



# DOCUMENTATION OF HELICOPTER AEROELASTIC STABILITY **ANALYSIS COMPUTER PROGRAM (HASTA)**

Lawrence R. Sutton

RASA Division

Systems Research Laboratories, Inc.

1055 J. Clyde Morris Blvd.

Newport News, Va. 23602

70

A

O December 1977

Final Report

Approved for public release; distribution unlimited.

Prepared for

APPLIED TECHNOLOGY LABORATORY U. S. ARMY RESEARCH AND TECHNOLOGY LABORATORIES (AVRADCOM) Fort Eustis, Va. 23604

BEST AVAILABLE COPY

### APPLIED TECHNOLOGY LABORATORY POSITION STATEMENT

This user's manual has been reviewed by Applied Technology Laboratory (ATL) and is considered to be technically sound. The user's manual has been prepared to provide personnel unfamiliar with the HASTA computer program the ability to apply the procedure to helicopter stability analysis. Because the subject of helicopter stability is inherently very complicated, the manual is primarily directed to experienced dynamicists and mathematicians. However, the test is not difficult to read and a series of simple examples has been provided to help make understanding the program as simple as possible. Therefore, the manual should provide the potential for direct application of the HASTA computer program by a user familiar with the fundamental helicopter dynamic system.

Mr. William E. Nettles of the Aeromechanics Technical Area served as the Army project engineer for this effort.

#### **DISCLAIMERS**

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.

When Government drawings, specifications, or other data are used for any purpose other than in connection with a definitely related Government procurement operation, the United States Government thereby incurs no responsibility nor any obligation whatsoever; and the fact that the Government may have formulated, furnished, or in any way supplied the said drawings, specifications, or other data is not to be regarded by implication or otherwise as in any manner licensing the holder or any other person or corporation, or conveying any rights or permission, to manufacture, use, or sell any patented invention that may in any way be related thereto.

Trade names cited in this report do not constitute an official endorsement or approval of the use of such commercial hardware or software.

#### DISPOSITION INSTRUCTIONS

Destroy this report when no longer needed. Do not return it to the originator.

UNCLASSIFIED

AGREPORT	DOCUMENTATION	PAGE		READ INSTR BEFORE COMPL	
HEPORT WHEEL		2. GOVT ACC	SSION NO. 3.	RECIPIENT'S CATALO	
USARTI TR-77-52		ı	(a)		
4. TITLE (and Subtitle)	-		11/2	THE OF REPORT A	ERIOD COVER
The state of the s	THE RESIDENCE OF THE PERSON OF	the supposed and the same of the same of	-	inal Report	-
DOCUMENTATION C	F HELICOPTER	AEROELAST	IC	THAT VELOCIE	<b>9</b>
STABILITY ANALY	SIS COMPUTER	PROGRAM	1	RERECOMME ORG. AL	PORT NUMBE
(HASTA)	and the first of the second se		一山山原	ASA/SRL-14-77	-d4
7. AUTHOR(a)		<del></del>	1	CONTRACT OR GRANT	NUMBER(a)
			11	云)	
1.			4		
Lawrence R./Sut			D	AAJ 02-76-C-08	
9. PERFORMING ORGANIZATION	TION NAME AND ADDRES	S	10	PROGRAM ELEMENT,	PROJECT, TA
Systems Research	h Laboratorie	s. Inc		(10)	
Systems Research 1055 J. Clyde M	orris Blvd.	,	6	2209X 11F2622	9AH76
Newport News, V	A 23602		11.776	1233 21	
11. CONTROLLING OFFICE				REPORT DATE	
Applied Technol and Technology	ogy Laboratory	y, Resear	CH TID	1977 <sub>1</sub>	
Fort Eustis, VA	23604	(AVRADCOM	77	A 1 1 D	
14. MONITORING AGENCY N		ent from Controllie	4 Ohicas Vi	SECURITY CLASS, for	this report)
The month of the first in					
			1	Unclassified	
				. DECLASSIFICATION	DOWNGRADIN
1				SCHEDULE	
Approved for p	ublic release;	: distrib	ution ur	limited	
Approved for policy property of the policy pr					
	NT (of the abetract entered				
17. DISTRIBUTION STATEME	NT (of the abetract entered				
17. DISTRIBUTION STATEME	NT (of the abetract entered				
17. DISTRIBUTION STATEME	NT (of the abetract entered				
17. DISTRIBUTION STATEME	NT (of the abetract entered	in Block 20, II o	illerent trom R		
17. DISTRIBUTION STATEME  18. SUPPLEMENTARY NOTE  19. KEY WORDS (Continue on	NT (of the abetract entered	i in Black 20, if a	illerent trom R		
17. DISTRIBUTION STATEME  18. SUPPLEMENTARY NOTE  19. KEY WORDS (Continue on Tail Rotor	NT (of the abetract entered	i in Block 20, if a	illerent trom R		
19. KEY WORDS (Continue on Tail Rotor Main Rotor	NT (of the abstract entered	i in Block 20, if a	illerent trom R		
19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics	NT (of the abetract entered	in Block 20, if a	illerent trom R		
19. KEY WORDS (Continue on Tail Rotor Main Rotor	NT (of the abstract entered	in Block 20, if a	illerent trom R		
19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics	NT (of the abetract entered	nd identify by blo nance	Illerent from R		
17. DISTRIBUTION STATEME  18. SUPPLEMENTARY NOTE  19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics Helicopter  20. ABSTRACT (Continue on Part Continue	NT (of the abetract entered  S  reverse side II necessary a  Air Reso Stabilit Rotor Vibratio	in Block 20, if a not be a not	illerent from R  ck number)	eport)	program
19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics Helicopter  20. ABSTRACT (Continue on This report is the continue on	NT (of the abetract entered  Air Reso Stabilit Rotor Vibratio	nd identify by bloom	illerent from R  ck number)  k number)	he computer	program ed under
19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics Helicopter  20. ABSTRACT (Continue on This report is the Helicopter Aeroe	NT (of the abetract entered  NT (of the abetract entered  Air Reso Stabilit Rotor Vibratio  Pereson and M macroscopy and the documentatelastic Stabil	and identify by bloomance  Ty  Indidentify by bloomance  Ty  Indidentify by bloomanuation manuatity Analy	ck number)  k number)  al for the sis (HA	he computer p	ed under
19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics Helicopter  20. ABSTRACT (Continue on This report is the Helicopter Aeroe Army Contract Nu	Air Reso Stabilit Rotor Vibratio the documentate lastic Stabilit mber DAAJ02-7	and identify by block	ck number)  al for the H	he computer postA) develope	ed under predict
19. KEY WORDS (Continue on Tail Rotor Main Rotor Dynamics Helicopter  20. ABSTRACT (Continue on This report is the Helicopter Aeroe	Air Reso Stabilit Rotor Vibratio the documentate lastic Stabilit mber DAAJ02-7 se behavior of the including	and Identify by bloomance  ion manuality Analy  coupled rotor dri	k number)  k number)  al for too sis (HA  The H  rotor/h  ve shaf	he computer postal develope ASTA program elicopter (substitutional statements)	ed under predict upport flexibil

DD 1 1AM 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE #09 781

1 SECUR

UNCLASSIFIED
SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

SECURITY CLASSIFICATION OF THIS PAGE(When Date Entered)

20. gimballed, teetering, flexstrap, and bearingless rotor systems is allowed. This manual contains: a description of the method of solution, a list of program variables, a discussion of the equations, a listing of the program, instructions on the use of the program, sample input and output listing, and additional information pertaining to the computer program.

NTIS DOC BRANNOUNCED JUSTIFICATION	White Section  Buff Section
DISTRIBUTION/AN	VAILABILITY CODES
DIST. A AIL	and for SPECIAL

# TABLE OF CONTENTS

					Page
LIST OF ILLUSTRATIONS		• • •		•	5
LIST OF TABLES				•	7
INTRODUCTION				•	8
OVERALL PROGRAM CAPABILITIES				•	11
HELICOPTER/ROTOR SYSTEM MODEL .				•	15
				•	15
Rotor Configuration Model .				•	22
Control System Model				•	24
Control Rod Model				•	26
Rotor Elastic Support Struct					27
Gearbox or Transmission Moun					28
Rotor Drive Shaft Torsional	Flexibil	ity Mc	del	_	28
COORDINATE SYSTEMS				•	30
Potor Wish Coordinate Customs					32
Rotor Hub Coordinate Systems					
Blade Coordinate Systems .			• •	•	35
Pitch Control Structure Coor				•	43
Control System Coordinate Sy				•	49
Control Rod Orientation					53
Support Structure Coordinate	Systems				55
Shaft-Rotor Hub Interface Re	lationsh	ips .			57
		•			
GENERAL DISCUSSION OF EQUATIONS		• •		•	59
Transfer Matrix Operations					59
Final Governing Matrix					64
Eigenvalue and Eigenvector S	olution	Method	1 .		69
Digonvarue una Digonvector D	orucro		•	•	0,5
COMPUTER PROGRAM METHOD OF SOLUTI	ON	• 1•1 •		•	73
INTERPRETATION OF COMPUTER PROGRA	M RESULT	s.		•	79
DESCRIPTION OF SUBROUTINES AND FU	NCTIONS			•	82
COMPUTER PROGRAM SYMBOL DICTIONAR	Y				90

	Page
USER'S GUIDE	125
Dimensions of Computer Array Variables Description of Input Data	125 145 198 214 227 262
PROGRAM LISTING	287
REFERENCES	411

**\*** 

# LIST OF ILLUSTRATIONS

Figure		Page
1	A Representative System That Can Be Considered	16
2	A General Blade Section	18
3	Simplified Sectionalization of a Blade Structure	19
4	Pitch Control and Blade Retention Structure for Three Different Types of Blade Models	23
5	Swashplate Control System Model and Fixed Coordinate System for Counterclockwise Rotating Rotor	25
6	Six Possible Rotor System Configurations	31
7	Fixed Hub Coordinate Systems for Two Directions of Rotor Rotation	33
8	Fixed Hub Coordinate System and Rotating Hub Coordinate System Corresponding to the First Blade for Two Directions of Rotor Rotation	35
9	General Description of the Rotating Local Blade Coordinate System for a jth Blade Section	36
10	Description of the Rotating Hub Coordinate System Rotations Required for Definition of the jth Section Local Blade Coordinate System Orientation	38
11	Relationship Between the Local Blade Aero- dynamic and Local Blade Coordinate Systems for the jth Blade Section	41
12	Description of Rotating Hub Coordinate System Rotations Required for Definition of the Pitch Arm Coordinate System Orientation	46

Figure		Page
13	Description of Torque Tube Coordinate System Rotations Required for Definition of the Pitch Arm Coordinate System	50
14	Description of the Relationship Between the Fixed Hub Coordinate System and the Fixed Control System Coordinate System	51
15	Description of the Relationship Between the Rotating Control System Coordinate System Associated with First Blade and the Fixed Control System Coordinate System	52
1.0		J.
16	Relationship Between Control Rod Axis and Rotating Hub Coordinate System	54
17	Fixed Fuselage Structure Coordinate System and Examples of Local Fuselage Structure Coordinate Systems	56
18	Relationship of the Local Support Structure Coordinate System and Fixed Hub Coordinate System Required at Shaft-Rotor	
	Hub Interface	58
19	Overall Iterative System Flow	74

# LIST OF TABLES

Table						Page
1	Values of Norm for Normalization to Various Blade Tip Deflections for Various System Models	•	•	•	•	157
2	Control Parameter Input Locations and Corresponding Program Variables	•	•	•	•	168
3	Section Data Input Locations and Corresponding Symbols			•		180

#### INTRODUCTION

The information presented in this documentation report is specifically directed at providing a User's Manual for the Helicopter Aeroelastic Stability Analysis computer program (HASTA) developed under Army Contract Number DAAJ02-76-C-0032. The primary purpose of this report is to inform the reader of the capabilities of HASTA and to provide the information required to construct an input data deck and successfully execute the program. Information pertaining to the construction and operation of HASTA is also presented to facilitate minor program alterations which may be desirable for specific HASTA applications; for example, redimensioning of variables.

The HASTA program was developed to provide a suitable analysis for representing the interaction of a rotor with its aerodynamic and support environment such that the air and ground resonance stability characteristics of fully coupled helicopter/rotor systems can be adequately predicted. HASTA can be used to predict the complex modal behavior of a main or tail rotor operating in vacuo or in air, with or without the effects of rotor support structure flexibilities included. These rotor support structure flexibilities include anisotropic gearbox or transmission support flexibility, anisotropic control system flexibility, rotor drive shaft torsional flexibility, and anisotropic landing gear flexibility, in addition to flexibilities associated with an elastic support structure such as the helicopter fuselage. The HASTA program is not limited to the consideration of a single type of rotor, but can be applied to a variety of rotor types including rigid to fully articulated, gimballed, teetering, flexstrap, and bearingless, the last type having pitch control provided to the blades through torque tubes.

The HASTA program is primarily a FORTRAN IV program developed for use on IBM 360/65 computer systems. However, to reduce program running time, several matrix multiplication-related subroutines are in assembler language. The program in its present form has been developed to operate efficiently within the operational constraints of the USAAVRADCOM IBM 360/65 in St. Louis through the Applied Technology Laboratory terminal. Therefore, the present version is limited to the consideration of rotor systems consisting of identical blades equally spaced azimuthally. This restricts array dimensions such that in combination with the use of an overlay structure, the requirement for a core storage of less than 250K is satisfied. High core requirements result due to the necessity of employing

double precision real and complex variables to achieve satisfactory convergence and accurate solution eigenvalues, eigenvectors, and mode shapes on an IBM 360/65 system. On elimination of the present program array dimension restrictions, a rotor consisting of identical blades not equally spaced azimuthally can be considered at a cost of higher core storage requirements and longer running time. The mathematical analysis on which HASTA is based allows for consideration of a rotor having non-identical blades. The program modifications necessary for considering non-identical blades are not complicated and can be easily implemented if the capability is required.

The CPU time required for a HASTA run is primarily dependent on the number of iterations executed and the dimensional size of the final matrix for which the determinant must be obtained on each iteration. The final matrix size is dependent on both the degree of interharmonic coupling allowed and the complexity of the coupled rotor/helicopter system of interest. The CPU time for a run is also dependent upon the number and complexity of the blade and fuselage representational sections. This latter CPU time dependency is of secondary importance in the determination of CPU running time. A rough estimate for the CPU time required for a run, based on times encountered for program execution on the AVRADCOM IBM 360/65 in St. Louis, is

# time = (# iterations allowed)\*MXQ\*MXQ minutes

where the number of iterations allowed is equal to the sum of the iterations allowed for each starting eigenvalue of each case of the run and MXQ is the number of rows in the final matrix.

Auxiliary equipment required for execution of the computer program consists of a card reader, a line printer, a tape or disk storage unit, and a card punch. Input data for the HASTA program is presently read in on cards. The program results, which are printed in a complex variable form, consist of the solution eigenvalues and their corresponding mode shapes defined relative to both the local blade coordinate systems and to the hub (or disk plane) coordinate systems. The disk plane mode shapes are printed in both complex variable and polar form, the latter allowing quick assessment as to the degree of coupling and phasing relationship occurring between blade motions. If desired, the resulting mode shapes can be punched on cards for subsequent use. The program can be readily modified to read aerodynamic coefficient input data from tape or disk data sets

as well as redimensioned for specific applications. It is recommended that the user consult his systems programmer if any program modifications are to be made.

A detailed discussion of the basic mathematical analysis on which the HASTA analysis largely is based is contained in Reference 1. Additional mathematical analysis was developed and used in the construction of the HASTA analysis to extend its capabilities. This analysis is discussed in Reference 2.

672 to 68

<sup>1.</sup> Sutton, Lawrence R., and Gangwani, Santu T., THE DEVELOP-MENT AND APPLICATION OF AN ANALYSIS FOR THE DETERMINATION OF COUPLED TAIL ROTOF/HELICOPTER AIR RESONANCE BEHAVIOR, USAAMRDL-TR-75-35, Eustis Directorate, US Army Air Mobility Research and Development Laboratory, Fort Eustis, Virginia, August 1975.

Sutton, Lawrence R., and White, Jr., Richard P., THE DEVELOPMENT AND APPLICATION OF AN ANALYSIS FOR THE STABILITY BEHAVIOR OF BEARINGLESS MAIN ROTOR SYSTEMS, Letter Report SRL 14-77-3, RASA Division, Systems Research Laboratories, Inc., 1055 J. Clyde Morris Blvd., Newport News, Virginia.

#### OVERALL PROGRAM CAPABILITIES

The HASTA program can predict the aeroelastic stability behavior of fully coupled helicopter/rotor systems of various degrees of complexity in hover or forward flight. gram is applicable to both tail rotor and main rotor systems with several different types of rotor support allowed. With a rotor support structure and aerodynamic effects included in the system model either air resonance or ground resonance stability results may be obtained depending on the rotor support structure model and its end conditions (free or cantilevered to ground). When a rotor support structure is not involved in the system model o only a rotor control system is involved, the rotor hub is assumed to be cantilevered to ground and rotor air resonance stability results are obtained if aerodynamic effects are included. If aerodynamic effects are not included, coupled or uncoupled normal mode results may be obtained. In all cases the results consist of solution eigenvalues in complex notation containing the damping and frequency characteristics of the modes and the corresponding mode shapes, i.e., the force, moment, deflection, and slope distributions along the blade span.

The rotor configurations which can be considered by the present form of the HASTA analysis, due to program dimensional and coding restrictions, consist of those having any number of identical flexible blades equally spaced azimuthally. Several different types of rotors can be considered. These include a rigid to fully articulated (hinged blade) rotor, a gimballed rotor, a teetering rotor, a flexstrap rotor, and a torque tube-type bearingless rotor. The orientation and amplitude of the gravitational field and flight velocity to which the rotor is exposed are treated as part of the rotor configuration and can be considered.

HASTA represents the blades comprising the rotor by a lumped-parameter approach in which up to 35 spanwise sections of the blade are allowed. This representation allows for the inclusion of all blade characteristics believed to be of significance. These characteristics, which are discussed in detail in the next section, include the blade geometric, structural, and aerodynamic properties. Regarding the aerodynamic representation, HASTA is capable of using airfoil coefficient data provided in series coefficient form and/or tabular form, one of the acceptable forms being that of the C-81 data tables. The blade lumped-parameter approach also allows consideration of blades having an applied control torque, a pitch bearing,

a flap hinge, and/or a lead-lag hinge. In addition, the applied control torque-imposed forces and moments acting on the blades of the more recent flexstrap and bearingless rotor concepts can be considered. By properly combining the blade representation with the rotor hub boundary conditions, most rotor system configurations can be represented and investigated by the HASTA program.

The HASTA program has the capability to include the effects on the rotor aeroelastic stability behavior of an anisotropically supported flexible swashplate-type control system. Basically, in this control system the flexible swashplate is anisotropically supported by linear spring-damper units, such that in combination with the control rod stiffness and damping characteristics any desired control system collective and cyclic stiffness and collective and cyclic damping may be ob-The HASTA program is capable of correctly representing the control system effects on system modal behavior when an elastic support structure is included, in that the linear spring-damper units are taken to be attached to the elastic support structure, instead of ground. Regarding the control rod representation, the program is only capable of considering the control rods to act in a direction parallel to the rotor drive shaft in the case of articulated, gimballed, or teetering rotor systems. For a flexstrap or bearingless rotor, the program is capable of considering the orientation of the control rods in that control rod angularity is usually more prevalent in these rotor types. The control rod for all rotor types is taken to be attached to the swashplate and pitch arm by swivel ball joints such that the control rods cannot carry moments or transverse loadings.

HASTA has the capability of including an elastic support struc-This elastic support structure is also represented by a lumped-parameter approach similar to that used for the blade representation, but it is simplified in that the elastic support structure is not a rotating member. A maximum of 15 elastic support structure sections are allowed in the representation of the elastic support structure unless there are more than 25 blade sections. Then the condition that the total number of blade and elastic support sections cannot exceed 40 must be satisfied. All elastic support structure geometric, structural, and aerodynamic properties believed to be of significance can be considered by this lumpedparameter representation. Elastic support structure aerodynamics, besides being based on airfoil data of the series or tabular form, can also be based on blockage (flat plate drag) effects or linearized NACA 0012 airfoil data.

program is also capable of considering the magnitude and orientation of the flight velocity vector acting on sections of the elastic support structure. The consideration of torsional spring-damper units on the elastic support structure provides the capability of representing anisotropic gearbox or transmission mounting stiffnesses and anisotropic landing gear stiffness. The landing gear stiffness representation used in combination with the elastic support structure cantilevered to ground allows the capability to determine ground resonance characteristics.

A fully coupled helicopter/rotor system will experience interharmonic coupling of motions. That is, motions at a given
frequency will couple with motions occurring at n/rev above
and below the given frequency, where n is an integer. In
particular, the aerodynamic environment acting on a blade will
provide interharmonic coupling of motions of the blade as a
result of aerodynamic damping effects. The inclusion of a
swashplate control system having collective and cyclic stiffnesses will provide interharmonic coupling of the motions of
one blade to the motions of another. The existence of an
elastic support structure in the system will provide interharmonic coupling between blade motions and the support structure motions. HASTA is capable of including these interharmonic
coupling effects.

A significant feature of the HASTA program is its capability to make use of a predefined phasing relationship between the motions of the blades of a rotor (blade phasing option). option, however, is only applicable to rotor systems having the blades equally spaced azimuthally. By specification of the type of blade motion of interest; e.g., umbrella, forward cyclic, backward cyclic, and reactionless; and the type of rotor system of interest, the motion of each rotor blade can be defined in terms of a reference blade. This allows the analysis to consider only one blade instead of several blades so that the size of the problem is much smaller. Thus, the HASTA analysis running time is substantially shorter when this option is used. In addition, solution eigenvalues associated with blade motion relationships other than that specified are removed from the problem, which facilitates a more rapid convergence to the desired results. Use of this option, due to the present dimensional restrictions imposed to satisfy core requirements, is the only manner in which HASTA can be applied to investigations of the aeroelastic stability characteristics of rotor systems at the present time.

In addition to obtaining solution eigenvalues by iterating from inputted starting eigenvalues based on prior experience or engineering judgment, HASTA is also capable of performing a scanning procedure to facilitate the determination of solu-This eigenvalue scanning procedure, based tion eigenvalues. on input, determines the final matrix determinant values in complex variable form for a rectangular grid of stability and frequency values over a range of stability (eigenvalue real part) and frequency (eigenvalue imaginary part) values. interpolation scheme is then used to determine possible solution eigenvalues, which are then treated as starting eigenvalues. Generally, due to the number of grid points required to avoid missing possible roots, the efficiency of using this procedure to obtain solution eigenvalues is poor compared to the use of guessed starting eigenvalues. Thus, this procedure should only be used as a last resort.

#### HELICOPTER/ROTOR SYSTEM MODEL

The HASTA computer program was developed from an analysis which models helicopter/rotor dynamic systems of varying degrees of complexity. These systems, besides having a rotor comprised of flexible blades subjected to various restraint conditions imposed by hinges and the manner in which control torque is provided, may have a control system, various local rotor support conditions, and an elastic rotor support structure. A knowledge of the types of system configurations which might be treated is necessary to use the HASTA program properly. The system model configurations allowed may consist of several basic model components which can be categorized as:

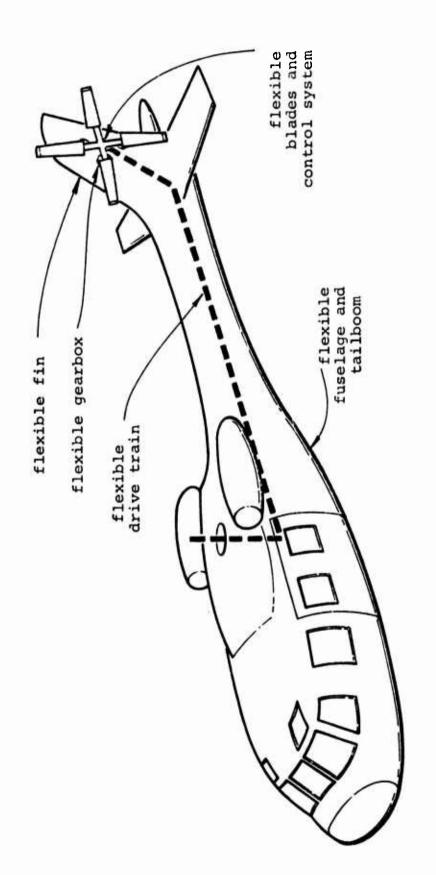
- 1. Rotor blade structure
- 2. Rotor hub restraints
- Control system
- 4. Control rod configurations
- 5. Elastic rotor support structure
- 6. Gearbox or transmission mounting flexibilities
- 7. Rotor drive shaft torsional flexibility

The computer program can mathematically model each of these basic model components individually and/or in combination with other basic model components. When all of the model components are included, the coupled and interdependent modal behavior of a total system such as that depicted in Figure 1 may be predicted. A description of the modeling of the individual system components is given in the following sections.

#### ROTOR BLADE MODEL

The basic blade model allows for the inclusion of all blade characteristics believed to be of significance in the determination of blade modal behavior. These are as follows:

- 1. Orientation of the blade shear center axis by precone and presweep distributions
- Location of the blade shear center axis (axis about which the blade cross section will rotate when perturbed)



A Representative System That Can Be Considered. Figure 1.

- 3. Localized rigid offsets of the shear center axis in the flapwise, edgewise, and spanwise directions (a spanwise offset denotes that the blade is rigid over this offset distance)
- 4. Variable twist distribution about the blade shear center axis including collective pitch
- Mass distribution and edgewise, flapwise, and torsional inertia distributions
- 6. Edgewise location of the center of mass relative to the blade shear center
- Edgewise, flapwise, and torsional bending stiffness distributions and inclusion of centrifugal stiffening effects
- 8. Localized torsional spring-damper unit application about the flapwise, edgewise, and spanwise directions
- 9. Structural damping
- 10. Gravitational perturbation moment effects
- 11. Edgewise location of blade aerodynamic center axis relative to blade midchord
- 12. Chord length distribution
- 13. Aerodynamic effects including cyclic pitch, aerodynamic damping and Theodorsen's unsteady aerodynamic effects
- 14. Up to five different airfoil sections along blade span with the aerodynamic coefficients determined from either series coefficient data and/or airfoil table data

The blade characteristics listed above are modeled by utilizing a lumped-parameter approach in which the blade is represented by consecutive sections from the blade tip to root. In this sectional representation, the blade is divided into a finite number of sections. Each blade section is allowed a specified orientation (precone, presweep, and pitch) and is located in space by specification of the location of its inboard end. In addition, each section may consist of the following characteristic groups: shear center axis rigid offsets including a rigid

spanwise length, local bends in the shear center axis, a centrifugally stiffened elastic length or either flexstrap or bearingless rotor pitch control-imposed restraints, concentrated torsional spring-damper units, mass and inertias, and aerodynamics. A pictorial representation of these blade characteristic groups and the order in which they are considered, proceeding outboard to inboard along the blade, is given in Figure 2. The consideration of local shear center axis bends allows for the change in the shear center axis orientation from one section to another.

