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APPLICATIONS OF NON-PARAMETRIC STATISTICS
AND ANALYSIS OF VARIANCE ON SAMPLE VARIANCES

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Applications of Non-Parametric Statistics and Analysis of Variance on Sample Variances

This report contains two natural distinct parts.

(i) Discussion of nonparametric methods that are available for NASA-type applications. An attempt will be made here to survey what can be used, to attempt recommendations as to when each would be applicable, and to compare the methods, when possible, with the usual normal-theory procedures that are available for the Gaussian analog. It is important here to point out the hypotheses that are being tested, the assumptions that are being made, and limitations of the nonparametric procedures.

(ii) Discussion and study of the appropriateness of doing analysis of variance on sample variances. This procedure is followed in several NASA simulation projects. On the surface this would appear to be a reasonably sound procedure. However, difficulties involved center around the normality problem and the basic homogeneous variance assumption that is made in usual analysis of variance problems. These difficulties will be discussed and guidelines will be given for using the method.

I. Nonparametrics

The nonparametrics survey will be broken down into two parts (a) the two sample problem, and (b) analysis of variance problems. Nonparametric statistics are used in cases where the data is clearly not Gaussian. For example, in the two sample problem, where one is testing for difference between two means, the t-test that is generally used would only apply where

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these data are taken from two normal populations. The same would hold for any F-tests in analysis of variance problems. The test is only correct if each of the populations being compared is Gaussian. Thus for NASA simulation type experiments in which the basic response represents pilot opinions, ratings, etc., or other categorical type responses, nonparametric statistics should be considered as a procedure. Ideally, in multivariate problems where a mixture of responses are used, standard procedure should involve separate analyses, parametric (analysis of variance) and nonparametric (for categorical responses) should be used in the same experiment.

(a) Two Sample Problem

Most of the procedures discussed in I will be tests which are based on ranks of the data. The two sample problem involves data taken under two conditions, called groups. These two groups might represent two pilots, two G-seat conditions, two panel displays, etc. Suppose data is taken from two populations, the model being

$$\begin{aligned} x_i &= \mu + \varepsilon_i & i=1,2,\dots,m \\ y_j &= \mu + \Delta + \varepsilon_{m+j} & j=1,2,\dots,n \end{aligned}$$

Here the ε_i are the usual unobservable random errors that are independent and came from the same population. Thus, we have the same model as is usually applied in univariate analysis comparing two categories. Of course, no distributional assumption is made on the ε_i . We wish to test

$$H_0: \Delta = 0$$

The Wilcoxon Rank Sum Test requires initially ordering the $N = m + n$ from lowest to highest. Then one of the samples, say the y_j are replaced by their ranks, and

$$W = \sum_{j=1}^n R_j$$

is computed, where R_j are the ranks. The test statistic is W and the upper and lower probability points for W are tabulated. Call $w(\alpha, m, n)$ the upper α^{th} per cent point of the distribution W . If the alternative hypothesis is written

$$H_1: \Delta > 0$$

we reject H_0 in favor of H_1 on a one tailed, upper tailed basis. Thus we reject H_0 when $W \geq w(\alpha, m, n)$. Now, for a one-sided alternative in the other direction, i.e., for

$$H_1: \Delta < 0$$

we reject H_0 when $W \leq [n(m+n+1) - w(\alpha, m, n)]$ and accept H_0 otherwise. Tables for the probability points of W are given in Table I. Two sided tests of location for two hypotheses now becomes obvious. One merely rejects H_0 if either

$$W \geq w(\alpha/2, m, n)$$

or

$$W \leq [n(m+n+1) - w(\alpha/2, m, n)]$$

and accept otherwise.

Normal Approximation of W

When the sample sizes for each category are larger (say greater than twenty) a normal approximation can be used very simply. This does not imply that we are assuming that the data is normal, merely that the rank sum W is asymptotically normal. In this case W is asymptotically normal with mean $n(m+n+1)/2$ and variance $mn(m+n+1)/12$ under the hypothesis of equal means. Thus the test procedure would be to compute a standardized W , say W^* , where

$$W^* = \frac{W - [n(m+n+1)/2]}{[mn(m+n+1)/12]^{1/2}}$$

and reject or accept according to one or two-sided (depending on the alternative) probability points of the standard normal distribution. One advantage of this procedure is that it results in a simple way of computing the power so one can rather easily determine if the sample sizes are adequate.

Ties. Minor modifications are made in the procedure if ties occur. Average ranks are used to compute the statistic W in the usual test. For the large sample approximation the W is calculated using average ranks, and the quantity $[mn(m+n+1)/12]^{1/2}$ is replaced by

$$\frac{mn}{12} \left[m+n+1 - \frac{\sum_{j=1}^g t_j (t_j^2 - 1)}{(m+n)(m+n-1)} \right]$$

Here g is the number of tied groups, and t_j is the size of tied group j .

Two-Sample Dispersion Problem

A reasonable nonparametric test exists for testing differences between variances of two populations when the samples are independent. Again, the populations do not have to be Gaussian. The application would be in areas where an alternative to the F-test on variances is needed. Again, it is assumed that $N = m + n$ independent observations are taken, m from the first population and n from the second. The hypothesis in question is

$$H_0: \gamma^2 = 1$$

where $\gamma = \sigma_2/\sigma_1$ the ratio of the two scale parameter for the two populations σ_2 for the x 's and σ_1 for the y 's. Once again, a ranking of the data is accomplished. The ranking is as follows: Assign rank 1 to the smallest and largest observation (for the complete array). Assign rank 2 to the second smallest and second largest, and continue. If N is even, the array of ranks is 1, 2, 3, ..., $N/2$, $N/2$, ..., 3, 2, 1 and if N is odd the array is 1, 2, 3, ..., $(\frac{N-1}{2})$, $(\frac{N+1}{2})$, $(\frac{N-1}{2})$, ..., 3, 2, 1. Again if we denote the observations as x_i ($i=1,2,\dots,m$) for the first group and y_i ($i=1,2,\dots,n$) for the second group, and denote R_i as the ranks of say the x_i , call

$$W = \sum_{i=1}^m R_i,$$

where again the test criterion depends on the rank sum statistic W . Call $\omega_2(\alpha, m, n)$ the upper α^{th} percentage point of the distribution. Then we reject H_0 of equal variances if

$$W \geq \omega_2(\alpha, m, n)$$

in the case of $H_1: \gamma^2 > 1$. For the alternative $H_1: \gamma^2 < 1$ we reject on small values of W . These lower tail percentage points are also tabulated and will be supplied. In addition, two sided tests can be conducted, with the hypothesis of equal variance accepted if

$$\omega_1(\alpha/2, m, n) < W < \omega_2(\alpha/2, m, n)$$

where $\omega_1(\alpha/2, m, n)$ is the $\alpha/2$ lower tailed percentage point. The above test is called the Ansari-Bradley test. Table II gives percentage points of the statistic W .

As in the case of the Wilcoxon test on location, there is a normal theory approximation to the test on variances. Again, this is helpful if the sample sizes are large and one is in need of getting an approximate power for the test. One merely computes

$$W^* = \frac{W - [m(m+n+2)/4]}{\{mn(m+n+1)[3+(m+n)^2]/[48(m+n)^2]\}^{1/2}} \quad \text{if } m+n \text{ is odd}$$

$$= \frac{W - \{m(m+n+1)^2/[4(m+n)]\}}{\{mn(m+n+1)[3+(m+n)^2]/[48(m+n)^2]\}^{1/2}} \quad \text{if } m+n \text{ is even}$$

and make appropriate tests on the $N(0,1)$ distribution. An important restriction here is that the means are assumed to be equal for the two groups, though if they are not equal, one can replace observations x_i by $x_i - \bar{x}$ and y_i by $y_i - \bar{y}$.

Again, ties in the data do not present difficulties. In the exact test one merely uses average ranks. For the large sample approximation,

the above $N(0,1)$ statistic is altered in the denominator, which is $\sqrt{\text{Var}(W)}$ under H_0 . $\text{Var}(W)$ becomes

$$\text{Var}(W) = \frac{\{mn[16 \sum_{j=1}^g t_j r_j^2 - (m+n)(m+n+2)^2]\}}{16(m+n)(m+n-1)} \quad (m+n \text{ even})$$

$$= \frac{\{mn[16(m+n) \sum_{j=1}^g t_j r_j^2 - (m+n+1)^4]\}}{16(m+n)^2(m+n-1)} \quad (m+n \text{ odd})$$

Again, t_j is the size of the tied group j and r_j is the average rank of the observation in the tied group j .

(b) Analysis of Variance - One Factor Problem

It is of interest here to present nonparametric methods for comparing means from say k categories or treatments, e.g., k test panels. Data, again, is obviously non-Gaussian. Suppose the data is of the form

1	2	3	...	k
x_{11}	x_{21}	x_{31}	...	x_{k1}
x_{12}	x_{22}	x_{32}	...	x_{k2}
\vdots	\vdots	\vdots		\vdots
x_{1,n_1}	x_{2,n_2}	x_{3,n_3}		x_{k,n_k}

As in all one-factor problems, the basic model is

$$x_{ij} = \mu + \tau_i + \epsilon_{ij} \quad \begin{array}{l} j=1,2,\dots,n_i \\ i=1,2,\dots,k \\ \sum_{i=1}^k n_i = N \end{array}$$

The ϵ_{ij} are independent from the same distribution. We again, test

$$H_0: \tau_1 = \tau_2 = \dots = \tau_k .$$

The test statistic is quite simple and actually has structure that somewhat resembles the analysis of variance F statistic. The procedure is called the Kruskal-Wallis procedure and is based on the statistic

$$H = \frac{12}{N(N+1)} \sum_{j=1}^k n_j (R_{j\cdot} - R_{\cdot\cdot})^2$$

$$= \left(\frac{12}{N(N+1)} \sum_{j=1}^k R_j^2/n_j \right) - 3(N+1)$$

where we have ranked all N observations jointly from least to greatest and r_{ij} denotes the rank of x_{ij} , R_j the sum of the ranks received by treatment j, $R_{j\cdot} = R_j/n_j$, and $R_{\cdot\cdot}$ is the average rank which is $\frac{N+1}{2}$. There are two procedures, one based on a large sample approximation and is given by

$$\text{Reject } H_0 \text{ if } H \geq \chi_{k-1, \alpha}^2$$

where $\chi_{k-1, \alpha}^2$ is the upper α^{th} probability point of the χ^2 distribution with $k-1$ degrees of freedom. For small samples, tables exist for the exact distribution of H under H_0 and thus one can use the exact test. The percentage points are given in Table III. As one can see, the exact tables are somewhat limited and thus one often must resort to the χ^2 distribution.

For ties, the user merely computes H by using average ranks and then compute

$$H' = \frac{H}{1 - \left(\sum_{j=1}^g T_j / [N^3 - N] \right)}$$

Here g is the number of tied groups, t_j is the size of the j^{th} tied group, and $T_j = (t_j^3 - t_j)$.

Multiple Comparisons

Though procedures for making paired or multiple comparisons following an analysis of variance in a nonparametric setting are rare, some do exist though they generally tend to be considerably more conservative than their parametric counterparts. Probably the most effective method of paired or multiple comparisons is based on the q-statistic or Tukey's procedure which was outlined and discussed in a previous report. Namely, if the Kruskal-Wallis test rejects the hypothesis of equality of treatments we can decide treatments u and v differ when

$$|R_{u\cdot} - R_{v\cdot}| \geq q(\alpha, k, \infty) \left[\frac{k(kn+1)}{12} \right]^{1/2}$$

(only for equal sample sizes n)

The quantity under the square root is the standard error of the rank r_{ij} . For unequal sample sizes an alternative procedure is to declare a significant difference when

$$|R_{u\cdot} - R_{v\cdot}| \geq Z_{\alpha} / [k(k-1)] \left[\frac{N(N+1)}{12} \right]^{1/2} \left(\frac{1}{n_u} + \frac{1}{n_v} \right)^{1/2}$$

(c) The Two-Factor Nonparametric Analysis of Variance

Suppose the model is a fairly simple one, namely there are nk observations with one observation taken from each of k treatments in n blocks, with the model being

$$x_{ij} = \mu + \tau_i + \beta_j + \epsilon_{ij}$$

and the errors are mutually independent and come from the same population.

Once again, we wish to test the hypothesis

$$H_0: \tau_1 = \tau_2 = \dots = \tau_k$$

The test, called the Friedman test is conducted as follows:

Within each block rank the k observations from lowest to highest.

Let r_{ij} denote the rank of x_{ij} in the joint ranking $x_{1j}, x_{2j}, \dots, x_{kj}$, and let $R_i = \sum_{j=1}^n R_{ij}$, $R_{i.} = \frac{R_i}{n}$ and of course $R_{..} = \frac{k+1}{2}$. Thus R_i is the sum of the ranks received by treatment i and $R_{i.}$ is the average rank received by treatment i . The test statistic is given by

$$\begin{aligned} S &= \frac{12n}{k(k+1)} \sum_{i=1}^k (R_{i.} - R_{..})^2 \\ &= \left[\frac{12}{nk(k+1)} \sum_{i=1}^k R_i^2 \right] - 3n(k+1) \end{aligned}$$

As usual there are two approaches. The statistic S can be compared to upper tail points of the χ_{k-1}^2 distribution or the exact percentage points of the distribution S can also be used. The exact percentage points are given in Table IV for 5 treatments and less. Note here, of course, the

strong resemblance between S and the treatment mean square used in parametric analysis of variance and, of course, here one is looking for significant differences between average rank.

If ties exist in the data, average ranks are used and S is replaced by

$$S' = \frac{12 \sum_{j=1}^k (R_j - nR_{..})^2}{nk(k+1) - [1/(k-1)] \sum_{i=1}^n \{ (\sum_{j=1}^{g_i} t_{i,j}^3) - k \}}$$

where g_i is the number of tied groups in block i , t_{ij} is the size of the j^{th} tied group in block i , and untied values within a block are counted as ties of size 1.

The test described here must be made in the case of a model with no interaction and one observation per combination of treatment and block. Paired or multiple comparisons can be made using q -statistics in the same fashion discussed previously. There is no exact nonparametric procedure for detecting interaction. In addition, there is no exact procedure for doing analysis of variance when more than two factors are involved. However, one procedure which appears to perform quite well under limited conditions when data is not normal and several factors are involved is the following:

- (a) Suppose there are three factors, A, B, and C with factor A at a levels. Take each (B-C) combination and treat them as "blocks".
- (b) In each "block", rank the a -treatments.
- (c) Do an analysis of variance (F-test, etc.) on A using the resulting ranks.

(d) The same procedure can now be used to test factors B and C. It should however be emphasized that this "analysis of variance of ranks" does not detect interaction.

It is imperative that when nonparametric procedures are necessary the number of factors should be kept low, i.e., the experiment should be a simple one. The main reason for this recommendation is that interaction cannot be detected and the exact procedures (Kruskal-Wallis and Friedman tests) only cover through a two factor model.

Examples. The following pages show sample data and computer print-out for the Wilcoxon test, Ansari-Bradley test, and Kruskal-Wallis test.

II. Analysis of Variance on Sample Variances

As was mentioned earlier, the second part of this phase involves a study of the appropriateness of doing analysis of variance on sample variances. Our approach to the problem is to determine how large the sample sizes for the sample variances must be in order that the method be a reasonable one. Sample variances follow a χ^2 distribution (apart from scale factor) and of course χ^2 variates are asymptotically normal. The obvious question is "How much information must be in each sample variance before the method results in only a negligible error?"

Let us begin by assuming that we have an analysis of variance problem with the basic unit being a sample variance s_i^2 and that the "sample size", i.e., the number of sample variances in each cell is say n . More importantly we must specify that m independent observations were used in creating the sample variances. Thus $r=m-1$ degrees of freedom are associated with each sample variance. Now, of course, to do analysis of variance on these

RANK-SUM EXAMPLE

IN THIS DATA SET THERE ARE 20 X-OBSERVATIONS AND 20 Y-OBSERVATIONS.

X-VALUES:

2.00000	3.00000	2.00000	4.00000	1.00000
4.00000	5.00000	2.00000	3.00000	5.00000
5.00000	4.00000	3.00000	2.00000	4.00000
1.00000	4.00000	5.00000	2.00000	5.00000

Y-VALUES:

4.00000	3.00000	2.00000	1.00000	1.00000
4.00000	2.00000	3.00000	2.00000	1.00000
4.00000	5.00000	3.00000	1.00000	4.00000
1.00000	2.00000	3.00000	2.00000	2.00000

THE WILCOXON RANK SUM STATISTIC $W = 343.50000$

AND THE LARGE SAMPLE APPROXIMATION $Z = -1.84138$.

Wilcoxon-Two Sample

significant at approx. .07 level

TEST DATA RUN FOR ANSARI-BRADLEY PROCEDURE.

IN THIS DATA SET THERE ARE 20 X-OBSERVATIONS AND 20 Y-OBSERVATIONS.

X-VALUES:

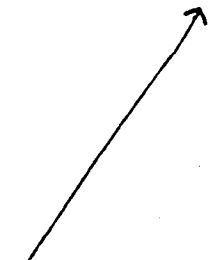
111.00000	107.00000	100.00000	99.00000	102.00000
106.00000	109.00000	108.00000	104.00000	99.00000
101.00000	96.00000	97.00000	102.00000	107.00000
113.00000	116.00000	113.00000	110.00000	98.00000

Y-VALUES:

107.00000	108.00000	106.00000	98.00000	105.00000
103.00000	110.00000	105.00000	104.00000	100.00000
96.00000	108.00000	103.00000	104.00000	114.00000
114.00000	113.00000	108.00000	106.00000	99.00000

THE ANSARI-BRADLEY STATISTIC IS: 105.50000
AND THE LARGE SAMPLE APPROXIMATION IS: -1.53028 .

Normal Approximation



not significant

KRUSKAL-WALLIS ONE-WAY ANOVA RANKED DATA

HIS KRUSKAL-WALLIS TEST HAS 5 TREATMENTS WITH THE FOLLOWING SIZES PER TREATMENT:

10 10 10 10 10

TREATMENT	1	2	3	4	5
9.00000	8.00000	7.00000	6.00000	5.00000	
5.00000	10.00000	9.00000	7.00000	6.00000	5.00000
6.00000	6.00000	5.00000	7.00000	6.00000	7.00000
10.00000	4.00000	5.00000	6.00000	5.00000	7.00000
1.00000	2.00000	7.00000	5.00000	3.00000	5.00000
3.00000	2.00000	7.00000	5.00000	3.00000	5.00000
2.00000	1.00000	5.00000	2.00000	4.00000	5.00000
3.00000	2.00000	4.00000	2.00000	4.00000	5.00000
6.00000	5.00000	7.00000	3.00000	2.00000	4.00000
4.00000	5.00000	5.00000	3.00000	2.00000	1.00000

1E TREATMENT RANK SUMS ARE

374.0000

2E TREATMENT RANK SUMS ARE

356.5000

3E TREATMENT RANK SUMS ARE

203.5000

4E TREATMENT RANK SUMS ARE

134.5000

5E TREATMENT RANK SUMS ARE

206.5000

HE STATISTIC H (WITH 4 DEGREES OF FREEDOM) = 20.94753
 AND THE TIES CORRECTED (ADJUSTED) H IS 20.94753
 WITH 4 DEGREES OF FREEDOM.

Treatment Rank Means

	1	2	3	4	5
	37.4	35.65	20.35	13.45	20.65
37.4		1.75	17.05	23.95**	16.75
35.65			15.30	22.20**	15.00
20.35				6.90	.30
13.45					7.20
20.65					

.05 q = 3.86 from q statistic tables

.01 q = 4.60

$$q_{\alpha=.05} \sqrt{\frac{K(KN+1)}{12}} = 17.78$$

$$q_{\alpha=.01} \sqrt{\frac{K(KN+1)}{12}} = 21.22$$

s_j^2 one must assume that the s_j^2 are normal with common variance. If the individual data points are Gaussian prior to forming sample variances, then the s_j^2 are distributed as $\frac{\chi_r^2 \sigma^2}{r}$, where σ^2 is the variance of the basic measurement. The homogeneous variance assumption on the s_j^2 certainly holds under the hypothesis being tested in the analysis of variance. In fact if we assume that m is the same value for each sample variance, then

$$\text{Var } s_j^2 = \frac{2\sigma^4}{r}$$

It is well known that the variate

$$\frac{\chi_r^2 - r}{\sqrt{2r}}$$

which is a standardized form of χ_r^2 , approaches $N(0,1)$ as r grows large. The basic issue then concerns how quickly the χ^2 variate approaches normality or more specifically, how does the nature of the distribution of s^2 (essentially chi-square) effect the performance of the analysis of variance.

Much work has been done on the robustness or sensitivity of analysis of variance to non-normal data. The bibliography listed in this document lists many pieces of work in this area. The general consensus of these works is that the analysis of variance is very insensitive to non-normality under a wide class of conditions. If the parent distribution is continuous and bell shaped, the performance of analysis of variance is very good, [5] [8]. "Bell-shaped" here means any distribution that is not L, U, or J-shaped and with a moderate or even an extreme amount of skewness. When the raw data in an analysis of variance follows a U-shaped distribution the analysis of variance is very poor. Clearly how well analysis of

variance performs, even for a bell shaped distribution, depends upon the amount of skew in the distribution and the amount of "peakedness" or kurtosis. As a result most robustness studies (either Monte Carlo or analytic) attempt to indicate how the significance level of the test compares with the "advertised" significance level, or that which appears to be dictated by the critical points from the F-distribution; the discrepancy between these two levels is then tabulated for various conditions on skewness and kurtosis. Many such studies have been conducted. In Ho [5] the author states "the distribution of the F-statistic in analysis of variance is practically unaffected by lack of symmetry but may be slightly affected if the underlying population is roughly symmetrical but very flat or very peaked. Since most non-normal distributions met in practice are non-normal because of skewness, departures from normality will likely have no appreciable effect on the validity of the F-test in analysis of variance." It remains then to investigate the χ^2 distribution and give a reasonable recommendation regarding what is the minimum value for degrees of freedom which would insure good performance of the analysis of variance. The skewness and kurtosis parameters that are ordinarily considered when comparing to normality are

$$\beta_1 = \mu_3^2 / \mu_2^3 \quad (\text{skewness coefficient})$$

$$\beta_2 = \mu_4 / \mu_2^2 \quad (\text{kurtosis coefficient})$$

where μ_j is the j^{th} central moment of the distribution. For the chi-square, $\mu_2 = 2r$, $\mu_3 = 8r$, and $\mu_4 = 48r + 12r^2$. As a result

$$\beta_1 = 8/r$$

$$\beta_2 = 3 + \frac{12}{r}$$

Clearly as r grows larger β_1 approaches zero, and β_2 approaches 3.0, both the Gaussian parameter values. For all practical purposes, if r were as large as 24, $\beta_1 = 0.33$ and $\beta_2 = 3.5$ and these values are themselves close enough to Gaussian to warrant safe use of analysis of variance. However, it is doubtful that it is necessary for r to be so large. Though it is difficult to get a "handle" on these two parameters, certainly any value of β_1 exceeded by 1.0 and β_2 in the vicinity of 4.0 should indicate "close enough" to symmetry to suggest safe use of analysis of variance. Thus if $r = 10$, $\beta_1 = 0.8$ and $\beta_2 = 4.2$ and since the distribution is bell shaped, this is well within the "safe" useage area indicated by Ho [5] and Norton [8] in their Monte Carlo work.

Conclusion

If one uses analysis of variance on sample variances, one can be assured of only minor errors if the sample variances are based on as many degrees of freedom as 10. If the sample variances are based on only 6-8 or fewer degrees of freedom, it might result in an error in the true significance level of the test and, as a result, a nonparametric approach should be considered as an alternative to ordinary analysis of variance.

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Table I Upper tail probabilities for the null distribution of Wilcoxon's rank sum W statistic: $m = 3(1)10, n = 1(1)m, m = 11(1)20, n = 1(1)4$

For given m and n , the table entry for the point x is $P_0\{W \geq x\}$. Under these conditions, if x is such that $P_0\{W \geq x\} = \alpha$, then $w(\alpha, m, n) = x$.

$n = 1$

x	$m = 3$	$m = 4$	$m = 5$	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$	$m = 11$
3	.500	.600							
4	.250	.400	.500	.571					
5		.200	.333	.429	.500	.556			
6			.167	.286	.375	.444	.500	.545	
7				.143	.250	.333	.400	.455	.500
8					.125	.222	.300	.364	.417
9						.111	.200	.273	.333
10							.100	.182	.250
11								.091	.167
12									.083

$n = 1$

x	$m = 12$	$m = 13$	$m = 14$	$m = 15$	$m = 16$	$m = 17$	$m = 18$	$m = 19$	$m = 20$
7	.538								
8	.462	.500	.533						
9	.385	.429	.467	.500	.529				
10	.308	.357	.400	.438	.471	.500	.526		
11	.231	.286	.333	.375	.412	.444	.474	.500	.524
12	.154	.214	.267	.312	.353	.389	.421	.450	.476
13	.077	.143	.200	.250	.294	.333	.368	.400	.429
14		.071	.133	.188	.235	.278	.316	.350	.381
15			.067	.125	.176	.222	.263	.300	.333
16				.062	.118	.167	.211	.250	.286
17					.059	.111	.158	.200	.238
18						.056	.105	.150	.190
19							.053	.100	.143
20								.050	.095
21									.048

Table I (continued)

$n = 2$

x	$m = 12$	$m = 13$	$m = 14$	$m = 15$	$m = 16$	$m = 17$	$m = 18$	$m = 19$	$m = 20$
33				.007	.026	.053	.084	.119	.156
34					.013	.035	.063	.095	.130
35					.007	.023	.047	.076	.108
36						.012	.032	.057	.087
37						.006	.021	.043	.069
38							.011	.029	.052
39							.005	.019	.039
40								.010	.026
41								.005	.017
42									.009
43									.004

$n = 3$

x	$m = 3$	$m = 4$	$m = 5$	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$	$m = 11$
11	.500								
12	.350	.571							
13	.200	.429							
14	.100	.314	.500						
15	.050	.200	.393	.548					
16		.114	.286	.452	.500				
17		.057	.196	.357	.500	.539			
18		.029	.125	.274	.417	.461			
19			.071	.190	.333	.388	.500		
20			.036	.131	.258	.388	.500	.521	
21			.018	.083	.192	.315	.432	.521	
22				.048	.133	.248	.364	.469	
23				.024	.092	.188	.300	.406	.500
24				.012	.058	.139	.241	.346	.442
25					.033	.097	.186	.287	.385
26					.017	.067	.141	.234	.330
27					.008	.042	.105	.185	.277
28						.024	.073	.143	.228
29						.012	.050	.108	.184
30						.006	.032	.080	.146
31							.018	.056	.113
32							.009	.038	.085
33							.005	.024	.063
34								.014	.044
35								.007	.030
36								.003	.019
37									.011
38									.005
39									.003

Table I (continued)

$n = 2$

x	$m = 3$	$m = 4$	$m = 5$	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$	$m = 11$
6	.600								
7	.400	.600							
8	.200	.400	.571						
9	.100	.267	.429	.571					
10		.133	.286	.429	.556				
11		.067	.190	.321	.444	.556			
12			.095	.214	.333	.444	.545		
13			.048	.143	.250	.356	.455	.545	
14				.071	.167	.267	.364	.455	.538
15				.036	.111	.200	.291	.379	.462
16					.056	.133	.218	.303	.385
17					.028	.089	.164	.242	.321
18						.044	.109	.182	.256
19						.022	.073	.136	.205
20							.036	.091	.154
21							.018	.061	.115
22								.030	.077
23								.015	.051
24									.026
25									.013

$n = 2$

x	$m = 12$	$m = 13$	$m = 14$	$m = 15$	$m = 16$	$m = 17$	$m = 18$	$m = 19$	$m = 20$
15	.538								
16	.462	.533							
17	.396	.467	.533						
18	.330	.400	.467	.529					
19	.275	.343	.408	.471	.529				
20	.220	.286	.350	.412	.471	.526			
21	.176	.238	.300	.360	.418	.474	.526		
22	.132	.190	.250	.309	.366	.421	.474	.524	
23	.099	.152	.208	.265	.320	.374	.426	.476	.524
24	.066	.114	.167	.221	.275	.327	.379	.429	.476
25	.044	.086	.133	.184	.235	.287	.337	.386	.433
26	.022	.057	.100	.147	.196	.246	.295	.343	.390
27	.011	.038	.075	.118	.163	.211	.258	.305	.351
28		.019	.050	.088	.131	.175	.221	.267	.312
29		.010	.033	.066	.105	.146	.189	.233	.277
30			.017	.044	.078	.117	.158	.200	.242
31			.008	.029	.059	.094	.132	.171	.212
32				.015	.039	.070	.105	.143	.182

Table I (continued)

$n = 3$

x	$m = 12$	$m = 13$	$m = 14$	$m = 15$	$m = 16$	$m = 17$	$m = 18$	$m = 19$	$m = 20$
24	.527								
25	.473								
26	.420	.500							
27	.367	.450	.524						
28	.316	.400	.476						
29	.268	.352	.429	.500					
30	.224	.305	.384	.486	.521				
31	.182	.261	.338	.412	.479				
32	.147	.220	.296	.369	.438	.500			
33	.116	.182	.254	.327	.396	.461	.519		
34	.090	.148	.216	.287	.356	.421	.481		
35	.068	.120	.181	.249	.317	.382	.444	.500	
36	.051	.095	.150	.217	.280	.345	.407	.464	.517
37	.035	.073	.122	.180	.244	.308	.370	.429	.483
38	.024	.055	.099	.151	.211	.273	.335	.394	.449
39	.015	.041	.078	.128	.180	.239	.300	.359	.415
40	.009	.029	.060	.102	.152	.208	.267	.325	.382
41	.004	.020	.046	.082	.127	.179	.235	.293	.349
42	.002	.012	.034	.065	.105	.153	.206	.262	.317
43		.007	.024	.050	.086	.129	.178	.232	.286
44		.004	.016	.038	.069	.108	.153	.204	.257
45		.002	.010	.028	.055	.089	.131	.178	.229
46			.006	.020	.042	.073	.111	.154	.202
47			.003	.013	.032	.059	.092	.132	.177
48			.001	.009	.024	.046	.077	.113	.155
49				.005	.017	.036	.062	.095	.134
50				.002	.011	.027	.050	.080	.115
51				.001	.007	.020	.040	.066	.098
52					.004	.014	.031	.054	.083
53					.002	.010	.023	.044	.069
54					.001	.006	.017	.034	.058
55						.004	.012	.027	.047
56						.002	.008	.020	.038
57						.001	.005	.015	.030
58							.003	.010	.023
59							.002	.007	.018
60							.001	.005	.013
61								.003	.009
62								.001	.006
63								.001	.004
64									.002
65									.001
66									.001

Table I (continued)

$n = 4$								
x	$m = 4$	$m = 5$	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$	$m = 11$
18	.557							
19	.443							
20	.343	.548						
21	.243	.452						
22	.171	.365	.543					
23	.100	.278	.457					
24	.057	.206	.381	.536				
25	.029	.143	.305	.464				
26	.014	.095	.238	.394	.533			
27		.056	.176	.324	.467			
28		.032	.129	.264	.404	.530		
29		.016	.086	.206	.341	.470		
30		.008	.057	.158	.285	.413	.527	
31			.033	.115	.230	.355	.473	
32			.019	.082	.184	.302	.420	.525
33			.010	.055	.141	.252	.367	.475
34			.005	.036	.107	.207	.318	.426
35				.021	.077	.165	.270	.377
36				.012	.055	.130	.227	.330
37				.006	.036	.099	.187	.286
38				.003	.024	.074	.152	.245
39					.014	.053	.120	.206
40					.008	.038	.094	.171
41					.004	.025	.071	.140
42					.002	.017	.053	.113
43						.010	.038	.08 ^o
44						.006	.027	.069
45						.003	.018	.052
46						.001	.012	.039
47							.007	.028
48							.004	.020
49							.002	.013
50							.001	.009
51								.005
52								.003
53								.001
54								.001

Table I- (continued)

$n = 4$

x	$m = 12$	$m = 13$	$m = 14$	$m = 15$	$m = 16$	$m = 17$	$m = 18$	$m = 19$	$m = 20$
34	.524								
35	.476								
36	.431	.522							
37	.385	.478							
38	.342	.435	.521						
39	.299	.392	.479						
40	.260	.352	.439	.519					
41	.223	.312	.399	.481					
42	.190	.274	.369	.453	.518				
43	.158	.239	.323	.405	.482				
44	.131	.206	.287	.368	.446	.517			
45	.106	.175	.253	.332	.410	.483			
46	.085	.148	.221	.298	.375	.449	.516		
47	.066	.123	.191	.265	.341	.415	.484		
48	.052	.101	.164	.235	.308	.381	.451	.516	
49	.039	.082	.139	.205	.277	.349	.419	.484	
50	.029	.065	.116	.179	.247	.318	.387	.453	.515
51	.021	.051	.096	.154	.219	.287	.356	.422	.485
52	.015	.039	.079	.131	.192	.258	.326	.392	.455
53	.010	.030	.063	.110	.168	.231	.297	.363	.426
54	.007	.022	.051	.092	.145	.205	.269	.334	.397
55	.004	.016	.040	.076	.124	.181	.242	.306	.368
56	.002	.011	.031	.062	.106	.158	.217	.279	.341
57	.001	.008	.023	.050	.089	.138	.193	.253	.314
58	.001	.005	.017	.040	.074	.119	.171	.228	.288
59		.003	.012	.031	.061	.101	.150	.205	.262
60		.002	.009	.024	.050	.086	.131	.183	.239
61		.001	.006	.018	.040	.072	.113	.162	.216
62		.000	.004	.014	.032	.060	.098	.143	.194
63			.002	.010	.025	.049	.083	.125	.174
64			.001	.007	.019	.040	.070	.109	.155
65			.001	.005	.015	.032	.059	.094	.137
66			.000	.003	.011	.026	.049	.081	.120
67				.002	.008	.020	.040	.069	.105
68				.001	.006	.016	.033	.058	.091
69				.001	.004	.012	.027	.049	.079
70				.000	.002	.009	.021	.041	.067
71					.001	.006	.017	.033	.057
72					.001	.005	.013	.027	.048
73					.000	.003	.010	.022	.041
74					.000	.002	.007	.018	.034
75						.001	.005	.014	.028
76						.001	.004	.011	.023
77						.000	.002	.008	.018

