



Pushback Rate Control

**The Design and Field-Testing of an
Airport Congestion Control Algorithm**

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Practical algorithms for air transportation

- Goal
 - Develop algorithms that increase **efficiency** and **robustness**, and ensure **safety**...
 - ... while coping with **uncertainty**, **human factors**, and **environmental concerns**

Practical algorithms for air transportation

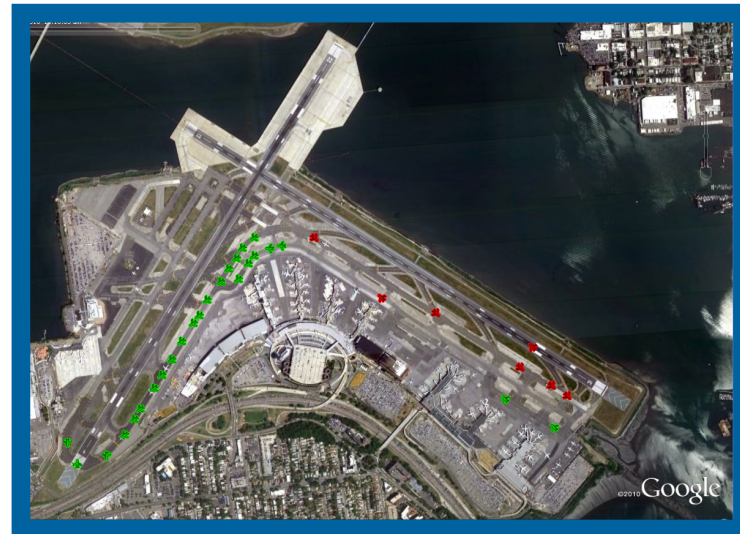
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 - Leverage large amounts of operational data to
 - Build **simple models** for desired objectives and operational constraints
 - Develop and implement **scalable control and optimization** algorithms
- Practical algorithms and decision-support automation are vital to meet future system demands

Practical algorithms for air transportation

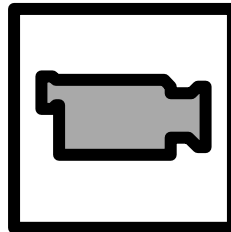
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- Air transportation: Cyber + physical + human components

Airport surface traffic operations

- **Modeling and analysis** of surface operations using data
- **Design and field testing** of congestion control strategies

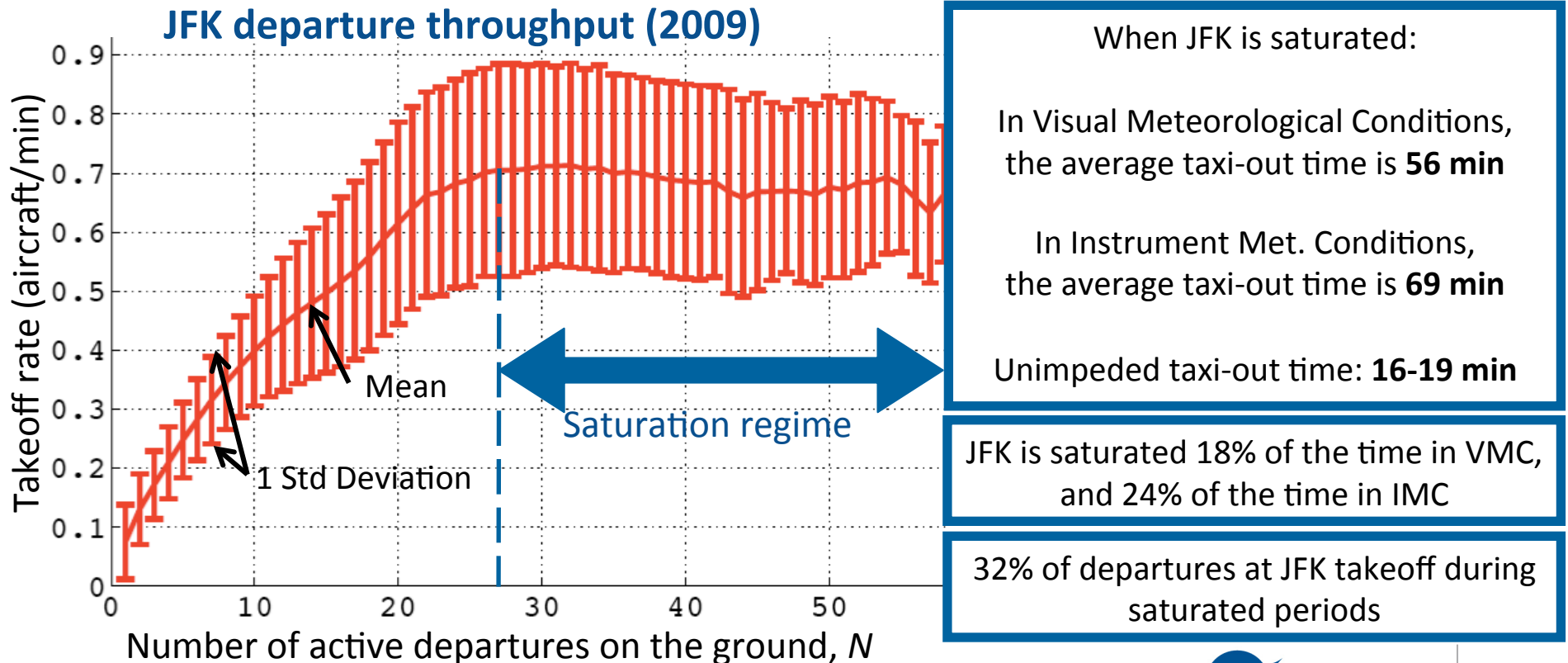


Boston Logan (BOS) airport (6/30/2012)



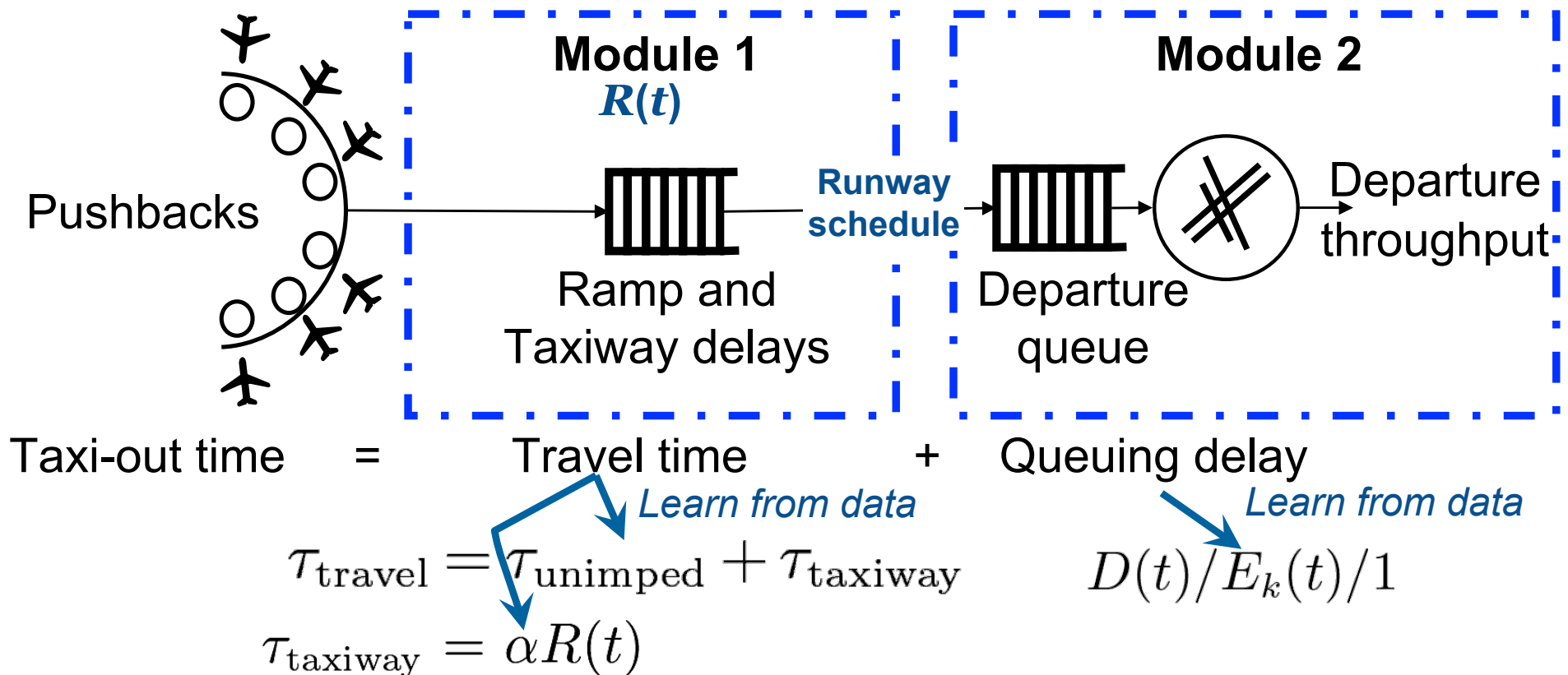
Problem: Airport surface congestion

- Frequent congestion at major airports results in inefficient operations, and increased fuel burn and emissions

