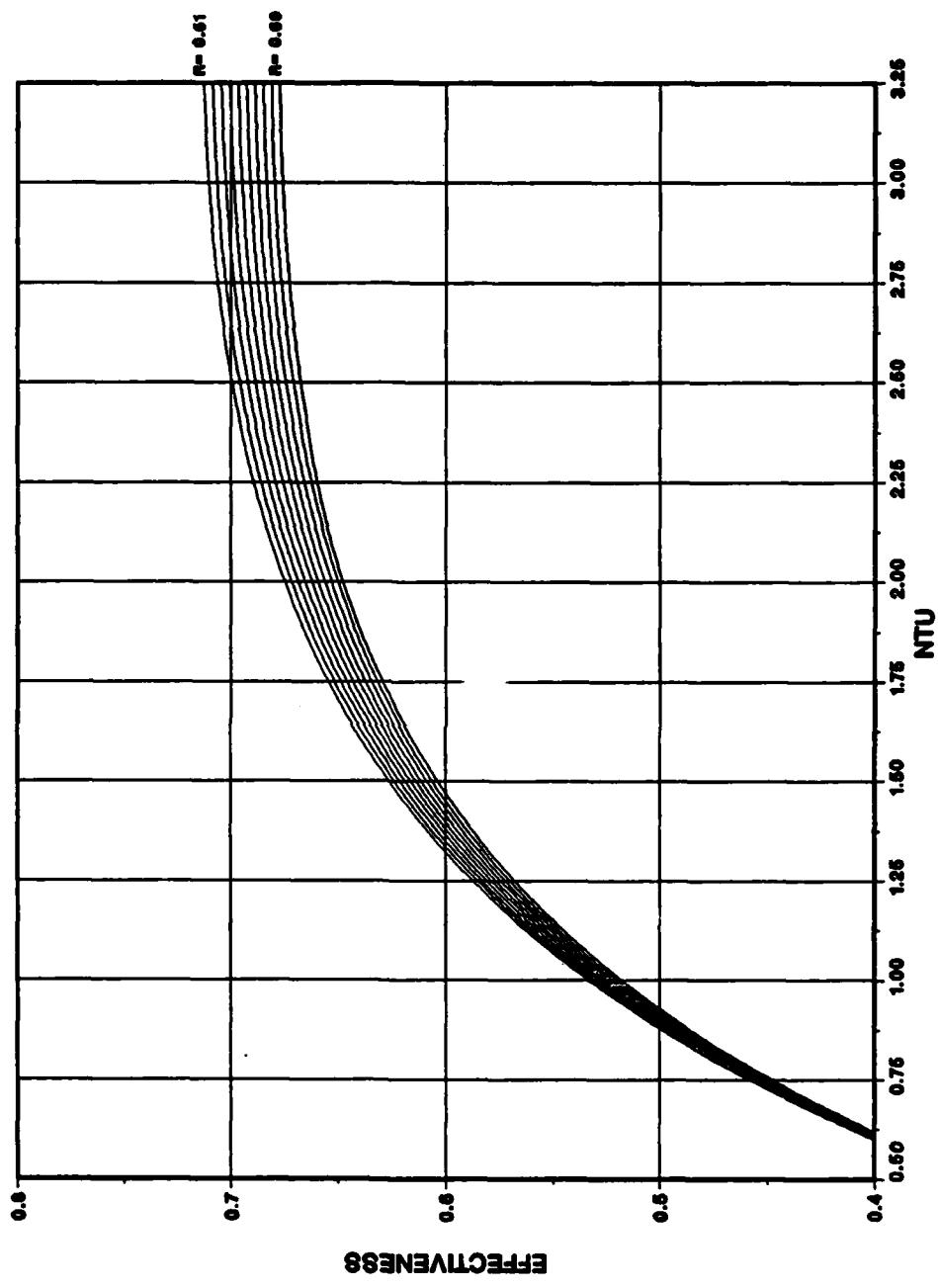


Figure N.7 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.51 to 0.6

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING BY .01 FROM .61 TO 0.7