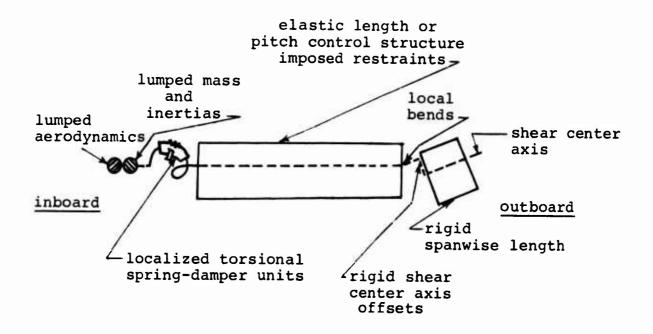


Figure 2. A General Blade Section.

The concentrated spring-damper units, shear center axis bends, and rigid offsets are allowed to occur relative to the local blade edgewise, flapwise, and spanwise directions at their point of application. Up to 35 blade sections may be used to represent the blade as a piecewise continuous structure. As an example of the lumped-parameter approach, a sectionalization of a blade having only mass, elastic, and coning properties is depicted in Figure 3.

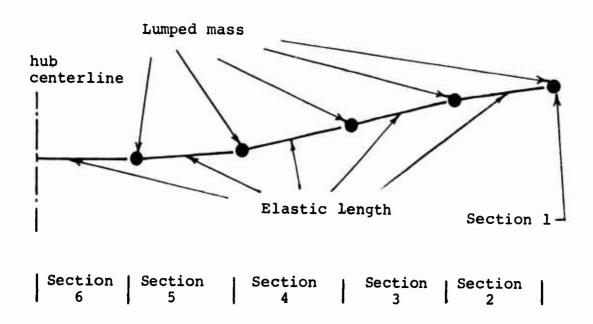


Figure 3. Simplified Sectionalization of a Blade Structure.

In addition to representing the basic blade geometric, structural, and aerodynamic characteristics, the blade model must also allow for the consideration of blade geometric and loading discontinuities which occur in the different rotor configurations allowed due to hinges on the blade and/or the manner of pitch control. An articulated rotor blade, besides having an applied control torque and pitch bearing, may have a flap hinge and/or a lead-lag hinge. The representation of a flap hinge, if required in the blade model, is accomplished in either of two ways. One way is to use a blade section with a torsional spring-damper unit (an allowed basic blade characteristic) having required torsional stiffness and damping value, with the condition that the axis of the spring-damper unit coincides with the flap hinge axis. This representation would be used in cases where the oscillatory flapping motion about the flap hinge is externally restrained (damped). The alignment of the torsional spring-damper unit axis with the flap hinge is achieved by proper location and orientation (through the use of section precone, presweep, and pitch angles) of the section containing the spring-damper unit.

The second way is to represent the flap hinge analytically by considering a discontinuity in the oscillatory flapping motion to occur at the flap hinge location and the condition that the local oscillatory flapwise moment must be zero at the hinge. For example, the oscillatory flapping motion of a rotating rigid blade attached to a rigid rotor hub by a flap hinge can be considered to be a flap angle discontinuity at the flap hinge. This method of representing a flap hinge does not allow inclusion of external damping of the oscillatory flapping motion. Both of these flap hinge models are included in the computer program to allow the user the choice of the most suitable model for particular program applications.

The representation of a lead-lag hinge, if required, is accomplished in either of two ways in a fashion similar to that of the flap hinge representation. The first way is to use a blade section with a torsional spring-damper unit having the required torsional stiffness and damping values and having its axis coincident with the lead-lag hinge axis. This representation would be used if the oscillatory lead-lag motion about the lead-lag hinge is externally damped. The second way is to represent the lead-lag hinge analytically by considering a discontinuity in the oscillatory lead-lag motion to occur at the lead-lag hinge location and the condition that the local oscillatory edgewise moment must be zero at the hinge. ternal damping of the oscillatory lead-lag motion is not allowed in this representation of the lead-lag hinge. computer program includes both of these lead-lag hinge representational models to allow the user the choice of the most suitable model.

The representation of a pitch bearing, if required, is accomplished by considering a discontinuity in the oscillatory pitching motion to occur at the pitch bearing location and the condition that the local oscillatory torque at the pitch bearing must be zero. The concept of a pitch angle discontinuity is similar to that of flap and lead-lag angle discontinuities except that it occurs about the pitch bearing axis. The control rod effects on an articulated blade, if they are to be included, are represented by considering the control rod to apply an oscillatory torque (torque discontinuity) to the blade shear center axis at the effective spanwise application point of this torque. The torque discontinuity is normally considered to be applied outboard of the pitch bearing location.

The models for the flap and lead-lag hinges can represent large pitch-flap coupling  $\delta_3$  and pitch-lag coupling  $\alpha_1$  effects. This is possible since the flap and lead-lag hinge

axes may be placed in any desired orientation by the use of local section precone, presweep, and pretwist angles. An alternate model for representing pitch-flap and pitch-lag coupling is also allowed. In this model the flap and lead-lag hinges are taken to act about the local edgewise and flapwise axes, respectively, with the required coupling of blade motions taken into account on specification of pitch-flap and pitch-lag coupling factors.

A blade of the flexstrap or bearingless type does not have flap or lead-lag hinges or a pitch bearing. Instead, the flapwise, edgewise, and torsional motions inboard of the effective pitch control point are allowed by the flexibilities inherent in the blade retention structure. While these flexibilities can be represented by the basic blade model elastic properties, the relationship between the elastic blade motions is also dependent upon the oscillatory forces and moments in three mutually orthogonal directions acting on the blade shear center axis due to the restraint provided by the blade pitch control structure.

In the flexstrap-type blade model the control rod is assumed to be attached to a flexible pitch arm having length and having orientation in three mutually orthogonal directions. This pitch arm is considered to be rigidly attached to the blade. The oscillatory forces and moments acting on the blade shear center axis at the effective pitch control point can be defined in terms of the pitch arm properties, local blade perturbation (oscillatory) slopes and deflections, and the oscillatory displacements of the control rod attachment point to the pitch arm. Thus, instead of dealing with six force and moment discontinuities, the three control rod attachment point oscillatory displacements are considered as discontinuity quantities (restraint unknowns).

In the bearingless-type blade model that can be treated by the computer program, the control rod is assumed to be attached to a rigid pitch arm having length and having orientation in three mutually orthogonal directions. The pitch arm is considered to be rigidly attached by a fitting to the inboard end of a flexible torque tube having length and having orientation in three mutually orthogonal directions. The torque tube at its outboard end is taken to be rigidly attached to the blade at the blade shear center axis. The pitch arm-torque tube fitting also is considered to have a shaft (spur) extending inboard along the torque tube axis which is restrained by a spherical bearing attached to the rotor hub. This spur, which is allowed flexibility in three mutually orthogonal directions, is free to slide in the direction of its lengthwise axis and to rotate about three mutually orthogonal axes

at the spherical bearing. The oscillatory forces and moments acting on the blade due to this torque tube pitch control structure can be defined in terms of the properties of this structure, local blade perturbation (oscillatory) slopes and deflections, control rod forces, and spherical bearing translations. The three control rod forces and three spherical bearing translations constitute the discontinuity quantities or restraint unknowns for the bearingless-type blade model.

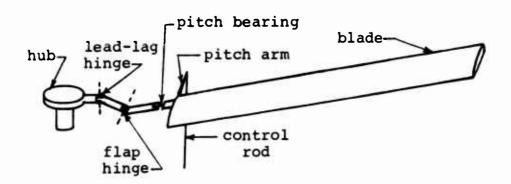
In the flexstrap or bearingless-type blade models, the pitch- $\delta_3$  and pitch-lag  $\alpha_1$  couplings are automatically included and are directly related to the blade retention strap or beam and the pitch control structure representation. A significant amount of elastic coupling of flapwise, edgewise, and torsional deflections can occur with both of these blade models due to the flexibilities inherent in the retention strap or beam structure and the fact that the control rod does not remove all of the blade torque. Since the elastic couplings are very dependent on the rapidly changing orientation of the retention strap or beam stiffness parameters, a sufficient knowledge of the mean coning, lag, and pitch along the retention structure due to built-in and mean elastic deformation is required. Because of these elastic couplings, the retention strap or beam must be represented by more lumped-parameter sections for a given spanwise length than is required in the representation of the rest of the blade.

The pitch control and blade retention structure for the three types of blade models discussed above are depicted in Figure 4. The blade models necessary for considering a teetering or gimballed rotor are achieved by using the articulated blade model with the required representational options.

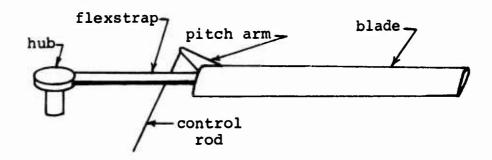
#### ROTOR CONFIGURATION MODEL

The rotor configuration model considered in the development of the representational analysis may consist of any number of flexible blades which can be arbitrarily located azimuthally. However, as noted in the introduction, the computer program was limited to rotor configurations consisting of identical flexible blades by the program coding and to rotor configurations consisting of any number of blades equally spaced azimuthally by restriction of array dimensions. These rotor configuration program limitations can be easily removed by increasing variable dimensions where required and by modifying the analytical coding.

## Articulated blade



## Flexstrap blade



# Bearingless blade

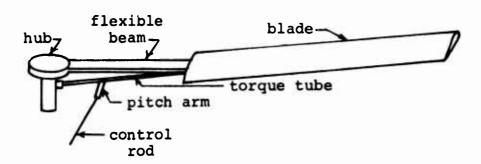


Figure 4. Pitch Control and Blade Retention Structure for Three Different Types of Blade Models.

The rotor configuration models allow consideration of the orientation and amplitude of the gravitational field and the rotor hub flight velocity. These orientations are specified relative to the reference (advancing) blade position. The rotor configuration models can be considered to be rotating in either a clockwise or counterclockwise (conventional) direction. The blades of all rotor configuration models which can be considered by the computer program can be considered to be cantilevered to a rigid rotor hub which may have degrees of freedom relative to its attachment to the rotor shaft. Types of rotor configuration models that can be considered are:

- A rigid rotor model that is constructed with the articulated blade model (flap and lead-lag hinge not included)
- 2. A partial to fully articulated rotor model constructed with the articulated blade model
- 3. A flexstrap rotor model constructed with the flexstrap blade model
- 4. A bearingless rotor model constructed with the bearingless blade model
- 5. A gimballed rotor (more than two blades) constructed with the articulated blade model
- 6. A teetering rotor (two blades only) constructed with the articulated blade model

The first four types of rotor models listed above require the rigid rotor hub to be cantilevered to the rotor shaft. The gimballed rotor model assumes the rigid rotor hub to be attached to the rotor shaft such that it is free to rotate about two mutually orthogonal axes rotating in the plane perpendicular to the rotor shaft at the rotor hub attachment point. The teetering rotor model assumes the rigid rotor hub to be attached to the rotor shaft such that it is free to rotate about one axis rotating in the plane perpendicular to the rotor shaft at the rotor hub attachment point.

#### CONTROL SYSTEM MODEL

The model of the rotor control system is based on the assumption of a swashplate-type control system. The main component of the swashplate control system model, depicted in Figure 5,

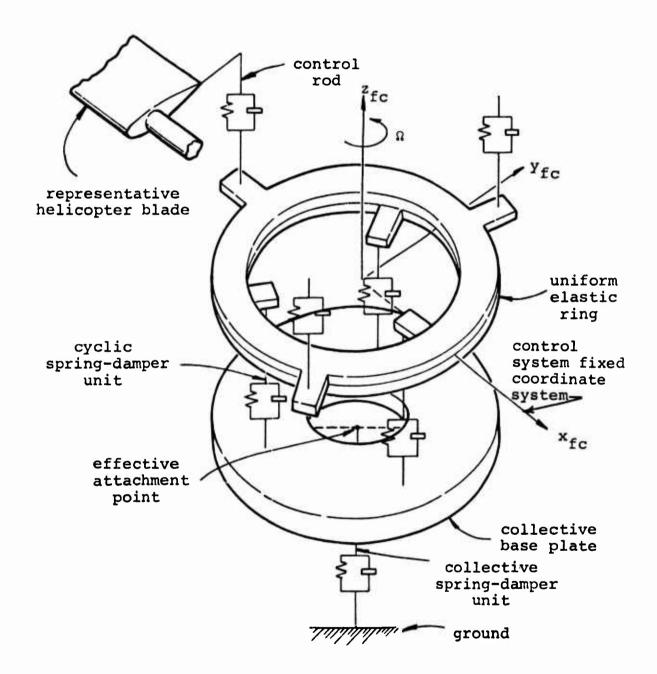


Figure 5. Swashplate Control System Model and Fixed Coordinate System for Counterclockwise Rotating Rotor.

is represented by a flexible ring having uniform mass distribution around its circumference and consisting of upper and lower portions. Both portions of the ring are allowed to translate along the rotor shaft axis ( $z_{fc}$ -axis) and ro-

tate about two mutually orthogonal axes perpendicular to the rotor shaft axis. The upper portion of the ring also rotates with the blades about the rotor shaft axis. The lower portion of the ring, which does not rotate with the blades, is supported by a finite number of supports located azimuthally around the ring. These supports have linear stiffness and damping characteristics. The collective base plate to which the ring supports are attached is assumed to be attached to ground or to the rotor support structure, if included in the system model, by a linear support having an effective stiffness and damping value. The forces parallel to the rotor drive shaft axis acting on the swashplate from the control rods are passed through the swashplate control system model and are applied to rotor support structure, if included. Thus, by variation of the stiffness and damping characteristics and azimuthal location of the supports involved, any degree of control system anisotropic flexibility can be modeled.

#### CONTROL ROD MODEL

There are two types of control rod models which can be considered by the HASTA program. One type can only be used in conjunction with the articulated blade model. The other type can only be used with flexstrap and bearingless blade models. In both control rod models, the control rod is assumed to have axial stiffness and damping characteristics and to be connected to the pitch arm and swashplate (or ground, if there is no swashplate) by swivel ball joints. Attached in this manner, the control rods cannot carry moments or transverse loadings. In the control rod model used with an articulated blade model, the control rod is assumed to apply only control torque to the blade and to act along a line parallel to the rotor drive shaft axis.

The control rod model used with a flexstrap or bearingless blade model is much more complex than that which is used with an articulated blade model. The primary reasons for this model complexity are: (1) the large angularity of the control rod occurring in these rotor types; and (2) the strong elastic coupling created by the pitch control structure in the retention strap or beam flapwise, edgewise, and torsional degrees of freedom. In addition, because of the angularity of the control rod and the offset due to the pitch arm, blade motions in the inplane and flapwise directions are coupled

through the control system. Thus, in addition to control rod stiffness and damping characteristics, the orientation and location of the control rod must also be considered.

The stiffness and damping characteristics of the control rods are also included with those associated with the swashplate representation, discussed previously, in order to adequately represent the cyclic and collective stiffness and damping acting on the blades due to the control system and control rods.

#### ROTOR ELASTIC SUPPORT STRUCTURE MODEL

The rotor elastic support structure model allows for the inclusion of all geometric, structural, and aerodynamic characteristics believed to be of significance. These characteristics are essentially the same as those which were listed for the blade model. Since the support structure is not subjected to a constant rotational speed, the mass, inertia, and aerodynamic effects on the support structure behavior differ from those for a blade. In particular, the support structure mass and inertia distributions do not provide centrifugal stiffening or damping effects, and the support structure aerodynamic environment does not provide interharmonic coupling of support structure motions. The support structure aerodynamics can be based on blockage (flat plate drag) effects or a series representation (linearized aerodynamics) for a NACA 0012 airfoil section. The magnitude and orientation of the steady air velocity acting on the support structure is allowed to vary along the support structure length.

The rotor elastic support structure characteristics are modeled by using a lumped-parameter approach similar to the technique used to model the blade characteristics. The support structure is represented by consecutive sections from its tip to its attachment to the rotor hub. The tip of the support structure is generally that part of the support structure farthest from the rotor hub and is allowed to be either free in space or cantilevered to ground. Thus, for the fully coupled system depicted in Figure 1, the fuselage-tailboomfin structure would be represented by consecutive sections from the front end of the fuselage, which would be treated as free in space, to the tail rotor hub.

The lumped-parameter sectional representation is used for the entire rotor support structure of interest, including the rotor gearbox or transmission mounting flexibilities and the rotor drive shaft, except for the drive shaft torsional

flexibility, which is treated in a different manner. Because of the similarity of the support structure and blade modeling techniques, Figure 2 is also valid for a support structure section on the condition that the outboard end of the section depicted is taken to correspond to the tipward end and the inboard end is taken to correspond to the end of the support structure section toward the rotor. Thus, the order in which the sectional characteristics can be considered in going outboard to inboard along a blade section is identical to the order that can be considered in going from the tipward end to the rotor attachment end of the support structure section. The section characteristics corresponding to the pitch controlimposed restraints which were allowed for a blade section are not allowed for a support structure section. A maximum of 15 support structure sections can be used to represent the entire support structure unless more than 25 blade sections are used in modeling the blade structure. Then the condition that the total number of blade and support structure sections cannot be greater than 40 must be satisfied.

#### GEARBOX OR TRANSMISSION MOUNTING MODEL

Rotor gearbox or transmission mounting flexibilities are represented by using the localized torsional spring-damper unit capabilities of a rotor support structure section. In particular, localized torsional spring-damper units having torsional stiffness and damping characteristics are applied about two mutually orthogonal axes at the attachment of the gearbox or transmission to its support structure (e.g., the fuselage). The specific orientation of the two axes relative to the support structure is accomplished through the use of the section orientation angles. By variation of the stiffness and damping characteristics of the two torsional spring-damper units, any degree of anisotropy in rotor gearbox or transmission mounting can be modeled.

#### ROTOR DRIVE SHAFT TORSIONAL FLEXIBILITY MODEL

In representing the drive shaft torsional flexibility, the rotor drive shaft, whether it be for a main or tail rotor, is assumed to be constrained in torsion at the main rotor transmission. The model of the torsional characteristics of the drive shaft system was formulated by considering a localized torsional spring at the root of each blade whose inplane flexibility is equivalent to the drive shaft torsional flexibility. The blade edgewise moments at the rotor hub are not allowed to provide torque to the shaft and thereby to the rest of the support structure since the torque on the rotor

shaft is assumed to be removed by the transmission. This torsional spring model is considered independent of the blade and support structure sectional representation and should not be construed to be modeled by use of blade or support structure section characteristics.

#### COORDINATE SYSTEMS

An understanding of the fundamental coordinate systems associated with the representation of the rotor/helicopter system model components and their relative orientation and use in defining program input variables is a prerequisite to proper use of the HASTA program. The information presented in this section is directed toward providing the user with this under-In particular, the coordinate systems pertaining standing. to the representation of the rotor hub, blade structure, pitch control structure, control system, and rotor elastic support structure, and the manner in which they are related for main or tail rotors rotating clockwise or counterclockwise, are described. The coordinate system relationships required at the rotor shaft-rotor hub interface for system representational continuity are also discussed. The coordinate system-related definitions of the gravitational field and free stream velocity orientation variables are not provided here but are presented in the Description of Input Data section of this report.

In the following discussion, two sets of coordinate systems are presented simultaneously for rotating system model components. One set of coordinate systems is pertinent to the consideration of a counterclockwise rotating rotor system. The second set of coordinate systems is associated with the consideration of a clockwise rotating rotor system. tion of rotation of a rotor system is based on that observed from above (main rotor) or from the port side of a helicopter (tail rotor). Six fundamental rotor system arrangements (two main rotor and four tail rotor) which are determined by combinations of the rotor system rotational directions and the location of the rotor attachment are depicted in Figure 6 as viewed from the port side of a helicopter. In this figure, the rotor disk plane for a rotor system arrangement coincides with the corresponding  $x_f - y_f$  plane where the  $(x_f, y_f, z_f)$ coordinate systems shown are the fixed (non-rotating) hub coordinate systems for the various rotor system arrangements. The detailed definition of fixed hub coordinate systems for counterclockwise and clockwise rotating rotor systems is provided below. In Figure 6 a rotor blade with its leading edge shaded is shown in the reference blade position (i.e., along the  $x_{\varepsilon}$  axis) for each rotor system arrangement, to further clarify the direction of rotation. The control system, represented by a ring, and the rotor drive shaft are depicted for each rotor system arrangement to show that although the fixed hub coordinate systems may be identical for two rotor arrangements, the arrangements differ in the location of drive shaft and control system. Specifically, rotor system arrangements

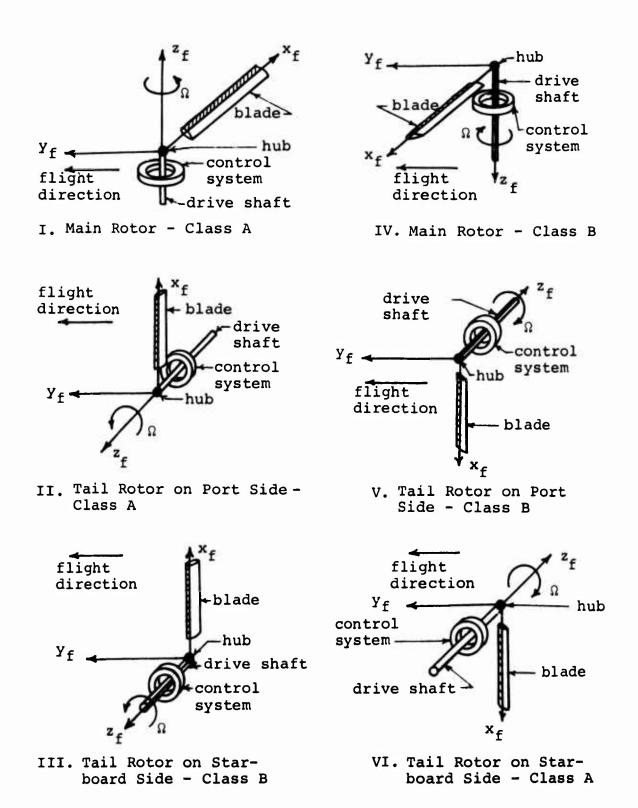


Figure 6. Six Possible Rotor System Configurations.

having the drive shaft and control system in the  $-z_{\rm f}$  direction are denoted as class A arrangements (arrangements I, II, and VI) and rotor system arrangements having the drive shaft and control system in the  $z_{\rm f}$  direction are denoted as class B arrangements (arrangements III, IV and V).

As originally developed, the HASTA program was based on a representational analysis for class A type arrangements. this form, the analysis was intended to be used for a rotor rotating counterclockwise when viewed from the side of the disk opposite the drive shaft. However, since a clockwise rotating rotor can be viewed from a position and orientation in which the rotational direction appears counterclockwise, the HASTA program is applicable to clockwise rotating rotors, providing proper coordinate systems are used in defining program input variables. For class B type arrangements (arrangements III, IV, and V), the HASTA program is applicable if extra care is taken in representing the rotor hub-drive shaft interface conditions and if the signs of input parameters associated with the effects of the elastic support structure motions on the pitch control structure for flexstrap and bearingless type rotors are changed. Both of these requirements are discussed in detail below. Regardless of whether a counterclockwise or clockwise rotating rotor system is considered, the rotor thrust is always positive in the fixed hub coordinate system z<sub>f</sub> direction and the control system (swashplate) displacement is always positive in the direction. The coordinate systems for various system model components will now be discussed in detail.

#### ROTOR HUB COORDINATE SYSTEMS

The coordinate systems associated with the rotor hub consist of a fixed (non-rotating) hub coordinate system (used in Figure 6) and a rotating hub coordinate system corresponding to each blade of the rotor. The fixed hub coordinate system has its origin at the intersection of the rotor drive shaft centerline and the rotor disk plane, which is perpendicular to the shaft centerline.

The rotor disk plane is the plane in which the rotor blades rotate at drive shaft rotational speed if the rotor blades are considered to be unconed, unswept, and unpitched (no pitch due to either pitch control or twist). The fixed hub coordinate system z-axis coincides with the rotor drive shaft centerline and is positive in the direction of the rotor

rotational velocity vector. The x and y axis of the fixed hub coordinate system both lie in the rotor disk plane. The x-axis is defined to be located on the advancing side of the rotor disk plane and oriented in space perpendicular to the helicopter longitudinal axis. The azimuthal location of the fixed hub coordinate system x-axis coincides with the reference blade position used for defining the azimuthal location of all blades of the rotor. The y-axis is mutually orthogonal to the x and z axes producing a righthanded Cartesian coordinate system. The location of the fixed hub coordinate system axes;  $x_f$ ,  $y_f$ , and  $z_f$ , was shown in Figure 6 for the different rotor system arrangements depicted.

To provide further clarification, the fixed hub coordinate system  $(x_f, y_f, z_f)$  is depicted in general in Figure 7 for the two directions of rotor rotation. The  $y_f$ -axis has not been shown parallel to the flight direction nor the  $z_f$ -axis

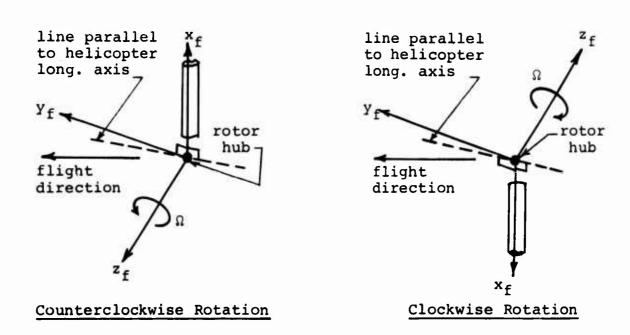


Figure 7. Fixed Hub Coordinate Systems for Two Directions of Rotor Rotation.

perpendicular to the flight direction since the rotor disk plane may be skewed with respect to the flight velocity vector. For an unconed, unpitched, and unswept blade at the reference blade position, as depicted in Figure 7, the  $y_f$ -axis is parallel to the blade chord and positive toward the blade leading edge. Also in Figure 7, a line parallel to the helicopter longitudinal axis has been drawn through the fixed hub coordinate system origin for the two directions of rotation. The  $x_f$ -axis, as previously defined, is perpendicular to this line. The  $y_f$ -axis, when viewed from a position on the  $z_f$ -axis, would appear to be coincident to this line.

The rotating hub coordinate systems, one corresponding to each blade, have the same origin and z-axes as the fixed shaft coordinate system, but their x- and y-related axes in the basic rotor plane are rotating about the  $z_{\rm f}$ -axis with a constant rotational speed of  $\Omega$  rad/sec. The rotating hub coordinate systems have their x-axis along the spanwise axis of the blades if the blades are unconed, unpitched, and unswept.

These coordinate systems can be related to the fixed hub coordinate system by the coordinate transformation

$$\begin{cases}
\vec{I}_{rm} \\
\vec{J}_{rm} \\
\vec{K}_{rm}
\end{cases} = \begin{bmatrix}
\cos(\Omega t + \phi_{m}) & \sin(\Omega t + \phi_{m}) & 0 \\
-\sin(\Omega t + \phi_{m}) & \cos(\Omega t + \phi_{m}) & 0 \\
0 & 0 & 1
\end{bmatrix} \begin{cases}
\vec{I}_{f} \\
\vec{J}_{f} \\
\vec{K}_{f}
\end{cases} (1)$$

where t is time (sec) and  $\phi_m$  is the angle between mth blade and the reference blade position at t = 0. The  $\overline{i}$ ,  $\overline{j}$ , and  $\overline{k}$  variables are unit vectors, with rm subscripts denoting the rotating hub coordinate system for the mth blade and f subscripts denoting the fixed hub coordinate system. The rotating hub coordinate system (x $_{rm}$ , y $_{rm}$ , z $_{rm}$ ) for the first blade relative to the fixed hub coordinate system is depicted in Figure 8 for the two directions of rotor rotation.