Table I (continued)

$n = 4$

x	$m = 12$	$m = 13$	$m = 14$	$m = 15$	$m = 16$	$m = 17$	$m = 18$	$m = 19$	$m = 20$
78						.000	.002	.006	.015
79							.001	.004	.011
80							.001	.003	.009
81							.000	.002	.007
82							.000	.001	.005
83								.001	.004
84								.000	.003
85								.000	.002
86								.000	.001
87									.001
88									.000
89									.000
90									.000

$n = 5$

x	$m = 5$	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$
28	.500					
29	.421					
30	.345	.535				
31	.274	.465				
32	.210	.396				
33	.155	.331	.500			
34	.111	.268	.438			
35	.075	.214	.378	.528		
36	.048	.165	.319	.472		
37	.028	.123	.265	.416		
38	.016	.089	.216	.362	.500	
39	.008	.063	.172	.311	.449	
40	.004	.041	.134	.262	.399	.523
41		.026	.101	.218	.350	.477
42		.015	.074	.177	.303	.430
43		.009	.053	.142	.259	.384
44		.004	.037	.111	.219	.339
45		.002	.024	.085	.182	.297
46			.015	.064	.149	.257
47			.009	.047	.120	.220
48			.005	.033	.095	.185
49			.003	.023	.073	.155
50			.001	.015	.056	.127
51				.009	.041	.103
52				.005	.030	.082

Table I (continued)

$n = 5$

x	$m = 5$	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$
53				.003	.021	.065
54				.002	.014	.050
55				.001	.009	.038
56					.006	.028
57					.003	.020
58					.002	.014
59					.001	.010
60					.000	.006
61						.004
62						.002
63						.001
64						.001
65						.000

$n = 6$

x	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$
39	.531				
40	.469				
41	.409				
42	.350	.527			
43	.294	.473			
44	.242	.418			
45	.197	.365	.525		
46	.155	.314	.475		
47	.120	.267	.426		
48	.090	.223	.377	.523	
49	.066	.183	.331	.477	
50	.047	.147	.286	.432	
51	.032	.117	.245	.388	.521
52	.021	.090	.207	.344	.479
53	.013	.069	.172	.303	.437
54	.008	.051	.141	.264	.396
55	.004	.037	.114	.228	.356
56	.002	.026	.091	.194	.318
57	.001	.017	.071	.164	.281
58		.011	.054	.136	.246
59		.007	.041	.112	.214
60		.004	.030	.091	.184
61		.002	.021	.072	.157
62		.001	.015	.057	.132
63		.001	.010	.044	.110

Table I (continued)

$n = 6$

x	$m = 6$	$m = 7$	$m = 8$	$m = 9$	$m = 10$
64			.006	.033	.090
65			.004	.025	.074
66			.002	.018	.059
67			.001	.013	.047
68			.001	.009	.036
69			.000	.006	.028
70				.004	.021
71				.002	.016
72				.001	.011
73				.001	.008
74				.000	.005
75				.000	.004
76					.002
77					.001
78					.001
79					.000
80					.000
81					.000

$n = 7$

x	$m = 7$	$m = 8$	$m = 9$	$m = 10$
53	.500			
54	.451			
55	.402			
56	.355	.522		
57	.310	.478		
58	.267	.433		
59	.228	.389		
60	.191	.347	.500	
61	.159	.306	.459	
62	.130	.268	.419	
63	.104	.232	.379	.519
64	.082	.198	.340	.481
65	.064	.168	.303	.443
66	.049	.140	.268	.406
67	.036	.116	.235	.370
68	.027	.095	.204	.335
69	.019	.076	.176	.300
70	.013	.060	.150	.268
71	.009	.047	.126	.237
72	.006	.036	.105	.209

Table I (continued)

<i>n</i> = 7					<i>n</i> = 8			
<i>x</i>	<i>m</i> = 7	<i>m</i> = 8	<i>m</i> = 9	<i>m</i> = 10	<i>x</i>	<i>m</i> = 8	<i>m</i> = 9	<i>m</i> = 10
73	.003	.027	.087	.182	80	.117	.240	.381
74	.002	.020	.071	.157	81	.097	.212	.348
75	.001	.014	.057	.138	82	.080	.185	.317
76	.001	.010	.043	.115	83	.065	.161	.286
77	.000	.007	.036	.097	84	.052	.138	.257
78		.005	.027	.081	85	.041	.118	.230
79		.003	.021	.067	86	.032	.100	.204
80		.002	.016	.054	87	.025	.084	.180
81		.001	.011	.044	88	.019	.069	.158
82		.001	.008	.035	89	.014	.057	.137
83		.000	.006	.028	90	.010	.046	.118
84		.000	.004	.022	91	.007	.037	.102
85			.003	.017	92	.005	.030	.086
86			.002	.012	93	.003	.023	.073
87			.001	.009	94	.002	.018	.061
88			.001	.007	95	.001	.014	.051
89			.000	.005	96	.001	.010	.042
90			.000	.003	97	.001	.008	.034
91			.000	.002	98	.000	.006	.027
92				.002	99	.000	.004	.022
93				.001	100	.000	.003	.017
94				.001	101		.002	.013
95				.000	102		.001	.010
96				.000	103		.001	.008
97				.000	104		.000	.006
98				.000	105		.000	.004
					106		.000	.003
					107		.000	.002
					108		.000	.002
					109			.001
					110			.001
					111			.000
					112			.000
					113			.000
					114			.000
					115			.000
					116			.000

<i>n</i> = 8			
<i>x</i>	<i>m</i> = 8	<i>m</i> = 9	<i>m</i> = 10
68	.520		
69	.480		
70	.439		
71	.399		
72	.360	.519	
73	.323	.481	
74	.287	.444	
75	.253	.407	
76	.221	.371	.517
77	.191	.336	.483
78	.164	.303	.448
79	.139	.271	.414

Table I (continued)

n = 9			n = 9			n = 10	
x	m = 9	m = 10	x	m = 9	m = 10	x	m = 10
86	.500		122	.000	.004	121	.124
87	.466		123	.000	.003	122	.109
88	.432		124	.000	.002	123	.095
89	.398		125	.000	.001	124	.083
90	.365	.516	126	.000	.001	125	.072
91	.333	.484	127		.001	126	.062
92	.302	.452	128		.000	127	.053
93	.273	.421	129		.000	128	.045
94	.245	.390	130		.000	129	.038
95	.218	.360	131		.000	130	.032
96	.193	.330	132		.000	131	.026
97	.170	.302	133		.000	132	.022
98	.149	.274	134		.000	133	.018
99	.129	.248	135		.000	134	.014
100	.111	.223				135	.012
101	.095	.200				136	.009
102	.081	.178				137	.007
103	.068	.158				138	.006
104	.057	.139				139	.004
105	.047	.121				140	.003
106	.039	.106				141	.003
107	.031	.091				142	.002
108	.025	.078				143	.001
109	.020	.067				144	.001
110	.016	.056				145	.001
111	.012	.047				146	.001
112	.009	.039				147	.000
113	.007	.033				148	.000
114	.005	.027				149	.000
115	.004	.022				150	.000
116	.003	.017				151	.000
117	.002	.014				152	.000
118	.001	.011				153	.000
119	.001	.009				154	.000
120	.001	.007				155	.000
121	.000	.005					

n = 10	
x	m = 10
105	.515
106	.485
107	.456
108	.427
109	.398
110	.370
111	.342
112	.315
113	.289
114	.264
115	.241
116	.218
117	.197
118	.176
119	.157
120	.140

Adapted from Table B of *A Nonparametric Introduction to Statistics*, by C. H. Kraft and C. van Eeden, Macmillan, New York, 1968, with the permission of the authors and the publisher. Copyright © 1968, by the Macmillan Company.

Table II Upper tail probabilities for the null distribution of the Ansari-Bradley \mathcal{W} statistic: $2 \leq m \leq n, (m+n) \leq 20$

For given m and n , the table entry for the point x is $P_0\{\mathcal{W} > x\}$. Under these conditions, if x is such that $P_0\{\mathcal{W} > x\} = \alpha$, then $\omega_1(\alpha, m, n) = x$. On the other hand, if x is such that $P_0\{\mathcal{W} > x\} = 1 - \alpha$, then $P_0\{\mathcal{W} < (x-1)\} = P_0\{\mathcal{W} < x\} = [1 - P_0\{\mathcal{W} > x\}] = [1 - (1 - \alpha)] = \alpha$, and $\omega_1(\alpha, m, n) = (x-1)$.

$m = 2$

x	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$
2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	.8333	.9000	.9333	.9524	.9643	.9722	.9778	.9818	.9848
4	.1667	.5000	.6667	.7619	.8214	.8611	.8889	.9091	.9242
5		.2000	.3333	.5238	.6429	.7222	.7778	.8182	.8485
6			.0667	.2381	.3571	.5000	.6000	.6727	.7273
7				.0952	.1786	.3056	.4000	.5091	.5909
8					.0357	.1389	.2222	.3273	.4091
9						.0556	.1111	.2000	.2727
10							.0222	.0909	.1515
11								.0364	.0758
12									.0152

$n = 2$

x	$n = 11$	$n = 12$	$n = 13$	$n = 14$	$n = 15$	$n = 16$	$n = 17$	$n = 18$
2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	.9872	.9890	.9905	.9917	.9926	.9935	.9942	.9947
4	.9359	.9451	.9524	.9583	.9632	.9673	.9708	.9737
5	.8718	.8901	.9048	.9167	.9265	.9346	.9415	.9474
6	.7692	.8022	.8286	.8500	.8676	.8824	.8947	.9053
7	.6538	.7033	.7429	.7750	.8015	.8235	.8421	.8579
8	.5000	.5714	.6286	.6750	.7132	.7451	.7719	.7947
9	.3590	.4286	.5048	.5667	.6176	.6601	.6959	.7263
10	.2308	.2967	.3714	.4333	.5000	.5556	.6023	.6421
11	.1410	.1978	.2667	.3250	.3897	.4444	.5029	.5526
12	.0641	.1099	.1714	.2250	.2868	.3399	.3977	.4474
13	.0256	.0549	.1048	.1500	.2059	.2549	.3099	.3579
14		.0110	.0476	.0833	.1324	.1765	.2281	.2737
15			.0190	.0417	.0809	.1176	.1637	.2053
16				.0083	.0368	.0654	.1053	.1421
17					.0147	.0327	.0643	.0947
18						.0065	.0292	.0526
19							.0117	.0263
20								.0053

Table II (continued)

$m = 3$

x	$n = 3$	$n = 4$	$n = 5$	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$
4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
5	.9000	.9429	.9643	.9762	.9833	.9879	.9909	.9930	.9945
6	.7000	.8286	.8929	.9286	.9500	.9636	.9727	.9790	.9835
7	.3000	.5714	.7143	.8095	.8667	.9030	.9273	.9441	.9560
8	.1000	.3429	.5000	.6548	.7500	.8182	.8636	.8951	.9176
9		.1429	.2857	.4643	.5833	.6909	.7636	.8182	.8571
10		.0286	.1071	.2857	.4167	.5455	.6364	.7168	.7747
11			.0357	.1429	.2500	.3939	.5000	.5979	.6703
12				.0595	.1333	.2606	.3636	.4755	.5604
13				.0119	.0500	.1455	.2364	.3497	.4396
14					.0167	.0727	.1364	.2413	.3297
15						.0303	.0727	.1503	.2253
16						.0061	.0273	.0839	.1429
17							.0091	.0420	.0824
18								.0175	.0440
19								.0035	.0165
20									.0055

$m = 3$

x	$n = 12$	$n = 13$	$n = 14$	$n = 15$	$n = 16$	$n = 17$
4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
5	.9956	.9964	.9971	.9975	.9979	.9982
6	.9868	.9893	.9912	.9926	.9938	.9947
7	.9648	.9714	.9765	.9804	.9835	.9860
8	.9341	.9464	.9559	.9632	.9690	.9737
9	.8857	.9071	.9235	.9363	.9463	.9544
10	.8198	.8536	.8794	.8995	.9154	.9281
11	.7341	.7821	.8206	.8505	.8741	.8930
12	.6374	.6964	.7485	.7892	.8225	.8491
13	.5297	.6000	.6632	.7132	.7575	.7930
14	.4242	.5000	.5735	.6324	.6852	.7281
15	.3209	.4000	.4794	.5441	.6058	.6561
16	.2286	.3036	.3868	.4559	.5232	.5789
17	.1516	.2179	.2985	.3676	.4396	.5000
18	.0945	.1464	.2206	.2868	.3591	.4211
19	.0527	.0929	.1529	.2108	.2817	.3439
20	.0264	.0536	.1015	.1495	.2136	.2719
21	.0110	.0286	.0632	.1005	.1548	.2070
22	.0022	.0107	.0353	.0637	.1073	.1509
23		.0036	.0176	.0368	.0712	.1070
24			.0074	.0196	.0444	.0719

Table II (continued)

$m = 3$

x	$n = 12$	$n = 13$	$n = 14$	$n = 15$	$n = 16$	$n = 17$
25			.0015	.0074	.0248	.0456
26				.0025	.0124	.0263
27					.0052	.0140
28					.0010	.0053
29						.0018

$m = 4$

x	$n = 4$	$n = 5$	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$
6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
7	.9857	.9921	.9952	.9970	.9980	.9986	.9990	.9993	.9995
8	.9286	.9603	.9762	.9848	.9899	.9930	.9950	.9963	.9973
9	.8000	.8889	.9333	.9576	.9717	.9804	.9860	.9897	.9923
10	.6286	.7778	.8571	.9091	.9394	.9580	.9700	.9780	.9835
11	.3714	.6032	.7333	.8242	.8788	.9161	.9401	.9560	.9670
12	.2000	.4286	.5810	.7152	.7980	.8573	.8961	.9238	.9429
13	.0714	.2619	.4190	.5818	.6889	.7762	.8342	.8769	.9066
14	.0143	.1349	.2567	.4424	.5677	.6783	.7542	.8154	.8582
15		.0476	.1429	.3030	.4323	.5650	.6593	.7385	.7951
16		.0159	.0667	.1939	.3111	.4503	.5554	.6520	.7225
17			.0238	.1061	.2020	.3357	.4446	.5546	.6374
18			.0048	.0515	.1212	.2378	.3407	.4564	.5473
19				.0182	.0606	.1538	.2458	.3590	.4527
20				.0061	.0283	.0923	.1658	.2711	.3626
21					.0101	.0490	.1039	.1934	.2775
22					.0020	.0238	.0599	.1319	.2049
23						.0084	.0300	.0821	.1418
24						.0028	.0140	.0484	.0934
25							.0050	.0256	.0571
26							.0010	.0125	.0330
27								.0044	.0165
28								.0015	.0077
29									.0027
30									.0005

Table II (continued)

$m = 4$

x	$n = 13$	$n = 14$	$n = 15$	$n = 16$
6	1.0000	1.0000	1.0000	1.0000
7	.9996	.9997	.9997	.9998
8	.9979	.9984	.9987	.9990
9	.9941	.9954	.9964	.9971
10	.9874	.9902	.9923	.9938
11	.9748	.9804	.9845	.9876
12	.9563	.9660	.9732	.9785
13	.9286	.9444	.9561	.9649
14	.8908	.9144	.9324	.9459
15	.8408	.8742	.9002	.9197
16	.7811	.8245	.8599	.8867
17	.7101	.7647	.8101	.8448
18	.6319	.6967	.7528	.7961
19	.5471	.6209	.6873	.7391
20	.4613	.5412	.6166	.6764
21	.3761	.4588	.5413	.6078
22	.2979	.3791	.4654	.5368
23	.2261	.3033	.3896	.4632
24	.1655	.2353	.3189	.3922
25	.1151	.1755	.2531	.3236
26	.0765	.1258	.1953	.2609
27	.0471	.0856	.1450	.2039
28	.0277	.0556	.1042	.1552
29	.0147	.0340	.0712	.1133
30	.0071	.0196	.0470	.0803
31	.0025	.0098	.0289	.0541
32	.0008	.0046	.0170	.0351
33		.0016	.0090	.0215
34		.0003	.0044	.0124
35			.0015	.0062
36			.0005	.0029
37				.0010
38				.0002

$m = 5$

x	$n = 5$	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$
9	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
10	.9921	.9957	.9975	.9984	.9990	.9993	.9995
11	.9762	.9870	.9924	.9953	.9970	.9980	.9986
12	.9286	.9610	.9773	.9860	.9910	.9940	.9959
13	.8492	.9156	.9495	.9689	.9800	.9867	.9908

Table II (continued)

$m = 5$

x	$n = 5$	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$
14	.7302	.8420	.9015	.9386	.9600	.9734	.9817
15	.5873	.7446	.8333	.8936	.9291	.9524	.9670
16	.4127	.6147	.7374	.8275	.8821	.9197	.9437
17	.2698	.4805	.6237	.7451	.8212	.8761	.9116
18	.1508	.3463	.5000	.6457	.7423	.8182	.8681
19	.0714	.2294	.3763	.5385	.6523	.7483	.8132
20	.0238	.1342	.2626	.4266	.5514	.6663	.7468
21	.0079	.0693	.1667	.3209	.4486	.5771	.6708
22		.0303	.0985	.2269	.3477	.4832	.5870
23		.0108	.0505	.1507	.2577	.3916	.5000
24		.0022	.0227	.0917	.1788	.3044	.4130
25			.0076	.0513	.1179	.2268	.3292
26			.0025	.0249	.0709	.1608	.2532
27				.0109	.0400	.1086	.1868
28				.0039	.0200	.0686	.1319
29				.0008	.0090	.0406	.0884
30					.0030	.0220	.0563
31					.0010	.0107	.0330
32						.0047	.0183
33						.0017	.0092
34						.0003	.0041
35							.0014
36							.0005

$m = 5$

x	$n = 12$	$n = 13$	$n = 14$	$n = 15$
9	1.0000	1.0000	1.0000	1.0000
10	.9997	.9998	.9998	.9999
11	.9990	.9993	.9995	.9996
12	.9971	.9979	.9985	.9988
13	.9935	.9953	.9966	.9974
14	.9871	.9907	.9931	.9948
15	.9767	.9832	.9876	.9907
16	.9601	.9711	.9787	.9840
17	.9368	.9538	.9659	.9743
18	.9047	.9295	.9476	.9604
19	.8633	.8978	.9235	.9417
20	.8116	.8569	.8920	.9171
21	.7508	.8079	.8533	.8861
22	.6810	.7498	.8067	.8483
23	.6054	.6846	.7530	.8038

Table II (continued)

$m = 5$

x	$n = 12$	$n = 13$	$n = 14$	$n = 15$
24	.5254	.6130	.6923	.7523
25	.4449	.5383	.6267	.6950
26	.3662	.4617	.5572	.6329
27	.2928	.3870	.4864	.5673
28	.2262	.3154	.4157	.5000
29	.1690	.2502	.3478	.4327
30	.1214	.1921	.2840	.3671
31	.0835	.1431	.2262	.3050
32	.0546	.1022	.1751	.2477
33	.0339	.0705	.1318	.1962
34	.0197	.0462	.0960	.1517
35	.0107	.0289	.0675	.1139
36	.0052	.0168	.0455	.0829
37	.0023	.0093	.0294	.0583
38	.0008	.0047	.0181	.0396
39	.0002	.0021	.0105	.0257
40		.0007	.0057	.0160
41		.0002	.0028	.0093
42			.0012	.0052
43			.0004	.0026
44			.0001	.0012
45				.0004
46				.0001

$m = 6$

x	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$	$n = 13$	$n = 14$
12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
13	.9989	.9994	.9997	.9998	.9999	.9999	.9999	1.0000	1.0000
14	.9946	.9971	.9983	.9990	.9994	.9996	.9997	.9998	.9999
15	.9848	.9918	.9953	.9972	.9983	.9989	.9992	.9995	.9996
16	.9632	.9802	.9887	.9932	.9958	.9973	.9982	.9987	.9991
17	.9264	.9592	.9760	.9856	.9910	.9942	.9961	.9973	.9981
18	.8658	.9242	.9547	.9724	.9825	.9887	.9925	.9948	.9964
19	.7846	.8735	.9217	.9518	.9692	.9799	.9865	.9907	.9935
20	.6807	.8048	.8751	.9215	.9487	.9663	.9772	.9843	.9890
21	.5649	.7203	.8139	.8803	.9202	.9469	.9636	.9749	.9823
22	.4351	.6189	.7366	.8260	.8812	.9199	.9445	.9613	.9725
23	.3193	.5122	.6474	.7600	.8322	.8849	.9190	.9431	.9591
24	.2154	.4038	.5501	.6829	.7717	.8407	.8860	.9191	.9413
25	.1342	.3030	.4499	.5984	.7025	.7877	.8451	.8887	.9184
26	.0736	.2133	.3526	.5085	.6246	.7259	.7962	.8514	.8896

Table II (continued)

$m = 6$

x	$n = 6$	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$	$n = 13$	$n = 14$
27	.0368	.1410	.2634	.4190	.5425	.6574	.7398	.8074	.8549
28	.0152	.0851	.1861	.3323	.4575	.5831	.6765	.7564	.8138
29	.0054	.0484	.1249	.2543	.3754	.5065	.6082	.6996	.7668
30	.0011	.0239	.0783	.1860	.2975	.4292	.5364	.6376	.7139
31		.0105	.0453	.1303	.2283	.3549	.4636	.5723	.6566
32		.0035	.0240	.0859	.1678	.2851	.3918	.5049	.5954
33		.0012	.0113	.0539	.1188	.2226	.3235	.4376	.5322
34			.0047	.0312	.0798	.1678	.2602	.3716	.4678
35			.0017	.0170	.0513	.1226	.2038	.3094	.4046
36			.0003	.0082	.0308	.0859	.1549	.2518	.3434
37				.0036	.0175	.0579	.1140	.2002	.2861
38				.0012	.0090	.0370	.0810	.1550	.2332
39				.0004	.0042	.0226	.0555	.1170	.1862
40					.0017	.0128	.0364	.0855	.1451
41					.0006	.0069	.0228	.0608	.1104
42					.0001	.0033	.0135	.0415	.0816
43						.0015	.0075	.0274	.0587
44						.0005	.0039	.0172	.0409
45						.0002	.0018	.0104	.0275
46							.0008	.0058	.0177
47							.0003	.0031	.0110
48							.0001	.0015	.0065
49								.0007	.0036
50								.0002	.0019
51								.0001	.0009
52									.0004
53									.0001
54									.0000

$m = 7$

x	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$	$n = 13$
16	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
17	.9994	.9997	.9998	.9999	1.0000	1.0000	1.0000
18	.9983	.9991	.9995	.9997	.9998	.9999	.9999
19	.9948	.9972	.9984	.9991	.9994	.9996	.9998
20	.9878	.9935	.9963	.9978	.9987	.9992	.9995
21	.9744	.9862	.9921	.9954	.9972	.9982	.9988
22	.9534	.9744	.9851	.9912	.9946	.9966	.9978
23	.9196	.9549	.9734	.9841	.9901	.9937	.9959
24	.8730	.9270	.9559	.9734	.9833	.9893	.9930
25	.8106	.8878	.9306	.9574	.9729	.9826	.9885

Table II (continued)

$m = 7$

x	$n = 7$	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$	$n = 13$
26	.7348	.8375	.8965	.9354	.9583	.9730	.9820
27	.6463	.7748	.8523	.9059	.9381	.9595	.9727
28	.5507	.7021	.7981	.8685	.9118	.9415	.9602
29	.4493	.6194	.7336	.8221	.8782	.9181	.9435
30	.3537	.5324	.6608	.7676	.8374	.8889	.9223
31	.2652	.4435	.5820	.7052	.7887	.8532	.8958
32	.1894	.3577	.5000	.6368	.7333	.8111	.8637
33	.1270	.2777	.4180	.5637	.6714	.7626	.8258
34	.0804	.2075	.3392	.4888	.6050	.7085	.7822
35	.0466	.1478	.2664	.4139	.5353	.6494	.7332
36	.0256	.1005	.2019	.3421	.4647	.5869	.6795
37	.0122	.0648	.1477	.2753	.3950	.5220	.6219
38	.0052	.0393	.1035	.2154	.3286	.4568	.5616
39	.0017	.0221	.0694	.1633	.2667	.3925	.5000
40	.0006	.0115	.0441	.1199	.2113	.3311	.4384
41		.0053	.0266	.0847	.1626	.2735	.3781
42		.0022	.0149	.0576	.1218	.2213	.3205
43		.0008	.0079	.0375	.0882	.1749	.2668
44		.0002	.0037	.0233	.0619	.1350	.2178
45			.0016	.0136	.0417	.1014	.1742
46			.0005	.0075	.0271	.0742	.1363
47			.0002	.0038	.0167	.0526	.1042
48				.0017	.0099	.0361	.0777
49				.0007	.0054	.0239	.0565
50				.0003	.0028	.0152	.0398
51				.0001	.0013	.0092	.0273
52					.0006	.0053	.0180
53					.0002	.0029	.0115
54					.0001	.0015	.0070
55						.0007	.0041
56						.0003	.0022
57						.0001	.0012
58						.0000	.0005
59							.0002
60							.0001
61							.0000

Table II (continued)

$m = 8$

x	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$
20	1.0000	1.0000	1.0000	1.0000	1.0000
21	.9999	1.0000	1.0000	1.0000	1.0000
22	.9996	.9998	.9999	.9999	1.0000
23	.9989	.9994	.9997	.9998	.9999
24	.9974	.9986	.9992	.9996	.9997
25	.9941	.9969	.9983	.9990	.9994
26	.9885	.9938	.9965	.9980	.9988
27	.9789	.9886	.9935	.9962	.9977
28	.9643	.9804	.9887	.9934	.9960
29	.9428	.9680	.9813	.9889	.9932
30	.9133	.9504	.9704	.9823	.9890
31	.8737	.9262	.9551	.9728	.9830
32	.8246	.8947	.9344	.9598	.9745
33	.7650	.8549	.9075	.9423	.9629
34	.6970	.8069	.8738	.9199	.9477
35	.6212	.7508	.8328	.8918	.9281
36	.5413	.6877	.7847	.8578	.9038
37	.4587	.6184	.7296	.8174	.8742
38	.3788	.5457	.6686	.7710	.8392
39	.3030	.4714	.6031	.7189	.7986
40	.2350	.3983	.5347	.6621	.7528
41	.1754	.3281	.4653	.6015	.7022
42	.1263	.2636	.3969	.5386	.6476
43	.0867	.2055	.3314	.4746	.5898
44	.0572	.1557	.2704	.4113	.5302
45	.0357	.1139	.2153	.3500	.4698
46	.0211	.0807	.1672	.2925	.4102
47	.0115	.0548	.1262	.2394	.3524
48	.0059	.0358	.0925	.1919	.2978
49	.0026	.0221	.0656	.1503	.2472
50	.0011	.0131	.0449	.1150	.2014
51	.0004	.0072	.0296	.0856	.1608
52	.0001	.0037	.0187	.0621	.1258
53		.0017	.0113	.0437	.0962
54		.0007	.0065	.0298	.0719
55		.0002	.0035	.0196	.0523
56		.0001	.0017	.0124	.0371
57			.0008	.0075	.0255
58			.0003	.0043	.0170
59			.0001	.0023	.0110
60			.0000	.0012	.0068
61				.0006	.0040
62				.0002	.0023
63				.0001	.0012

Table II (continued)

$m = 8$

x	$n = 8$	$n = 9$	$n = 10$	$n = 11$	$n = 12$
64				.0000	.0006
65					.0003
66					.0001
67					.0000
68					.0000

$m = 9$

x	$n = 9$	$n = 10$	$n = 11$
25	1.0000	1.0000	1.0000
26	1.0000	1.0000	1.0000
27	.9999	.9999	1.0000
28	.9996	.9998	.9999
29	.9991	.9995	.9997
30	.9981	.9990	.9995
31	.9963	.9980	.9989
32	.9932	.9964	.9980
33	.9882	.9937	.9964
34	.9805	.9894	.9940
35	.9695	.9831	.9903
36	.9540	.9741	.9849
37	.9332	.9618	.9773
38	.9062	.9453	.9669
39	.8724	.9240	.9532
40	.8313	.8972	.9355
41	.7833	.8646	.9133
42	.7283	.8259	.8862
43	.6677	.7813	.8538
44	.6025	.7310	.8160
45	.5346	.6759	.7731
46	.4654	.6166	.7251
47	.3975	.5548	.6729
48	.3323	.4916	.6173
49	.2717	.4287	.5593

$m = 9$

x	$n = 9$	$n = 10$	$n = 11$
50	.2167	.3673	.5000
51	.1687	.3092	.4407
52	.1276	.2552	.3827
53	.0938	.2064	.3271
54	.0668	.1632	.2749
55	.0460	.1262	.2269
56	.0305	.0952	.1840
57	.0195	.0700	.1462
58	.0118	.0500	.1138
59	.0068	.0347	.0867
60	.0037	.0232	.0645
61	.0019	.0150	.0468
62	.0009	.0093	.0331
63	.0004	.0056	.0227
64	.0001	.0031	.0151
65	.0000	.0017	.0097
66		.0008	.0060
67		.0004	.0036
68		.0002	.0020
69		.0001	.0011
70		.0000	.0005
71			.0003
72			.0001
73			.0000
74			.0000

Table II (continued)

$m = 10$		$m = 10$		$m = 10$	
x	$n = 10$	x	$n = 10$	x	$n = 10$
30	1.0000	47	.8993	64	.1007
31	1.0000	48	.8694	65	.0761
32	1.0000	49	.8344	66	.0560
33	.9999	50	.7940	67	.0403
34	.9998	51	.7486	68	.0282
35	.9996	52	.6986	69	.0192
36	.9992	53	.6449	70	.0126
37	.9984	54	.5881	71	.0080
38	.9971	55	.5296	72	.0049
39	.9951	56	.4704	73	.0029
40	.9920	57	.4119	74	.0016
41	.9874	58	.3551	75	.0008
42	.9808	59	.3014	76	.0004
43	.9718	60	.2514	77	.0002
44	.9597	61	.2060	78	.0001
45	.9440	62	.1656	79	.0000
46	.9239	63	.1306	80	.0000

Computed by G. A. Mack on the Ohio State University IBM 370/165.