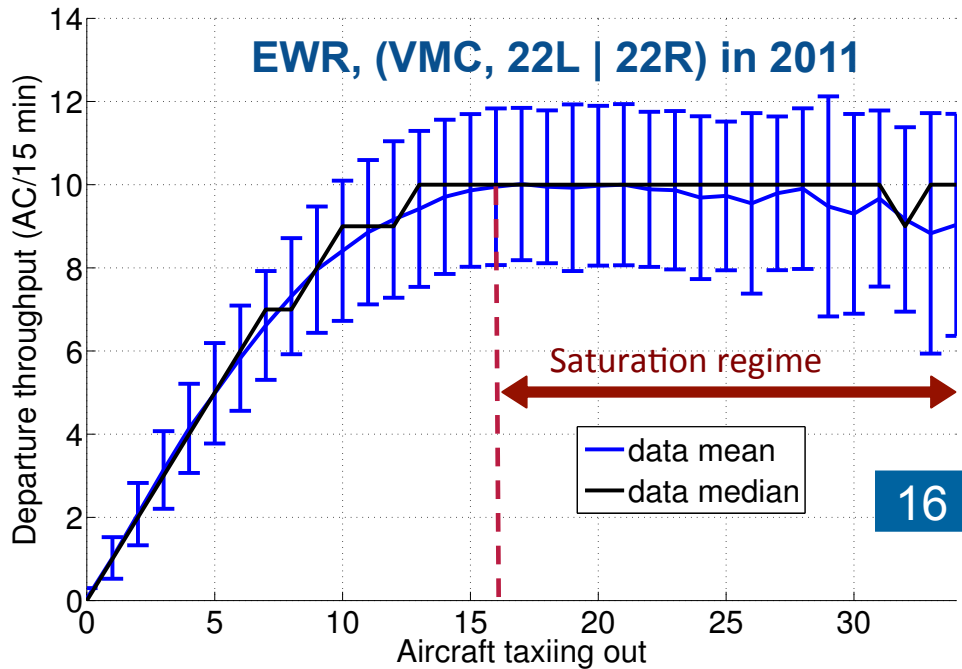


Simaiakis and Balakrishnan, *Transportation Research Record*, 2010
(Confirms Pujet, Delcaire and Feron, BOS 1999).

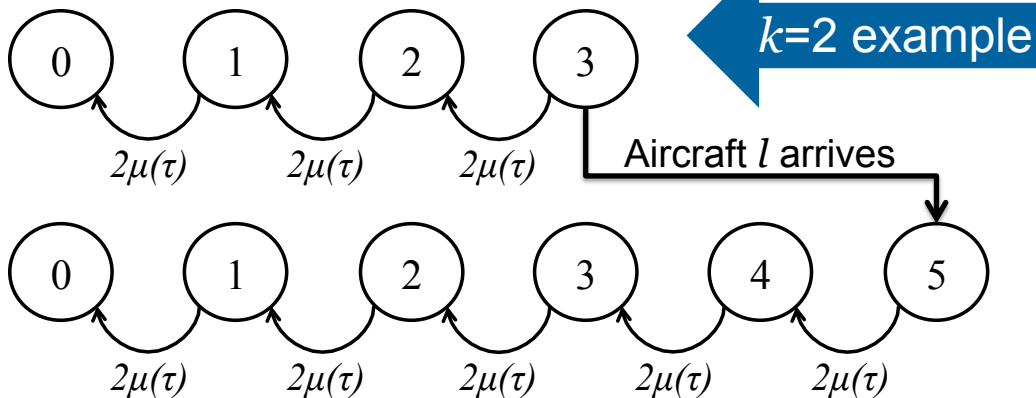
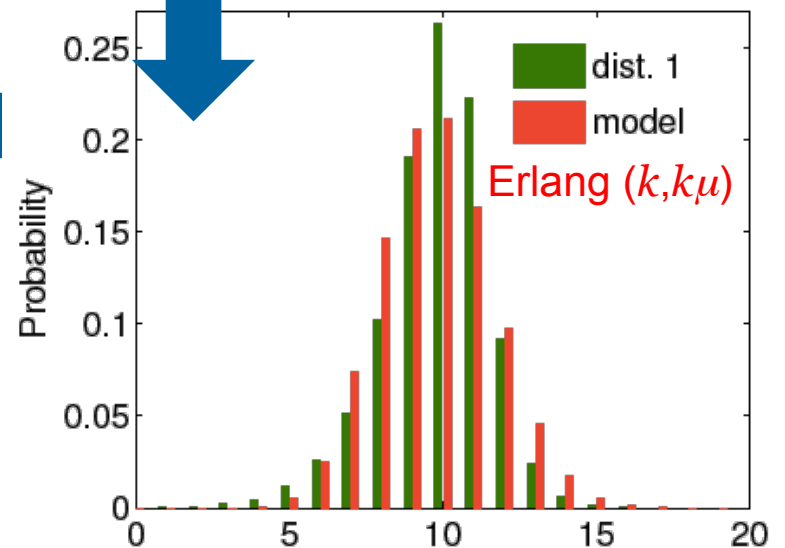
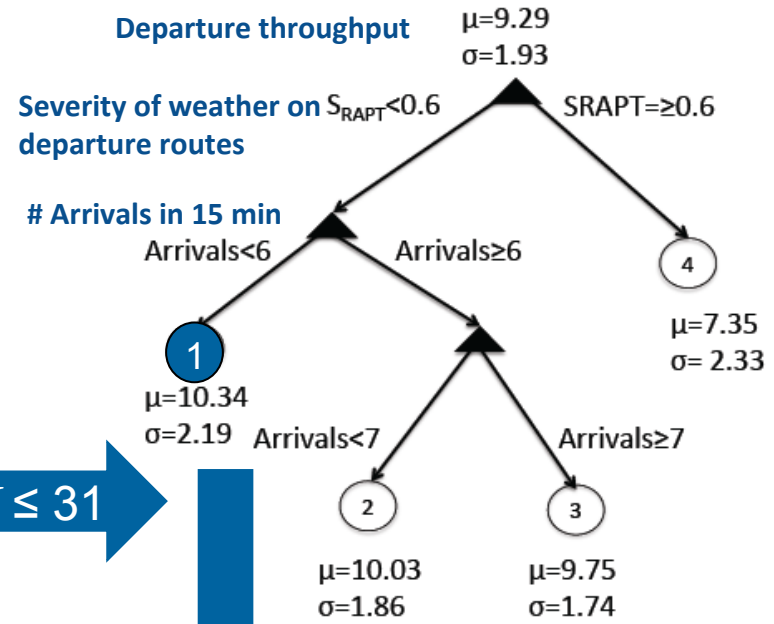
Queuing model of the departure process



Runway service process model



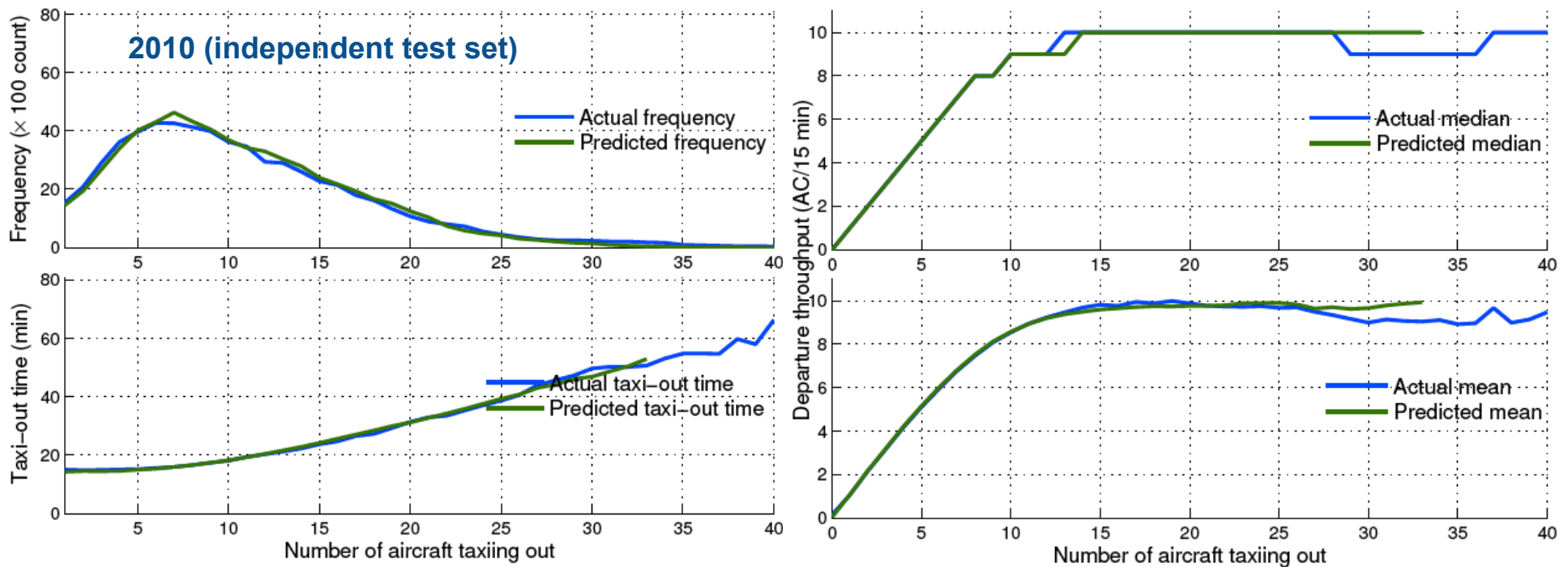
$16 \leq N \leq 31$



$k=2$ example

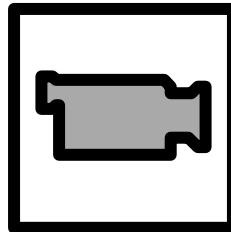
EWR model predictions

- Model parameters identified from 2011 data, predictions carried out on 2010 data (pushback schedules)