### Clockwise Rotation

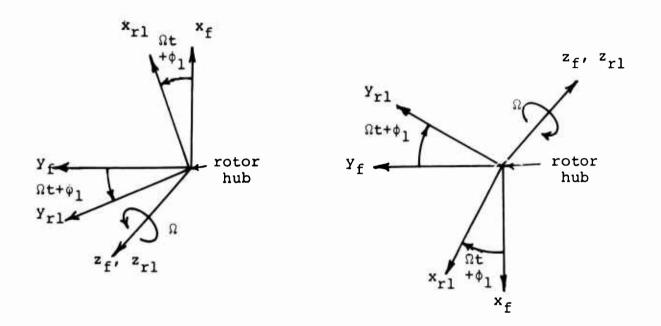


Figure 8. Fixed Hub Coordinate System and Rotating Hub Coordinate System Corresponding to the First Blade for Two Directions of Rotor Rotation.

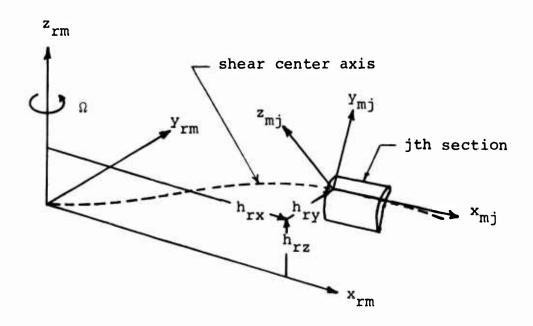
### BLADE COORDINATE SYSTEMS

In addition to the hub coordinate systems (rotating and non-rotating) previously discussed, there are blade coordinate systems defined which account for the mean orientation and deflection of the blade structure along its span.

The fundamental coordinate systems associated with the blade structure consist of the rotating local blade coordinate systems, one for each blade section. The local blade coordinate systems are attached to the blade sections in their mean deformed position and rotate about the fixed hub coordinate system z-axis with the same rotational velocity as the rotating hub coordinate systems. Thus, the orientation and location of the local blade coordinate systems are defined relative to the associated rotating hub coordinate system. In the sectional modeling procedure for the lumped-parameter representation of a blade, the blade is subdivided into a number of straight sections that may be oriented relative to each other. One of these blade sections for a deformed blade

rotating either counterclockwise or clockwise is depicted in Figure 9 relative to its associated rotating hub coordinate system and with its local blade coordinate system shown. As can be noted in Figure 9, the origin of the local blade coordinate system for a blade section is located on the section shear center axis at the inboard end of the blade section.

# Counterclockwise Rotation



## Clockwise Rotation

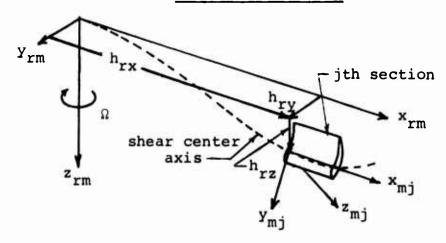


Figure 9. General Description of the Rotating Local Blade Coordinate System for a jth Blade Section.

The location of the origin of the local blade coordinate system for a blade section is defined relative to the associated rotating hub coordinate system axis by specification of the hrx, hry, and hrz values for the blade section. These three parameters, depicted in Figure 9, correspond to the three components of a position vector and are positive for a translation in the direction of the  $x_{rm}$ ,  $y_{rm}$ , and  $z_{rm}$  axes, respectively. The x-axis of a local blade coordinate system is coincident with the blade section shear center axis and is positive in the outboard direction. The y-axis is perpendicular to the x-axis and parallel to the chordline of the airfoil section at the coordinate system origin and is positive toward the blade leading edge. The z-axis is perpendicular to both the x and y axes such as to produce a righthanded coordinate system. As depicted in Figure 9 by use of an airfoil shape having camber, the positive direction of the z-axis of a local blade coordinate system is toward the airfoil surface, normally considered to be the upper surface for a positive angle of attack.

The orientation of the local blade coordinate system  $(x_{mj}, y_{mj}, z_{mj})$  for a blade section is defined relative to the associated rotating hub coordinate system  $(x_{rm}, y_{rm}, z_{rm})$  by specification of the three angles;  $\Phi$ ,  $\Theta$ , and  $\Psi$ . These three angles, in the order listed, correspond to three consecutive rotations that must be applied to the rotating hub coordinate system (placed at the local blade coordinate system origin) to align it with the local blade coordinate system. In particular:

- $\Phi$  corresponds to local blade section presweep about the  $z_{\mbox{rm}}\text{-axis}$  and is positive in the direction that the rotor rotates,
- $^{\Theta}$  corresponds to local blade section precone about the preswept  $y_{rm}$ -axis and is positive if the outboard end of the section is rotated in the -z<sub>rm</sub> direction, and
- $\Psi$  corresponds to local blade section prepitch about the preswept and preconed  $x_{rm}$ -axis and is positive if the leading edge of the blade section is rotated in the preconed  $z_{rm}$  direction.

The consecutive application of these angles to obtain the orientation of a local blade coordinate system relative to the associated rotating hub coordinate system orientation is depicted in Figure 10 for a counterclockwise and a clockwise rotating rotor system.

# Counterclockwise Rotation $\mathbf{y}_{mj}$ $\mathbf{z}_{\mathtt{mj}}$ Clockwise Rotation Y<sub>mj</sub>

Figure 10. Description of the Rotating Hub Coordinate System Rotations Required for Definition of the jth Section Local Blade Coordinate System Orientation.

The orientation relationship between the rotating hub coordinate system and a local blade coordinate system is represented by the coordinate transformation

$$\begin{bmatrix}
\vec{i}_{mj} \\
\vec{j}_{mj}
\end{bmatrix} = \begin{bmatrix}
c \circ c \circ \\
-s \circ c \lor + c \circ s \circ s \lor \\
s \circ s \lor + c \circ s \circ c \lor \\
-c \circ s \lor + s \circ s \circ c \lor \\
-c \circ s \lor + s \circ s \circ c \lor \\
-c \circ s \lor + s \circ s \circ c \lor \\
-c \circ s \lor + s \circ s \circ c \lor \\
-c \circ s \lor + s \circ s \circ c \lor \\
-c \circ c \circ c \lor \\$$

where a short form of denoting the sine and cosine functions has been utilized (e.g., SΦ represents sin  $\Phi_j$  and CΦ represents cos  $\Phi_j$ ). The  $\bar{i}$ ,  $\bar{j}$ , and  $\bar{k}$  variables are unit vectors, with rm subscripts denoting the rotating hub coordinate system associated with the mth blade and mj subscripts denoting the local blade coordinate system for the jth section of the mth blade.

The local blade coordinate systems are the coordinate systems to which the blade slopes, deflections, forces and moments along the blade span are referenced. In particular, the blade state variables at the inboard end of the jth blade section act on the outboard end of the next inboard blade section in the positive axis directions of the jth section local blade coordinate system. These state variables are defined as follows:

- ux, uy, uz are the blade deflections in the local blade coordinate system x, y, and z directions, respectively,
- N, Vy, Vz are the axial, edgewise shear, and flapwise shear forces acting in the local blade coordinate system x, y, and z directions, respectively,
- \$\phi\_x\$, \$\phi\_y\$, \$\phi\_z\$ are the torsional, flapwise, and edgewise
  bending slopes about the local blade coordinate system x, y, and z directions, respectively, and
- T, My, Mz are the torsional, flapwise bending, and edgewise bending moments about the local blade coordinate system x, y, and z directions, respectively.

Since the blade state variables along the blade are defined relative to the local blade coordinate system, the blade state variables can also be defined relative to the rotating hub coordinate system by use of the coordinate transformation relationship specified in Equation (2).

The  $\Phi$  and  $\Theta$  values for a blade section having an elastic length but not shear center axis rigid offsets can be determined by consideration of the changes occuring in the  $h_{rx}$ ,  $h_{ry}$ , and  $h_{rz}$  sectional parameters in going from the blade section of interest to the next outboard section, since the section shear center axis is a straight line. In particular, for the jth blade section

$$\Phi_{j} = \arctan \left(\Delta h_{ry} / \Delta h_{rx}\right)$$
 (3)

$$\Theta_{j} = \arctan \left(-\Delta h_{rz} / \sqrt{\Delta h_{rx}^{2} + \Delta h_{ry}^{2}}\right) \tag{4}$$

where

$$\Delta h_{rx} = h_{rx}^{j-1} - h_{rx}^{j},$$

$$\Delta h_{ry} = h_{ry}^{j-1} - h_{ry}^{j},$$

$$\Delta h_{rz} = h_{rz}^{j-1} - h_{rz}^{j},$$

and the j-l superscript denotes the blade section just outboard of the jth section. If shear center axis rigid offsets are involved in the blade section, the  $h_{rx}$ ,  $h_{ry}$ , and  $h_{rz}$  parameters corresponding to the next outboard section in the previous expressions would be replaced by those corresponding to the location at which the rigid offsets occur on the shear center axis segment which passes through the local coordinate system origin. In the representation of the blade sectional characteristics (Figure 2), the localized change in the coordinate system orientation from that of the previous outboard section (local bends) can only be considered inboard of the section shear center axis rigid offset characteristics. Thus, the section shear center axis rigid offsets always are along the axis directions of the local coordinate system of the next outboard blade section. The use of the method described above for determining the blade section  $\Phi$  and  $\Theta$  values is particularly advantageous when blades having mean deformation due to steady loading effects in addition to built-in geometric angles are being considered.

The local blade aerodynamic coordinate system for a blade section having aerodynamic characteristic is oriented such that the sectional lift and drag forces act along its z and y axes, respectively. The origin and x-axis of the local blade aerodynamic coordinate system for a blade section coincide with those of the associated local blade coordinate system. The orientation of the local blade aerodynamic coordinate system is obtained by rotating the local coordinate system about its x-axis. The relationship between the local blade aerodynamic and local blade coordinate systems of a blade section and several aerodynamic-related parameters are depicted in Figure ll for the two directions of rotor rotation, as viewed from a position on the positive x-axes of the coordinate systems.

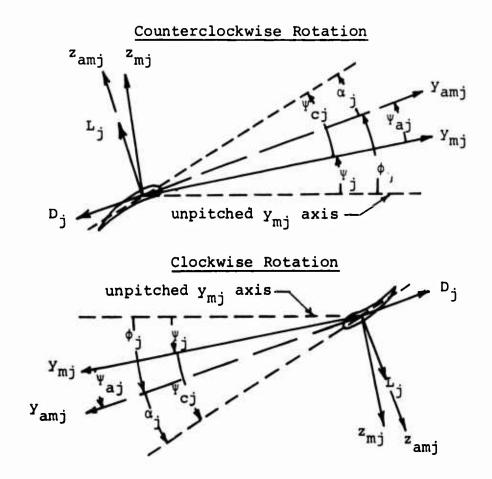


Figure 11. Relationship Between the Local Blade Aerodynamic and Local Blade Coordinate Systems for the jth Blade Section.

In Figure 11,  $\Psi_j$  is the previously discussed blade section prepitch which includes collective pitch,  $\Psi_{cj}$  is the blade cyclic pitch,  $\phi_j$  is the section inflow angle,  $\alpha_j$  is the section aerodynamic angle of attack,  $\Psi_{aj}$  is the angle of rotation between the local aerodynamic and local coordinate systems, and  $L_j$  and  $D_j$  are the section lift and drag forces, respectively. Since these parameters, except  $\Psi_j$ , are dependent on the blade azimuthal position in forward flight the relationship between these two blade section coordinate systems may vary azimuthally. This relationship is represented by the coordinate transformation

$$\begin{cases}
\overline{I}_{amj} \\
\overline{J}_{amj}
\end{cases} = \begin{bmatrix}
1 & 0 & 0 \\
0 & C\Psi_{a} & S\Psi_{a}
\end{bmatrix} \begin{cases}
\overline{I}_{mj} \\
\overline{J}_{mj}
\end{cases}$$

$$\overline{k}_{mj}$$
(5)

where  $S^{\Psi}_{a}$  represents  $\sin^{\Psi}_{aj}$ ,  $C^{\Psi}_{a}$  represents  $\cos^{\Psi}_{aj}$ , and the  $\bar{i}$ ,  $\bar{j}$ , and  $\bar{k}$  variables are unit vectors, with amj subscripts denoting the local aerodynamic coordinate system and mj subscripts denoting the local coordinate system of the jth section of the mth blade. As can be noted in Figure 11, the rotation angle  $\Psi_{aj}$  is defined by  $\Psi_{aj} = \phi_{j} - \Psi_{j}$ .

Regardless of whether a counterclockwise or clockwise rotating rotor is being considered, the lift force generated by the rotor is positive if it acts on the rotor hub in the positive fixed hub coordinate system z-axis direction. This definition is consistent with the direction of the positive section lift force resulting from a positive blade section angle of attack, as depicted in Figure 11. For some rotor systems (for example, the rotor system depicted in Figure 6 as Arrangement IV) a negative lift force as defined relative to the rotor's fixed hub coordinate system is desirable. For a symmetrical airfoil this can be achieved by defining the  $\Psi_j$ ,  $\Psi_{cj}$ , and  $\phi_j$  blade section parameters such that the  $\alpha_j$  (blade section aerodynamic angle of attack) parameters would be for the most part negative in value. In particular, the  $\Psi_j$  and  $\Psi_{cj}$  blade parameters would have values opposite in

sign to that required for positive rotor lift. In that the  $\phi_j$  parameter is dependent on the magnitude and orientation of the hub flight velocity and the induced velocity field, the value of  $\phi_j$  need not be negative, but the induced velocity should be negative in value (defined as positive acting on the rotor disk in the  $-z_{rm}$  axis direction).

The above comments for a symmetrical airfoil do not suffice for a cambered airfoil producing negative rotor lift. In addition, the airfoil coefficient data must be defined such that the cambered airfoil represented has a profile which is inverted compared to the cambered airfoil profile depicted in Figure 11. This is necessary since a cambered airfoil having its lower surface on the  $z_{mj}$ -axis side of the airfoil chordline would normally be used to generate rotor lift in the  $-z_{rm}$  direction. The lift, drag and moment coefficients as a function of angle of attack,  $\alpha$ , and Mach number, M, necessary to construct the airfoil coefficient data deck for this inverted cambered airfoil profile (inverted relative to the local aerodynamic coordinate system) can be obtained by use of the expressions:

$$C_{L}^{I}(\alpha, M) = -C_{L}^{N}(-\alpha, M)$$

$$C_{D}^{I}(\alpha, M) = C_{D}^{N}(-\alpha, M)$$

$$C_{M}^{I}(\alpha, M) = C_{M}^{N}(-\alpha, M)$$
(6)

In these expressions  $C_L$ ,  $C_D$ , and  $C_M$  correspond to the airfoil lift, drag, and moment coefficients, respectively, with the I superscripts denoting the coefficients for the inverted airfoil profile and the N superscripts denoting the coefficients as normally defined. As an example, the inverted cambered airfoil lift coefficient for an angle of attack of -6 degrees and a given Mach number would have the same magnitude as but be opposite in sign to the standard cambered airfoil lift coefficient for an angle of attack of 6 degrees and the same Mach number. The airfoil coefficient data for a symmetrical airfoil inherently satisfies the expressions of Equation (6).

# PITCH CONTROL STRUCTURE COORDINATE SYSTEMS

The pitch control structure, as previously defined, consists

of the structure connecting the control rod to the blade. The HASTA analysis can represent three different types of pitch control structure, the use of which is dependent on the type of rotor being considered. These are:

- an arbitrarily oriented rigid pitch arm which applies only torque about the blade shear center axis at the pitch arm-blade attachment point (articulated teetering, or gimballed rotor),
- an arbitrarily oriented flexible pitch arm which applies forces and moments in three directions to the blade (flexstrap rotor), and
- 3. a torque tube structure which applies forces and moments in three directions to the blade and consists of a flexible torque tube and spur, both of which are allowed the same arbitrary orientation, and an arbitrarily oriented rigid pitch arm (bearingless rotor);

all of which have been depicted in Figure 4. The coordinate systems associated with the different pitch control structures consist of those necessary to define the orientation of the pitch arm, torque tube, and spur components and the axes about which the stiffness characteristics of a component are taken to act.

The articulated rotor type of pitch control structure, consisting of a rigid pitch arm of length Lpa, has the origin of its associated coordinate system located at the pitch arm-blade attachment point. The x-axis of the pitch arm coordinate system coincides with the lengthwise axis of the pitch arm and is positive in the direction toward the pitch arm-control rod attachment point. The y and z axes of the pitch arm coordinate system are both perpendicular to the pitch arm coordinate system x-axis as well as perpendicular to each other. The azimuthal orientation of these two axes relative to the pitch arm coordinate system x-axis is arbitrary. However, the positive directions of the x and y axes must be chosen such that a right-handed Cartesian coordinate system is produced.

The orientation of the pitch arm coordinate system  $(x_p, y_p, z_p)$  is defined relative to the associated rotating hub coordinate system  $(x_{rm}, y_{rm}, z_{rm})$  by specification of the three angles,  $\alpha$ ,  $\beta$ , and  $\gamma$ . These angles, in the order listed, correspond to three consecutive rotations, which must be applied to the rotor

hub coordinate system (placed at the pitch arm-blade attachment point) to align it with the pitch arm coordinate system. The application of the  $\alpha$ ,  $\beta$ , and  $\gamma$  angles is conceptually identical to that of the  $\Phi$ ,  $\Theta$ , and  $\Psi$  angles used to define the orientation of a local blade coordinate system. The use of these angular rotations in defining the orientation of the pitch arm coordinate system relative to the rotating hub coordinate system is depicted in Figure 12 for both directions of rotor rotation.

The relationship between the pitch arm coordinate system  $(x_{pm}, y_{pm}, z_{pm})$  is represented by the coordinate transformation

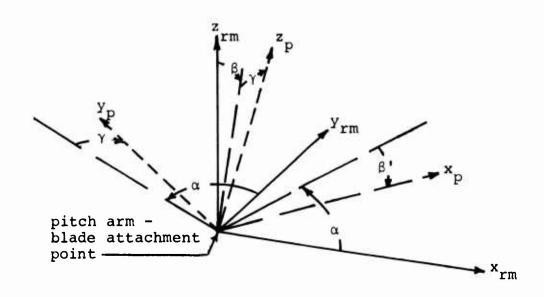
where a short form of denoting the sine and cosine functions has been used and the  $\bar{i}$ ,  $\bar{j}$ , and  $\bar{k}$  variables are unit vectors, with the subscripts denoting the coordinate system to which unit vectors correspond.

This rigid pitch arm pitch control structure is only allowed to apply torque to the blade about the local blade shear center axis (x<sub>mj</sub>-axis) at the pitch arm-blade attachment point. This torque can be defined in terms of the control rod force applied to the pitch arm and an effective moment arm. The value of this effective moment arm is, in fact, the only data required by HASTA to represent this pitch control structure used with articulated, gimballed, or teetering rotors, since the control rod applied force in this case is considered to act in a direction parallel to the rotating hub coordinate system z-axis. This effective moment arm as required by the HASTA program is defined by

$$a = -L_{p} (S\alpha C\Phi - C\alpha S\Phi) C\beta C\Theta,$$
 (8)

the terms on the right hand side having been previously defined. As can be noted from Equation (8) for a blade without presweep, precone, and prepitch at the pitch arm-blade attachment point, a is negative in value if the pitch arm is directed toward the blade leading edge  $(0^{\circ}<\alpha<180^{\circ})$  and positive if the pitch arm is directed aft  $(180^{\circ}<\alpha<360^{\circ})$ .

# Counterclockwise Rotation



## Clockwise Rotation

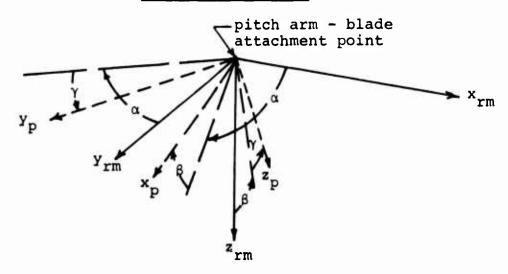


Figure 12. Description of Rotating Hub Coordinate System Rotations Required for Definition of the Pitch Arm Coordinate System Orientation.

The pitch arm of the flexstrap pitch control structure differs from that discussed above in that the pitch arm is allowed bending and axial flexibility and applies restraining forces and moments to the blade in three mutually orthogonal directions. The definition of the flexstrap pitch arm coordinate system orientation is identical to that presented above for the rigid pitch arm. Thus, the orientation angles and  $\gamma$ ) and the coordinate system relationships depicted in Figure 12 and represented by the coordinate transformation of Equation (7) are directly applicable to the flexstrap pitch Since the flexstrap pitch arm representation requires bending stiffness information about the pitch arm coordinate system y and z axes ( $EI_{yy}$  and  $EI_{zz}$ , respectively), the azimuthal orientation of these two axes relative to the pitch arm coordinate system x-axis should be based on the axes about which these stiffness parameters are known. The data required by HASTA to represent the flexstrap pitch arm, in addition to the bending stiffnesses, consists of the pitch arm length Lp, the axial stiffness EA, and the three orientation angles  $\alpha$ ,  $\beta$ , and  $\gamma$ . The flexstrap pitch arm representation requires also that the shear center axis at the pitch arm-blade attachment point be parallel to the x<sub>rm</sub>-axis (i.e., unswept, unconed, and unpitched). The positional parameters hry and hrz for the pitch arm-blade attachment point need not be zero in value and, in fact, would not normally be zero due to the presweep, precone, and prepitch distributions occurring inboard of the attachment point.

The torque tube pitch control structure coordinate systems consist of the torque tube, spur, and pitch arm coordinate systems. The torque tube of length L, has the origin of its associated coordinate system located on the blade shear center axis at the torque tube-blade attachment point. The x-axis of the torque tube coordinate system coincides with the lengthwise axis of the torque tube and is positive in the direction toward the torque tube-spur-pitch arm attachment point. y and z axes of the torque tube coordinate system are defined in the same manner as the y and z axes of the flexstrap pitch arm coordinate system. The definition of the torque tube coordinate system orientation relative to the rotating hub coordinate system is identical to the definition of the rigid pitch arm orientation. Thus, as was also noted for the flexstrap arm, the  $\alpha$ ,  $\beta$ , and  $\gamma$  orientation angles and the coordinate system relationships depicted in Figure 12 and represented by Equation (7) are directly applicable to the torque tube representation. For the torque tube coordinate system, the value

of  $\alpha$  in degrees should be close to 180 degrees since the x-axis of the torque tube should be primarily in the -x\_{rm} direction. The data required by the HASTA program to represent the torque tube portion of the torque tube pitch control structure consists of data similar to that required for the flexstrap pitch arm and the torsional stiffness of the torque tube. In addition, the blade structure must be modeled such that the blade shear center axis at the torque tube-blade attachment point is unswept, unconed, and unpitched regardless of the location of the attachment point. This condition is identical to that required for the flexstrap pitch arm.

The spur (extension shaft) of length L, has the origin of its associated coordinate system located at the torque tube-spurpitch arm attachment point. The orientation of the spur coordinate system is identical to the orientation of the torque tube coordinate system and as such is defined by the  $\alpha$ ,  $\beta$ , and  $\gamma$  orientation angles used in the representation of the torque tube. Thus, the numerical forms of the coordinate transformation matrix presented in Equation (7) for the torque tube and the spur are always identical. Since the spur is attached to the hub structure by a spherical bearing such that the torque and axial force cannot be applied to the spur and the orientation angles are provided via torque tube data, data required by HASTA for the representation of the spur consists of its length and bending stiffnesses. If the rotor hub is allowed rotational and translational degrees of freedom due to its support structure, an additional length parameter is required to define the tranverse motions of the spherical bearing relative to the rotating hub coordinate system z<sub>rm</sub>-axis. This length, L<sub>h</sub>, is the perpendicular distance from the rotor disk plane  $(x_{rm}^{}-y_{rm}^{}$  plane) to the spherical bearing (i.e., measured along a line parallel to the  $z_{\rm rm}$ -This length is positive in value if the spherical bearing is in the  $-z_{rm}$  direction from the rotor disk plane regardless of the direction of rotor rotation. For example, if the spherical bearing is on the same side of the rotor disk plane as the control system, the length L<sub>b</sub> is positive for the Class A rotors and negative for the Class B rotors depicted in Figure 6.

The torque tube pitch control structure pitch arm of length L has the origin of its associated coordinate system also located at the torque tube-spur-pitch arm attachment point. The

axes of this rigid pitch arm coordinate system are located relative to the pitch arm structure in the same manner as for the rigid pitch arm used with articulated rotor blades. The orientation of this rigid pitch arm coordinate system, however, is not defined relative to the rotating hub coordinate system but rather to the torque tube coordinate system. This orientation is specified by the three angles  $\alpha'$ ,  $\beta'$ , and  $\gamma'$  which are applied conceptually in the same manner as  $\alpha$ ,  $\beta$ , and  $\gamma$ . The use of these three angular rotations in defining the orientation of this rigid pitch arm coordinate system relative to the torque tube coordinate system (placed at the torque tube-spur-pitch arm attachment point) is depicted in Figure 13 for the two directions of rotor rotation. In this figure, the torque tube orientation angles  $\alpha$ ,  $\beta$ , and  $\gamma$  have been assumed to have values (in degrees) of 180, 0, and 0, respectively.

The relationship between this rigid pitch arm coordinate system  $(x_p, y_p, z_p)$  and the torque tube coordinate system  $(x_p, y_p, z_p)$  is represented by Equation (7) with the p and rm subscripts replaced by p' and p, respectively, and  $\alpha$ ,  $\beta$ , and  $\gamma$  replaced by  $\alpha'$ ,  $\beta'$ , and  $\gamma'$ , respectively. Since the pitch arm is rigid, only the correct orientation of the pitch arm coordinate system x-axis is required. This orientation can be achieved by use of only  $\alpha$  and  $\beta$  angular rotations. The data required by the HASTA program for the representation of the pitch arm component of the torque tube pitch control structure consists of the pitch arm length and orientation parameters.

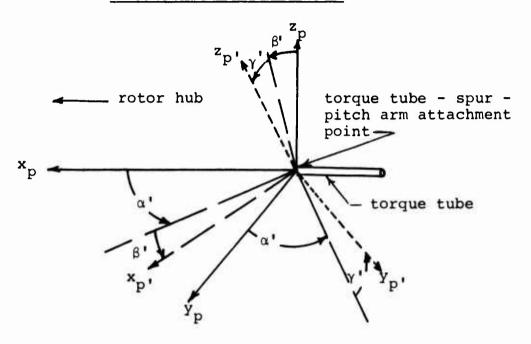
### CONTROL SYSTEM COORDINATE SYSTEMS

The fundamental coordinate systems required for the representation of the control system consist of a fixed coordinate system and a rotating coordinate system corresponding to each rotor blade. The origin of the fixed control system coordinate system is located on the rotor drive shaft axis (same as the  $\mathbf{z_f}$ -axis of the fixed hub coordinate system) where the

plane of the control system ring intersects it. The x and y axes of this coordinate system lie in the unperturbed plane of the control system ring which is also parallel to the rotor disk plane. The x-axis is defined to be along the line from the coordinate system origin to the location on the control ring at which the control rod of the first blade is attached when this blade is in the reference blade position (i.e., the position at which the spanwise axis of the unswept, unconed, and unpitched blade coincides with the  $x_f$ -axis). The orien-

tation and positive direction of the y-axis is defined as required to produce a right-handed Cartesian coordinate system.