Table III

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

The upper 10% of the exact probability distribution of the Kruskal-Wallis test statistic is given for the following cases involving k samples.

$$k = 3, n_i \leq 6$$

$$n_1 = n_2 = n_3 = 7$$

$$n_1 = n_2 = n_3 = 8$$

$$k = 4, n_i \leq 4$$

$$k = 5, n_i \leq 3$$

h	P(H>h)	h	P(H>h)	h	P(H>h)	h	P(H>h)
2	2 2	4	3 1	4	3 3	4	4 3
3.714	.20000	3.889	.12857	6.564	.01714	4.598	.09333
4.571	.06667	4.056	.09286	6.664	.01381	4.712	.09022
		4.097	.08571	6.709	.01286	4.750	.08745
		4.208	.07857	6.745	.01000	4.894	.08364
3	2 1	4.764	.07143	7.000	.00619	5.053	.07810
4.286	.10000	5.000	.05714	7.318	.00429	5.144	.07290
		5.208	.05000	7.436	.00238	5.182	.06840
		5.389	.03571	8.018	.00143	5.212	.06563
		5.833	.02143			5.295	.06320
4.464	.10476			4	4 1	5.303	.06078
4.500	.06667	4	3 2	4.067	.10159	5.326	.05801
4.714	.04762	4.444	.10159	4.167	.08264	5.386	.05385
5.357	.02857	4.511	.09841	4.267	.06984	5.500	.05177
		4.544	.08571	4.800	.06667	5.576	.05074
		4.611	.08264	4.867	.05397	5.598	.04866
3	3 1	4.711	.07937	4.967	.04762	5.667	.04693
4.571	.10000	4.811	.07619	5.100	.04127	5.803	.04485
5.143	.04286	4.878	.07302	5.667	.03492	5.932	.04312
		4.900	.07143	6.000	.02857	5.962	.04139
		4.978	.05873	6.167	.02222	6.000	.04000
		5.078	.05714	6.667	.00952	6.045	.03861
3	3 2	5.144	.05397			6.053	.03481
4.556	.10000	5.378	.05238	4	4 2	6.144	.03203
4.694	.09286	5.400	.05079	4.445	.10286	6.167	.03065
5.000	.07500	5.444	.04603	4.555	.09778	6.182	.02961
5.139	.06071	5.500	.03968	4.582	.09397	6.348	.02719
5.361	.03214	5.611	.03175	4.591	.08000	6.386	.02615
5.556	.02500	6.000	.02381	4.773	.07492	6.394	.02476
6.250	.01071	6.111	.02063	4.855	.07111	6.409	.02338
		6.144	.01429	4.971	.06476	6.417	.02165
		6.300	.01111	4.991	.06476	6.545	.02061
		6.444	.00794	5.127	.05714	6.659	.02009
		7.000	.00476	5.236	.05206	6.712	.01905
				5.355	.04571	6.727	.01835
				5.509	.04444	6.962	.01662
		4	3 3	5.536	.04190	7.000	.01593
		4.700	.10095	5.645	.03937	7.053	.01420
		4.709	.09238	5.727	.03429	7.076	.01143
		4.818	.08476	5.945	.02794	7.136	.01074
		4.845	.08095	6.082	.02530	7.144	.00970
		5.000	.07429	6.327	.02413	7.212	.00909
		5.064	.07048	6.409	.02159	7.477	.00623
		5.109	.06762	6.545	.02032	7.598	.00416
		5.255	.06381	6.600	.01651	7.636	.00381
		5.436	.06190	6.600	.01651	7.682	.00312
		5.500	.05619	6.677	.01597	7.848	.00294
		5.573	.05333	6.873	.01079	8.227	.00156
		5.727	.05048	7.036	.00571	8.326	.00121
		5.791	.04571	7.282	.00344	8.909	.00052
		5.936	.03619	7.855	.00190		
		5.982	.03429			4	4 4
		6.018	.02667			4.500	.10424
		6.155	.02476	4	4 3	4.654	.09662
		6.300	.02286	4.477	.10216	4.769	.09351
				4.545	.09905	4.985	.08589
				4.576	.09714		

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h			h			h			h		
P(H ₂ ≥ h)			P(H ₂ ≥ h)			P(H ₂ ≥ h)			P(H ₂ ≥ h)		
4	4	4	5	3	1	5	3	3	5	4	1
4.962	.08000		4.284	.08333		4.800	.08658		5.558	.03492	
5.115	.07411		4.338	.07937		4.848	.08528		5.596	.03333	
5.346	.06268		4.551	.07540		4.861	.08182		5.733	.02698	
5.538	.05749		4.711	.05556		4.909	.07922		5.776	.02540	
5.654	.05455		4.871	.05159		5.042	.07749		5.858	.02381	
5.692	.04866		4.960	.04762		5.079	.06926		5.864	.02222	
5.808	.04416		5.404	.04365		5.103	.06710		5.967	.02063	
6.000	.04035		5.440	.03571		5.212	.06494		6.431	.01905	
6.038	.03654		5.760	.02778		5.261	.06234		6.578	.01587	
6.269	.03273		6.044	.01984		5.345	.05758		6.818	.01270	
6.500	.02996		6.400	.01190		5.442	.05498		6.840	.01111	
6.577	.02632					5.503	.05325		6.955	.00794	
6.615	.02424		5	3	2	5.515	.05065		7.364	.00476	
6.731	.02147					5.648	.04892				
6.962	.01939		4.495	.10079		5.770	.04675		5	4	2
7.038	.01766		4.651	.09127		5.867	.04156				
7.269	.01593		4.695	.08889		6.012	.03983		4.518	.10072	
7.385	.01455		4.724	.08730		6.061	.03290		4.541	.09841	
7.423	.01316		4.727	.08492		6.109	.03203		4.614	.09004	
7.538	.01074		4.815	.07143		6.194	.02684		4.664	.08831	
7.654	.00762		4.869	.06667		6.303	.02554		4.768	.07937	
7.731	.00658		4.913	.06349		6.315	.02121		4.791	.07792	
8.000	.00485		4.942	.06190		6.376	.02035		4.800	.07561	
8.115	.00312		5.076	.05952		6.533	.01905		4.818	.07417	
8.346	.00242		5.087	.05317		6.594	.01861		4.841	.07244	
8.654	.00139		5.105	.05159		6.715	.01385		4.868	.07100	
8.769	.00121		5.251	.04921		6.776	.01299		4.950	.06263	
9.269	.00052		5.349	.04603		6.861	.01212		5.073	.06147	
9.846	.00017		5.513	.04444		6.992	.01126		5.155	.05916	
			5.524	.04286		7.079	.00866		5.164	.05310	
			5.542	.04127		7.333	.00779		5.255	.05195	
			5.727	.03651		7.467	.00758		5.268	.05051	
			5.742	.03413		7.503	.00584		5.273	.04877	
			5.755	.03333		7.515	.00541		5.300	.04762	
			5.804	.03254		7.636	.00411		5.314	.04618	
			5.949	.02619		7.879	.00291		5.414	.04502	
			6.004	.02460		8.048	.00195		5.518	.04271	
			6.033	.02381		8.242	.00108		5.523	.04156	
			6.091	.02063		8.727	.00065		5.564	.03810	
			6.124	.01984					5.641	.03694	
			6.295	.01667		5	4	1	5.664	.03608	
			6.385	.01587					5.755	.03492	
			6.415	.01508		3.960	.10159		5.823	.03377	
			6.818	.01190		3.987	.09841		5.891	.03203	
			6.822	.01032		4.205	.09524		5.955	.03030	
			6.909	.00873		4.222	.08730		5.973	.02915	
			6.949	.00556		4.287	.07143		6.005	.02626	
			7.182	.00397		4.549	.06667		6.041	.02540	
			7.636	.00238		4.636	.06349		6.068	.02482	
						4.724	.06032		6.118	.02395	
			5	3	3	4.833	.05873		6.141	.02280	
						4.860	.05556		6.223	.02193	
			4.412	.10409		4.985	.04444		6.368	.02136	
			4.532	.09697		5.078	.04127		6.391	.02078	
			4.679	.09351		5.160	.03810		6.473	.02020	
			4.776	.09004		5.515	.03651		6.505	.01962	

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
5	4	2	5	4	3	5	4	3	5	4	4
6.541	.01732		5.614	.05115		7.563	.00722		5.476	.05741	
6.550	.01674		5.631	.05026		7.641	.00707		5.486	.05617	
6.564	.01616		5.656	.04863		7.703	.00635		5.489	.05550	
6.655	.01558		5.660	.04791		7.753	.00613		5.519	.05426	
6.723	.01501		5.677	.04719		7.810	.00599		5.568	.05195	
6.905	.01385		5.718	.04574		7.876	.00584		5.571	.05084	
6.914	.01328		5.722	.04502		7.887	.00570		5.618	.05031	
7.000	.01299		5.753	.04430		7.906	.00512		5.657	.04906	
7.018	.01212		5.779	.04300		7.927	.00498		5.637	.04773	
7.064	.01183		5.804	.04113		8.029	.00455		5.756	.04658	
7.118	.01010		5.814	.04033		8.060	.00440		5.782	.04555	
7.205	.00895		5.862	.03961		8.077	.00426		5.815	.04458	
7.255	.00866		5.876	.03889		8.118	.00390		5.819	.04342	
7.291	.00750		5.964	.03831		8.122	.00375		5.914	.04245	
7.450	.00722		6.026	.03773		8.215	.00317		6.003	.04151	
7.500	.00693		6.029	.03716		8.256	.00274		6.013	.04063	
7.568	.00606		6.060	.03658		8.429	.00216		6.030	.03965	
7.573	.00491		6.087	.03550		8.446	.00209		6.096	.03867	
7.773	.00375		6.164	.03492		8.481	.00180		6.119	.03783	
7.814	.00260		6.173	.03369		8.503	.00137		6.132	.03694	
8.018	.00202		6.231	.03312		8.573	.00130		6.201	.03601	
8.114	.00144		6.265	.03167		8.626	.00123		6.214	.03357	
8.591	.00087		6.272	.03009		8.795	.00094		6.227	.03263	
			6.337	.02951		9.035	.00065		6.267	.03183	
			6.368	.02900		9.118	.00051		6.310	.03108	
			6.369	.02864		9.199	.00036		6.343	.02957	
			6.395	.02597		9.692	.00022		6.382	.02877	
			6.410	.02496					6.399	.02802	
			6.491	.02453					6.462	.02731	
			6.522	.02367					6.544	.02686	
			6.542	.02330		5	4	4	6.547	.02620	
4.523	.10332		6.579	.02078		4.619	.10003		6.597	.02557	
4.549	.09892		6.635	.02035		4.668	.09817		6.673	.02429	
4.564	.09747		6.676	.01991		4.685	.09608		6.676	.02353	
4.645	.09466		6.676	.01991		4.701	.09417		6.804	.02291	
4.676	.09329		6.703	.01912		4.711	.09244		6.860	.02229	
4.754	.09076		6.779	.01869		4.727	.09053		6.870	.02180	
4.788	.08939		6.785	.01789		4.747	.08880		6.887	.02122	
4.810	.08831		6.799	.01631		4.760	.08782		6.890	.02073	
4.829	.08326		6.829	.01595		4.813	.08587		6.943	.02020	
4.856	.08225		6.891	.01537		4.830	.08392		6.953	.01958	
4.881	.08102		7.004	.01508		4.833	.08232		6.976	.01851	
4.891	.07763		7.010	.01472		4.896	.08076		7.058	.01794	
4.938	.07540		7.096	.01443		4.975	.07739		7.075	.01749	
4.953	.07424		7.106	.01356		5.014	.07575		7.101	.01661	
4.983	.07330		7.188	.01299		5.024	.07428		7.124	.01612	
5.041	.07229		7.195	.01241		5.027	.07264		7.190	.01567	
5.045	.07121		7.256	.01212		5.090	.07108		7.203	.01518	
5.106	.07013		7.260	.01183		5.173	.06935		7.233	.01474	
5.137	.06825		7.272	.01162		5.196	.06793		7.240	.01439	
5.158	.06732		7.291	.01133		5.225	.06633		7.256	.01390	
5.179	.06530		7.318	.01111		5.344	.06496		7.256	.01390	
5.291	.06320		7.395	.01089		5.360	.06349		7.418	.01354	
5.308	.06241		7.445	.00974		5.370	.06225		7.467	.01330	
5.342	.06140		7.465	.00952		5.387	.06101		7.470	.01301	
5.349	.06061		7.477	.00931		5.410	.05985		7.497	.01265	
5.353	.05880		7.523	.00743		5.440	.05861		7.503	.01234	
5.414	.05808										
5.426	.05657										
5.549	.05390										
5.568	.05245										

h			P(H ≥ h)			h			P(H ≥ h)			h			P(H ≥ h)		
5	5	4	5	5	4	5	5	4	5	5	4	5	5	5			
4.520	.10093		6.406	.03053		8.280	.00621		4.940	.08067							
4.523	.09935		6.440	.02988		8.340	.00578		5.040	.07461							
4.531	.09785		6.451	.02926		8.363	.00564		5.120	.07179							
4.591	.09617		6.486	.02865		8.371	.00548		5.180	.07039							
4.611	.09473		6.531	.02809		8.386	.00532		5.360	.06495							
4.660	.09311		6.543	.02754		8.431	.00518		5.420	.06259							
4.706	.09172		6.603	.02697		8.463	.00502		5.460	.06015							
4.806	.08894		6.623	.02644		8.523	.00480		5.540	.05539							
4.843	.08825		6.626	.02593		8.543	.00467		5.580	.05312							
4.851	.08558		6.671	.02543		8.546	.00440		5.660	.05092							
4.866	.08419		6.760	.02490		8.683	.00427		5.780	.04878							
4.886	.08293		6.763	.02443		8.691	.00418		5.820	.04775							
4.911	.07894		6.771	.02398		8.726	.00381		5.840	.04580							
4.943	.07765		6.786	.02300		8.751	.00368		6.000	.04398							
4.980	.07637		6.806	.02210		8.771	.00357		6.020	.04312							
5.023	.07512		6.831	.02165		8.966	.00344		6.080	.03963							
5.071	.07383		6.900	.02122		8.980	.00330		6.140	.03800							
5.126	.07267		6.943	.02040		9.000	.00322		6.180	.03640							
5.163	.07020		7.000	.01910		9.011	.00293		6.260	.03480							
5.171	.06911		7.046	.01889		9.026	.00284		6.320	.03326							
5.186	.06785		7.080	.01847		9.071	.00249		6.480	.03182							
5.206	.06673		7.106	.01806		9.103	.00232		6.500	.03118							
5.231	.06552		7.171	.01770		9.163	.00197		6.540	.02981							
5.263	.06446		7.183	.01733		9.231	.00189		6.620	.02846							
5.323	.06327		7.220	.01690		9.286	.00160		6.660	.02718							
5.400	.06122		7.243	.01676		9.323	.00141		6.720	.02593							
5.446	.05905		7.266	.01578		9.411	.00135		6.740	.02475							
5.460	.05807		7.311	.01543		9.503	.00109		6.860	.02356							
5.483	.05715		7.320	.01516		9.506	.00103		6.980	.02141							
5.491	.05621		7.426	.01484		9.606	.00098		7.020	.02038							
5.526	.05576		7.446	.01424		9.643	.00095		7.220	.01935							
5.571	.05486		7.471	.01394		9.651	.00071		7.260	.01799							
5.583	.05205		7.491	.01364		9.686	.00063		7.280	.01759							
5.620	.05102		7.503	.01302		9.926	.00059		7.340	.01598							
5.643	.05016		7.563	.01269		9.986	.00043		7.440	.01521							
5.666	.04931		7.586	.01238		10.051	.00040		7.460	.01450							
5.711	.04845		7.631	.01161		10.063	.00036		7.580	.01371							
5.780	.04761		7.640	.01134		10.100	.00032		7.620	.01304							
5.803	.04721		7.686	.01102		10.260	.00029		7.740	.01233							
5.811	.04642		7.720	.01074		10.511	.00019		7.760	.01168							
5.871	.04473		7.766	.01047		10.520	.00017		7.940	.01109							
5.903	.04322		7.791	.01021		10.566	.00014		7.980	.01054							
5.963	.04241		7.823	.00978		10.646	.00013		8.000	.00946							
5.983	.04173		7.860	.00965		11.023	.00007		8.060	.00918							
5.986	.04094		7.903	.00941		11.083	.00006		8.180	.00813							
6.031	.04022		7.906	.00919		11.571	.00002		8.240	.00766							
6.086	.03951		8.006	.00897					8.340	.00725							
6.100	.03797		8.043	.00865					8.420	.00682							
6.123	.03729		8.051	.00849					8.540	.00639							
6.146	.03661		8.066	.00819		4.500	.10150		8.640	.00568							
6.166	.03527		8.086	.00798		4.560	.09952		8.660	.00553							
6.211	.03458		8.131	.00776		4.580	.09582		8.720	.00523							
6.223	.03388		8.143	.00757		4.740	.09211		8.780	.00496							
6.283	.03355		8.223	.00687		4.820	.08863		8.820	.00466							
6.303	.03291		8.226	.00670		4.860	.08530		8.880	.00423							
6.351	.03229		8.271	.00654		4.880	.08373		8.960	.00396							

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
5	5	5	6	3	1	6	3	2	6	3	3
9.060	.00374		3.818	.11905		7.045	.00693		8.628	.00141	
9.140	.00349		3.909	.09524		7.409	.00649		8.692	.00097	
9.260	.00328		3.964	.09048		7.500	.00563		8.936	.00054	
9.360	.00308		4.127	.08571		7.515	.00476		9.346	.00032	
9.380	.00292		4.418	.08333		7.576	.00390				
9.420	.00241		4.545	.06429		7.803	.00216		6	4	1
9.500	.00211		4.691	.06190		8.182	.00130				
9.620	.00182		4.782	.05238					3.864	.10996	
9.680	.00143		4.855	.05000		6	3	3	4.038	.09437	
9.740	.00136		5.127	.04762					4.106	.09177	
9.780	.00122		5.273	.03571		4.538	.10335		4.197	.08831	
9.920	.00100		5.509	.03333		4.590	.09773		4.273	.08571	
9.980	.00090		5.582	.03095		4.628	.09491		4.341	.08139	
10.140	.00073		5.727	.02857		4.731	.09037		4.356	.07879	
10.220	.00063		5.855	.02619		4.795	.08193		4.402	.06667	
10.260	.00049		5.945	.02143		4.949	.07695		4.538	.06320	
10.500	.00041		6.236	.01667		5.038	.07478		4.583	.06061	
10.580	.00030		6.582	.01190		5.141	.06981		4.818	.05887	
10.640	.00027		6.873	.00714		5.154	.06786		4.841	.05714	
10.820	.00022					5.244	.06331		4.924	.05541	
11.060	.00014		6	3	2	5.346	.06115		4.947	.04675	
11.180	.00011					5.359	.05768		5.023	.04416	
11.520	.00006		4.545	.10087		5.410	.05422		5.091	.04242	
11.580	.00006		4.682	.08528		5.449	.05271		5.152	.03983	
12.020	.00002		4.742	.07922		5.551	.05119		5.197	.03810	
12.500	.00001		4.803	.07662		5.615	.04968		5.318	.03636	
			4.848	.07489		5.654	.04665		5.455	.03463	
	6	1	4.909	.07186		5.756	.04394		5.568	.03377	
			5.015	.06061		5.769	.04221		5.652	.02857	
4.083	.10714		5.045	.05887		5.821	.04026		5.674	.02684	
			5.076	.05628		5.859	.03896		5.697	.02597	
	6	2	5.136	.05498		5.974	.03766		5.856	.02424	
			5.167	.05368		6.064	.03636		5.924	.02251	
3.822	.12698		5.227	.05195		6.179	.03398		6.038	.02165	
4.200	.09524		5.348	.04632		6.231	.03312		6.114	.02078	
4.289	.08730		5.379	.04502		6.269	.02879		6.174	.01991	
4.356	.07937		5.394	.04372		6.385	.02532		6.288	.01905	
4.622	.06349		5.500	.04069		6.436	.02229		6.402	.01558	
4.822	.04762		5.576	.03983		6.577	.02143		6.523	.01472	
5.400	.03175		5.636	.03896		6.590	.01645		6.538	.01385	
5.600	.02381		5.682	.03420		6.679	.01558		6.606	.01299	
			5.742	.03247		6.782	.01472		6.697	.01212	
	6	2	5.879	.03117		6.846	.01429		7.000	.01126	
			5.894	.02987		6.885	.01212		7.083	.01039	
4.436	.10794		6.000	.02900		7.051	.01061		7.106	.00866	
4.545	.08889		6.061	.02554		7.192	.01017		7.424	.00693	
4.655	.08571		6.136	.02294		7.410	.00779		7.500	.00519	
4.982	.05397		6.227	.01948		7.462	.00714		7.614	.00433	
5.018	.05079		6.242	.01861		7.603	.00649		7.955	.00260	
5.345	.03810		6.409	.01602		7.615	.00606				
5.527	.03651		6.545	.01558		7.872	.00433		6	4	2
5.745	.02063		6.561	.01342		8.013	.00390				
6.182	.01746		6.682	.01255		8.115	.00379		4.436	.10361	
6.545	.01111		6.712	.01169		8.231	.00292		4.494	.09986	
6.655	.00794		6.727	.01126		8.321	.00271		4.615	.09812	
6.982	.00476		6.970	.00909		8.423	.00206		4.647	.09004	

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
6	4	2	6	4	2	6	4	3	6	4	3
4.673	.08413		8.051	.00375		5.634	.04809		7.247	.01222	
4.744	.08268		8.186	.00361		5.670	.04649		7.319	.01202	
4.878	.07547		8.205	.00346		5.725	.04599		7.324	.01179	
4.904	.07446		8.308	.00289		5.753	.04532		7.368	.01159	
4.955	.06753		8.365	.00245		5.756	.04472		7.396	.01136	
4.974	.06638		8.494	.00188		5.786	.04422		7.418	.01109	
5.032	.06407		8.538	.00159		5.797	.04309		7.467	.01006	
5.051	.06205		8.667	.00101		5.885	.04259		7.500	.00966	
5.109	.05974		8.827	.00072		5.901	.04049		7.538	.00929	
5.128	.05830		9.231	.00043		5.918	.03993		7.544	.00912	
5.135	.05325					5.956	.03903		7.560	.00892	
5.186	.05108		6	4	3	5.962	.03859		7.599	.00872	
5.263	.05022					5.989	.03756		7.632	.00859	
5.340	.04906		4.599	.10220		6.011	.03696		7.681	.00846	
5.417	.04805		4.604	.09997		6.099	.03643		7.687	.00826	
5.436	.04430		4.615	.09890		6.110	.03493		7.714	.00809	
5.494	.04170		4.643	.09584		6.132	.03447		7.747	.00793	
5.590	.04084		4.654	.09494		6.154	.03360		7.775	.00709	
5.596	.03997		4.670	.09391		6.181	.03317		7.819	.00669	
5.667	.03911		4.681	.09184		6.187	.03150		7.846	.00650	
5.769	.03636		4.687	.09088		6.242	.03104		7.868	.00609	
5.801	.03146		4.725	.08988		6.253	.03057		7.940	.00596	
5.827	.03088		4.742	.08881		6.275	.03007		8.011	.00566	
5.974	.02929		4.747	.08781		6.313	.02964		8.027	.00519	
6.000	.02785		4.758	.08678		6.330	.02927		8.033	.00496	
6.032	.02597		4.819	.08575		6.401	.02887		8.132	.00483	
6.109	.02511		4.830	.08485		6.429	.02854		8.170	.00473	
6.186	.02453		4.846	.08388		6.440	.02751		8.176	.00460	
6.282	.02280		4.857	.08075		6.456	.02704		8.187	.00446	
6.288	.02165		4.868	.07969		6.462	.02597		8.203	.00413	
6.494	.02049		4.901	.07869		6.500	.02534		8.242	.00403	
6.519	.02006		4.918	.07782		6.538	.02498		8.258	.00356	
6.571	.01962		4.962	.07689		6.544	.02351		8.275	.00346	
6.590	.01833		5.033	.07443		6.604	.02281		8.346	.00333	
6.647	.01775		5.038	.07353		6.615	.02244		8.385	.00326	
6.667	.01732		5.044	.07263		6.632	.02211		8.390	.00316	
6.692	.01530		5.082	.06986		6.676	.02181		8.418	.00306	
6.724	.01385		5.110	.06830		6.714	.02013		8.538	.00293	
6.750	.01342		5.170	.06657		6.725	.01995		8.571	.00266	
6.878	.01299		5.225	.06573		6.753	.01928		8.615	.00260	
6.974	.01227		5.253	.06424		6.797	.01891		8.654	.00250	
7.032	.01169		5.275	.06354		6.813	.01865		8.687	.00216	
7.205	.01140		5.286	.06284		6.868	.01805		8.819	.00210	
7.212	.01082		5.313	.06194		6.885	.01718		8.901	.00203	
7.340	.00967		5.346	.06121		6.896	.01692		8.918	.00183	
7.385	.00938		5.357	.06054		6.940	.01642		8.967	.00176	
7.417	.00880		5.385	.05927		6.956	.01618		9.000	.00170	
7.436	.00823		5.390	.05784		6.973	.01585		9.038	.00153	
7.513	.00707		5.396	.05651		7.027	.01505		9.154	.00127	
7.571	.00678		5.401	.05574		7.033	.01479		9.170	.00100	
7.590	.00649		5.462	.05508		7.060	.01452		9.176	.00097	
7.647	.00563		5.489	.05431		7.104	.01429		9.297	.00083	
7.724	.00548		5.538	.05245		7.115	.01409		9.330	.00080	
7.821	.00519		5.571	.05108		7.143	.01322		9.346	.00067	
7.846	.00447		5.604	.05042		7.154	.01295		9.357	.00047	
7.904	.00390		5.610	.04862		7.187	.01242		9.615	.00043	

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
6	4	3	6	4	4	6	4	4	6	5	1
9.753	.00030		6.367	.03208		8.557	.00388		5.336	.04040	
9.824	.00023		6.424	.03149		8.595	.00375		5.359	.03932	
9.962	.00017		6.429	.03027		8.767	.00325		5.400	.03427	
10.385	.00010		6.481	.02944		8.781	.00314		5.459	.03247	
			6.495	.02889		8.824	.00299		5.562	.03066	
			6.514	.02761		8.857	.00285		5.574	.02958	
			6.557	.02704		8.881	.00251		5.728	.02886	
			6.581	.02651		8.900	.00240		5.767	.02778	
4.524	.10312		6.595	.02599		8.957	.00230		5.769	.02706	
4.595	.09847		6.667	.02495		8.981	.00221		5.862	.02633	
4.614	.09549		6.695	.02413		8.995	.00213		5.951	.02453	
4.667	.09240		6.724	.02316		9.095	.00202		6.074	.02092	
4.714	.09082		6.781	.02264		9.167	.00192		6.138	.01984	
4.724	.08808		6.800	.02211		9.257	.00160		6.344	.01804	
4.824	.08650		6.824	.02154		9.324	.00156		6.382	.01732	
4.829	.08515		6.881	.02108		9.395	.00150		6.485	.01659	
4.881	.08448		6.900	.01977		9.414	.00143		6.567	.01587	
4.895	.08060		6.924	.01935		9.467	.00137		6.600	.01515	
4.957	.07911		7.014	.01893		9.524	.00129		6.628	.01263	
4.981	.07780		7.029	.01850		9.600	.00110		6.690	.01190	
4.995	.07656		7.124	.01806		9.629	.00103		6.805	.01154	
5.095	.07532		7.224	.01726		9.681	.00089		6.874	.01082	
5.124	.07304		7.229	.01655		9.714	.00084		6.997	.01010	
5.129	.07173		7.267	.01587		9.795	.00070		7.182	.00974	
5.167	.07047		7.281	.01558		9.857	.00067		7.246	.00938	
5.181	.06809		7.314	.01496		9.895	.00057		7.297	.00902	
5.224	.06676		7.357	.01474		9.929	.00053		7.305	.00866	
5.257	.06558		7.381	.01413		10.024	.00042		7.421	.00722	
5.281	.06431		7.395	.01323		10.057	.00038		7.451	.00685	
5.295	.06313		7.414	.01293		10.314	.00029		7.490	.00649	
5.357	.06199		7.495	.01261		10.381	.00022		7.574	.00613	
5.395	.05995		7.529	.01236		10.424	.00014		7.592	.00577	
5.400	.05788		7.581	.01181		10.629	.00012		7.667	.00541	
5.429	.05736		7.624	.01150		10.881	.00009		8.067	.00505	
5.514	.05510		7.681	.01124		11.000	.00005		8.077	.00433	
5.581	.05411		7.695	.01101		11.429	.00003		8.167	.00397	
5.600	.05306		7.700	.01068					8.331	.00325	
5.624	.05254		7.714	.01040					8.436	.00253	
5.657	.05151		7.724	.01011					8.515	.00180	
5.667	.05052		7.795	.00990		6	5	1	8.885	.00108	
5.681	.04881		7.914	.00964		3.921	.10426				
5.781	.04793		7.929	.00945		4.128	.09271				
5.795	.04713		7.967	.00903		4.167	.09091		6	5	2
5.814	.04633		8.000	.00886		4.221	.08874		4.475	.10046	
5.857	.04464		8.024	.00852		4.269	.08550		4.596	.09807	
5.867	.04304		8.067	.00791		4.344	.08009		4.613	.09707	
5.895	.04207		8.081	.00758		4.374	.06962		4.615	.09596	
5.967	.04131		8.095	.00739		4.385	.06782		4.640	.09357	
6.024	.04059		8.181	.00654		4.497	.06566		4.668	.09241	
6.081	.03771		8.195	.00633		4.590	.06349		4.714	.08958	
6.095	.03703		8.214	.00617		4.782	.06205		4.727	.08780	
6.114	.03623		8.257	.00543		4.823	.05952		4.738	.08675	
6.124	.03543		8.324	.00519		4.836	.05087		4.811	.07842	
6.157	.03477		8.381	.00480		4.990	.04726		4.824	.07509	
6.195	.03400		8.495	.00430		5.028	.04618		4.833	.07420	
6.200	.03334		8.524	.00415		5.090	.04293		4.846	.07332	
6.329	.03267					5.151	.04185				

h P(H≥h)			h P(H≥h)			h P(H≥h)			h P(H≥h)		
6	5	2	6	5	2	6	5	2	6	5	3
4.890	.07237		6.987	.01371		9.738	.00028		5.808	.04574	
4.903	.07132		6.989	.01349		10.154	.00017		5.829	.04529	
4.932	.07032		7.042	.01321					5.830	.04350	
4.956	.06494		7.068	.01260				6 5 3	5.869	.04315	
5.044	.06416		7.119	.01210		4.497	.10022		5.874	.04198	
5.075	.06327		7.132	.01182		4.535	.09932		5.884	.04117	
5.090	.06205		7.185	.01104		4.550	.09938		5.950	.04070	
5.101	.06022		7.218	.01071		4.564	.09757		5.960	.03996	
5.154	.05744		7.299	.01016		4.589	.09665		5.981	.03922	
5.229	.05556		7.376	.00982		4.640	.09502		6.021	.03840	
5.233	.05467		7.382	.00955		4.640	.09502		6.029	.03803	
5.240	.05384		7.404	.00932		4.655	.09259		6.067	.03766	
5.273	.05234		7.462	.00916		4.695	.09006		6.074	.03724	
5.286	.05150		7.481	.00894		4.762	.08921		6.088	.03657	
5.319	.05056		7.640	.00821		4.802	.08838		6.097	.03546	
5.338	.04729		7.646	.00744		4.808	.08766		6.135	.03439	
5.440	.04662		7.673	.00727		4.817	.08695		6.150	.03401	
5.486	.04595		7.701	.00705		4.840	.08540		6.164	.03363	
5.497	.04529		7.738	.00688		4.855	.08402		6.189	.03326	
5.530	.04446		7.760	.00672		4.869	.08333		6.227	.03293	
5.585	.04135		7.804	.00655		4.884	.08031		6.240	.03261	
5.615	.03924		7.833	.00638		4.893	.07878		6.255	.03122	
5.618	.03857		7.870	.00599		4.924	.07814		6.257	.03085	
5.624	.03757		7.910	.00583		4.954	.07747		6.288	.03028	
5.662	.03691		7.956	.00566		5.008	.07547		6.362	.02997	
5.767	.03513		7.958	.00544		5.021	.07479		6.364	.02964	
5.813	.03452		8.068	.00527		5.069	.07406		6.402	.02895	
5.881	.03397		8.167	.00516		5.084	.07277		6.408	.02863	
5.899	.03269		8.187	.00505		5.097	.07139		6.417	.02792	
5.932	.03030		8.196	.00488		5.114	.06944		6.448	.02766	
5.958	.02980		8.200	.00455		5.122	.06816		6.469	.02741	
6.033	.02925		8.240	.00444		5.173	.06748		6.590	.02654	
6.057	.02853		8.273	.00427		5.189	.06680		6.600	.02626	
6.099	.02753		8.299	.00405		5.190	.06499		6.621	.02561	
6.110	.02697		8.332	.00394		5.267	.06436		6.667	.02452	
6.130	.02636		8.354	.00383		5.274	.06370		6.669	.02425	
6.189	.02570		8.404	.00372		5.297	.06256		6.684	.02369	
6.196	.02481		8.503	.00361		5.335	.06083		6.697	.02298	
6.218	.02442		8.530	.00350		5.341	.06025		6.707	.02224	
6.262	.02392		8.571	.00339		5.402	.05962		6.714	.02199	
6.275	.02214		8.615	.00316		5.417	.05907		6.722	.02172	
6.327	.02176		8.662	.00283		5.448	.05678		6.760	.02151	
6.354	.02137		8.727	.00272		5.457	.05516		6.789	.02101	
6.415	.02092		8.747	.00266		5.493	.05467		6.829	.01904	
6.525	.02054		8.800	.00233		5.495	.05412		6.874	.01879	
6.538	.02009		8.947	.00205		5.524	.05364		6.897	.01835	
6.585	.01970		8.967	.00200		5.541	.05313		6.935	.01786	
6.613	.01837		9.000	.00176		5.554	.05265		6.941	.01727	
6.646	.01798		9.011	.00161		5.600	.05001		6.981	.01678	
6.657	.01765		9.046	.00155		5.602	.04956		6.989	.01657	
6.673	.01732		9.185	.00122		5.617	.04903		7.002	.01639	
6.690	.01587		9.189	.00100		5.630	.04857		7.017	.01615	
6.771	.01537		9.275	.00094		5.640	.04808		7.124	.01558	
6.811	.01499		9.415	.00072		5.648	.04706		7.154	.01481	
6.824	.01465		9.453	.00050		5.722	.04658		7.217	.01418	
6.954	.01432		9.670	.00039		5.762	.04614		7.230	.01381	