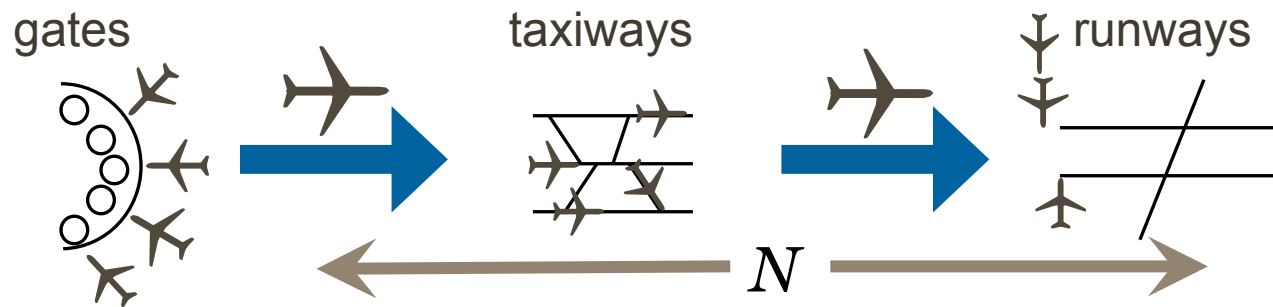
- Similar prediction performance shown for BOS, CLT, DTW, LGA, PHL, ...

PHL operations (08/09/2011)



Airport congestion control

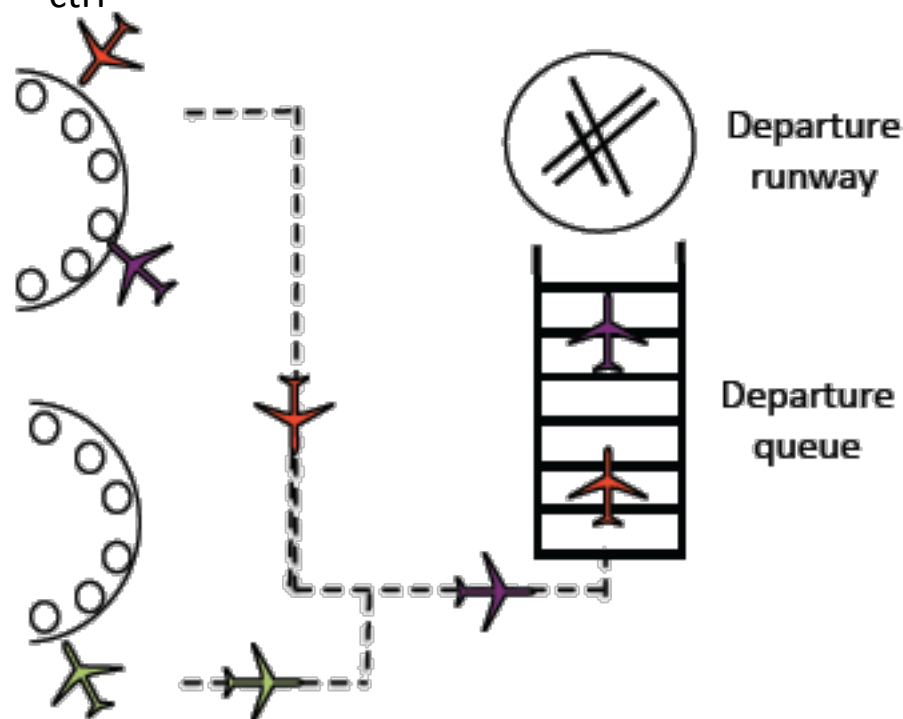
- Aircraft pushback from gates, start their engines, and then taxi until they takeoff



- Control pushbacks in order to maintain runway utilization while avoiding excessive levels of congestion
- Key challenges:
 - How do we design a congestion control strategy?
 - How do we implement control strategy?
 - How do we interface with human controllers?

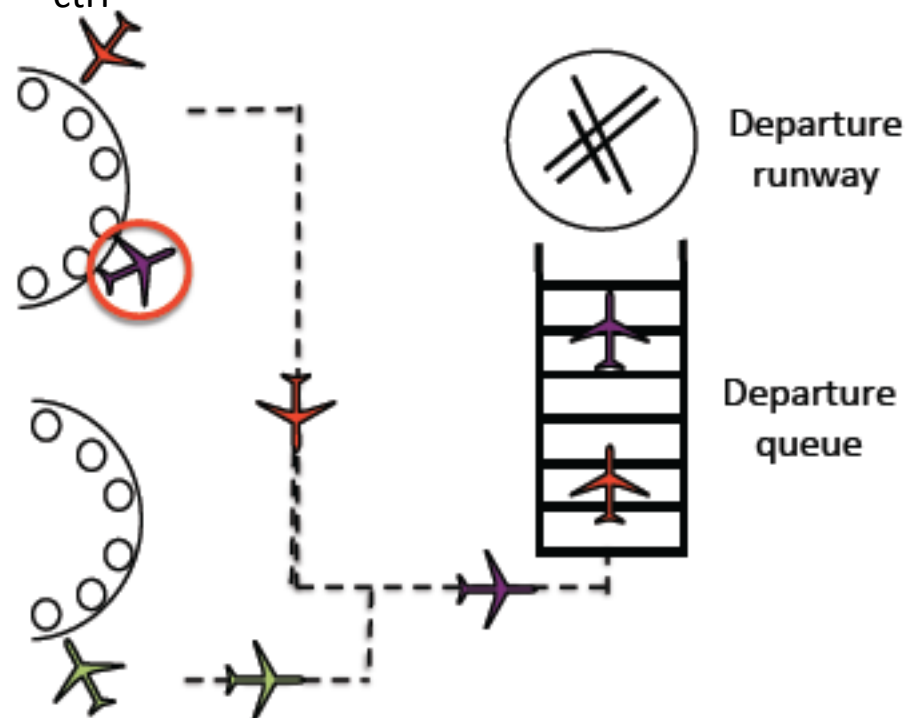
1. Designing control strategy

- Threshold policy (N-control) possible option [Feron et al. 1997]
 - Departure throughput saturates when number of aircraft taxiing out, N , exceeds a certain threshold, N^*
 - Stop pushbacks when N exceeds N_{ctrl} , where $N_{ctrl} \gg N^*$
- Example: $N_{ctrl} = 5$