# Counterclockwise Rotation



# Clockwise Rotation

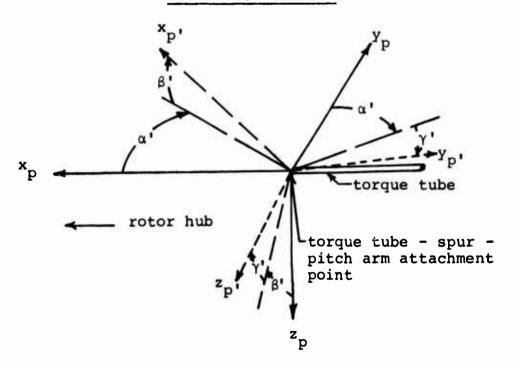


Figure 13. Description of Torque Tube Coordinate System Rotations Required for Definition of the Pitch Arm Coordinate System.

The orientation of the fixed control system coordinate system  $(x_{fc}, y_{fc}, z_{fc})$  relative to the fixed hub coordinate system  $(x_f, y_f, z_f)$  is depicted in Figure 14 for both directions of rotor rotation.

## Counterclockwise Rotation

### Clockwise Rotation

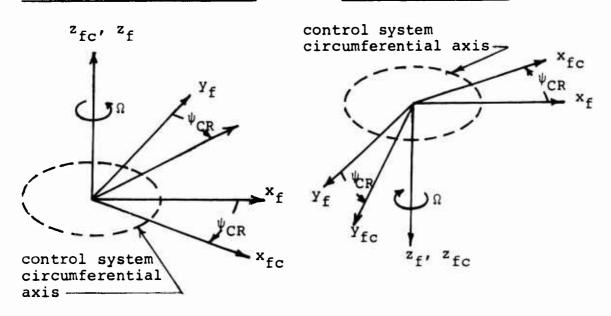


Figure 14. Description of the Relationship Between the Fixed Hub Coordinate System and the Fixed Control System Coordinate System.

The angle  $\psi_{CR}$  denotes the degree of azimuthal shift occurring between the two fixed coordinate systems that results from the control rods being attached to the control system ring at locations not in their associated blade-related rotating hub coordinate system x-z planes. The value of  $\psi_{CR}$  is not used by the HASTA program. Instead, the azimuthal location  $(\chi_j)$  of the cyclic spring-damper units depicted in Figure 5 are defined relative to the fixed control system coordinate system. In addition, the control system displacement results obtained from HASTA application must be interpreted relative to the fixed and rotating coordinate systems associated with the control system and not those associated with the rotor hub.

The rotating control system coordinate systems, one for each blade but associated with the azimuthal location of the related control rod-control system ring attachment point, have the same origin and z-axes as the fixed control system coordinate system. Their x- and y-related axes are in the same plane as the x- and y-axes of the fixed coordinate system but are rotating about the  $z_{\rm fc}$ -axis with a constant rotational speed of  $\Omega$  rad/sec. The relationship between the rotating control system coordinate system ( $x_{\rm mc}$ ,  $y_{\rm mc}$ ,  $z_{\rm mc}$ ) associated with the first blade and the fixed control system coordinate system is depicted in Figure 15. As can be noted in this figure, the angular relationship includes  $\phi_1$ . This is

# Counterclockwise Rotation

# Clockwise Rotation

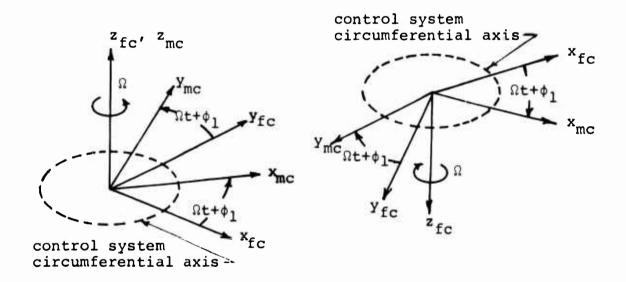


Figure 15. Description of the Relationship Between the Rotating Control System Coordinate System Associated with First Blade and the Fixed Control System Coordinate System.

necessary since  $\phi_1$ , if non-zero, shifts not only the azimuthal location of the first blade but also shifts its control rod-control system attachment point. Due to the azimuthal shift occurring between the fixed control system coordinate system and the fixed hub coordinate system, the orientation of a rotating control system coordinate system will lag by  $\psi_{CR}$  that of the corresponding rotating hub

coordinate system. The relationship between the rotating and fixed control system coordinate systems is defined by Equation (1) with the rm and f subscripts replaced by mc and fc, respectively. The above discussion is valid for both Class A and Class B control systems.

### CONTROL ROD ORIENTATION

The control rod representation does not require coordinate system definition per se. Only the orientation of the control rod lengthwise axis need be defined, since the control rods are only subjected to axial loading. There are two types of control rod representation, the use of which is dependent on the type of rotor being considered. The first type is that used for the articulated, gimballed, or teetering rotor. In this representation the control rod is assumed to act only in the rotating hub coordinate system z<sub>rm</sub>-axis direction (i.e., perpendicular to the rotor disk plane), although it actually may or not act only in that direction. The second type is that used for the flexstrap or bearingless rotor. This control rod representation allows for arbitrary orientation of the control rod relative to the rotating hub coordinate system (placed at the control rod-control system attachment point). The orientation of the control rod lengthwise axis is specified by the orientation angles  $\phi_{c}$  and  $\theta_{c}$ , which correspond to the consecutive angular rotations that must be applied to the rotating hub coordinate system to align its z-axis with the control rod axis. The application of the angles is identical in concept to that of the angles used for specification of the local blade coordinate system orientation. The relationship between the control rod axis and the rotating hub coordinate system is depicted in Figure 16 for the two directions of rotor rotation. If a Class B rotor system (i.e., control system located in the +z<sub>rm</sub> direction relative to the rotor disk plane) is being considered, the value of  $\theta_c$  will be greater than 90 degrees.

## Counterclockwise Rotation

### Clockwise Rotation

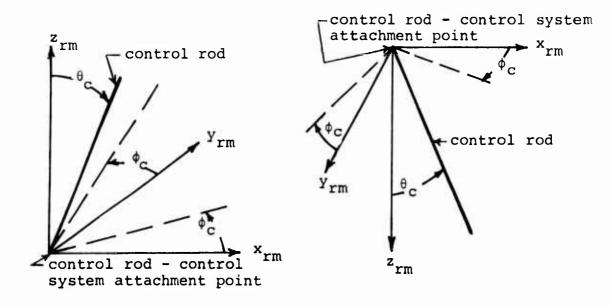


Figure 16. Relationship Between Control Rod Axis and Rotating Hub Coordinate System.

The data required by the HASTA program for the first type of control rod representation, that associated with articulated, gimballed, and teetering rotor systems, consists of the effective control rod stiffness and damping characteristics in the  $z_{\rm rm}^{-}$ axis direction. The primary data required for the control rod representation associated with a flexstrap or bearingless rotor system consists of the orientation angles, and  $\theta_{c}$ , and the control rod axial stiffness and damping characteristics. In the latter case, an additional length parameter, similar in concept to the length L, is required if the rotor hub is allowed rotational and translational degrees of freedom due to its support structure. This length parameter is necessary to define the transverse motions of the control rod-control system attachment point relative to the rotating hub coordinate system  $z_{\rm rm}$ -This length,  $L_{\rm CC}$ , is defined as the perpendicular distance from the rotor disk plane  $(x_{rm}-y_{rm})$  plane) to the control rodcontrol system attachment point. This length is positive in value for Class A rotors and negative for Class B rotors.

### SUPPORT STRUCTURE COORDINATE SYSTEMS

The coordinate systems associated with the rotor elastic support structure consist of a fixed coordinate system and local section coordinate systems which are conceptually similar to the rotating hub and local blade coordinate systems, respectively. primary difference is that the support structure-related coordinate systems are not rotating. The fixed (reference) support structure coordinate system has its origin located on the shear center axis at the tip end of the support structure (the end of the support structure furthest from its attachment to the rotor hub). In that the orientation of the fixed coordinate system axes is in general arbitrary except when gravitational effects on the support structure are included, two different possible fixed coordinate systems are discussed below. These coordinate systems are defined on the basis of the elastic support structure being a helicopter fuselage-tailboom-fin structure but are also valid for any other elastic support structure.

The inclusion of the effects of gravity requires the fixed coordinate system y-axis to be parallel to but opposite in direction to the gravity force (weight) vector acting on the fuselage structure. Thus, the fixed coordinate system y-axis is positive in the general direction toward the top of the helicopter fuselage. The x- and z-axes of this fixed coordinate system must lie in a plane perpendicular to the y-axis at the fixed coordinate system origin. The azimuthal orientation of the x- and z-axes relative to the y-axis is arbitrary providing that the positive directions of these axes are such that a right-handed Cartesian coordinate system is produced. However, for convenience in generating input data, the positive direction of the fixed coordinate system x- and y-axes should be toward the tailboom (aft) and to the port side of the helicopter, respectively.

When gravity effects are not to be included, the orientation and positive direction of the fixed support structure coordinate system axes are arbitrary providing that a right-handed Cartesian coordinate system is produced. However, a fixed support structure coordinate system can be defined that is convenient to the determination of support structure input data. In this fixed coordinate system, the x-axis is defined to be parallel to the forward flight velocity of the helicopter in level forward flight and to be positive directed aft. The y-axis is defined to be perpendicular to the x-axis, to

lie in the vertical plane of the helicopter fuselage, and to be positive toward the top of the helicopter. The z-axis is mutually orthogonal to the x- and y-related axes such as to produce a right-handed coordinate system. The two fixed support structure coordinate systems described above are depicted in Figure 17 as they relate to a fuselage-tailboom-fin support structure. In regard to the fixed coordinate system depicted for the case of inclusion of gravitational effects, the gravity vector and therefore the y-axis have been assumed to be in the vertical plane of the fuselage. Examples of local support structure coordinate systems are also shown in Figure 17.

The local support structure coordinate systems are obtained by application of the orientation angles  $\Phi$ ,  $\Theta$ , and  $\Psi$  in the same manner as is used in defining the orientation of the rotating local blade coordinate systems. Thus, the relationship between the local support structure coordinate systems ( $\mathbf{x_s}$ ,  $\mathbf{y_s}$ ,  $\mathbf{z_s}$ ) and the fixed structure coordinate system ( $\mathbf{x_{fs}}$ ,  $\mathbf{y_{fs}}$ ,  $\mathbf{z_{fs}}$ ) is represented by Equation (2) with the mj and rm subscripts replaced by  $\mathbf{s}$  and  $\mathbf{fs}$  subscripts, respectively. It should be noted that the local coordinate system y-axis for a support structure section is the axis taken as the chordline for aerodynamic purposes.

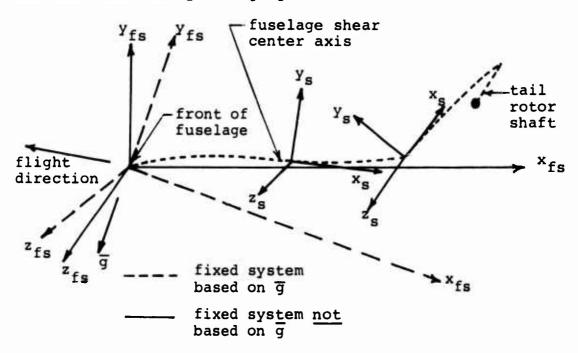


Figure 17. Fixed Fuselage Structure Coordinate System and Examples of Local Fuselage Structure Coordinate Systems.

### SHAFT-ROTOR HUB INTERFACE RELATIONSHIPS

The matching of boundary conditions at the interface of the rotor drive shaft and the rotor hub requires a defined relationship between the local support structure coordinate system at the end of the rotor drive shaft and the fixed hub coordinate system. The orientation of the local support structure coordinate system at the end of the rotor drive shaft is accomplished through the use of the  $\Phi$ ,  $\Theta$ , and  $\Psi$  angles. In that the blade state variables involved in the boundary condition equations must be defined relative to the rotating hub coordinate system, the most inboard blade section should end at the hub centerline and have no built-in presweep, precone, or prepitch; i.e.,  $\Phi$ ,  $\Theta$ , and  $\Psi$  should be zero in value.

The relationship between the two coordinate systems used for the matching of boundary conditions is that at the rotor drive shaft-rotor hub interface, in terms of unit vectors

$$\overline{i}_{s} = \overline{k}_{f}$$

$$\overline{j}_{s} = \overline{j}_{f}$$

$$\overline{k}_{s} = -\overline{I}_{f}$$
(9)

Thus, the required relationship between the support structure coordinate system and the fixed hub coordinate system at this interface is as depicted in Figure 18 for the two directions of rotor rotation. Note: This coordinate system relationship which is dependent upon the direction of rotor rotation, must be satisfied whether the rotor drive shaft is modeled on the positive or negative  $\mathbf{z_f}$ -axis side of the rotor disk plane.

If this required relationship is not satisfied by the modeling of the support structure, the computer program will yield erroneous results except for the case of reactionless blade modes. The necessary orientation of the hub end of the rotor drive shaft can be easily specified by taking the last section of the support structure to consist of only the localized bending lumped-parameter characteristics  $\Phi$ ,  $\Theta$ , and  $\Psi$ , which must be properly defined.

# Counterclockwise Rotation

# Clockwise Rotation

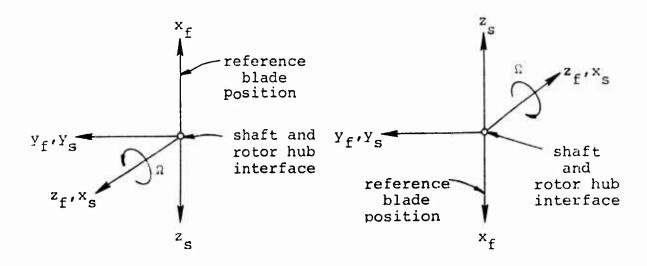


Figure 18. Relationship of the Local Support Structure Coordinate System and Fixed Hub Coordinate System Required at Shaft-Rotor Hub Interface.

### GENERAL DISCUSSION OF EQUATIONS

Most of the mathematical representation of the various coupled rotor-helicopter systems that can be analyzed was developed rigorously in Reference 1. Additional mathematical analysis developed to extend the capabilities of the HASTA program was discussed in Reference 2. Thus, the mathematical analysis involved will not be discussed in detail herein. The intent of this section of the report is to provide a background concerning the primary computational procedures utilized by the HASTA program. In particular, the discussion herein is concerned with the numerical application of transfer matrix procedures, the numerical construction of the final governing matrix, and the eigenvalue and eigenvector solution method. This information should provide the user with a sufficient knowledge of the overall concept of the computer program.

It is to be noted that the representational equations (i.e., control system equations, rotor support structure equations, and blade equations) and thereby the final governing matrix equation are in a Laplace transformed form involving the Laplace transform variable s and frequency-shifted Laplace transform variables such as  $s-ik\Omega$ , where k has a non-zero integer value. The application of Laplace transformation techniques provides an effective means of converting timedifferential equations having first and second order \_imederivative terms, as well as periodically varying coefficients, to an algebraic form which can be efficiently manipulated. addition, a characteristic of Laplace transformed equations allows the development of the additional equations necessary to define the harmonically shifted variables required for the consideration of interharmonic coupling due to the control system and/or rotor hub motion and to periodically varying aerodynamic coefficients. Because of the nature of the rotor/ helicopter problem, the resulting algebraic equations involve complex variable notation such that the Laplace transform variables must be allowed to be complex variables.

### TRANSFER MATRIX OPERATIONS

The HASTA program operation required for the transfer matrix procedure representation of a blade will be initially presented, followed by the operational modifications required for the rotor support structure representation. By considering the blade to be divided into sections representing the lumped-parameter characteristics of the blade, the k-frequency-shifted state

variable column vector at the inboard end of the ith section of the mth blade can be shown to be defined in general by the expression

$$\left\{\overline{s}_{k}\right\}_{m}^{i} = \sum_{n=-Nf}^{Nf} \left[\overline{B}_{k,n}\right]_{m}^{i} \left\{\overline{s}_{n}\right\}_{m}^{*} - \left\{\overline{b}_{k,n}\right\}_{m}^{i} \left(\overline{\Delta I}_{n}\right)_{m} - \left\{\overline{c}_{k,n}\right\}_{m}^{i} \left(\overline{\Delta 2}_{n}\right)_{m} - \left\{\overline{d}_{k,n}\right\}_{m}^{i} \left(\overline{\Delta 3}_{n}\right)_{m} - \left\{\overline{e}_{k,n}\right\}_{m}^{i} \left(\overline{\Delta 4}_{n}\right)_{m} - \left\{\overline{f}_{k,n}\right\}_{m}^{i} \left(\overline{\Delta 5}_{n}\right)_{m} - \left\{\overline{g}_{k,n}\right\}_{m}^{i} \left(\overline{\Delta 6}_{n}\right)_{m} \right] . \tag{10}$$

In this expression, the state variable column vector is defined by the form

$$\left\{ \overline{S} \right\} = \left\{ \overline{ux} \ \overline{N} \ \overline{\phi x} \ \overline{T} \ \overline{uy} \ \overline{\phi z} \ \overline{Mz} \ -\overline{Vy} \ -\overline{uz} \ \overline{\phi y} \ \overline{My} \ \overline{Vz} \right\}$$

where the state variables were defined previously in the discussion following Figure 10 and the n-frequency-shifted blade tip unknowns column vector is defined by

$$\left\{\overline{S}_{n}\right\}_{m}^{\star} = \left\{\overline{ux} \ \overline{\phi x} \ \overline{uy} \ \overline{\phi z} \ -\overline{uz} \ \overline{\phi y}\right\}_{n,m}^{\star}$$

The  $(\overline{\Delta 1}_n)_m$ ,  $(\overline{\Delta 2}_n)_m$ ,  $(\overline{\Delta 3}_n)_m$ ,  $(\overline{\Delta 4}_n)_m$ ,  $(\overline{\Delta 5}_n)_m$ , and  $(\overline{\Delta 6}_n)_m$  quantities are the n-frequency-shifted blade discontinuity unknowns. The specific definition of these unknowns and the inclusion of their contribution to Equation (10) is dependent upon the type of rotor system being considered. The

associated blade matrices  $\begin{bmatrix} \bar{B}_{k,n} \end{bmatrix}^i_m$  denote the contribution of the n-frequency-shifted mth blade tip unknowns to the k-frequency-shifted state variables at the ith section of the mth blade. These matrices are 12 x 6 arrays due to the implementation of the blade tip boundary conditions (i.e., blade tip shears and moments are zero in value). The blade discontinuity column vectors

$$\left\{\overline{b}_{k,n}\right\}_{m'}^{i} \left\{\overline{c}_{k,n}\right\}_{m'}^{i} \left\{\overline{d}_{k,n}\right\}_{m'}^{i} \left\{\overline{e}_{k,n}\right\}_{m'}^{i} \left\{\overline{f}_{k,n}\right\}_{m'}^{i} \text{ and } \left\{\overline{g}_{k,n}\right\}_{m}^{i}$$

denote the contribution of the n-frequency-shifted mth blade discontinuity unknowns to the k-frequency state variables at the ith section of the mth blade. The quantity Nf represents the number of harmonics above and below the main eigenvalue of interest s which are allowed to couple with the main eigenvalue-related behavior. Thus, if Nf is 1, the 1/rev and -1/rev shifted frequencies will be allowed to couple with the 0 shifted frequencies.

The computer program during a normal iteration does not calculate the state variables at the inboard end of the ith blade section. Instead, the computer program determines the associated blade transfer matrices and the necessary blade discontinuity vectors at the inboard end of each section. This is accomplished by consecutively multiplying, in matrix form, the associated blade transfer matrices and the necessary blade discontinuity vectors for the inboard end of the previous section by the individual transfer matrices for the section lumped-parameters, as these parameters are crossed in going inboard along the section. The associated blade transfer matrices and blade discontinuity vectors are not stored for each section but are updated by successive transfer matrix multiplication such that their final numerical values for an iteration correspond to those defining the blade state variables at the rotor hub centerline as required for construction of the final matrix. The construction of the final matrix also requires information concerning the numerical values occurring in specific rows of these matrices and vectors at the blade discontinuity locations. formation is saved in storage arrays as these discontinuities are crossed. After eigenvalue convergence is obtained the blade transfer matrix procedure is used to obtain the values of the k-frequency-shifted state variables at the inboard end of each blade section. These state variables are determined relative to both their local coordinate systems and the disk plane (rotating hub coordinate system).

The general manner in which the associated blade transfer matrices and discontinuity vectors are obtained will be briefly discussed. At the start of the transfer matrix procedure the off-diagonal associated blade transfer matrices  $(k\neq n)$  are initialized to 12 x 6 arrays consisting of zeroes.

The diagonal associated blade transfer matrices (k=n) are initialized to zeroes except for a value of unity in each of the six columns such that on multiplying the blade tip unknown column vector by the 12 x 6 array the same vector results. As each lumped-parameter characteristic is crossed, the associated blade transfer matrices inboard of the lumped-parameter characteristic are obtained in terms of those outboard by carrying out the numerical operation specified by

$$\left[\overline{B}_{k,n}\right]_{m}^{j} = \left[\overline{G}_{k}\right]_{m}^{j} \left[\overline{B}_{k,n}\right]_{m}^{j-1} \tag{11}$$

if a non-aerodynamic lumped-parameter characteristic is being considered and

$$\left[\overline{B}_{k,n}\right]_{m}^{j} = \sum_{\ell=-m}^{Nf} \left[\overline{G}_{k,\ell}\right]_{m}^{j} \left[\overline{B}_{\ell,n}\right]_{m}^{j-1}$$
(12)

if an aerodynamic lumped-parameter characteristic is being considered. In these expressions j is used to denote the

lumped-parameter characteristic index and  $\left[\overline{G}_k\right]_m^j$  may represent a k-frequency-shifted mass or spring transfer matrix or an unshifted (not involving s) elastic, bend, restraint, or rigid transfer matrix. These transfer matrices specify the effect of a particular lumped-parameter characteristic on the k-frequency-shifted state variables as the parameter is crossed.

The required blade discontinuity vectors, diagonal (k=n) and off-diagonal  $(k\neq n)$ , initially consist of all zeroes. When a discontinuity is encountered the corresponding diagonal blade discontinuity vectors (k=n) are defined as necessary for the type of discontinuity involved. After a discontinuity has been crossed the corresponding blade discontinuity vectors are updated in the identical manner as exemplified by Equations (11) and (12) for the associated blade transfer matrices.

The rotor support structure is not exposed to any representational discontinuities or self-induced interharmonic coupling. Thus the k-frequency-shifted support structure state variables just beyond the ith section can be defined by the expression

$$\left\{\overline{S}_{k}\right\}_{s}^{i} = \left[\overline{S}_{k}\right]_{s}^{i} \left\{\overline{S}_{k}\right\}_{s}^{\star}, \tag{13}$$

where the support structure state variables and the k-shifted support structure state variable vector are defined in the same manner as that for the blades except that they are related to the rotor support structure. In this expression

 $\left[\overline{S}_k\right]_s^i$  is a 12 x 6 array representing the k-frequency-shifted associated support structure transfer matrix for the ith support structure section. The k-frequency-shifted support structure unknowns vector may consist of either the rotor support structure tip slope and deflection unknowns similar to that for the blades and corresponding free and conditions, or rotor support structure tip moments and shears corresponding to cantilevered end conditions such that

$$\left\{\overline{S}_{k}\right\}_{s}^{\star} = \left\{\overline{N}_{s} \ \overline{T}_{s} \ \overline{MZ}_{s} - \overline{VY}_{s} \ \overline{MY}_{s} \ \overline{VZ}_{s}\right\}_{k}^{\star}.$$

The support structure transfer matrix procedure is carried out by the computer program in a manner similar to that used in the blade transfer matrix procedure. The starting k-frequency-shifted associated support structure transfer matrices are all initialized to consist of zeroes except for a value of unity in each of the six columns such that on multiplying the support structure unknowns vector by the initial 12 x 6 matrices the same vector results. It is to be noted that there are no off-diagonal associate transfer matrices for this structure and the initial form of the associate transfer matrices is dependent upon the form of the support structure unknowns vector. As each lumpedparameter characteristic is crossed, the associated support structure transfer matrices just beyond the lumped-parameter characteristic are obtained in terms of those previous by use of the form specified in Equation (11) with

$$\left[\overline{B}_{k,n}\right]_{m}^{i}$$
 replaced by  $\left[\overline{S}_{k}\right]_{s}^{i}$ .

After eigenvalue convergence is obtained, the k-frequencyshifted support structure state variables are then determined at each section relative to the local and fixed coordinate systems of the rotor support structure by use of the support structure transfer matrix procedure.

### FINAL GOVERNING MATRIX

The system representational equations (Equations (20), (21), (29), (30), (31), (32), (33), and (35) of Reference 1 and the additional blade discontinuity-related equations discussed in Reference 2), as required for the coupled rotor/helicopter system of interest, can be used in conjunction with Equations (10) and (13) to define the k-frequency-shifted governing equations. These k-frequency-shifted governing equations can be expressed in the simple matrix form

$$\sum_{n=Nf}^{Nf} \left[ \overline{T}_{k,n} \right] \left\{ \overline{q}_{n} \right\}^{*} = 0$$
 (14)

where  $\left[ T_{k,n} \right]$  specifies the contribution of n-frequency-shifted unknowns contained in  $\left\{ \overline{q}_{n} \right\}^{*}$  to the k-frequency-shifted governing equations.