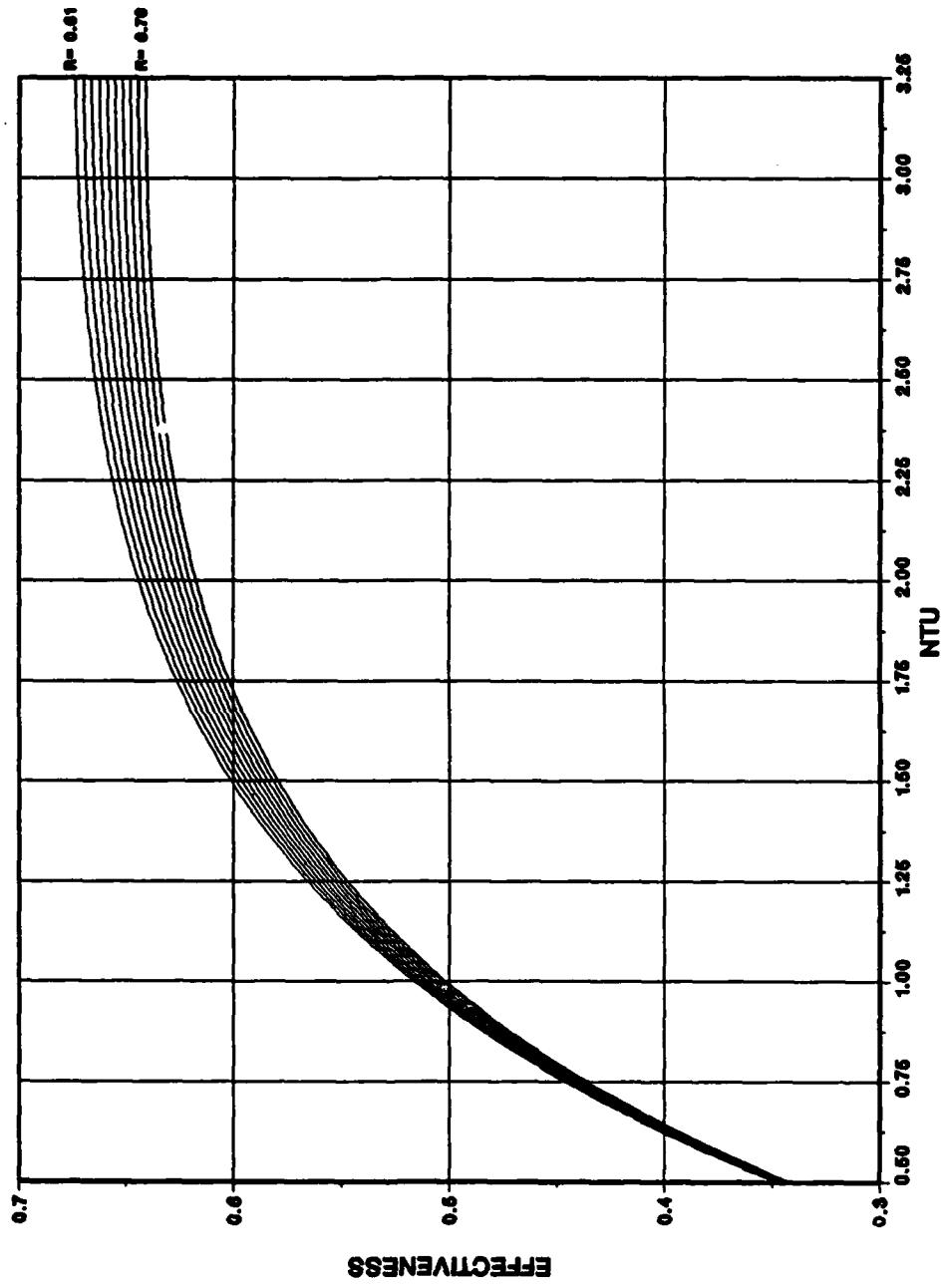


Figure N.8 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.61 to 0.7

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARING BY .01 FROM .71 TO 0.8

