

V. Maulerova-Subert, I. Dawson,
E. Garutti, M.Moll



NIEL (non-ionizing energy loss)

Simulations and displacement damage studies towards a more complex NIEL concept for radiation damage modelling and prediction,

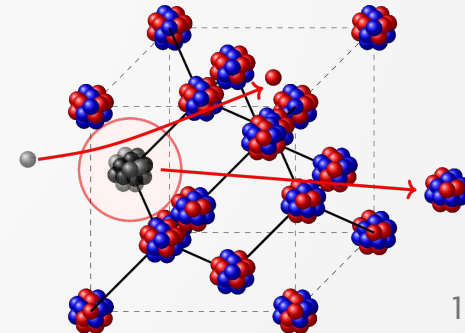


Previous RD50 contributions:

<https://indico.cern.ch/event/1074989/contributions/4601973/> (Valencia)

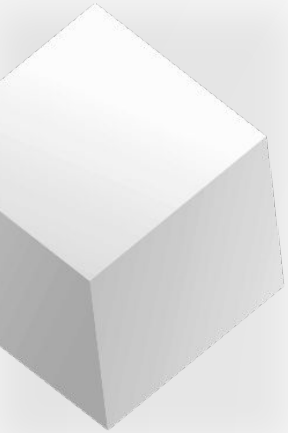
<https://indico.cern.ch/event/1157463/contributions/4922734/> (CERN)

<https://indico.cern.ch/event/1132520/contributions/5147237/> (Seville)

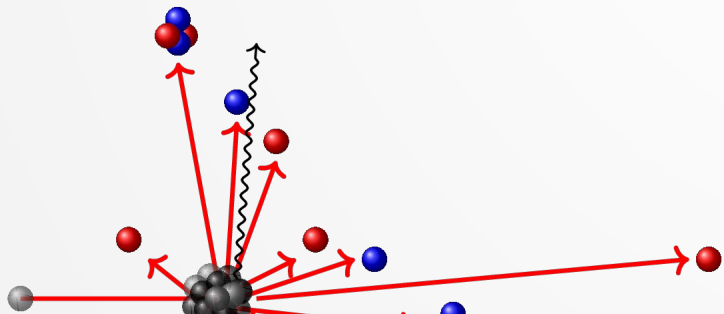


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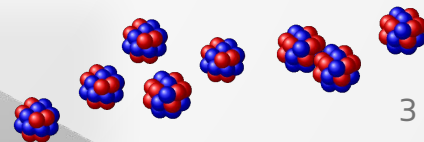
1. The **NIEL** hypothesis & motivation for this study
2. **Overview** of the **Integration of simulations**
3. **Geant4**: simulations of Primary knocked-on atoms (**PKA**) <- 3GeV-24 GeV newly simulated (corrected physics list)
4. **TRIM**: Secondary recoils and atomic cascades
5. **OPTICS**: (Ordering points to identify clustering structure): Isolated vs clustered defects (new Integration of TRIM and OPTICS)
6. **Atomic displacements** produced by high energy particles
 - a. NIEL curve updated (New integration of G4 and TRIM)
 - b. Clustered vs. isolated defects (New integration of G4, TRIM and OPTICS)
7. **Summary** and next steps



The NIEL hypothesis & motivation for this study

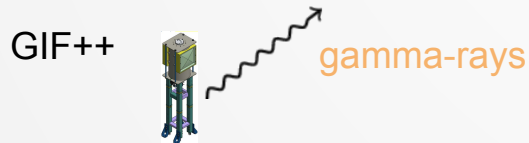
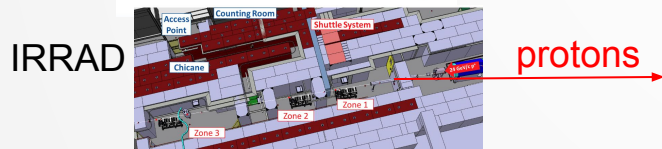
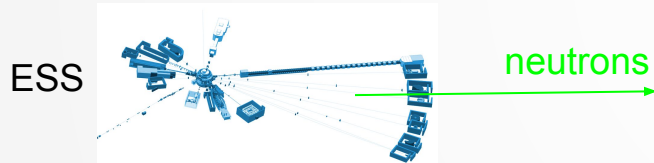


42st RD50 Workshop, 20.06.2023
Vendula Maulerova-Subert



NIEL (non-ionizing energy loss)

- **NIEL** is a physical quantity describing the non-ionizing energy loss as the particle travels through the medium.
- The amount of **NIEL** can be correlated to the amount of radiation damage (NIEL scaling model) and therefore to predict the life time of the detectors
- **NIEL scaling assumption is used by the LHC experiments and beyond** (fluence is expressed in ~ 1 MeV neutron eq. ~ 95 MeV mb)



- **Long term goal:** revisit the damage factors stated by different irradiation facilities and used by the experiments.

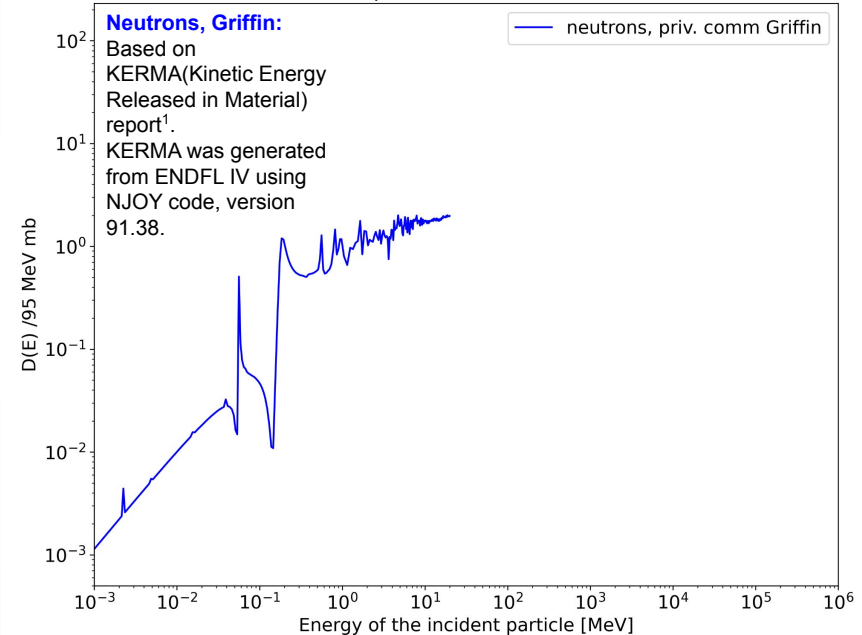
NIEL (non-ionizing energy loss)

$$NIEL(T_0) = \frac{N_A}{A} \sum_i \int_{T_{min}}^{T_{max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$

For Silicon in RD-48 collaboration, A. Vasilescu and G. Lindstrom collected data for neutrons, protons, electrons and pions.

- T_0 : energy of incident particle
- T : energy transferred to the recoil atom
- $(d\sigma/dT)$: differential partial cross section for a particle with energy T_0 to create a recoil atom with energy T in the i -th reaction
- $Q(T)$: partition factor giving the fraction of T that is going into further displacements
- N_A : Avogadro number
- A : atomic mass of target atom

NIEL compared to reference values.



1) P.J. Griffin et al., SAND92-0094 (Sandia Natl. Lab.93), priv. comm. 1996: E = 1.025E-10 - 1.995E+01 MeV, (<https://raw.githubusercontent.com/njoy/NJOY2016-manual/master/njoy16.pdf> (page 120-130 for KERMA and damage))

Displacement damage function

$$NIEL(T_0) = \frac{N_A}{A} D(T)$$

↓
MeV cm²/g

↓
MeV mb

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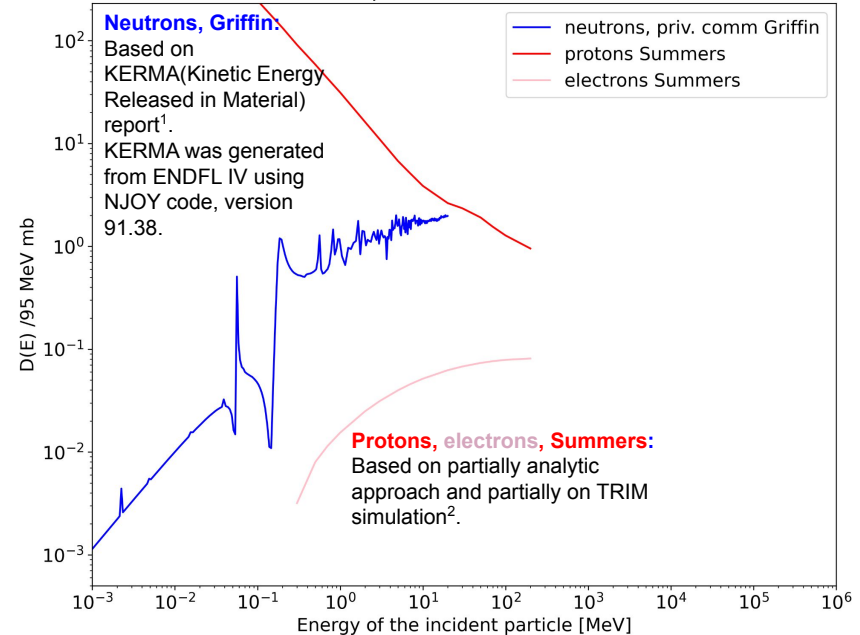
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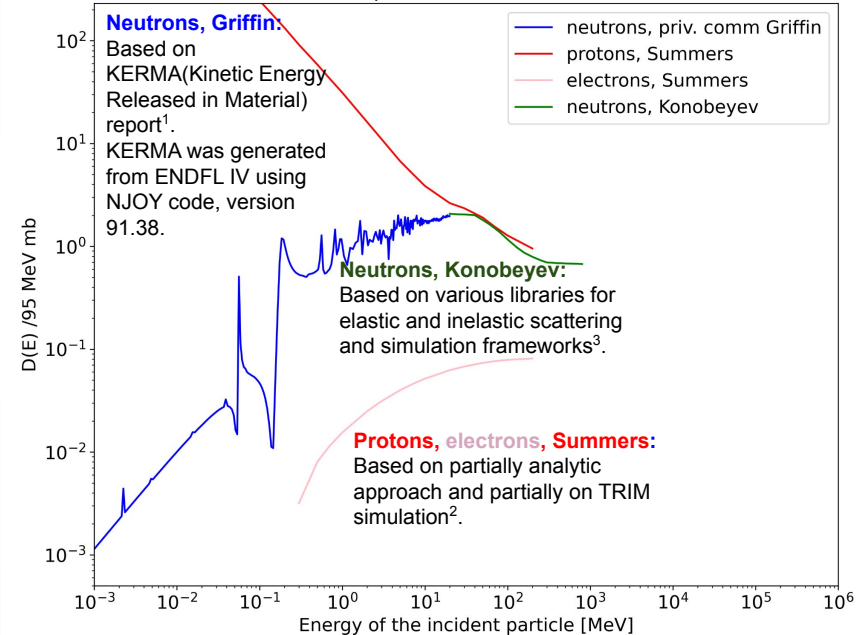
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- 3) Konobeyev, Alexander Yu., et al. "Nuclear Data to Study Damage in Materials under Irradiation by Nucleons with Energies up to 25 GeV." Journal of Nuclear Science and Technology, vol. 39, no. sup2, Aug. 2002, pp. 1236-39. Taylor and Francis+NEJM, <https://doi.org/10.1080/00223131.2002.10875327>.

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Displacement damage function

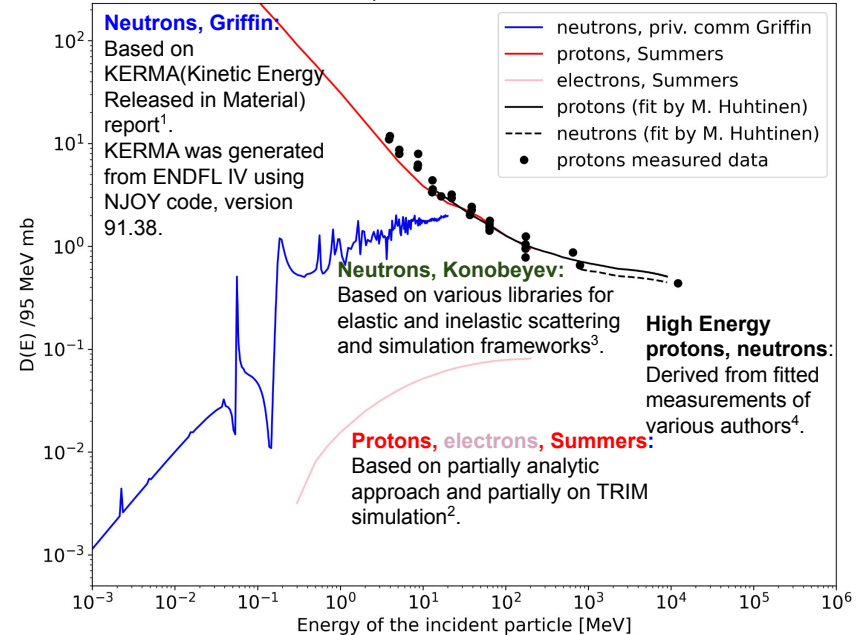
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- 4) Huhtinen, M., and P. A. Aarnio. "Pion Induced Displacement Damage in Silicon Devices." Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, vol. 335, no. 3, Nov. 1993, pp. 580-82. ScienceDirect, [https://doi.org/10.1016/0168-9002\(93\)91246-J](https://doi.org/10.1016/0168-9002(93)91246-J).

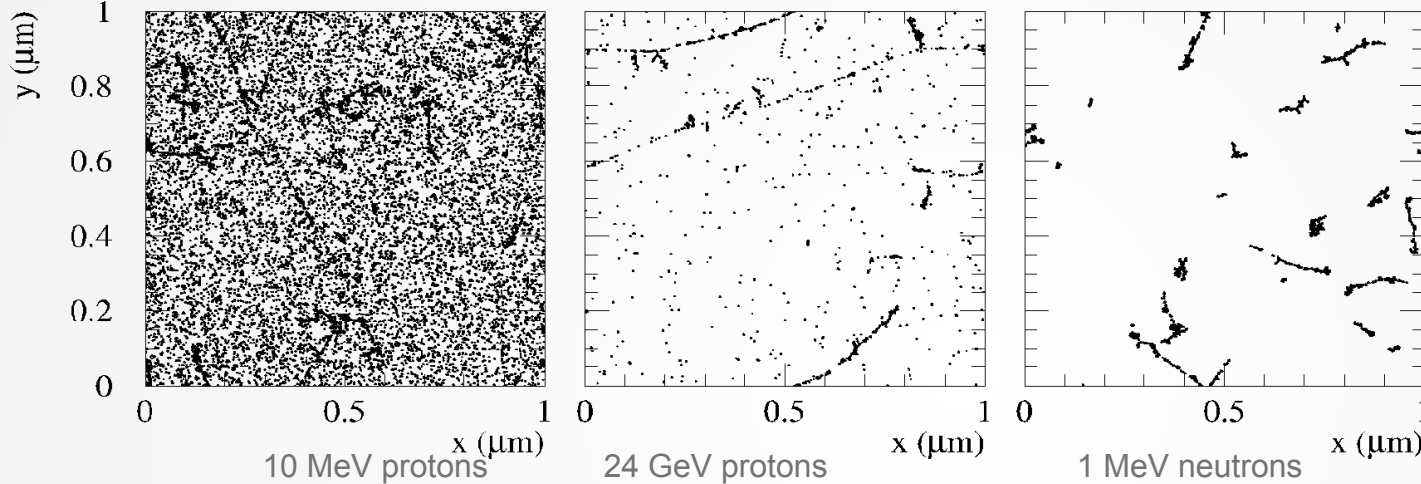
Revisiting NIEL

Simulations of radiation damage by M. Huhtinen⁵.

36824 vacancies

4145 vacancies

8870 vacancies



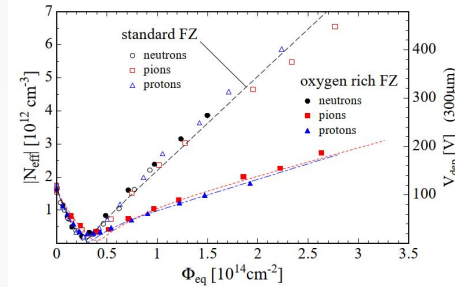
- NIEL doesn't distinguish between cluster and point displacement, i.e. the same displacement energy has a very different distribution of damage on the microscopic level.
- NIEL scaling violation reported in oxygen enriched silicon samples (CERN RD-48, $V_{dep}(\Phi_{eq})$ dependence on particle type), differences between neutron's and proton's damage.

5) Huhtinen, M. "Simulation of Non-Ionising Energy Loss and Defect Formation in Silicon." Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, vol. 491, no. 1, Sept. 2002, pp. 194–215. ScienceDirect, [https://doi.org/10.1016/S0168-9002\(02\)01227-5](https://doi.org/10.1016/S0168-9002(02)01227-5).

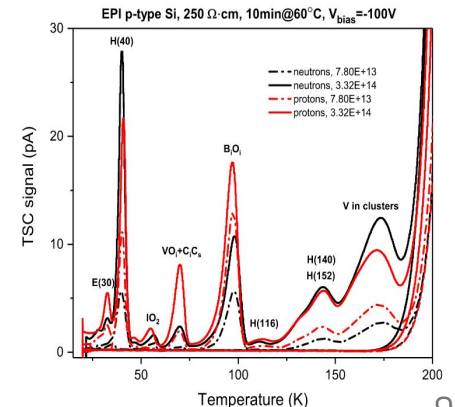
6) G. Lindström et al., Nucl. Instrum. Meth. A466 (2001) 308, doi:10.1016/S0168-9002(01)00560-5.

7) Gurimskaya, Yana, et al. "Radiation Damage in P-Type EPI Silicon Pad Diodes Irradiated with Protons and Neutrons." Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, vol. 958, Apr. 2020, p. 162221. ScienceDirect, <https://doi.org/10.1016/j.nima.2019.05.062>.