As an example of the construction of  $[\overline{T}_k,n]$ , the general form of this matrix for a coupled three-bladed rotor/helicopter system is given by the expression

	$\left[ \overline{sw}_{k,n} \right]$	SF <sub>k,n</sub>	$\left[\overline{SB}_{k,n}\right]_{1}$	$\left[\overline{SB}_{k,n}\right]_{2}$	$\begin{bmatrix} \overline{SB}_{k,n} \end{bmatrix}$ 3	
$\left[\overline{T}_{k,n}\right] =$	0	$\left[\overline{FU}_{\underline{k}}\right]\delta_{n}^{k}$	FB <sub>k,n</sub> 1	$\left[\overline{FB}_{k,n}\right]_{2}$	$\left[\overline{FB}_{k,n}\right]_3$	
	$\left[\overline{\mathtt{BS}}_{k}\right]_{1} \delta_{n}^{k}$	BF <sub>k,n</sub> ]1	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{1}^{1}$	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{1}^{2}$	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{1}^{3}$	(15)
	$\begin{bmatrix} \overline{BS}_k \end{bmatrix}_2 \delta_n^k$	BF <sub>k,n</sub> 2	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{2}^{1}$	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{2}^{2}$	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{2}^{3}$	
	$\left[\overline{BS}_{k}\right]_{3} \delta_{n}^{k}$	$\left[\overline{BF}_{k,n}\right]_3$	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{3}^{1}$	$\left[\overline{BB}_{k,n}\right]_{3}^{2}$	$\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{3}^{3}$	

where integers have been used for blade subscripts and super-The top row of submatrices are obtained from the control system governing equations. The second row of submatrices are obtained from the moment and shear boundary condition equations at shaft-rotor hub interface. The third, fourth, and fifth rows of submatrices are obtained from the slope and displacement boundary condition equations at the shaft-rotor hub interface and from the blade discontinuity equations for the first, second, and third blades, respec-These submatrices have been defined in detail in tively. Reference 1 for a fully coupled flexstrap, articulated, gimballed, or teetering rotor/helicopter system. For a fully coupled bearingless rotor/helicopter system the submatrix definitions are different than those of Reference 1 due to the different discontinuity unknowns and discontinuity equations which are involved. It is to be noted that the content and dimensions of some of the submatrices for a particular system are dependent upon the degree of inclusion of control system spatial harmonic effects, the number of blade discontinuities, and the type of rotor system.

The n-frequency-shifted unknowns vector is defined by

$$\left\{\overline{q}_{n}\right\}^{*} = \begin{cases} \left\{\overline{r}_{n}\right\}_{s}^{*} \\ \left\{\overline{s}_{n}\right\}_{s}^{*} \\ \left\{\overline{p}_{n}\right\}_{1}^{*} \\ \left\{\overline{p}_{n}\right\}_{2} \\ \left\{\overline{p}_{n}\right\}_{3} \end{cases}$$

$$(16)$$

where the n-frequency-shifted control system unknowns are given by the general form

$$\left\{ \vec{r}_{n} \right\} = \left\{ \begin{aligned} & \vec{w}_{-\text{Nmax}}(s-\text{i}n\Omega) \\ & \vdots \\ & \vec{w}_{-1}(s-\text{i}n\Omega) \\ & \vec{w}_{0}(s-\text{i}n\Omega) \\ & \vec{w}_{1}(s-\text{i}n\Omega) \\ & \vdots \\ & \vec{w}_{\text{Nmax}}(s-\text{i}n\Omega) \end{aligned} \right\}$$

in which Nmax is the limit on the number of spatial harmonics retained in the control system representation, the n-frequency-shifted support structure unknowns are given by

 $\left\{\overline{S}_{n}\right\}_{s}^{\pi}$ , and the n-frequency-shifted mth blade unknowns are given by the general form

$$\left\{\overline{\mathbf{F}}_{\mathbf{n}}\right\}_{\mathbf{m}}^{\star} = \left\{\left\{\overline{\mathbf{S}}_{\mathbf{n}}\right\}_{\mathbf{m}}^{\star} \left(\overline{\Delta \mathbf{I}}_{\mathbf{n}}\right)_{\mathbf{m}} \left(\overline{\Delta \mathbf{I}}_{\mathbf{n}}\right)$$

Blade discontinuity unknowns that are not to be included for a particular system of interest are omitted from the blade unknowns vectors. In addition, the individual columns of the last three columns of submatrices in Equation (15), which in the general form of these submatrices would multiply the discontinuity unknowns not included, would also be omitted.

The definitions provided by Equations (15) and (16) assume a coupled rotor/helicopter system having a control system and a rotor support structure in addition to the rotor blades. With alterations in the coupled rotor/helicopter system complexity the construction of this matrix and the unknowns column vector is modified. As an example, if a particular coupled tail rotor/helicopter system does not have a control system, the first row of submatrices and the first column of submatrices are omitted from the matrix and the control system unknowns are omitted from the unknowns vector. Similarly, if a particular system does not have a rotor support structure the second row of submatrices and the second column of submatrices are omitted from the matrix and the support structure unknowns are omitted from the unknowns vector. In addition, the removal of a blade requires the omission of the corresponding blade unknowns (including discontinuity unknowns) from the unknowns vector and the omission of the row and column of submatrices containing the associated diagonal blade

array. Thus, analytically the  $\left[\overline{T}_{k,n}\right]$  matrices can be as complex as shown in Equation (15), more complex due to additional blades, or as simple as  $\left[\overline{BB}_{k,n}\right]_{1}^{1}$ .

The use of the blade phasing assumption for which all blades of the rotor are identical and equally spaced azimuthally

allows the size of the  $\left[\overline{T}_{k,n}\right]$  matrices to be significantly

reduced by the removal of the submatrices associated with blades other than the first blade. With the use of this

assumption the submatrices  $[\overline{SB}_{k,n}]_1$  and  $[\overline{FB}_{k,n}]_1$  have an

altered form to include the contributions of the additional blades. In the case of a gimballed or teetering rotor, the

submatrices  $\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}$  also are modified. This option allows

the user to specify the type of blade modes to be obtained

(i.e., umbrella, reactionless, forward cyclic, or backward cyclic modes).

The k-frequency-shifted matrix equations represented by Equation (14) involve n-frequency-shifted unknowns which can be defined by considering values of k from -Nf to +Nf such that the final governing matrix equation required for solution may be obtained in the form

$$\begin{bmatrix}
\overline{T}_{-1}, -1 \\
\overline{T}_{0}, -1
\end{bmatrix}
\begin{bmatrix}
\overline{T}_{-1}, 0 \\
\overline{T}_{0}, 1
\end{bmatrix}
\begin{bmatrix}
\overline{T}_{0}, 1
\end{bmatrix}
\begin{bmatrix}
\overline{T}_{0}, 1
\end{bmatrix}
\begin{bmatrix}
\overline{T}_{0}, 1
\end{bmatrix}
\begin{bmatrix}
\overline{T}_{1}, 1
\end{bmatrix}$$

$$= 0$$
(17)

for Nf=1. In general, the number of  $[\overline{T}_k, n]$  matrices re-

quired to construct the final governing matrix is defined by (2Nf+1)<sup>2</sup>. Thus, the size of the final governing matrix for a particular coupled tail rotor/helicopter system is dependent on the value of Nf and the size of the indivi-

dual  $\left[\overline{T}_{k,n}\right]$  matrices. The use of the blade phasing assump-

tion can be seen to significantly decrease the size of the final governing matrix which must be solved.

The operational procedure that the computer program uses to obtain the final g verning matrix in numerical form is to determine the numerical form of the individual

 $\left[\overline{T}_{k,n}\right]$  matrices involved in the final governing matrix and

to store this information in a consistent order in a temporary storage unit (disk or tape). The final governing matrix in numerical form as required for the determination of the determinant and assumed mode shape correction values is ob-

tained by reading the stored values of the  $\left[\overline{T}_{k,n}\right]$  matrix in the proper sequential order. It is to be noted that when

the numerical content of each  $\left[\overline{T}_{k,n}\right]$  matrix is fully determined, the data is dumped off to tape so that the matrix storage array can be used for the next matrix.

The numerical construction of a  $\begin{bmatrix} \overline{T}_{k,n} \end{bmatrix}$  matrix is achieved by determination of the numerical content of each submatrix which is required to construct the matrix and proper placement of this information in the matrix storage array. In the majority of submatrices, the required numerical information is obtained by use of the final associated transfer matrices for the blade and rotor elastic support structure and the stored information required at blade discontinuity Although the analytical representation uses locations. matrix operators in addition to numerical operators to specify the particular information required for a submatrix, the computer program achieves the same representation by use of numerical operators, whose values can be obtained from input parameters, and proper indexing procedures. Some of the control system-related submatrices are directly constructed with only manipulation of the control system input parameters and proper indexing control. Due to the allowance of several different program representational options such as the type of rotor system, the type of blades, and the use of the blade phasing assumption, the construction of submatrices may have several different forms. Thus, the computer program coding for the construction of a submatrix may consist of several parts, of which only one part may be used for a particular coupled rotor/helicopter system.

### EIGENVALUE AND EIGENVECTOR SOLUTION METHOD

The solution method used to obtain the eigenvalues and eigenvectors is based on a modified transfer-matrix method. This method avoids the numerical accuracy problems due to the taking of small differences of large numbers that generally occurs in transfer matrix techniques, particularly when the frequency determinant is computed for higher natural frequencies. In the solution procedure the eigenvector corresponding to the system unknowns and the eigenvalue are iterated simultaneously until the desired degree of eigenvalue convergence is achieved. This is accomplished by considering the eigenvector to consist of the sum of a trial eigenvector and a correction eigenvector such that as the trial eigenvalues are used in the iteration procedure to obtain a solution eigenvalue the trial eigenvector is being continuously updated.

The determination of the correction eigenvector for a given trial eigenvalue requires a modification of the final matrix equation for the trial eigenvalue. The final governing matrix equation, as represented by Equation (17), can be expressed in the form  $[\overline{A}]$   $\{\overline{X}\}$  = 0. The  $\{\overline{X}\}$  column vector can be defined in general as  $\{\overline{X}\} = \{\overline{\lambda}\} + \{\overline{\varepsilon}\}$  where  $\{\overline{\lambda}\}$  is the trial eigenvector for an iteration and  $\{\overline{\epsilon}\}$  is the correction eigenvector. By substitution of the  $[\overline{X}]$  definition into the final governing matrix, the expression  $[\overline{A}]$   $\{\overline{\epsilon}\}$  =  $\{\overline{F}\}$  where  $\{\overline{F}\}=[\overline{A}]$   $\{\lambda\}$  can be obtained. Premultiplication of this equation by the inverse of  $[\overline{A}]$  results in  $\{\overline{X}\} = 0$ . problem of indeterminate equations is avoided by normalizing a particular element  $\overline{X}_i$  of  $\{\overline{X}\}$  to unity such that the corresponding  $\{\overline{\lambda}\}$  and  $\{\overline{\epsilon}\}$  elements,  $\overline{\lambda}_{j}$  and  $\overline{\epsilon}_{j}$ , can be defined to Since  $\overline{\epsilon}_{i}$  will always be always be unity and zero in value. zero by definition, the jth column of  $[\overline{A}]$  can be removed from  $[\overline{A}]$  and the  $\overline{\epsilon}_{+}$  element removed from  $\{\overline{\epsilon}\}$  such that the modified matrix equation  $[\overline{A}']$   $\{\overline{\epsilon}'\} = -\{\overline{F}\}\$  results where  $[\overline{A}']$  is a nx(n-1) matrix and  $\{\overline{\epsilon}'\}$  consists of n-1 elements. Thus, in this form the modified matrix equation represents one more equation than there are unknowns. Although, in general, any kth row of the modified matrix equation can be removed, best results for the coupled rotor/helicopter problem are obtained when  $\lambda_{\mathbf{k}}$  is a variable closely associated with the  $\lambda_{i}$  defined as unity. For example, if the blade flapwise tip deflection is normalized to unity, the  $\lambda_k$ should correspond to the blade flapwise tip slope. On removal of the kth row from the modified equation, the equation  $[\overline{A}'']$   $\{\overline{\epsilon}'\} = -\{\overline{F}'\}$  is obtained, where  $[\overline{A}'']$  results due to removal of the kth row of elements from  $[\overline{A}']$  and  $\{\overline{F}'\}$  results due to removal of the kth element from  $\{\overline{F}\}$ . By multiplying both sides of this equation by the inverse of  $[\overline{A}^*]$ , the n-1 element correction vector is defined by

$$\{\bar{\mathbf{\epsilon}}'\} = [\bar{\mathbf{A}}'']^{-1} \{\bar{\mathbf{F}}'\}. \tag{18}$$

The computer program for each trial eigenvalue, as the individual  $\left[\overline{T}_{k,n}\right]$  matrices are constructed, also carries out the matrix multiplications necessary to determine  $\{\overline{F}\}$ . The determinant and correction eigenvector are determined on the basis of the  $\left[\overline{T}_{k,n}\right]$  matrices and  $\{\overline{F}\}$  by performing several steps.

First, the final matrix is constructed numerically by reading information in proper sequence from the auxiliary storage  $\overline{u}$ nit. The  $[\overline{A}]$  matrix is then reordered by switching the jth column and last column of  $[\overline{A}]$ , which technically switches the jth variable and last variable of  $\{\bar{\epsilon}\}$ . Then the kth row and last row of the resulting matrix are switched and the kth element and last element of  $\{\overline{\mathbf{F}}\}$  are switched. procedure is then applied which obtains the determinant of the modified nxn matrix and obtains the numerical  $\{\bar{\epsilon}'\}$ correction factor using the modified nxn matrix with the last row and column omitted and the last element of the modified  $\{\bar{F}\}\$  vector omitted. In this procedure the  $\{\bar{\epsilon}'\}\$  correction vector is returned to the inputted  $\{\bar{\mathbf{F}}\}\$ . The  $\{\bar{\epsilon}\}\$ correction vector is obtained by defining the last element of what was  $\{\overline{F}\}$  to have the value of  $\epsilon_{\dot{1}}$  as zero in value. This program operation accomplishes the manipulation required by Equation (18).

For the solution method iterative scheme, the program considers trial eigenvalues until the convergence criteria based on the changes in trial eigenvalues are satisfied or the number of allowed iterations have occurred. In particular, for a given starting trial eigenvalue and a set of parameters required for the analysis, the determinant of  $[\overline{A}]$  and the correction vector  $\{\overline{\epsilon}\}$  by use of Equation (18) are determined based on all quantities of the trial eigenvector  $\{\overline{\lambda}\}$  being equal to unity. The  $\{\overline{\epsilon}\}$  quantities are then added to the  $\{\overline{\lambda}\}$  quantities to define a new  $\{\overline{\lambda}\}$ . new trial eigenvalue is obtained by increasing the starting trial eigenvalue by a specified percentage. The new trial eigenvalue and new  $\{\overline{\lambda}\}$  are used to determine a new determinant of  $[\overline{\mathbf{A}}]$  and a new  $\{\overline{\varepsilon}\}$  which is used to update  $\{\overline{\lambda}\}$ . From this point on the new trial eigenvalues are based upon a slope interpolation scheme using the previous two eigenvalues and corresponding determinant values of the form

$$s_{NE} = s_{CU} - \overline{\Delta}_{CU} (s_{CU} - s_{LA}) / (\overline{\Delta}_{CU} - \overline{\Delta}_{LA}).$$

In this expression,  $\overline{\Delta}_{CU}$  and  $\overline{\Delta}_{LA}$  denote the determinant values of  $[\overline{A}]$  for the iteration just completed and the iteration just prior to the one just completed, respectively, and  $s_{CU}$ ,  $s_{LA}$ , and  $s_{NE}$  denote the trial eigenvalues for the iteration just completed, the iteration just prior to the one just completed, and the next iteration, respectively. For each new eigenvalue the determinant and  $\{\overline{\epsilon}\}$  are calculated with the latter used to update the  $\{\overline{\lambda}\}$ . After each iteration after the

first two trial eigenvalues have been used, a convergence criteria test is applied such that a sufficient eigenvalue and eigenvector have been obtained if

 $|(s_{NE} - s_{CU})/s_{CU}| \le .1^{Mer}$ , where || denotes the complex

absolute value and Mer is an integer defining the convergence limit desired. As the program iteration proceeds, the determinant of  $[\bar{A}]$  and the  $\{\bar{\epsilon}\}$  quantities should both approach zero.

#### COMPUTER PROGRAM METHOD OF SOLUTION

The overall execution of the computer program is controlled by the main program. The main program initially determines, on the basis of input parameters, whether or not the scanning procedure is to be employed to obtain starting eigenvalues, and if so, specifies the operational procedure required. The main program then, on the basis of the number of starting eigenvalues inputted or obtained from the scanning procedure, the convergence criteria, and the iteration limit, directs the operational procedure of the program. If more than one case is to be considered in a computer run, the main program repeats the process for the additional runs. The overall iterative system flow for the computer program, assuming that starting eigenvalues are provided, is depicted in Figure 19.

The basic operational steps involved in the program method of solution are:

- 1. the input of system parameters,
- 2. the determination of intermediate terms,
- 3. the eigenvalue scanning procedure,
- 4. the blade transfer matrix procedure,
- 5. the rotor support structure transfer matrix procedure,
- 6. the construction of the  $[\overline{T}_{k,n}]$  matrices and the trial eigenvector forcing function vectors  $\{\overline{F}\}$ .
- 7. the determination of the final matrix determinant and eigenvector correction array  $\{\overline{\epsilon}\}$ .

Each of these operational components will be discussed to various degrees.

The system model parameters, program logic parameters, and, if needed, aerodynamic coefficient data are required as input to the program. The method of input of data consists of reading into a storage array all data (except aerodynamic data) using a single format which requires specification of

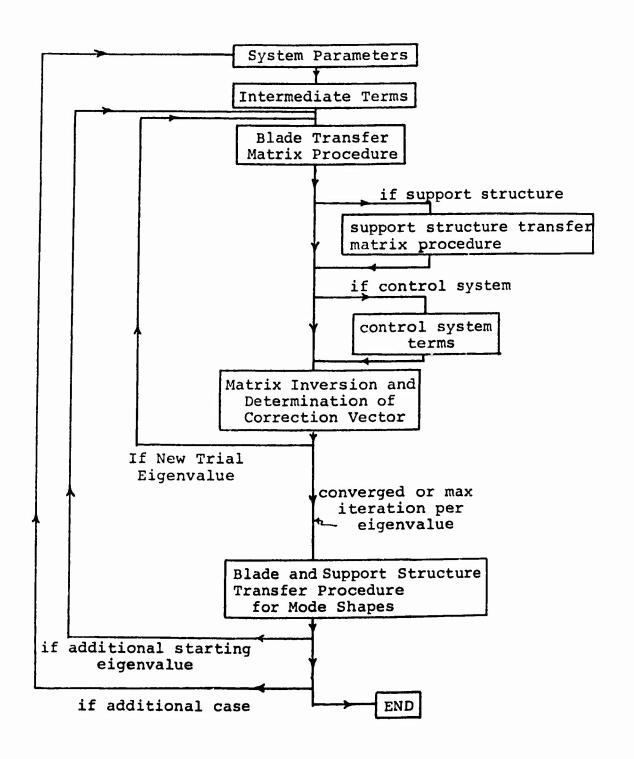


Figure 19. Overall Iterative System Flow.

the variable array location and the variable value in floating point form. The storage array input in floating point form corresponding to program integer variables is used to define the respective integer variables. The storage array consists of control and system parameter input stored in the first 200 locations, blade and rotor support structure section data in the next 2000 locations (50 locations per section), and a radial and azimuthally varying induced velocity distribution, if desired, in the last 600 locations. reason for the use of this input form was to eliminate the necessity of a defined order of input so that input cards out of order would not result in erroneous results or aborted This method of input also allows several computer runs. model configurations to be considered consecutively, with only system values inputted for those that are altered from the previous configuration. In addition, a variable can be modified to a new value after being previously defined in the same set of input, such that a basic input deck followed by input modifications can be used for the specific configurations of interest. The aerodynamic coefficient data, if required, must be read in for each case of a run. of this data allows the use of several input formats.

Since many terms and multiplying coefficients involved in the analysis are not a function of the Laplace transform variables and thereby the trial eigenvalue, these terms and coefficients (intermediate terms) are computed and stored prior to the first iteration of a case instead of being recalculated on every iteration of the iteration procedure for every initial eigenvalue. Intermediate terms required for the representation of the blade and rotor support structure sectional characteristics, except for aerodynamics, are stored in the SD vector which is contained in the labelled common SAIN. Intermediate terms for the representation of the blade and rotor support structure aerodynamic sectional characteristics are stored in the AMA vector contained in the labelled common AMAT and the AFA vector contained in the labelled common FUSA. In addition, intermediate terms associated with the control system representation and the blade discontinuities are also stored. This procedure of calculating and storing intermediate terms was instituted to reduce the program running time for a system configuration.

The eigenvalue scanning procedure was incorporated into the program mainline as an independent control segment to allow the determination of the possible solution eigenvalues in a specified range of stability (real part of the eigenvalue) and frequency (imaginary part of the eigenvalue) values. If

this procedure is utilized, the program operation equivalent to a single iteration is executed for each eigenvalue of a grid of values defined by the specification of the lowest stability and frequency values to be considered, the stability and frequency step sizes, and the number of stability and frequency steps to be taken. For each trial eigenvalue of the grid, the determinant of the final governing matrix is determined. An interpolation scheme is applied to the resulting information to determine possible solution eigenvalues, which are then used as starting eigenvalues for the normal iterative procedure to determine the solution eigenvalues and corresponding eigenvectors and mode shapes for the problem of interest. This procedure is not foolproof, however, since reasonable step sizes in both frequency and stability values are required to avoid missing possible eigenvalues.

The blade and rotor support structure transfer matrix procedures are discussed in a previous section; therefore, only the overall concept of these procedures is reviewed here. The blade transfer matrix procedure consists of two basic forms, that used during the iterative procedure and that used to obtain the state variables (mode shapes) at the end of each section. During the iterative procedure, the representation of the blade variables at the rotor hub - in terms of the blade tip and discontinuity unknowns - is obtained for each trial eigenvalue by successive multiplication of the initial blade tip-associated transfer matrices and discontinuity columns by the individual lumped-parameter characteristic transfer arrays as each characteristic is crossed in transferring from blade tip to rotor hub. individual blade transfer matrices are obtained by use of the stored intermediate terms and from the value of the trial eigenvalue. Also, during the application of the blade transfer matrices, information required for the blade discontinuity equations is stored as the discontinuities are crossed. When a solution eigenvalue is obtained (converged eigenvalue) the blade transfer matrix procedure is repeated for the solution eigenvalue in the same manner as during an iteration, except that at the inboard end of each blade section the associated blade transfer matrices and discontinuity columns corresponding to this location are applied to pertinent blade solution eigenvectors to obtain the frequency-shifted and unshifted blade section state variables. The solution eigenvector used to determine the values for the blade section state variables is equivalent to the sum of the trial eigenvector and the correction eigenvector associated with the iteration involving the solution eigenvalue.

The rotor support structure transfer matrix procedure is similar in concept to the blade transfer matrix procedure, except that due to the lack of structural discontinuities and aerodynamic interharmonic coupling the form of the representation is simpler. This transfer matrix procedure also consists of two basic forms; that used during the iterative procedure and that used to obtain the state variables (mode shapes) at each section of the rotor support structure when the eigenvalue has converged. These procedures are carried out in the same manner as for the blade representation but involve rotor support structure variables, unknowns, and intermediate parameters.

The representation of the frequency-shifted and unshifted blade and rotor support structure state variables for each trial eigenvalue at the rotor hub and discontinuity locations, in terms of the blade tip unknowns, discontinuity unknowns, and the rotor support structure unknowns, provides the majority of the terms necessary for the construction of the

 $\overline{T}_{k,n}$  matrices as defined by Equation (15). The remaining terms, such as control system governing equation terms, can be obtained by direct use of the system parameters or a combination of system parameters and blade and rotor support structure variable representations. As previously discussed, the complexity of these matrices is dependent on the degree of interharmonic coupling involved, the degrees of freedom of the rotor shaft-rotor hub interface, the number of rotor blades, the inclusion of control system representation, the inclusion of a rotor support structure, the use of the blade phasing assumption, etc. Through the use of subroutines, the program for each trial eigenvalue determines the numer-

ical construction of each  $\left[\overline{T}_{k,n}\right]$  matrix as required by the value of Nf and stores this information on an auxiliary storage input and also obtains the trial eigenvector forcing function  $\{\overline{F}\}$ .

The determination of the final governing matrix determinant and the correction eigenvector for each trial eigenvalue, and the iteration procedure used to obtain the solution eigenvalue, eigenvector, and mode shapes, is discussed in detail in the previous section. It should be noted that the determinant of the final governing matrix and the correction vector for each trial eigenvalue are obtained simultaneously by use of a sophisticated triangularization technique. This technique operates on the total final governing matrix and trial eigenvector forcing function in a manner such that an iterative procedure to obtain the determinant and a matrix

inversion for the correction eigenvector are not required. This technique has proven to be much faster in execution time and more accurate than previously used matrix manipulation procedures.

The roles which the various subroutines perform in the overall operation of the computer program to obtain the solution for the eigenvalues, eigenvectors, and mode shapes of a coupled rotor/helicopter system can be noted in the section pertaining to the description of the functionality of the various subroutines.

#### INTERPRETATION OF COMPUTER PROGRAM RESULTS

The resultant eigenvalue and eigenvector values obtained by the use of the HASTA program represent the behavior of the total system investigated. This program provides the fundamental and harmonic coefficients in a complex variable form of the real-time control system, blade, and rotor support structure state variables. A rotor support structure state variable at the hubward end of the ith section can be expressed as a function of time in the general form

$$f(t) \stackrel{(i)}{=} \sum_{p=-\infty}^{\infty} (X_p^{(i)} + iY_p^{(i)}) e^{\sigma t} e^{i(\omega t + p\Omega t)}. \quad (19)$$

In this expression,  $X_p^{(i)}$  and  $Y_p^{(i)}$  are the real and imaginary part, respectively, of the state variable of interest, of and  $\omega$  are the real and imaginary part, respectively, of the solution eigenvalue, and p is an integer that when positive in value denotes an oscillatory behavior at a frequency  $p\Omega$  radians per second higher than that corresponding to  $\omega$ . In the HASTA program output the state variables are printed in the order of p, going from positive to negative. By conversion of the exponential function with the imaginary argument in Equation (19) to a sine and cosine equivalent representation, the form of this equation can be modified to

$$f(t)^{(i)} = \sum_{p=-\infty}^{\infty} R_p^{(i)} e^{\sigma t} \cos(\omega t + p\Omega t + \beta_p^{(i)})$$
 (20)

where 
$$R_p^{(i)} = \sqrt{(X_p^{(i)})^2 + (Y_p^{(i)})^2}$$
 and  $\beta_p^{(i)} = \arctan(Y_p^{(i)}/X_p^{(i)})$ .

To be practical, the summation can be truncated to the range -Nf to Nf.

This state variable representation can be modified to represent a blade state variable at the inboard end of the ith section when the blade phasing assumption is not employed, by adding m subscripts to all blade-related variables. The behavior of the mth blade is relative to the rotating coordinate system of the mth blade on an azimuthal basis. Thus, at t equal to zero, the value of a state variable for the mth blade defined by the form of Equation (20) is for the

blade  $\phi_m$  radians azimuthally ahead of the fixed reference blade location. The variable  $\phi_m$  is not involved in the non-phased blade state variable definition of the form of Equation (20) since the contribution of this variable has been included in the blade tip state variables by the analysis coded.

When blade phasing is used, state variable coefficients are obtained for the first blade for which  $\phi_1$  is defined to be 0 in value, such that the definition for additional blades is obtained by use of the phasing relationship

$$\left\{\overline{S}_{n}\right\}_{m}^{(i)} = \left\{\overline{S}_{n}\right\}_{1}^{(i)} e^{i(-n-Nps)\phi_{m}}$$
 where Nps is an integer

denoting the type of phasing specified. From this relationship the p-related coefficients for a state variable of the mth blade can be defined as the corresponding state variable  $i \, (p\text{-Nps}) \, \phi_m$ 

of the first blade multiplied by e Thus, for blade phasing the representation used above for a support structure state variable would be modified, with the blade-related quantities having a subscript of 1 added, except for f(t) (i), which would have an m subscript added and would have p $\Omega$ t replaced with p( $\Omega$ + $\phi_m$ ) - Nps $\phi_m$ . The resulting mth blade state variables are azimuthally referenced to their own rotating hub coordinate system.