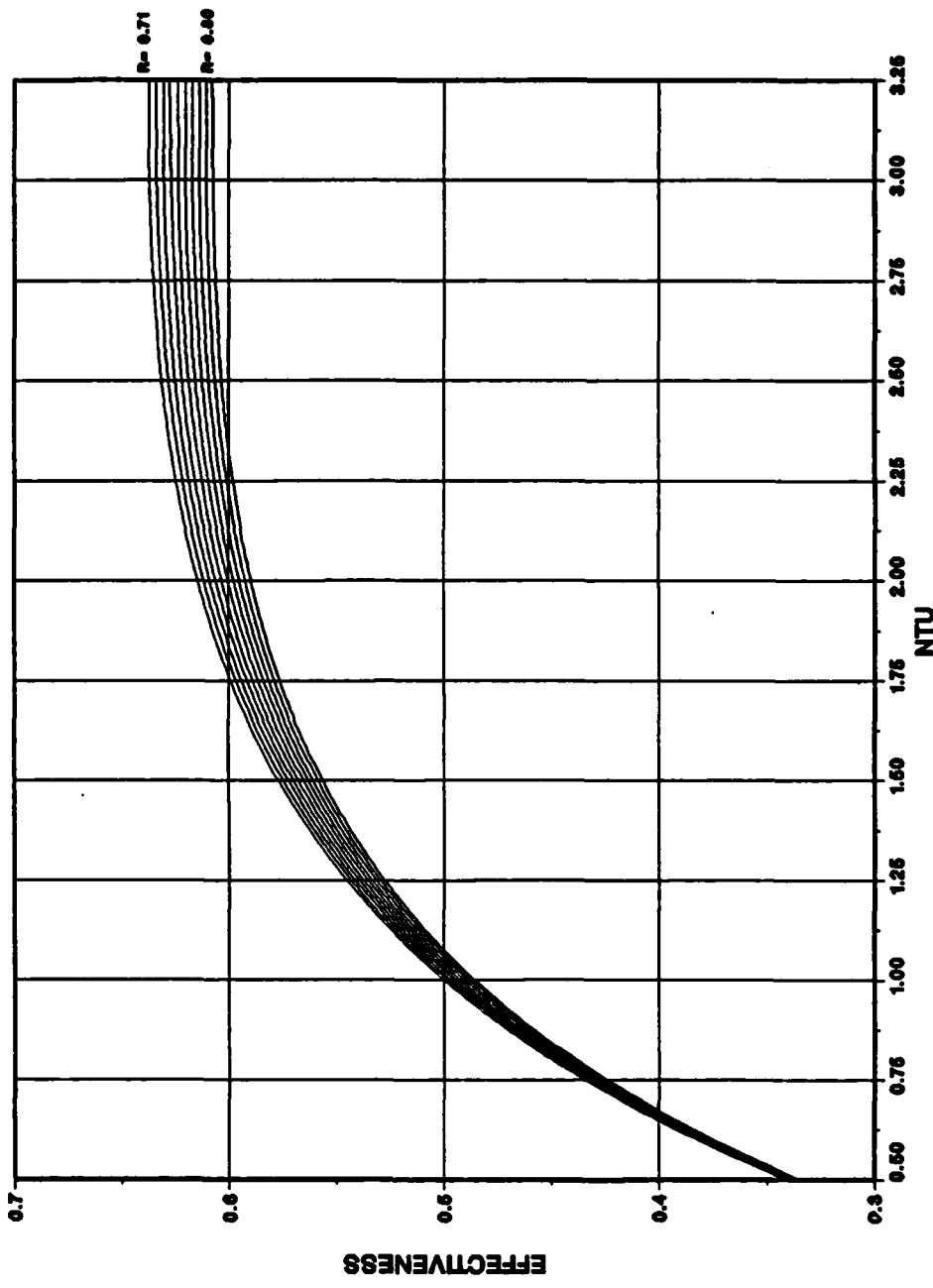


Figure N.9 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.71 to 0.8

**EFFECTIVENESS VS. NTU**  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING BY .01 FROM .81 TO 0.9

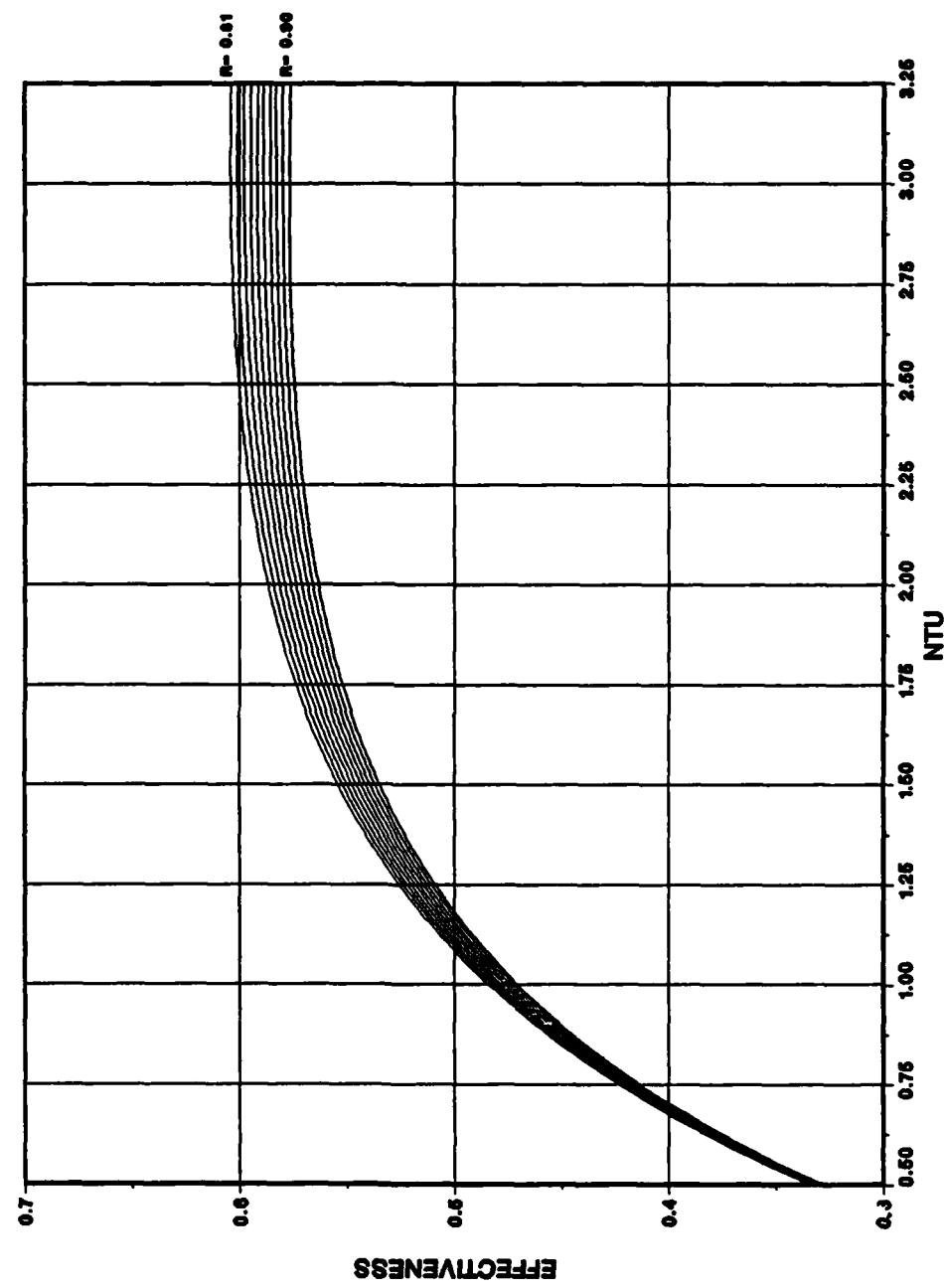


Figure N.10 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.81 to 0.9

EFFECTIVENESS VS. NTU  
2 OUT OF 3 PASSES IN PARALLEL FLOW  
FOR R VARYING BY .01 FROM 0.9 TO 1.0

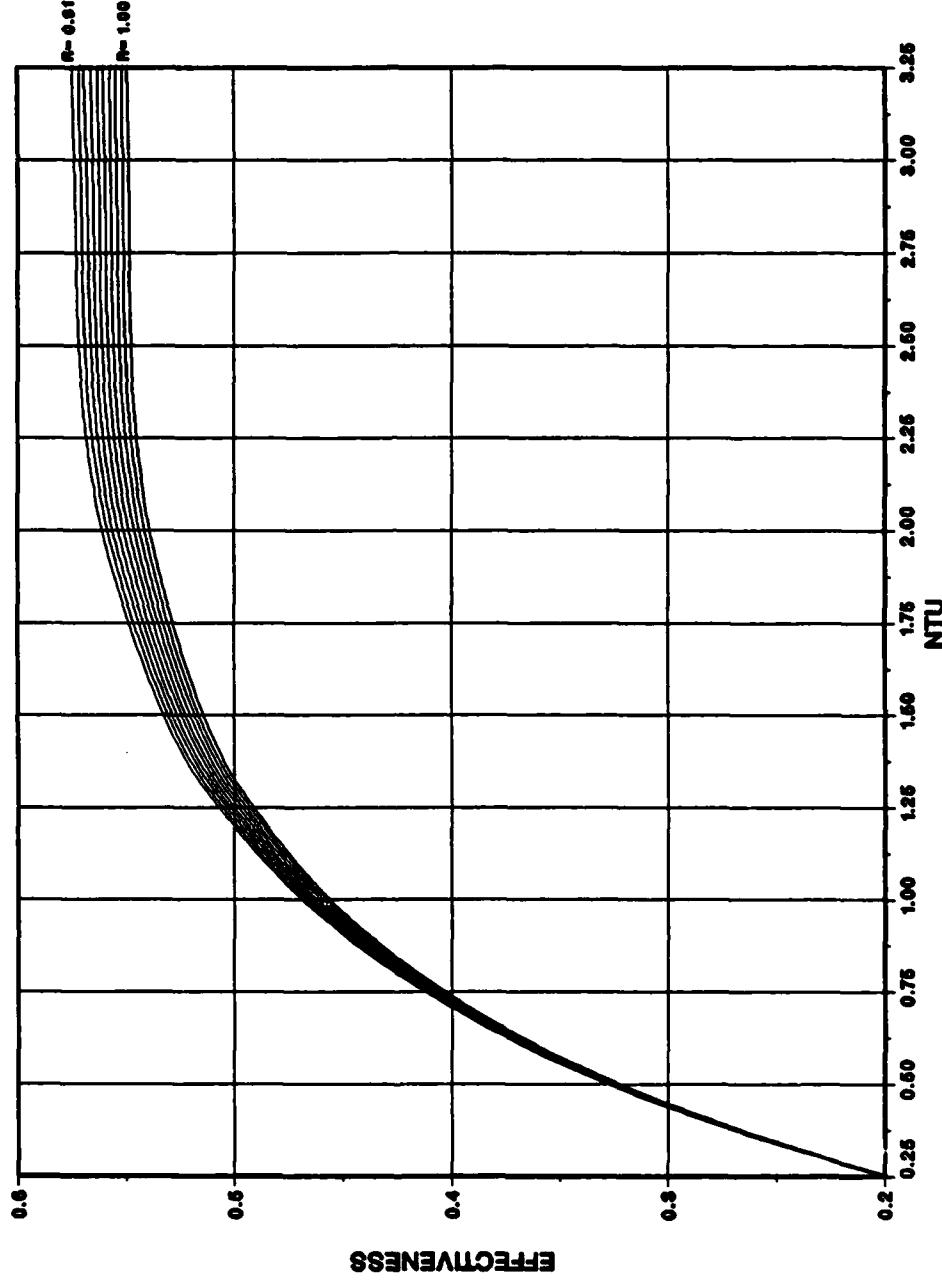


Figure N.11 1-3:2P Effectiveness vs.  $N_{tu}$  over Range of R from 0.91 to 1.0

APPENDIX O  
 SAMPLE DISSPLAY PROGRAM USED FOR GRAPHING DATA

```

C ****
C *      DISSPLAY GRAPHING ROUTINE
C *      by
C *      LCDR MARK S O'HARE U.S.N
C *      8 MAY 1985
C *      NAVAL POSTGRADUATE SCHOOL, MONTEREY, CA
C ****

C CALL DISSPLA GRAPHICS PACKAGE
C DIMENSION X1(12),Y1(12)
C DIMENSION X2(12),Y2(12)
C DIMENSION X3(12),Y3(12)
C DIMENSION X4(12),Y4(12)
C DIMENSION X5(12),Y5(12)