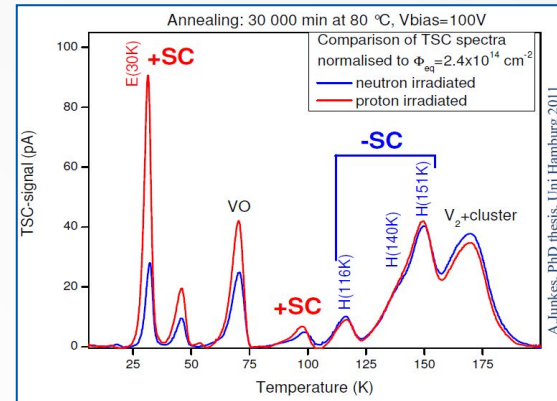
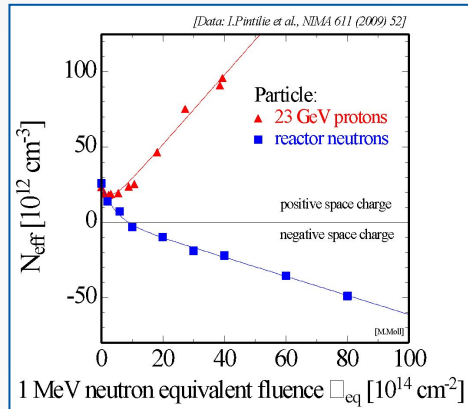
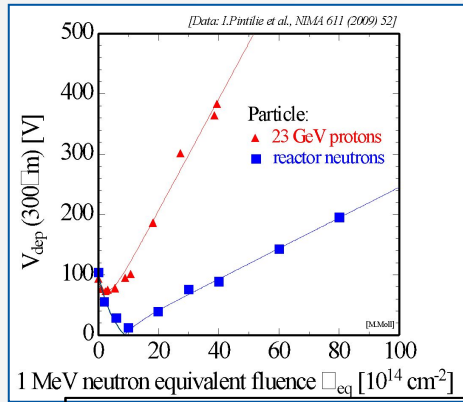
CERN RD48 : oxygen enriched silicon sensors⁶.



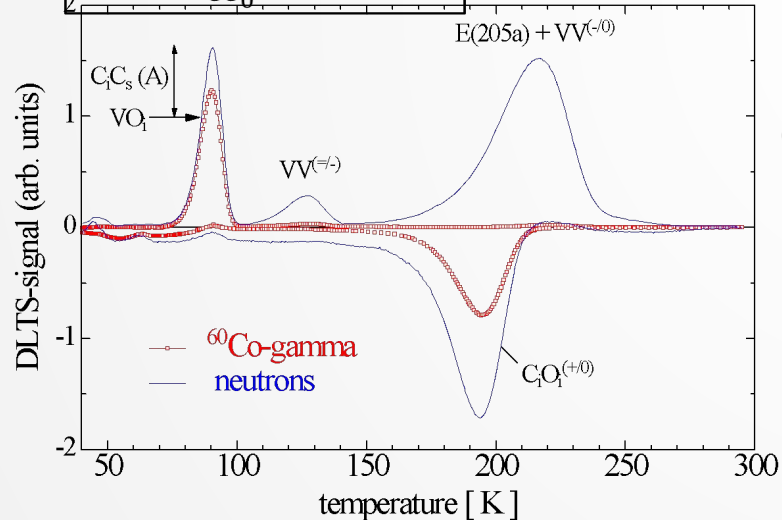
Radiation Damage in P-Type EPI Silicon Pad Diodes Irradiated with Protons and Neutrons⁷.



Revisiting NIEL



$$V_{dep} = \frac{q_0}{\epsilon \epsilon_0} \cdot |N_{eff}| \cdot d^2$$



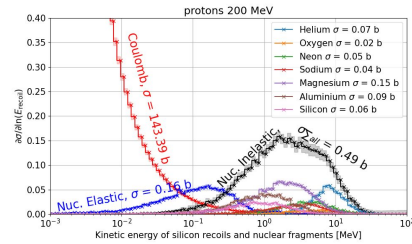
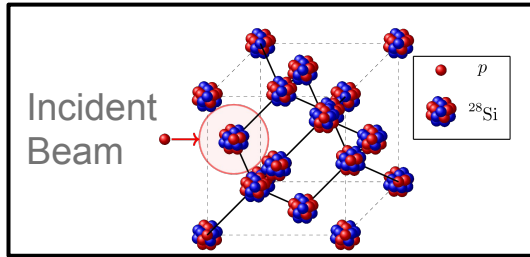
Protons: no space charge inversion
 Neutron: space inversion

From the microscopic perspective: (DLTS measurement)
 Gamma irradiation: only point defects
 Neutron irradiation: cluster and point defects

Therefore the aim of this study is to **partition NIEL function into cluster contribution and point defects contribution.**

Overview of the simulations

GEANT4 \longrightarrow PKA distribution

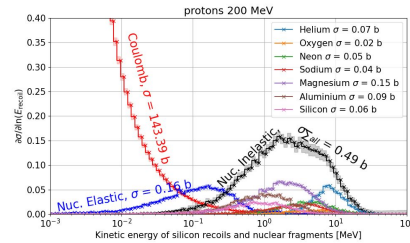
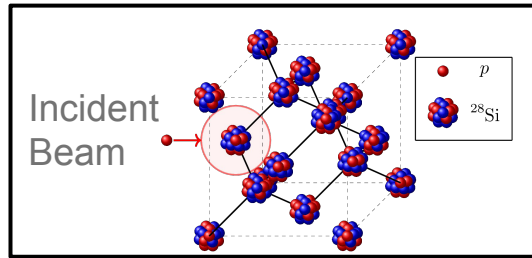


Overview of the simulations

GEANT4



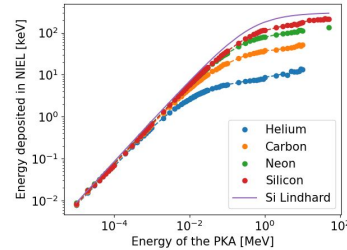
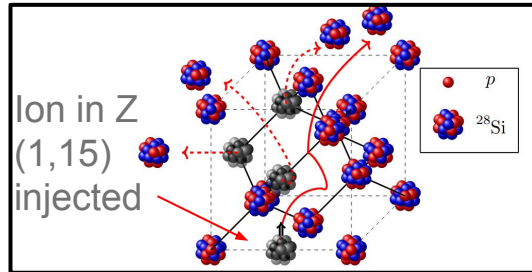
PKA distribution



TRIM



NIEL of low E recoils

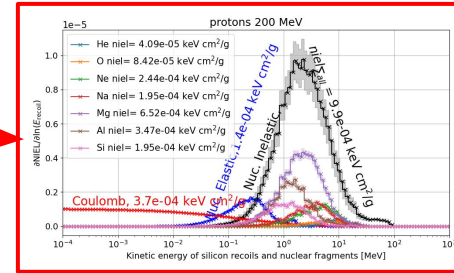
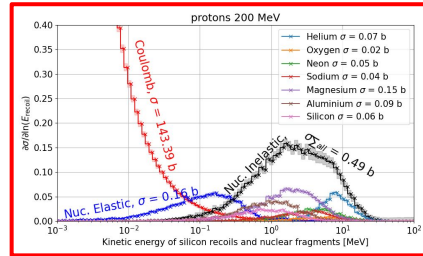
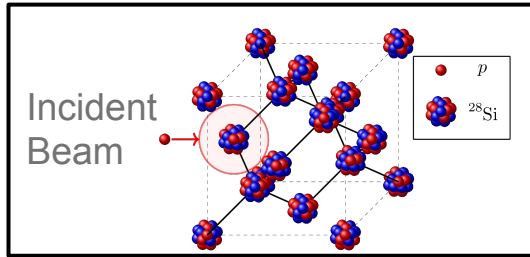


Overview of the simulations

GEANT4

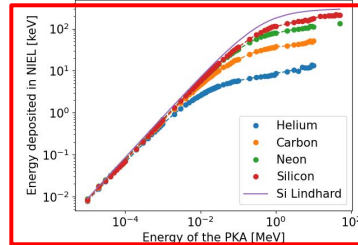
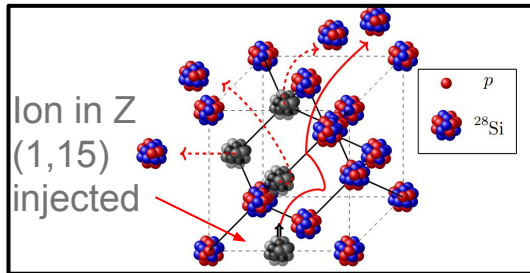
PKA distribution

NIEL/NIEL_{vac} distribution for high E particles



TRIM

NIEL of low E recoils

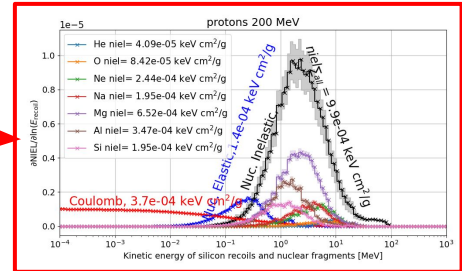
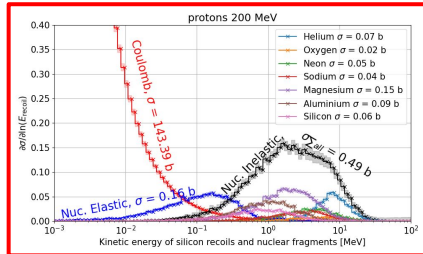
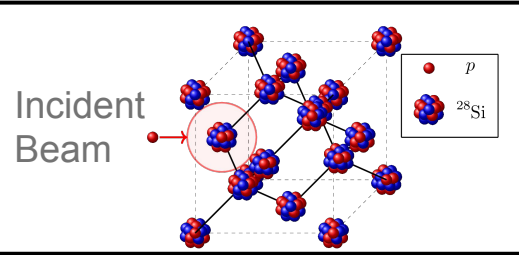


Overview of the simulations

GEANT4

PKA distribution

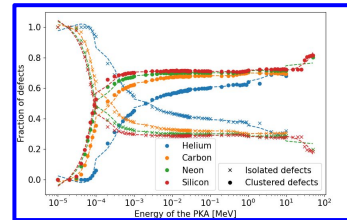
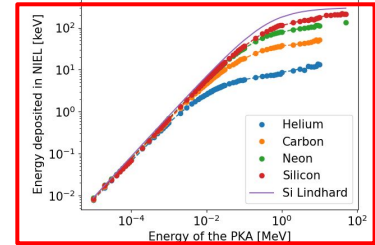
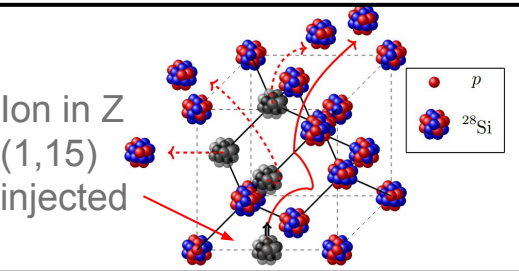
NIEL/NIEL_{vac} distribution for high E particles



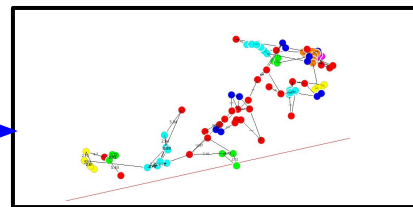
TRIM

NIEL of low E recoils

Isolated/Clustered for low E recoils



OPTICS

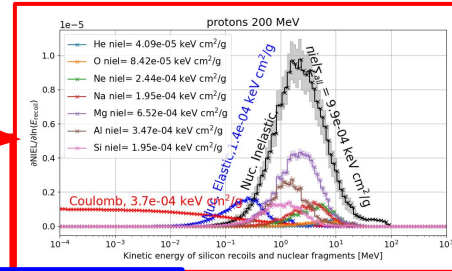
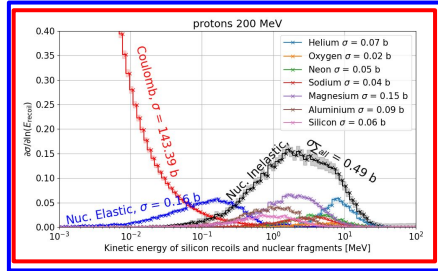
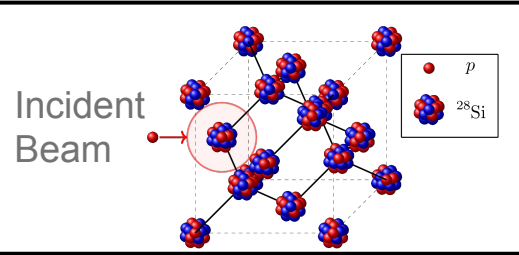


Overview of the simulations

GEANT4

PKA distribution

NIEL/NIEL_{vac} distribution for high E particles

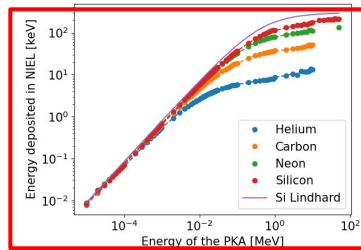
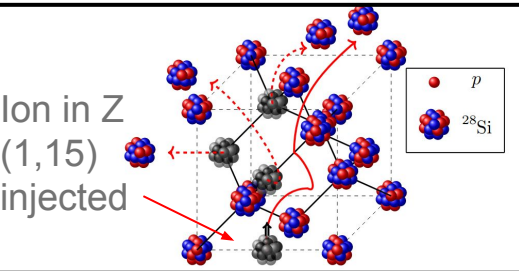


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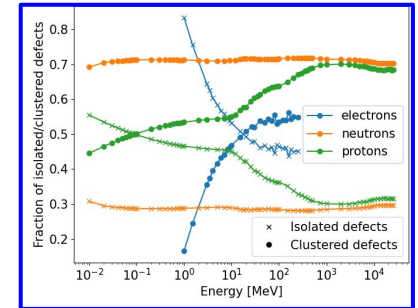
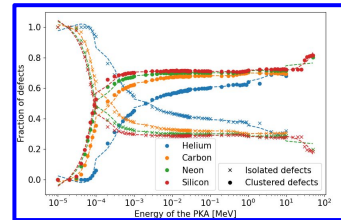
NIEL of low E recoils

Isolated/Clustered for low E recoils

Isolated/Clustered for high E recoils

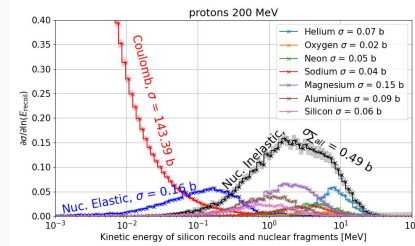
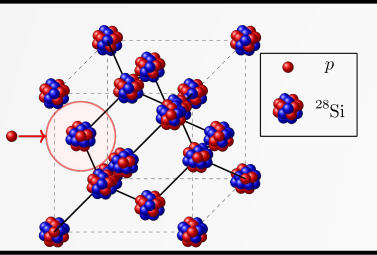


OPTICS



Geant4: Simulation of the Primary knocked-on atoms (PKA)

GEANT4 \longrightarrow PKA distribution



Geant4 simulation framework

Geant4^{8,9}(for GEometry ANd Tracking) is a Monte Carlo simulation platform for the passage of particles through matter.

Define a geometry:



1mm x1 mm x100 μm

Choose a physics list:

1. For PKA (Primary knocked-on atoms):
 - a. *QGSP_BERT_HP* (Nuclear scattering < 3 GeV)
 - b. *QGSP_BERT_HP__SS* (Coulomb scattering for electrons)
 - c. ***FTFP_BERT_HP (Nuclear scattering > 3 GeV)***

New!

Launch a simulation:

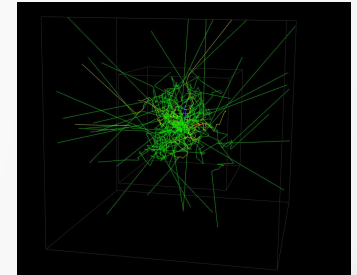
QGSP_BERT_HP
QGSP_BERT_HP__SS

Define a beam profile:



1. Monochromatic pencil beam protons and neutrons of various energies (generally 10^6 - 10^8).
2. For electrons, also 1 μm x 1 μm beam investigated.

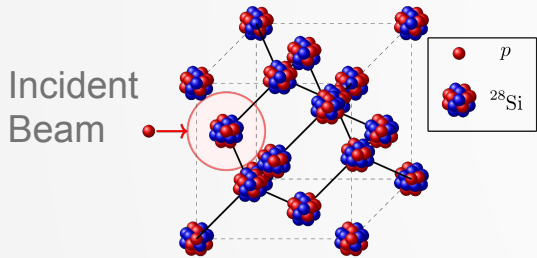
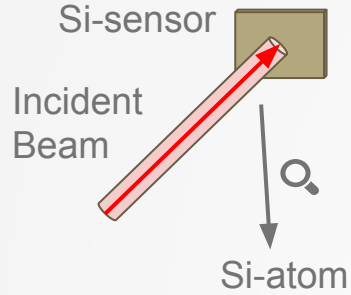
**Analyze (c++, python),
Save results.**



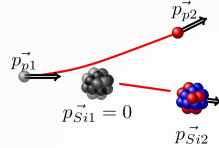
8) Agostinelli, S., et al. "Geant4—a Simulation Toolkit." Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, D Detectors and Associated Equipment, vol. 506, no. 3, July 2003, pp. 250–303. ScienceDirect, [https://doi.org/10.1016/S0168-9002\(03\)01368-8](https://doi.org/10.1016/S0168-9002(03)01368-8).

9) Allison, J., K. Amako, J. Apostolakis, H. Araujo, et al. "Geant4 Developments and Applications." IEEE Transactions on Nuclear Science, vol. 53, no. 1, Feb. 2006, pp. 270–78. IEEE Xplore, <https://doi.org/10.1109/TNS.2006.869826>.