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h P(H≥h)			h P(H≥h)			h P(H≥h)			h P(H≥h)		
6	5	3	6	5	3	6	5	4	6	5	4
7.255	.01338		8.954	.00285		4.698	.09152		5.548	.05549	
7.322	.01318		9.000	.00279		4.702	.09089		5.556	.05507	
7.354	.01303		9.008	.00270		4.704	.08912		5.561	.05433	
7.362	.01211		9.028	.00265		4.747	.08787		5.573	.05396	
7.408	.01193		9.031	.00246		4.773	.08729		5.583	.05360	
7.429	.01177		9.069	.00241		4.781	.08669		5.602	.05282	
7.430	.01143		9.074	.00237		4.815	.08613		5.610	.05210	
7.474	.01126		9.114	.00228		4.860	.08555		5.618	.05170	
7.484	.01079		9.122	.00207		4.861	.08444		5.636	.05131	
7.522	.01062		9.135	.00203		4.873	.08392		5.647	.05096	
7.550	.01032		9.150	.00187		4.890	.08283		5.656	.05061	
7.560	.01016		9.257	.00182		4.898	.08231		5.661	.04991	
7.590	.00999		9.274	.00161		4.927	.08175		5.668	.04957	
7.621	.00984		9.335	.00156		4.936	.08073		5.681	.04917	
7.627	.00967		9.364	.00151		4.948	.08023		5.685	.04882	
7.674	.00913		9.455	.00147		4.956	.07968		5.708	.04846	
7.697	.00885		9.457	.00144		4.961	.07868		5.736	.04769	
7.733	.00861		9.488	.00132		4.965	.07819		5.743	.04735	
7.750	.00849		9.541	.00130		4.981	.07763		5.756	.04702	
7.764	.00836		9.598	.00126		5.018	.07664		5.760	.04670	
7.789	.00808		9.617	.00112		5.021	.07612		5.773	.04633	
7.855	.00771		9.669	.00100		5.023	.07513		5.790	.04600	
7.933	.00756		9.714	.00083		5.036	.07463		5.818	.04563	
7.941	.00744		9.754	.00074		5.043	.07415		5.823	.04528	
8.002	.00716		9.790	.00071		5.061	.07364		5.843	.04495	
8.008	.00704		9.869	.00059		5.063	.07314		5.856	.04459	
8.069	.00692		9.897	.00057		5.068	.07119		5.896	.04428	
8.084	.00668		9.960	.00055		5.073	.07067		5.936	.04367	
8.093	.00655		9.973	.00052		5.085	.07020		5.940	.04337	
8.114	.00645		10.029	.00043		5.122	.06968		5.948	.04275	
8.154	.00624		10.141	.00036		5.136	.06922		5.981	.04209	
8.160	.00617		10.202	.00031		5.148	.06874		6.000	.04179	
8.221	.00576		10.217	.00030		5.161	.06824		6.015	.04149	
8.230	.00554		10.267	.00023		5.181	.06732		6.021	.04116	
8.269	.00536		10.364	.00021		5.193	.06688		6.022	.04030	
8.284	.00528		10.400	.00020		5.227	.06640		6.068	.04000	
8.297	.00519		10.522	.00015		5.261	.06596		6.083	.03971	
8.314	.00477		10.707	.00011		5.281	.06510		6.093	.03914	
8.373	.00467		10.829	.00008		5.298	.06467		6.098	.03887	
8.389	.00459		10.888	.00006		5.310	.06377		6.128	.03856	
8.421	.00440		11.314	.00004		5.333	.06290		6.135	.03801	
8.495	.00433					5.336	.06246		6.143	.03771	
8.535	.00423					5.340	.06205		6.156	.03712	
8.573	.00416					5.381	.06163		6.161	.03686	
8.589	.00410		4.500	.06111		5.415	.06121		6.165	.03660	
8.602	.00396		4.522	.06074		5.418	.06077		6.181	.03631	
8.617	.00389		4.536	.06043		5.422	.06035		6.188	.03605	
8.688	.00367		4.548	.06013		5.423	.05995		6.202	.03498	
8.695	.00360		4.560	.05983		5.436	.05956		6.223	.03473	
8.741	.00344		4.570	.05954		5.456	.05917		6.247	.03444	
8.754	.00337		4.581	.05925		5.458	.05877		6.256	.03418	
8.817	.00323		4.593	.05897		5.468	.05839		6.281	.03392	
8.840	.00316		4.596	.05869		5.481	.05752		6.288	.03368	
8.855	.00306		4.591	.05842		5.523	.05712		6.281	.03340	
8.907	.00300		4.588	.05816		5.527	.05671		6.285	.03315	
8.924	.00293		4.593	.05790		5.535	.05633		6.298	.03288	

h			P(H≥h)			h			P(H≥h)			h			P(H≥h)			h			P(H≥h)		
6	5	4	6	5	4	6	5	4	6	5	4	6	5	4	6	5	4	6	5	4	6	5	4
6.322	.03260		7.236	.01749		8.061	.00891		8.898	.00369													
6.333	.03212		7.256	.01734		8.063	.00883		8.902	.00358													
6.336	.03163		7.260	.01720		8.081	.00867		8.910	.00354													
6.361	.03139		7.261	.01706		8.083	.00861		8.956	.00327													
6.375	.03115		7.268	.01693		8.085	.00843		9.000	.00333													
6.396	.03061		7.273	.01677		8.098	.00833		9.015	.00324													
6.427	.03015		7.290	.01663		8.122	.00815		9.021	.00320													
6.468	.02991		7.293	.01634		8.148	.00798		9.023	.00315													
6.473	.02965		7.327	.01621		8.156	.00790		9.043	.00310													
6.503	.02941		7.333	.01608		8.160	.00782		9.061	.00307													
6.521	.02896		7.335	.01579		8.218	.00774		9.073	.00302													
6.547	.02852		7.336	.01564		8.223	.00766		9.081	.00298													
6.556	.02807		7.348	.01550		8.227	.00759		9.148	.00291													
6.615	.02785		7.361	.01535		8.236	.00751		9.156	.00281													
6.618	.02761		7.381	.01509		8.243	.00743		9.188	.00278													
6.622	.02718		7.418	.01495		8.250	.00735		9.202	.00275													
6.623	.02697		7.423	.01481		8.258	.00716		9.210	.00271													
6.643	.02677		7.436	.01455		8.273	.00696		9.218	.00267													
6.656	.02654		7.447	.01442		8.281	.00689		9.247	.00263													
6.661	.02634		7.458	.01429		8.302	.00683		9.261	.00259													
6.668	.02614		7.468	.01402		8.323	.00663		9.268	.00256													
6.681	.02592		7.473	.01389		8.333	.00644		9.293	.00252													
6.693	.02572		7.498	.01364		8.340	.00638		9.322	.00249													
6.723	.02551		7.521	.01352		8.381	.00630		9.336	.00246													
6.735	.02532		7.522	.01318		8.415	.00624		9.375	.00242													
6.736	.02511		7.556	.01296		8.422	.00598		9.393	.00237													
6.750	.02473		7.561	.01286		8.456	.00591		9.396	.00233													
6.756	.02412		7.581	.01266		8.490	.00584		9.418	.00226													
6.765	.02373		7.593	.01254		8.498	.00578		9.423	.00217													
6.793	.02353		7.628	.01242		8.521	.00572		9.427	.00209													
6.818	.02334		7.636	.01221		8.527	.00559		9.436	.00206													
6.833	.02316		7.668	.01213		8.535	.00553		9.443	.00203													
6.840	.02279		7.688	.01187		8.536	.00545		9.458	.00199													
6.847	.02261		7.693	.01165		8.543	.00541		9.461	.00189													
6.856	.02242		7.736	.01154		8.561	.00525		9.493	.00185													
6.861	.02223		7.740	.01146		8.618	.00520		9.498	.00184													
6.885	.02206		7.747	.01126		8.636	.00514		9.521	.00181													
6.896	.02148		7.748	.01118		8.640	.00503		9.523	.00176													
6.898	.02113		7.756	.01106		8.643	.00497		9.536	.00173													
6.948	.02096		7.761	.01086		8.647	.00492		9.547	.00168													
6.956	.02076		7.815	.01076		8.661	.00487		9.548	.00167													
6.961	.02042		7.818	.01064		8.681	.00482		9.556	.00164													
6.973	.02026		7.823	.01052		8.685	.00471		9.563	.00162													
6.993	.02009		7.856	.01042		8.693	.00466		9.656	.00150													
7.018	.01993		7.861	.01033		8.698	.00461		9.673	.00148													
7.021	.01975		7.881	.01022		8.708	.00454		9.690	.00146													
7.027	.01942		7.896	.01015		8.722	.00427		9.698	.00147													
7.036	.01925		7.936	.00998		8.736	.00421		9.708	.00140													
7.043	.01910		7.948	.00989		8.760	.00416		9.735	.00137													
7.056	.01894		7.961	.00979		8.761	.00412		9.748	.00128													
7.068	.01877		7.965	.00962		8.781	.00406		9.781	.00123													
7.098	.01858		8.002	.00943		8.827	.00395		9.818	.00121													
7.123	.01842		8.010	.00925		8.856	.00392		9.833	.00119													
7.125	.01826		8.018	.00917		8.868	.00388		9.843	.00116													
7.147	.01792		8.036	.00908		8.873	.00377		9.856	.00114													
7.222	.01777		8.040	.00899		8.881	.00373		9.873	.00112													

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
6	5	4	6	5	5	6	5	5	6	5	5
9.896	.00110		4.529	.10250		5.828	.04590		7.134	.01972	
9.922	.00104		4.547	.09835		5.910	.04538		7.141	.01919	
9.936	.00102		4.557	.09732		5.934	.04487		7.165	.01894	
9.960	.00100		4.604	.09625		5.941	.04436		7.216	.01843	
9.961	.00098		4.624	.09523		5.959	.04338		7.229	.01818	
10.056	.00097		4.640	.09422		5.981	.04288		7.251	.01795	
10.081	.00095		4.663	.09323		6.012	.04190		7.287	.01771	
10.083	.00093		4.688	.09225		6.016	.04095		7.310	.01748	
10.103	.00087		4.710	.09130		6.040	.04047		7.324	.01723	
10.110	.00085		4.746	.09031		6.051	.04023		7.353	.01677	
10.125	.00084		4.782	.08934		6.053	.03975		7.371	.01622	
10.147	.00074		4.804	.08844		6.087	.03880		7.416	.01579	
10.161	.00067		4.812	.08705		6.106	.03832		7.424	.01569	
10.181	.00066		4.816	.08614		6.146	.03786		7.463	.01548	
10.215	.00064		4.829	.08521		6.157	.03743		7.512	.01483	
10.323	.00057		4.851	.08430		6.224	.03697		7.522	.01463	
10.328	.00056		4.882	.08338		6.228	.03677		7.604	.01421	
10.356	.00050		4.887	.08164		6.241	.03549		7.635	.01401	
10.361	.00049		4.910	.08075		6.294	.03508		7.640	.01364	
10.365	.00048		4.922	.07987		6.299	.03427		7.653	.01345	
10.396	.00047		4.924	.07899		6.318	.03385		7.706	.01327	
10.402	.00043		4.957	.07813		6.382	.03345		7.710	.01293	
10.458	.00042		4.971	.07728		6.440	.03192		7.729	.01276	
10.468	.00041		4.993	.07645		6.463	.03153		7.734	.01259	
10.481	.00037		5.063	.07479		6.476	.03114		7.747	.01243	
10.485	.00036		5.087	.07316		6.499	.03078		7.769	.01226	
10.548	.00031		5.094	.07235		6.506	.03041		7.794	.01207	
10.560	.00030		5.112	.07156		6.524	.02971		7.816	.01158	
10.636	.00029		5.165	.07002		6.546	.02935		7.840	.01142	
10.673	.00028		5.188	.06928		6.569	.02901		7.887	.01125	
10.688	.00027		5.206	.06817		6.581	.02864		7.888	.01110	
10.708	.00023		5.228	.06668		6.618	.02829		7.918	.01093	
10.836	.00020		5.240	.06594		6.651	.02762		7.922	.01079	
10.881	.00020		5.259	.06519		6.665	.02729		7.957	.01063	
10.890	.00019		5.346	.06448		6.671	.02663		7.988	.01047	
10.893	.00017		5.347	.06378		6.687	.02630		7.993	.01017	
10.935	.00016		5.376	.06309		6.710	.02597		8.012	.01002	
10.981	.00013		5.394	.06242		6.722	.02580		8.028	.00988	
10.993	.00013		5.404	.06110		6.757	.02548		8.051	.00973	
11.036	.00012		5.416	.05943		6.781	.02517		8.063	.00944	
11.063	.00011		5.447	.05879		6.788	.02484		8.076	.00930	
11.228	.00010		5.451	.05817		6.793	.02453		8.157	.00915	
11.348	.00008		5.471	.05687		6.816	.02423		8.169	.00908	
11.348	.00007		5.522	.05561		6.859	.02390		8.171	.00882	
11.396	.00006		5.535	.05501		6.887	.02332		8.204	.00868	
11.443	.00006		5.557	.05440		6.899	.02301		8.218	.00855	
11.458	.00005		5.593	.05379		6.947	.02271		8.310	.00831	
11.565	.00004		5.629	.05317		6.953	.02242		8.346	.00818	
11.843	.00003		5.676	.05202		6.969	.02215		8.359	.00793	
11.896	.00002		5.699	.05090		6.993	.02187		8.365	.00759	
11.948	.00002		5.729	.04973		7.028	.02157		8.369	.00748	
12.375	.00001		5.734	.04917		7.040	.02130		8.404	.00735	
			5.757	.04860		7.071	.02102		8.416	.00724	
			5.769	.04803		7.088	.02076		8.451	.00703	
			5.804	.04751		7.099	.02025		8.482	.00691	
			5.824	.04696		7.110	.01998		8.487	.00670	

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
6	5	5	6	5	5	6	5	5	6	6	1
8.500	.00659		9.912	.00163		12.393	.00002		8.516	.00283	
8.553	.00649		9.934	.00156		12.435	.00002		8.923	.00250	
8.576	.00638		9.965	.00150		12.440	.00002		9.000	.00216	
8.581	.00633		9.969	.00137		12.534	.00001		9.077	.00183	
8.593	.00624		9.993	.00133		12.876	.00001		9.393	.00117	
8.594	.00614		10.006	.00129		12.922	.00000		9.692	.00050	
8.616	.00604		10.053	.00126		13.346	.00000				
8.647	.00594		10.110	.00123					6	6	2
8.699	.00566		10.169	.00113					4.419	.10670	
8.722	.00556		10.176	.00111					4.438	.09824	
8.735	.00546		10.194	.00106		3.978	.10706		4.552	.09586	
8.765	.00529		10.216	.00103		4.000	.09774		4.610	.09319	
8.782	.00511		10.271	.00100		4.077	.09441		4.800	.08786	
8.835	.00502		10.287	.00098		4.209	.09775		4.819	.08477	
8.859	.00494		10.288	.00095		4.308	.08208		4.838	.08063	
8.910	.00486		10.335	.00088		4.352	.07676		4.876	.07749	
8.934	.00471		10.341	.00083		4.593	.06943		4.933	.06829	
8.946	.00467		10.459	.00080		4.648	.06677		4.971	.06667	
8.981	.00451		10.487	.00078		4.692	.06377		5.010	.06425	
9.016	.00443		10.499	.00074		4.769	.05711		5.105	.06287	
9.018	.00437		10.529	.00067		4.857	.05112		5.219	.05782	
9.047	.00423		10.593	.00066		4.945	.04779		5.238	.05525	
9.051	.00418		10.628	.00061		5.220	.04679		5.276	.05340	
9.110	.00412		10.640	.00057		5.231	.04346		5.352	.05140	
9.118	.00398		10.699	.00055		5.264	.03746		5.410	.04993	
9.122	.00379		10.710	.00051		5.352	.03546		5.486	.04531	
9.159	.00373		10.712	.00050		5.451	.03380		5.505	.04212	
9.206	.00367		10.741	.00048		5.626	.03180		5.638	.04158	
9.212	.00356		10.759	.00043		5.736	.03114		5.676	.03777	
9.216	.00349		10.781	.00041		5.791	.02747		5.733	.03673	
9.228	.00344		10.804	.00040		5.912	.02514		5.752	.03520	
9.263	.00330		10.812	.00037		5.923	.02381		5.867	.03420	
9.334	.00323		10.816	.00036		6.055	.02248		6.019	.03216	
9.347	.00312		10.946	.00034		6.088	.02148		6.038	.03007	
9.357	.00302		11.016	.00031		6.286	.01981		6.076	.02926	
9.404	.00296		11.024	.00027		6.352	.01748		6.132	.02721	
9.440	.00291		11.041	.00026		6.407	.01693		6.171	.02574	
9.441	.00285		11.118	.00025		6.626	.01532		6.210	.02443	
9.488	.00275		11.122	.00024		6.637	.01432		6.305	.02367	
9.494	.00269		11.135	.00021		6.769	.01365		6.343	.02305	
9.510	.00265		11.169	.00020		6.802	.01265		6.419	.02200	
9.534	.00261		11.324	.00018		6.879	.01199		6.552	.02119	
9.546	.00256		11.334	.00014		7.066	.01032		6.667	.01905	
9.581	.00251		11.475	.00013		7.121	.00932		6.705	.01848	
9.629	.00245		11.522	.00012		7.374	.00899		6.819	.01577	
9.682	.00241		11.557	.00012		7.407	.00833		6.876	.01477	
9.687	.00237		11.559	.00011		7.495	.00766		7.010	.01453	
9.706	.00233		11.581	.00010		7.516	.00699		7.067	.01296	
9.722	.00219		11.659	.00009		7.592	.00599		7.105	.01234	
9.746	.00206		11.663	.00008		7.769	.00566		7.276	.01173	
9.757	.00204		11.863	.00006		7.934	.00500		7.352	.01097	
9.771	.00200		11.941	.00005		8.165	.00433		7.371	.01063	
9.793	.00188		11.981	.00005		8.195	.00450		7.410	.01020	
9.851	.00184		12.029	.00005		8.220	.00383		7.467	.00982	
9.894	.00172		12.035	.00004		8.264	.00350		7.505	.00949	
9.899	.00167		12.181	.00003		8.429	.00316				

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
6	6	2		6	6	3		6	6	3		6	6	3	
7.543	.00916			5.292	.06419	7.350	.01426	9.858	.00130						
7.619	.00830			5.333	.06329	7.358	.01277	9.933	.00125						
7.638	.00764			5.350	.06280	7.392	.01249	10.017	.00121						
7.752	.00725			5.358	.06085	7.417	.01219	10.025	.00117						
7.886	.00697			5.392	.05993	7.433	.01189	10.100	.00110						
8.019	.00668			5.400	.05894	7.483	.01166	10.125	.00106						
8.038	.00635			5.433	.05662	7.525	.01136	10.150	.00098						
8.076	.00592			5.483	.05570	7.567	.01065	10.192	.00079						
8.152	.00540			5.548	.05395	7.625	.01034	10.225	.00076						
8.210	.00488			5.567	.05237	7.683	.01009	10.350	.00062						
8.305	.00459			5.600	.05160	7.725	.00985	10.392	.00049						
8.400	.00411			5.625	.04999	7.733	.00934	10.417	.00046						
8.533	.00404			5.692	.04836	7.817	.00911	10.500	.00045						
8.610	.00343			5.725	.04760	7.833	.00859	10.525	.00040						
8.819	.00328			5.733	.04613	7.858	.00837	10.558	.00030						
8.838	.00314			5.750	.04546	7.892	.00821	10.733	.00029						
8.876	.00256			5.817	.04386	8.000	.00801	10.750	.00027						
8.933	.00252			5.833	.04306	8.025	.00782	10.858	.00019						
9.010	.00238			5.892	.04238	8.058	.00744	11.017	.00017						
9.086	.00224			5.933	.04100	8.067	.00725	11.025	.00015						
9.105	.00209			6.017	.04031	8.100	.00716	11.125	.00010						
9.219	.00200			6.025	.03998	8.150	.00660	11.267	.00009						
9.352	.00176			6.058	.03885	8.192	.00622	11.350	.00008						
9.505	.00167			6.100	.03835	8.225	.00604	11.567	.00004						
9.600	.00157			6.125	.03715	8.350	.00560	11.725	.00003						
9.638	.00138			6.150	.03545	8.400	.00543	12.150	.00001						
9.676	.00109			6.192	.03356	8.417	.00514					6	6	4	
9.752	.00095			6.225	.03291	8.458	.00497								
9.867	.00067			6.267	.03130	8.600	.00483	4.518	.10088						
9.943	.00062			6.350	.03070	8.625	.00471	4.548	.09982						
10.076	.00043			6.358	.02961	8.683	.00437	4.603	.09878						
10.210	.00040			6.400	.02873	8.692	.00423	4.636	.09774						
10.305	.00021			6.483	.02820	8.725	.00397	4.662	.09575						
10.552	.00017			6.525	.02765	8.750	.00384	4.695	.09469						
10.971	.00007			6.558	.02576	8.767	.00371	4.706	.09372						
		6	6	3		8.817	.00359	4.724	.09164						
						8.858	.00341	4.765	.08968						
						8.900	.00330	4.779	.08869						
						8.958	.00310	4.783	.08572						
						9.017	.00300	4.824	.08479						
						9.058	.00289	4.871	.08295						
						9.083	.00282	4.897	.08026						
						9.150	.00273	4.930	.07930						
						9.225	.00253	4.956	.07842						
						9.392	.00228	5.000	.07753						
						9.400	.00213	5.048	.07403						
						9.433	.00206	5.077	.07324						
						9.458	.00199	5.132	.07244						
						9.483	.00193	5.165	.07160						
						9.525	.00185	5.191	.07006						
						9.567	.00174	5.195	.06930						
						9.600	.00161	5.224	.06855						
						9.667	.00153	5.235	.06781						
						9.683	.00147	5.254	.06626						
						9.725	.00141	5.294	.06554						
						9.792	.00136								

h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
6	6	4	6	6	4	6	6	4	6	6	4	6	6	4	
5.309	.06406		6.824	.02396		8.529	.00652		10.250	.00108					
5.313	.06372		6.842	.02328		8.577	.00605		10.283	.00102					
5.342	.06163		6.882	.02298		8.588	.00595		10.342	.00100					
5.368	.06096		6.901	.02233		8.603	.00576		10.426	.00094					
5.401	.05951		6.930	.02203		8.607	.00554		10.430	.00092					
5.426	.05819		6.989	.02090		8.636	.00546		10.460	.00090					
5.485	.05750		7.015	.02060		8.665	.00537		10.471	.00086					
5.489	.05680		7.074	.02031		8.706	.00527		10.489	.00083					
5.544	.05618		7.107	.01974		8.721	.00506		10.588	.00081					
5.577	.05491		7.118	.01949		8.754	.00497		10.607	.00074					
5.607	.05367		7.132	.01924		8.765	.00487		10.647	.00067					
5.695	.05188		7.165	.01870		8.783	.00467		10.662	.00062					
5.706	.05130		7.176	.01844		8.838	.00459		10.695	.00055					
5.721	.05009		7.250	.01797		8.842	.00449		10.721	.00053					
5.724	.04950		7.254	.01747		8.897	.00418		10.754	.00052					
5.754	.04894		7.313	.01724		8.901	.00410		10.779	.00045					
5.765	.04785		7.342	.01676		8.960	.00401		10.871	.00044					
5.783	.04728		7.353	.01654		9.000	.00394		10.882	.00042					
5.838	.04673		7.371	.01561		9.015	.00377		10.901	.00035					
5.871	.04617		7.426	.01518		9.074	.00369		10.956	.00033					
5.882	.04565		7.460	.01475		9.107	.00361		10.989	.00030					
5.897	.04396		7.485	.01455		9.165	.00356		11.048	.00029					
5.930	.04340		7.518	.01435		9.191	.00349		11.136	.00024					
5.941	.04290		7.529	.01396		9.195	.00331		11.191	.00023					
5.956	.04185		7.548	.01372		9.224	.00325		11.250	.00022					
5.960	.04129		7.577	.01353		9.235	.00318		11.254	.00017					
5.989	.04080		7.607	.01333		9.250	.00305		11.313	.00016					
6.015	.04030		7.647	.01314		9.283	.00290		11.353	.00016					
6.018	.03977		7.662	.01240		9.313	.00278		11.368	.00015					
6.118	.03928		7.779	.01219		9.368	.00265		11.489	.00014					
6.136	.03829		7.783	.01211		9.401	.00259		11.518	.00011					
6.191	.03786		7.813	.01179		9.412	.00255		11.529	.00010					
6.195	.03738		7.838	.01117		9.426	.00242		11.588	.00010					
6.224	.03650		7.871	.01083		9.489	.00236		11.765	.00009					
6.235	.03609		7.956	.01071		9.529	.00231		11.779	.00006					
6.250	.03521		7.960	.01054		9.548	.00225		11.783	.00006					
6.283	.03388		7.989	.01027		9.577	.00220		11.882	.00005					
6.312	.03347		8.000	.00998		9.603	.00211		11.960	.00005					
6.368	.03269		8.015	.00964		9.647	.00206		12.077	.00004					
6.371	.03228		8.059	.00934		9.662	.00195		12.235	.00003					
6.401	.03189		8.074	.00904		9.695	.00190		12.283	.00002					
6.412	.03149		8.077	.00887		9.721	.00185		12.368	.00002					
6.485	.03068		8.107	.00862		9.724	.00180		12.426	.00002					
6.489	.03050		8.136	.00849		9.812	.00177		12.721	.00001					
6.518	.02978		8.165	.00835		9.842	.00173		12.812	.00001					
6.544	.02942		8.191	.00821		9.897	.00169		13.235	.00000					
6.548	.02866		8.224	.00807		9.901	.00165					6	6	5	
6.577	.02795		8.254	.00797		9.930	.00161					4.541	.10077		
6.603	.02761		8.309	.00772		9.941	.00154					4.542	.09987		
6.636	.02723		8.342	.00747		10.000	.00144					4.548	.09900		
6.647	.02690		8.368	.00734		10.018	.00134					4.562	.09813		
6.665	.02618		8.401	.00721		10.074	.00127					4.563	.09726		
6.721	.02585		8.430	.00700		10.077	.00124					4.574	.09641		
6.779	.02555		8.471	.00690		10.107	.00121					4.626	.09556		
6.783	.02521		8.485	.00676		10.132	.00118								
6.812	.02458		8.489	.00663		10.176	.00112								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
6	6	5	6	6	5	6	6	5	6	6	5
4.635	.09472		5.641	.05182		6.654	.02754		7.587	.01443	
4.652	.09387		5.705	.05133		6.685	.02725		7.607	.01426	
4.654	.09304		5.740	.05086		6.718	.02696		7.626	.01411	
4.659	.09222		5.752	.05039		6.727	.02669		7.629	.01394	
4.719	.09134		5.765	.04993		6.759	.02615		7.648	.01378	
4.727	.09099		5.771	.04970		6.770	.02589		7.680	.01363	
4.740	.09020		5.786	.04924		6.822	.02562		7.685	.01348	
4.746	.08934		5.809	.04878		6.829	.02538		7.707	.01331	
4.752	.08861		5.818	.04790		6.838	.02514		7.720	.01302	
4.763	.08783		5.830	.04746		6.848	.02489		7.763	.01287	
4.771	.08707		5.835	.04702		6.871	.02465		7.791	.01272	
4.882	.08628		5.844	.04659		6.876	.02441		7.835	.01258	
4.889	.08554		5.848	.04615		6.895	.02417		7.838	.01243	
4.897	.08481		5.871	.04571		6.897	.02393		7.858	.01229	
4.903	.08407		5.881	.04528		6.915	.02370		7.889	.01215	
4.907	.08192		5.907	.04445		6.942	.02357		7.920	.01202	
4.915	.08118		5.940	.04404		6.946	.02311		7.927	.01176	
4.929	.08046		5.942	.04363		6.948	.02286		7.929	.01163	
4.940	.07976		5.956	.04321		6.959	.02263		7.940	.01149	
4.946	.07905		5.959	.04281		6.974	.02217		7.942	.01136	
4.956	.07765		6.018	.04200		7.007	.02172		7.946	.01123	
4.982	.07695		6.026	.04160		7.026	.02149		7.962	.01110	
5.018	.07558		6.038	.04119		7.038	.02127		7.982	.01098	
5.054	.07423		6.054	.04042		7.041	.02106		7.993	.01072	
5.060	.07354		6.059	.03964		7.058	.02083		8.014	.01060	
5.071	.07288		6.080	.03925		7.080	.02061		8.026	.01047	
5.085	.07222		6.142	.03887		7.093	.02040		8.041	.01035	
5.119	.07155		6.162	.03814		7.105	.02017		8.073	.01023	
5.165	.07027		6.165	.03776		7.152	.01996		8.103	.01011	
5.182	.06965		6.191	.03740		7.162	.01975		8.119	.01001	
5.191	.06907		6.214	.03704		7.209	.01955		8.124	.00990	
5.229	.06840		6.273	.03668		7.214	.01935		8.129	.00966	
5.248	.06810		6.315	.03634		7.230	.01916		8.152	.00956	
5.254	.06689		6.319	.03600		7.237	.01896		8.170	.00944	
5.273	.06629		6.320	.03566		7.260	.01876		8.182	.00939	
5.281	.06568		6.327	.03533		7.282	.01855		8.214	.00918	
5.295	.06508		6.340	.03483		7.315	.01836		8.222	.00907	
5.346	.06450		6.341	.03449		7.319	.01818		8.241	.00895	
5.348	.06392		6.352	.03415		7.340	.01781		8.260	.00885	
5.374	.06334		6.371	.03349		7.365	.01763		8.282	.00865	
5.378	.06277		6.393	.03315		7.371	.01743		8.319	.00854	
5.391	.06191		6.400	.03250		7.378	.01724		8.348	.00834	
5.407	.06136		6.413	.03234		7.386	.01706		8.365	.00813	
5.430	.06025		6.430	.03169		7.387	.01687		8.386	.00804	
5.437	.05914		6.437	.03139		7.407	.01668		8.391	.00794	
5.452	.05859		6.452	.03107		7.438	.01649		8.459	.00784	
5.482	.05752		6.476	.03076		7.459	.01630		8.485	.00774	
5.495	.05696		6.503	.03045		7.471	.01612		8.495	.00765	
5.503	.05644		6.505	.03014		7.497	.01594		8.505	.00748	
5.505	.05590		6.518	.02984		7.511	.01560		8.511	.00738	
5.515	.05538		6.541	.02954		7.518	.01552		8.515	.00730	
5.524	.05486		6.587	.02924		7.524	.01534		8.542	.00720	
5.587	.05432		6.609	.02895		7.529	.01518		8.563	.00711	
5.593	.05381		6.613	.02867		7.563	.01510		8.570	.00702	
5.629	.05281		6.622	.02839		7.570	.01475		8.600	.00685	
5.635	.05231		6.629	.02810		7.574	.01459		8.609	.00677	

h			P(H ≥ h)			h			P(H ≥ h)			h			P(H ≥ h)		
6	6	5	6	6	5	6	6	5	6	6	5	6	6	5	6	6	5
8.626	.00659		9.673	.00279		10.635	.00089		12.171	.00007							
8.641	.00651		9.693	.00275		10.641	.00088		12.209	.00006							
8.652	.00642		9.707	.00271		10.648	.00084		12.230	.00006							
8.673	.00635		9.719	.00262		10.718	.00082		12.260	.00005							
8.680	.00627		9.720	.00258		10.771	.00080		12.438	.00005							
8.705	.00619		9.724	.00255		10.786	.00079		12.485	.00004							
8.711	.00611		9.740	.00247		10.837	.00076		12.489	.00004							
8.724	.00607		9.746	.00244		10.848	.00074		12.562	.00003							
8.746	.00591		9.759	.00240		10.888	.00071		12.574	.00003							
8.763	.00583		9.770	.00236		10.895	.00069		12.607	.00003							
8.778	.00576		9.829	.00229		10.920	.00068		12.740	.00003							
8.818	.00569		9.844	.00222		10.942	.00067		12.903	.00002							
8.829	.00561		9.871	.00219		10.948	.00065		12.941	.00002							
8.835	.00547		9.881	.00215		10.959	.00064		12.946	.00002							
8.837	.00540		9.897	.00212		10.993	.00063		12.982	.00001							
8.881	.00537		9.927	.00206		11.000	.00062		13.071	.00001							
8.903	.00522		9.929	.00202		11.014	.00060		13.346	.00001							
8.920	.00515		9.948	.00199		11.038	.00055		13.348	.00001							
8.962	.00508		9.986	.00196		11.058	.00054		13.386	.00001							
8.982	.00502		10.000	.00193		11.059	.00050		13.430	.00001							
8.987	.00495		10.013	.00191		11.073	.00048		13.778	.00000							
9.014	.00488		10.018	.00187		11.119	.00048		13.818	.00000							
9.018	.00482		10.052	.00184		11.129	.00046		14.235	.00000							
9.038	.00475		10.054	.00180		11.142	.00042										
9.044	.00470		10.073	.00177		11.162	.00041					6	6	6			
9.093	.00458		10.080	.00174		11.171	.00040					4.538	.10000				
9.097	.00446		10.085	.00169		11.230	.00039					4.643	.09874				
9.118	.00440		10.097	.00166		11.241	.00035					4.667	.09669				
9.129	.00434		10.118	.00163		11.273	.00034					4.678	.09261				
9.156	.00429		10.142	.00160		11.289	.00034					4.713	.09160				
9.163	.00423		10.163	.00157		11.307	.00033					4.784	.08764				
9.171	.00416		10.178	.00155		11.359	.00031					4.819	.08573				
9.182	.00411		10.209	.00152		11.371	.00028					4.877	.08381				
9.191	.00406		10.241	.00145		11.387	.00027					4.924	.08199				
9.237	.00395		10.248	.00143		11.393	.00026					4.994	.08019				
9.254	.00389		10.289	.00142		11.418	.00025					5.053	.07676				
9.280	.00384		10.293	.00140		11.476	.00024					5.064	.07580				
9.281	.00373		10.327	.00135		11.518	.00023					5.099	.07420				
9.327	.00368		10.346	.00132		11.582	.00020					5.135	.07251				
9.341	.00363		10.348	.00130		11.629	.00020					5.158	.07092				
9.348	.00358		10.352	.00128		11.652	.00019					5.193	.06852				
9.352	.00354		10.374	.00125		11.654	.00018					5.240	.06693				
9.365	.00349		10.378	.00123		11.659	.00017					5.298	.06536				
9.374	.00344		10.393	.00121		11.705	.00017					5.345	.06391				
9.393	.00335		10.426	.00119		11.727	.00015					5.415	.06240				
9.400	.00330		10.430	.00117		11.746	.00014					5.474	.06107				
9.426	.00326		10.437	.00113		11.765	.00013					5.485	.05968				
9.437	.00322		10.452	.00111		11.809	.00013					5.509	.05704				
9.458	.00317		10.471	.00109		11.882	.00012					5.556	.05575				
9.505	.00313		10.482	.00106		11.915	.00012					5.626	.05448				
9.529	.00305		10.503	.00104		11.920	.00011					5.661	.05200				
9.541	.00302		10.515	.00102		11.942	.00010					5.696	.05138				
9.548	.00298		10.524	.00100		12.058	.00009					5.719	.05021				
9.574	.00290		10.593	.00097		12.093	.00009					5.801	.04905				
9.609	.00286		10.607	.00095		12.103	.00008					5.836	.04789				
9.613	.00283		10.629	.00093		12.165	.00008										