C DIMENSION X6(12),Y6(12)
C DIMENSION X7(12),Y7(12)
C DIMENSION X8(12),Y8(12)
C DIMENSION X9(12),Y9(12)
C DIMENSION X10(12),Y10(12)
C DIMENSION X11(12),Y11(12)
C DIMENSION X12(12),Y12(12)
C DIMENSION X13(12),Y13(12)
C DIMENSION X14(12),Y14(12)
C DIMENSION X15(12),Y15(12)
C DIMENSION X16(12),Y16(12)
C DIMENSION X17(12),Y17(12)
C DIMENSION X18(12),Y18(12)

C THIS IS THE DISTANCE OF THE VALUE FOR R
C THIS T=3.315
C THIS T=3.265
C CALL TEK618
C CALL COMPRS
C *** START LEVEL 1 WORK *****
C CALL BCOMMON(10*21+2)
C DATA WW/0.01,0.05,0.10,0.15,0.20,0.25,0.30,0.35,0.40,0.45,0.5,
C *0.55,0.60,0.65,0.75,0.80,0.85,0.90,0.95,1.0/
1000 FORMAT(6X,F4.2,3X,F6.4)
DO 20 I=1,1
READ(21,1000) X1(I),Y1(I)
CONTINUE
20 DO 30 I=1,1
READ(22,1000) X2(I),Y2(I)
CONTINUE
30 DO 40 I=1,1
READ(23,1000) X3(I),Y3(I)
CONTINUE
40 DO 50 I=1,1

```

```

      READ(24,1000) X4(I),Y4(I)
      CONTINUE
      DO 60 I=1,11
      READ(25,1000) X5(I),Y5(I)
      CONTINUE
      DO 70 I=1,11