The fundamental and harmonic coefficients of the blade state variables defined both relative to the local blade coordinate system axes and to the rotating hub coordinate system (disk plane) axes can be provided in complex variable form by the HASTA program. Thus, the required form of Equations (19) and (20) can be used to determine the time-dependent behavior of the blade state variables as defined relative to either set of coordinate system axes, depending on which state variable output is used. The disk plane-related blade state variable fundamental and harmonic coefficients, if provided in complex variable form, are also provided in polar form such that only Equation (20) need be used to define the time-dependent behavior of the blade state variable as defined relative to the disk plane coordinate system axes. Similar comments are appropriate to the support structure state variables in that the fundamental and harmonic coefficients of these state variables can be provided relative to the support structure

fixed coordinate system in both complex variable and polar form, in addition to those of the standard complex variable form defined relative to the local support structure coordinate systems. The control system rotating frame displacement variable  $\mathbf{w}_{\ell}(t)$  can be defined in the same form of representation as for the rotor support structure, with  $\mathbf{f(t)}^{(i)}$  replaced by  $\mathbf{w}_{\ell}(t)$  and  $\mathbf{x}_{p}^{(i)}$  and  $\mathbf{y}_{p}^{(i)}$  replaced by  $\mathbf{x}_{\ell,p}$  and  $\mathbf{y}_{\ell,p}$ , respectively. The latter corresponds to the coefficients of the  $\ell$ th spatial harmonic of control system ring motion in the rotating control system coordinate system at a frequency of  $\omega + p\Omega$ .

## DESCRIPTION OF SUBROUTINE AND FUNCTIONS

Subroutine or function	Description		
ACOEFF	called from AERO and computes the two- dimensional lift, drag, and moment coeffi- cients and their slopes based on an airfoil angle of attack, Mach number, and specified type of aerodynamic coefficient representation		
AERO	called from BAERO and FAERO and computes aerodynamic angle of attack, Mach number, and preliminary aerodynamic terms (including Theodorsen aerodynamics on blade) required to determine the intermediate terms necessary for the aerodynamic transfer matrices at an aerodynamic load point		
BAERO	called from SECPAR and computes the inter- mediate terms necessary for the construction of the aerodynamic transfer matrices at a blade aerodynamic load point by performing a harmonic analysis of functions		
BARRAY	called from the main program and performs the transfer matrix procedure for successive blade sections to obtain the associated blade transfer matrices and discontinuity column vectors with the necessary information at discontinuity locations being stored for subsequent use during an iteration and the blade state variables at each section (mode shapes) being determined with respect to the local section and disk plane coordinate system after eigenvalue convergence		
BEND	called from BARRAY and SARRAY and constructs the bend transfer matrix necessary to account for changes in the local blade or rotor sup- port structure section coning, pitch, and sweep angles		

Subroutine or function	Description
BLARO	called from BARRAY and constructs the aero- dynamic transfer matrices necessary to ac- count for aerodynamic effects on a blade section
BMASS	called from BARRAY and constructs the mass transfer matrices necessary to account for mass and inertia effects on a blade section
CDOT	called from MLCC2 and is a FORTRAN-callable complex function written in assembler language that obtains the dot product of two complex vectors
DCMAT	called from SOLVE and computes the determinant of a nxn complex matrix and solves the nxn complex matrix equation, returning the matrix inverse to the input matrix and the solution to the input column
ELAST	called from BARRAY and SARRAY and constructs the elastic transfer matrix necessary to account for flexibility of a blade or rotor support structure section or constructs a transfer matrix associated with flexstrap or torque tube blade restraints (blade sec- tion only)
EPSOLN	called from the main program and controls the order of determination of the $\begin{bmatrix} \mathbf{T}_{k,n} \end{bmatrix}$ matrices and their transferral to auxiliary storage (tape or disk) and constructs the $[\overline{\mathbf{F}}]$ vector
ERRSET	called from SOLVE and is an IBM-supplied sub- routine for handling errors
EXCHI	called from ZLN, XNLQ, and ULN and computes exponential functions of the general form i(L-Q)X; where L and Q are both integers

Subroutine or function	Description		
EXPON	called from SUBMA, SUBMB, SUBMF, SWA, SWB, and ZTEGI; computes the exponential functions i.L.		
FAERO	called from SETUP and computes from the pre- liminary aerodynamic terms the intermediate terms necessary for the construction of the aerodynamic transfer matrices at a rotor support structure aerodynamic load point		
FMASS	called from SARRAY and constructs the mass transfer matrices necessary to account for mass and inertia effects on a rotor support structure section		
FUARO	called from SARRAY and constructs the aero- dynamic transfer matrices necessary to account for aerodynamic effects on a rotor support structure section		
LOADIN	called from SETUP and reads in the program control parameters, blade and fuselage section data, and control system data		
MLCC2	called from BARRAY and SARRAY and multiplies, in string mode, a complex 12xn matrix by a complex 12x12 matrix, returning the complex results in the input 12xn matrix		
MLRC2	called from BARRAY and SARRAY and multiplies, in string mode, a complex 12xn matrix by a real 12x12 matrix, returning the complex results in the input matrix		
POLAR	called from BARRAY and SARRAY and converts state variable harmonic coefficients to a polar form		
RCDOT	called from MLRC2; obtains dot products of a real and a complex vector and is a FORTRAN-callable complex function written in assembler language		

# Subroutine or function

#### Description

RIGID

called from BARRAY and SARRAY and constructs the rigid transfer matrix necessary to account for rigid shear center axis offsets on a blade or rotor support structure section

ROWSUM

called from DCMAT and is a FORTRAN-callable subroutine written in assembler language which performs matrix row operations

**SARRAY** 

called from the main program and performs the transfer matrix procedure for successive rotor support structure sections to obtain the associated rotor support structure transfer matrices with the rotor support structure state variables at each section (mode shapes) being determined with respect to the local and fixed rotor support structure coordinate systems after eigenvalue convergence

SECPAR

called from SETUP and computes the intermediate transfer matrix-related terms for both blade and rotor support structure sections and stores this information in the SD storage array, constructs the aerodynamic AMA storage array, and also outputs the section input data for all sections and the blade section steady forces and moments

SETUP

called from the main program and calls LOADIN and TABLU for the reading of system input parameters and aerodynamic data, respectively; defines integer control variables based on their corresponding floating point form variables, calculates intermediate terms including the construction of the aerodynamic AFA storage array, calculates program control parameters including indexing parameters, and outputs input data with descriptive headings

Subroutine or function	Description
SOLVE	called from the main program; reads the final matrix from the auxiliary storage unit and obtains the determinant of the final matrix and the correction eigenvector on each iteration
STIFF	called from BARRAY and SARRAY and constructs the transfer matrices necessary to account for torsional spring-damper units on a blade or rotor support structure section; can be used to account for a flap or lead-lag hinge between two blade sections
SUBMA	called from TKNS; for a value of $k$ and $n$ constructs the elements of the $\begin{bmatrix} \overline{T}_k, n \end{bmatrix}$ matrix corresponding to the $\begin{bmatrix} \overline{FU}_k \end{bmatrix}$ and $\begin{bmatrix} \overline{BF}_k, n \end{bmatrix}$ m submatrices of Equation (15), which specify the contribution of the rotor support structure unknowns to the blade and rotor support structure related governing equations
SUBMB	called from TKNS; for a value of $k$ and $n$ constructs the elements of the $\overline{T}_{k,n}$ matrix corresponding to the $\overline{FB}_{k,n}$ submatrices of Equation (15), which specify the contribution of the blade unknowns to the rotor support structure-related governing equations; constructs the first six rows of the $\overline{BB}_{k,n}$ l submatrix of Equation (15), which specify the contribution of the blade unknowns of the first blade to the blade-related governing equations of the first blade (not including discontinuity equations)

Subroutine or function	Description		
SUBMF	called from TKNS and for a value of k and		
	n constructs the elements of the $[\overline{T}_k, \underline{n}]$		
	matrix corresponding to the $\begin{bmatrix} \overline{BB}_{k,n} \end{bmatrix}_{m}^{m}$ sub-		
	matrices of Equation (15) for values of mother than unity		
SUBMG	called from TKNS and for a value of k and		
	n constructs the elements of the $[\overline{T}_{k,n}]$		
	matrix corresponding to discontinuity rows		
	of the $[\overline{BB}_{k,n}]_{1}^{1}$ submatrix of Equation (15),		
	which specify the contribution of the blade unknowns of the first blade to the blade discontinuity equations of the first blade		
SWA	called from TKNS and for a value of k and		
	n constructs the elements of the $[\overline{T}_k, \underline{n}]$		
	matrix corresponding to the $[\overline{SW}_{k,n}]$ and		
	$\overline{BS}_{k}$ m submatrices of Equation (15), which		
	specify the contribution of the control system unknowns to the control system governing equations and to the blade-related governing equations, respectively		
SWAPS	called from SOLVE; swaps the column designated by NORM with the last column of the final matrix and then swaps the row designated by IREM with the last row of the final matrix (note: NORM and IREM are associated with the location of a column and row in the $\left[\overline{T}_{0,0}\right]$ matrix		

Subroutine or function	Description		
SWB	called from TKNS and for a value of k and		
	n constructs the elements of the $[\overline{T}_{k,n}]$		
	matrix corresponding to the $\overline{\overline{SF}}_{k,n}$ and		
	$\overline{SB}_{k,n}$ m submatrices of Equation (15), which		
	specify contributions of the rotor support structure and blade unknowns to the control system governing equations		
TABLU	called from SETUP and reads in aerodynamic data, if required		
TKNS	called from EPSOLN and for each value of k and n calls the subroutines necessary		
	for the construction of $[\overline{T}_{k,n}]$		
ULN	called from SWB and computes multiplier terms involved in the determination of the		
	elements of the $[\overline{T}_{k,n}]$ matrix corresponding		
	to the $[\overline{SF}_{k,n}]$ submatrix		
XNLQ	called from SWA and computes the elements		
	of the $[\overline{T}_{k,n}]$ matrix corresponding to the		
	diagonal elements of $\overline{SW}_{k,n}$		
ZLN	called from SWA and computes the elements		
	of the $[\overline{T}_{k,\underline{n}}]$ matrix corresponding to the		
	off-diagonal elements of $\overline{SW}_{k,n}$		

# Subroutine or function

### Description

ZTEGI

called from TKNS when the rotor system is gimballed or teetering and computes the elements of the  $[\overline{T}_k, n]$  matrix corresponding to the  $[\overline{BB}_k, n]^j$  submatrices of Equation (15) where  $j \neq m$ , redefines some of the elements corresponding to  $[\overline{BB}_k, n]^m$  as required for these two types of rotor systems

#### COMPUTER PROGRAM SYMBOL DICTIONARY

Due to the quantity of computer program variables involved in the HASTA program, the program variables to be included in this section are restricted to those which are more significant. Thus, input variables which are only used to define other program variables on a one-to-one basis (such as floating point variables which define integer variables), some of the intermediate variables that are used to define other intermediate and final variables, and indexing variables are not included in the following definitions. number of indices involved in array variables is denoted by using the general form exemplified by AA(I,J,K,L). The dimensional requirements and present dimensions of the program arrays are specified as part of the user's manual portion of this report. The algebraic symbols used in Reference 1 and this report corresponding to the computer program variables are provided where applicable. It is to be noted that although a program name may represent more than one variable there is no conflict since an identical program name may be used in a subroutine. Where applicable, units are given in English units but equivalent SI units or other systems of units (e.g., inches instead of feet) may be used if applied to all definitions of program variables.

Computer Name  A(I)	Algebraic Symbol  A  A  A  B  M  M	Definition or Description  array representing a blade mass transfer matrix in string mode by row
A(I,J)	$\left[\overline{A}_{ij}\right],\left[\overline{A}\right]$	final governing matrix array
AC(I)	cj	<pre>damping coefficient of the con- trol system ring jth cyclic spring-damper unit support, lb-sec/ft</pre>
AC(I)	$\left[\overline{c}_{n-k}\right]_{m}^{i}$	array specifying the contribution of aerodynamic damping terms to a blade section aerodynamic transfer matrix in string mode by row

Computer Name	Algebraic Symbol	Definition or Description
ACP(I)	<sup>cφ</sup> j	torsional damping coefficient of control system ring jth torsional spring-damper unit counteracting local ring longitudinal rotation, ft-lb-sec/rad
ACT(I)	c <sup>θ</sup> j	torsional damping coefficient of control system ring jth torsional spring-damper unit counteracting local ring lateral rotation, ft-lb-sec/rad
AD(I)	¯n−k m	array specifying the contribution of non-damping aerodynamic terms to a blade section aerodynamic transfer matrix in string mode by row
AEXT	L <sub>s</sub>	<pre>length of torque tube pitch control structure spur or ex- tension shaft, ft</pre>
AFA(I)		storage array for intermediate support structure section aerodynamic terms
AG	g	<pre>gravitational acceleration constant, ft/sec<sup>2</sup></pre>
AIRD	ρ	air density, lb-sec <sup>2</sup> /ft <sup>4</sup>
AK(I)	<sup>k</sup> j	linear stiffness of the control system ring jth cyclic spring-damper unit support, lb/ft
AKCI(I)	1/k <sub>m</sub>	reciprocal of the mth blade control rod axial stiffness for an articulated type blade, ft/lb

Computer Name	Algebraic Symbol	Definition or Description
AKP(I)	k¢j	torsional stiffness of control system ring jth torsional spring-damper unit counteracting local ring longitudinal rotation, ft-lb/rad
AKT(I)	kθ <sub>j</sub>	torsional stiffness of control system ring jth torsional spring-damper unit counteracting local ring lateral rotation, ft-lb/rad
AL(I,J)		trigonometric functions of control rod orientation angles for the jth flexstrap or bearingless blade
AL12(I)	L12 <sub>m</sub> , L <sub>cc</sub>	perpendicular distance between rotor disk plane and mth blade control rod-control system attachment point, positive if attachment point is in -z <sub>rm</sub>
		direction from disk plane, ft (for flexstrap or bearingless blade)
ALM(I)	<b>{λ}</b>	trial eigenvector column array
ALPHS(I,J,K,L)	α <sub>i</sub>	storage array for the angles of attack inputted for each Mach number for each type of aerodynamic coefficient for each aerodynamic table number
ALPHZ	αj	calculated angle of attack at an aerodynamic load point, rad (but usually converted to degrees, dependent on aerody- namic coefficient representa- tion used)

Í

Computer Name	Algebraic Symbol	Definition or Description
ALSTH(I)	L <sub>b</sub>	perpendicular distance between rotor disk plane and spur spherical bearing attachment point, positive if attachment point is in -z direction
		<pre>from disk plane, ft (for bear- ingless blade)</pre>
AMA(I)		storage array for intermediate blade section aerodynamic terms
AMACH(I,J,K)	M <sub>i</sub>	storage array for the Mach number inputted for each type of aerodynamic coefficient for each aerodynamic table number
AMACZ		calculated Mach number at an aerodynamic load point
AMKC(I)	1/K <sub>c,m</sub>	reciprocal of the mth blade control rod axial stiffness for a flexstrap or bearingless blade, ft/lb
AMY(I,J,K), AMZ(I,J,K)	$(\overline{My}_{m})_{k}, (\overline{Mz}_{m})_{k}$	arrays containing the shifted and unshifted flapwise and edgewise bending moments, re- spectively, acting on each section of each blade
AMY(I,J) AMZ(I,J)	(My <sub>s</sub> ), (Mz <sub>s</sub> ),	arrays containing the shifted and unshifted lateral and ver- tical bending moments, respec- tively, acting on each support structure section
AN (I,J,K)	( $\overline{N}_{m}$ ) k	array containing the shifted and unshifted radial forces acting on each section of each blade

Computer Name	Algebraic Symbol	Definition or Description
AN(I,J)	$(\overline{\mathtt{N}}_{\mathbf{s}})_{\mathrm{k}}^{1}$	array containing the shifted and unshifted axial forces acting on each support structure section
ARMO, ARVZ, ARVY		steady torque, flapwise force, and edgewise force, respec- tively acting on a blade sec- tion due to aerodynamic effects
ATAB		number of the aerodynamic data table to be used for an aerodynamic section
AZER		velocity of sound, ft/sec
B(I)	BE m	array representing a blade or support structure bend transfer matrix in string mode by row
B(I)	$\left[\overline{B}_{k,n}\right]^{i}_{m}$	array representing all k and n subscripted associated blade transfer matrices at a section where each matrix is stored in string mode by column and the order of storage of these matrices in the array is accomplished by varying n from -Nf to +Nf for each value of k from -Nf to +Nf
BJ(I)	b	offset of the control system jth cyclic spring-damper unit attachment point from the circumferential axis of the control system ring, positive toward center of ring, ft
BSAVE(I)		storage array for the blade- associated transfer matrices B(I) at an aerodynamic charac- teristic; required to properly transfer across this type of characteristic because of inter- harmonic coupling effects

Computer Name	Algebraic Symbol	Definition or Description
BVLI,BVLJ, BVLK		calculated velocities of an aerodynamic load point with respect to the first blade-associated rotating hub coordinate system $\bar{i}$ , $\bar{j}$ , and $\bar{k}$ directions, respectively, ft/sec
C(I)	$\begin{bmatrix} c_{n-k} \end{bmatrix}_{m}^{i}$	aerodynamic transfer matrix array identical to AC(I)
CAPC	С	damping coefficient of control system base plate spring-damper unit support, lb-sec/ft
CAPFY, CAPFZ, CAPM		steady two-dimensional local aerodynamic edgewise force, flapwise force, and moment, respectively, at an aerodynamic load point
CAPK	К	linear stiffness of control system base plate spring-damper unit support, lb/ft
CAPP		effective rotational velocity of the blade around its span-wise axis due to coning, rad/sec
CCS(I,J,K)	c1 <sub>i</sub> ,c2 <sub>i</sub> ,c3 <sub>i</sub>	storage array for series representation coefficients inputted for each type of aerodynamic coefficient for each aerodynamic table number
CFORC	$^{ ext{P}} ext{T}$	centrifugal force acting on a blade section, lb
CHI	X	one of two angles which specify orientation of the helicopter velocity vector with respect to the fixed hub coordinate system, rad

Computer Name	Algebraic Symbol	Definition or Description
CI,CR		frequency (rad/sec) and stabil- ity (l/sec) parts of a trial eigenvalue used during the search option procedure
CIS,CRS		frequency (rad/sec) and stabil- ity (l/sec) parts of the initial eigenvalue used during the search option procedure
CLALP, CDALP, CMALP		calculated lift, drag, and moment coefficient slopes, respectively, at an aerodynamic load point
CLDM(I,J,K,L)	CL <sub>i</sub> ,CD <sub>i</sub> ,CM <sub>i</sub>	storage array for the values of the aerodynamic coefficients for each angle of attack for each Mach number for each type of aerodynamic coefficient for each aerodynamic table number
CMl	i	imaginary number, $\sqrt{-1}$
CMS	s	Laplace transform variable
COE1		steady blade torque at pitch control structure - blade at- tachment point not removed by pitch control structure, ft-lb (for articulated blade without pitch bearing, flexstrap blade, or bearingless blade)
COE2		effective distance, which in conjunction with COEl defines steady flapwise shear force acting on blade as a result of steady blade torque removed by pitch control structure, ft
COE 3		percentage of steady blade torque not removed by pitch con- trol structure (for articulated blades with a pitch bearing)

Computer Name	Algebraic Symbol	Definition or Description
COLL	<sup>θ</sup> coll	collective pitch of the blades, rad, if not included in the blade section twist distribution
CPSI(I,J)		array containing terms of the form $cos(L(K-1)2\pi/NAS)$
CS(I,J)		array containing terms of the form $\text{cosL}\phi_{m}$
CS1,CS2		k-frequency-shifted Laplace transform variable s-ik $\Omega$ and (s-ik $\Omega$ ) <sup>2</sup> , respectively
CSA(I,J)		array containing terms of the form $cosL\chi_{\dot{j}}$
CSUBL, CSUBD, CSUBM		calculated lift, drag, and moment coefficients at an aero-dynamic load point
CTAU(I)	Ct <sub>C,m</sub>	damping coefficient of the mth blade control rod for a flex- strap or bearingless blade, lb-sec/ft
CTB(I)		array representing contribu- tions of the blade tip state variables to the control torque discontinuity equations for an articulated blade, to the forces acting on the control rod end of the pitch arm in the rotating hub coordinate system x-axis direction for a flex- strap blade, and to the de- flection of the control rod end of the pitch arm in the rota- ting hub coordinate system x-axis direction for a bearing- less blade, where in all cases the information is stored by varying n from -Nf to +Nf for each value of k from -Nf to +Nf

Computer Name	Algebraic Symbol	Definition or Description
CTB1(I), CTB2(I), CTB3(I), CTB4(I)		arrays containing the elements required to denote the blade torque, pitch bearing, flap, and lead-lag discontinuity contributions, respectively, to the control torque discontinuity equations for an acticulated blade where the order of storage is the same as for CTB(I)
CX(I)	C <sub>i,m</sub>	influence coefficients used to construct the restraint trans- fer matrices associated with the pitch control structure of a flexstrap or bearingless blade
CYFA		fore and aft blade cyclic pitch corresponding to the value of blade cyclic pitch when blade is located in the fixed hub coordinate system -y-axis direction, rad
CYLA		lateral blade cyclic pitch corresponding to the value of blade cyclic pitch when blade is located in the fixed hub coordinate system x-axis direction, rad
D(I)	$\begin{bmatrix} D_{n-k} \end{bmatrix}_{m}^{1}$	aerodynamic transfer matrix array identical to AD(I)
DACO		control variable such that if greater than zero in value, mass and inertia-related damping are not included in blade mass transfer matrix
DAT(I)		input data storage array which is equivalenced to labelled common PLOAD

Computer Name	Algebraic Symbol	Definition or Description
DB(I,J)	$\left[\overline{A}_{i}\right]$ , $\left[\overline{A}\right]$	final governing matrix array-identical to A(I,J)
DETR(I)		array storing the real part of the determinant for a zero- valued imaginary part based on interpolation at the first change in sign of the imagi- nary part during scan of sta- bility values for each fre- quency
DETR2(I)		<pre>same concept as DETR(I) but pertains to a second change in sign of the imaginary part of the determinant</pre>
DETSV		value of the determinant of the final governing matrix with a factor of 10**(n*20) removed to avoid overflow problems
DFAC		corresponds to the power of 10 (10**DFAC) which is removed on calculating DETSV and is an integer multiple of 20
DFYDP, DFZDP, DMDP		change in the total local aerodynamic edgewise force, flapwise force, and moment, respectively, with respect to a change in the blade local torsional angle at an aerodynamic load point
DFYDVZ,DFZDVZ, DMDVZ		change in the total local aerodynamic edgewise force, flapwise force, and moment, respectively, with respect to a change in the blade local flapwise velocity at an aerodynamic load point

Computer Name	Algebraic Symbol	Definition or Description
DMS(I)	d <sub>m</sub>	rigid offset of the mth blade control rod attachment point from the circumferential axis of the control system ring, positive outward, ft
DPHAS, DPIVOT		complex numbers which when multiplied together provide the determinant value of the determinant matrix modified to have diagonal elements of a complex absolute value of unity
DTLG10	i	factor removed from the de- terminant in the process of reducing the determinant ma- trix to one which has diag- onal elements with a complex absolute value of unity
E(I)	E m	array representing a blade or support structure elastic transfer matrix in string mode by row where this matrix can also represent an elastic restraint applied to the blade as in the case of a flexstrap or bearingless blade
EC(I)		array storing the interpolated eigenvalues associated with the data stored in DETR(I)
EC(2)		array storing the interpolated eigenvalues associated with the data stored in DETR2(I)
ECHI(I)	Хj	azimuthal angle of the jth control system cyclic spring-damper unit support relative to the fixed shaft coordinate system, rad

Computer Name	Algebraic Symbol	Definition or Description
EE(I)		integer data block whose six values specify the elements of the initial associated support structure transfer matrices that are set to unity for free support structure conditions
EGNC, EGNN, EGNL		trial eigenvalue for the iteration just completed, the next iteration, and previous iteration, respectively
EGNS(I)		starting eigenvalues for the solution iteration procedure (five values allowed for each case)
EGNSL(I)		array containing final eigen- values obtained for each starting eigenvalue
EM(I)		integer data block used to define initial associated transfer matrices corresponding to initial section end conditions in BARRAY specifies free end conditions - in SARRAY specifies cantilevered end conditions (similar in concept to EE(I))
EPS(I)	$\{\overline{\varepsilon}\}$ and $\{\overline{F}\}$	used as both correction eigen- vector column and trial eigen- vector forcing function column array
EYEX		flapwise bending stiffness of the torque tube pitch control structure spur about its local coordinate system y-axis, lb-ft <sup>2</sup>

Computer Name	Algebraic Symbol	Definition or Description
EZEX		edgewise bending stiffness of the torque tube pitch con- trol structure spur about its local coordinate system z-axis, lb-ft <sup>2</sup>
FAB(I)		same concept as for CTB(I) except that the contributions specified are for the pitch bearing discontinuity equations for an articulated blade, for the forces acting on the control rod end of the pitch arm in the rotating hub coordinate system y-axis direction for a flexstrap blade, and for the deflection of the control rod end of the pitch arm in the rotating hub coordinate system y-axis direction for a bearingless blade
FAB1(I), FAB3(I), FAB4(I)		arrays containing the elements required to denote the blade torque, flap, and lead-lag discontinuity contributions, respectively, to the pitch bearing discontinuity equations for an articulated blade (similar in concept to CTB1(I), CTB3(I), and CTB4(I))
FACC, FACL		value of DFAC on iteration just completed and previous iteration, respectively
FACT		correction factor to account for a change in DFAC on suc- cessive iterations, required for proper interpolation to obtain the next trial eigen- value
FGRA		gravitational acceleration constant, ft/sec - identical to AG

Computer Name	Algebraic Symbol	Definition or Description
FLB(I)		same concept as for CTB(I) except that the contributions specified are for the flap discontinuity equations for an articulated blade and for the forces acting on the control rod end of the pitch arm in the rotating hub coordinate system z-axis direction for a flexstrap or bearingless blade
FLB1(I),FLB3(I) FLB4(I)	•,	arrays containing the elements required to denote the blade torque, pitch bearing, and lead-lag discontinuity contributions, respectively, to the flap discontinuity equations for an articulated blade (similar in concept to CTB1(I), CTB2(I), and CTB4(I))
FORCE(I)	{ <b>F</b> },{ε}	trial eigenvectors forcing function column array in SOLVE which on solution is converted to the correction eigenvector column array
FSB(I)		same concept as for CTB(I) except that the contributions specified are for the lead-lag discontinuity equations for an articulated blade and for the deflection of the control rod end of the pitch arm in the rotating hub coordinate system z-axis direction for a bearingless blade (not involved with flexstrap blade representation)