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
6	6	6	6	6	6	6	6	6	7	7	7
5.930	.04679		8.456	.00939		10.959	.00085		4.683	.09476	
5.942	.04523		8.468	.00817		10.982	.00082		4.698	.09349	
5.977	.04417		8.503	.00792		11.088	.00079		4.727	.09223	
6.000	.04214		8.526	.00770		11.099	.00075		4.772	.08850	
6.035	.04112		8.561	.00758		11.240	.00069		4.831	.08728	
6.117	.04011		8.573	.00735		11.275	.00065		4.839	.08492	
6.140	.03916		8.643	.00714		11.310	.00062		4.876	.08375	
6.187	.03824		8.667	.00692		11.368	.00059		4.905	.08260	
6.222	.03779		8.784	.00652		11.380	.00057		4.965	.08146	
6.327	.03596		8.842	.00634		11.404	.00051		4.994	.08036	
6.351	.03513		8.854	.00613		11.415	.00049		5.010	.07928	
6.398	.03430		8.924	.00595		11.474	.00045		5.017	.07874	
6.421	.03350		8.982	.00560		11.556	.00041		5.039	.07715	
6.468	.03272		8.994	.00552		11.591	.00036		5.076	.07503	
6.503	.03117		9.029	.00535		11.614	.00034		5.098	.07399	
6.538	.03039		9.064	.00519		11.661	.00032		5.106	.07297	
6.632	.02891		9.088	.00502		11.684	.00029		5.128	.07195	
6.678	.02821		9.170	.00471		11.789	.00027		5.195	.07094	
6.737	.02752		9.205	.00448		11.801	.00024		5.217	.06997	
6.749	.02717		9.275	.00434		11.825	.00023		5.262	.06803	
6.772	.02652		9.310	.00407		11.942	.00021		5.276	.06709	
6.877	.02588		9.404	.00392		11.977	.00019		5.351	.06616	
6.889	.02493		9.485	.00379		12.012	.00018		5.365	.06435	
6.924	.02372		9.509	.00368		12.035	.00017		5.373	.06346	
6.982	.02311		9.556	.00356		12.117	.00015		5.395	.06257	
7.029	.02253		9.579	.00334		12.292	.00012		5.410	.06169	
7.053	.02196		9.626	.00312		12.316	.00011		5.432	.06125	
7.064	.02141		9.696	.00302		12.363	.00010		5.440	.06039	
7.099	.02085		9.719	.00293		12.433	.00009		5.484	.05953	
7.170	.02030		9.731	.00283		12.538	.00008		5.499	.05869	
7.240	.01979		9.789	.00272		12.573	.00006		5.573	.05702	
7.298	.01929		9.836	.00263		12.737	.00006		5.610	.05622	
7.310	.01880		9.871	.00259		12.772	.00005		5.618	.05544	
7.345	.01856		9.906	.00249		12.784	.00005		5.662	.05466	
7.380	.01807		9.930	.00241		12.877	.00004		5.699	.05312	
7.404	.01763		9.977	.00232		13.053	.00003		5.707	.05275	
7.450	.01720		10.047	.00224		13.135	.00003		5.729	.05201	
7.520	.01590		10.140	.00217		13.205	.00002		5.751	.05128	
7.614	.01549		10.152	.00213		13.345	.00002		5.766	.05055	
7.626	.01471		10.187	.00198		13.520	.00001		5.819	.04911	
7.684	.01430		10.211	.00184		13.556	.00001		5.840	.04806	
7.731	.01391		10.246	.00177		13.661	.00001		5.885	.04736	
7.825	.01355		10.257	.00170		13.930	.00001		5.907	.04601	
7.871	.01320		10.327	.00164		14.000	.00000		5.967	.04534	
7.895	.01287		10.398	.00157		14.327	.00000		6.019	.04470	
7.906	.01269		10.433	.00146		14.363	.00000		6.033	.04406	
7.942	.01217		10.526	.00140		14.749	.00000		6.063	.04343	
8.000	.01151		10.561	.00137		15.158	.00000		6.078	.04220	
8.035	.01117		10.608	.00127					6.108	.04098	
8.047	.01087		10.667	.00122					6.152	.04038	
8.082	.01055		10.713	.00117					6.167	.03979	
8.187	.01024		10.749	.00112		4.549	.10069		6.174	.03921	
8.222	.00994		10.772	.00108		4.594	.09933		6.212	.03863	
8.292	.00940		10.819	.00104		4.631	.09800		6.241	.03806	
8.316	.00913		10.842	.00101		4.638	.09670		6.263	.03778	
8.433	.00886		10.889	.00097		4.660	.09604		6.286	.03723	

h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
7	7	7	7	7	7	7	7	7	7	7	7	7	7	7	7
6.301	.03669	7.978	.01290	9.647	.00392	11.421	.00090								
6.330	.03614	8.037	.01270	9.670	.00385	11.451	.00086								
6.375	.03561	8.045	.01240	9.707	.00378	11.488	.00085								
6.434	.03509	8.067	.01220	9.774	.00371	11.495	.00083								
6.442	.03484	8.082	.01201	9.803	.00364	11.518	.00082								
6.454	.03384	8.104	.01191	9.818	.00358	11.584	.00080								
6.479	.03286	8.111	.01153	9.826	.00348	11.629	.00076								
6.501	.03236	8.156	.01134	9.848	.00342	11.644	.00074								
6.509	.03188	8.171	.01097	9.885	.00335	11.673	.00072								
6.553	.03140	8.223	.01078	9.892	.00329	11.688	.00071								
6.597	.03093	8.282	.01061	9.937	.00317	11.718	.00069								
6.620	.03001	8.289	.01043	9.974	.00305	11.777	.00068								
6.679	.02956	8.304	.01026	10.004	.00299	11.785	.00067								
6.701	.02934	8.334	.01009	10.026	.00293	11.807	.00065								
6.731	.02847	8.378	.00992	10.085	.00282	11.844	.00063								
6.768	.02804	8.401	.00976	10.160	.00277	11.852	.00060								
6.798	.02763	8.438	.00960	10.174	.00269	11.874	.00058								
6.820	.02722	8.468	.00944	10.182	.00264	11.896	.00058								
6.835	.02681	8.482	.00914	10.249	.00254	11.941	.00055								
6.865	.02641	8.512	.00898	10.293	.00249	11.963	.00053								
6.879	.02601	8.557	.00869	10.308	.00239	12.030	.00051								
6.909	.02562	8.579	.00854	10.338	.00234	12.045	.00050								
6.954	.02446	8.601	.00847	10.360	.00225	12.074	.00049								
6.968	.02408	8.616	.00818	10.382	.00221	12.089	.00047								
7.035	.02371	8.638	.00804	10.419	.00216	12.141	.00046								
7.043	.02335	8.668	.00790	10.442	.00212	12.178	.00045								
7.132	.02263	8.690	.00777	10.486	.00203	12.223	.00044								
7.154	.02212	8.779	.00763	10.516	.00199	12.230	.00043								
7.176	.02179	8.839	.00725	10.560	.00191	12.252	.00042								
7.213	.02145	8.883	.00713	10.575	.00187	12.297	.00040								
7.221	.02129	8.905	.00689	10.605	.00183	12.312	.00039								
7.236	.02065	8.913	.00683	10.709	.00179	12.341	.00037								
7.243	.02033	8.935	.00672	10.716	.00172	12.378	.00036								
7.280	.02001	8.972	.00649	10.738	.00167	12.386	.00035								
7.332	.01970	9.002	.00627	10.776	.00164	12.430	.00034								
7.354	.01910	9.024	.00615	10.783	.00162	12.445	.00033								
7.369	.01880	9.091	.00605	10.905	.00159	12.475	.00031								
7.399	.01850	9.106	.00589	10.828	.00153	12.497	.00031								
7.414	.01821	9.113	.00579	10.842	.00149	12.519	.00030								
7.481	.01792	9.135	.00569	10.887	.00146	12.564	.00029								
7.488	.01765	9.173	.00558	10.894	.00143	12.609	.00028								
7.503	.01737	9.180	.00549	10.917	.00140	12.623	.00027								
7.577	.01709	9.269	.00539	10.961	.00137	12.675	.00026								
7.599	.01683	9.284	.00529	11.006	.00132	12.712	.00025								
7.622	.01670	9.291	.00520	11.043	.00129	12.787	.00024								
7.636	.01619	9.358	.00511	11.050	.00126	12.824	.00023								
7.666	.01568	9.373	.00493	11.072	.00123	12.831	.00023								
7.688	.01543	9.380	.00485	11.109	.00121	12.846	.00021								
7.711	.01494	9.403	.00476	11.139	.00118	12.853	.00020								
7.770	.01470	9.447	.00459	11.250	.00113	12.891	.00020								
7.800	.01446	9.492	.00442	11.273	.00111	12.920	.00019								
7.814	.01423	9.506	.00434	11.288	.00104	12.942	.00019								
7.844	.01400	9.581	.00418	11.310	.00100	12.965	.00018								
7.884	.01355	9.618	.00411	11.317	.00098	13.009	.00018								
7.933	.01333	9.625	.00407	11.362	.00096	13.032	.00017								
7.955	.01311	9.640	.00400	11.377	.00094	13.054	.00017								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h			h			h			h		
P(H ₂ ≥ h)			P(H ₂ ≥ h)			P(H ₂ ≥ h)			P(H ₂ ≥ h)		
7	7	7	7	7	7	8	8	8	8	8	8
13.091	.00016		15.414	.00000		5.255	.06865		6.395	.03557	
13.113	.00016		15.503	.00000		5.265	.06802		6.405	.03523	
13.180	.00015		15.636	.00000		5.285	.06739		6.455	.03454	
13.187	.00014		15.703	.00000		5.315	.06615		6.480	.03421	
13.232	.00014		15.725	.00000		5.345	.06554		6.485	.03404	
13.276	.00013		15.792	.00000		5.360	.06494		6.495	.03372	
13.291	.00013		15.904	.00000		5.375	.06434		6.500	.03339	
13.299	.00013		16.052	.00000		5.415	.06374		6.515	.03306	
13.365	.00012		16.096	.00000		5.420	.06267		6.540	.03274	
13.380	.00012		16.186	.00000		5.435	.06229		6.585	.03242	
13.410	.00011		16.393	.00000		5.445	.06172		6.605	.03211	
13.425	.00010		16.416	.00000		5.460	.06143		6.615	.03180	
13.447	.00010		16.482	.00000		5.465	.06030		6.620	.03135	
13.455	.00010		16.750	.00000		5.495	.05973		6.635	.03104	
13.514	.00009		16.794	.00000		5.505	.05862		6.660	.03074	
13.544	.00008		17.098	.00000		5.540	.05807		6.665	.03044	
13.566	.00008		17.121	.00000		5.580	.05752		6.695	.02984	
13.588	.00007		17.462	.00000		5.585	.05699		6.720	.02926	
13.647	.00007		17.818	.00000		5.595	.05646		6.740	.02897	
13.677	.00007					5.615	.05593		6.755	.02868	
13.722	.00006					5.645	.05540		6.795	.02812	
13.744	.00006					5.660	.05489		6.845	.02784	
13.781	.00005		4.580	.10023		5.685	.05438		6.855	.02743	
13.811	.00005		4.595	.09933		5.705	.05388		6.860	.02717	
13.855	.00005		4.605	.09845		5.715	.05268		6.905	.02663	
13.892	.00005		4.625	.09757		5.735	.05239		6.935	.02637	
13.900	.00004		4.635	.09670		5.765	.05141		6.945	.02586	
13.922	.00004		4.655	.09583		5.780	.05092		6.965	.02561	
14.033	.00004		4.685	.09326		5.795	.05068		6.980	.02510	
14.048	.00004		4.695	.09241		5.805	.04973		6.995	.02485	
14.078	.00004		4.740	.09157		5.820	.04926		7.020	.02460	
14.093	.00003		4.745	.09075		5.840	.04879		7.035	.02436	
14.182	.00003		4.805	.08911		5.855	.04833		7.065	.02387	
14.278	.00003		4.820	.08792		5.915	.04787		7.085	.02364	
14.315	.00002		4.835	.08712		5.955	.04653		7.115	.02317	
14.345	.00002		4.860	.08634		5.985	.04609		7.125	.02293	
14.367	.00002		4.865	.08595		6.000	.04523		7.145	.02270	
14.390	.00002		4.875	.08441		6.005	.04502		7.215	.02247	
14.456	.00002		4.880	.08364		6.020	.04460		7.220	.02204	
14.494	.00002		4.905	.08288		6.045	.04375		7.235	.02171	
14.523	.00002		4.940	.08212		6.065	.04292		7.260	.02149	
14.568	.00002		4.955	.08063		6.080	.04251		7.265	.02138	
14.701	.00001		4.965	.07990		6.125	.04210		7.280	.02117	
14.716	.00001		4.995	.07916		6.135	.04150		7.295	.02075	
14.774	.00001		4.995	.07844		6.140	.04110		7.305	.02054	
14.746	.00001		5.040	.07771		6.155	.04070		7.335	.02033	
14.835	.00001		5.045	.07701		6.180	.04031		7.340	.02012	
14.924	.00001		5.055	.07631		6.185	.03993		7.355	.01992	
14.968	.00001		5.105	.07561		6.245	.03954		7.385	.01972	
15.028	.00001		5.120	.07492		6.255	.03917		7.415	.01932	
15.050	.00001		5.135	.07458		6.260	.03879		7.440	.01912	
15.117	.00001		5.145	.07324		6.305	.03842		7.445	.01893	
15.147	.00001		5.165	.07191		6.315	.03770		7.460	.01873	
15.228	.00001		5.180	.07125		6.320	.03734		7.485	.01855	
15.369	.00000		5.195	.06993		6.335	.03698		7.505	.01835	
15.384	.00000		5.235	.06928		6.365	.03627		7.580	.01798	

n		P(-≥h)		n		P(-≥h)		n		P(-≥h)	
h	P	h	P	h	P	h	P	h	P	h	P
7.595	.01780	8.705	.00847	9.905	.00381	11.045	.0014				
7.605	.01727	8.720	.00838	9.915	.00373	11.060	.0014				
7.620	.01701	8.735	.00829	9.920	.00368	11.085	.0014				
7.625	.01683	8.765	.00820	9.935	.00364	11.105	.0014				
7.655	.01666	8.780	.00811	9.965	.00359	11.115	.0014				
7.665	.01649	8.795	.00802	9.980	.00355	11.120	.0014				
7.695	.01615	8.820	.00793	9.995	.00351	11.179	.0014				
7.715	.01599	8.835	.00780	10.035	.00347	11.195	.0014				
7.740	.01562	8.880	.00763	10.055	.00343	11.255	.0014				
7.745	.01566	8.885	.00755	10.085	.00339	11.265	.0014				
7.760	.01550	8.915	.00747	10.095	.00335	11.285	.0014				
7.805	.01534	8.945	.00738	10.115	.00331	11.315	.0014				
7.835	.01502	8.955	.00730	10.125	.00327	11.340	.0014				
7.845	.01487	8.960	.00723	10.140	.00325	11.345	.0014				
7.865	.01471	9.005	.00715	10.145	.00320	11.355	.0014				
7.875	.01456	9.015	.00707	10.160	.00316	11.375	.0014				
7.895	.01441	9.035	.00699	10.185	.00312	11.405	.0014				
7.935	.01426	9.045	.00684	10.205	.00305	11.420	.0014				
7.940	.01419	9.060	.00677	10.220	.00298	11.435	.0014				
7.955	.01405	9.065	.00669	10.260	.00291	11.445	.0014				
7.980	.01376	9.105	.00647	10.265	.00287	11.465	.0014				
7.985	.01347	9.125	.00640	10.305	.00283	11.495	.0014				
8.000	.01333	9.140	.00633	10.320	.00280	11.520	.0014				
8.015	.01326	9.155	.00626	10.355	.00277	11.535	.0014				
8.045	.01298	9.195	.00619	10.365	.00270	11.540	.0014				
8.060	.01285	9.215	.00612	10.385	.00267	11.555	.0014				
8.105	.01258	9.245	.00598	10.415	.00260	11.580	.0014				
8.115	.01244	9.260	.00588	10.445	.00257	11.585	.0014				
8.135	.01231	9.285	.00582	10.460	.00254	11.625	.0014				
8.145	.01218	9.305	.00575	10.500	.00251	11.655	.0014				
8.180	.01206	9.335	.00589	10.535	.00248	11.705	.0009				
8.205	.01193	9.360	.00562	10.545	.00239	11.735	.0009				
8.235	.01181	9.365	.00556	10.565	.00234	11.760	.0009				
8.240	.01168	9.375	.00550	10.580	.00231	11.765	.0009				
8.255	.01156	9.380	.00547	10.595	.00230	11.780	.0009				
8.285	.01132	9.395	.00535	10.635	.00224	11.795	.0009				
8.295	.01120	9.420	.00529	10.640	.00221	11.805	.0009				
8.315	.01097	9.455	.00523	10.655	.00216	11.840	.0007				
8.340	.01085	9.465	.00511	10.665	.00213	11.855	.0008				
8.345	.01074	9.485	.00505	10.685	.00211	11.885	.0008				
8.375	.01062	9.495	.00494	10.715	.00208	11.895	.0008				
8.385	.01051	9.500	.00488	10.745	.00205	11.915	.0008				
8.405	.01029	9.555	.00483	10.805	.00200	11.940	.0008				
8.420	.01023	9.620	.00466	10.815	.00198	11.945	.0007				
8.435	.01012	9.645	.00456	10.820	.00193	12.005	.0007				
8.465	.00991	9.665	.00450	10.845	.00191	12.020	.0007				
8.495	.00980	9.680	.00445	10.860	.00188	12.060	.0007				
8.505	.00970	9.695	.00443	10.895	.00186	12.065	.0007				
8.540	.00959	9.740	.00433	10.905	.00184	12.080	.0007				
8.565	.00939	9.755	.00428	10.935	.00181	12.125	.0007				
8.615	.00929	9.765	.00423	10.940	.00180	12.140	.0006				
8.640	.00919	9.780	.00413	10.955	.00178	12.165	.0006				
8.645	.00914	9.785	.00409	10.980	.00174	12.185	.0006				
8.655	.00876	9.815	.00399	10.985	.00172	12.195	.0006				
8.660	.00866	9.855	.00390	10.995	.00167	12.215	.0006				
8.685	.00857	9.875	.00366	11.015	.00165	12.245	.0006				

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h			h			h			h		
P(H≥h)			P(H≥h)			P(H≥h)			P(H≥h)		
R	R	R	R	R	R	R	R	R	R	R	R
12.255	.00062		13.460	.00021		14.640	.00006		15.935	.00001	
12.260	.00060		13.500	.00021		14.660	.00005		15.965	.00001	
12.285	.00059		13.505	.00020		14.715	.00005		15.995	.00001	
12.335	.00057		13.520	.00020		14.735	.00005		16.035	.00001	
12.345	.00056		13.535	.00019		14.765	.00005		16.055	.00001	
12.365	.00056		13.545	.00019		14.780	.00005		16.080	.00001	
12.380	.00055		13.565	.00018		14.820	.00005		16.085	.00001	
12.395	.00054		13.580	.00018		14.855	.00005		16.145	.00001	
12.435	.00053		13.595	.00017		14.865	.00005		16.205	.00001	
12.465	.00052		13.605	.00017		14.885	.00005		16.220	.00001	
12.480	.00051		13.625	.00017		14.895	.00004		16.245	.00001	
12.500	.00050		13.655	.00017		14.915	.00004		16.260	.00001	
12.515	.00050		13.680	.00016		14.945	.00004		16.265	.00001	
12.545	.00049		13.715	.00016		14.955	.00004		16.305	.00001	
12.555	.00048		13.740	.00016		14.985	.00004		16.340	.00001	
12.560	.00047		13.745	.00015		15.005	.00004		16.380	.00001	
12.605	.00046		13.760	.00015		15.020	.00004		16.415	.00000	
12.615	.00046		13.785	.00015		15.035	.00004		16.485	.00000	
12.620	.00045		13.815	.00014		15.095	.00003		16.535	.00000	
12.635	.00045		13.820	.00014		15.120	.00003		16.565	.00000	
12.660	.00043		13.835	.00014		15.125	.00003		16.595	.00000	
12.695	.00042		13.875	.00014		15.135	.00003		16.620	.00000	
12.705	.00042		13.895	.00014		15.140	.00003		16.625	.00000	
12.735	.00041		13.905	.00013		15.155	.00003		16.640	.00000	
12.740	.00040		13.955	.00013		15.165	.00003		16.715	.00000	
12.755	.00039		13.965	.00013		15.185	.00003		16.785	.00000	
12.785	.00038		13.985	.00012		15.245	.00003		16.805	.00000	
12.795	.00037		14.000	.00012		15.260	.00003		16.820	.00000	
12.845	.00037		14.015	.00012		15.305	.00003		16.835	.00000	
12.860	.00036		14.045	.00011		15.315	.00003		16.880	.00000	
12.875	.00035		14.055	.00011		15.335	.00003		16.955	.00000	
12.885	.00035		14.060	.00011		15.360	.00003		16.980	.00000	
12.935	.00034		14.085	.00011		15.365	.00003		16.985	.00000	
12.965	.00033		14.105	.00011		15.380	.00002		17.060	.00000	
13.005	.00033		14.165	.00010		15.395	.00002		17.115	.00000	
13.020	.00032		14.180	.00010		15.405	.00002		17.145	.00000	
13.040	.00031		14.220	.00009		15.435	.00002		17.165	.00000	
13.055	.00031		14.235	.00009		15.440	.00002		17.195	.00000	
13.065	.00030		14.255	.00009		15.485	.00002		17.205	.00000	
13.085	.00029		14.285	.00009		15.495	.00002		17.295	.00000	
13.095	.00029		14.315	.00009		15.500	.00002		17.360	.00000	
13.115	.00028		14.345	.00008		15.540	.00002		17.405	.00000	
13.140	.00027		14.405	.00008		15.545	.00002		17.415	.00000	
13.155	.00027		14.475	.00008		15.585	.00002		17.420	.00000	
13.205	.00027		14.420	.00008		15.605	.00002		17.465	.00000	
13.220	.00026		14.435	.00007		15.665	.00002		17.540	.00000	
13.235	.00025		14.460	.00007		15.680	.00001		17.565	.00000	
13.245	.00025		14.480	.00007		15.695	.00001		17.645	.00000	
13.265	.00025		14.495	.00007		15.705	.00001		17.705	.00000	
13.295	.00024		14.505	.00007		15.740	.00001		17.735	.00000	
13.335	.00023		14.540	.00007		15.765	.00001		17.780	.00000	
13.355	.00023		14.580	.00006		15.795	.00001		17.795	.00000	
13.380	.00022		14.585	.00006		15.815	.00001		17.885	.00000	
13.385	.00022		14.595	.00006		15.855	.00001		18.000	.00000	
13.415	.00022		14.615	.00006		15.860	.00001		18.005	.00000	
13.445	.00021		14.625	.00006		15.920	.00001		18.015	.00000	

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h				h				h				h			
P(H≥h)				P(H≥h)				P(H≥h)				P(H≥h)			
3	3	3	2	3	3	3	2	3	3	3	3	4	2	2	2
6.439	.05974			8.727	.00221			9.513	.00084			6.409	.05556		
6.485	.05922			8.803	.00182			9.564	.00071			6.436	.05238		
6.545	.05857			8.924	.00104			9.667	.00065			6.545	.04921		
6.561	.05740			9.030	.00065			9.974	.00026			6.627	.04667		
6.606	.05688			9.405	.00026			10.385	.00006			6.655	.04095		
6.621	.05338											6.736	.03714		
6.682	.05078											6.764	.03460		
6.727	.04948											6.845	.03333		
6.742	.04883			5.974	.10273			4.929	.11429			6.873	.03270		
6.788	.04506			6.026	.09779							6.982	.02889		
6.803	.04312			6.077	.09649			4	2	1	1	7.064	.02222		
6.848	.04260			6.179	.09182							7.091	.01714		
6.864	.04221			6.231	.08773			5.208	.11429			7.282	.01651		
6.909	.04039			6.282	.08500			5.250	.09048			7.309	.01397		
6.924	.03987			6.385	.07883			5.417	.07619			7.391	.00889		
6.970	.03935			6.436	.07455			5.458	.07143			7.527	.00762		
6.985	.03818			6.487	.06935			5.833	.04286			7.718	.00698		
7.030	.03584			6.590	.06805			6.083	.02857			7.855	.00508		
7.045	.03468			6.641	.06169							7.964	.00317		
7.091	.03455			6.692	.05987			4	2	2	1	8.291	.00127		
7.106	.03312			6.795	.05364										
7.152	.02974			6.846	.05149			5.500	.10317			4	3	1	1
7.212	.02961			6.897	.05019			5.533	.09788			4.978	.10635		
7.227	.02935			7.000	.04351			5.600	.09577			5.067	.09524		
7.273	.02818			7.051	.04182			5.633	.08624			5.111	.09365		
7.288	.02792			7.103	.03935			5.700	.08519			5.144	.09206		
7.333	.02766			7.205	.03825			5.733	.06825			5.200	.08889		
7.348	.02753			7.256	.03331			5.800	.06720			5.411	.08730		
7.409	.02649			7.308	.03279			5.933	.06085			5.467	.08413		
7.455	.02610			7.410	.02994			5.967	.05873			5.511	.08254		
7.470	.02584			7.462	.02929			6.000	.05661			5.644	.06984		
7.515	.02390			7.513	.02838			6.133	.04180			5.678	.06667		
7.530	.02195			7.615	.02571			6.167	.03968			5.767	.06349		
7.576	.02169			7.667	.02338			6.200	.03545			5.867	.05714		
7.591	.02013			7.718	.02104			6.300	.03333			6.000	.05397		
7.636	.01831			7.821	.02052			6.467	.02910			6.044	.05238		
7.652	.01740			7.872	.01844			6.500	.02698			6.178	.04921		
7.697	.01662			7.923	.01792			6.533	.02063			6.211	.04603		
7.712	.01649			8.026	.01662			6.667	.01905			6.267	.03492		
7.758	.01416			8.077	.01649			6.700	.01587			6.400	.03333		
7.818	.01364			8.128	.01519			6.800	.01270			6.567	.02857		
7.833	.01286			8.231	.01370			7.000	.00952			6.711	.01905		
7.879	.01260			8.282	.01214			7.200	.00635			7.067	.00952		
7.939	.01208			8.333	.01175										
7.955	.01117			8.436	.01084			4	2	2	2	4	3	2	1
8.015	.00961			8.538	.00838										
8.061	.00948			8.641	.00779			5.673	.10190			5.573	.10032		
8.076	.00870			8.692	.00688			5.755	.09302			5.591	.09857		
8.182	.00818			8.744	.00636			5.782	.08222			5.600	.09746		
8.197	.00766			8.897	.00442			5.891	.08095			5.618	.09508		
8.242	.00597			8.949	.00390			5.973	.07905			5.645	.09476		
8.318	.00545			9.051	.00325			6.082	.07143			5.655	.09444		
8.379	.00377			9.154	.00279			6.109	.07016			5.709	.09333		
8.485	.00364			9.256	.00227			6.191	.06698			5.727	.09175		
8.545	.00338			9.359	.00201			6.218	.06254			5.736	.08794		
8.561	.00312			9.462	.00143			6.327	.06000						

h				h				h				h			
P(H ₂ h)				P(H ₂ h)				P(H ₂ h)				P(H ₂ h)			
4	3	2	1	4	3	2	1	4	3	2	2	4	3	2	2
5.764	.08651			7.291	.01333			6.295	.06364			7.098	.03224		
5.791	.08635			7.318	.01302			6.326	.06335			7.121	.03154		
5.809	.08302			7.336	.01143			6.348	.06317			7.144	.03120		
5.864	.08095			7.364	.01111			6.366	.06271			7.159	.03056		
5.873	.07984			7.455	.00984			6.371	.06208			7.167	.02981		
5.891	.07952			7.482	.00762			6.386	.06104			7.205	.02918		
5.955	.07429			7.609	.00667			6.394	.06087			7.212	.02906		
5.982	.06762			7.636	.00571			6.409	.05977			7.227	.02773		
6.000	.06556			7.727	.00524			6.417	.05861			7.235	.02704		
6.009	.06460			7.773	.00429			6.432	.05804			7.258	.02681		
6.027	.06413			7.891	.00333			6.439	.05758			7.280	.02646		
6.036	.06349			8.018	.00238			6.477	.05723			7.303	.02595		
6.055	.06206			8.182	.00190			6.485	.05711			7.318	.02508		
6.082	.06175							6.500	.05550			7.326	.02496		
6.091	.06143			4	3	2	2	6.508	.05515			7.341	.02485		
6.145	.06016							6.530	.05423			7.348	.02439		
6.164	.05540			5.712	.10118			6.545	.05411			7.364	.02427		
6.173	.05524			5.750	.09980			6.553	.05354			7.417	.02332		
6.200	.05397			5.758	.09922			6.568	.05267			7.439	.02228		
6.227	.05381			5.773	.09749			6.576	.05244			7.455	.02193		
6.245	.05238			5.780	.09680			6.591	.05232			7.462	.02165		
6.273	.05175			5.803	.09622			6.598	.05186			7.477	.02159		
6.300	.05111			5.818	.09582			6.614	.05152			7.485	.02113		
6.309	.04937			5.826	.09573			6.621	.04949			7.500	.02084		
6.327	.04873			5.848	.09319			6.636	.04869			7.508	.02026		
6.382	.04841			5.864	.09290			6.659	.04834			7.523	.02014		
6.391	.04762			5.871	.09227			6.667	.04811			7.530	.01991		
6.418	.04619			5.886	.09152			6.682	.04776			7.545	.01962		
6.436	.04603			5.894	.09123			6.689	.04736			7.568	.01939		
6.445	.04540			5.909	.09053			6.712	.04713			7.576	.01859		
6.464	.04476			5.932	.09019			6.727	.04603			7.598	.01685		
6.473	.04032			5.939	.08955			6.735	.04569			7.621	.01645		
6.491	.03921			5.955	.08903			6.750	.04442			7.636	.01616		
6.527	.03889			5.962	.08863			6.758	.04297			7.644	.01582		
6.582	.03857			5.985	.08724			6.780	.04216			7.682	.01460		
6.609	.03667			6.000	.08649			6.795	.04193			7.705	.01426		
6.636	.03587			6.008	.08372			6.803	.04176			7.712	.01397		
6.664	.03556			6.023	.08176			6.818	.04153			7.727	.01374		
6.682	.03381			6.030	.08147			6.848	.04107			7.773	.01345		
6.709	.03286			6.053	.07934			6.864	.04049			7.780	.01299		
6.745	.03222			6.068	.07882			6.871	.04032			7.803	.01276		
6.764	.03159			6.076	.07726			6.894	.03945			7.818	.01229		
6.818	.03127			6.091	.07685			6.909	.03934			7.826	.01212		
6.827	.03063			6.114	.07657			6.917	.03928			7.841	.01201		
6.855	.03032			6.121	.07633			6.932	.03789			7.848	.01126		
6.873	.02968			6.136	.07478			6.955	.03766			7.871	.00999		
6.909	.02730			6.144	.07385			6.962	.03720			7.886	.00952		
6.955	.02317			6.167	.07229			6.977	.03709			7.894	.00918		
7.018	.02000			6.182	.07079			6.985	.03662			7.939	.00905		
7.036	.01873			6.189	.07045			7.000	.03616			7.962	.00860		
7.045	.01841			6.205	.06952			7.023	.03512			8.000	.00831		
7.073	.01651			6.227	.06756			7.030	.03501			8.008	.00820		
7.118	.01619			6.235	.06722			7.045	.03495			8.030	.00808		
7.145	.01587			6.250	.06693			7.053	.03483			8.045	.00797		
7.182	.01556			6.258	.06566			7.076	.03391			8.076	.00773		
7.200	.01524			6.273	.06433			7.091	.03333			8.114	.00727		

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h				h				h				h			
P(H ≥ h)				P(H ≥ h)				P(H ≥ h)				P(H ≥ h)			
4	3	2	2	4	3	2	1	4	3	3	1	4	3	3	2
8.167	.00704			6.485	.05290			8.212	.00420			6.436	.06632		
8.182	.00670			6.515	.05273			8.235	.00403			6.462	.06584		
8.189	.00618			6.535	.05152			8.242	.00385			6.474	.06488		
8.212	.00571			6.565	.04952			8.295	.00377			6.487	.06426		
8.250	.00525			6.594	.04944			8.333	.00359			6.494	.06358		
8.273	.00433			6.606	.04857			8.356	.00240			6.532	.06244		
8.326	.00427			6.659	.04814			8.394	.00238			6.545	.06201		
8.348	.00404			6.667	.04701			8.548	.00221			6.577	.06098		
8.417	.00392			6.697	.04398			8.697	.00169			6.583	.06027		
8.432	.00358			6.720	.04390			8.727	.00143			6.590	.05925		
8.455	.00346			6.727	.04294			8.841	.00130			6.603	.05889		
8.530	.00271			6.758	.04268			8.939	.00104			6.635	.05818		
8.591	.00260			6.780	.04000			9.182	.00052			6.641	.05709		
8.667	.00225			6.788	.03879							6.647	.05700		
8.689	.00156			6.848	.03870			4	3	3	2	6.667	.05638		
8.795	.00139			6.879	.03853							6.679	.05592		
8.894	.00104			6.902	.03784			5.859	.10025			6.686	.05447		
8.909	.00069			6.939	.03766			5.872	.09929			6.692	.05400		
9.000	.00052			6.962	.03749			5.878	.09872			6.699	.05391		
9.273	.00035			6.970	.03688			5.885	.09681			6.705	.05286		
				7.000	.03680			5.917	.09554			6.737	.05183		
				7.023	.03567			5.929	.09453			6.744	.05157		
				7.030	.03532			5.968	.09310			6.750	.05123		
				7.061	.03325			5.974	.09235			6.782	.05014		
5.667	.10043			7.083	.03307			5.987	.09203			6.795	.04925		
5.689	.09602			7.121	.03030			6.000	.09089			6.801	.04880		
5.697	.09541			7.144	.02978			6.026	.09045			6.808	.04824		
5.758	.09212			7.152	.02848			6.032	.08993			6.821	.04714		
5.788	.09152			7.205	.02805			6.051	.08895			6.840	.04678		
5.811	.08996			7.212	.02771			6.064	.08815			6.853	.04615		
5.871	.08580			7.242	.02753			6.071	.08778			6.872	.04558		
5.909	.08329			7.265	.02537			6.083	.08670			6.891	.04485		
5.932	.08268			7.273	.02511			6.096	.08615			6.947	.04414		
5.939	.08251			7.326	.02329			6.122	.08462			6.910	.04387		
5.970	.08139			7.333	.02052			6.128	.08369			6.949	.04290		
5.992	.08069			7.424	.02048			6.167	.08359			6.955	.04257		
6.000	.07939			7.447	.02030			6.173	.08190			6.987	.04219		
6.030	.07922			7.485	.01987			6.179	.08154			6.994	.04130		
6.053	.07801			7.508	.01658			6.186	.08121			7.006	.04095		
6.061	.07593			7.515	.01528			6.205	.08013			7.013	.04030		
6.114	.07333			7.545	.01458			6.224	.07941			7.026	.03994		
6.121	.07117			7.576	.01450			6.231	.07877			7.045	.03962		
6.152	.07056			7.606	.01442			6.237	.07825			7.051	.03893		
6.174	.06892			7.629	.01433			6.256	.07667			7.090	.03880		
6.182	.06745			7.636	.01329			6.276	.07602			7.096	.03851		
6.212	.06693			7.667	.01286			6.282	.07550			7.103	.03794		
6.235	.06641			7.689	.01234			6.288	.07488			7.109	.03776		
6.242	.06424			7.750	.01190			6.295	.07407			7.147	.03726		
6.273	.06407			7.758	.00974			6.333	.07257			7.154	.03698		
6.303	.06338			7.848	.00922			6.340	.07218			7.160	.03664		
6.333	.06095			7.879	.00905			6.372	.07154			7.199	.03597		
6.356	.06087			7.970	.00818			6.378	.07061			7.205	.03525		
6.394	.06043			7.992	.00688			6.391	.07001			7.212	.03508		
6.417	.05965			8.053	.00654			6.397	.06880			7.218	.03468		
6.424	.05567			8.091	.00619			6.410	.06789			7.256	.03405		
6.455	.05377			8.121	.00541			6.429	.06711			7.263	.03372		
6.477	.05342														

h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
4	3	3	2	4	3	3	2	4	3	3	2	4	3	3	3
7.282		.03319		8.083		.01471		8.955		.00292		6.324		.08131	
7.295		.03297		8.103		.01461		8.994		.00286		6.330		.08032	
7.301		.03192		8.122		.01445		9.006		.00281		6.352		.08009	
7.314		.03165		8.128		.01398		9.045		.00272		6.368		.07932	
7.321		.03120		8.135		.01395		9.051		.00269		6.374		.07908	
7.353		.03055		8.141		.01372		9.058		.00258		6.412		.07790	
7.359		.02991		8.179		.01310		9.103		.00276		6.418		.07709	
7.397		.02977		8.186		.01308		9.128		.00223		6.440		.07684	
7.410		.02944		8.218		.01234		9.141		.00214		6.456		.07558	
7.417		.02931		8.224		.01185		9.147		.00209		6.462		.07408	
7.436		.02863		8.237		.01181		9.160		.00203		6.484		.07346	
7.455		.02823		8.244		.01158		9.167		.00197		6.500		.07300	
7.468		.02804		8.256		.01146		9.199		.00191		6.505		.07121	
7.487		.02732		8.276		.01109		9.244		.00183		6.527		.07087	
7.500		.02674		8.282		.01090		9.263		.00162		6.544		.06963	
7.506		.02599		8.308		.01084		9.282		.00151		6.549		.06890	
7.513		.02566		8.321		.01061		9.314		.00148		6.588		.06781	
7.526		.02541		8.333		.00985		9.333		.00145		6.615		.06682	
7.558		.02504		8.340		.00968		9.346		.00142		6.632		.06625	
7.564		.02494		8.378		.00965		9.372		.00123		6.637		.06560	
7.571		.02475		8.391		.00918		9.404		.00105		6.659		.06400	
7.603		.02447		8.423		.00913		9.455		.00094		6.676		.06367	
7.609		.02375		8.429		.00895		9.468		.00085		6.703		.06231	
7.615		.02356		8.449		.00881		9.487		.00082		6.720		.06119	
7.622		.02335		8.481		.00855		9.551		.00079		6.725		.05948	
7.628		.02290		8.487		.00820		9.577		.00069		6.764		.05892	
7.641		.02255		8.494		.00812		9.697		.00061		6.769		.05867	
7.660		.02203		8.513		.00797		9.756		.00052		6.791		.05820	
7.667		.02173		8.526		.00770		9.776		.00035		6.808		.05756	
7.673		.02170		8.532		.00744		9.859		.00026		6.813		.05693	
7.705		.02098		8.538		.00740		9.865		.00022		6.835		.05599	
7.718		.02035		8.545		.00722		9.949		.00017		6.852		.05568	
7.724		.02025		8.551		.00676		10.269		.00009		6.857		.05372	
7.731		.02013		8.583		.00656						6.879		.05317	
7.763		.01999		8.596		.00649						6.896		.05243	
7.776		.01986		8.628		.00646						6.901		.05176	
7.814		.01962		8.641		.00626		6.000		.10009		6.940		.05107	
7.821		.01958		8.647		.00624		6.016		.09779		6.945		.05044	
7.833		.01949		8.654		.00621		6.022		.09675		6.967		.05025	
7.846		.01896		8.667		.00574		6.060		.09640		6.984		.04897	
7.872		.01861		8.686		.00563		6.066		.09367		6.989		.04802	
7.878		.01853		8.699		.00549		6.083		.09349		7.011		.04747	
7.897		.01830		8.718		.00500		6.104		.09283		7.027		.04727	
7.910		.01789		8.737		.00477		6.110		.09259		7.033		.04683	
7.917		.01752		8.756		.00458		6.132		.09134		7.055		.04676	
7.929		.01736		8.795		.00452		6.148		.09094		7.071		.04646	
7.936		.01688		8.801		.00435		6.154		.09047		7.077		.04645	
7.968		.01661		8.833		.00429		6.176		.09011		7.115		.04382	
7.974		.01641		8.840		.00386		6.192		.08900		7.121		.04320	
8.013		.01626		8.853		.00377		6.198		.08714		7.143		.04292	
8.019		.01597		8.859		.00372		6.236		.08608		7.159		.04209	
8.026		.01569		8.872		.00331		6.242		.08560		7.165		.04109	
8.032		.01551		8.891		.00323		6.264		.08520		7.187		.04062	
8.051		.01516		8.936		.00317		6.280		.08464		7.203		.04032	
8.071		.01500		8.942		.00308		6.286		.08327		7.209		.03992	
8.077		.01490		8.949		.00298		6.308		.08217		7.231		.03960	