      READ(26,1000) X6(I),Y6(I)
      CONTINUE
      DO 80 I=1,11
      READ(27,1000) X7(I),Y7(I)
      CONTINUE
      DO 90 I=1,11
      READ(28,1000) X8(I),Y8(I)
      CONTINUE
      DO 100 I=1,11
      READ(29,1000) X9(I),Y9(I)
      CONTINUE
      DO 110 I=1,11
      READ(30,1000) X10(I),Y10(I)
      CONTINUE
      DO 120 I=1,11
      READ(31,1000) X11(I),Y11(I)
      CONTINUE
      DO 130 I=1,11
      READ(32,1000) X12(I),Y12(I)
      CONTINUE
      DO 140 I=1,11
      READ(33,1000) X13(I),Y13(I)
      CONTINUE
      DO 150 I=1,11
      READ(34,1000) X14(I),Y14(I)
      CONTINUE
      DO 160 I=1,11
      READ(35,1000) X15(I),Y15(I)
      CONTINUE
      DO 170 I=1,11
      READ(36,1000) X16(I),Y16(I)
      CONTINUE
      DO 180 I=1,11
      READ(37,1000) X17(I),Y17(I)
      CONTINUE
      DO 190 I=1,11
      READ(38,1000) X18(I),Y18(I)
      CONTINUE
      DO 200 I=1,11
      READ(39,1000) X19(I),Y19(I)
      CONTINUE
      DO 210 I=1,11