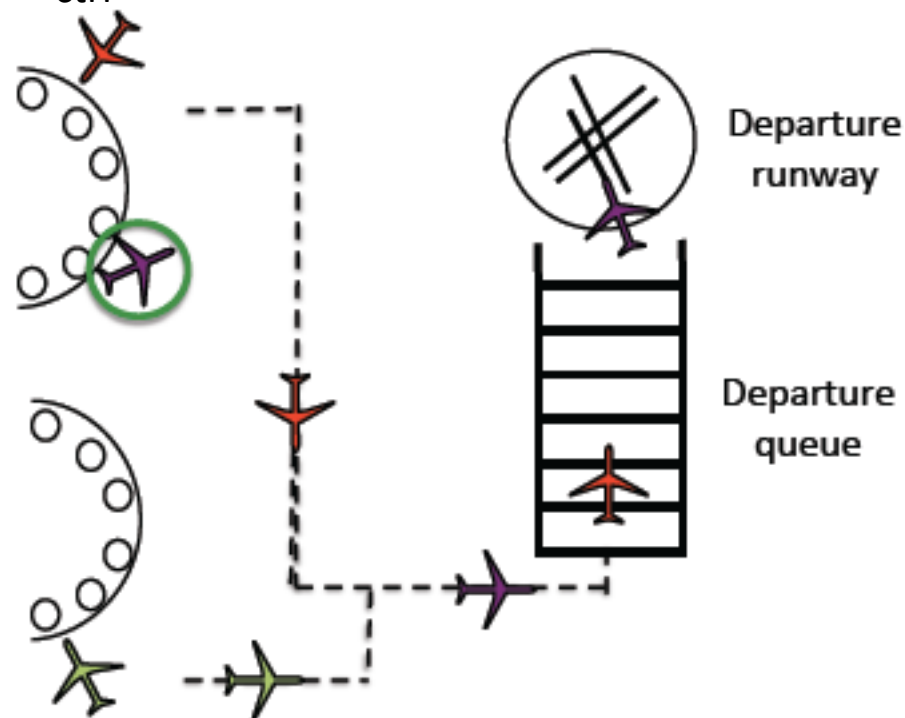
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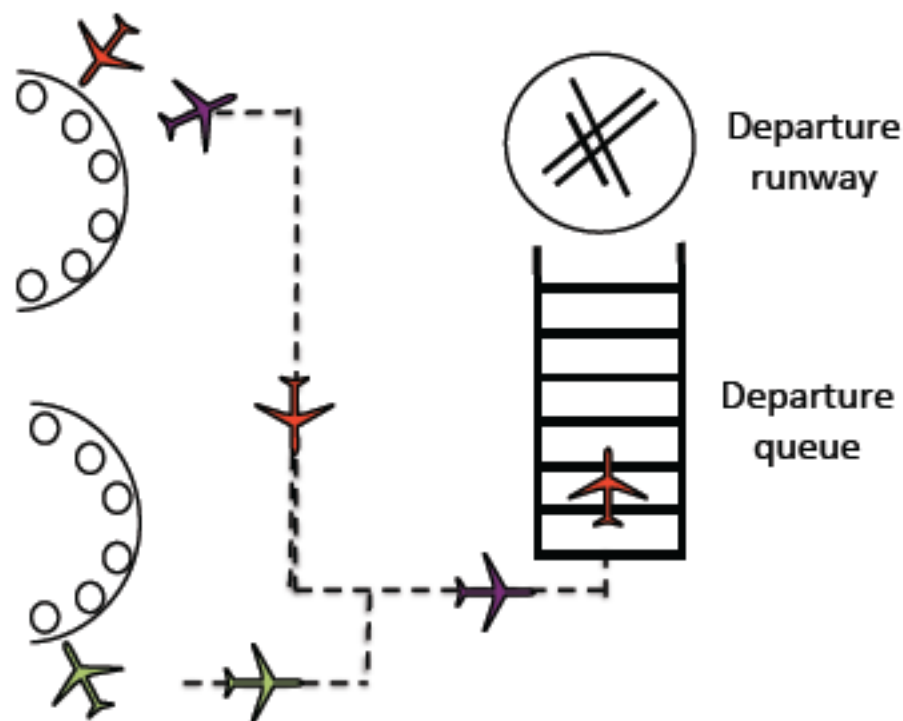
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2. Implementing control strategy

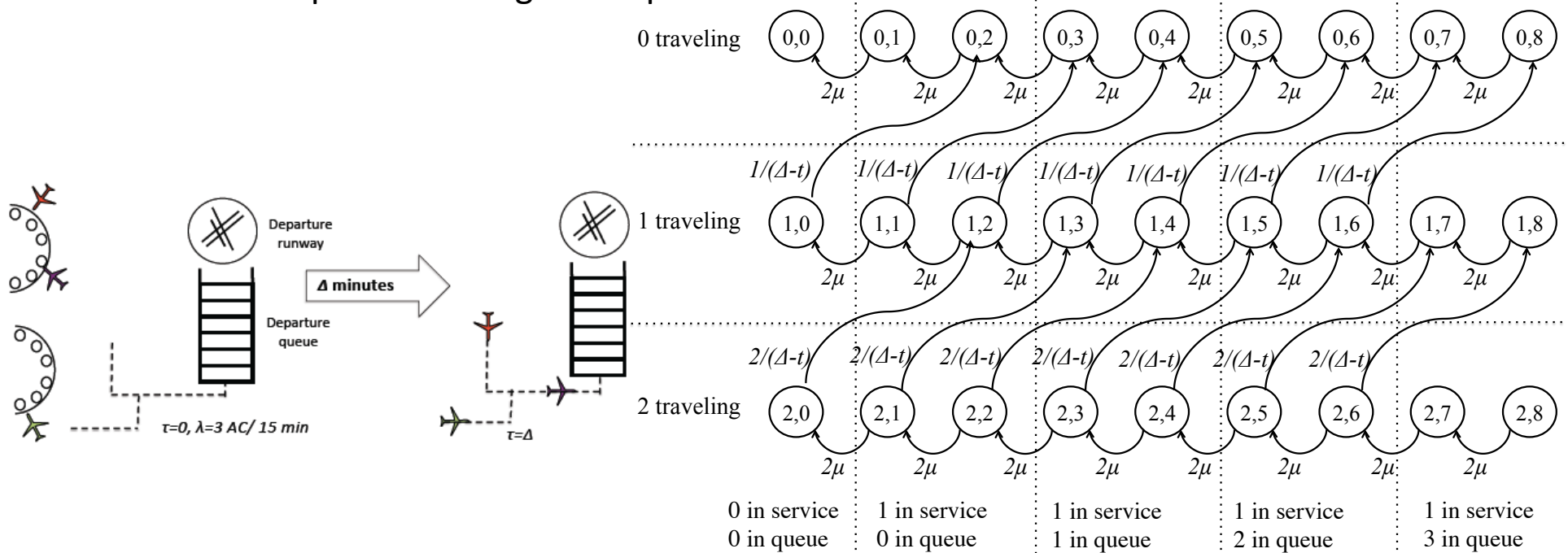
- Threshold control (N-control) does not work in practice
 - Rather than release an aircraft every time that a flight takes off, **controllers prefer a rate** at which to let aircraft pushback from their gates
 - Rate is updated periodically
 - **Pushback Rate Control (PRC)**
- **Option 1:** Adapt N-control policy (PRC v1.0)
- **Option 2:** **(PRC v2.0)** Formulate control problem to
 - Minimize expected queue length
 - Maximize expected number of aircraft served (throughput)

Revisit Step 1. Designing control strategy: Pushback Rate Control

- Dynamic programming formulation to recommend pushback rate, given loading of taxiway and runway queues
- Challenges
 - Random travel time between actuation (at the gate) and queue being controlled (runway)
 - Runway process is a dynamic and stochastic process with a great variability (fleet mix, weather, arrival demand, route availability, human factors)
- State space, $N_t = (D_t, R_t)$: Number of aircraft in departure queue, D_t , and number of aircraft traveling toward departure queue, R_t .
- Time window, Δ : Average travel time from gates to the runway

Departure process model

- At the start of each time window, a pushback rate is chosen
- Pushbacks occur randomly within this time window
- Departure runway service times are Erlang ($k, k\mu$)
 - Departure runway queuing system modeled as $(M(t) | R_\tau) / E_k / 1$
 - Chapman-Kolmogorov equations to describe evolution of Markov chain model



System dynamics

- Queue at next epoch depends on state at current epoch
- State probabilities computed numerically using C-K equations
- Model assumes that $(D_{\tau+\Delta}, R_{\tau+\Delta}) = (f(D_\tau, R_\tau), \lambda_\tau)$
- However, in reality, nonzero probabilities of flights being early or late to reach the runway:

$$(D_{\tau+\Delta}, R_{\tau+\Delta}) = \begin{cases} (f(D_\tau, R_\tau), \lambda_\tau), & \text{w.p. } 1 - \sum \beta_i - \sum \gamma_i \\ (f(D_\tau, R_\tau + i), \lambda_\tau - i), & \text{w.p. } \beta_i, i = 1, \dots, \lambda_\tau \\ (f(D_\tau, R_\tau - i), \lambda_\tau + i), & \text{w.p. } \gamma_i, i = 1, \dots, R_\tau \end{cases}$$

- Cost function:

$$c(D) = \begin{cases} M, & D = 0 \\ D^2 & D = 1, \dots, C \end{cases}$$

- M is the (very high) cost of not utilizing runway (set to equivalent of 25 aircraft in queue)