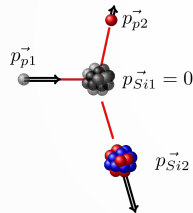
PKA generation example



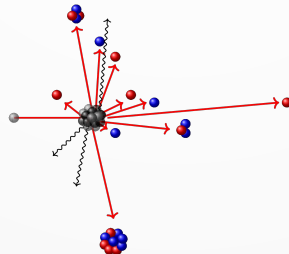
1) Coulomb elastic scattering (only charged particles)



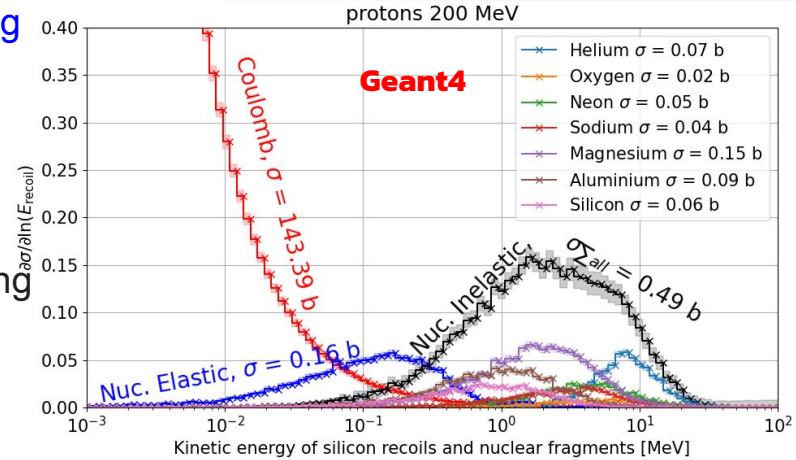
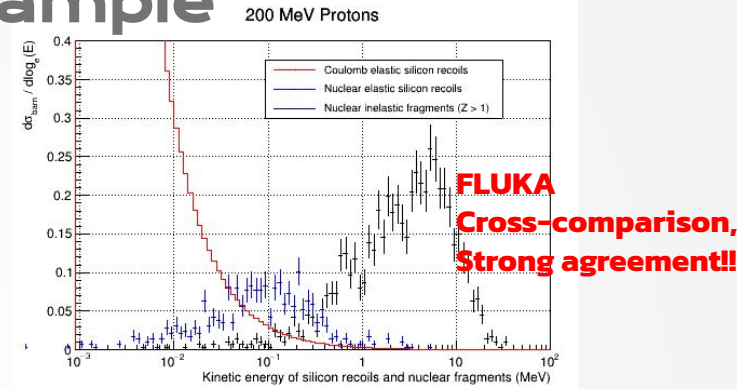
2) Nuclear elastic scattering



3) Nuclear inelastic scattering

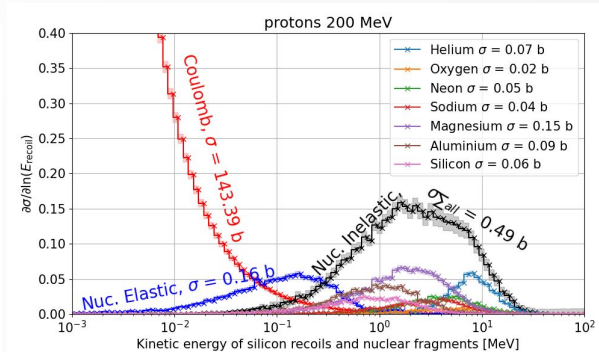
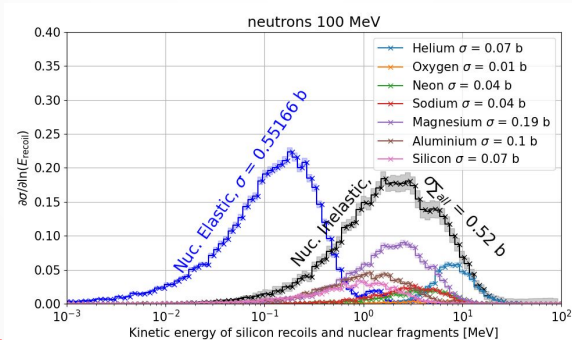
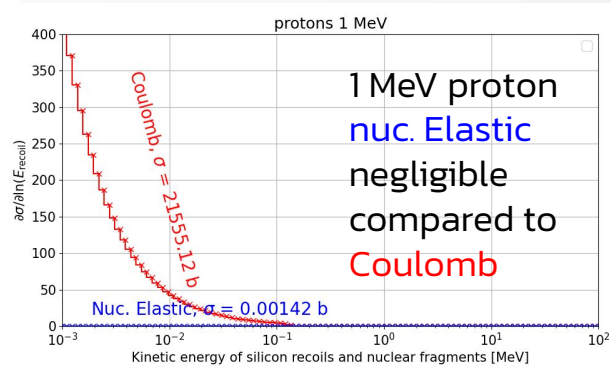
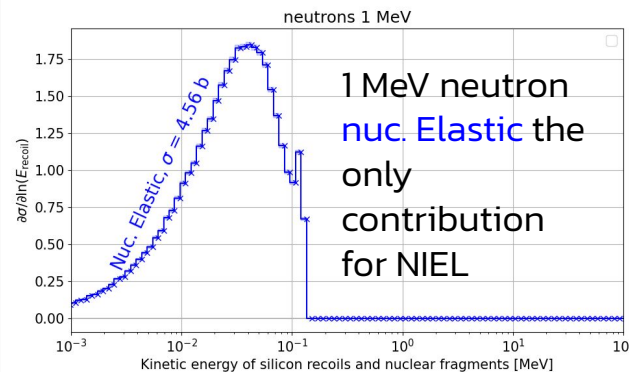
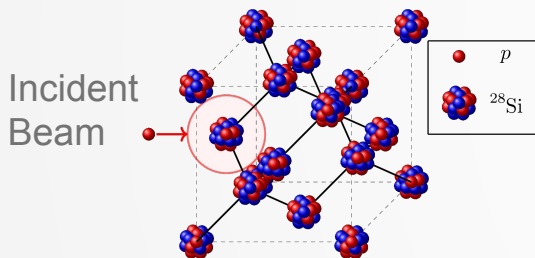
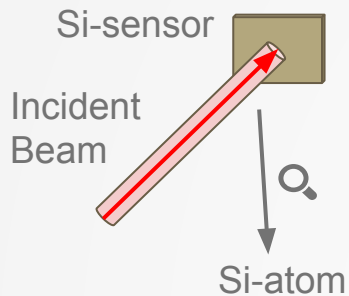


$$NIEL(T_0) = \frac{N_A}{A} \sum_i \int_{T_{min}}^{T_{max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$



Area below the curve corresponds to the cross section. Displacement threshold = **21 eV**.

PKA generation examples



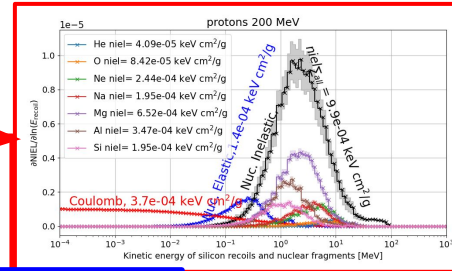
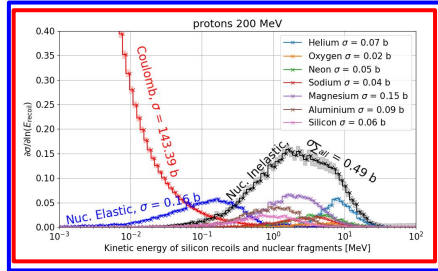
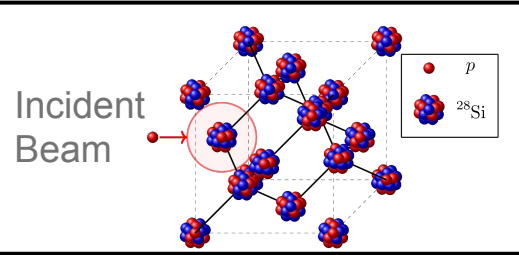
$$NIEL(T_0) = \frac{N_A}{A} \sum_i \int_{T_{\min}}^{T_{\max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$

Overview of the simulations

GEANT4

PKA distribution

NIEL/NIEL_{vac} distribution for high E particles

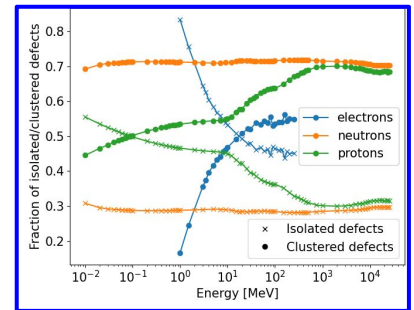
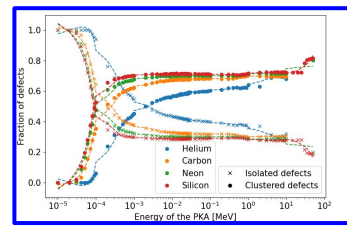
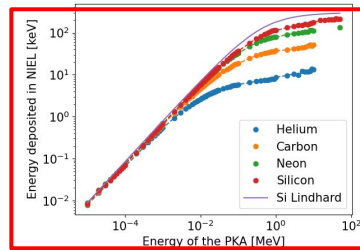
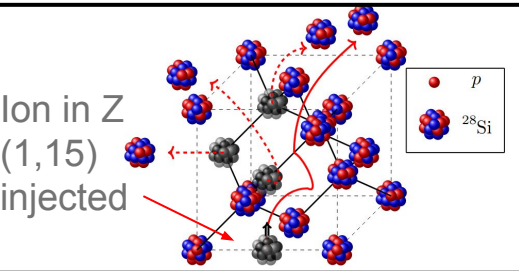


TRIM

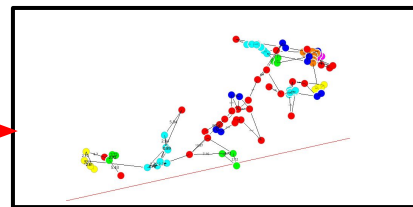
NIEL of low E recoils

Isolated/Clustered for low E recoils

Isolated/Clustered for high E recoils



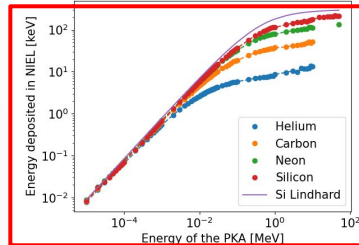
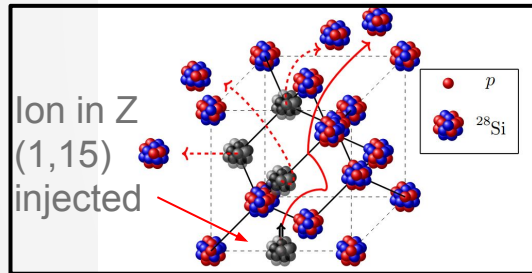
OPTICS



TRIM: Secondary recoils and atomic cascades

TRIM

NIEL of low E recoils



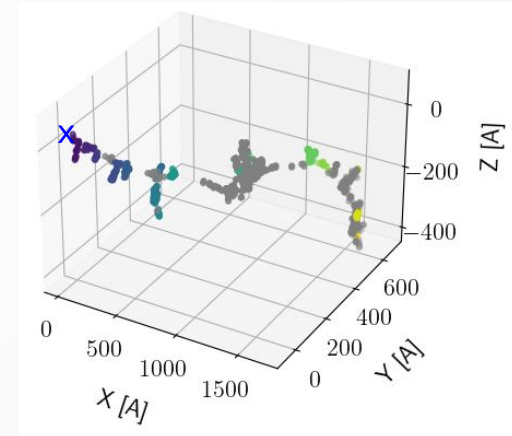
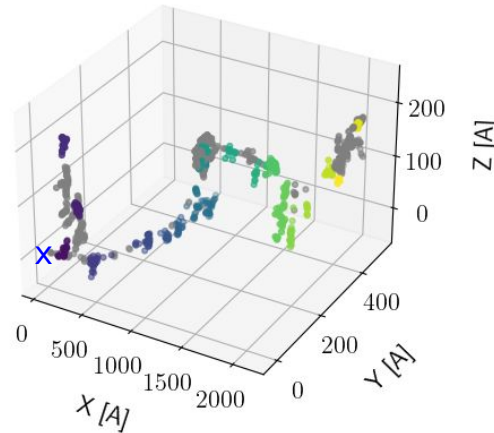
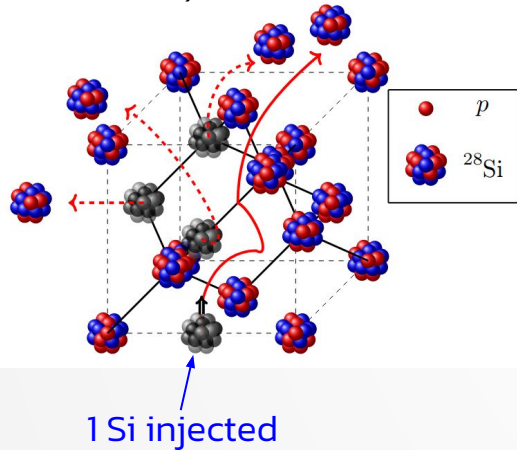
TRIM: 3D representation of 100 keV Si cascade

- TRIM simulations^{10,11}
- TRIM based on Binary Collision Approximation
- focus on the propagation of Si-recoil in Silicon (no incident beam)

Example:

- 100 keV Silicon track
- originating from [the blue cross](#) (position 0,0,0)
- initial momentum in +x direction

Grey dots: isolated displacements
 Colored dots: clustered displacements

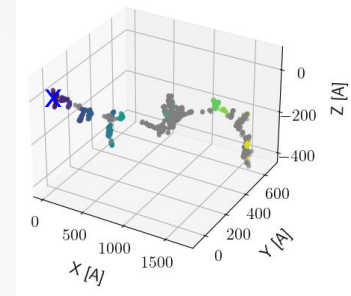


10) SRIM, the Stopping and Range of Ions in Matter, James F. Ziegler, J. P. Biersack, Matthias D. Ziegler
 11) www.srim.org

TRIM ionizing vs. non-ionizing energy

From TRIM it is possible to obtain:

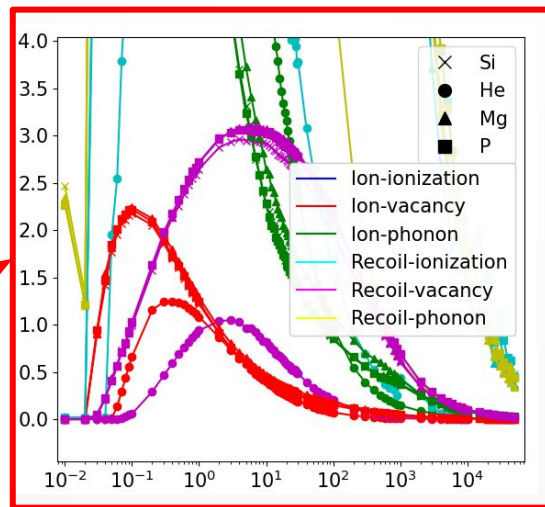
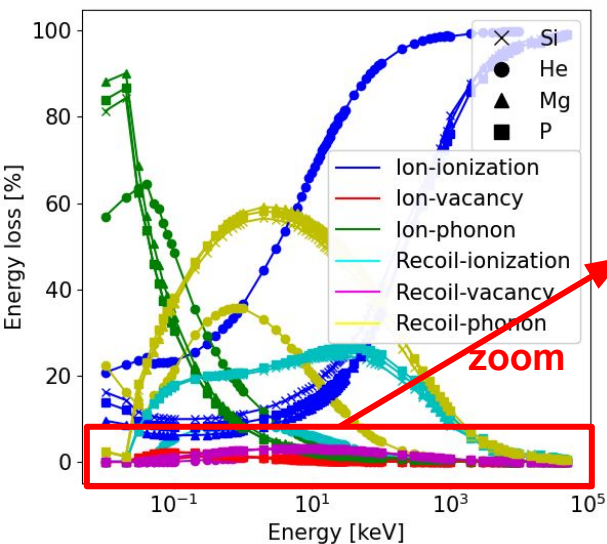
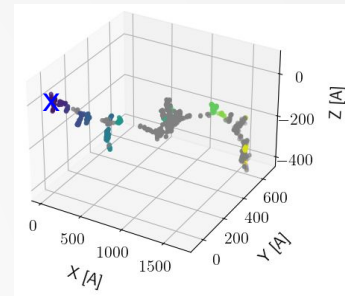
- Spatial distribution of the vacancies created by the low-energy recoils



TRIM ionizing vs. non-ionizing energy

From TRIM it is possible to obtain:

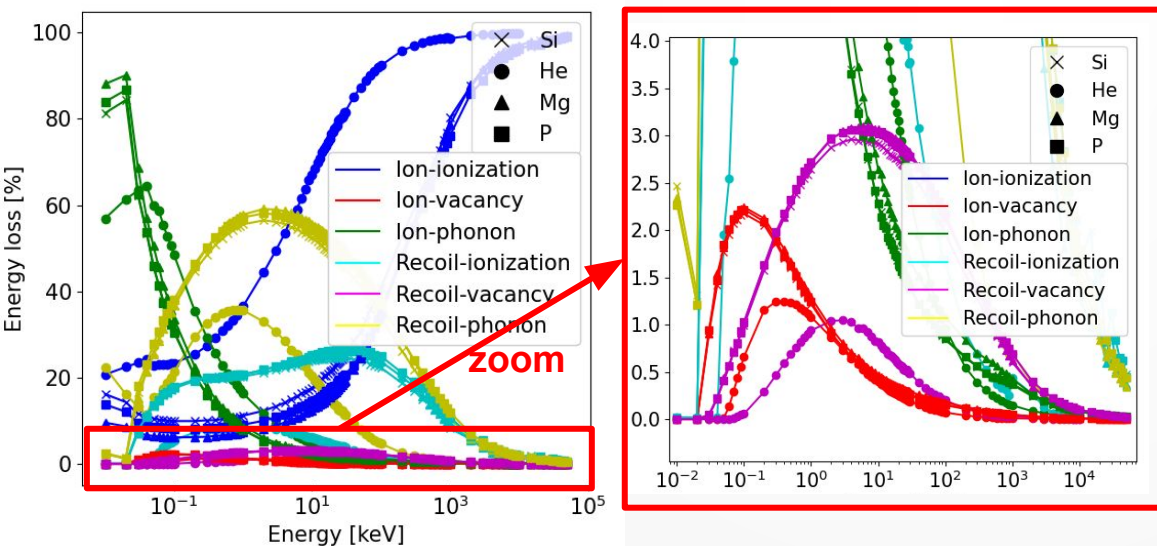
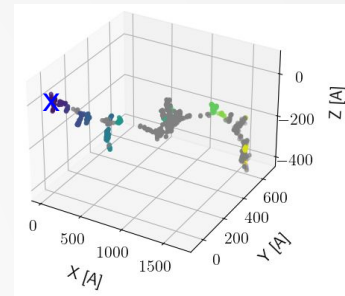
- Spatial distribution of the vacancies created by the low-energy recoils
- Fraction of the energy that is carried out by the:
 - Ionizing energy by the incident ion (lon-ionization) or by the recoils (Recoil-ionization)
 - Phonon energy by the incident ion (lon-phonon) or by the recoils (Recoil-phonon)
 - Energy transferred to kinetic and release energy of the vacancies (lon-vacancy, lon-phonon)



TRIM ionizing vs. non-ionizing energy

From TRIM it is possible to obtain:

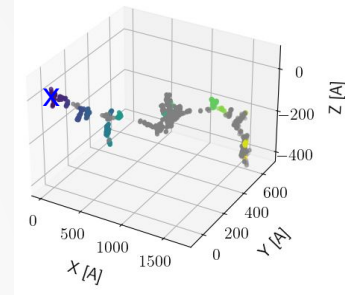
- Spatial distribution of the vacancies created by the low-energy recoils
- Fraction of the energy that is carried out by the:
 - Ionizing energy by the incident ion (Ion-ionization) or by the recoils (Recoil-ionization)
 - Phonon energy by the incident ion (Ion-phonon) or by the recoils (Recoil-phonon)
 - Energy transferred to kinetic and release energy of the vacancies (Ion-vacancy, Ion-phonon)
- $NIEL = I_{\text{ion-vacancy}} + I_{\text{ion-phonon}} + \text{Recoil}_{\text{ion-vacancy}} + \text{Recoil}_{\text{ion-phonon}}$