```

```

      READ(40,1000) X20(I),Y20(I)
CONTINUE
DO 220 I=1,11
      READ(41,1000) X21(I),Y21(I)
CONTINUE
CALL NOBDRDR
CALL SWISSM
CALL BASALF('STANDARD')
CALL MIXALF('L/CSTD')
CALL HWROT('COMIC')
CALL SHDCHR(90,1,0,005,1)
CALL HEIGHT(.17)
CALL HWSCL('SCREEN')
CALL PAGE(14,0,11,0)
CALL XNAME('NTUS',100)
CALL YNAME('EFFECTIVENESS$',100)
CALL AREA2D(11,0,85)
CALL HEADIN('EFFECTIVENESS VS. NTUS',100)
CALL HEADIN('OUT OF 3 PASSES IN COUNTER FLOW',100,1.0,2)
CALL YTICKS(2)
CALL XTICKS(2)
CALL YAXANG(180)
CALL GRAF(0,0,25,3.25,0.0,0.10,1.0)
CALL HEIGHT(.10)
CALL POLY5
CALL CURVE(X1,Y1,11,0)
W=WW(1)
Z=Y1(1)
CALL RLREAL(W,R=2,TT,Z)
CALL RMESS(X2,Y2,11,0,Z)
CALL CURVE(X2,Y2,11,0)
W=WW(2)
Z=Y2(1)
CALL RLREAL(W,R=2,TT,Z)
CALL RMESS(X3,Y3,11,0,Z)
CALL CURVE(X3,Y3,11,0)
W=WW(3)
Z=Y3(1)
CALL RLREAL(W,R=2,TT,Z)
CALL RMESS(X4,Y4,11,0,Z)
CALL CURVE(X4,Y4,11,0)
W=WW(4)
Z=Y4(1)
CALL RLREAL(W,R=2,TT,Z)
CALL RMESS(X5,Y5,11,0,Z)
CALL CURVE(X5,Y5,11,0)
W=WW(5)
Z=Y5(1),

```

```

CALL RLREAL (W22 TT22 Z)
CALL RMESS (X6,Y6,11,0)
CALL CURVE (Z=WW{6})
W=WW{11}
Z=Y6{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X6,Y6,11,0)
CALL CURVE (Z=WW{7})
W=WW{11}
Z=Y7{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X7,Y7,11,0)
CALL CURVE (Z=WW{8})
W=WW{11}
Z=Y8{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X8,Y8,11,0)
CALL CURVE (Z=WW{9})
W=WW{11}
Z=Y9{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X9,Y9,11,0)
CALL CURVE (Z=WW{10})
W=WW{10}
Z=Y10{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X10,Y10,11,0)
CALL CURVE (Z=WW{11})
W=WW{11}
Z=Y11{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X11,Y11,11,0)
CALL CURVE (Z=WW{12})
W=WW{12}
Z=Y12{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X12,Y12,11,0)
CALL CURVE (Z=WW{13})
W=WW{13}
Z=Y13{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X13,Y13,11,0)
CALL CURVE (Z=WW{14})
W=WW{14}
Z=Y14{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X14,Y14,11,0)
CALL CURVE (Z=WW{15})
W=WW{15}
Z=Y15{11}
CALL RLREAL (W22 TT22 Z)
CALL RMESS (X15,Y15,11,0)
CALL CURVE (Z=WW{16})
W=WW{16}
Z=Y16{11}

```

```

W=WW{15}
Z=Y1{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X16,Y16,Z0}
CALL CURVE (X16,Y16,Z0)
W=WW{16}
Z=Y1{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X17,Y17,Z0}
CALL CURVE (X17,Y17,Z0)
W=WW{17}
Z=Y1{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X18,Y18,Z0}
CALL CURVE (X18,Y18,Z0)
W=WW{18}
Z=Y1{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X19,Y19,Z0}
CALL CURVE (X19,Y19,Z0)
W=WW{19}
Z=Y1{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X20,Y20,Z0}
CALL CURVE (X20,Y20,Z0)
W=WW{20}
Z=Y2{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X21,Y21,Z0}
CALL CURVE (X21,Y21,Z0)
W=WW{21}
Z=Y2{1}
CALL RLREAL {WR2TTZ2}
CALL RMESS {X21,Y21,Z0}
C *** START LEVEL 3 WORK ****
C CALL FRAME
C *** START LEVEL 3 WORK ****
CALL GRID {1,1}
CALL ENDPL {C}
CALL DONEPL
STOP
END

```

RD-A159 706

THE EFFECTIVENESS OF HEAT EXCHANGERS WITH ONE SHELL  
PASS AND THREE TUBE PASSES(U) NAVAL POSTGRADUATE SCHOOL  
MONTEREY CA M S O'HARE JUN 85