Dynamic programming formulation

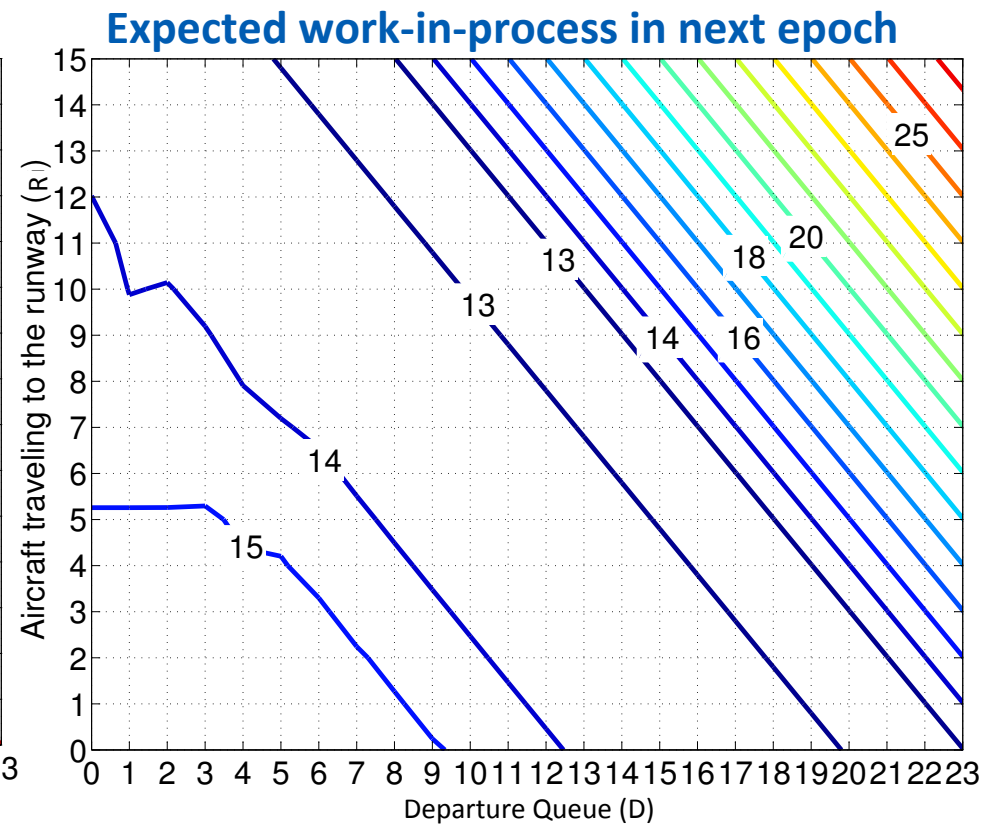
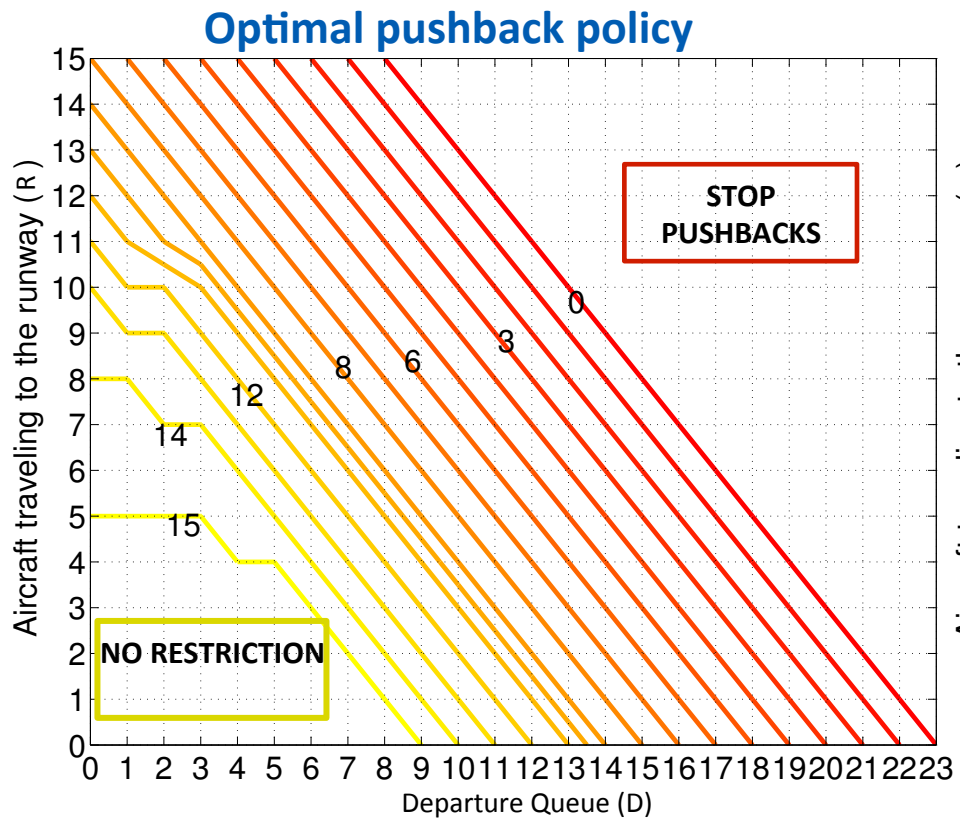
- Bellman equation for infinite horizon average cost problem with discount factor α

$$J^*(q, r) = \min_{\lambda \in \Lambda} \left\{ \begin{aligned} &(1 - \sum \beta_i - \sum \gamma_i)[\bar{c}(q, r) + \alpha \mathbf{p}_q(q, r) \cdot \mathbf{J}^*(\lambda)] \\ &+ \sum \beta_i [\bar{c}(q, r + i) + \alpha \mathbf{p}_q(q, r + i) \cdot \mathbf{J}^*(\lambda - i)] \\ &+ \sum \gamma_i [\bar{c}(q, r - i) + \alpha \mathbf{p}_q(q, r - i) \cdot \mathbf{J}^*(\lambda + i)] \end{aligned} \right\}$$

- Policy iteration converges in fewer than 10 iterations
- Can also be formulated as minimum average cost per stage problem
- Multiple ramp towers can be incorporated

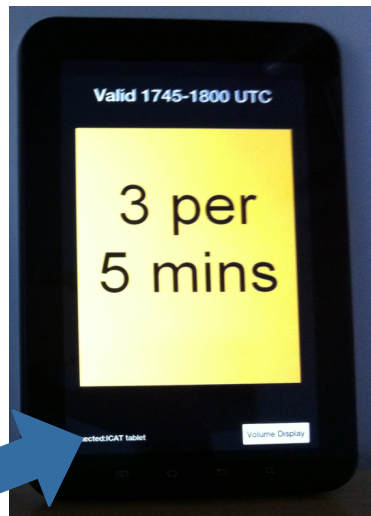
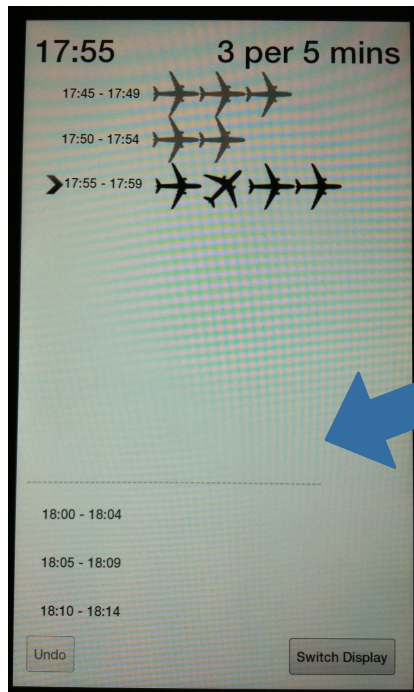
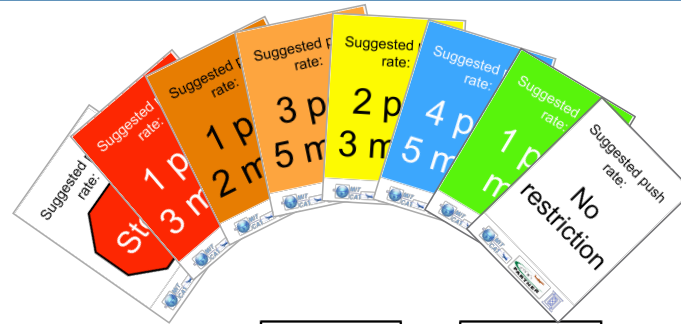
Optimal pushback rate