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
4	3	3	3	4	3	3	3	4	3	3	3	4	4	1	1
7.247	.03917	8.258	.01554	9.231	.00501	5.127	.10349								
7.253	.03874	8.264	.01517	9.253	.00499	5.182	.09968								
7.291	.03833	8.286	.01509	9.269	.00475	5.209	.09587								
7.319	.03739	8.302	.01412	9.275	.00454	5.291	.08698								
7.335	.03664	8.308	.01384	9.297	.00425	5.345	.07746								
7.341	.03628	8.346	.01346	9.313	.00418	5.427	.07619								
7.363	.03600	8.352	.01336	9.319	.00398	5.564	.07492								
7.379	.03576	8.374	.01328	9.341	.00395	5.618	.07365								
7.407	.03488	8.390	.01320	9.357	.00374	5.645	.06857								
7.423	.03434	8.396	.01300	9.363	.00336	5.755	.06603								
7.429	.03406	8.418	.01274	9.401	.00332	5.782	.06476								
7.467	.03246	8.434	.01249	9.429	.00329	5.864	.05714								
7.495	.03201	8.462	.01228	9.445	.00305	5.945	.04952								
7.511	.03157	8.478	.01200	9.451	.00286	5.973	.04762								
7.516	.03049	8.484	.01171	9.473	.00278	6.000	.04635								
7.538	.02973	8.522	.01159	9.489	.00276	6.055	.04381								
7.555	.02943	8.527	.01151	9.516	.00270	6.164	.04254								
7.560	.02900	8.549	.01145	9.533	.00262	6.382	.04190								
7.582	.02886	8.566	.01117	9.538	.00260	6.436	.03810								
7.599	.02853	8.571	.01093	9.577	.00255	6.518	.03556								
7.604	.02816	8.593	.01072	9.604	.00245	6.600	.03302								
7.643	.02805	8.610	.01064	9.621	.00233	6.627	.03175								
7.670	.02707	8.615	.01048	9.626	.00219	6.818	.02921								
7.687	.02691	8.637	.01039	9.670	.00207	6.845	.02857								
7.692	.02678	8.654	.01009	9.692	.00205	6.927	.02603								
7.714	.02599	8.659	.00990	9.709	.00195	6.955	.02349								
7.731	.02569	8.698	.00975	9.714	.00193	7.036	.02095								
7.736	.02533	8.725	.00934	9.753	.00169	7.091	.01968								
7.758	.02522	8.742	.00902	9.797	.00161	7.364	.01524								
7.775	.02437	8.747	.00898	9.824	.00155	7.500	.01143								
7.780	.02361	8.769	.00879	9.868	.00153	7.909	.00381								
7.819	.02349	8.786	.00876	9.885	.00144										
7.824	.02282	8.791	.00863	9.890	.00138	4	4	2	1						
7.846	.02269	8.813	.00857	9.929	.00123										
7.863	.02232	8.830	.00837	9.973	.00107	5.545	.10026								
7.868	.02191	8.835	.00794	10.000	.00101	5.568	.09980								
7.890	.02161	8.874	.00790	10.016	.00096	5.591	.09703								
7.907	.02139	8.879	.00774	10.044	.00092	5.614	.09633								
7.912	.02122	8.901	.00770	10.060	.00080	5.636	.09576								
7.934	.02108	8.918	.00757	10.066	.00073	5.659	.09091								
7.951	.02087	8.923	.00747	10.148	.00069	5.682	.09056								
7.956	.02043	8.945	.00743	10.154	.00065	5.705	.08733								
7.995	.01985	8.962	.00727	10.220	.00061	5.727	.08433								
8.022	.01973	8.967	.00711	10.236	.00057	5.773	.08364								
8.038	.01922	9.011	.00707	10.396	.00044	5.795	.08317								
8.044	.01853	9.049	.00668	10.456	.00034	5.818	.08294								
8.082	.01822	9.077	.00626	10.484	.00032	5.841	.08225								
8.110	.01794	9.093	.00602	10.500	.00023	5.864	.07867								
8.126	.01771	9.099	.00591	10.505	.00021	5.886	.07775								
8.132	.01747	9.121	.00576	10.527	.00015	5.909	.07694								
8.170	.01735	9.137	.00572	10.659	.00014	5.932	.07648								
8.176	.01699	9.143	.00548	10.852	.00008	5.955	.07544								
8.198	.01689	9.165	.00544	10.923	.00005	5.977	.07475								
8.214	.01647	9.181	.00516	11.275	.00002	6.000	.07198								
8.220	.01594	9.187	.00514			6.023	.07152								
8.242	.01573	9.225	.00504			6.045	.07117								

h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
4	4	2	1	4	4	2	1	4	4	2	2	4	4	2	2
6.068	.06805	7.523	.01709	6.442	.06082	7.981	.01445								
6.114	.06690	7.545	.01697	6.500	.06020	8.000	.01406								
6.136	.06609	7.568	.01651	6.519	.05884	8.038	.01364								
6.159	.06390	7.591	.01582	6.577	.05684	8.058	.01328								
6.182	.06343	7.614	.01535	6.596	.05595	8.077	.01312								
6.205	.05732	7.636	.01374	6.615	.05437	8.115	.01254								
6.227	.05628	7.682	.01351	6.654	.05376	8.135	.01247								
6.295	.05582	7.773	.01253	6.672	.05360	8.154	.01162								
6.318	.05478	7.795	.01137	6.692	.05191	8.192	.01154								
6.341	.05143	7.818	.01091	6.731	.04872	8.212	.01139								
6.364	.05004	7.841	.01068	6.750	.04825	8.231	.01101								
6.386	.04981	7.864	.01045	6.769	.04571	8.288	.01037								
6.409	.04947	7.886	.01022	6.808	.04487	8.308	.01018								
6.432	.04704	7.909	.00906	6.827	.04412	8.346	.00941								
6.455	.04635	7.955	.00833	6.846	.04342	8.365	.00922								
6.477	.04612	7.977	.00779	6.885	.04333	8.423	.00829								
6.523	.04519	8.000	.00756	6.904	.04287	8.462	.00779								
6.545	.04392	8.023	.00745	6.923	.04229	8.500	.00768								
6.568	.04121	8.091	.00583	6.962	.04186	8.519	.00745								
6.591	.04075	8.114	.00560	6.981	.04033	8.538	.00706								
6.614	.04017	8.182	.00537	7.000	.03810	8.596	.00660								
6.636	.03971	8.227	.00514	7.038	.03779	8.615	.00564								
6.659	.03925	8.341	.00317	7.058	.03721	8.654	.00548								
6.682	.03740	8.364	.00294	7.077	.03636	8.673	.00514								
6.705	.03729	8.568	.00260	7.115	.03575	8.692	.00494								
6.727	.03706	8.591	.00190	7.135	.03556	8.769	.00477								
6.773	.03521	8.705	.00156	7.192	.03502	8.808	.00416								
6.795	.03394	8.909	.00087	7.212	.03477	8.827	.00400								
6.818	.03244	9.045	.00069	7.231	.03269	8.846	.00354								
6.841	.03221			7.269	.03242	8.885	.00331								
6.864	.03209	4 4 2 2		7.288	.03119	8.904	.00300								
6.886	.03036	5.769	.10195	7.308	.03069	8.962	.00292								
6.909	.02990	5.808	.09882	7.346	.02980	8.981	.00291								
6.932	.02967	5.827	.09812	7.365	.02949	9.059	.00275								
6.977	.02955	5.846	.09131	7.385	.02911	9.077	.00244								
7.000	.02909	5.885	.09054	7.423	.02857	9.135	.00225								
7.023	.02874	5.904	.08910	7.442	.02807	9.231	.00217								
7.045	.02863	5.962	.08760	7.462	.02584	9.269	.00183								
7.068	.02840	5.981	.08733	7.500	.02542	9.288	.00175								
7.091	.02771	6.000	.08637	7.519	.02503	9.308	.00121								
7.114	.02701	6.038	.08217	7.538	.02453	9.346	.00117								
7.136	.02609	6.058	.08152	7.577	.02376	9.442	.00106								
7.159	.02459	6.077	.07767	7.596	.02349	9.462	.00098								
7.182	.02424	6.115	.07617	7.615	.02295	9.577	.00052								
7.205	.02413	6.135	.07521	7.654	.02161	9.750	.00046								
7.227	.02297	6.192	.07405	7.673	.02138	9.846	.00023								
7.273	.02251	6.212	.07302	7.692	.02095	9.923	.00017								
7.295	.02078	6.231	.07136	7.731	.02053	10.154	.00012								
7.318	.02043	6.269	.07038	7.750	.01901										
7.341	.02020	6.288	.06990	7.809	.01801	4 4 3 1									
7.364	.01974	6.308	.06686	7.827	.01778	5.660	.10020								
7.409	.01952	6.346	.06597	7.846	.01709	5.692	.09853								
7.432	.01951	6.365	.06293	7.885	.01587	5.712	.09625								
7.455	.01905	6.385	.06263	7.904	.01572	5.718	.09550								
7.477	.01789	6.423	.06101	7.923	.01499	5.737	.09509								
7.500	.01743			7.962	.01460										

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
4	4	3	1	4	4	3	1	4	4	3	1	4	4	3	2
5.756	.09411	6.987	.03850	8.231	.00955	5.956	.09514								
5.769	.09169	7.019	.03804	8.250	.00877	5.967	.09477								
5.795	.09091	7.026	.03671	8.256	.00866	5.973	.09460								
5.808	.08848	7.038	.03596	8.276	.00837	5.984	.09421								
5.814	.08768	7.045	.03584	8.353	.00834	5.989	.09302								
5.865	.08592	7.096	.03469	8.372	.00776	6.005	.09262								
5.891	.08392	7.122	.03351	8.404	.00759	6.016	.09214								
5.910	.08245	7.141	.03333	8.429	.00747	6.022	.09205								
5.923	.08144	7.192	.03255	8.462	.00733	6.033	.09043								
5.942	.08078	7.199	.03160	8.481	.00661	6.038	.09020								
5.968	.08035	7.250	.03131	8.506	.00638	6.049	.08940								
6.000	.07928	7.256	.03068	8.526	.00554	6.055	.08912								
6.026	.07899	7.276	.02999	8.564	.00537	6.066	.08871								
6.045	.07827	7.295	.02918	8.577	.00534	6.082	.08849								
6.064	.07694	7.327	.02877	8.583	.00470	6.098	.08820								
6.096	.07556	7.333	.02848	8.635	.00459	6.099	.08801								
6.103	.07518	7.353	.02785	8.641	.00444	6.104	.08735								
6.115	.07319	7.410	.02745	8.660	.00361	6.115	.08685								
6.122	.07296	7.429	.02675	8.679	.00352	6.121	.08664								
6.173	.07212	7.449	.02635	8.692	.00349	6.132	.08615								
6.179	.07128	7.481	.02548	8.712	.00346	6.137	.08597								
6.199	.07004	7.500	.02462	8.769	.00341	6.148	.08493								
6.218	.06843	7.506	.02439	8.795	.00335	6.154	.08476								
6.231	.06681	7.538	.02424	8.814	.00312	6.165	.08371								
6.269	.06644	7.558	.02358	8.865	.00300	6.170	.08357								
6.276	.06496	7.564	.02326	8.872	.00248	6.181	.08309								
6.327	.06436	7.583	.02271	8.891	.00231	6.187	.08280								
6.333	.06280	7.603	.02202	8.968	.00208	6.198	.08154								
6.353	.06219	7.615	.02199	9.000	.00202	6.203	.08139								
6.372	.06173	7.641	.02121	9.038	.00185	6.214	.08027								
6.385	.06101	7.654	.02052	9.096	.00176	6.220	.08015								
6.404	.06014	7.660	.01954	9.122	.00170	6.231	.08000								
6.410	.05957	7.712	.01893	9.173	.00165	6.236	.07938								
6.429	.05769	7.737	.01861	9.179	.00159	6.247	.07866								
6.506	.05665	7.756	.01804	9.199	.00118	6.253	.07849								
6.526	.05582	7.769	.01740	9.256	.00113	6.264	.07814								
6.558	.05463	7.788	.01665	9.276	.00107	6.269	.07804								
6.577	.05255	7.814	.01625	9.295	.00101	6.280	.07673								
6.583	.05201	7.846	.01602	9.327	.00084	6.286	.07614								
6.615	.05094	7.872	.01593	9.500	.00078	6.297	.07607								
6.635	.04978	7.891	.01590	9.583	.00069	6.302	.07599								
6.641	.04949	7.910	.01567	9.692	.00052	6.313	.07565								
6.660	.04898	7.942	.01541	9.788	.00043	6.319	.07512								
6.679	.04877	7.949	.01483	9.872	.00026	6.330	.07450								
6.718	.04724	7.962	.01414	10.077	.00017	6.335	.07350								
6.731	.04652	7.968	.01359			6.346	.07326								
6.737	.04557	8.026	.01339			6.352	.07310								
6.788	.04494	8.045	.01253			6.363	.07278								
6.795	.04401	8.064	.01224	5.890	.10070	6.368	.07258								
6.814	.04361	8.077	.01209	5.901	.09950	6.379	.07213								
6.833	.04228	8.115	.01186	5.907	.09932	6.385	.07142								
6.846	.04196	8.122	.01177	5.918	.09835	6.401	.07087								
6.891	.04156	8.173	.01131	5.923	.09808	6.412	.07016								
6.923	.04029	8.179	.01056	5.934	.09684	6.418	.07008								
6.949	.03945	8.199	.01051	5.940	.09566	6.429	.06974								
6.968	.03896	8.218	.01027	5.951	.09523	6.434	.06965								

h				h				h				h			
P(H≥h)				P(H≥h)				P(H≥h)				P(H≥h)			
4	4	3	2	4	4	3	2	4	4	3	2	4	4	3	2
6.445	.06897			6.923	.04812			7.407	.03295			7.918	.02060		
6.451	.06880			6.940	.04801			7.418	.03291			7.934	.02045		
6.462	.06737			6.945	.04783			7.423	.03224			7.945	.02025		
6.467	.06696			6.956	.04690			7.434	.03191			7.951	.01998		
6.478	.06625			6.962	.04672			7.440	.03187			7.962	.01982		
6.484	.06587			6.973	.04641			7.456	.03176			7.967	.01955		
6.495	.06568			6.978	.04616			7.467	.03160			7.984	.01944		
6.500	.06557			6.989	.04563			7.473	.03109			8.011	.01928		
6.511	.06550			6.995	.04542			7.484	.03069			8.016	.01910		
6.516	.06530			7.005	.04510			7.489	.03062			8.027	.01887		
6.527	.06494			7.011	.04496			7.505	.03050			8.033	.01879		
6.533	.06478			7.022	.04461			7.516	.02967			8.044	.01845		
6.544	.06445			7.027	.04422			7.522	.02938			8.049	.01828		
6.549	.06411			7.038	.04388			7.533	.02911			8.060	.01795		
6.560	.06343			7.044	.04373			7.538	.02891			8.066	.01769		
6.566	.06311			7.055	.04349			7.549	.02878			8.077	.01765		
6.577	.06286			7.060	.04336			7.555	.02866			8.082	.01760		
6.582	.06260			7.077	.04295			7.566	.02852			8.093	.01740		
6.593	.06231			7.088	.04255			7.582	.02829			8.099	.01737		
6.599	.06214			7.093	.04240			7.588	.02821			8.110	.01721		
6.610	.06123			7.104	.04198			7.599	.02776			8.115	.01712		
6.615	.06116			7.110	.04190			7.604	.02773			8.126	.01689		
6.626	.06101			7.121	.04156			7.615	.02750			8.132	.01677		
6.632	.05996			7.126	.04094			7.621	.02727			8.148	.01654		
6.648	.05944			7.137	.04065			7.632	.02713			8.159	.01648		
6.659	.05896			7.143	.04048			7.637	.02708			8.165	.01625		
6.665	.05891			7.154	.04042			7.648	.02686			8.176	.01613		
6.676	.05858			7.159	.04014			7.654	.02677			8.181	.01608		
6.681	.05801			7.170	.03985			7.665	.02671			8.192	.01594		
6.692	.05698			7.176	.03936			7.670	.02641			8.198	.01582		
6.698	.05680			7.187	.03904			7.681	.02636			8.209	.01568		
6.709	.05627			7.192	.03899			7.687	.02624			8.225	.01518		
6.714	.05609			7.203	.03848			7.698	.02592			8.231	.01514		
6.725	.05597			7.209	.03822			7.703	.02578			8.247	.01506		
6.731	.05522			7.220	.03792			7.714	.02561			8.258	.01491		
6.742	.05472			7.225	.03776			7.720	.02554			8.264	.01479		
6.747	.05460			7.236	.03757			7.736	.02535			8.275	.01438		
6.758	.05451			7.242	.03737			7.747	.02500			8.280	.01430		
6.764	.05444			7.253	.03683			7.753	.02493			8.291	.01423		
6.775	.05408			7.258	.03659			7.764	.02466			8.297	.01410		
6.780	.05372			7.269	.03619			7.769	.02438			8.308	.01387		
6.791	.05332			7.275	.03600			7.780	.02371			8.313	.01378		
6.797	.05312			7.291	.03592			7.797	.02360			8.324	.01364		
6.808	.05289			7.302	.03566			7.802	.02349			8.330	.01357		
6.813	.05269			7.308	.03554			7.813	.02343			8.341	.01340		
6.824	.05173			7.319	.03532			7.819	.02333			8.346	.01339		
6.830	.05156			7.324	.03514			7.830	.02314			8.363	.01328		
6.841	.05126			7.335	.03480			7.835	.02295			8.379	.01324		
6.846	.05100			7.341	.03477			7.846	.02267			8.390	.01292		
6.863	.05070			7.352	.03440			7.852	.02261			8.396	.01290		
6.874	.04983			7.357	.03434			7.863	.02212			8.407	.01273		
6.879	.04925			7.368	.03429			7.868	.02191			8.412	.01270		
6.890	.04913			7.374	.03386			7.885	.02144			8.423	.01254		
6.896	.04872			7.385	.03364			7.896	.02121			8.429	.01247		
6.907	.04840			7.390	.03330			7.901	.02116			8.440	.01245		
6.912	.04826			7.401	.03301			7.912	.02106			8.445	.01230		

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h				h				h				h			
P(H≥h)				P(H≥h)				P(H≥h)				P(H≥h)			
4	4	3	2	4	4	3	2	4	4	3	2	4	4	3	2
8.456	.01215			8.989	.00642			9.582	.00221			10.582	.00020		
8.473	.01186			9.000	.00638			9.593	.00218			10.681	.00015		
8.478	.01174			9.005	.00631			9.599	.00211			10.736	.00012		
8.489	.01165			9.016	.00626			9.610	.00201			10.753	.00009		
8.495	.01160			9.038	.00621			9.615	.00200			10.830	.00007		
8.505	.01151			9.049	.00605			9.626	.00188			10.901	.00004		
8.511	.01142			9.055	.00593			9.632	.00187			11.176	.00003		
8.522	.01120			9.066	.00587			9.648	.00186						
8.527	.01110			9.082	.00582			9.665	.00184			4	4	3	3
8.538	.01099			9.088	.00580			9.681	.00177						
8.544	.01095			9.099	.00554			9.692	.00174			6.005	.10028		
8.555	.01083			9.104	.00523			9.698	.00168			6.019	.09948		
8.560	.01071			9.115	.00512			9.709	.00167			6.024	.09897		
8.571	.01047			9.121	.00508			9.725	.00167			6.029	.09826		
8.577	.01043			9.132	.00507			9.731	.00166			6.043	.09803		
8.593	.01024			9.137	.00506			9.747	.00164			6.048	.09788		
8.604	.01014			9.148	.00503			9.758	.00163			6.062	.09736		
8.610	.01004			9.154	.00501			9.764	.00160			6.067	.09660		
8.621	.00999			9.165	.00476			9.775	.00158			6.081	.09613		
8.626	.00991			9.170	.00475			9.791	.00156			6.095	.09546		
8.637	.00974			9.181	.00464			9.813	.00142			6.105	.09488		
8.654	.00968			9.187	.00462			9.830	.00131			6.119	.09453		
8.659	.00955			9.198	.00457			9.841	.00119			6.124	.09387		
8.676	.00931			9.203	.00436			9.846	.00115			6.133	.09322		
8.687	.00913			9.220	.00417			9.879	.00111			6.138	.09156		
8.692	.00910			9.231	.00416			9.890	.00109			6.157	.09136		
8.703	.00906			9.236	.00415			9.896	.00103			6.171	.09105		
8.709	.00883			9.247	.00396			9.907	.00102			6.176	.09099		
8.720	.00880			9.253	.00389			9.912	.00101			6.181	.09032		
8.725	.00876			9.264	.00385			9.945	.00099			6.195	.09006		
8.736	.00874			9.269	.00382			9.962	.00088			6.200	.08956		
8.742	.00862			9.280	.00380			9.978	.00083			6.210	.08883		
8.753	.00856			9.302	.00379			9.995	.00081			6.214	.08839		
8.758	.00849			9.313	.00378			10.011	.00079			6.219	.08825		
8.769	.00832			9.319	.00375			10.022	.00076			6.233	.08807		
8.775	.00830			9.335	.00361			10.044	.00074			6.248	.08705		
8.791	.00816			9.346	.00355			10.060	.00072			6.252	.08649		
8.802	.00801			9.352	.00337			10.093	.00068			6.257	.08574		
8.808	.00788			9.363	.00314			10.104	.00067			6.276	.08568		
8.824	.00782			9.368	.00307			10.126	.00066			6.286	.08509		
8.835	.00758			9.379	.00301			10.137	.00065			6.290	.08487		
8.841	.00757			9.385	.00301			10.159	.00055			6.295	.08439		
8.852	.00747			9.396	.00300			10.176	.00052			6.310	.08398		
8.868	.00736			9.418	.00286			10.187	.00051			6.324	.08328		
8.874	.00728			9.434	.00283			10.225	.00050			6.329	.08268		
8.885	.00726			9.445	.00278			10.242	.00047			6.333	.08251		
8.890	.00724			9.451	.00267			10.253	.00045			6.348	.08162		
8.901	.00718			9.462	.00262			10.258	.00043			6.352	.08118		
8.907	.00713			9.467	.00260			10.286	.00042			6.362	.08070		
8.923	.00704			9.484	.00254			10.302	.00041			6.367	.08029		
8.934	.00671			9.495	.00245			10.374	.00040			6.371	.07880		
8.940	.00670			9.500	.00241			10.385	.00040			6.386	.07862		
8.951	.00665			9.516	.00240			10.407	.00036			6.405	.07850		
8.956	.00650			9.527	.00239			10.418	.00028			6.410	.07798		
8.967	.00646			9.544	.00235			10.434	.00027			6.424	.07775		
8.973	.00643			9.566	.00222			10.489	.00021			6.429	.07735		

h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
4	4	3	3	4	4	3	3	4	4	3	3	4	4	3	3
6.438	.07723	6.976	.05311	7.529	.03426	8.062	.02213								
6.448	.07651	6.981	.05236	7.543	.03415	8.076	.02172								
6.462	.07639	6.995	.05216	7.548	.03408	8.081	.02159								
6.476	.07576	7.010	.05200	7.552	.03381	8.086	.02145								
6.481	.07535	7.014	.05166	7.567	.03368	8.105	.02136								
6.500	.07465	7.019	.05122	7.571	.03313	8.119	.02096								
6.505	.07417	7.033	.05093	7.581	.03285	8.124	.02079								
6.514	.07361	7.038	.04990	7.586	.03261	8.138	.02069								
6.519	.07341	7.048	.04932	7.590	.03255	8.152	.02058								
6.524	.07299	7.052	.04884	7.605	.03238	8.162	.02032								
6.538	.07271	7.057	.04843	7.614	.03204	8.176	.02022								
6.552	.07214	7.090	.04824	7.624	.03172	8.181	.01999								
6.557	.07180	7.095	.04801	7.629	.03152	8.190	.01967								
6.562	.07175	7.110	.04793	7.648	.03144	8.195	.01953								
6.576	.07146	7.114	.04756	7.657	.03126	8.214	.01938								
6.581	.07103	7.124	.04740	7.662	.03098	8.233	.01922								
6.590	.07024	7.133	.04716	7.667	.03071	8.238	.01884								
6.595	.06995	7.148	.04642	7.681	.03052	8.252	.01872								
6.600	.06959	7.162	.04626	7.695	.03016	8.257	.01838								
6.629	.06942	7.167	.04580	7.700	.02997	8.267	.01824								
6.633	.06898	7.186	.04528	7.705	.02951	8.271	.01804								
6.638	.06752	7.190	.04493	7.719	.02938	8.276	.01793								
6.652	.06741	7.200	.04479	7.724	.02923	8.290	.01777								
6.667	.06706	7.205	.04466	7.733	.02896	8.305	.01763								
6.671	.06601	7.210	.04414	7.738	.02848	8.310	.01746								
6.676	.06591	7.224	.04393	7.743	.02825	8.314	.01727								
6.690	.06555	7.238	.04347	7.757	.02822	8.333	.01724								
6.705	.06486	7.243	.04313	7.776	.02816	8.343	.01681								
6.710	.06427	7.248	.04298	7.781	.02794	8.348	.01670								
6.714	.06392	7.262	.04274	7.795	.02782	8.352	.01657								
6.729	.06379	7.267	.04231	7.800	.02753	8.367	.01651								
6.733	.06361	7.276	.04162	7.810	.02730	8.381	.01619								
6.748	.06259	7.281	.04106	7.819	.02714	8.386	.01605								
6.752	.06209	7.286	.04088	7.833	.02697	8.390	.01601								
6.767	.06183	7.314	.04082	7.848	.02629	8.405	.01582								
6.781	.06080	7.319	.04060	7.852	.02593	8.410	.01565								
6.790	.06055	7.324	.04006	7.871	.02579	8.419	.01551								
6.805	.06033	7.338	.03982	7.876	.02568	8.424	.01531								
6.810	.05982	7.352	.03970	7.890	.02558	8.429	.01520								
6.819	.05928	7.357	.03946	7.895	.02523	8.443	.01516								
6.824	.05865	7.362	.03933	7.910	.02511	8.462	.01504								
6.843	.05830	7.376	.03913	7.924	.02502	8.467	.01477								
6.857	.05796	7.390	.03882	7.929	.02487	8.481	.01455								
6.862	.05769	7.395	.03853	7.933	.02479	8.486	.01443								
6.867	.05740	7.400	.03812	7.948	.02460	8.495	.01440								
6.881	.05686	7.414	.03798	7.952	.02445	8.505	.01429								
6.886	.05660	7.419	.03779	7.962	.02426	8.519	.01425								
6.895	.05639	7.433	.03735	7.967	.02405	8.533	.01422								
6.900	.05602	7.438	.03681	7.971	.02357	8.538	.01377								
6.905	.05568	7.452	.03666	8.000	.02354	8.557	.01363								
6.919	.05547	7.467	.03649	8.005	.02322	8.562	.01349								
6.933	.05500	7.476	.03576	8.010	.02306	8.571	.01321								
6.938	.05433	7.490	.03552	8.024	.02288	8.576	.01313								
6.943	.05386	7.495	.03501	8.038	.02267	8.581	.01305								
6.962	.05384	7.505	.03483	8.043	.02249	8.595	.01298								
6.971	.05327	7.510	.03464	8.048	.02233	8.610	.01280								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

h		P(H ₂ ≥ h)		h		P(H ₂ ≥ h)		h		P(H ₂ ≥ h)		h		P(H ₂ ≥ h)	
4	4	3	3	4	4	3	3	4	4	3	3	4	4	3	3
8.619	.01271	9.181	.00709	9.738	.00377	10.329	.00137								
8.633	.01255	9.190	.00705	9.752	.00373	10.333	.00135								
8.638	.01233	9.205	.00703	9.757	.00371	10.348	.00131								
8.648	.01224	9.219	.00683	9.762	.00370	10.362	.00130								
8.652	.01215	9.224	.00673	9.776	.00367	10.367	.00129								
8.657	.01201	9.243	.00666	9.781	.00357	10.371	.00121								
8.686	.01198	9.248	.00661	9.790	.00356	10.390	.00120								
8.690	.01195	9.257	.00644	9.795	.00355	10.400	.00117								
8.695	.01177	9.262	.00643	9.800	.00351	10.405	.00108								
8.710	.01175	9.267	.00640	9.833	.00344	10.410	.00105								
8.724	.01169	9.281	.00634	9.838	.00328	10.424	.00104								
8.729	.01158	9.295	.00632	9.852	.00325	10.443	.00104								
8.733	.01149	9.300	.00627	9.857	.00324	10.462	.00103								
8.748	.01135	9.305	.00619	9.867	.00321	10.467	.00098								
8.762	.01112	9.319	.00611	9.876	.00305	10.476	.00089								
8.767	.01104	9.324	.00599	9.890	.00303	10.486	.00087								
8.771	.01095	9.333	.00588	9.905	.00298	10.524	.00085								
8.786	.01089	9.338	.00575	9.910	.00296	10.538	.00083								
8.790	.01079	9.343	.00570	9.929	.00295	10.552	.00080								
8.805	.01068	9.371	.00569	9.933	.00291	10.576	.00078								
8.810	.01060	9.376	.00563	9.943	.00276	10.590	.00078								
8.824	.01056	9.381	.00562	9.948	.00273	10.614	.00077								
8.838	.01043	9.395	.00559	9.952	.00268	10.619	.00075								
8.848	.01031	9.410	.00554	9.967	.00264	10.629	.00072								
8.862	.01016	9.414	.00546	9.981	.00246	10.633	.00071								
8.867	.01003	9.419	.00540	9.986	.00244	10.638	.00063								
8.876	.00974	9.433	.00536	9.990	.00242	10.652	.00062								
8.881	.00966	9.448	.00529	10.005	.00236	10.667	.00060								
8.900	.00955	9.452	.00526	10.010	.00234	10.676	.00057								
8.914	.00935	9.457	.00520	10.019	.00231	10.695	.00055								
8.919	.00930	9.476	.00516	10.024	.00230	10.705	.00055								
8.924	.00918	9.490	.00503	10.029	.00228	10.714	.00054								
8.938	.00916	9.495	.00497	10.057	.00227	10.748	.00053								
8.943	.00902	9.510	.00497	10.062	.00225	10.752	.00052								
8.952	.00889	9.524	.00488	10.067	.00222	10.767	.00051								
8.957	.00885	9.533	.00483	10.081	.00212	10.781	.00048								
8.962	.00884	9.548	.00475	10.095	.00207	10.786	.00047								
8.976	.00880	9.552	.00466	10.100	.00202	10.819	.00046								
8.990	.00870	9.562	.00463	10.105	.00196	10.829	.00045								
8.995	.00855	9.567	.00456	10.119	.00193	10.848	.00044								
9.019	.00849	9.586	.00451	10.133	.00188	10.867	.00042								
9.029	.00840	9.605	.00443	10.138	.00176	10.881	.00039								
9.033	.00836	9.610	.00439	10.143	.00175	10.919	.00038								
9.038	.00820	9.624	.00431	10.162	.00171	10.933	.00037								
9.052	.00816	9.629	.00429	10.176	.00169	10.976	.00035								
9.067	.00809	9.638	.00424	10.181	.00168	10.981	.00034								
9.071	.00806	9.643	.00417	10.195	.00166	11.000	.00034								
9.076	.00800	9.648	.00416	10.219	.00165	11.010	.00031								
9.090	.00797	9.662	.00415	10.233	.00164	11.033	.00030								
9.095	.00782	9.676	.00413	10.238	.00155	11.048	.00025								
9.105	.00767	9.681	.00404	10.248	.00152	11.076	.00024								
9.110	.00759	9.686	.00400	10.271	.00149	11.090	.00022								
9.148	.00750	9.705	.00398	10.290	.00146	11.095	.00022								
9.152	.00743	9.714	.00393	10.295	.00145	11.110	.00021								
9.167	.00733	9.719	.00389	10.310	.00141	11.133	.00021								
9.171	.00711	9.724	.00383	10.324	.00140	11.152	.00016								