3/3

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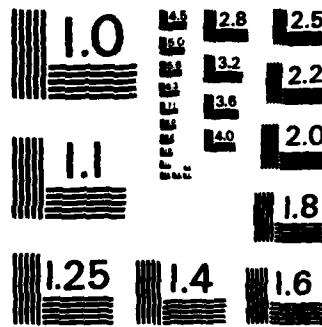
END

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DTB



MICROCOPY RESOLUTION TEST CHART  
NATIONAL BUREAU OF STANDARDS - 1963 - A

APPENDIX P  
POLYNOMIAL REGRESSION CURVEFIT PROGRAM

PROGRAM POLYFIT

PURPOSE: TO AN NTH ORDER LEAST-SQUARES FIT OF THE INPUT VALUES  
X AND Y.

INPUT: I) X.

I) Y.

OUTPUT: I) MEAN OF X.

I) RANGE OF X.

I) ORDER OF THE FIT.

I) COEFFICIENTS IN DOUBLE PRECISION.

V) R.M.S. ERROR OF THE RESIDUALS.

CALL: I) CURFIT(IORDER,NITEMS,X,Y,AA)

I) SOLVE(NRC)

I) FUNCTION AMAX(X,NITEMS)

I) FUNCTION AMIN(X,NITEMS)

```
INTEGER I,NITEMS,MAXORD,J,K,L,M,N
DOUBLE PRECISION AA(40)
DIMENSION X(11),Y(11),XCMP(11),ONE(11,2),TWO(11,2)
COMMON IDIAGN
```

1. ZERO ALL VALUES THAT WILL BE USED TO COMPUTE SUMS.

RMSUM = 0.0

2. INPUT THE DATA.

```
IDIAGN=0
WRITE(6,100)
FORMAT(2X,MAXIMUM ORDER OF THE FIT?)
```

C100

```

120      FORMAT(2X,'')
C      READ(5,*),MAXORD
C
C      DO 10 I=1,11
C          READ(1,*),ONE(I,1),TWO(I,2)
C          X(I)=ONE(I,1)
C          Y(I)=TWO(I,2)
C          CONTINUE
C
C      NITEMS = I - 2
C
C      CCCCCCCCCCCCCCCCC
C
3.      COMPUTE THE LEAST-SQUARES COEFFICIENTS BY CALLING "CURFIT()".
      THE COEFFICIENTS ARE RETURNED IN AA(). SUCH THAT:
      Y=AA(1)+AA(2)*X+...+AA(N)*(X**N)
      CALL CURFIT(MAXORD,NITEMS,X,Y,AA)
      NITEMS = I - 2
      DO 90 I=1,NITEMS
          YCOMP(I)=0.0
          IJUNK=MAXORD+1
          DO 91 J=1,I
              YCOMP(I)=YCOMP(I)+AA(J)*(X(I)**(J-1))
              IF(X(I).EQ.0.0)CONTINUE
              91
              CONTINUE
              RMSUM = RMSUM + (Y(I)-YCOMP(I))*(Y(I)-YCOMP(I))
      90
      RMS = SQRT(RMSUM/FLOAT(NITEMS))
      CCCCCCCCCCCCCCCCC
      5. PRINT OUT THE RESULTS.
      WRITE(7,120)
      WRITE(7,120)

```



```

DIMENSION X(NITEMS) Z(NITEMS)
DIMENSION X(500) Z(500)
DIMENSION XXX(2) ZZZ(2)
DOUBLE PRECISION SMATR(100,100),AA(40)
DIMENSION SUBSUM(40)
COMMON IDIAGN

```

## 1. NORMALIZE "X" AND "Z" BETWEEN "-1" AND "1".

XMAX =	AMAX(X,NITEMS)	= XMAX	{1}
XMIN =	AMIN(X,NITEMS)	= ABS(XMIN)	{2}
ZMAX =	AMAX(Z,NITEMS)	= ZMAX	{3}
ZMIN =	AMIN(Z,NITEMS)	= ABS(ZMIN)	{4}
		= AMAX(XXXX,2)	{5}
		= AMAX(ZZZZ,2)	{6}
		= AMAX(ZNORM,2)	{7}
		= AMAX(ZNORM,2)	{8}

```
LIF(IDIAGN, 'EORF3', WRITE(7, 107) XNORM, ZNORM)
FFORMAT(2X, 'CURFIT': XNORM, ZNORM = ,3F15.5)
```

```
DO 96 I=1,NITEMS
  XX(I)=X(I)/XNORM
  ZZ(I)=Z(I)/ZNORM
  IF(IDIAGN.EQ.4) WRITE(7,108) I,XX(I),ZZ(I)
```

```
FORMAT(2X,'CURFIT: I,XX,ZZ = ',15,3F12.4)
```