- BOS (22L, 27 | 22L, 22R) configuration

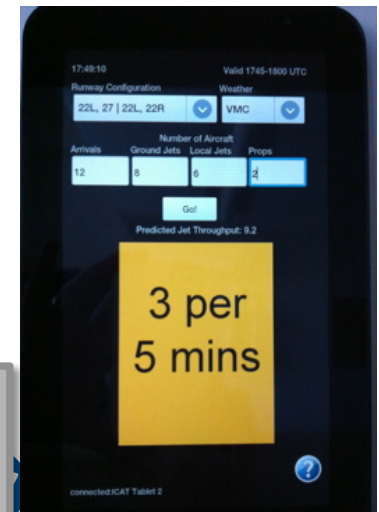
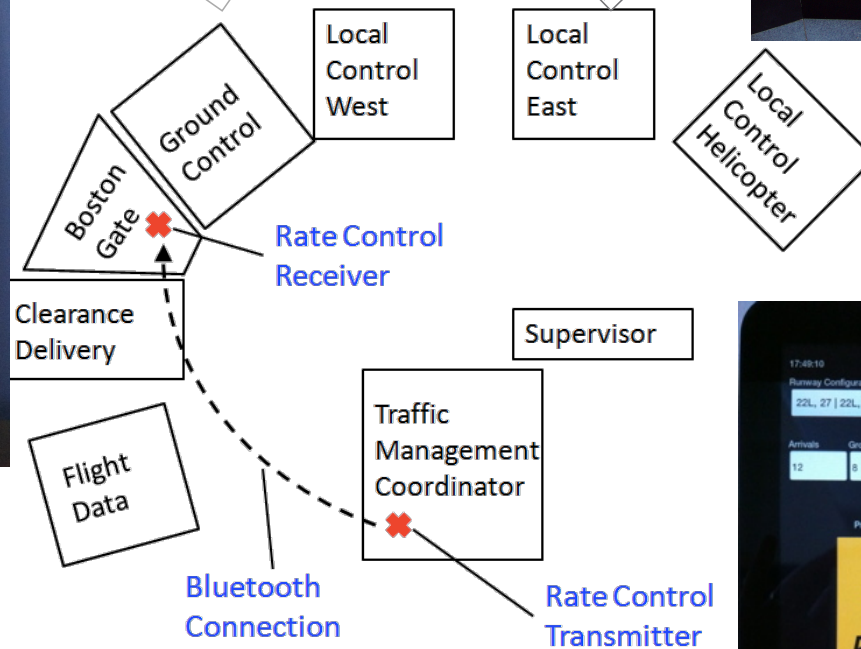


3. Interfacing with human controllers

- Suggest pushback rate (color-coded cards or a tablet display)



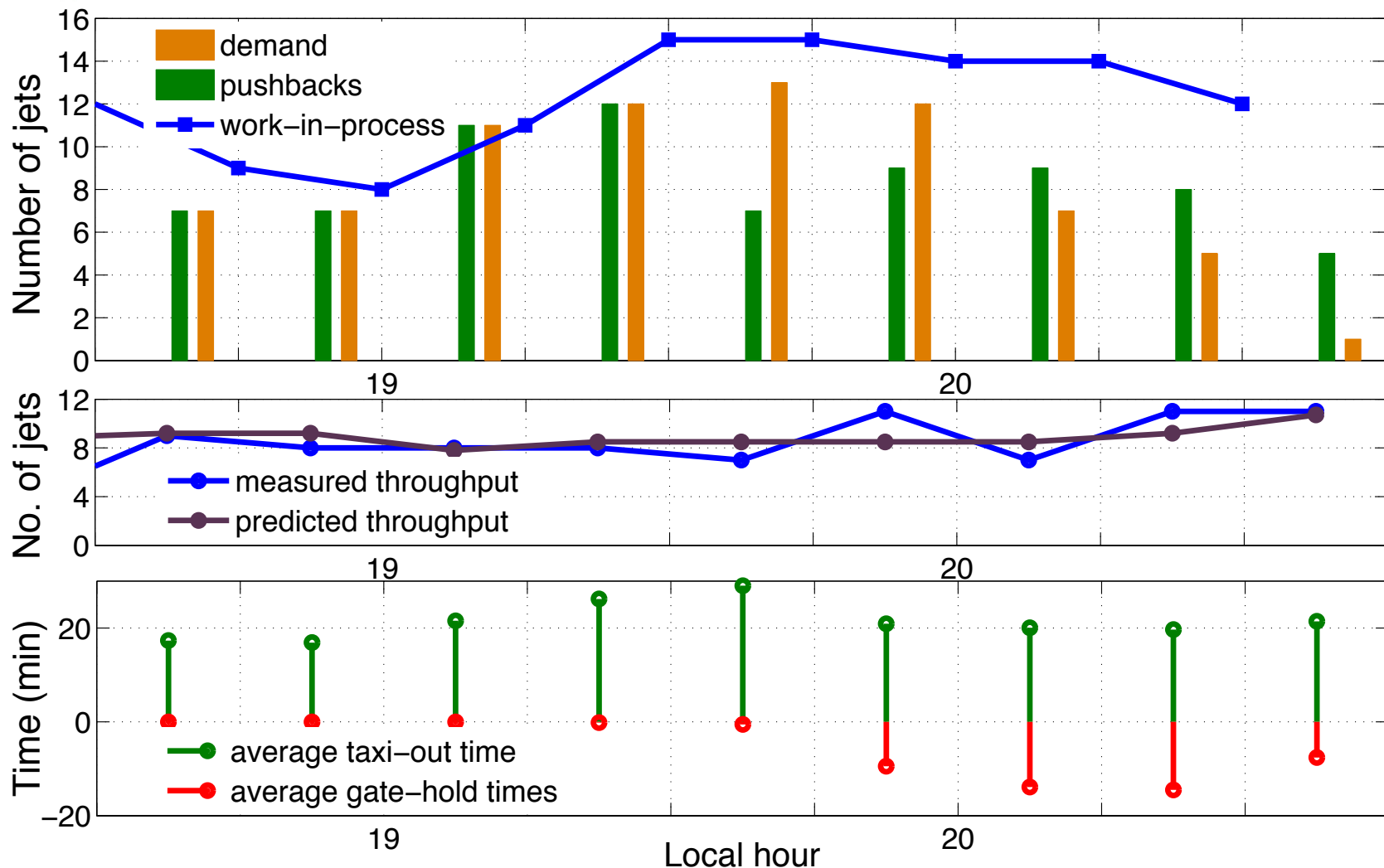
Alternative display modes



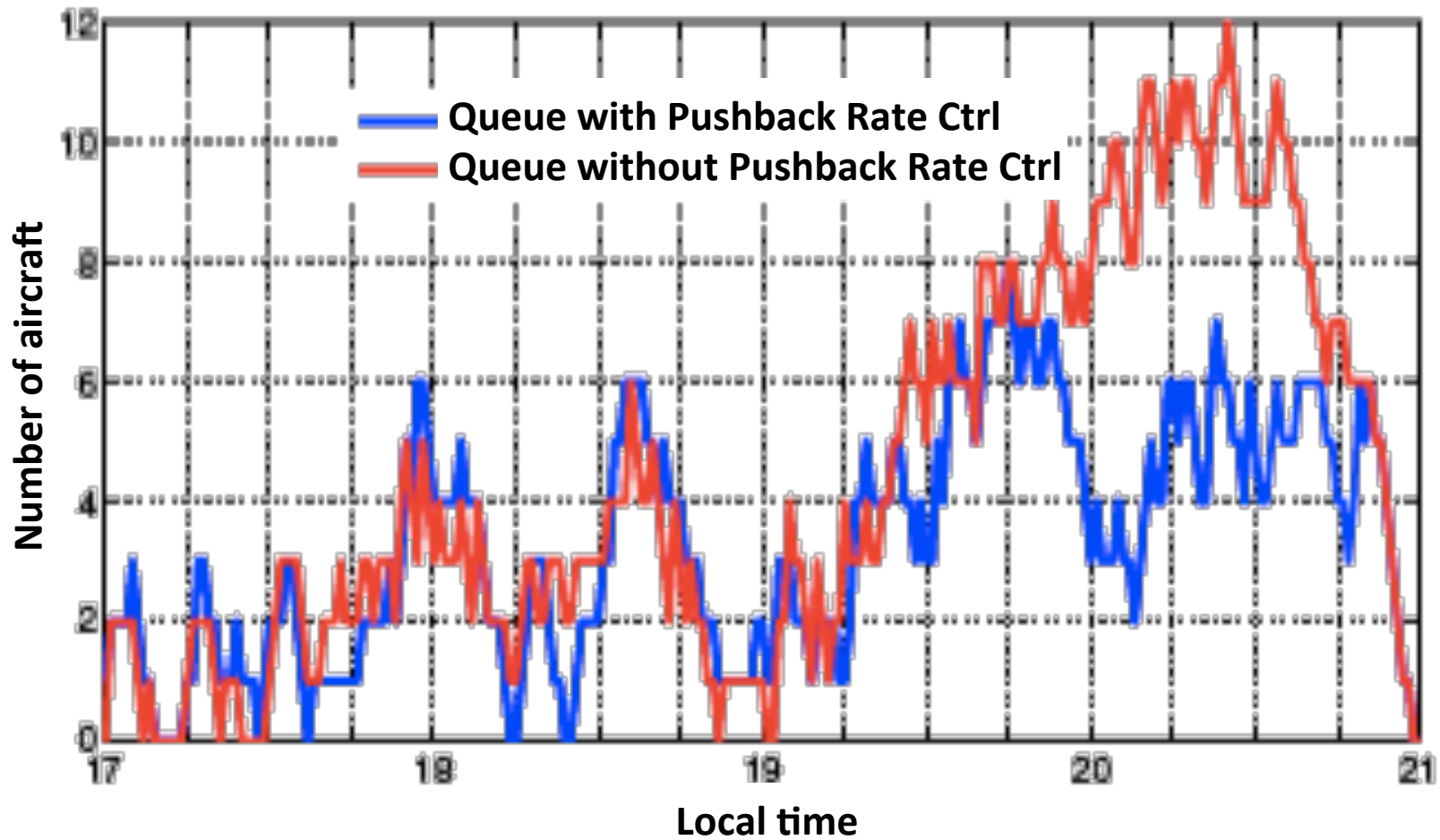
- Pushbacks in current time interval can be released (grayed out)
- Unused rate is carried over to the next time interval, up to 2/min
- Pushbacks in future time intervals can be reserved (angled)
- Pushbacks can be reserved for the following 15-min time period