h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
4	4	3	3	4	4	4	1	4	4	4	1	4	4	4	1
11.167	.00015	6.396	.06204	7.594	.02579	8.802	.00682								
11.224	.00014	6.412	.06178	7.615	.02541	8.835	.00661								
11.238	.00013	6.429	.06053	7.632	.02517	8.852	.00639								
11.300	.00013	6.462	.05821	7.648	.02470	8.868	.00631								
11.376	.00009	6.478	.05757	7.665	.02454	8.901	.00618								
11.400	.00009	6.495	.05674	7.681	.02443	8.934	.00578								
11.429	.00008	6.544	.05648	7.714	.02432	8.951	.00522								
11.438	.00008	6.560	.05552	7.731	.02350	9.000	.00496								
11.467	.00007	6.577	.05461	7.747	.02334	9.033	.00490								
11.490	.00006	6.593	.05405	7.764	.02227	9.049	.00424								
11.514	.00006	6.610	.05379	7.780	.02219	9.066	.00400								
11.533	.00005	6.626	.05288	7.797	.02198	9.082	.00394								
11.667	.00003	6.659	.05219	7.813	.02089	9.099	.00392								
11.771	.00002	6.676	.05102	7.846	.02065	9.115	.00378								
11.833	.00002	6.709	.05032	7.863	.02049	9.132	.00373								
11.895	.00001	6.725	.04979	7.879	.01966	9.181	.00352								
12.200	.00001	6.742	.04944	7.896	.01947	9.198	.00309								
		6.758	.04931	7.929	.01934	9.214	.00258								
		6.791	.04737	7.945	.01897	9.247	.00253								
		6.808	.04707	7.978	.01828	9.264	.00248								
		6.824	.04646	7.995	.01817	9.330	.00245								
		6.857	.04555	8.011	.01758	9.379	.00240								
		6.874	.04534	8.027	.01732	9.396	.00224								
		6.890	.04446	8.044	.01721	9.429	.00216								
		6.923	.04412	8.060	.01684	9.478	.00176								
		6.940	.04393	8.077	.01652	9.527	.00160								
		6.956	.04321	8.126	.01644	9.593	.00148								
		6.973	.04095	8.143	.01622	9.610	.00145								
		6.989	.04065	8.159	.01497	9.626	.00143								
		7.005	.04007	8.192	.01487	9.643	.00132								
		7.022	.03921	8.209	.01447	9.709	.00124								
		7.071	.03903	8.242	.01396	9.725	.00121								
		7.088	.03799	8.258	.01343	9.758	.00097								
		7.104	.03756	8.275	.01316	9.775	.00092								
		7.137	.03692	8.291	.01308	9.824	.00081								
		7.154	.03642	8.308	.01295	9.841	.00079								
		7.187	.03498	8.324	.01268	9.989	.00068								
		7.203	.03482	8.341	.01257	10.088	.00065								
		7.220	.03442	8.390	.01217	10.121	.00049								
		7.236	.03373	8.407	.01180	10.170	.00044								
		7.253	.03330	8.423	.01169	10.187	.00039								
		7.269	.03301	8.440	.01162	10.236	.00036								
		7.286	.03247	8.456	.01156	10.269	.00031								
		7.319	.03173	8.522	.01092	10.516	.00025								
		7.335	.03128	8.538	.01076	10.681	.00017								
		7.352	.03117	8.555	.01012	10.764	.00013								
		7.368	.03082	8.571	.01007	11.011	.00005								
		7.401	.03061	8.588	.00986										
		7.418	.03002	8.604	.00943										
		7.451	.02893	8.654	.00892										
		7.467	.02808	8.687	.00871										
		7.484	.02795	8.703	.00826	5.900	.10136								
		7.500	.02773	8.720	.00807	5.914	.09940								
		7.516	.02731	8.736	.00797	5.929	.09799								
		7.533	.02712	8.769	.00783	5.943	.09759								
		7.549	.02661	8.786	.00778	5.971	.09719								
						5.986	.09602								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
4	4	4	2	4	4	4	2	4	4	4	2	4	4	4	2
6.014	.09515	6.957	.04960	7.929	.02428	8.886	.00983								
6.029	.09478	6.971	.04902	7.943	.02393	8.900	.00975								
6.043	.09241	7.000	.04807	7.957	.02388	8.914	.00911								
6.057	.09087	7.014	.04724	7.971	.02367	8.943	.00905								
6.086	.09060	7.029	.04680	7.986	.02310	8.957	.00883								
6.100	.08999	7.043	.04647	8.000	.02305	8.971	.00866								
6.114	.08832	7.057	.04626	8.029	.02265	8.986	.00862								
6.129	.08729	7.071	.04557	8.043	.02242	9.000	.00857								
6.143	.08713	7.086	.04516	8.057	.02203	9.014	.00816								
6.157	.08632	7.114	.04500	8.071	.02188	9.029	.00803								
6.171	.08515	7.129	.04436	8.086	.02174	9.057	.00778								
6.200	.08457	7.143	.04403	8.100	.02131	9.071	.00770								
6.214	.08143	7.157	.04368	8.114	.02050	9.086	.00748								
6.229	.08087	7.171	.04347	8.143	.02029	9.100	.00742								
6.243	.08059	7.186	.04299	8.157	.01992	9.114	.00732								
6.257	.07964	7.200	.04233	8.171	.01975	9.129	.00711								
6.271	.07873	7.229	.04149	8.186	.01937	9.171	.00701								
6.286	.07838	7.243	.04086	8.200	.01915	9.186	.00684								
6.314	.07732	7.257	.04027	8.214	.01876	9.214	.00668								
6.329	.07669	7.271	.04010	8.257	.01825	9.229	.00664								
6.343	.07551	7.286	.03968	8.271	.01760	9.243	.00659								
6.357	.07505	7.300	.03940	8.300	.01751	9.257	.00635								
6.371	.07473	7.314	.03883	8.314	.01710	9.286	.00622								
6.386	.07406	7.343	.03876	8.329	.01684	9.300	.00592								
6.400	.07321	7.357	.03842	8.343	.01653	9.314	.00583								
6.429	.07297	7.386	.03756	8.371	.01622	9.329	.00573								
6.443	.07149	7.400	.03732	8.386	.01610	9.343	.00565								
6.471	.07102	7.414	.03539	8.400	.01555	9.357	.00558								
6.486	.07044	7.429	.03512	8.414	.01509	9.400	.00553								
6.500	.06995	7.457	.03488	8.429	.01502	9.414	.00526								
6.514	.06773	7.471	.03390	8.443	.01472	9.429	.00521								
6.543	.06739	7.486	.03367	8.457	.01453	9.443	.00518								
6.557	.06608	7.500	.03342	8.486	.01445	9.457	.00517								
6.571	.06567	7.514	.03295	8.500	.01420	9.471	.00502								
6.586	.06539	7.529	.03268	8.514	.01391	9.486	.00487								
6.600	.06498	7.571	.03199	8.529	.01385	9.514	.00484								
6.614	.06274	7.586	.03139	8.543	.01378	9.529	.00481								
6.629	.06217	7.600	.03088	8.557	.01359	9.543	.00474								
6.657	.06193	7.614	.03061	8.571	.01340	9.557	.00456								
6.671	.06139	7.629	.03022	8.600	.01322	9.571	.00455								
6.686	.06044	7.643	.02998	8.614	.01229	9.586	.00451								
6.700	.06011	7.657	.02982	8.629	.01198	9.600	.00444								
6.714	.05972	7.686	.02961	8.643	.01184	9.629	.00433								
6.729	.05853	7.700	.02927	8.657	.01167	9.643	.00412								
6.743	.05787	7.714	.02842	8.671	.01154	9.671	.00395								
6.771	.05763	7.729	.02811	8.686	.01135	9.686	.00383								
6.786	.05706	7.743	.02797	8.714	.01121	9.700	.00376								
6.800	.05667	7.757	.02716	8.729	.01111	9.714	.00370								
6.814	.05555	7.771	.02696	8.757	.01100	9.743	.00356								
6.829	.05495	7.800	.02684	8.771	.01089	9.757	.00348								
6.843	.05439	7.814	.02636	8.786	.01066	9.771	.00324								
6.857	.05385	7.843	.02609	8.800	.01054	9.786	.00315								
6.886	.05366	7.857	.02601	8.829	.01039	9.800	.00314								
6.900	.05247	7.871	.02570	8.843	.01014	9.814	.00292								
6.929	.05099	7.886	.02527	8.857	.01006	9.829	.00286								
6.943	.05040	7.914	.02499	8.871	.00987	9.857	.00283								

h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
4	4	4	2	4	4	4	2	4	4	4	3	4	4	4	3
9.871	.00277	11.186	.00015	6.429	.07975	6.992	.05517								
9.886	.00275	11.229	.00014	6.442	.07902	7.013	.05460								
9.900	.00264	11.314	.00014	6.450	.07812	7.017	.05408								
9.914	.00255	11.357	.00011	6.454	.07787	7.029	.05389								
9.929	.00250	11.386	.00010	6.475	.07759	7.050	.05348								
9.943	.00241	11.429	.00010	6.479	.07692	7.054	.05319								
9.971	.00240	11.457	.00008	6.488	.07671	7.067	.05286								
9.986	.00225	11.471	.00008	6.492	.07640	7.075	.05269								
10.000	.00220	11.600	.00005	6.513	.07589	7.079	.05223								
10.014	.00214	11.686	.00003	6.517	.07543	7.092	.05168								
10.029	.00208	11.814	.00002	6.529	.07495	7.113	.05123								
10.043	.00194	12.114	.00001	6.542	.07415	7.117	.05057								
10.057	.00191			6.554	.07401	7.129	.05022								
10.100	.00185	4	4	4	3	6.563	.07348	7.142	.04954						
10.129	.00158			6.567	.07335	7.150	.04902								
10.143	.00157	6.029	.10084	6.579	.07312	7.154	.04882								
10.157	.00156	6.042	.09980	6.583	.07262	7.163	.04860								
10.200	.00155	6.054	.09966	6.592	.07199	7.167	.04831								
10.229	.00150	6.063	.09922	6.600	.07136	7.179	.04822								
10.243	.00142	6.067	.09893	6.617	.07124	7.188	.04778								
10.257	.00139	6.075	.09879	6.629	.07094	7.192	.04770								
10.271	.00136	6.079	.09872	6.642	.07037	7.225	.04720								
10.286	.00135	6.092	.09795	6.654	.06955	7.242	.04647								
10.314	.00131	6.100	.09677	6.663	.06914	7.254	.04605								
10.329	.00114	6.113	.09631	6.675	.06828	7.263	.04579								
10.357	.00110	6.117	.09574	6.679	.06777	7.267	.04534								
10.371	.00105	6.129	.09537	6.692	.06716	7.275	.04527								
10.386	.00104	6.142	.09460	6.700	.06630	7.279	.04489								
10.400	.00102	6.154	.09381	6.713	.06595	7.292	.04446								
10.429	.00089	6.167	.09332	6.717	.06564	7.300	.04443								
10.443	.00088	6.175	.09311	6.742	.06530	7.313	.04418								
10.457	.00084	6.179	.09207	6.750	.06488	7.317	.04409								
10.471	.00081	6.192	.09133	6.754	.06486	7.329	.04379								
10.486	.00080	6.213	.09084	6.767	.06459	7.342	.04334								
10.500	.00072	6.217	.09004	6.775	.06427	7.367	.04288								
10.543	.00069	6.225	.08981	6.779	.06365	7.375	.04265								
10.600	.00062	6.229	.08930	6.789	.06302	7.379	.04243								
10.614	.00061	6.242	.08906	6.792	.06282	7.388	.04204								
10.629	.00057	6.254	.08806	6.825	.06254	7.392	.04184								
10.657	.00055	6.263	.08763	6.829	.06215	7.413	.04125								
10.671	.00054	6.267	.08698	6.842	.06173	7.417	.04090								
10.686	.00051	6.279	.08672	6.850	.06127	7.425	.04086								
10.700	.00048	6.288	.08615	6.854	.06095	7.429	.04078								
10.729	.00045	6.300	.08580	6.867	.06079	7.442	.04015								
10.743	.00045	6.317	.08567	6.879	.06066	7.450	.03976								
10.800	.00039	6.325	.08539	6.889	.05987	7.454	.03945								
10.829	.00036	6.329	.08465	6.892	.05953	7.463	.03917								
10.857	.00034	6.342	.08383	6.900	.05911	7.467	.03889								
10.886	.00034	6.354	.08296	6.925	.05889	7.479	.03886								
10.900	.00032	6.363	.08286	6.929	.05805	7.488	.03867								
10.957	.00030	6.367	.08214	6.942	.05761	7.492	.03843								
11.000	.00027	6.375	.08174	6.954	.05701	7.500	.03800								
11.014	.00021	6.379	.08164	6.963	.05655	7.517	.03796								
11.043	.00019	6.392	.08060	6.967	.05581	7.525	.03776								
11.114	.00018	6.400	.08006	6.975	.05543	7.529	.03726								
11.171	.00016	6.413	.07999	6.979	.05525	7.554	.03699								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h				h				h				h			
P(H ≥ h)				P(H ≥ h)				P(H ≥ h)				P(H ≥ h)			
4	4	4	3	4	4	4	3	4	4	4	3	4	4	4	3
7.567	.03678	8.125	.02398	8.663	.01452	9.267	.00808								
7.575	.03657	8.129	.02395	8.667	.01446	9.279	.00806								
7.579	.03620	8.142	.02369	8.679	.01444	9.288	.00798								
7.592	.03594	8.154	.02340	8.692	.01431	9.292	.00791								
7.600	.03560	8.163	.02322	8.700	.01408	9.300	.00787								
7.613	.03554	8.175	.02294	8.717	.01400	9.317	.00779								
7.629	.03529	8.179	.02281	8.725	.01386	9.325	.00769								
7.642	.03502	8.192	.02250	8.729	.01370	9.329	.00758								
7.650	.03470	8.200	.02227	8.742	.01364	9.342	.00743								
7.654	.03462	8.217	.02218	8.754	.01341	9.354	.00732								
7.675	.03441	8.229	.02207	8.763	.01335	9.363	.00730								
7.679	.03412	8.242	.02204	8.767	.01309	9.367	.00725								
7.688	.03386	8.250	.02181	8.775	.01302	9.379	.00719								
7.692	.03381	8.254	.02176	8.779	.01297	9.392	.00706								
7.713	.03351	8.267	.02156	8.829	.01274	9.400	.00697								
7.717	.03310	8.275	.02151	8.842	.01248	9.413	.00695								
7.725	.03287	8.279	.02114	8.850	.01233	9.429	.00689								
7.729	.03247	8.288	.02078	8.867	.01224	9.442	.00679								
7.742	.03238	8.313	.02071	8.875	.01222	9.450	.00672								
7.754	.03197	8.317	.02064	8.879	.01216	9.454	.00670								
7.763	.03174	8.325	.02052	8.892	.01200	9.467	.00665								
7.767	.03169	8.329	.02040	8.913	.01177	9.475	.00662								
7.779	.03151	8.342	.02020	8.925	.01161	9.479	.00644								
7.788	.03099	8.350	.01991	8.929	.01152	9.488	.00642								
7.792	.03069	8.354	.01976	8.942	.01137	9.492	.00639								
7.800	.03060	8.363	.01973	8.954	.01127	9.513	.00632								
7.817	.03054	8.367	.01953	8.963	.01121	9.517	.00620								
7.825	.03041	8.379	.01934	8.967	.01105	9.525	.00613								
7.829	.03003	8.388	.01919	8.979	.01093	9.529	.00607								
7.842	.02958	8.392	.01905	8.988	.01087	9.550	.00597								
7.863	.02929	8.400	.01889	8.992	.01077	9.554	.00592								
7.867	.02887	8.425	.01885	9.017	.01061	9.567	.00588								
7.879	.02874	8.429	.01851	9.025	.01051	9.579	.00580								
7.892	.02849	8.442	.01819	9.029	.01031	9.588	.00566								
7.900	.02826	8.454	.01794	9.042	.01019	9.592	.00559								
7.913	.02802	8.463	.01786	9.054	.01016	9.629	.00554								
7.917	.02782	8.467	.01762	9.063	.01008	9.642	.00547								
7.929	.02777	8.475	.01759	9.067	.01003	9.654	.00544								
7.942	.02749	8.492	.01744	9.075	.01000	9.663	.00541								
7.950	.02722	8.513	.01728	9.079	.00988	9.675	.00536								
7.954	.02715	8.517	.01706	9.092	.00975	9.679	.00532								
7.967	.02693	8.529	.01694	9.100	.00965	9.692	.00521								
7.975	.02676	8.542	.01670	9.117	.00953	9.700	.00516								
7.988	.02644	8.554	.01667	9.129	.00945	9.713	.00510								
7.992	.02635	8.567	.01654	9.142	.00930	9.717	.00504								
8.013	.02611	8.575	.01634	9.150	.00919	9.742	.00498								
8.025	.02581	8.579	.01608	9.154	.00913	9.754	.00489								
8.029	.02563	8.588	.01585	9.175	.00903	9.767	.00486								
8.042	.02541	8.592	.01574	9.179	.00882	9.775	.00481								
8.050	.02528	8.613	.01560	9.188	.00870	9.779	.00475								
8.054	.02505	8.617	.01537	9.192	.00869	9.788	.00467								
8.079	.02494	8.625	.01528	9.213	.00860	9.792	.00466								
8.088	.02469	8.629	.01521	9.242	.00840	9.813	.00464								
8.092	.02457	8.642	.01503	9.250	.00823	9.817	.00463								
8.100	.02414	8.650	.01480	9.254	.00820	9.825	.00459								
8.117	.02411	8.654	.01465	9.263	.00813	9.829	.00454								

h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
4	4	4	3	4	4	4	3	4	4	4	3	4	4	4	3
9.842	.00446	10.429	.00226	11.050	.00077	11.754	.00016								
9.850	.00437	10.442	.00223	11.054	.00075	11.763	.00015								
9.863	.00429	10.450	.00220	11.067	.00074	11.767	.00014								
9.879	.00424	10.454	.00217	11.079	.00072	11.775	.00014								
9.888	.00416	10.463	.00215	11.088	.00070	11.779	.00013								
9.892	.00412	10.467	.00214	11.092	.00069	11.842	.00012								
9.917	.00407	10.488	.00213	11.100	.00069	11.850	.00011								
9.925	.00406	10.492	.00213	11.117	.00068	11.854	.00011								
9.929	.00400	10.500	.00211	11.125	.00066	11.867	.00011								
9.942	.00395	10.517	.00209	11.129	.00064	11.913	.00010								
9.954	.00385	10.525	.00209	11.142	.00063	11.942	.00010								
9.963	.00382	10.529	.00203	11.154	.00063	11.950	.00009								
9.967	.00377	10.542	.00196	11.163	.00061	11.988	.00008								
9.975	.00374	10.554	.00195	11.167	.00057	12.025	.00008								
9.979	.00367	10.567	.00190	11.175	.00056	12.029	.00007								
9.992	.00364	10.579	.00187	11.179	.00055	12.075	.00007								
10.000	.00356	10.592	.00184	11.192	.00053	12.079	.00007								
10.013	.00356	10.600	.00182	11.213	.00051	12.100	.00007								
10.029	.00354	10.613	.00180	11.229	.00051	12.129	.00006								
10.050	.00351	10.617	.00177	11.242	.00050	12.142	.00005								
10.054	.00349	10.629	.00173	11.254	.00048	12.175	.00005								
10.075	.00346	10.642	.00166	11.275	.00046	12.179	.00004								
10.079	.00338	10.650	.00157	11.279	.00045	12.192	.00004								
10.088	.00332	10.654	.00155	11.288	.00045	12.217	.00004								
10.092	.00331	10.675	.00154	11.317	.00045	12.363	.00003								
10.113	.00326	10.679	.00149	11.325	.00044	12.375	.00002								
10.117	.00318	10.692	.00148	11.329	.00043	12.429	.00002								
10.129	.00314	10.713	.00146	11.342	.00041	12.450	.00002								
10.142	.00309	10.717	.00141	11.363	.00040	12.454	.00001								
10.154	.00305	10.725	.00137	11.367	.00040	12.475	.00001								
10.163	.00303	10.729	.00134	11.379	.00038	12.567	.00001								
10.179	.00298	10.742	.00134	11.388	.00037	12.775	.00001								
10.188	.00294	10.750	.00134	11.392	.00036	12.829	.00000								
10.192	.00293	10.754	.00133	11.400	.00036	13.150	.00000								
10.217	.00290	10.763	.00129	11.425	.00035										
10.225	.00287	10.767	.00127	11.429	.00034	4	4	4	4						
10.229	.00283	10.779	.00126	11.442	.00033										
10.242	.00281	10.788	.00123	11.454	.00032	6.066	.10033								
10.254	.00277	10.825	.00119	11.475	.00031	6.088	.09900								
10.263	.00276	10.829	.00116	11.492	.00031	6.110	.09814								
10.267	.00267	10.842	.00115	11.513	.00030	6.132	.09601								
10.275	.00266	10.863	.00110	11.517	.00029	6.154	.09548								
10.279	.00263	10.879	.00104	11.529	.00028	6.176	.09320								
10.292	.00259	10.892	.00103	11.542	.00028	6.199	.09279								
10.300	.00257	10.900	.00102	11.550	.00028	6.221	.09205								
10.313	.00254	10.929	.00100	11.575	.00027	6.243	.09138								
10.317	.00253	10.942	.00096	11.579	.00024	6.265	.08864								
10.329	.00252	10.954	.00093	11.592	.00023	6.287	.08825								
10.342	.00250	10.967	.00093	11.629	.00022	6.331	.08687								
10.350	.00245	10.975	.00091	11.642	.00021	6.353	.08548								
10.367	.00244	10.988	.00089	11.650	.00020	6.375	.08523								
10.379	.00241	10.992	.00086	11.654	.00019	6.397	.08374								
10.388	.00236	11.013	.00083	11.663	.00018	6.419	.08312								
10.392	.00235	11.017	.00083	11.679	.00017	6.441	.08179								
10.413	.00233	11.025	.00080	11.725	.00017	6.463	.08034								
10.425	.00229	11.029	.00079	11.742	.00016	6.485	.07891								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)		h		P(H ≥ h)	
4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
6.507	.07855	7.853	.03242	9.199	.01073	10.522	.00271								
6.529	.07702	7.875	.03207	9.221	.01052	10.566	.00258								
6.551	.07684	7.897	.03125	9.243	.01027	10.610	.00249								
6.574	.07436	7.919	.03091	9.265	.01013	10.632	.00239								
6.596	.07338	7.941	.03053	9.287	.00999	10.654	.00236								
6.618	.07280	7.963	.03032	9.309	.00964	10.676	.00227								
6.640	.07197	7.985	.02967	9.331	.00960	10.699	.00220								
6.684	.07025	8.007	.02939	9.353	.00908	10.721	.00217								
6.706	.06941	8.029	.02866	9.375	.00898	10.743	.00215								
6.728	.06890	8.051	.02821	9.397	.00877	10.765	.00202								
6.750	.06806	8.096	.02787	9.419	.00871	10.787	.00202								
6.772	.06730	8.118	.02662	9.441	.00816	10.809	.00196								
6.794	.06498	8.140	.02645	9.463	.00806	10.831	.00192								
6.816	.06436	8.162	.02587	9.507	.00789	10.853	.00189								
6.838	.06354	8.184	.02544	9.529	.00785	10.875	.00185								
6.860	.06307	8.206	.02517	9.551	.00771	10.919	.00172								
6.904	.06229	8.228	.02476	9.574	.00720	10.941	.00161								
6.926	.05999	8.250	.02402	9.596	.00717	10.963	.00157								
6.949	.05962	8.272	.02392	9.618	.00699	10.985	.00154								
6.971	.05842	8.316	.02327	9.640	.00684	11.007	.00153								
6.993	.05788	8.338	.02274	9.662	.00666	11.029	.00149								
7.037	.05700	8.360	.02235	9.684	.00660	11.051	.00145								
7.059	.05581	8.382	.02176	9.728	.00643	11.074	.00140								
7.081	.05567	8.404	.02166	9.750	.00617	11.096	.00137								
7.103	.05475	8.449	.02134	9.772	.00606	11.140	.00134								
7.125	.05390	8.471	.02078	9.794	.00592	11.184	.00128								
7.147	.05301	8.493	.02075	9.816	.00578	11.206	.00124								
7.169	.05244	8.515	.01997	9.860	.00553	11.228	.00119								
7.191	.05080	8.537	.01989	9.882	.00534	11.272	.00117								
7.213	.05071	8.559	.01916	9.904	.00529	11.294	.00110								
7.235	.04922	8.581	.01859	9.926	.00522	11.316	.00110								
7.257	.04875	8.603	.01828	9.949	.00514	11.338	.00100								
7.279	.04833	8.625	.01813	9.971	.00491	11.360	.00098								
7.301	.04797	8.647	.01752	9.993	.00484	11.382	.00096								
7.324	.04687	8.669	.01741	10.015	.00466	11.404	.00094								
7.346	.04632	8.691	.01705	10.037	.00461	11.426	.00084								
7.390	.04486	8.713	.01686	10.059	.00450	11.449	.00083								
7.412	.04431	8.735	.01656	10.081	.00448	11.471	.00081								
7.434	.04409	8.757	.01528	10.103	.00422	11.493	.00079								
7.456	.04295	8.801	.01538	10.125	.00418	11.515	.00077								
7.478	.04264	8.824	.01507	10.147	.00409	11.537	.00073								
7.500	.04170	8.846	.01488	10.169	.00392	11.559	.00067								
7.522	.04109	8.868	.01462	10.213	.00389	11.581	.00066								
7.544	.04054	8.890	.01441	10.235	.00362	11.625	.00062								
7.566	.04013	8.912	.01387	10.257	.00360	11.647	.00061								
7.588	.03873	8.934	.01375	10.279	.00347	11.669	.00059								
7.610	.03865	8.956	.01310	10.301	.00341	11.691	.00055								
7.632	.03796	8.978	.01297	10.324	.00330	11.713	.00053								
7.654	.03740	9.000	.01276	10.346	.00319	11.735	.00050								
7.676	.03699	9.022	.01267	10.368	.00312	11.757	.00045								
7.699	.03643	9.044	.01216	10.390	.00308	11.801	.00044								
7.743	.03536	9.066	.01205	10.412	.00305	11.846	.00041								
7.765	.03474	9.088	.01172	10.434	.00303	11.868	.00037								
7.787	.03463	9.110	.01130	10.456	.00300	11.890	.00035								
7.809	.03372	9.154	.01111	10.478	.00296	11.912	.00034								
7.831	.03358	9.176	.01077	10.500	.00274	11.934	.00032								

h				P(H≥h)				h				P(H≥h)				h				P(H≥h)				h				P(H≥h)			
4	4	4	4	2	2	2	1	1	3	2	2	1	1	3	2	2	2	2													
11.978	.00029	6.500	.05238	7.200	.02460	7.030	.09449																								
12.000	.00028	6.750	.02381	7.244	.02063	7.045	.09414																								
12.022	.00027			7.400	.01429	7.076	.09322																								
12.044	.00026	2 2 2 2 1		7.600	.00794	7.091	.08906																								
12.066	.00025					7.121	.08768																								
12.088	.00024	6.533	.10476	3 2 2 2 1		7.136	.08560																								
12.110	.00023	6.600	.08889			7.167	.08537																								
12.132	.00021	6.667	.08254	6.691	.10111	7.182	.08341																								
12.176	.00021	6.733	.07619	6.709	.09873	7.212	.08144																								
12.199	.00020	6.800	.06984	6.745	.09238	7.227	.07948																								
12.221	.00017	6.933	.05714	6.818	.09143	7.258	.07856																								
12.243	.00017	7.000	.05397	6.855	.09000	7.303	.07671																								
12.265	.00016	7.133	.04127	6.873	.08667	7.318	.07290																								
12.287	.00015	7.200	.03492	6.909	.08286	7.348	.07082																								
12.331	.00013	7.333	.02222	6.927	.07905	7.364	.06967																								
12.375	.00013	7.533	.00952	6.964	.07794	7.394	.06753																								
12.397	.00012	7.733	.00529	6.982	.07730	7.409	.06684																								
12.419	.00011			7.018	.07349	7.439	.06661																								
12.441	.00011	2 2 2 2 2		7.073	.06698	7.455	.06361																								
12.463	.00010			7.127	.06365	7.485	.06153																								
12.507	.00009	6.873	.10159	7.145	.06079	7.500	.05980																								
12.574	.00008	6.982	.09101	7.182	.05698	7.530	.05887																								
12.640	.00007	7.091	.07937	7.200	.05603	7.545	.05795																								
12.706	.00006	7.309	.06349	7.291	.05381	7.576	.05726																								
12.728	.00006	7.418	.04868	7.309	.04889	7.591	.05460																								
12.750	.00005	7.527	.03810	7.345	.04651	7.621	.05322																								
12.772	.00005	7.636	.03386	7.364	.04365	7.636	.05102																								
12.794	.00004	7.745	.03175	7.400	.04143	7.667	.05079																								
12.860	.00003	7.855	.02540	7.455	.04111	7.682	.04745																								
12.882	.00003	7.964	.02222	7.473	.03714	7.712	.04652																								
12.904	.00003	8.073	.01270	7.509	.03556	7.727	.04560																								
12.926	.00002	8.291	.00952	7.564	.03413	7.773	.04421																								
13.059	.00002	8.400	.00529	7.582	.03063	7.803	.04283																								
13.081	.00001	8.727	.00106	7.635	.03032	7.818	.04121																								
13.125	.00001			7.727	.02746	7.848	.04063																								
13.169	.00001	3 1 1 1 1		7.745	.02317	7.864	.03867																								
13.257	.00001			7.800	.02270	7.894	.03706																								
13.434	.00000	5.571	.14286	7.836	.01937	7.909	.03636																								
13.456	.00000			7.855	.01841	7.939	.03532																								
13.500	.00000	3 2 1 1 1		7.891	.01794	7.985	.03267																								
13.787	.00000			8.000	.01270	8.000	.03117																								
14.118	.00000	6.139	.10000	8.018	.01079	8.030	.03094																								
		6.333	.05714	8.127	.00937	8.045	.02978																								
		6.583	.03571	8.164	.00889	8.076	.02782																								
				8.182	.00698	8.091	.02713																								
2 1 1 1 1				8.291	.00508	8.121	.02672																								
4.857	.33333	3 2 2 1 1		8.327	.00317	8.136	.02649																								
				8.455	.00254	8.167	.02557																								
2 2 1 1 1		6.511	.10000	8.618	.00159	8.182	.02384																								
		6.533	.08466			8.212	.02297																								
5.464	.20952	6.600	.08254	3 2 2 2 2		8.258	.02124																								
5.786	.09524	6.711	.06984			8.273	.02078																								
		6.800	.04921	6.939	.10257	8.303	.01962																								
2 2 2 1 1		6.844	.04841	6.955	.09922	8.318	.01870																								
		6.867	.04206	6.985	.09680	8.348	.01847																								
6.083	.12381	7.044	.03889	7.000	.09553	8.394	.01801																								
6.250	.08810	7.067	.02937																												