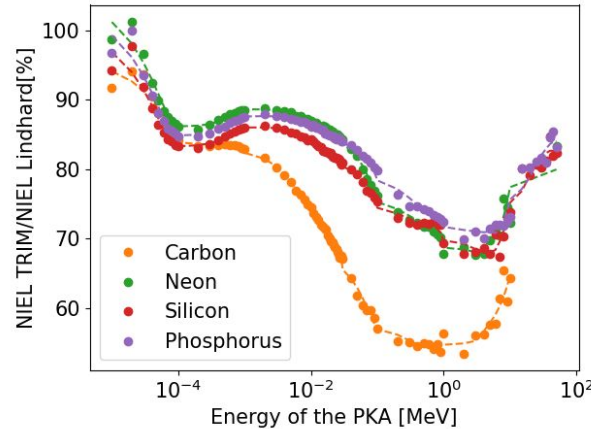
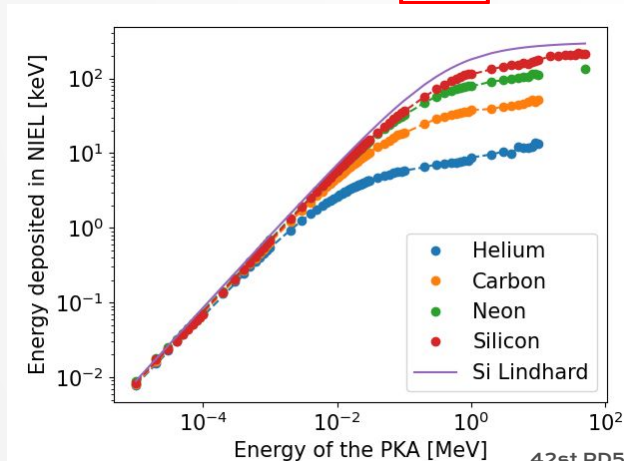
TRIM ionizing vs. non-ionizing energy

From TRIM it is possible to obtain:

- Spatial distribution of the vacancies created by the low-energy recoils
- Fraction of the energy that is carried out by the:
 - Ionizing energy by the incident ion (Ion-ionization) or by the recoils (Recoil-ionization)
 - Phonon energy by the incident ion (Ion-phonon) or by the recoils (Recoil-phonon)
 - Energy transferred to kinetic and release energy of the vacancies (Ion-vacancy, Ion-phonon)
- $NIEL = \text{Ion}_{\text{vacancy}} + \text{Ion}_{\text{phonon}} + \text{Recoil}_{\text{vacancy}} + \text{Recoil}_{\text{phonon}}$



$$NIEL(T_0) = \frac{N_A}{A} \sum_i \int_{T_{min}}^{T_{max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$



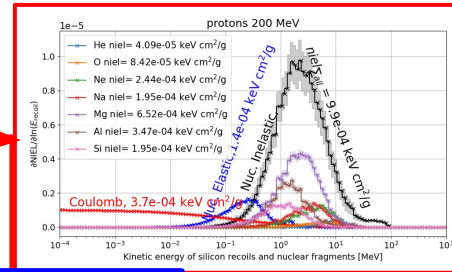
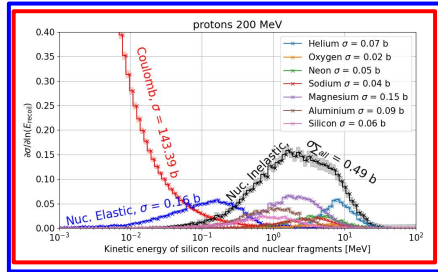
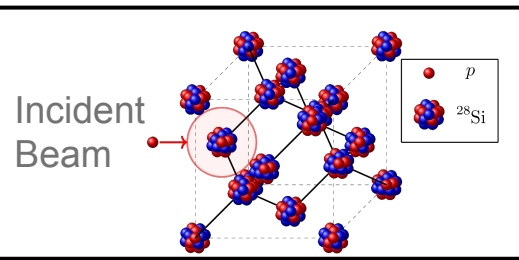
- Alternative simplified solution used before: Lindhard¹² equations are overestimating the NIEL.
- Specifically this difference becomes very pronounced at high energies.
- Lindhard should not be used for low Z ions.

Overview of the simulations

GEANT4

PKA distribution

NIEL/NIEL_{vac} distribution for high E particles

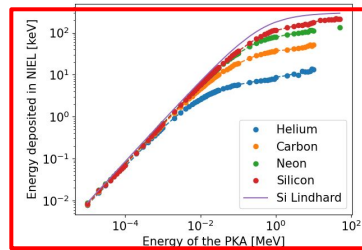
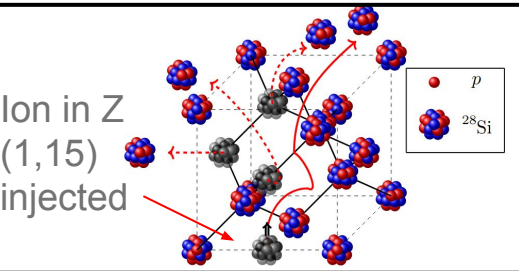


TRIM

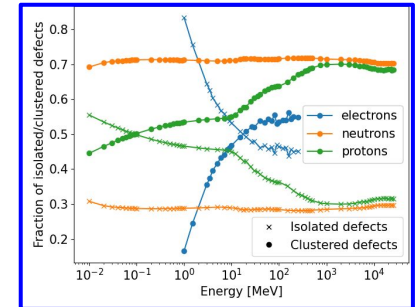
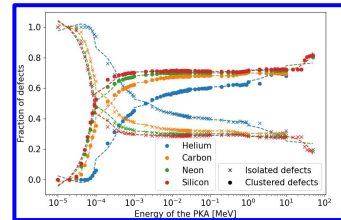
NIEL of low E recoils

Isolated/Clustered for low E recoils

Isolated/Clustered for high E recoils

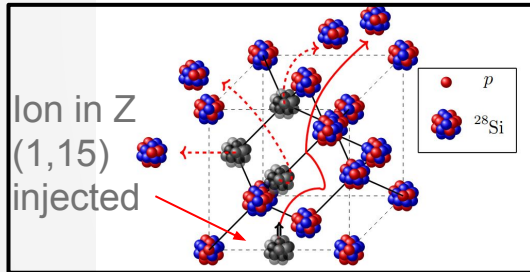


OPTICS

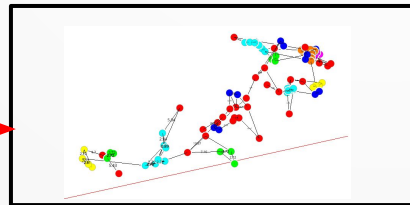


OPTICS^{15,16} (Ordering points to identify the clustering structure)

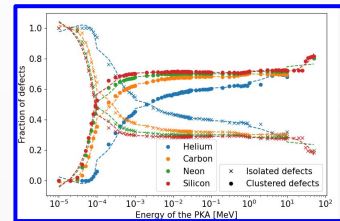
TRIM



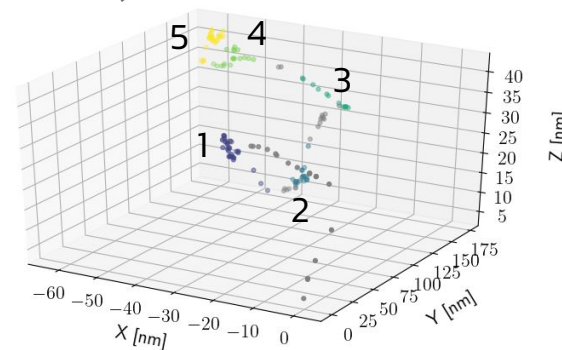
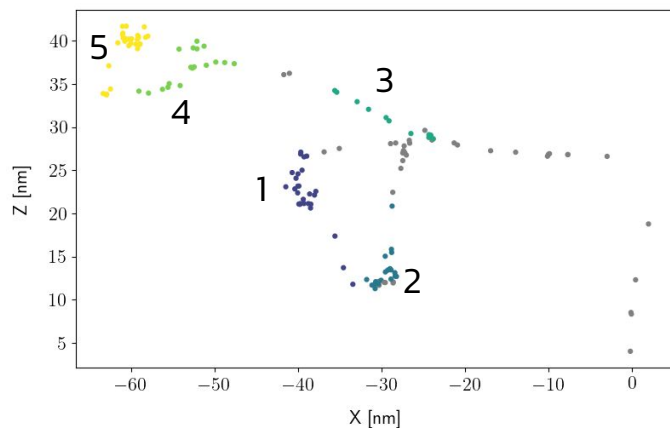
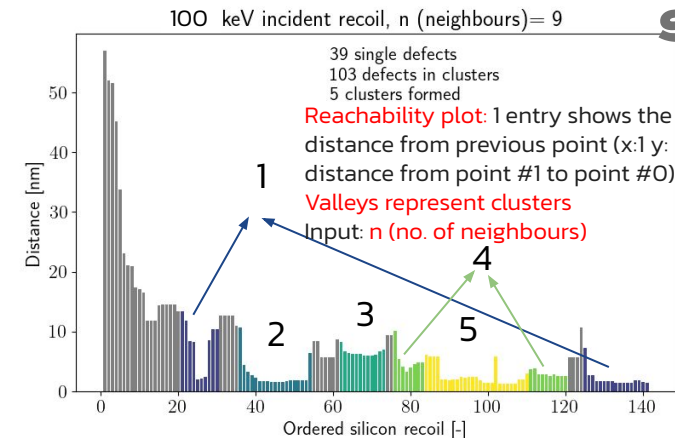
OPTICS



Isolated/Clustered
for low E recoils



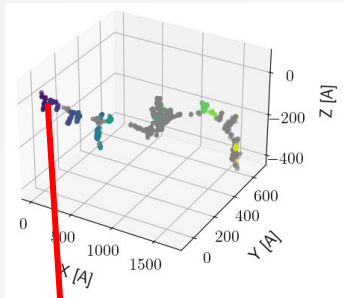
OPTICS¹³⁻¹⁵ (Ordering points to identify the clustering structure)



- Algorithm flow explain in the Appendix (Slide 34)
- Basic idea:
 - Ordering points and plotting their distances produces **Reachability plot**
 - Valleys in the reachability plot represent clusters
- Algorithm needs a user input: minimum number of samples to create cluster

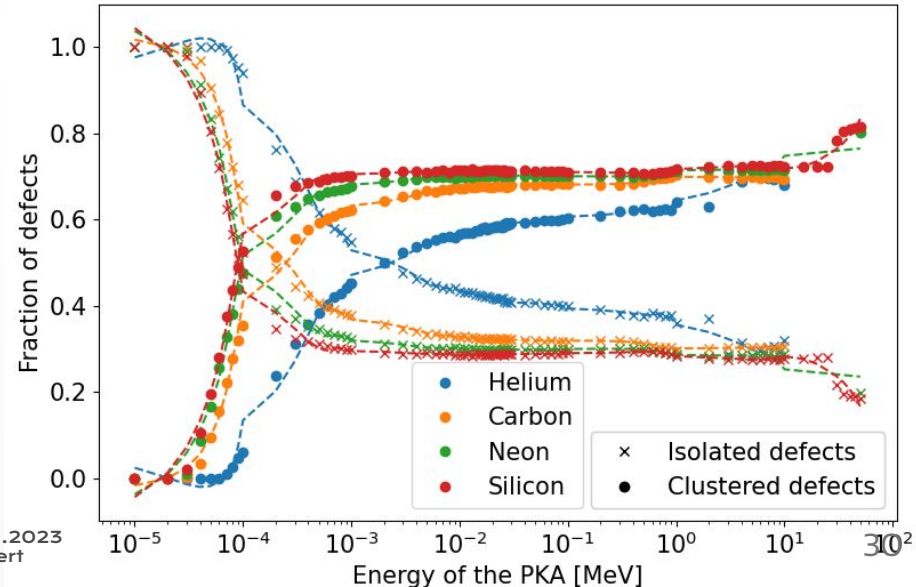
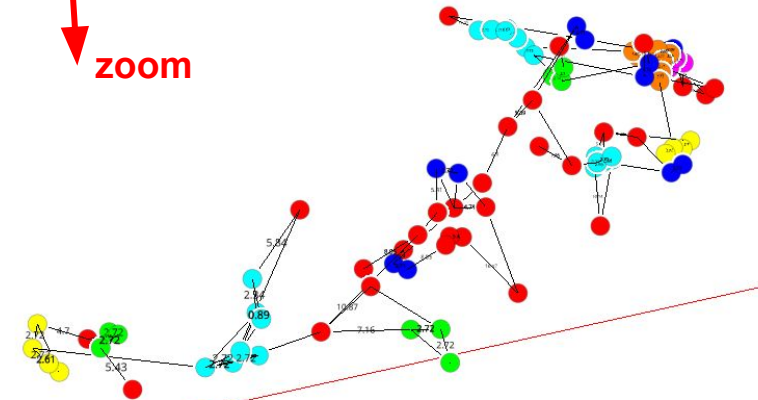
13) Ankerst, Mihael, Markus M. Breunig, Hans-Peter Kriegel, and Jörg Sander. "OPTICS: ordering points to identify the clustering structure." ACM SIGMOD Record 28, no. 2 (1999): 49-60.
 14) Schubert, Erich, Michael Gertz. "Improving the Cluster Structure Extracted from OPTICS Plots." Proc. of the Conference "Lernen, Wissen, Daten, Analysen" (LWDA) (2018): 318-329.
 15) <https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s> tutorial

OPTICS: Isolated vs clustered defect



- TRIM provides 3D distribution of a track created by recoil with Z (1,15)
- OPTICS algorithm can further analyze this track
- Example cluster graph below (in order to be part of a cluster, the vacancies have to be closer than 4.7 Å):
 - Red: Single vacancies, Blue: Divacancies
 - Green: trivacancies, Yellow: Tetravacancies, Pink: Pentavacancies
 - Cyan: cluster with 6–10 vacancies, Orange: 11–50 Vacancies
- Ratio of Isolated vs Clustered vacancies is stable for most elements >5 keV

zoom

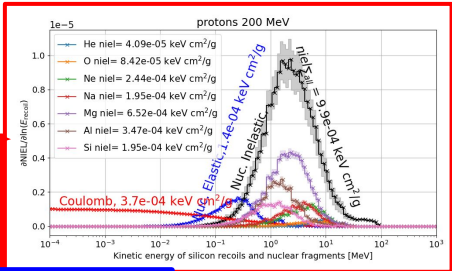
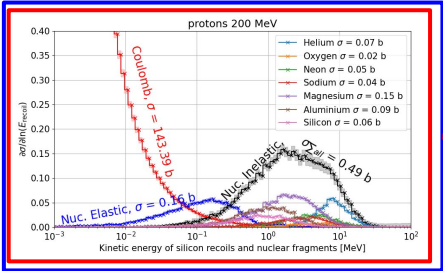
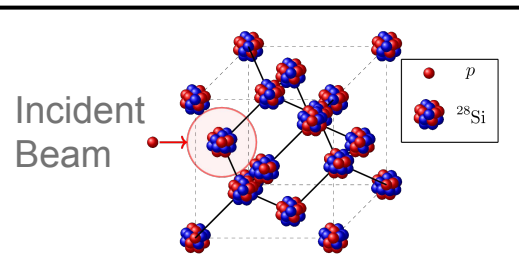


Overview of the simulations

GEANT4

PKA distribution

NIEL/NIEL_{vac} distribution for high E particles

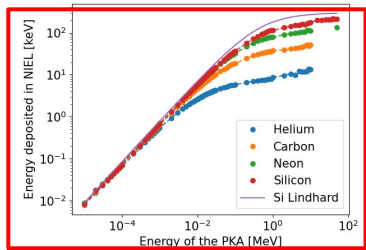
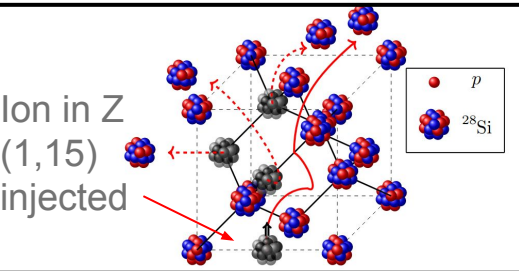


TRIM

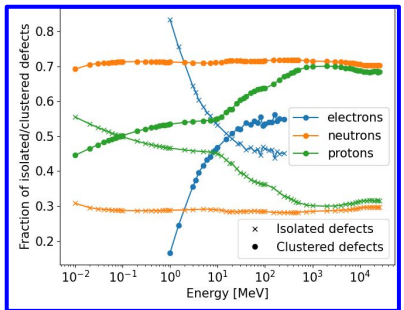
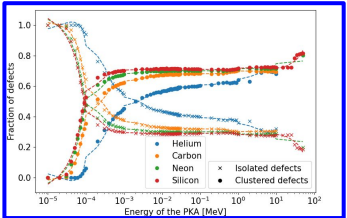
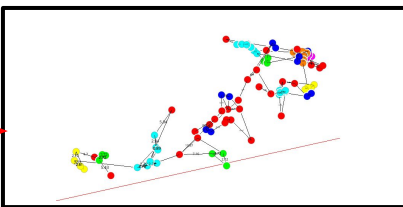
NIEL of low E recoils

Isolated/Clustered for low E recoils

Isolated/Clustered for high E recoils



OPTICS

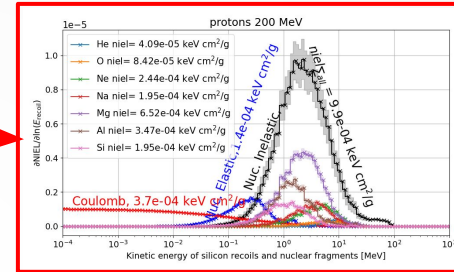
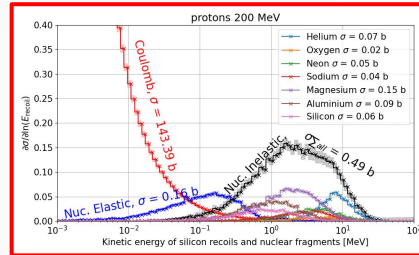
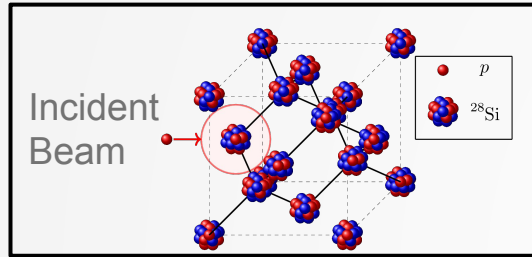


NIEL by high-energy particles

GEANT4

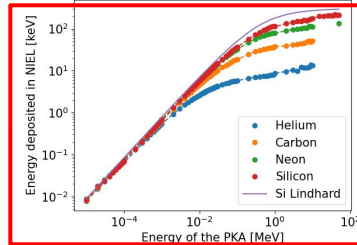
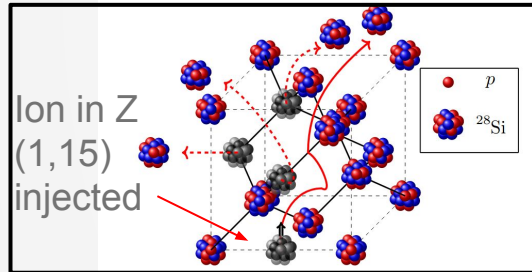
PKA distribution