## 2. COMPUTE ALL NECESSARY SUMS:

ICOEF = IORDER + 1

```

      IF(IDIAGN < 2X, 'CURFIT', WRITE(7,111), ICOEF, NITEMS = 2110)
      FORMAT(2X, 'CURFIT', ICOEF, NITEMS = 2110)

```

```

DO 97 I=1,ICOEF
   IJUNK = ICOEF + 1
   DO 97 J=1,IJUNK
      SMATRX(I,J) = 0.0
CONTINUE
C
C      DO 900 N=1,NITEMS
C         SUBSUM(1) = 1.0
C         DO 98 I=1,IORDER
C            SUBSUM(I+1) = XX(N)**(I)
C         CONTINUE
C      DO 900 J=1,ICOEF
C         DO 99 I=1,ICOEF
C            SMATRX(J,I) = SMATRX(J,I) + SUBSUM(I)*SUBSUM(J)
C         CONTINUE
C         SMATRX(J,ICOEF+1)=SMATRX(J,ICOEF+1)+SUBSUM(J)*ZZ(N)
C         CONTINUE
C
C      IF(IDIAGN .NE. 6) GO TO 22
C      DO 906 I=1,ICOEF
C         IJUNK = ICOEF + 1
C         DO 906 J=1,IJUNK
C            WRITE(7,110) I,J,SMATRX(I,J)
C         CONTINUE
C      FORMAT(2X,'CURFIT: SMATRX(' ,I3,' ,',I3,',') = ',1F15.5)
C
C      3. NOW INVERT THE MATRIX. (SOLVE THE SET OF
C         SIMULTANEOUS EQUATIONS.)
C
C      CALL SOLVE(SMATRX,ICOEF)
C
C      DO 903 I=1,ICOEF
C         AA(I) = SMATRX(I,ICOEF+1)
C         IF(IDIAGN.EQ.8) WRITE(7,112) I,AA(I)
C         CONTINUE
C      FORMAT(2X,'CURFIT: AA(' ,I3,' ) = ',1F15.5)
C
C      4. "UNNORMALIZE" THE RETURNED COEFFICIENTS.

```

```

C      DO 901 I=2, ICOEF AA(I)=AA(I)/XNORM***(I-1)
C      CONTINUE
C
C      DO 902 I=1, ICOEF AA(I)=AA(I) * ZNORM
C      IF(IDIAGN.EQ.9) WRITE(7,113) I,AA(I)
C      CONTINUE
C      FORMAT(2X,'CURFIT: AA(' ,I3, ') = ',1F15.5)
C      RETURN
C      END
C
CCCCCCC SUBROUTINE SOLVE(C,NR)
C
C PURPOSE:  SOLVE A SET OF "NR" SIMULTANEOUS EQUATIONS
C           USING GAUSSIAN ELIMINATION.
C
C DOUBLE PRECISION C(100,100),SAVE
C INTEGER NR
C
C      NC = NR + 1
C      DO 303 I=1, NR
C          KEXCH = 1
C          M = I + 1
C          IF(DABS(C(I,I))-1.D-5) 308, 308, 307
C          DO 301 J=M,NC
C              C(I,J)=C(I,J)/C(I,I)
C              DO 303 J=1, NR
C                  IF(J-I) 322, 303, 322
C                  DO 302 K=M,NC
C                      C(J,K)=C(J,K)-C(J,I)*C(I,K)
C
C      CONTINUE
C      RETURN
C
C      L = I-NR
C      IF(L-NR) 309, 309, 330

```

```

309 DO 311 N=I,NC
      SAVE = C(I,N)
      C{I,N} = C{L,N}
      C{L,N} = SAVE
      KEXCH = KEXCH + 1
      GO TO 306
C
C   WRITE(7,331)
      FORMAT(7,331)
      EQUATIONS CANNOT BE SOLVED... ')
      END
C
C 330
C 331

```

REAL FUNCTION AMAX(X,NITEMS)  
 PURPOSE: FIND THE MAXIMUM VALUE IN AN ARRAY.

DIMENSION X(500)  
 INTEGER NITEMS

```

XMAX = X(1)
DO 340 I=1,NITEMS
      IF(X(I) .GT. XMAX) XMAX = X(I)
      CONTINUE
      AMAX = XMAX
      RETURN
      END
C
C

```

REAL FUNCTION AMIN(X,NITEMS)  
 PURPOSE: FIND THE MINIMUM VALUE IN AN ARRAY.

DIMENSION X(500)

INTEGER NITEMS

C  
XMIN = X(1)  
DO 340 I=1,NITEMS  
CONTINUE  
IF(X(I).LT. XMIN) XMIN = X(I)  
AMIN = XMIN  
RETURN  
END  
340

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Department of Mechanical Engineering  
Naval Postgraduate School  
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