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h					h					h					h				
P(H ₂ ≥ h)					P(H ₂ ≥ h)					P(H ₂ ≥ h)					P(H ₂ ≥ h)				
3	2	2	2	2	3	3	2	1	1	3	3	2	2	1	3	3	2	2	1
8.409	.01720				7.400	.03841				7.591	.04919				9.167	.00199			
8.439	.01651				7.418	.03349				7.606	.04908				9.182	.00130			
8.455	.01582				7.491	.03317				7.636	.04658				9.273	.00113			
8.530	.01455				7.564	.02548				7.652	.04571				9.303	.00095			
8.545	.01339				7.618	.02452				7.667	.04364				9.409	.00061			
8.576	.01258				7.691	.02357				7.697	.04315				9.545	.00043			
8.591	.01224				7.764	.02071				7.712	.04302								
8.621	.01154				7.782	.01853				7.727	.04019				3	3	2	2	2
8.636	.01108				7.855	.01262				7.758	.03993				7.013	.10045			
8.667	.01097				7.927	.01214				7.773	.03924				7.026	.09897			
8.682	.00958				8.055	.01024				7.788	.03811				7.051	.09706			
8.712	.00889				8.073	.00738				7.818	.03785				7.064	.09685			
8.758	.00854				8.218	.00714				7.833	.03768				7.090	.09494			
8.818	.00716				8.345	.00333				7.848	.03646				7.103	.09363			
8.894	.00629				8.509	.00238				7.879	.03349				7.115	.09321			
8.909	.00525									7.894	.03309				7.128	.09214			
8.955	.00508				3	3	2	2	1	7.909	.03159				7.154	.09069			
8.985	.00462									7.939	.03139				7.167	.09043			
9.000	.00392				6.758	.10316				7.955	.03087				7.179	.08936			
9.030	.00323				6.788	.09892				7.970	.02997				7.205	.08708			
9.091	.00231				6.803	.09794				8.015	.02789				7.218	.08690			
9.258	.00214				6.818	.09577				8.030	.02723				7.231	.08559			
9.273	.00167				6.848	.09511				8.061	.02685				7.256	.08468			
9.364	.00098				6.864	.09447				8.076	.02605				7.269	.08442			
9.636	.00029				6.879	.09352				8.091	.02501				7.282	.08405			
					6.924	.09100				8.121	.02437				7.295	.08244			
					6.939	.08889				8.182	.02391				7.321	.08084			
					6.970	.08817				8.197	.02333				7.333	.07973			
					6.985	.08742				8.212	.02140				7.359	.07856			
					7.000	.08407				8.242	.02004				7.372	.07830			
					7.030	.08346				8.258	.01973				7.385	.07639			
					7.045	.08205				8.303	.01817				7.397	.07605			
					7.061	.08185				8.318	.01794				7.410	.07452			
					7.091	.08141				8.333	.01687				7.436	.07439			
					7.106	.08069				8.379	.01452				7.462	.07255			
					7.121	.07789				8.394	.01414				7.474	.07243			
					7.152	.07362				8.424	.01397				7.487	.07149			
					7.167	.07319				8.439	.01362				7.500	.06952			
					7.212	.07137				8.455	.01304				7.513	.06873			
					7.227	.07074				8.485	.01201				7.526	.06823			
					7.242	.06909				8.500	.01114				7.564	.06709			
					7.273	.06646				8.561	.01102				7.577	.06642			
					7.288	.06600				8.576	.00984				7.590	.06569			
					7.303	.06436				8.621	.00926				7.603	.06437			
					7.333	.06421				8.697	.00840				7.615	.06297			
					7.348	.06338				8.727	.00710				7.628	.06289			
					7.364	.06038				8.758	.00680				7.641	.06190			
					7.394	.05921				8.788	.00671				7.667	.06038			
					7.409	.05880				8.803	.00645				7.679	.06028			
					7.424	.05863				8.818	.00576				7.692	.05898			
					7.470	.05823				8.864	.00571				7.705	.05802			
					7.485	.05707				8.924	.00476				7.718	.05667			
					7.515	.05387				8.939	.00433				7.731	.05618			
					7.530	.05317				9.030	.00260				7.744	.05602			
					7.545	.05124				9.045	.00225				7.782	.05514			
					7.576	.05107				9.061	.00216								

h				P(H≥h)				h				P(H≥h)				h				P(H≥h)				
3	3	2	2	2	3	3	2	2	2	3	3	2	2	2	3	3	3	1	1	3	3	3	1	1
7.795		.05423			8.718		.01903			9.744		.00250			9.455		.00065							
7.808		.05280			8.731		.01772			9.754		.00215												
7.821		.05218			8.744		.01725			9.764		.00198			3	3	3	2	1					
7.833		.05206			8.756		.01716			9.795		.00189												
7.846		.05117			8.769		.01677			9.833		.00176			6.897		.10222							
7.872		.05058			8.795		.01663			9.859		.00159			6.910		.09916							
7.897		.05048			8.821		.01631			9.885		.00146			6.949		.09694							
7.910		.04934			8.833		.01592			9.936		.00138			6.962		.09596							
7.923		.04788			8.846		.01503			9.949		.00125			7.000		.09495							
7.936		.04771			8.859		.01497			10.000		.00103			7.013		.09395							
7.949		.04710			8.872		.01448			10.026		.00090			7.051		.08937							
7.974		.04564			8.910		.01379			10.038		.00082			7.064		.08800							
7.987		.04519			8.936		.01312			10.064		.00079			7.103		.08725							
8.013		.04440			8.949		.01250			10.167		.00045			7.115		.08576							
8.026		.04291			8.962		.01236			10.256		.00042			7.154		.08384							
8.038		.04279			8.974		.01198			10.269		.00025			7.167		.08232							
8.051		.04240			9.000		.01164			10.346		.00016			7.205		.08136							
8.077		.04155			9.013		.01161			10.577		.00007			7.218		.07948							
8.090		.04145			9.026		.01135							7.256		.07721								
8.103		.04084			9.051		.01063			3	3	3	1	1	7.269		.07641							
8.128		.03974			9.064		.01057							7.308		.07548								
8.141		.03951			9.077		.01034			6.727		.10156			7.321		.07451							
8.154		.03828			9.103		.01005			6.788		.09779			7.359		.07106							
8.179		.03766			9.115		.00996			6.848		.08753			7.372		.06979							
8.192		.03753			9.128		.00990			6.909		.08623			7.410		.06930							
8.205		.03717			9.141		.00938			6.970		.08247			7.423		.06835							
8.218		.03551			9.167		.00887			7.030		.08156			7.462		.06584							
8.244		.03413			9.179		.00861			7.091		.07753			7.474		.06475							
8.256		.03377			9.205		.00817			7.152		.07597			7.513		.06394							
8.282		.03294			9.218		.00802			7.212		.06688			7.526		.06199							
8.295		.03284			9.231		.00771			7.273		.06545			7.564		.06018							
8.308		.03193			9.244		.00739			7.333		.06091			7.577		.05972							
8.321		.03150			9.256		.00705			7.394		.05896			7.615		.05938							
8.333		.03050			9.282		.00702			7.455		.05506			7.628		.05868							
8.359		.03002			9.308		.00685			7.515		.05377			7.667		.05561							
8.385		.02910			9.321		.00682			7.576		.04545			7.679		.05341							
8.397		.02881			9.333		.00649			7.636		.04481			7.718		.05301							
8.410		.02775			9.346		.00637			7.697		.04247			7.731		.05166							
8.423		.02701			9.359		.00609			7.758		.03812			7.769		.04885							
8.436		.02684			9.372		.00500			7.818		.03227			7.782		.04867							
8.449		.02681			9.423		.00577			7.879		.03104			7.821		.04767							
8.487		.02622			9.436		.00547			7.939		.03000			7.833		.04693							
8.500		.02618			9.449		.00522			8.000		.02844			7.872		.04532							
8.513		.02579			9.474		.00496			8.061		.02325			7.885		.04427							
8.526		.02514			9.487		.00488			8.121		.02273			7.923		.04405							
8.538		.02408			9.526		.00442			8.242		.01909			7.936		.04298							
8.551		.02400			9.538		.00433			8.303		.01416			7.974		.03985							
8.564		.02346			9.551		.00416			8.364		.01390			7.987		.03922							
8.590		.02266			9.564		.00352			8.424		.00909			8.026		.03878							
8.603		.02245			9.577		.00346			8.606		.00825			8.038		.03832							
8.615		.02182			9.590		.00339			8.667		.00591			8.077		.03748							
8.628		.02139			9.628		.00335			8.727		.00513			8.090		.03640							
8.641		.02046			9.641		.00317			8.848		.00435			8.128		.03597							
8.654		.02036			9.654		.00297			8.909		.00396			8.141		.03435							
8.667		.01991			9.679		.00284			8.970		.00377			8.179		.03324							
8.705		.01931			9.692		.00258			9.212		.00221			8.192		.03281							

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h			P(H ≥ h)			h			P(H ≥ h)			h			P(H ≥ h)			h			P(H ≥ h)				
3	3	3	2	1	3	3	3	2	1	3	3	3	2	2	3	3	3	2	2	3	3	3	2	2	
8.231	.03209				9.718	.00221				7.670	.06658				8.495	.03357									
8.244	.03181				9.769	.00198				7.692	.06579				8.505	.03308									
8.282	.02929				9.782	.00192				7.703	.06511				8.527	.03285									
9.295	.02828				9.833	.00130				7.714	.06446				8.538	.03266									
8.333	.02798				9.872	.00123				7.736	.06427				8.549	.03229									
8.346	.02752				9.885	.00120				7.747	.06398				8.571	.03128									
8.385	.02618				9.923	.00114				7.758	.06309				8.582	.03108									
8.397	.02587				9.974	.00097				7.790	.06186				8.593	.03060									
8.436	.02566				9.987	.00081				7.791	.06141				8.615	.03043									
8.449	.02471				10.090	.00052				7.802	.06012				8.626	.03007									
8.487	.02357				10.179	.00039				7.824	.05974				8.637	.02943									
8.500	.02284				10.295	.00026				7.835	.05923				8.659	.02880									
8.538	.02265				10.385	.00013				7.846	.05834				8.670	.02856									
8.551	.02169				10.500	.00011				7.868	.05749				8.681	.02795									
8.590	.01950									7.879	.05730				8.703	.02773									
8.603	.01927				3	3	3	2	2	7.890	.05630				8.714	.02760									
8.641	.01908									7.912	.05594				8.725	.02671									
8.654	.01870				7.099	.10016				7.923	.05558				8.747	.02616									
8.692	.01764				7.121	.09979				7.934	.05419				8.758	.02599									
8.705	.01722				7.132	.09923				7.956	.05344				8.769	.02566									
8.744	.01676				7.143	.09749				7.967	.05288				8.791	.02548									
8.756	.01592				7.165	.09627				7.978	.05218				8.802	.02517									
8.795	.01495				7.176	.09576				8.000	.05202				8.813	.02472									
8.808	.01474				7.187	.09488				8.011	.05178				8.835	.02397									
8.846	.01463				7.209	.09447				8.022	.05088				8.846	.02384									
8.859	.01448				7.220	.09400				8.044	.04915				8.857	.02286									
8.897	.01323				7.231	.09252				8.055	.04899				8.879	.02274									
8.910	.01225				7.253	.09037				8.066	.04793				8.890	.02243									
8.949	.01214				7.264	.08983				8.088	.04783				8.901	.02206									
8.962	.01155				7.275	.08822				8.099	.04737				8.923	.02134									
9.000	.01049				7.297	.08798				8.110	.04687				8.934	.02125									
9.013	.01013				7.308	.08739				8.132	.04589				8.945	.02099									
9.051	.00976				7.319	.08587				8.143	.04566				8.967	.02086									
9.064	.00956				7.341	.08473				8.154	.04516				8.978	.02071									
9.103	.00846				7.352	.08446				8.176	.04488				8.989	.02009									
9.115	.00831				7.363	.08334				8.187	.04454				9.011	.01981									
9.154	.00820				7.385	.08275				8.198	.04333				9.022	.01931									
9.167	.00766				7.396	.08229				8.220	.04277				9.033	.01901									
9.205	.00732				7.407	.08053				8.231	.04247				9.055	.01895									
9.218	.00701				7.429	.07943				8.242	.04184				9.066	.01882									
9.256	.00684				7.440	.07872				8.264	.04163				9.077	.01803									
9.269	.00656				7.451	.07794				8.275	.04144				9.099	.01722									
9.308	.00567				7.473	.07767				8.286	.04078				9.110	.01714									
9.321	.00561				7.484	.07725				8.308	.03957				9.121	.01668									
9.359	.00548				7.495	.07593				8.319	.03925				9.143	.01666									
9.372	.00514				7.516	.07449				8.330	.03856				9.154	.01650									
9.410	.00466				7.527	.07406				8.352	.03840				9.165	.01606									
9.462	.00461				7.538	.07265				8.363	.03791				9.187	.01551									
9.474	.00423				7.560	.07241				8.374	.03733				9.198	.01541									
9.513	.00353				7.571	.07200				8.396	.03663				9.209	.01509									
9.526	.00327				7.582	.07108				8.407	.03648				9.231	.01494									
9.564	.00323				7.604	.06979				8.418	.03584				9.242	.01468									
9.577	.00319				7.615	.06945				8.440	.03560				9.253	.01430									
9.628	.00240				7.626	.06874				8.451	.03546				9.275	.01394									
9.667	.00237				7.648	.06838				8.462	.03446				9.286	.01379									
9.679	.00231				7.659	.06808				8.484	.03390				9.297	.01329									

h		P(H≥h)		h		P(H≥h)		h		P(H≥h)		h		P(H≥h)	
3	3	3	2	2	3	3	3	2	2	3	3	3	3	3	1
9.319	.01323	10.132	.00335	7.033	.10030	9.495	.00921								
9.330	.01307	10.154	.00316	7.077	.09836	9.538	.00865								
9.341	.01283	10.165	.00311	7.121	.09482	9.582	.00803								
9.363	.01191	10.176	.00290	7.165	.09279	9.626	.00782								
9.374	.01170	10.198	.00288	7.209	.08807	9.670	.00687								
9.385	.01129	10.209	.00286	7.253	.08597	9.714	.00674								
9.407	.01123	10.220	.00271	7.297	.08332	9.758	.00609								
9.418	.01110	10.242	.00250	7.341	.08207	9.802	.00590								
9.429	.01082	10.253	.00249	7.385	.07880	9.846	.00493								
9.451	.01053	10.264	.00235	7.429	.07692	9.890	.00481								
9.462	.01045	10.286	.00231	7.473	.07342	9.934	.00432								
9.473	.01015	10.297	.00225	7.516	.07269	9.978	.00423								
9.495	.01008	10.308	.00219	7.560	.06848	10.022	.00374								
9.505	.00999	10.330	.00196	7.604	.06660	10.066	.00342								
9.516	.00940	10.341	.00194	7.648	.06388	10.110	.00273								
9.538	.00905	10.374	.00187	7.692	.06257	10.154	.00266								
9.549	.00893	10.385	.00185	7.736	.06034	10.198	.00254								
9.560	.00876	10.396	.00171	7.780	.05919	10.242	.00235								
9.582	.00868	10.418	.00164	7.824	.05555	10.286	.00188								
9.593	.00861	10.429	.00162	7.868	.05471	10.330	.00181								
9.604	.00835	10.462	.00154	7.912	.05217	10.374	.00171								
9.626	.00790	10.473	.00151	7.956	.05051	10.418	.00165								
9.637	.00785	10.484	.00144	8.000	.04792	10.462	.00133								
9.648	.00759	10.505	.00128	8.044	.04722	10.505	.00131								
9.670	.00755	10.516	.00127	8.088	.04395	10.549	.00100								
9.681	.00744	10.527	.00126	8.132	.04226	10.593	.00096								
9.692	.00732	10.549	.00125	8.176	.04097	10.681	.00071								
9.714	.00699	10.560	.00120	8.220	.04049	10.725	.00041								
9.725	.00684	10.571	.00114	8.264	.03779	10.769	.00038								
9.736	.00666	10.593	.00108	8.308	.03654	10.857	.00036								
9.758	.00662	10.604	.00106	8.352	.03333	10.901	.00021								
9.769	.00656	10.637	.00097	8.396	.03284	10.945	.00018								
9.780	.00610	10.648	.00096	8.440	.03153	11.121	.00012								
9.802	.00580	10.659	.00088	8.484	.03047	11.297	.00006								
9.813	.00576	10.692	.00068	8.527	.02792	11.473	.00002								
9.824	.00562	10.725	.00064	8.571	.02755										
9.846	.00560	10.736	.00062	8.615	.02627	3	3	3	3	2					
9.857	.00553	10.747	.00060	8.659	.02539										
9.868	.00529	10.769	.00050	8.703	.02396	7.181	.10196								
9.890	.00495	10.791	.00045	8.747	.02326	7.210	.09965								
9.901	.00485	10.824	.00044	8.791	.02140	7.219	.09880								
9.912	.00471	10.868	.00036	8.835	.02105	7.248	.09849								
9.934	.00470	10.912	.00033	8.879	.01939	7.257	.09735								
9.945	.00456	10.923	.00031	8.923	.01905	7.286	.09442								
9.956	.00439	10.945	.00025	8.967	.01829	7.295	.09348								
9.978	.00421	10.989	.00025	9.011	.01753	7.324	.09275								
9.989	.00417	11.000	.00022	9.055	.01664	7.333	.09150								
10.000	.00411	11.044	.00021	9.099	.01638	7.362	.09020								
10.022	.00407	11.099	.00017	9.143	.01490	7.371	.08914								
10.033	.00406	11.187	.00009	9.187	.01411	7.400	.08851								
10.044	.00392	11.264	.00007	9.231	.01342	7.410	.08720								
10.066	.00378	11.275	.00003	9.275	.01328	7.438	.08554								
10.077	.00368	11.341	.00002	9.319	.01216	7.448	.08484								
10.088	.00356	11.538	.00002	9.363	.01166	7.476	.08426								
10.110	.00355			9.407	.01030	7.486	.08372								
10.121	.00350			9.451	.00997	7.514	.08176								

EXACT PROBABILITY LEVELS FOR THE KRUSKAL-WALLIS TEST

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h					h					h					h				
P(H ₂ ≥ h)					P(H ₂ ≥ h)					P(H ₂ ≥ h)					P(H ₂ ≥ h)				
3	3	3	3	2	3	3	3	3	2	3	3	3	3	2	3	3	3	3	2
7.524	.08049				8.590	.03587				9.657	.01297				10.724	.00240			
7.552	.08004				8.619	.03560				9.686	.01282				10.752	.00237			
7.562	.07930				8.629	.03528				9.695	.01248				10.762	.00229			
7.590	.07745				8.657	.03400				9.724	.01186				10.790	.00216			
7.600	.07653				8.667	.03339				9.733	.01159				10.800	.00212			
7.629	.07588				8.695	.03312				9.762	.01144				10.829	.00206			
7.638	.07451				8.705	.03263				9.771	.01128				10.838	.00198			
7.667	.07293				8.733	.03195				9.800	.01064				10.867	.00187			
7.676	.07229				8.743	.03159				9.810	.01036				10.876	.00180			
7.705	.07190				8.771	.03137				9.838	.01028				10.905	.00178			
7.714	.07115				8.781	.03093				9.848	.01010				10.914	.00174			
7.743	.06907				8.810	.02985				9.876	.00966				10.943	.00158			
7.752	.06823				8.819	.02959				9.886	.00951				10.952	.00155			
7.781	.06771				8.848	.02939				9.914	.00937				10.981	.00153			
7.790	.06677				8.857	.02901				9.924	.00912				10.990	.00147			
7.819	.06512				8.886	.02811				9.952	.00859				11.019	.00135			
7.829	.06463				8.895	.02766				9.962	.00850				11.029	.00130			
7.857	.06400				8.924	.02738				9.990	.00843				11.057	.00127			
7.867	.06323				8.933	.02689				10.000	.00817				11.067	.00120			
7.895	.06170				8.962	.02621				10.029	.00780				11.095	.00106			
7.905	.06082				8.971	.02585				10.038	.00754				11.133	.00104			
7.933	.06060				9.000	.02556				10.067	.00744				11.143	.00102			
7.943	.05990				9.010	.02515				10.076	.00721				11.171	.00096			
7.971	.05845				9.038	.02452				10.105	.00691				11.181	.00091			
7.981	.05763				9.048	.02419				10.114	.00683				11.210	.00091			
8.010	.05713				9.076	.02402				10.143	.00666				11.219	.00091			
8.019	.05642				9.086	.02376				10.152	.00653				11.248	.00082			
8.048	.05530				9.114	.02292				10.181	.00625				11.257	.00080			
8.057	.05483				9.124	.02251				10.190	.00609				11.286	.00079			
8.086	.05416				9.152	.02224				10.219	.00604				11.295	.00078			
8.095	.05345				9.162	.02189				10.229	.00590				11.324	.00070			
8.124	.05221				9.190	.02117				10.257	.00547				11.333	.00065			
8.133	.05147				9.200	.02093				10.267	.00529				11.362	.00064			
8.162	.05113				9.229	.02069				10.295	.00526				11.371	.00060			
8.171	.05044				9.238	.02022				10.305	.00513				11.400	.00054			
8.200	.04940				9.267	.01975				10.333	.00487				11.410	.00050			
8.210	.04870				9.276	.01934				10.343	.00478				11.438	.00048			
8.238	.04841				9.305	.01916				10.371	.00474				11.448	.00047			
8.248	.04797				9.314	.01889				10.381	.00462				11.476	.00038			
8.276	.04673				9.343	.01799				10.410	.00437				11.486	.00037			
8.286	.04626				9.352	.01752				10.419	.00427				11.514	.00036			
8.314	.04592				9.381	.01749				10.448	.00422				11.524	.00034			
8.324	.04499				9.390	.01724				10.457	.00412				11.552	.00032			
8.352	.04362				9.419	.01664				10.486	.00375				11.590	.00030			
8.362	.04312				9.429	.01649				10.495	.00368				11.600	.00027			
8.390	.04273				9.457	.01634				10.524	.00358				11.629	.00022			
8.400	.04221				9.467	.01592				10.533	.00351				11.638	.00021			
8.429	.04056				9.495	.01537				10.562	.00328				11.667	.00021			
8.438	.04002				9.505	.01501				10.571	.00318				11.676	.00020			
8.467	.03925				9.533	.01486				10.600	.00315				11.743	.00018			
8.476	.03926				9.543	.01467				10.610	.00302				11.752	.00016			
8.505	.03854				9.571	.01407				10.638	.00283				11.781	.00013			
8.514	.03809				9.581	.01396				10.648	.00274				11.829	.00012			
8.543	.03773				9.610	.01372				10.676	.00272				11.867	.00007			
8.552	.03732				9.619	.01352				10.686	.00261				11.905	.00007			
8.581	.03639				9.648	.01324				10.714	.00245				11.933	.00007			

h					h					h					h				
P(H≥h)					P(H≥h)					P(H≥h)					P(H≥h)				
3	3	3	3	2	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3
11.971	.00006				8.833	.03408				10.700	.00510				12.667	.00005			
11.981	.00005				8.867	.03263				10.733	.00492				12.700	.00005			
12.086	.00003				8.900	.03227				10.767	.00478				12.767	.00004			
12.133	.00003				8.933	.03119				10.800	.00437				12.833	.00003			
12.210	.00002				8.967	.03015				10.833	.00426				12.900	.00002			
12.276	.00001				9.000	.02922				10.867	.00387				12.933	.00001			
12.514	.00000				9.033	.02884				10.900	.00362				12.967	.00001			
					9.067	.02787				10.933	.00355				13.033	.00001			
					9.100	.02715				10.967	.00338				13.233	.00000			
					9.133	.02641				11.000	.00319				13.500	.00000			
					9.167	.02608				11.033	.00313								
7.300	.10075				9.200	.02500				11.067	.00288								
7.333	.09922				9.233	.02463				11.100	.00273								
7.367	.09692				9.267	.02330				11.133	.00252								
7.400	.09488				9.300	.02291				11.167	.00246								
7.433	.09383				9.333	.02220				11.200	.00226								
7.467	.09020				9.367	.02169				11.233	.00222								
7.500	.08902				9.400	.02102				11.267	.00196								
7.533	.08670				9.433	.02078				11.300	.00190								
7.567	.08576				9.467	.01970				11.333	.00183								
7.600	.08256				9.500	.01931				11.367	.00173								
7.633	.08100				9.533	.01866				11.400	.00160								
7.667	.07882				9.567	.01840				11.433	.00155								
7.700	.07791				9.600	.01762				11.467	.00135								
7.733	.07665				9.633	.01713				11.500	.00132								
7.767	.07487				9.667	.01647				11.533	.00122								
7.800	.07202				9.700	.01617				11.567	.00119								
7.833	.07139				9.733	.01579				11.600	.00107								
7.867	.06882				9.767	.01521				11.633	.00104								
7.900	.06763				9.800	.01435				11.667	.00093								
7.933	.06573				9.833	.01426				11.700	.00092								
7.967	.06479				9.867	.01357				11.733	.00086								
8.000	.06311				9.900	.01334				11.767	.00080								
8.033	.06220				9.933	.01266				11.800	.00071								
8.067	.06039				9.967	.01235				11.833	.00070								
8.100	.05933				10.000	.01198				11.867	.00060								
8.133	.05741				10.033	.01170				11.900	.00057								
8.167	.05623				10.067	.01130				11.933	.00054								
8.200	.05453				10.100	.01111				11.967	.00051								
8.233	.05410				10.133	.01065				12.000	.00047								
8.267	.05178				10.167	.01036				12.033	.00045								
8.300	.05054				10.200	.00986				12.067	.00041								
8.333	.04955				10.233	.00973				12.100	.00039								
8.367	.04872				10.267	.00903				12.133	.00034								
8.400	.04737				10.300	.00863				12.167	.00033								
8.433	.04641				10.333	.00842				12.233	.00029								
8.467	.04413				10.367	.00822				12.267	.00022								
8.500	.04369				10.400	.00779				12.300	.00021								
8.533	.04269				10.433	.00761				12.333	.00019								
8.567	.04193				10.467	.00697				12.367	.00019								
8.600	.04017				10.500	.00684				12.400	.00016								
8.633	.03967				10.533	.00651				12.433	.00015								
8.667	.03865				10.567	.00627				12.467	.00010								
8.700	.03778				10.600	.00576				12.533	.00009								
8.733	.03681				10.633	.00565				12.567	.00008								
8.767	.03602				10.667	.00526				12.633	.00006								
8.800	.03451																		

Table IV Upper tail probabilities for the null distribution of Friedman's S statistic:

$$k = 3, n = 2(1)13; k = 4, n = 2(1)8; k = 5, n = 3, 4, 5$$

For given k and n , the tabled entry for the point x is $P_0\{S \geq x\}$. Under these conditions, if x is such that $P_0\{S \geq x\} = \alpha$, then $x(\alpha, k, n) = x$. For given k and n , the entries are terminated at $x_{k,n}$, where $x_{k,n}$ is the smallest value of x such that $P_0\{S \geq x\}$ is zero to three decimal places.

$k = 3, n = 2$		$k = 3, n = 5$		$k = 3, n = 7$		$k = 3, n = 8$	
x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$
0	1.000	.0	1.000	.000	1.000	5.25	.079
1	.833	.4	.954	.286	.964	6.25	.047
3	.500	1.2	.691	.857	.768	6.75	.038
4	.167	1.6	.522	1.143	.620	7.00	.030
		2.8	.367	2.000	.486	7.75	.018
		3.6	.182	2.571	.305	9.00	.010
		4.8	.124	3.429	.237	9.25	.008
		5.2	.093	3.714	.192	9.75	.005
$k = 3, n = 3$							
x	$P_0\{S \geq x\}$	6.4	.049	4.571	.112	10.75	.002
0.00	1.000	7.6	.024	5.429	.085	12.00	.001
.667	.944	8.4	.008	6.000	.051	12.25	.001
2.000	.528	10.0	.001	7.143	.027	13.00	.000
2.667	.361			7.714	.021		
4.667	.194	$k = 3, n = 6$		8.000	.016		
6.000	.028			8.857	.008	$k = 3, n = 9$	
				10.286	.004		
				10.571	.003		
				11.143	.001		
				12.286	.000		
$k = 3, n = 4$							
x	$P_0\{S \geq x\}$.000	1.000			.000	1.000
.5	.931	.333	.956			.222	.971
1.5	.653	1.000	.740	$k = 3, n = 8$.667	.814
2.0	.431	1.333	.570			.889	.685
3.5	.273	2.333	.439			1.556	.569
4.5	.125	3.000	.252			2.000	.398
6.0	.069	4.000	.184			2.667	.328
6.5	.042	5.333	.142			2.889	.278
8.0	.005	6.333	.072			3.556	.187
		7.333	.052			4.222	.154
		8.333	.029			4.667	.107
		9.000	.012			5.556	.069
		9.333	.006			6.000	.057
		10.333	.002			6.222	.048
		12.000	.000			6.889	.031
						8.000	.019

Table IV (continued)

$k = 4, n = 6$		$k = 4, n = 7$		$k = 4, n = 8$		$k = 4, n = 8$	
x	$P_0\{S > x\}$	x	$P_0\{S > x\}$	x	$P_0\{S > x\}$	x	$P_0\{S > x\}$
10.8	.006	5.229	.161	.00	1.000	6.60	.081
11.0	.006	5.571	.143	.15	.998	6.75	.079
11.4	.004	5.743	.122	.30	.971	7.05	.068
11.6	.003	5.914	.118	.45	.959	7.20	.060
11.8	.003	6.257	.100	.60	.912	7.35	.058
12.0	.002	6.429	.093	.75	.890	7.50	.051
12.2	.002	6.600	.085	.90	.849	7.65	.049
12.6	.001	6.943	.073	1.05	.837	7.80	.046
12.8	.001	7.114	.063	1.20	.765	7.95	.042
13.0	.001	7.286	.056	1.35	.757	8.10	.038
13.2	.001	7.629	.052	1.50	.710	8.25	.037
13.4	.001	7.800	.041	1.65	.681	8.55	.031
13.6	.000	7.971	.038	1.80	.654	8.70	.028
		8.314	.035	1.95	.629	8.85	.025
		8.486	.033	2.25	.558	9.00	.023
		8.657	.030	2.40	.517	9.15	.022
		9.000	.023	2.55	.507	9.45	.019
		9.171	.020	2.70	.471	9.60	.016
		9.343	.017	2.85	.450	9.75	.015
		9.686	.015	3.00	.404	9.90	.014
		9.857	.013	3.15	.389	10.05	.014
		10.029	.012	3.30	.362	10.20	.011
		10.371	.010	3.45	.350	10.35	.011
		10.543	.009	3.60	.326	10.50	.009
		10.714	.008	3.75	.323	10.65	.009
		11.057	.007	3.90	.287	10.80	.008
		11.229	.005	4.05	.278	10.95	.008
		11.400	.004	4.20	.242	11.10	.006
		11.743	.004	4.35	.226	11.25	.006
		11.914	.003	4.65	.219	11.40	.005
		12.086	.003	4.80	.193	11.55	.005
		12.429	.002	4.95	.191	11.85	.004
		12.600	.002	5.10	.168	12.00	.004
		12.771	.002	5.25	.158	12.15	.004
		13.114	.001	5.40	.148	12.30	.003
		13.286	.001	5.55	.141	12.45	.003
		13.457	.001	5.70	.121	12.60	.002
		13.800	.001	5.85	.117	12.75	.002
		13.971	.001	6.00	.110	12.90	.002
		14.143	.001	6.15	.106	13.05	.002
		14.486	.000	6.30	.100	13.20	.002
				6.45	.094	13.35	.001
						13.50	.001

Table IV (continued)

k = 4, n = 8		k = 5, n = 3		k = 5, n = 4		k = 5, n = 4	
x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$
13.65	.001	8.000	.063	4.8	.329	13.6	.001
13.80	.001	8.267	.056	5.0	.317	13.8	.000
13.95	.001	8.533	.045	5.2	.286		
14.25	.001	8.800	.038	5.4	.275		
14.40	.001	9.067	.028	5.6	.249		
14.55	.001	9.333	.026	5.8	.227		
14.70	.001	9.600	.017	6.0	.205		
14.85	.000	9.867	.015	6.2	.197		
		10.133	.008	6.4	.178		
		10.400	.005	6.6	.161		
		10.667	.004	6.8	.143		
		10.933	.003	7.0	.136		
		11.467	.001	7.2	.121		
		12.000	.000	7.4	.113		
				7.6	.095		
				7.8	.086		
				8.0	.080		
				8.2	.072		
				8.4	.063		
				8.5	.060		
				8.8	.049		
				9.0	.043		
				9.2	.038		
				9.4	.035		
				9.6	.028		
				9.8	.025		
				10.0	.021		
				10.2	.019		
				10.4	.017		
				10.6	.014		
				10.8	.011		
				11.0	.010		
				11.2	.008		
				11.4	.007		
				11.6	.006		
				11.8	.005		
				12.0	.004		
				12.2	.004		
				12.4	.003		
				12.6	.002		
				12.8	.002		
				13.0	.001		
				13.2	.001		
				13.4	.001		

k = 5, n = 3		k = 5, n = 4	
x	$P_0\{S \geq x\}$	x	$P_0\{S \geq x\}$
.000	1.000	.00	1.000
.267	1.000	.16	1.000
.533	.988	.32	.994
.800	.972	.48	.986
1.067	.941	.64	.972
1.333	.914	.80	.958
1.600	.845	.96	.932
1.867	.831	1.12	.925
2.133	.768	1.28	.891
2.400	.720	1.44	.865
2.667	.682	1.60	.842
2.933	.649	1.76	.823
3.200	.595	1.92	.789
3.467	.559	2.08	.765
3.733	.493	2.24	.721
4.000	.475	2.40	.707
4.267	.432	2.56	.679
4.533	.406	2.72	.657
4.800	.347	2.88	.613
5.067	.326	3.04	.594
5.333	.291	3.20	.562
5.600	.253	3.36	.535
5.867	.236	3.52	.518
6.133	.213	3.68	.494
6.400	.172	3.84	.454
6.667	.163	4.00	.443
6.933	.127	4.16	.410
7.200	.117	4.32	.398
7.467	.096	4.48	.371
7.733	.080	4.64	.349
		4.80	.325
		4.96	.316
		5.12	.295
		5.28	.275
		5.44	.255
		5.60	.246

Table IV (continued)

$k = 5, n = 5$		$k = 5, n = 5$		$k = 5, n = 5$		$k = 5, n = 5$	
λ	$P_0\{S > x\}$	x	$P_0\{S > x\}$	λ	$P_0\{S > x\}$	x	$P_0\{S > x\}$
5.76	.227	8.16	.077	10.56	.019	12.96	.003
5.92	.218	8.32	.073	10.72	.018	13.12	.003
6.08	.195	8.48	.066	10.88	.015	13.28	.003
6.24	.183	8.64	.058	11.04	.013	13.44	.002
6.40	.174	8.80	.056	11.20	.012	13.60	.002
6.56	.164	8.96	.049	11.36	.012	13.76	.002
6.72	.151	9.12	.046	11.52	.010	13.92	.002
6.88	.146	9.28	.042	11.68	.009	14.08	.001
7.04	.130	9.44	.038	11.84	.008	14.24	.001
7.20	.121	9.60	.035	12.00	.007	14.40	.001
7.36	.112	9.76	.032	12.16	.006	14.56	.001
7.52	.107	9.92	.029	12.32	.006	14.72	.001
7.68	.094	10.08	.026	12.48	.005	14.88	.001
7.84	.089	10.24	.024	12.64	.004	15.04	.000
8.00	.082	10.40	.022	12.80	.004		

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16. Abstract This report contains two natural distinct parts: (i) Discussion of nonparametric methods that are available for NASA-type applications. An attempt will be made here to survey what can be used, to attempt recommendations as to when each would be applicable, and to compare the methods, when possible, with the usual normal-theory procedures that are available for the Gaussian analog. It is important here to point out the hypotheses that are being tested, the assumptions that are being made, and limitations of the nonparametric procedures. (ii) Discussion and study of the appropriateness of doing analysis of variance on sample variances. This procedure is followed in several NASA simulation projects. On the surface this would appear to be a reasonably sound procedure. However, difficulties involved center around the normality problem and the basic homogeneous variance assumption that is made in usual analysis of variance problems. These difficulties will be discussed and guidelines will be given for using the method.					
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