NIEL/NIEL_{vac} distribution
for high E particles



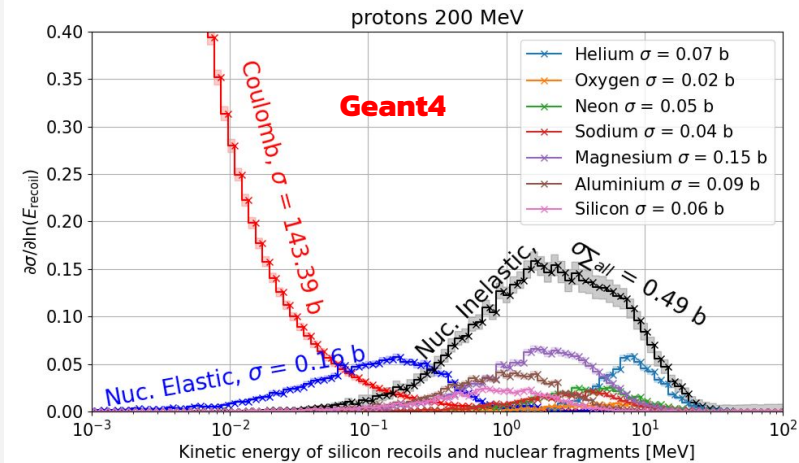
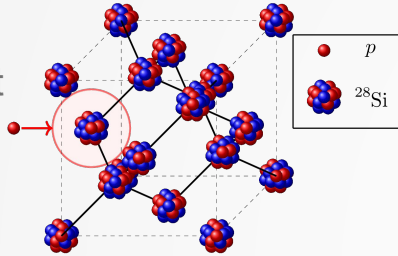
TRIM

NIEL of low E recoils



Integration of Geant4 PKA and TRIM NIEL

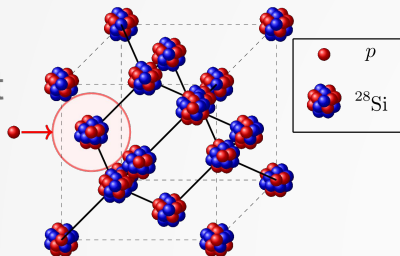
Si-atom

Incident
Beam

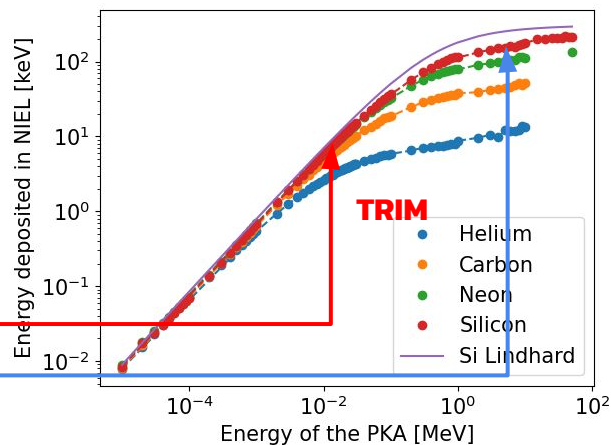
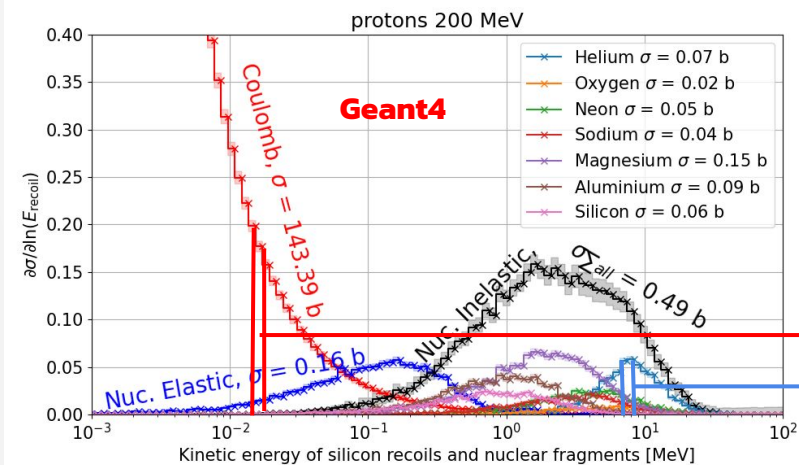
$$\text{NIEL}(T_0) = \frac{N_A}{A} \sum_i \int_{T_{\min}}^{T_{\max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$

Integration of Geant4 PKA and TRIM NIEL

Si-atom

Incident
Beam

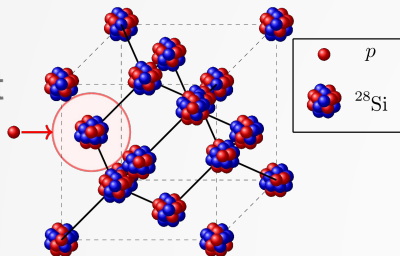
- 1) The PKA Energy distribution can be sliced.
- 2) The slice of an Energy E for ion with proton number Z can be correlated to particular NIEL ($NIEL_{\text{vacancy}}$)



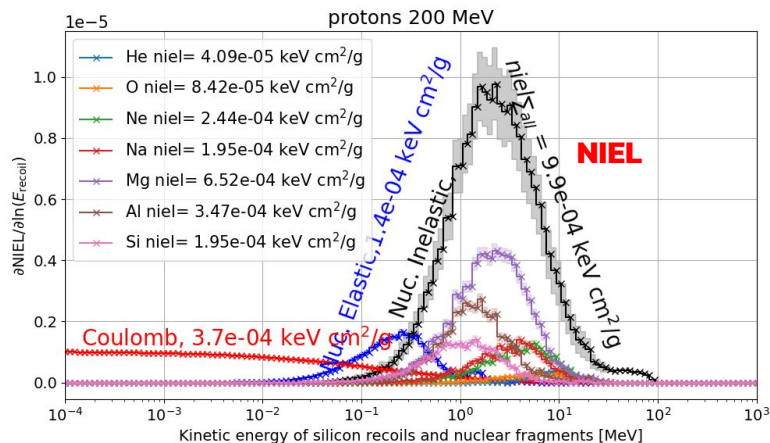
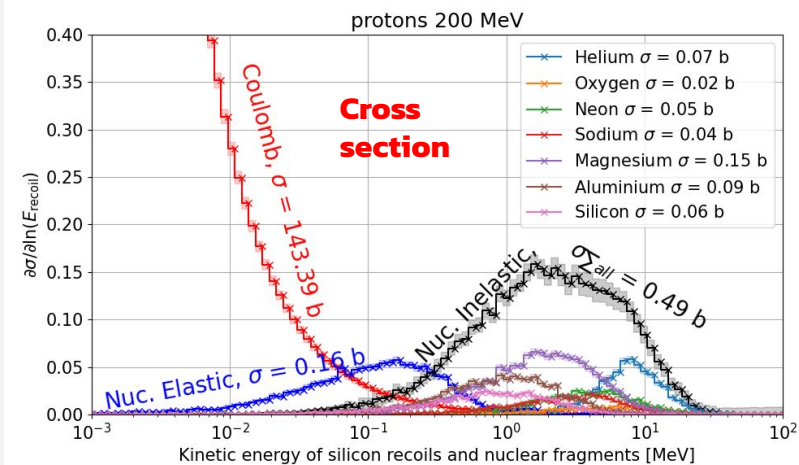
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Integration of Geant4 PKA and TRIM NIEL

Si-atom

Incident
Beam

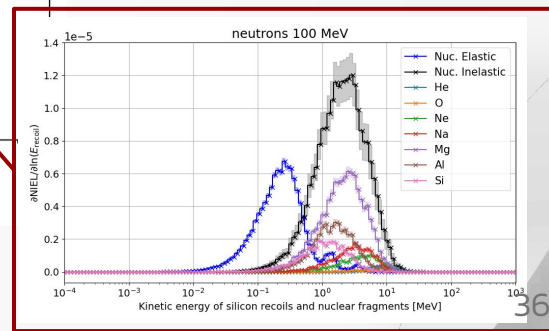
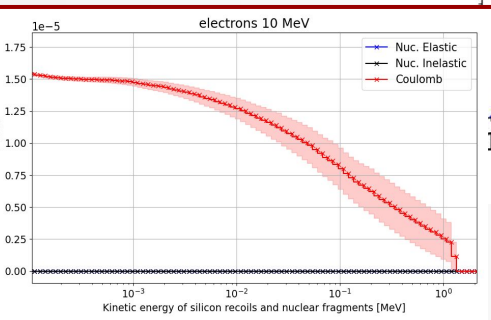
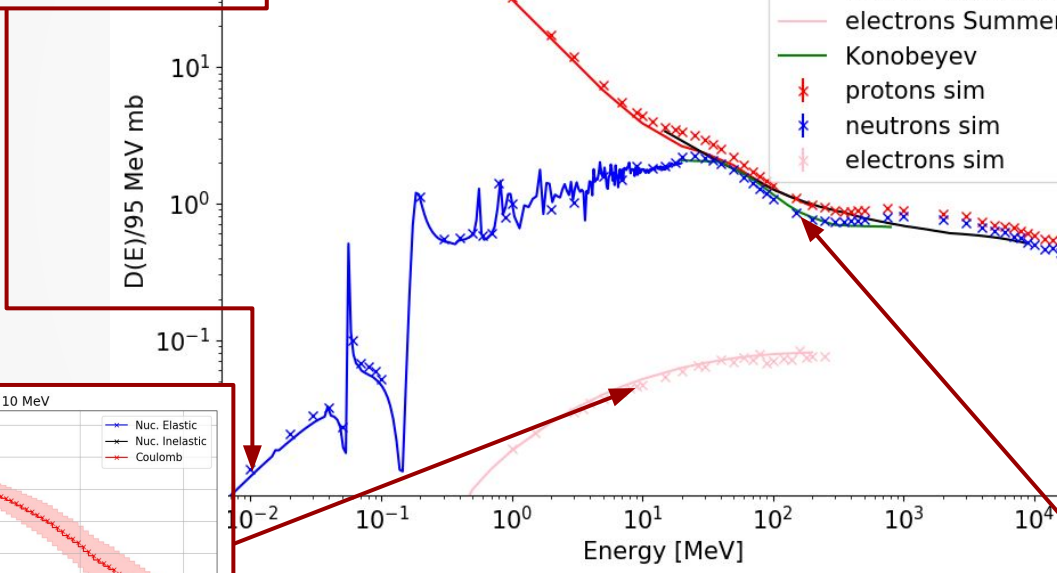
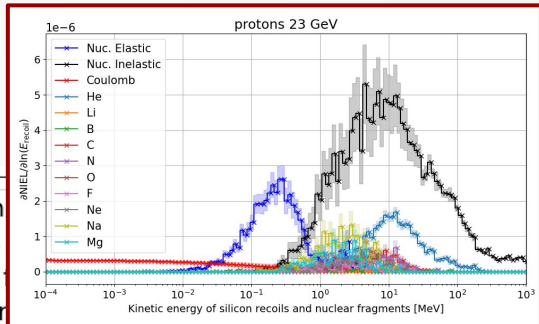
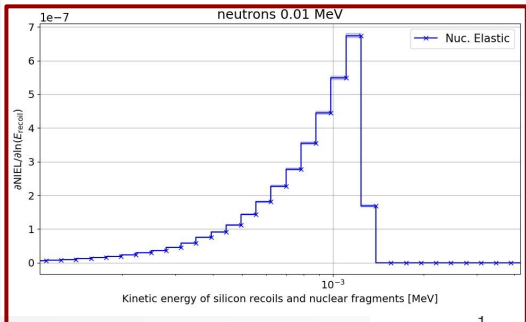
- 1) The PKA Energy distribution can be sliced.
- 2) The slice of an Energy E for ion with proton number Z can be correlated to particular NIEL ($\text{NIEL}_{\text{vacancy}}$)
- 3) A corresponding NIEL curve can be created



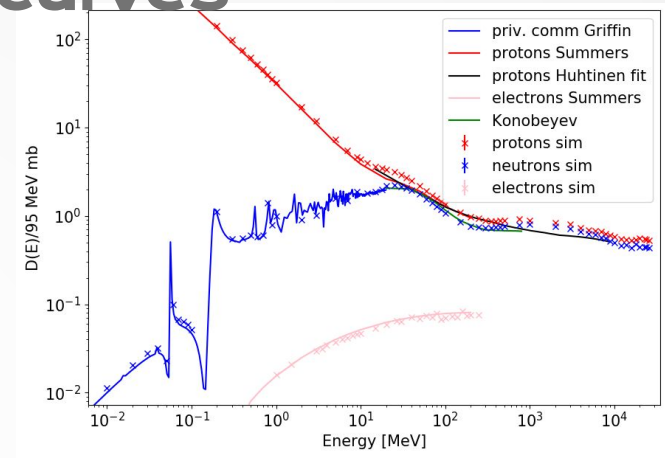
$$\text{NIEL}(T_0) = \frac{N_A}{A} \sum_i \int_{T_{\min}}^{T_{\max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$

Producing NIEL curves

- Integrating the recoil spectra above threshold displacement energy (21 eV) yields 1 point on the NIEL curve



Producing NIEL curves

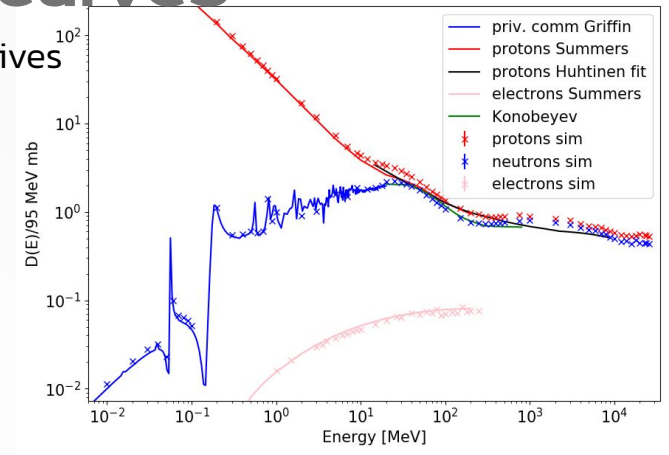
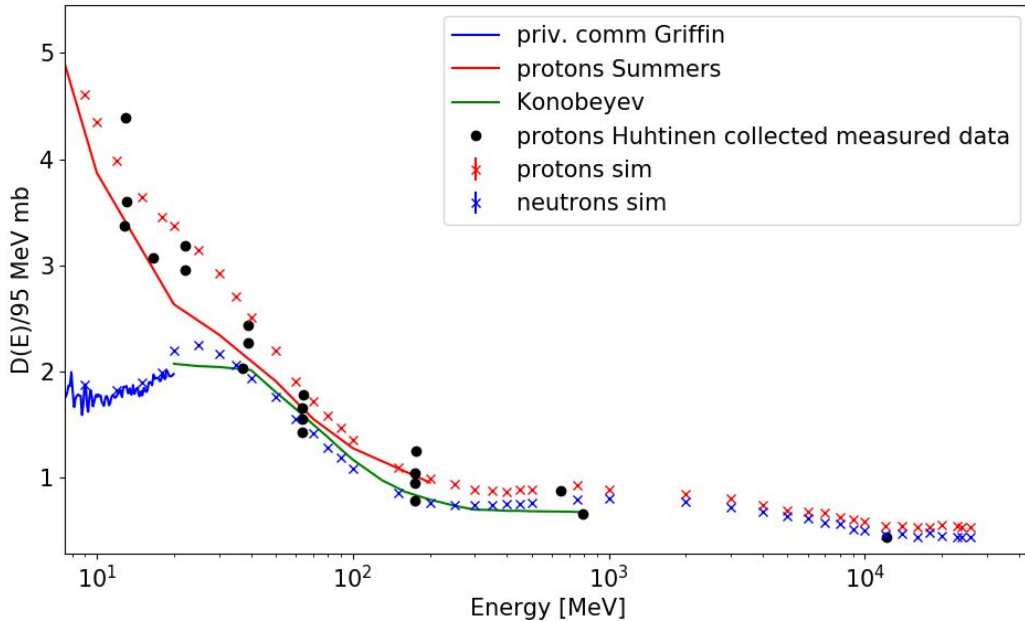


- **RD48 curve reproduced!**

Producing NIEL curves

Benchmarking:

- Against the measurements: M. Huhtinen collected data (1993). Gives the theoretical understanding for the part of the curve only measured in RD-48 standard.

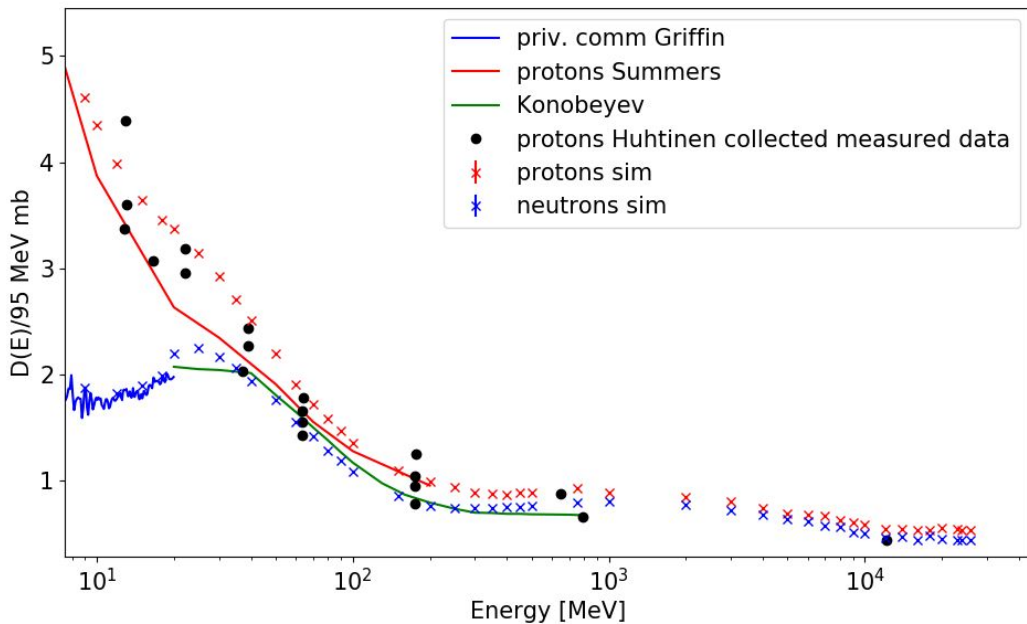


- RD48 curve reproduced!**

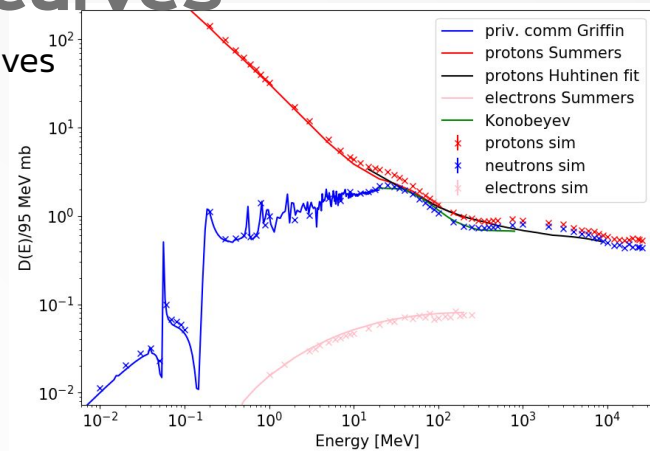
Producing NIEL curves

Benchmarking:

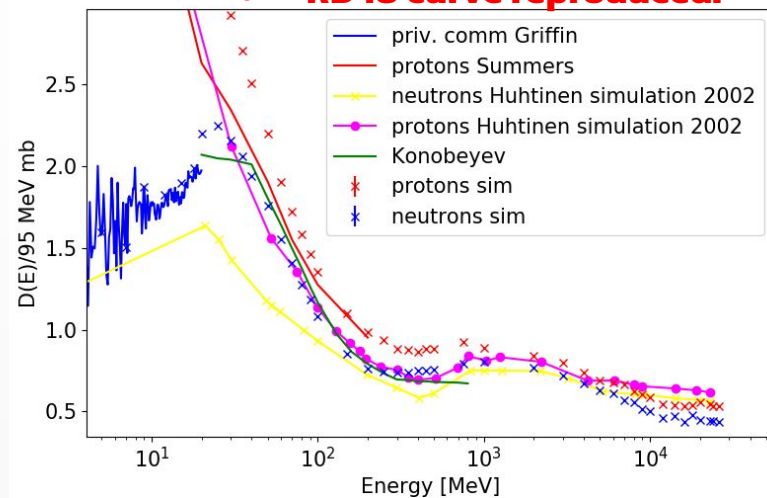
- Against the measurements: M. Huhtinen collected data (1993). Gives the theoretical understanding for the part of the curve only measured in RD-48 standard.
- Against other simulations (Konobeyev, M. Huhtinen 2002)
- Gives confidence in the approach.