Sandberg et al.
IEEE Trans. on Human-Machine Systems 2014

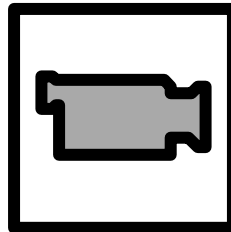
Sample test results: 7/21/2011



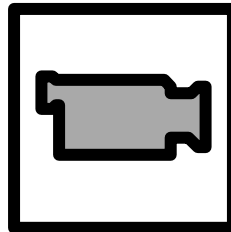
Reduced queue sizes



Visualization of operations (7/21/2011)



Visualization of operations (9/2/2010)



BOS field test results

- Aug-Sep`10 & Jul-Aug`11
- 4PM-8PM departure push
- Average gate-hold: 4.7 min
- 23-25 US tons (6,600-7,300 gal) reduction in fuel burn
- 52-58 kg decrease in fuel burn / gate-held flight
- 71-79 tons CO₂ reduction
- Fair distribution of benefits
- 1 min gate-hold => 1 min of taxi-out time savings
- Positive stakeholder feedback, from both airlines and Tower personnel

Configuration	# of gate holds	Taxi-out time savings (min)
27, 22L 22R	63	256
27, 32 33L	34	114
27, 32 33L	8	38
27, 22L 22R	45	295
27, 22L 22R	19	42
27, 22L 22R	11	23
27, 32 33L	11	24
27, 32 33L	56	210
2010	247	1003 min = 16.7 hours
27, 22L 22R	14	28
27, 22L 22R	42	384
27, 22L 22R	50	290
4L, 4R 4L, 4R,9	11	13
4L, 4R 4L, 4R,9	7	13
27, 22L 22R	6	9
27, 22L 22R	12	23
2011	142	760 min = 12.7 hours

Some other projects:

Prediction of air traffic network delays

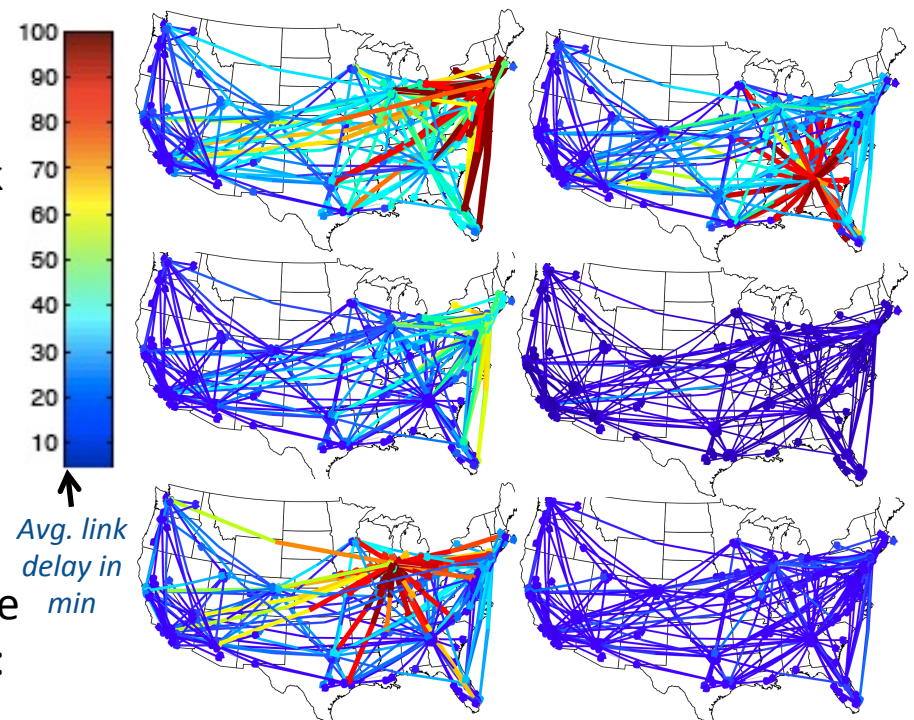
- Predict departure delay on a link considering:

- Current delay state of the network
- Interdependencies between network elements
- Time-of-day and day-of-the-week
- Delays at origin, destination, and on link
- Delay state of National Airspace System
- Type of delay day in the NAS

- Delay states obtained by k -means clustering of delays

- 100 most-delayed OD pairs and major carriers

- Avg. classification test errors to decide whether delays exceed 15 min or not:
 - 18%, 2 hours ahead
 - 21%, 6 hours ahead
- Avg. (regression) median test error:
 - 13.5 min, 2 hours ahead
 - 17.1 min, 6 hours ahead

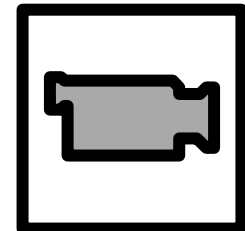


Centroids of NAS delay states.
Color represents avg. link departure delay over 2-hr time-window

Some other projects:

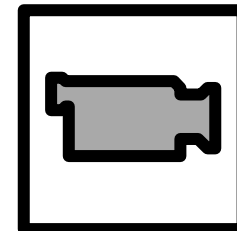
Large-scale Air Traffic Flow Management

- Optimize aircraft trajectories (in space and time) with recourse on a system-wide scale, to accommodate capacity-demand imbalances
 - Use stochastic capacity forecasts (for airspace and ground resources)
 - Consider ground delays, speed changes, reroutes and cancellations
 - Account for operational constraints (flight connectivity, speeds, etc.)
- We solve largest instances of the ATFM to-date, with faster run times
- Case studies drawn from real data:
 - ~17,500 flights
 - 24-h/5-min discretization
 - 370 airports, 375 airspace sectors
 - Deterministic: Optimal in ~5-10 min
 - Stochastic: Optimal in ~30 min
 - Distributed decision-making



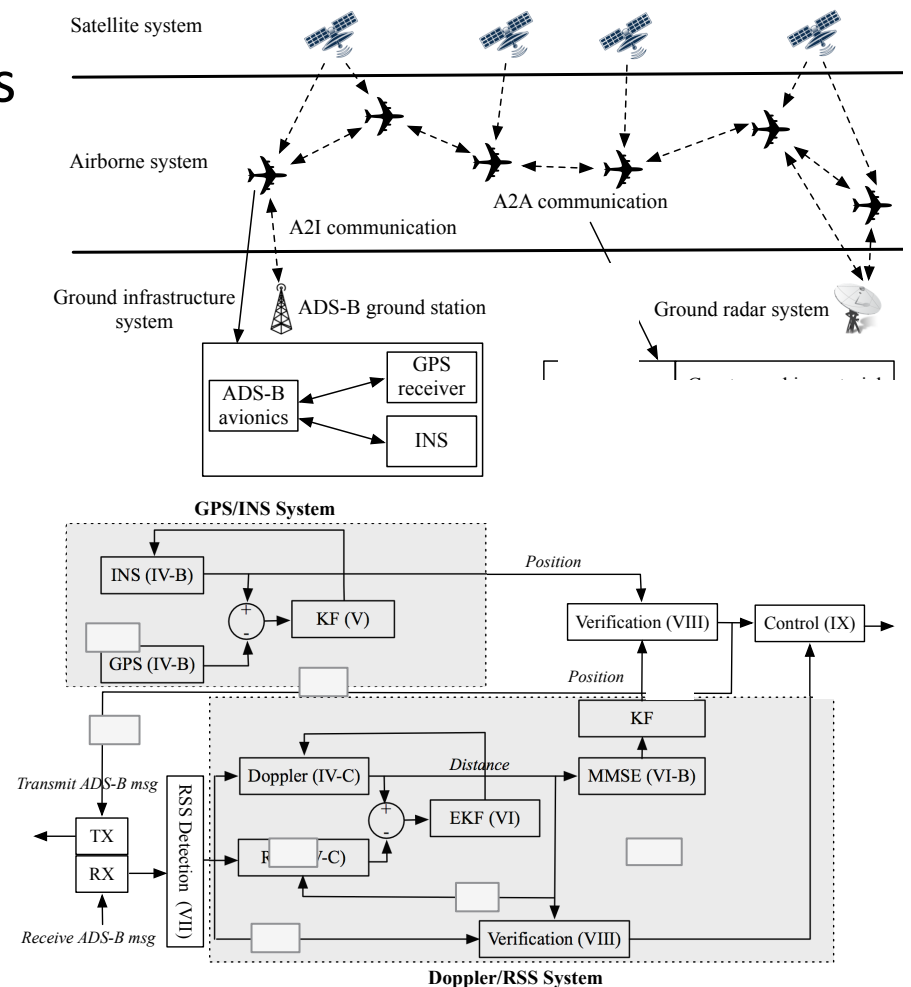
Some other projects: Integrated control & communication protocols