Computer Name	Algebraic Symbol	Definition or Description
FSB1(I),FSB2(I), FSB3(I)		array containing the elements required to denote the blade torque, pitch bearing, and flap discontinuity contributions, respectively, to the lead-lag discontinuity equations for an articulated blade (similar in concept to CTB1(I), CTB2(I), and CTB3(I))
FVEL		helicopter velocity with respect to a stationary reference coordinate system, ft/sec
FVLA, FVLP, FVLT		helicopter velocity in the x, z, and y axis directions of the fixed hub coordinate system, respectively, ft/sec
GCTCP		component of gravitational acceleration acting perpendicular to the rotor disk plane, ft/sec2
GP,GT	$\phi_g$ and $\theta_g$	two angles that specify orientation of the gravity vector relative to the fixed hub coordinate system, rad
IALP		integer data block whose six values specify the rows of the associated transfer matrices at the shaft-hub interface that correspond to slope and deflection definitions
IBW		internal control variable allowing use of blockage (MTAB=7) or simplified NACA 0012 linear aerodynamics (MTAB=6) for the support structure

Computer Name	Algebraic Symbol	Definition or Description
ICHG(I)		operational integer array utilized in triangularization of the final governing matrix
ICOL, IROW		number of the column and row, respectively, of the final governing matrix to be switched with the last column and row of the matrix for determination of the correction eigenvector (ICOL=NHC*NRIFC+NORM andIROW=NHC*NRIFC+IREM)
IF, IG		number of frequency and sta- bility steps, respectively, to be used in the search option solution method
ILL		index denoting aerodynamic load point number for use of azimuthal and radially variable induced velocity field
IPCT		number denoting the percentage of a 1-percent increment of the starting trial eigenvalue to be added to obtain the second trial eigenvalue
IPU		control parameter which controls punched shape vector output (0-no punched output, 1-punched output)
IREM		the number of the row in the set of unshifted equations of the final governing matrix which is to be removed for obtaining the correction eigenvector (see definition of IROW)

Computer Name	Algebraic Symbol	Definition or Description
IROW1(I)		integer data block whose six values specify the rows of the associated transfer matrices at shaft-hub shaft interface that correspond to force and moment definitions
IROW3(I)		integer data block whose two values specify the rows of the associated transfer matrices at the shaft-hub interface that corresond to the blade flapwise and edgewise force definitions
ISER		control parameter that specifies whether aerodynamic coefficient data corresponding to a data table number is to be inputted in the standard tabular form, C-81 tabular form, or a series representation form (0-standard tabular data, 81- C-81 tabular data, 1-series data)
ITI		iteration index with ITI equal to zero on the first iteration
KSML	k	integer denoting the frequency shift of the equations and Laplace transform variables
Ml→M7		section control parameters where M1,M2,M3,M4,M5,M6, and M7 correspond to mass and inertia, bend, aerodynamic, elastic, rigid offset, torsional stiffness, and elastic restraint lumped-parameter characteristics of a section, respectively (the section control parameter associated with a lumped-parameter characteristic is 0 if characteristic

Computer Name	Algebraic Symbol	Definition or Description
		is not to be included, 1 if included in a blade section, and 2 if included in a support structure section) Note: M7 must = 0 if MFLEX = 0
MAER		<pre>aerodynamic control parameter (0-no aerodynamics, 1-blade and/or support structure aero- dynamics included)</pre>
MAXN	Nmax	highest azimuthal (spatial) harmonic of control system ring displacement to be included
MCON	Mr	control parameter for the in- clusion of the effects of the pitch control structure re- straint unknowns on the flex- strap or bearingless blade behavior (0-these effects not included, 1-these effects included)
MCT,MFEA, MFLAP,MLEL	Mct,Mfea, Mflap,Mlel	
MCTY		control parameter used in conjunction with MFLEX=1 to denote whether a flexstrap or bearingless rotor is of interest (0-flexstrap, 1-bearingless)
MER	Mer	number of repeatable signifi- cant figures required for convergence of the iteration procedure for each starting eigenvalue

Computer Name	Algebraic Symbol	Definition or Description
MFASB		number of elements required in storing discontinuity contri- butions to the discontinuity equations (e.g., CTBl(I))
MFLEX		<pre>blade type control parameter (0-articulated, 1-flexstrap or bearingless)</pre>
MFUS		<pre>support structure control pa- rameter (0-no support struc- ture, 1-support structure is included)</pre>
MODE		internal iteration control parameter (0-iteration procedure to continue, 1-mode shapes to be determined for solution eigenvalue)
MSC	-	control system collective spring-damper unit control parameter (0-no unit, 1-collective spring-damper unit included)
MTAB		number of the aerodynamic data table to be used for an aerodynamic section
МХСРК		<pre>number of elements required in the associated blade trans- fer matrix storage arrays B(I) and BSAVE(I)</pre>
MXCPL		<pre>number of combinations of k and n values required (MXSMI*MXSMI)</pre>
МХСРМ		number of elements in an in- dividual associated transfer matrix array (72)
MXCSB		number of elements in an in- dividual discontinuity column array (12)

Computer Name	Algebraic Symbol	Definition or Description
MXFAB		number of elements required in the arrays used for storing the blade tip variable contributions to the discontinuity equations (i.e., CTB(I))
MXKQ		number of elements required to store the n-related discontinuity column arrays for a particular value of k
MXQ		number of equations in the final governing matrix (MXQ $x$ MXQ)
MXSMB		number of elements required in the arrays used for storing the discontinuity column ar- rays (e.g., SMLB(I))
MXSMI		<pre>number of sets of k-fre- quency-shifted equations (2*NHC+1)</pre>
MXT2P1		number of control system equations for a particular value of k
MXTKN		number of elements in TKN(I)
NAMA		number of blade aerodynamic intermediate terms stored for each blade section having aerodynamic lumped-parameter characteristics
NAS	NAS	number of azimuthal steps to be used for the blade aero- dynamic harmonic computations
NB	Nb	number of blades unless the blade phasing assumption is used (NBP \neq 0) where NB must be equal to 1

Computer Name	Algebraic Symbol	Definition or Description
NBC		<pre>number specifying type of rotor hub conditions (0-can- tilevered, 1-gimballed, 2-teetering)</pre>
NBP		number of blades when the blade phasing option is used (otherwise equal to zero)
NBSEC	NS	number of blade sections (cannot be greater than 35)
NCACF, NCACG		internal logic control parameters that specify application of the transfer matrix procedures to SMLF(I) and SMLG(I), respectively, after the pitch control structure restraint application point is crossed for a bearingless blade
NCCT, NCFFA, NCFLP		internal logic control parameters that specify application of transfer matrix procedures to the control torque, pitch bearing, and flap discontinuity column arrays (SMLB(I), SMLC(I), SMLD(I)), respectively, after the respective discontinuities are crossed for an articulated blade; specifies application of the transfer matrix procedures to the SMLB(I), SMLC(I), and SMLD(I) arrays after the pitch control structure restraint application point is crossed for a flexstrap or bearingless blade

Computer Name	Algebraic Symbol	Definition or Description
NCLEL		internal logic control parameter which specifies application of the transfer matrix procedures to SMLE(I) after the lead-lag discontinuity is crossed for an articulated blade or the pitch control structure restraint application point is crossed for a bearingless blade
NCLS(I,J,K)		storage array for the number of angles of attack for each Mach number for each type of aerodynamic coefficient for each aerodynamic table number
NCOLS		number of blade tip variable unknowns for a particular value of k (6)
NCON	Nr	blade section number of section at which the pitch control structure restraint is applied for a flexstrap or bearingless blade
NCT, NFEA, NFLAP, NLEL		blade section number just in- board of which the control torque, pitch bearing, flap, and lead-lag discontinuities, respectively, are applied for an articulated rotor (Note: if MFEA=0, NFEA still denotes the location at and outboard of which the collective pitch is added to the sectional twist distribution)
NDAT		number of elements in DAT(I) array, defined internally in SETUP as 2800

Computer Name	Algebraic Symbol	Definition or Description
NDIM		number of rows dimensioned for the final governing matrix ar- ray as defined in DCMAT; must be altered if the dimen- sions of the arrays in this subroutine are altered
NEBC		number of elements required to store the n-related asso- ciated blade transfer matrices for a particular value of k
NEGN		number of starting eigenvalues to be considered for a model
NEIFC		number of elements required to represent the first column of submatrices in Equation (15) (0 if no control system)
NEISC		number of elements required to represent the second column of submatrices in Equation (15) (0 if no rotor support structure)
NEITÇ		number of elements required to represent the third column of submatrices in Equation (15)
NES	Nes	number of azimuthally located control system cyclic spring-damper unit supports
NESBC		number of elements required to store the n-related discontinuity column arrays for a particular value of k
NEX		must have same value as IREM in the present solution technique

Computer Name	Algebraic Symbol	Definition or Description
NFFB		control parameter specifying boundary conditions at the first section of the support structure (0-cantilevered to ground, 1-free)
NFP1		NHC+1
NFSEC	NSF	<pre>number of support structure sections (NFSEC+NBSEC cannot be greater than 10)</pre>
NFUS		<pre>number of support structure- related governing equations for a particular value of k (6*MFUS)</pre>
NHC	N£	maximum number of harmonics included for interharmonic coupling
NIT		maximum number of iterations, in addition to the initial iteration, which are allowed for each starting eigenvalue
NMACH(I,J)		storage array for the number of Mach numbers for each type of aerodynamic coefficient for each aerodynamic table number
NOGNS		number of starting eigenvalues obtained from use of the search option procedure or set equal to NEGN
NORM		the number of the column in the set of the (n=0) related columns of the final governing matrix which is to be removed for obtaining the correction eigenvector (corresponds to the row number of the unknown in the unshifted solution eigenvector which is normal- ized to unity; see definition of ICOL)

Computer Name	Algebraic Symbol	Definition or Description
NPD		control parameter for the de- termination of the disk plane blade shape vectors and sup- port structure shape vectors relative to the support struc- ture fixed coordinate system in both complex variable and polar form. (0-shape vectors only with respect to local axis systems, 1-shape vectors calculated and outputted rela- tive to the additional coordi- nate systems in complex variable and polar form)
NPRS		control parameter for output of control parameter input in labelled form (0-no output, 1-output)
NPS		number denoting the type of blade phasing to be considered (-1 backward cyclic mode, 0-umbrella mode, 1-forward cyclic mode, 2-reactionless mode)
NRBD		number of blade-related gov- erning equations including blade discontinuity equations for each blade for a particular value of k
NRIFC		number of rows (or columns) in the matrix represented by TKN(I)
NSCH		control parameter for use of search option solution method (0-no search option use, 1-search option used)

Computer Name	Algebraic Symbol	Definition or Description
NSK		control parameter for use of sup- port structure aerodynamics (0-no support structure aerodynamics, 1-support structure aerodynamics included if MAER ≠ 0)
NSP		control parameter for use of control system representation (0-no control system equations, 1-control system equations included)
NSY		number of element in Y(I) (100 by definition in SETUP)
NTAB		number of aerodynamic tables (or series form representations) to be inputted
NTOT		total number of lumped-parameter sections (NBSEC+NFSEC) and cannot exceed 40
NVI		control parameter for use of radial and azimuthally variant induced velocity distribution (0-section input induced velocity used, 1-radial and azimuthally variant distribution used)
OM,OM1	Ω	<pre>rotor rotational speed, rad/ sec</pre>
OM2	$\Omega^2$	square of the rotor rotational speed, rad <sup>2</sup> /sec <sup>2</sup>
P(I)		storage array for all blade and support structure section data with 50 elements to each section

Computer	Algebraic	
Name	Symbol	Definition or Description
PENOM(I)		array containing each final frequency obtained, in non-dimensional form, for each starting eigenvalue pitch-flap coupling factor
FFC		representing pitch-flap coupling for an articulated blade, if this coupling is not represented by blade modeling (see definition of input Loc. 9 in the Description of Input Data section of this report)
PHIC(I)	<sup>φ</sup> c,m	one of two angles defining the orientation of the mth flex- strap or bearingless blade control rod with respect to the blade's rotating hub coor- dinate system, rad
PHIM(I)	φ <sub>m</sub>	angular position of the mth blade relative to the reference blade position (azimuthal location of fixed hub coordinate system x-axis) at time equal to zero, rad
PHIX(I,J,K), PHIY(I,J,K), PHIZ(I,J,K)	$(\overline{\phi x}_{m})_{k}^{i}, (\overline{\phi y}_{m})_{k}^{i},$ $(\overline{\phi z}_{m})_{k}^{i}$	arrays containing the shifted and unshifted torsional, flap- wise, and edgewise bending slopes, respectively, for each section of each blade
PHIX(I,J), PHIY(I,J), PHIZ(I,J)	$(\overline{\phi x}_{s})_{k}^{i}, (\overline{\phi y}_{s})_{k}^{i}$ $(\overline{\phi z}_{s})_{k}^{i}$	arrays containing the shifted and unshifted torsional, lat- eral, and vertical bending slopes, respectively, for each support structure section
PHOTT(I)		array containing length, stiff- ness, and orientation param- eters associated with the flex- strap pitch arm (MCTY=0) or with the torque tube (MCTY=1)

Computer Name	Algebraic Symbol	Definition or Description
PHWTT(I)		array containing length, stiff- ness and orientation param- eters associated with the pitch arm of the torque tube pitch control structure (MCTY=1)
PINO	π	pi, 3.141592654
PLC		pitch-lag coupling factor representing pitch-lag coupling for an articulated blade, if this coupling is not represented by blade modeling (see definition of input Loc. 10 in the Description of Input Data section of this report)
QBAR(I)		temporary storage array of 12 elements for the shifted and unshifted support structure state variable vectors at a section as each is determined
R(I)	[R]im	array reporesenting a blade or support structure rigid offset transfer matrix in string mode by row
R(I)		operational complex variable array used in BARRAY and SARRAY which takes on the values of complex variable transfer matrix arrays generated in transfer matrix subroutines, except for the blade aerodynamic transfer matrices
REMC, REML		value of the determinant on the iteration just completed and the previous iteration, respectively

Computer Name	Algebraic Symbol	Definition or Description
RREAL(I)		operational real variable array used in BARRAY and SAR-RAY which takes on the values of real variable transfer matrix arrays generated in transfer matrix subroutines
S(I)	\$\overline{S}_k\$     s	array representing all k- subscripted associated sup- port structure transfer ma- trices at a section where each matrix is stored in string mode by column and the order of storage of the ma- trices is for k from -Nf to +Nf
SA(I,J)		used to represent coordinate system transformation arrays for a bend lumped-parameter characteristic and also used in the determination of terms associated with the represen- tation of the flexstrap or torque tube restraints
SAT(I,J)		used to represent a coordinate system transformation array for the next section outboard of a section having a bend lumped-parameter characteristic (multiplication of this array by the SA(I,J) array of the next inboard section with a change in orientation provides the intermediate terms required for a bend transfer matrix) and also used in the determination of terms associated with the representation of the torque tube restraints

A.

Computer Name	Algebraic Symbol	Definition or Description
SD(I)		storage array for the Y(I) arrays of each blade and support structure section
SDCO		structural damping coefficient factor
SDVEL		velocity of sound, ft/sec
SHAPE(I)		temporary storage array of 12 elements for the shifted and unshifted blade state variable vectors at a section of a blade as each is determined
SI(I)	ω	array of the frequency components of the starting eigenvalues, rad/sec
SK(I)	[SKk] i m	array representing a blade or support structure torsional spring-damper transfer matrix in string mode by row
SMLA(I)	a <sub>m</sub>	effective torque arm length of the mth blade pitch arm for an articulated blade, positive if pitch arm is aft of blade shear center, ft
SMLB(I), SMLC(I), SMLD(I), SMLE(I), SMLF(F), SMLG(G)	$ \begin{cases} \overline{b}_{k,n} \\ \overline{d}_{k,n} \end{cases}_{m}^{i}, \begin{cases} \overline{c}_{k,n} \\ \overline{e}_{k,n} \end{cases}_{m}^{i}, \begin{cases} \overline{e}_{k,n} \\ \overline{f}_{k,n} \end{cases}_{m}^{i}, \begin{cases} \overline{g}_{k,n} \\ \overline{g}_{k,n} \end{cases}_{m}^{i} $	arrays representing all k- and n-subscripted associated blade discontinuity vectors corresponding to the contribu- tions of specific discontinuity unknowns, where each type of column array is stored in its respective array in the same manner as the associated blade transfer matrices are stored in B(I)

Computer Name	Algebraic Symbol	Definition or Description
Name	Symbol	belinition of bescription
SMLBSV(I), SMLCSV(I), SMLDSV(I), SMLESV(I), SMLFSV(I), SMLGSV(I)		storage arrays for SMLB(I), SMLC(I), SMLD(I), SMLE(I), SMLF(I), and SMLG(I), respec- tively, at an aerodynamic characteristic; required to properly transfer across this characteristic due to inter- harmonic coupling effects
SN(I,J)		array containing terms of the form $\text{sinL} \boldsymbol{\phi}_m$
SNA(I,J)		erray containing terms of the form $sinL\chi_j$
SPSI(I,J)		array containing terms of the form $sin(L(K-1)2\pi/NAS)$
SR(I)	σ	array of the stability com- ponents of the starting eigen- values, rad/sec
STF,STG		stepsize of frequency, rad/sec, and stability (growth rate), rad/sec, respectively, to be used if the search option method is to be used
SWEI .	EI	control system ring local bending stiffness about a radial axis perpendicular to its circumferential axis, lb-ft <sup>2</sup>
SWGJ	GJ	control system ring local torsional stiffness about its circumferential axis, lb-ft <sup>2</sup>
SWM	М	mass of the control system ring, lb-sec <sup>2</sup> /ft
SWR	R	control system ring radius, ft

Computer Name	Algebraic Symbol	Definition or Description
T(I)		operational array for passing an associated transfer matrix or discontinuity column into a matrix multiplication subrou- tine and returning the resul- tant matrix
TAU(I)	τ <sub>m</sub>	damping retardation time of the mth articulated blade control rod spring-damper representation, sec
TC(I)		temporary array containing in- termediate aerodynamic terms at an aerodynamic load point for use in the generation of AMA(I)
TEA(I,J,K)	$(\overline{T}_{\mathfrak{m}})_{k}^{i}$	array containing the shifted and unshifted torque for each section of each blade
TEA(I,J)	(T <sub>s</sub> ) i	array containing the shifted and unshifted torque for each support structure section
TEMPN, TEMVY, TEMVZ		temporary parameters for the steady axial, edgewise, and flapwise forces, respectively, acting on the blade and which are updated as each of the sec- tion lumped-parameter charac- teristics are crossed
TEMPT, TEMMY, TEMMZ		temporary parameters for the steady torque, flapwise bending moment, and edgewise bending moment, respectively, acting on the blade and which are updated as each of the section lumped-parameter characteristics are crossed
THC		real part of Theodorsen's co- efficient for unsteady aerody- namics

Computer Name	Algebraic Symbol	Definition or Description
тнск		real part of Theodorsen's co- efficient for unsteady aerody- namics (identical to THC)
THEC(I)	θ <sub>c,m</sub>	one of two angles defining the orientation of the mth flex- strap blade control rod with respect to its reference ro- tating coordinate system, rad
THLD(I)		resulting associated transfer matrix or discontinuity column obtained in multiplication subroutines which is passed back to the calling subroutine by T(I)
TKN	$\left[\overline{\mathbf{T}}_{k,n}\right]$	array representing the contri- bution of all n-frequency- shifted unknowns to all k- frequency-shifted governing equations for a particular value of k and n where placement of data is in string mode by column
TORFLX	1/kd	reciprocal of drive shaft tor- sional stiffness, rad/(ft-lb)
UBX(I,J,K), UBY(I,J,K), UBZ(I,J,K)	$(\overline{ux}_{m})_{k}^{i}, (\overline{uy}_{m})_{k}^{i},$ $(\overline{uz}_{m})_{k}^{i}$	arrays containing the shifted and unshifted radial, edgewise, and flapwise deflections, respectively, for each section of each blade
UBX(I,J), UBY(I,J), UBZ(I,J)	$(\overline{ux}_{s})_{k}^{i}, (\overline{uy}_{s})_{k}^{i},$ $(\overline{uz}_{s})_{k}^{i}$	arrays containing the shifted and unshifted axial, vertical, and lateral deflections, re- spectively, for each support structure section
V(I,J)		radially and azimuthally variant induced velocity distribution array defined by input, ft/sec

Computer Name	Algebraic Symbol	Definition or Description
VELIK		induced velocity at an aero- dynamic load point (radially and azimuthally located) that may be defined by use of V(I,J), if NVI=1; or the blade section inputted induced veloc- ities, ft/sec
VLLX,VLLY, VLLZ		calculated velocities of an aerodynamic load point with respect to the local blade rotating coordinate system x, y, and z axes, respectively, ft/sec
VY(I,J,K), VZ(I,J,K)	$(\nabla \overline{y}_{m})_{k}^{i}, (\nabla \overline{z}_{m})_{k}^{i}$	arrays containing the shifted and unshifted edgewise and flapwise shear forces, respectively, for each section of each blade
VY(I,J) VZ(I,J)	$(\overline{Vy}_{S})_{k}^{i}, (\overline{Vz}_{S})_{k}^{i}$	arrays containing the shifted and unshifted vertical and lateral shear forces, re- spectively, for each support structure
VZERO		calculated resultant velocity acting on an aerodynamic load point, ft/sec
W(I)	$\left[\overline{\mathtt{w}}_{\mathtt{k}}\right]_{\mathtt{s}}^{\mathtt{i}}$	array representing the support structure mass transfer matrix in string mode by row
X(I)		operational array in DCMAT, required for solution of the correction eigenvector
Y(I)		storage array for the inter- mediate terms associated with a section and required for construction section transfer matrices

Computer Name	Algebraic Symbol	Definition or Description
Y(I)		array in DCMAT corresponding to FORCE(I)
YKM'(I,J)		temporary storage array for terms required in specifying the contribution of the con- trol system unknowns to the blade-related governing equations
ZETA	ζ	one of two angles which specify orientation of the helicopter velocity vector with respect to the fixed hub coordinate system, rad

#### USER'S GUIDE

This section of the report describes in detail the input data and its format required for execution of the HASTA computer program and the output which results. As an aid to possible redimensioning of the program for specific applications, the dimension sizes of the arrays contained in the program are presented. A listing of a sample input deck for a flexstrap rotor in forward flight with aerodynamics included is provided. Some of the output produced by use of this input deck is also presented.

#### DIMENSIONS OF COMPUTER ARRAY VARIABLES

The HASTA program in its present form is restricted to the investigation of the aeroelastic stability behavior of coupled rotor/helicopter systems in which the rotor is taken to consist of an arbitrary number of identical blades equally spaced azimuthally. This restriction is due to the dimensions of some of the larger arrays being based upon the use of the blade phasing option, which provides an adequate representation of system behavior without the penalty of higher core requirements and running time. The program coding allows the consideration of identical blades arbitrarily spaced azimuthally if the restrictive array sizes are increased, and provides the basis for program modifications required to represent nonidentical blades. The program coding also allows for use of up to five different aerodynamic data tables. However, the present associated storage array dimensions are such that only one aerodynamic data table can be inputted. To facilitate possible program redimensioning, the dimensions of the HASTA program arrays are presented in terms of program or defining variables in addition to their present (maximum) numerical dimensions. The variables necessary to specify the required array dimension sizes are defined below in a tabular form.

Defining Variable	Definition
MAFA	16*NAEF
MAMB	NAMA*NAERB
MAXN	highest harmonic of control system to

# Defining Variable

# Definition

MCON	<pre>1 - effects of restraint related un- knowns included for flexstrap or bearingless blades, 0 - effects of restraint-related unknowns not in- cluded for flexstrap or bearingless blades</pre>
MCT	<pre>1 - control torque discontinuity con- sidered for articulated blades, 0 - no control torque discontinuity</pre>
MCTY	<pre>1 - bearingless blade, 0 - flexstrap blade</pre>
MFASB	NCSB*MXCPL
MFEA	<pre>l - pitch bearing discontinuity included for articulated blades, 0 - no pitch bearing discontinuity</pre>
MFLAP	<ul> <li>1 - flap hinge discontinuity included for articulated blades, 0 - flap hinge discontinuity not included</li> </ul>
MFLEX	<ul><li>1 - flexstrap or bearingless blades,</li><li>0 - articulated blades</li></ul>
MFUS	<pre>1 - support structure is included, 0 - no support structure</pre>
MLEL	<pre>1 - lead-lag hinge discontinuity in- cluded for articulated blades, 0 - 0 - lead-lag hinge discontinuity not included</pre>
МХСРК	MXCPL*MXCPM
MXCPL	MXSMI*MXSMI
MXCPM	12*NCOLS
MXFAB	NCOLS*MXCPL
MXQ	NRIFC*MXSMI

#### Defining Variable

#### Definition

MXSMI

2\*NHC+1

**MXTKN** 

NRIFC\*NRIFC

MXT2P1

(2\*MAXN+1)\*NSP

NAEF

number of support structure sections having aerodynamic characteristics

included

NAERB

number of radial aerodynamic load points (number of blade sections having aerodynamic characteristics included)

NAMA

34\*MXSMI

NAS

maximum number of azimuthal locations considered for a radial aerodynamic load point in one rotor revolution

NB

number of blades on the rotor;

Note: NB=1 if NBP≠0

NBP

0 - if blade phasing option not to be used; equals the number of blades on rotor if blade phasing option is to

be used

NBSEC

number of blade sections

NCOLS

6

NCSB

1

NDAT\*\*

200+50\* (NBSEC+NFSEC) +NAERB\*NAS

NEBC

MXCPM\*MXSMI

NESMI

MXSMI or MXT2Pl; whichever is larger

in value

<sup>\*\*</sup>NDAT is equivalent to the number of variables in labelled common PLOAD and is set equal to 2800 in subroutine SETUP

## Defining Variable

### Definition

NEI	number of starting eigenvalues
NEIT	number of crossover eigenvalues to be stored during use of search option
NES	number of control system elastic supports
NESBC	12*MXSMI
NFSEC	number of support structure sections
NHC	highest harmonic of system motion to be included for interharmonic coupling - corresponds to Nf
NRBD	NCOLS+3*MCON*MFLEX*(1+MCTY)+(MCT+MFEA+ MFLAP+MLEL)*(1-MFLEX)
NRIFC	MXT2P1+6*MFUS+NB*NRBD
NSD	NSY* (NBSEC+NFSEC)
NSP	<pre>1 - control system to be included, 0 - no control system</pre>
NSY	100
NTAB	number of aerodynamic data sets
NTAL	maximum number of angle of attack values for a Mach number
NTC	maximum number of series representation coefficients
NTM	maximum number of Mach number values for an aerodynamic coefficient table

The dimensions of the arrays involved in the computer program are given by subroutines as follows: where the arrays of each subroutine are grouped by type of variable (i.e.,

integer, real, or complex), an asterisk (\*) following an array variable is used to denote that the variable is in double precision; the letter p following an array variable denotes that the array is involved in the labelled common PLOAD such that any change in dimension size requires modification of the data input format.