42st RD50 Workshop, 20.06.2023
Vendula Maulerova-Subert



● **RD48 curve reproduced!**

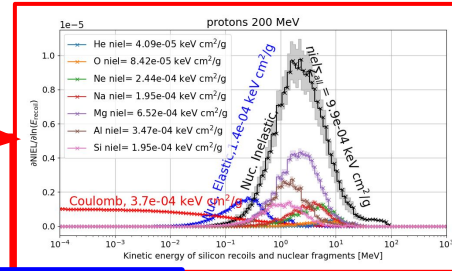
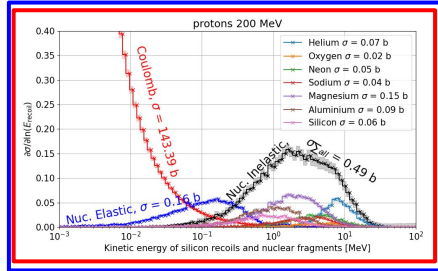
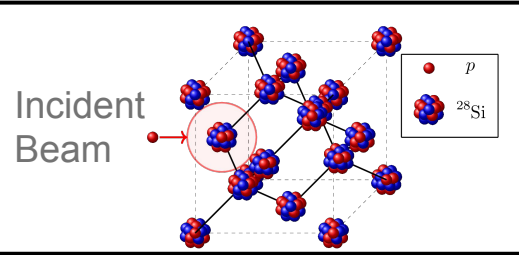


Overview of the simulations

GEANT4

PKA distribution

NIEL/NIEL_{vac} distribution for high E particles

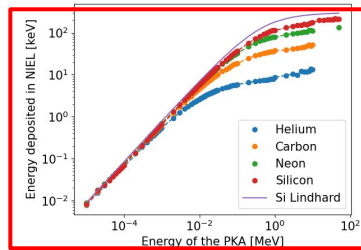
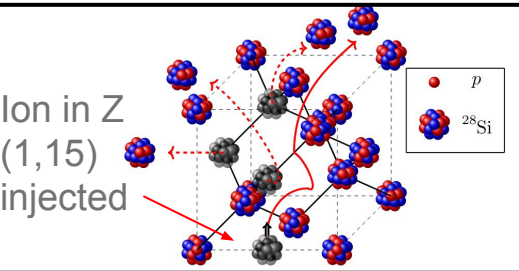


TRIM

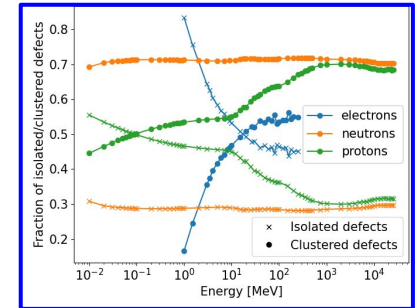
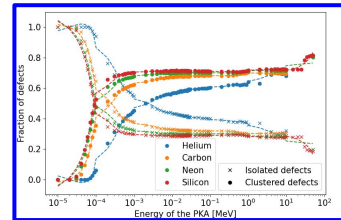
NIEL of low E recoils

Isolated/Clustered for low E recoils

Isolated/Clustered for high E recoils



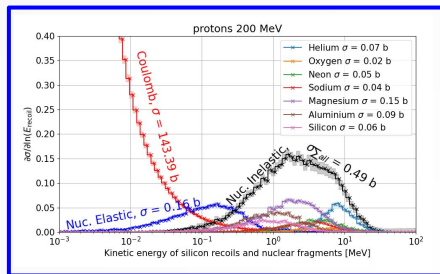
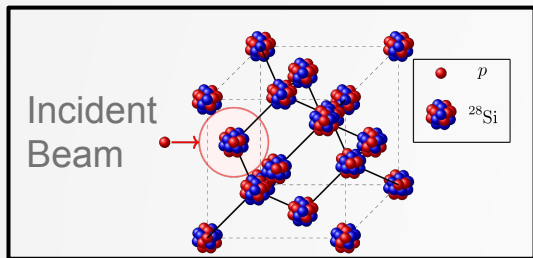
OPTICS



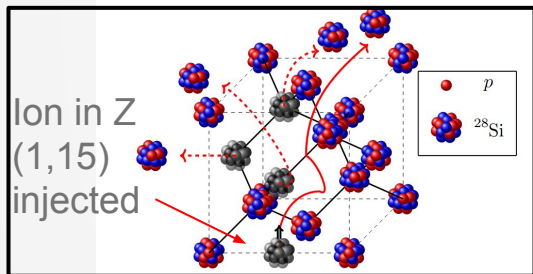
Atomic displacements by high-energy particles

GEANT4

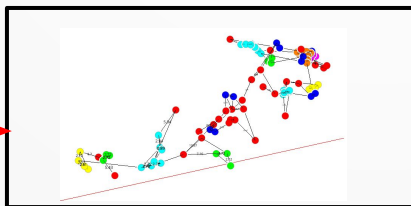
PKA distribution



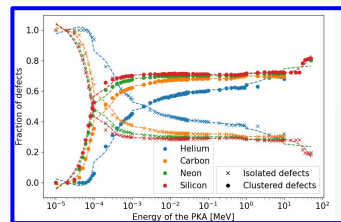
TRIM



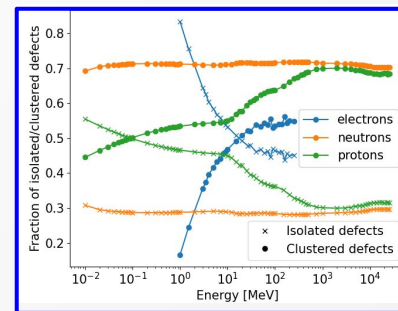
OPTICS



Isolated/Clustered for low E recoils



Isolated/Clustered for high E recoils

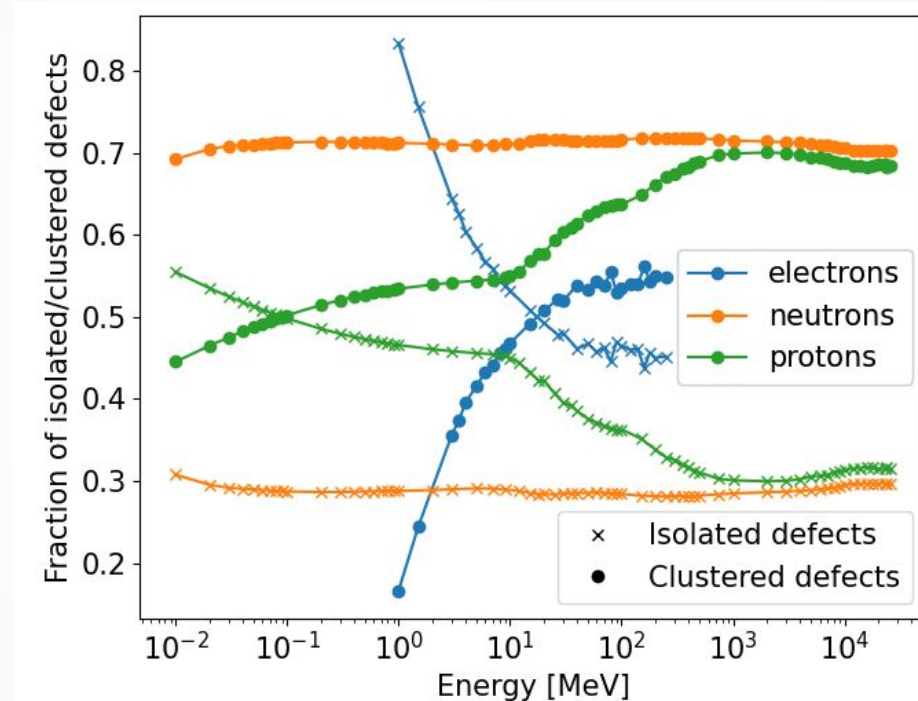


Isolated vs clustered vacancies

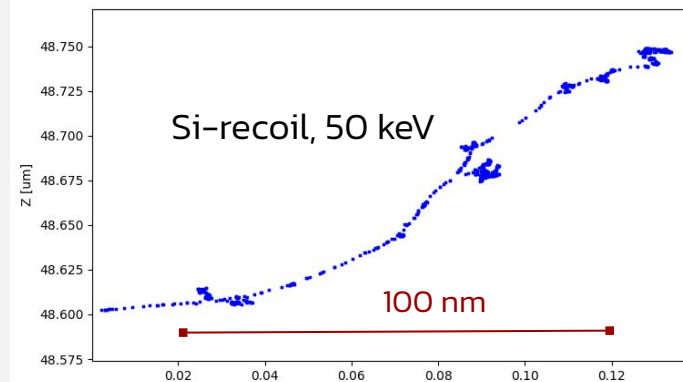
Results for minimum interatomic distance to be considered isolated vacancy.

Here cluster is consider anything \geq divacancy.

- For neutrons the ratio of the creation of isolated vacancies vs clustered is stable.
- For protons the ratio of the isolated/clustered vacancies is decreasing as the Coulomb reaction becomes less of an effect compared to inelastic and elastic scattering.
- For electrons the ratio rapidly changes with energy before eventually reaching a plateau as well.

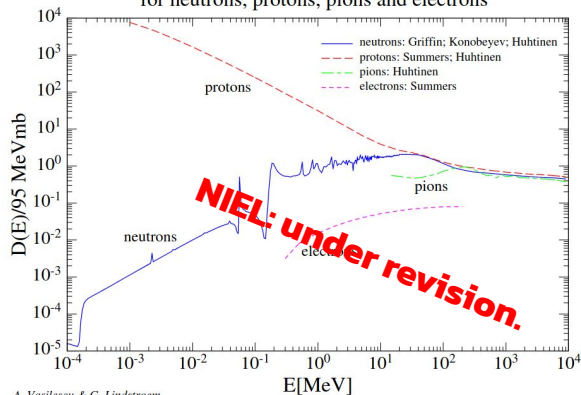


Outlook & next steps



- Geant4 and FLUKA-based simulations have been carried out to produce Primary knocked-on atoms. Simulations agree within limit.
- TRIM simulations had been used to relate NIEL to the low-energy recoil ions.
- NIEL curves from literature (RD-48¹) were successfully reproduced.
- Several cluster-finding algorithms have been tested to establish differences between different particles and particle energies.
 - Promising datasets for protons, neutrons and electrons shown in this presentation.

Displacement damage in Silicon
for neutrons, protons, pions and electrons



A. Vasilescu & G. Lindström

16) Data from A. Vasilescu (INPE Bucharest) and G. Lindström (Univ. of Hamburg), <https://rd50.web.cern.ch/niel/>

- Ongoing work:
 - Investigation of the relationship of NIEL (including phonons) and NIEL_{vacancy}
 - Systematic studies on OPTICS with parameter tuning.
 - Studies and comparisons with the literature (cluster sizes, differences between vacancies and interstitials,...).
 - Measurements of introduction rates benchmarking of the clustered and isolated defects for protons and neutrons.
 - Extending studies to gammas.
 - Comparison to other simulations (TRIM, kinetic monte-carlo, molecular dynamics, quasi-chemical).

THANKS!

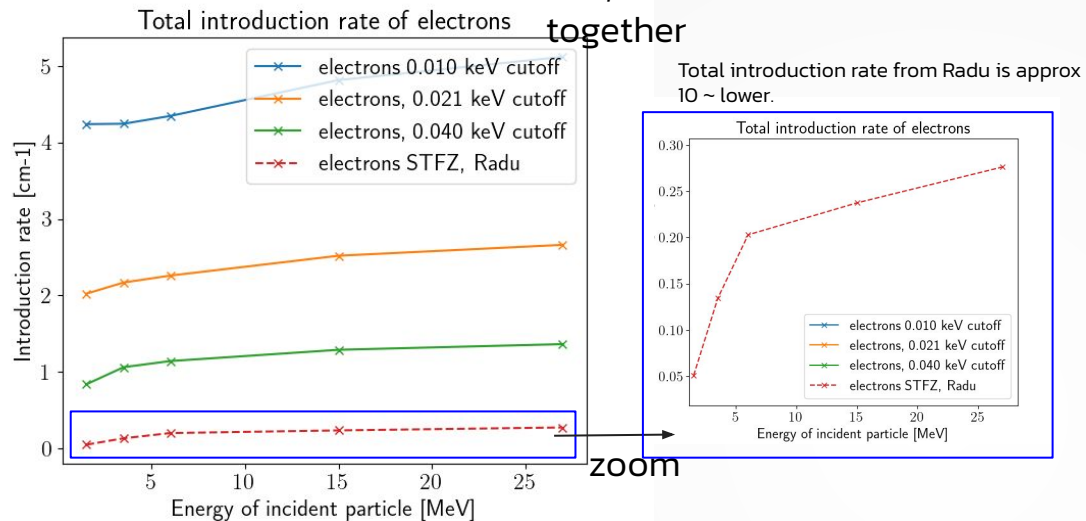


Do you have any questions?

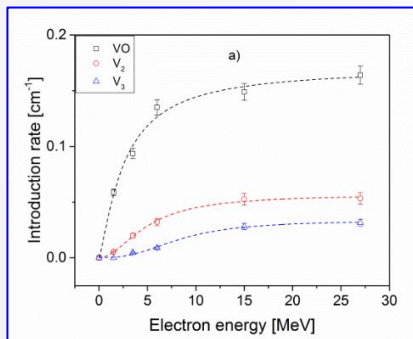


Electron induced damage

VOi, V3 and V2



- The aim is to tune the parameters by using the measured values that we know.
- We would like to compare the total introduction rates and the rates between clustered and point defects.
- Tuning might depend on n , ξ , cutoff limit.
- One of the options for the fine tuning would be to use a different constant for the processes that create only 1 PKA (a) and processes that create many SKA afterwards



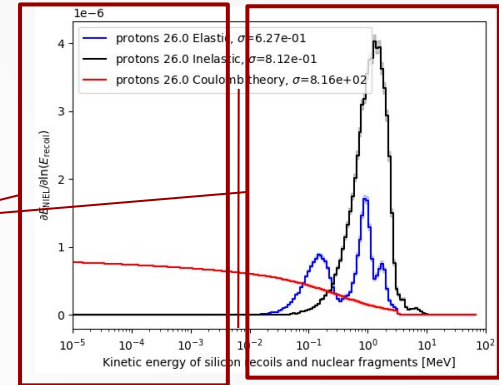
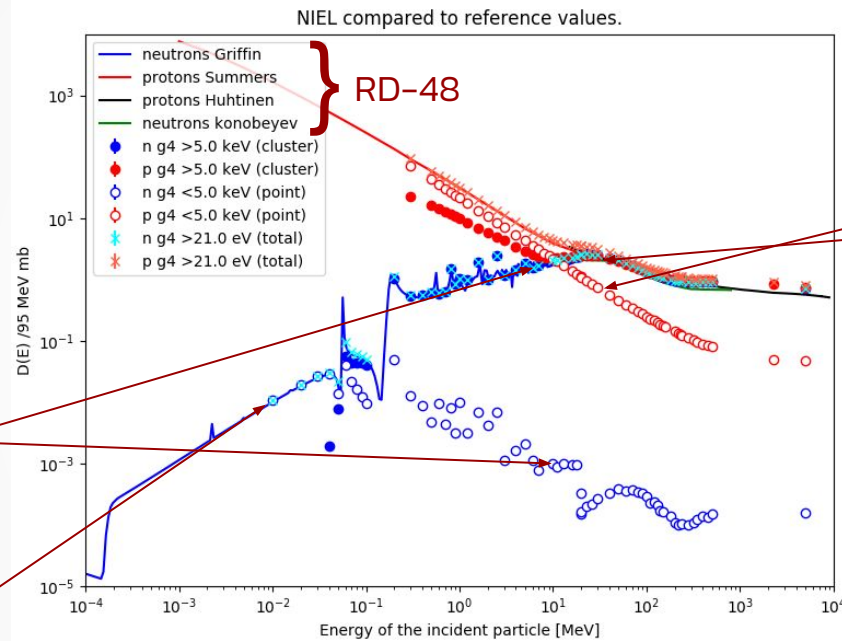
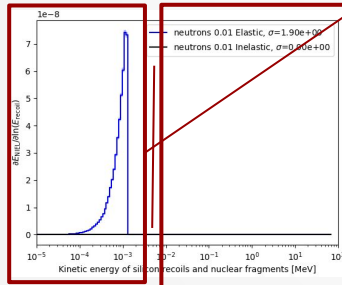
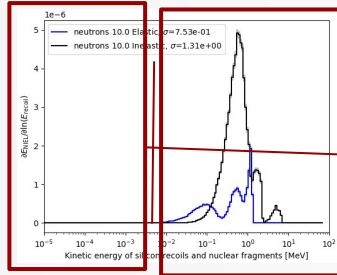
R. Radu: Bulk radiation damage in silicon:
from point defects to clusters

How to divide NIEL into clustered/isolated defects?