- Objectives: Safety and efficiency
 - Conflict detection and resolution
 - Optimize State Update Interval
 - Minimize flight times
- Decentralized at longer range
 - Low traffic density
 - ADS-B surveillance
 - Max transmit power
- Handover zone
 - Decentralized control
 - Adaptively adjust transmit power
- Centralized close to the airport
 - High traffic density
 - Min transmit power
- Ground radar surveillance
 - Augmented by ADS-B



Some other projects: High-confidence network control for NextGen

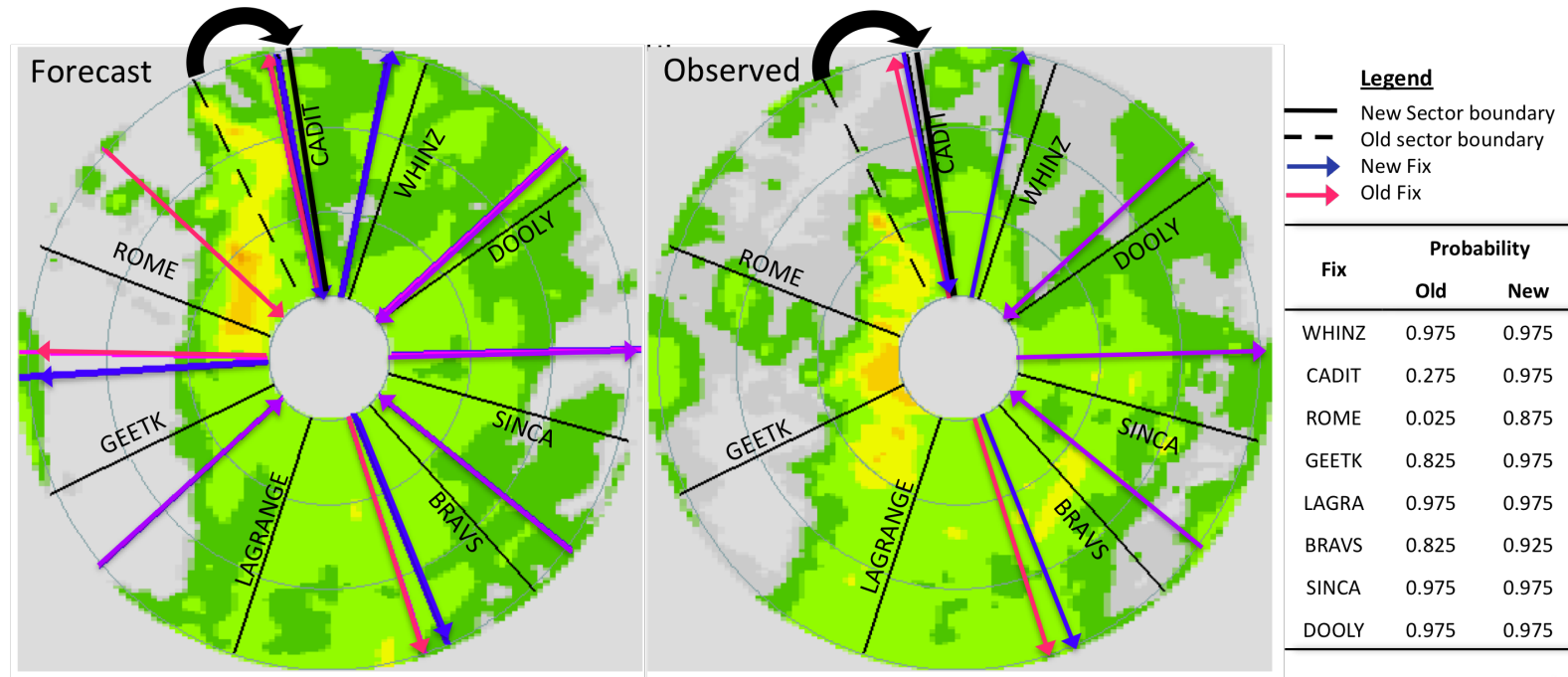
- Secure, fault-tolerant control in the presence of adversaries
 - Distributed control using onboard threat detection
 - GPS and inertial sensor data fusion
 - Verification using Doppler effect and RSS of ADS-B messages from neighboring aircraft
 - Control objectives
 - Conflict avoidance, maintaining separation in the presence of uncertainty
 - Minimizing flight times
 - Fault detection



Some other projects:

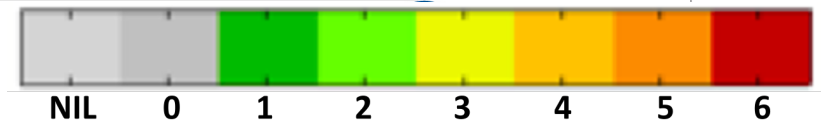
Robust routing through thunderstorms

- Integrating weather forecasts into air traffic management algorithms
 - Given a forecast, can we identify which routes are most likely to remain open, and the associated probabilities?
 - Development and validation of classification algorithms for predicting route blockage using weather and operations data
 - Dynamic airspace reconfiguration using convective weather forecasts



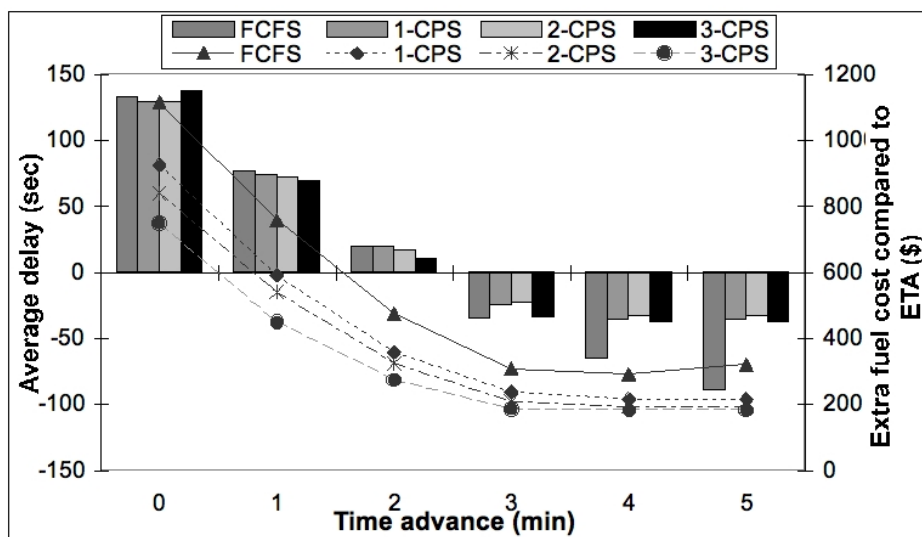
Pfeil and Balakrishnan, *Transportation Science* 2012

Lin and Balakrishnan, *Transportation Research Record* 2014



Some other projects: Arrival/Departure scheduling

- Given a set of flights with estimated arrival times at the airport, the aircraft need to be sequenced into the landing (takeoff) order, and the landing (takeoff) times need to be determined
 - Need minimum (wt. class dependent) wake vortex separation (Safety)
 - Currently FCFS; resequencing could increase throughput (Efficiency)
 - “Fair” resequencing: Constrained Position Shifting (CPS) [Dear 1976]
- Show that scheduling under constrained position shifting can be solved in (pseudo-)polynomial time as shortest-path problems



Balakrishnan and Chandran, *Operations Research* 2010
Lee and Balakrishnan, *Proceedings of the IEEE* 2008

Summary

- Practical ATM algorithms can enhance **system efficiency, robustness and safety**, and address **uncertainty, competition and environmental impact**
 - Leveraging *cyber-physical* aspects of the system is key!
- These challenges arise in all stages of flight as well as on a system-wide scale, including:
 - Data-driven modeling of human decision processes
[Ramanujam and Balakrishnan, *American Control Conference* 2010]
 - Characterizing and providing feedback on operational performance
[Khadilkar and Balakrishnan, *Air Traffic Control Quarterly* 2013]
 - Network modeling and congestion control of airport surface operations
[Khadilkar and Balakrishnan, *AIAA Journal of Guidance, Control and Dynamics* 2014]
 - Mechanisms for resource allocation and reallocation
[Balakrishnan, *Conference on Decision and Control* 2007; Ramanujam and Balakrishnan, *Conference on Decision and Control* 2014]
 - Distributed feedback control of the National Airspace System
[Le Ny and Balakrishnan, *AIAA Journal of Guidance, Control and Dynamics* 2011]
 - Models of engine performance from flight recorder data
[Khadilkar and Balakrishnan, *Transp. Research Part D* 2012;
Chati and Balakrishnan, *ATIO* 2013 and *ICRAT* 2014]