Initial approach :

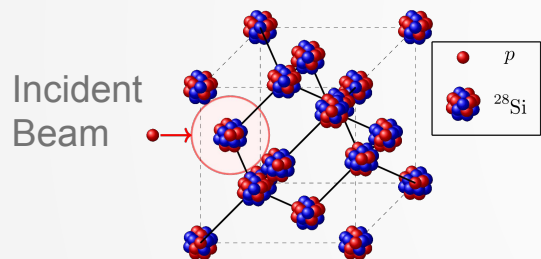
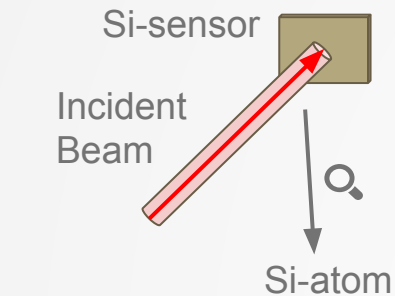
Use threshold (from the literature) for cluster formation

- Recoils < 5 keV: point displacements
- Recoils > 5 KeV: point displacements+ cluster displacements

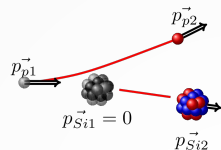


- Good as initial approach
- Not clear which part of the >5 keV is point-defects and which part is the cluster defect

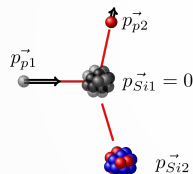
PKA cross section example



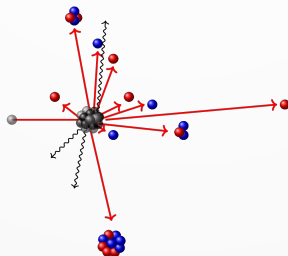
1) Coulomb elastic scattering
(only protons)



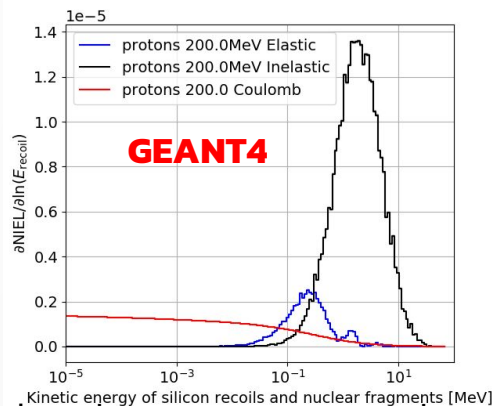
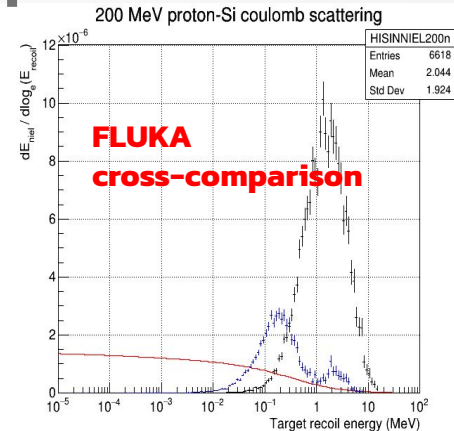
2) Nuclear elastic scattering



3) Nuclear inelastic scattering

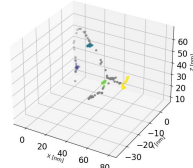
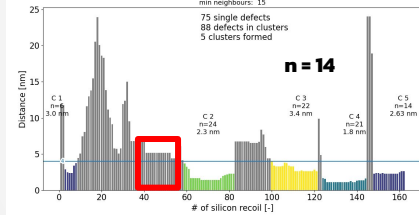
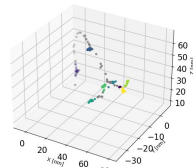
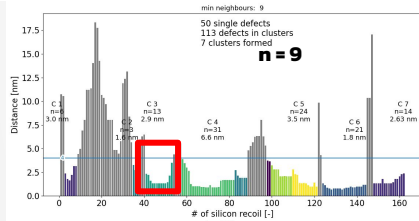
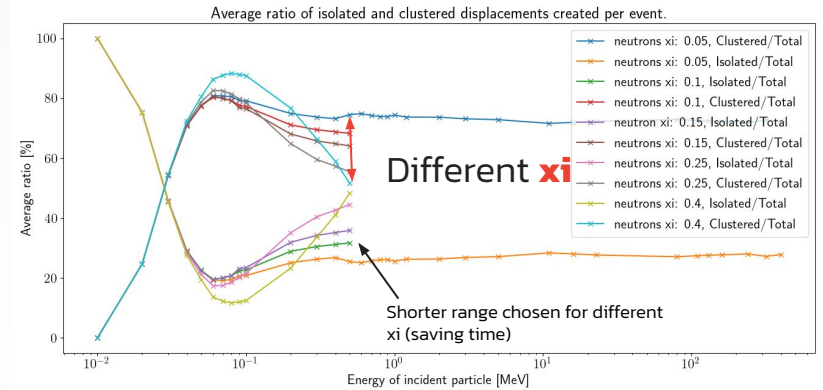
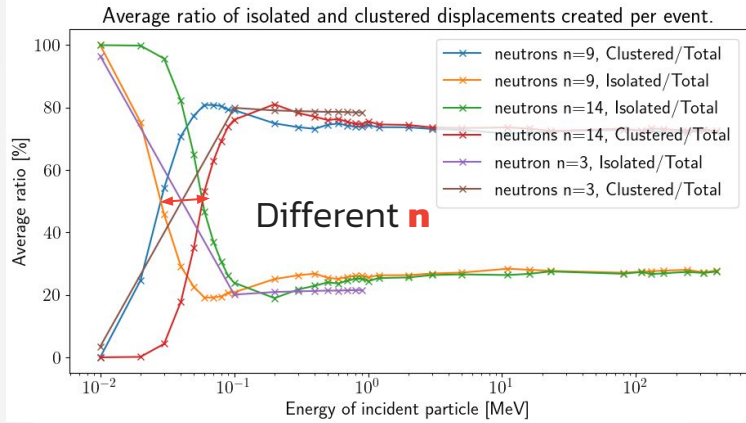


$$NIEL(T_0) = \frac{N_A}{A} \sum_i \int_{T_{min}}^{T_{max}} Q(T) T \left(\frac{d\sigma}{dT} \right)_i dT$$



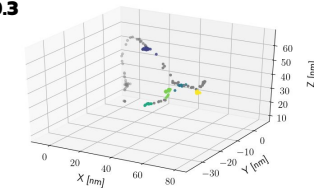
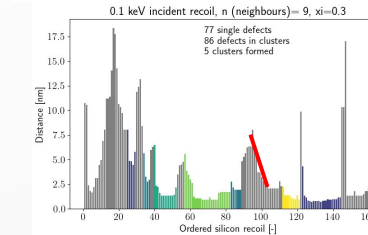
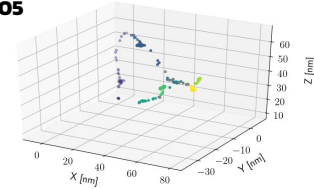
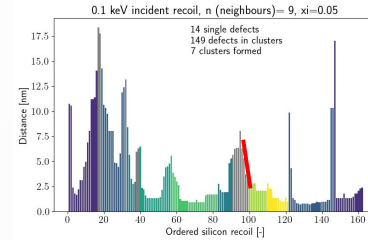
Area below the curve corresponds to the NIEL for respective reaction.

Parameter tuning: neutrons



For the total ratio of Clustered vs isolated defects:

- n seems to shift the curve horizontally
- ξ shifts the constant value the ratio eventually reaches.



Deeper explanation of the parameters:

<https://scikit-learn.org/stable/modules/generated/sklearn.cluster.OPTICS.html>

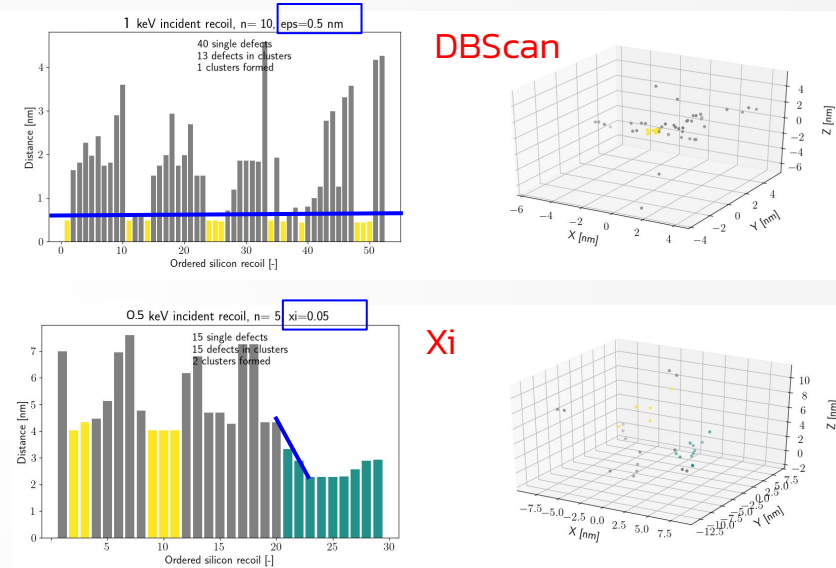
<https://dl.acm.org/doi/pdf/10.1145/304181.304187>

Tuning of the cluster model parameters

Method:

- Optics (number of samples, xi: steepness parameter)
- DBScan (number of samples, eps: extraction parameter)
 - The idea for DBScan could be to set $\text{eps}=0.47$ nm (2x interatomic distance) in order to be considered a cluster
 - The number of neighbours could be tuned by
 - <1-2 keV 0 clusters
 - <12 keV 1 cluster
 - >20 keV stable ratio of clusters and single displacements

1



Geant4 physics list, step functions

Derived from CERN Geant4 User's Workshop November 11th–15th 2002, John Apostolakis, Marc Verderi
Ecole Polytechnique - LLR

For physics list:

- **AtRest functions:** decay, e+ annihilation
- **AlongStep functions:** to describe continuous (inter)actions, occurring along the path of the particle, like ionisation
- **PostStep actions:** For describing point-like (inter)actions, like decay in flight, hard Radiation..

G4VProcess: can implement any combination of **AtRest**, **AlongStep**, **PostStep** action

GetPhysicalInteractionLength():

- Used to limit the step size:
 - either because the process « triggers » an interaction, a decay;
 - Or any other reasons, like fraction of energy loss;
 - geometry boundary;
 - user's limit ..

Geant4 physics list, step

Derived from CERN Geant4 User's Workshop November 11th–15th 2002, John Apostolakis, Marc Verderi
Ecole Polytechnique - LLR

The stepping:

- The stepping treats processes generically:
- The stepping does not know what processes it is Handling
- The stepping imposes on the processes to Cooperate in their **AlongStep** actions;
Compete for PostStep and **AtRest** actions;
- Processes can optionally emit also a «signal» to require particular treatment:
 - notForced: «standard» case;
 - forced: PostStepDolt action is applied anyway;
 - conditionallyForced: PostStepDolt
 - applied if AlongStep has limited the step;

The stepping: Stepping Invocation Sequence of Processes for a particle travelling

1. At the beginning of the step, determine the step length: Consider all processes attached to the current G4Track; Define the step length as the smallest of the lengths among: All AlongStepGetPhysicalInteractionLength(), All PostStepGetPhysicalInteractionLength()
2. Apply all AlongStepDolt() actions, « at once »: Changes computed from particle state at the beginning of the step; Accumulated in the G4Step; Then applied to the G4Track, from the G4Step.
3. Apply PostStepDolt() action(s) « sequentially », as long as the particle is alive: Apply PostStepDolt() of process which proposed the smallest step length; apply « forced » and « conditionally forced » actions

Geant4 physics list, step

Derived from CERN Geant4 User's Workshop November 11th–15th 2002, John Apostolakis, Marc Verderi

At rest: Ecole Polytechnique - LLR

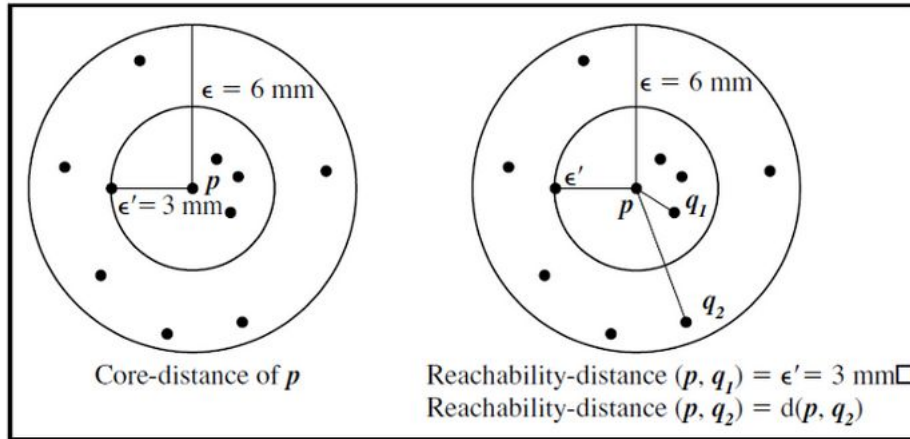
1. If the particle is **at rest**, is stable and can't annihilate, it is killed by the tracking: To be more accurate: if a particle at rest has no « AtRest » actions defined, it is killed.
2. Otherwise determine the lifetime: Take the smallest time among: All AtRestGetPhysicalInteractionLength() Called «physical interaction length» but returns a time!
3. Apply the AtRestDoIt() action of the process which returned the smallest time.

OPTICS^{15,16} (Ordering points to identify the clustering structure)

Important concepts:

- **n (number of neighbours):** user input
- **Core distance:** The minimum distance to make a point a core point, so that it contains number of neighbours n
- **Reachability-distance:**
 - a. If point $<$ the core-distance reachability distance = core-distance
 - b. If point $>$ core-distance, reachability distance = distance between the point and core point

If $n = 4$



15) Ankerst, Mihael, Markus M. Breunig, Hans-Peter Kriegel, and Jörg Sander. "OPTICS: ordering points to identify the clustering structure." ACM SIGMOD Record 28, no. 2 (1999): 49-60.

16) Schubert, Erich, Michael Gertz. "Improving the Cluster Structure Extracted from OPTICS Plots." Proc. of the Conference "Lernen, Wissen, Daten, Analysen" (LWDA) (2018): 318-329.

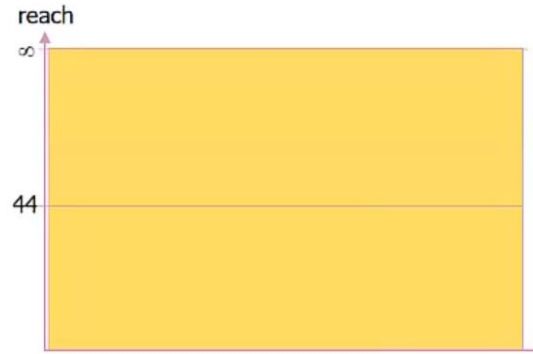
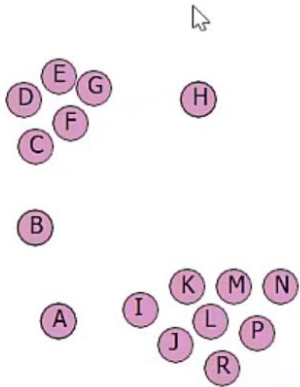
OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

Optics algorithm takes the points in a certain order and assigns them properties.

- $\epsilon = 44$, $MinPts = 3$



seedlist:

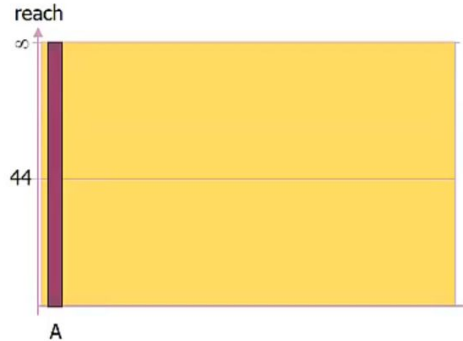
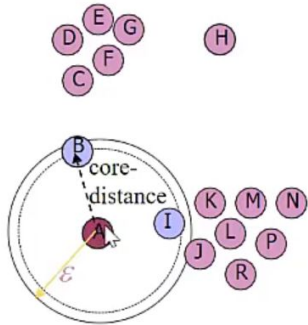
Min neighbours:2

OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)
- $\epsilon = 44$, $MinPts = 3$



seedlist: (B,40) (I, 40)

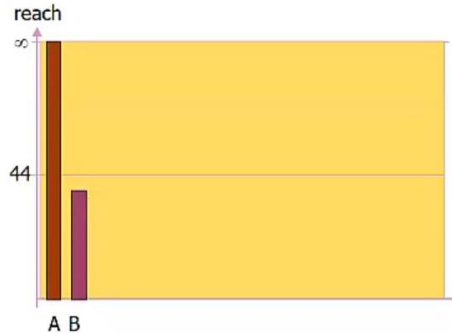
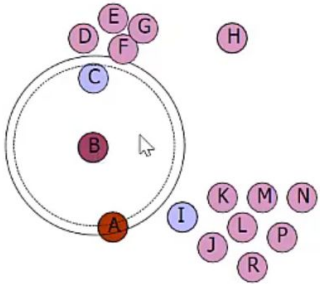
- A is the first point \rightarrow it's reachability is infinite. (How far is the point from the last point?)
- B and C have are 40 units far away from A.

Min neighbours:2

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)
- $\epsilon = 44$, $MinPts = 3$



seedlist: (I, 40) (C, 40)

- Next point: B.
- Seedlist is updated and ordered by reachability.

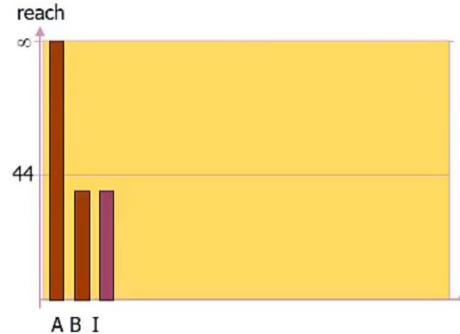
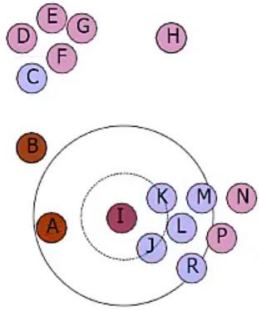
Min neighbours:2

OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)
- $\epsilon = 44$, $MinPts = 3$



seedlist: (J, 20) (K, 20) (L, 31) (C, 40) (M, 40) (R, 43)

Min neighbours:2

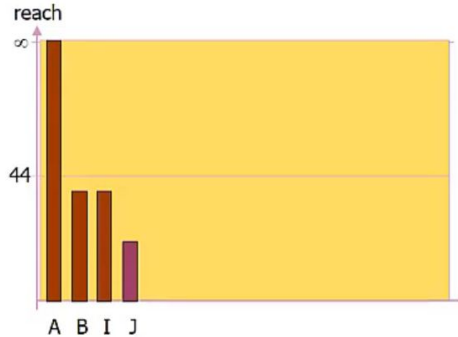
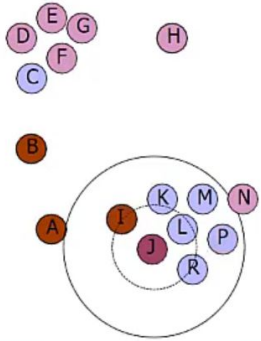
- Next point I.
- The core distance is much smaller (K and J are close).
- The seedlist is updated and ordered by reachability.

OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)
- $\epsilon = 44$, $MinPts = 3$



- Next point J
- The seedlist is updated and ordered by the reachability.

seedlist: (L, 19) (K, 20) (R, 21) (M, 30) (P, 31) (C, 40)

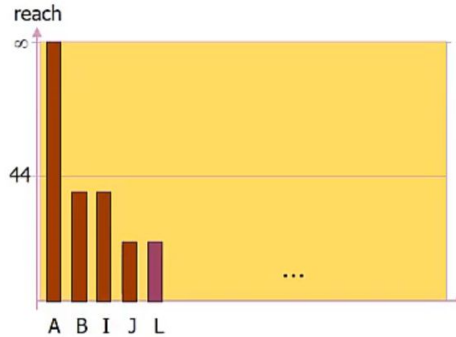
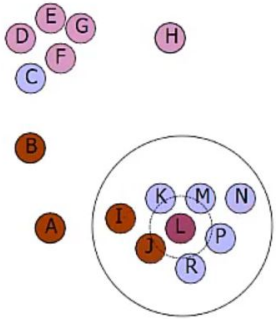
Min neighbours:2

OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)
- $\epsilon = 44$, $MinPts = 3$



- Next point L
- The seedlist is updated and ordered by the reachability.

seedlist: (M, 18) (K, 18) (R, 20) (P, 21) (N, 35) (C, 40)

Min neighbours:2

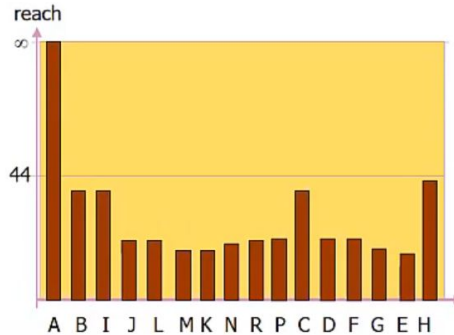
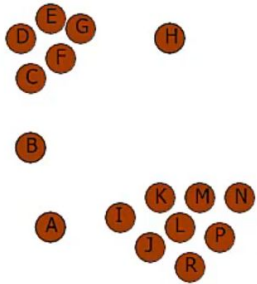
OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)

- $\epsilon = 44$, $MinPts = 3$



- The valleys represent the clusters.

seedlist: -

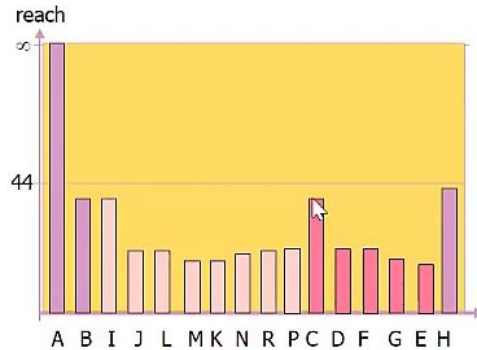
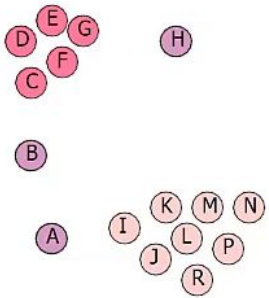
Min neighbours:3

OPTICS

Explanation from:

<https://www.youtube.com/watch?v=CV0mWaHOTA8&t=133s>

- Example Database (2-dimensional, 16 points)
- $\epsilon = 44$, $MinPts = 3$



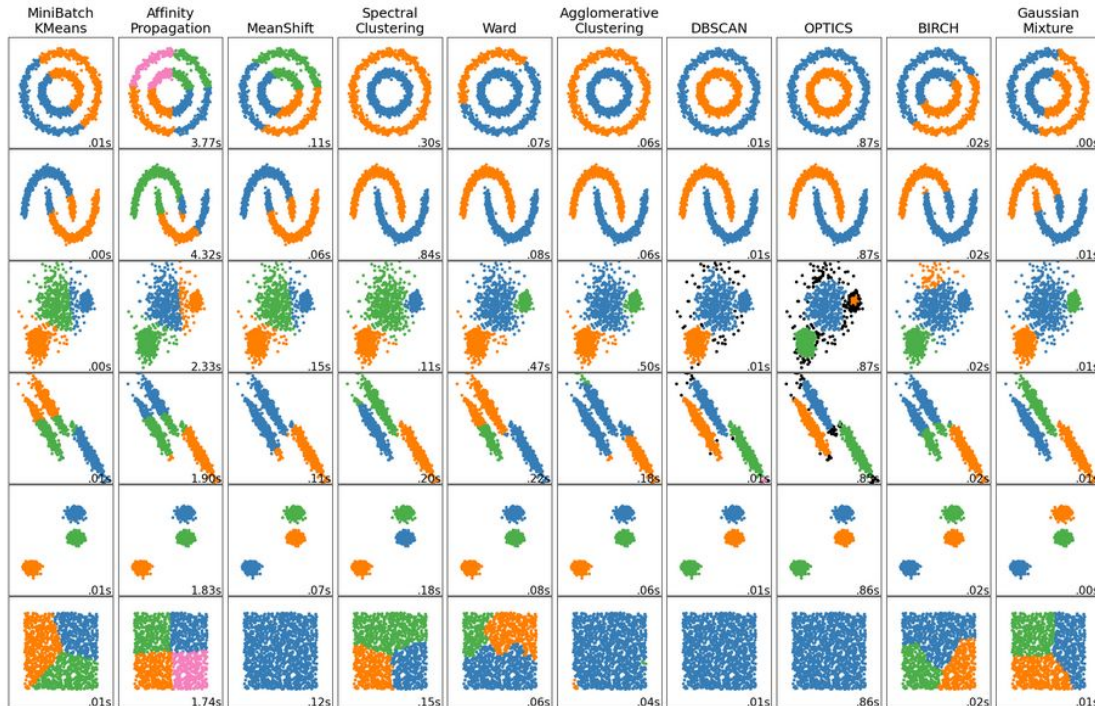
- The valleys represent the clusters.
- Parameter ξ is parameter that is applied on the reachability plot in order to extract the clusters.

Min neighbours:2

Clusters

- Cluster detection is a big topic in machine learning and mathematics
- Depending on its application, different algorithms are the best fit.

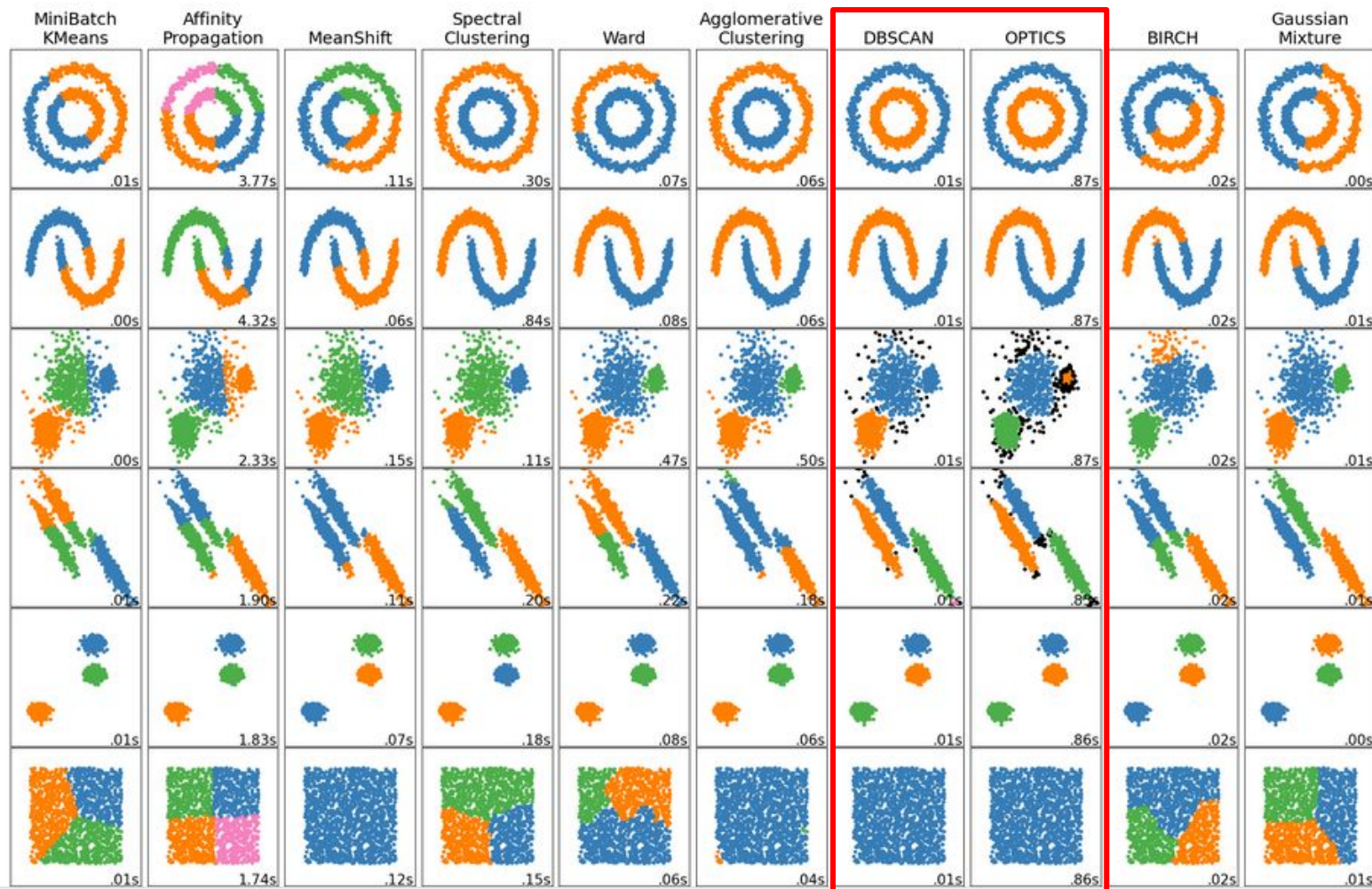
Image from^{12,13}



- Various clustering algorithms applied to 6 different sample datasets
- aim : identify clusters
- Algorithm must be able to process:
 - samples with large number of "outliers" (=single displacements for us)
 - samples with clusters of different shapes
 - samples with clusters with various densities

12) Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., ... Duchesnay, E. (2011). Scikit-learn: Machine Learning in Python. *Journal of Machine Learning Research*, 12, 2825–2830.

13) https://scikit-learn.org/stable/auto_examples/cluster/plot_cluster_comparison.html#sphx-glr-auto-examples-cluster-plot-cluster-comparison-py



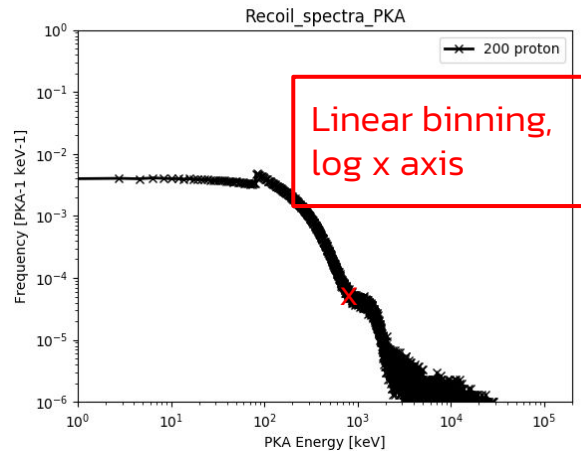
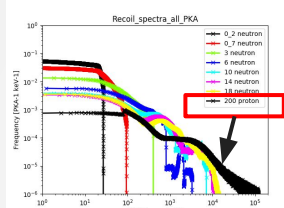
OPTICS performs better than DBSCAN for clusters with **varying densities**¹⁴.

12) Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., ... Duchesnay, E. (2011). Scikit-learn: Machine Learning in Python. *Journal of Machine Learning Research*, 12, 2825–2830.

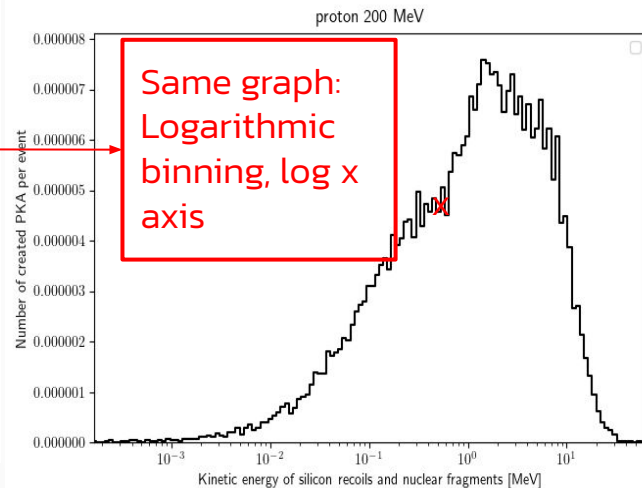
13) https://scikit-learn.org/stable/auto_examples/cluster/plot_cluster_comparison.html#sphx-glr-auto-examples-cluster-plot-cluster-comparison-py

14) <https://scikit-learn.org/stable/modules/clustering.html#optics>

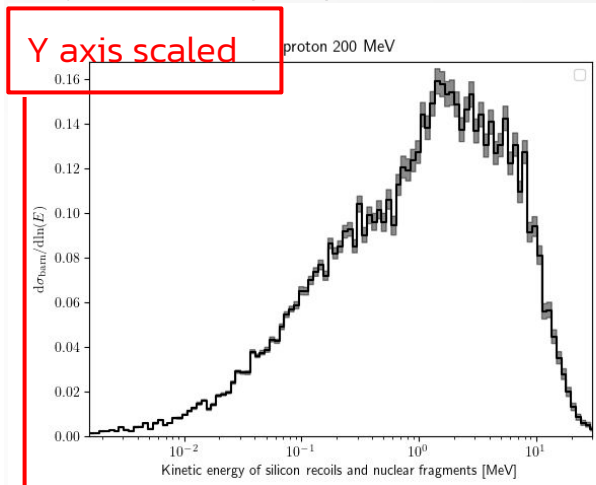
note: representing y axis as $\partial\sigma_{barn} / \partial \ln(E)$



- 1) PKA are summed and divided by the number of incident particles.



- 2) Logarithmic binning is used instead.



- 3) Each content in a bin is divided by the length of the bin. That makes the y-axis linear. Furthermore the y axis is scaled by:

Conversion from σ to probability:

$$\frac{I_{scattered}}{I_{incident}} = \frac{N_A \rho_{Si} d}{m_{Si}} \sigma = 0.0005 \sigma_{barn}$$

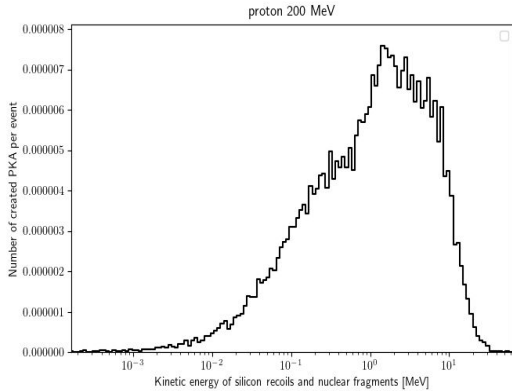
$$\frac{10^{24}}{N_{targ} d} \quad d = 0.01 \text{ cm}$$

$$N_{targ} = \frac{N_A \rho_{Si}}{m_{Si}}$$

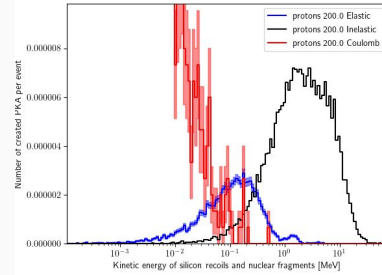
so that the **total area** corresponds to the **total cross section** of creating the PKA.

note: representing

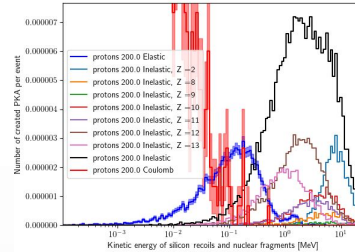
y axis as $\partial E_{NIEL} / \partial \ln(E_{recoil})$



2) PKA are divided into Elastic and Inelastic parts (Coulomb part is added from QGSP_BIC_HP_SS simulation). Inelastic part is further divided into different spectra according to the Z number.



3) Inelastic part is further divided into different spectra according to the Z number.



4) For Coulomb, Elastic and Inelastic Si, Al and Mg recoils a Lindhard formulation is used¹².

For a recoil silicon in a silicon lattice, they read as:

$$E_{dc} = \frac{E_{Si}}{1 + k \times g(\epsilon)}, \quad (2)$$

with $k = 0.1462$, $\epsilon = 1.014 \times 10^{-2} \times Z_{Si}^{-7/3} \times E_{Si} = 2.147 \times 10^{-5} E_{Si}$ and the universal function

$$g(\epsilon) = 3.4008 \times \epsilon^{1/6} + 0.40244 \times \epsilon^{3/4} + \epsilon \quad (3)$$

5) For alphas¹³, Xapsos-Burke values were used to calculate NIEL.

6) Each content in a bin is divided by the length of the bin so that the **total area** corresponds to the **total NIEL**.

1) PKA are summed and divided by the number of incident particles. Logarithmic binning is used instead, that makes the y axis linear.

12) Bergmann, Benedikt, et al. "Ionizing Energy Depositions After Fast Neutron Interactions in Silicon." IEEE Transactions on Nuclear Science, vol. 63, Aug. 2016, pp. 2372–78. NASA ADS, <https://doi.org/10.1109/TNS.2016.2574961>.

13) Xapsos, M.A. & Burke, E.A. & Badavi, F.F. & Townsend, Lawrence & Wilson, John & Jun, I.. (2005). NIEL calculations for high-energy heavy ions. Nuclear Science, IEEE Transactions on. 51. 3250 - 3254. 10.1109/TNS.2004.839136.