Variable	-	Dimensions	Maximum Size
	ACOEFF		
NCC NCLS NMACH	(Integer)	NTAB,3 NTM,NTAB,3 NTAB,3	1,3 11,1,3 1,3
ALPHS AMACH CCS CLDM	(Real)	NTM, NTAL, NTAB, 3 NTM, NTAB, 3 NTC, NTAB, 3 NTM, NTAL, NTAB, 3	11,50,1,3 11,1,3 25,1,3 11,50,1,3
	BAERO		
ACE P AKC P AKE P ATAU P BJE P BLI2 P BTAU P CLESP P CPSI DBS P ECHI P		NES NB NES NB NES NB NB NB NB NB NB NB NAS, 2*MXSMI NB NB	4 6 4 6 4 6 6 6 6 24,6 6
P p PAC p PAK p PHIC p PHIM p PHOTT p PHWTT p SD SI p SMA p SPSI SR p	(Real)	(NBSEC+NFSEC) *50 NES NES NB NB 8 8 NSD NEI NB NAS, 2*MXSMI NEI	2000 4 4 6 6 8 8 4000 5 6 24,6

Variable	•	<u>Dimensions</u>	Maximum Size
STKC p TAC p TAK p TC* THEC p V p Y		NB NES NES 34 NB NAERB, NAS	6 4 4 34 6 25,24 100
AMA*	(Complex)	MAMB	2550

Note: The AMA array is presently initialized to zero in this subroutine by a use of a loop from 1 to 2550, such that if the dimensions of this array are altered, the upper limit of this loop must be modified.

М	(Integer)		

BARRAY

EM	(Integer)	6	6
CX*		75	75
RREAL*	(Real)	144	144
SD		NSD	4000
Y		NSY	100
ALM*		MXQ	63
AMY		NB, NBSEC, MXSMI	1,35,3
AMZ		NB, NBSEC, MXSMI	1,35,3
AN		NB, NBSEC, MXSMI	1,35,3
B*		MXCPK	648
BSAVE*		MXCPK	648
C*		144	144
CTB*		MXFAB	54
CTB1*		MFASB	9
CTB2*		MFASB	9
CTB3*		MFASB	9
CTB4*		MFASB	9
D*		144	144
EPS*		MXQ	63
FAB*		MXFAB	54
FAB1*		MFASB	9
FAB3*		MFASB	9
FAB3*		MFASB	9
FLB*	(Complex)	MXFAB	54

Variable		Dimensions	Maximum Size
FLB1* FLB2* FLB4* FSB* FSB1* FSB2*		MFASB MFASB MFASB MXFAB MFASB MFASB	9 9 9 54 9
FSB3* PHIX PHIY PHIZ R* SHAPE*		MFASB NB,NBSEC,MXSMI NB,NBSEC,MXSMI NB,NBSEC,MXSMI 144 12	9 1,35,3 1,35,3 1,35,3 144
SMLB* SMLBSV* SMLC* SMLCSV* SMLD*		NESBC NESBC NESBC NESBC NESBC	108 108 108 108 108
SMLDSV* SMLE* SMLESV* SMLF* SMLFSV* SMLFSV*		NESBC NESBC NESBC NESBC NESBC NESBC	108 108 108 108 108
SMLGSV* T* TEA UBX UBY		NESBC 72 NB,NBSEC,MXSMI NB,NBSEC,MXSMI NB,NBSEC,MXSMI	108 72 1,35,3 1,35,3 1,35,3
UBZ VY VZ	BEND	NB, NBSEC, MXSMI NB, NBSEC, MXSMI NB, NBSEC, MXSMI	1,35,3 1,35,3 1,35,3
B*	BLARO	NSY 144	100 144
AC* AD* AMA*	(Complex)	144 144 MAMB	144 144 2550

Variable		<u>Dimensions</u>	Maximum Size
	BMASS		
Y	(Real)	NSY	100
A*	(Complex)	144	144
	DCMAT		
ICHG	(Integer)	MXQ	63
A* X* Y*	(Complex)	MXQ,MXQ MXQ MXQ	63,63. 63

Note: When dimensions are changed, change the statement defining NDIM in this subroutine such that NDIM is equal to the magnitude of the variable MXQ, i.e., if MXQ is to be 135, put NDIM=135.

	ELAST		
CX* E* Y	(Real)	75 144 NSY	75 144 100
	EPSOLN		
ALM* EPS* FTEMP* TKN*	(Complex)	MXQ MXQ NRIFC MXTKN	63 63 21 441
	EXCHI		
CSA SNA	(Real)	NES,MXT2P1 NES,MXT2P1	4,24 4,24
	EXPON		
CS SN	(Real)	NB,NESMI NB,NESMI	4,6 4,6
	FAERO		
ACE p		NES	4

<u>Variable</u>		Dimensions	Maximum Size
AFA AKC p AKE p		MAFA NB NES NB	240 6 4 6
ATAU p BJE p BL12 p		NES NB	<b>4</b> 6
BTAU p CLESP p DBS p		NB NB NB	6 6
ECHI p	(Real)	NES	4
P p		(NBSEC+NFSEC) *50	2000
PAC p		NES	4
PAK p PHIC p		NES NB	4
PHIM p		NB	6
PHOTT p		8	8
PHWTT p		8	8
SD		NSD	4000
SI p		NEI	5
SMA p		NB	6
SR p		NEI	5
STKC p		NB	6
TAC p		NES	4
TAK p		NES	4
THEC p		NB	6
V P		NAERB, NAS	25,24
Y		NSY	100

Note: The AFA array is presently initialized to zero in this subroutine by a use of a loop from 1 to 240, such that if the dimensions of this array are altered, the upper limit of this loop must be modified.

	<u>FMASS</u>		
Y	(Real)	NSY	100
W*	(Complex)	144	144
	FUARO		
AFA Y	(Real)	MAFA NSY	240 100

<u>Variable</u>		Dimensions	Maximum Size
C*	(Complex)	144	144
	LOADIN		
T X	(Real)	5 1	5 1
	MAIN		
NBIGMD	(Integer)	NEI	5
AC ACE P ACP ACT AFA AK AKC P AKCI AKE P AKP AKT AL ALSTH AL12 AMKC ARRAY* ATAU P BJE P BL12 P BL12 P BTAU P CLESP P CONV CPSI CS CSA CTAU CX* DBS P DETR DETR2 DMS ECHI P	(Real)	NES NES NES NES MAFA NES NB NB NES NES NES NES NES NB	4 4 4 4 240 4 6 6 6 6 6 6 6 6 6 7 5 24,6 4,6 4,24 6 7 5 6 6 25 25 6

Variable	1	Dimensions	Maximum Size
P P PAC P PAK P PENOM PHIC P PHIM P PHOTT P SD SI P SMA P SMLA SN SNA SPSI SR P STKC P TAC P TAC P TAC P TAC P TAC P TAU THEC P Y		(NBSEC+NFSEC) *50 NES NES NEI NB NB 8 8 NSD NEI NB NB NB,NESMI NES,MXT2P1 NAS, 2*MXSMI NEI NB NES NES NB NB NB NBS NES NB NB NBS NAS NSY	2000 4 4 5 6 6 8 8 4000 5 6 4,6 4,24 24,6 5 6 4 4 6 6 25,24 100
ALM* AMA* EC EC2 EGNS EGNSL* EPS*	(Complex)	MXQ MAMB 25 25 NEI NEI MXQ	63 2550 25 25 5 5
	MLCC2		
R* T* THLD*	(Complex)	144 84 84	144 84 84
	MLRC2		
R*	(Real)	144	144
T* THLD*	(Complex)	84 84	84 84

Variable	_	Dimensions	Maximum Size
	RIGID		
R* Y	(Real)	144 NSY	144 100
	SARRAY		
EE EM	(Integer)	6 6	6 6
RREAL* SD Y	(Real)	144 NSD NSY	144 4000 100
ALM* AMY AMZ AN EPS* PHIX PHIY PHIZ QBAR* R* S* T* TEA UBX UBY UBZ VY	(Complex)	MXQ NFSEC, MXSMI NFSEC, MXSMI NFSEC, MXSMI MXQ NFSEC, MXSMI NFSEC, MXSMI NFSEC, MXSMI 12 144 NEBC 72 NFSEC, MXSMI	63 25,3 25,3 25,3 25,3 25,3 25,3 12 144 216 72 25,3 25,3 25,3 25,3 25,3
	SECPAR		
ACE P AKC P AKE P ATAU P BC BJE P BL12 P BTAU P CLESP P CX*	(Real)	NES NB NES NB 3 NES NB NB NB NB	4 6 4 6 3 4 6 6 6 6

Variable	_	<u>Dimensions</u>	Maximum Size
DBS P ECHI P P P P P PAC P PHIC P PHIM P PHOTT P SA SAT SBT SD SI P SMA P SR P STKC P TAC P TAC P TAK P THEC P Y		NB NES (NBSEC+NFSEC) *50 NES NES NB NB 8 8 3,3 3,3 3,3 NSD NEI NB NEI NB NEI NB NES NES NB NAERB, NAS NSY	6 4 2000 4 4 6 6 8 8 3,3 3,3 3,3 4000 5 6 5 6 4 4 4 6
	SETUP		
AC ACE P ACP ACT AK AKC P AKCI AKE P AKP AKT AL ALSTH AL12 AMKC ATAU P		NES NES NES NES NB NB NB NES NES NES NES NES NES NES NB NB NB	4 4 4 4 6 6 6 4 4 4 6 6 6 6 6 6 6 6 6 6
BJE p BL12 p BTAU p	(Real)	NES NES NB NB	4 4 6 6

Variable		Dimensions	Maximum Size
CLESP p		NB	6
CPSI		NAS,2*MXSMI	24,6
**CS		NB, NESMI	4,6
**CSA		NES,MXT2P1	4,24
CTAU		NB	6
DAT p		NDAT	2800
DBS p		NB	6
DMS		NB	6
ECHI p		NES	4
Pр		(NBSEC+NFSEC) *50	2000
PAC p		NES	4
PAK p		NES	4
PHIC p		NB	6
PHIM p		NB	6
PHOTT p		8	8
PHWTT p		8	8
SIp		NEI	5
SMA p		NB	6
SMLA		NB	6
**SN		NB, NESMI	4,6
**SNA		NES,MXT2P1	4,24
SPSI		NAS,2*MXSMI	24,6
SR p		NEI	5
STKC p		NB	6
TAC p		NES	4
TAK p		NES	4
TAU		NB	6
THEC p		NB	6
V p		NAERB, NAS	25,24
EGNS		NEI	5
AMA*	(Complex)	MAMB	2550

\*\*Note: At present the program in subroutine SETUP determines values of CS and SN arrays for values of the second index up to and including a value of six, and values of CSA and SNA arrays for values of the second index up to and including a value of 24 due to internal numerical definitions of the upper values on two loops. Dimensional modifications involving these arrays requires the internal numerical definitions of the upper values on these two loops to be such that the values for these arrays must be defined at least for values of the second index up to that specified by the dimensional definitions of these arrays.

<u>Variable</u>		Dimensions	Maximum Size
	SOLVE		
DB* EPS* FORCE*	(Complex)	MXQ,MXQ MXQ MXQ	63,63 63 63
	STIFF		
Y	(Real)	NSY	100
SK*	(Complex)	144	144
	SUBMA		
IROWl	(Integer)	6	6
S* TKN*	(Complex)	NEBC MXTKN	216 441
	SUBMB		
IALP IROWC IROW3	(Integer)	6 2 2	6 2 2
CX*	(Real)	75	75
B* CTB1* CTB1* CTB2* CTB3* CTB4* FAB1* FAB1* FAB1* FAB2* FLB1* FLB1* FLB1* FLB2* FSB1* FSB1* FSB2* FSB3*	(Complex)	MXCPK MXFAB MFASB MFASB MFASB MFASB MXFAB MFASB	648 54 9 9 9 9 54 9 9 54 9 9 9 54 9

Variable	1	Dimensions	Maximum Size
SMLB* SMLC* SMLD* SMLE* SMLF* SMLF* SMLG*		NESBC NESBC NESBC NESBC NESBC NESBC MXTKN	108 108 108 108 108 108 441
	SUBMF		
TKN*	(Complex)	MXTKN	441
	SUBMG		
AC AK AKCI AL ALSTH AL12 AL436 AL536 AMKC BJ CTAU CX* DMS SMLA TAU	(Real)	NES NES NB 6,NB NB N	4 4 6 6 6 6 6 6 4 6 7 5 6 6
B* CTB1* CTB2* CTB3* CTB4* FAB1* FAB1* FAB1* FAB1* FAB2*	(Complex)	MXCPK MXFAB MFASB MFASB MFASB MFASB MFASB MXFAB MFASB MFASB MFASB MFASB MFASB MFASB	648 54 9 9 9 9 54 9 9

<u>Variable</u>		Dimensions	Maximum Size
FLB4* FSB* FSB1 FSB2 FSB3 SMLB* SMLC* SMLC* SMLC* SMLG* SMLE* SMLF* SMLF*		MFASB MXFAB MFASB MFASB MFASB NESBC	54 9 9 9 9 108 108 108 108 108 108 441 3,6
	SWA		
AC AK AKCI BJ DMS SMLA TAU	(Real)	NES NES NB NES NB NB	4 4 6 4 6 6 6
TKN* YKM*	(Complex)	MXTKN MXSMI,NB	441 3,4
	SWAPS		
DB*	(Complex)	MXQ,MXQ	63,63
	SWB		
AC AK AKC1 BJ CX* DMS SMLA TAU	(Real)	NES NES NB NES 75 NB NB	4 4 6 4 75 6 6 6
B* CTB*		MXCPK MXFAB	648 54

Variable		Dimensions	Maximum Size
CTB1* CTB2* CTB3* CTB4*		MFASB MFASB MFASB MFASB	9 9 9 9
FAB* FAB1* FAB3* FAB4* FLB* FLB1* FLB2* FLB4* FSB1* FSB2* FSB3* S* SMLC* SMLC* SMLC* SMLC* SMLC* SMLC* SMLC* SMLC*	(Complex)	MXFAB MFASB MEBC NESBC	54 9 9 9 54 9 9 9 54 9 9 216 108 108 108 108 108 108
	TABLU		
NCC NCLS NMACH	(Integer)	NTA,3 NTM,NTA,3 NTA,3	5,3 10,5,3 5,3
ALPHS AMACH CCS CLDM	(Real)	NTM, NTAL, NTA, 3 NTM, NTA, 3 NTC, NTA, 3 NTM, NTAL, NTA, 3	10,15,5,3 10,5,3 25,5,3 10,15,5,3
	TKNS		
TKN*	(Complex)	MXTKN	441
AC		NES	4

<u>Variable</u>		Dimensions	Maximum Size
AK AKCI BJ DMS SMLA TAU	(Real)	NES NB NES NB NB NB	4 6 4 6 6 6
	XNLQ		
AC ACP ACT AK AKCI AKP AKT BJ DMS SMLA TAU	(Real)	NES NES NES NB NES NES NES NES NES NES NB NB	4 4 4 4 6 4 4 4 6 6 6
	ZLN		
AC ACP ACT AK AKCI AKP AKT BJ DMS SMLA TAU	(Real)	NES NES NES NB NES NES NES NES NES NB NB NB	4 4 4 6 4 4 4 6 6 6
	ZTEGI	÷	
B* CTB* CTB1* CTB2* CTB3* CTB4* FAB*		MXCPK MXFAB MFASB MFASB MFASB MFASB MXFAB	648 54 9 9 9 9

<u>Variable</u>		Dimensions	Maximum Size
FAB1*		MFASB	9
FAB3*		MFASB	9
FAB4*		MFASB	9
FLB*	(Complex)	MXFAB	54
FLBl*		MFASB	9
FLB2*		MFASB	9
FLB4*		MFASB	9
FSB*		MXFAB	54
FSB1*		MFASB	9
FSB2*		MFASB	9
FSB3*		MFASB	9
SMLB*		NESBC	108
SMLC*		NESBC	108
SMLD*		NESBC	108
SMLE*		NESBC	108
SMLF*		NESBC	108
SMLG*		NESBC	108
TKN*		MXTKN	441

#### DESCRIPTION OF INPUT DATA

The input required for the computer program consists of values for (1) system model and program logic parameters and, if required, (2) aerodynamic coefficient tables. system model and program logic parameters are inputted directly into a single storage array equivalent to the labelled common PLOAD by specification of their associated array locations and input values. In that all elements of this storage array are initialized to zero when the program is entered, only values for parameters which are non-zero in value need to be read in for the first set of input to be used in a program run. For convenience, the storage array is divided into three parts containing values for specific The array location numbers types of input parameters. 2 - 200 correspond to control parameter input consisting of values for program logic control, flight condition, rotor configuration, and control system parameters. The array location numbers 201 - 2200 correspond to blade and support structure section input consisting of values for the blade and support structure sectional parameters. Array location numbers 2201 - 2800 correspond to values defining a radiably and azimuthally varying induced velocity distribution if this program option is to be used.

The value of parameters represented by the storage array are inputted by use of punched data cards with an I4, I1, 5El4.7 format. The first four columns contain the rightjustified array location number specifying the array location in which the first parametric value on the card is to be stored. The fifth column contains the number of parametric values to be read from the data card (up to five values may be read). The remaining columns, consisting of five fields of 14 columns each, contain consecutive arraylocated parametric values. Thus, columns 6 - 19 contain the parametric value to be stored in the array location specified on the card, columns 20 - 33 contain the parametric value to be stored in the next array location, and so on until the specified number of values to be read are contained on the card. For example, the input of a card punched will set the value of array location 1016 and array location 1017 to 0.01 and 1.57, respectively.

Data cards of the same format are used to denote the end of storage array input for an input case and to terminate the

program execution. In particular, a card with an 8 punched in the fifth column must be placed at the end of the storage array input for each case and a card with a 9 punched in the fifth column must be placed at the end of all input for a run. These cards, in combination with storage array input and aero-dynamic coefficient tables (if required), are used to construct the input for a run. The input for running more than one case in a run is exemplified by the input for two cases per run which has the form:

- 1. Storage array input for Case I
- 2. Card with 8 punched in fifth column
- 3. Aerodynamic tables (if required)
- 4. Storage array input for Case II
- 5. Card with 8 punched in fifth column
- 6. Aerodynamic tables (if required)
- 7. Card with 9 punched in fifth column

The aerodynamic coefficient tables must be included in the input for a case if in the same case the storage array location corresponding to the parameter MAER is to be non-zero.

Since the storage array is only initialized to zero prior to reading storage array input for the first input case, the input for a subsequent case needs only to consist of the data necessary to update the values already in the storage array. For example, if the input parameter values for Case I and Case II of a run are identical except for the helicopter velocity, then the storage array input for Case II consists of a single card, which when read updates the value of the storage array location associated with helicopter velocity to that desired. The remainder of the storage array for Case II is automatically taken as that for Case I. This input procedure of updating the existing storage array reduces drastically the number of input cards that have to be read for additional cases in the same run. The value of a storage array location can also be defined more than once in the storage array input for a case with the last values read being that used for the case. This input capability allows the use of a basic storage array input deck in combination with a correction (update) input deck to construct the input deck for the initial case of a run. The correction deck is added to the end of the basic storage array input deck.

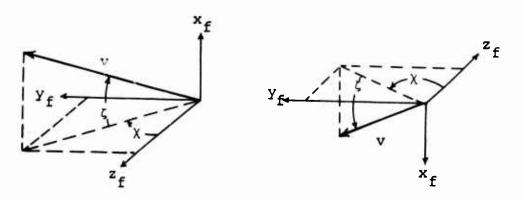
The program storage array input parameters and their associated array location numbers, and also the aerodynamic coefficient table input, are discussed in detail in the following sections. Prior to the generation of input data for a coupled rotor/helicopter system of interest, the inexperienced HASTA program user should be cognizant of the information presented in this report regarding the capabilities of the program, the coupled rotor/helicopter models, and the representational coordinate systems including definitions of various system parameters.

### Control Parameter Input

As mentioned previously, control parameter input information is stored in the first 200 elements of the storage array corresponding to array location numbers 2 - 200. The definition of the specific input information stored in each of these 200 storage array elements is provided on this and the following pages where Loc. is used to denote array location number. Table 2 at the end of this section lists the array location numbers for the storage array elements defined herein and the computer program variables to which they correspond. It is to be noted that although an element of the input data storage array may correspond to a system parameter which is an integer, the value inputted must be provided in decimal form.

- Loc. 2: Rotational speed of the rotor, rad/sec (must always be positive in value)
- Loc. 3: Velocity of sound, ft/sec, is used to determine the Mach number at aerodynamic stations when aerodynamics are included
- Loc. 4: Air density, lb-sec<sup>2</sup>/ft<sup>4</sup>, is used when aerodynamics are included
- Loc. 5: Helicopter velocity, ft/sec
  Note: This is the total velocity at which the
  craft is moving with respect to a stationary
  reference coordinate system

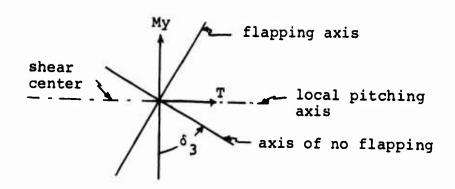
Loc. 6 Two angles  $\chi$  and  $\zeta$ , respectively, in radians, which specify the orientation of the helicopter velocity vector relative to the fixed rotor hub coordinate system as shown in the following sketch for two directions of rotation:



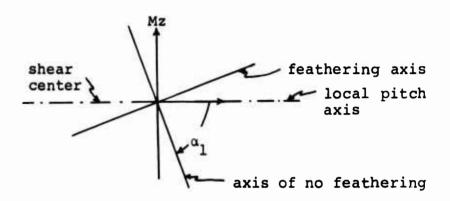
## Counterclockwise Rotation

Clockwise Rotation

- Loc. 8: Real part of Theodorsen's coefficient for unsteady aerodynamics, normally taken equal to 1.0
- Loc. 9: Pitch-flap coupling factor representing pitch-flap coupling for an articulated blade with a flap hinge, if this coupling is not represented through blade modeling, defined as the cot  $\delta_3$  where  $\delta_3$  is the angle between the no-flapping axis and the line perpendicular to the local pitching axis at the flap hinge location as shown in the following sketch



Loc. 10: Pitch-lag coupling factor representing the pitch-lag coupling for an articulated blade with a pitch bearing, if this coupling is not represented through blade modeling, defined as the cot  $\alpha_1$  where  $\alpha_1$  is the angle between the no feathering axis and local pitching axis at the pitch bearing location as shown in the following sketch

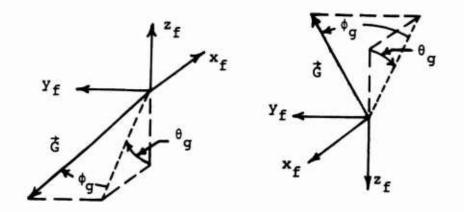


Loc. 11: Collective pitch of the blades, if not included in the blade section pitch angles specified in the sectional input (Locs. seventeen), in radians (the collective pitch value is added to the section pitch angle of each blade section for a flexstrap or bearingless blade, and added to the sectional pitch angle at each blade section outboard of, and including, the blade section at the inboard end of which the pitch bearing is located for an articulated blade). Note: If collective pitch is inputted, care must be taken to insure that the total geometric pitch distribution is that desired. Also, the condition that the blade total geometric pitch must be zero at the inboard end of the blade (shaft-hub interface) and at the pitch control structure-blade attachment point, if a flexstrap or bearingless blade is involved, must be satisfied.

Loc. 12: Gravitational acceleration constant, ft/sec<sup>2</sup>, inputted if gravitational effects are to be included
Note: As discussed in the section pertaining

to coordinate systems, the fixed support structure coordinate system y-axis orientation is dependent on the direction of the gravity field vector if gravitational effects are included.

Loc. 13 and Loc. 14: Two angles  $\theta_g$  and  $\phi_g$ , respectively, in radians, which specify the orientation of the gravity vector relative to the fixed rotor hub coordinate system and are required if gravity effects are to be included. They are depicted in the following sketch for two directions of rotation



Counterclockwise Rotation Clockwise Rotation

- Loc. 15: Logic control parameter, which equals 1.0 if the blade shape vectors relative to the rotor disk plane and the support structure vectors relative to the fixed support structure coordinate system are to be determined in complex variable and polar form; equals 0.0 if these shape vectors are not to be determined
- Loc. 16: Logic control parameter, which equals 1.0 if support structure aerodynamics are to be included and equals 0.0 if support structure aerodynamics are not to be included

  Note: For support structure aerodynamics to be included Loc. 26 (MAER) cannot be 0.0.

- Loc. 17: Number of rotor blades (NB) if the blade phasing option is not to be used, in which case Loc. 18 (NBP) equals 0.0; equals 1.0 if the blade phasing option is to be used Important Note: The present program is dimensioned such that only the blade phasing option can be used to represent rotors having more than one blade. Thus, Loc. 17 must always equal 1.0 for the present version of the HASTA program.
- Loc. 18: Number of rotor blades (NBP) if the blade phasing option is to be used, in which case Loc. 17 (NB) must equal 1.0; equals 0.0 if the blade phasing option is not to be used

  Note: The blade phasing option takes advantage of defined relationships between the motions of the blades, which are assumed identical and equally spaced azimuthally such that core requirements and running time are significantly reduced. To use this option Loc. 18 must be defined as greater than or equal to 2.0 and the assumed relation—ship of blade motions specified by Loc. 65 (NPS).
- Loc. 19: Number of blade sections (NBSEC) representing the blade with a maximum value of 35.0 allowed; NBSEC+NFSEC (Loc. 20) cannot exceed 40.0
- Loc. 20: Number of support structure sections (NFSEC) representing the support structure with a maximum value of 15.0 allowed; NBSEC (Loc. 19) + NFSEC cannot exceed 40.0
- Loc. 21: Logic control parameter (MFLAP), which equals
  1.0 if a flap hinge is to be included for an
  articulated blade and equals 0.0 if a flap hinge
  is not to be included
- Loc. 22: Logic control parameter (MFEA), which equals 1.0 if a pitch bearing is to be included for an articulated blade and equals 0.0 if a pitch bearing is not to be included
- Loc. 23: Logic control parameter (MCT), which equals 1.0 if control torque is to be applied for an articulated blade and equals 0.0 if control torque is not to be applied

- Loc. 24: Logic control parameter (MCON), which equals 1.0 if the restraint applied to the flexstrap or bearingless blade includes the effects of the pitch control structure-related discontinuity unknowns and equals 0.0 if these effects are not to be included

  Note: Normally would be 1.0 if Loc. 25 (MFLEX)=1.0.
- Loc. 25: Logic control parameter (MFLEX), which equals 1.0 if the rotor consists of flexstrap or bearingless blades and equals 0.0 if the rotor consists of articulated blades
- Loc. 26: Logic control parameter (MAER), which equals 1.0 if blade and/or support structure aerodynamics are to be included and equals 0.0 if aerodynamics are not to be included

  Note: For support structure aerodynamics to be included, Loc. 16 (NSK) must also be 1.0.
- Loc. 27: Logic control parameter (NFFB), which equals 1.0 if the first section of the support structure lumped-parameter model is to be considered as unrestrained (free) and equals 0.0 if the first section of the support structure is to be cantilevered (to ground)
- Loc. 28: Number of blade section (NFLAP), counting from the blade tip inboard, at the inboard end of which the flap hinge is to be located for an articulated blade if a flap hinge is to be included; i.e., Loc. 21 (MFLAP) ≠0.0
- Loc. 29: Number of blade section (NFEA), counting from the blade tip inboard, at the inboard end of which the pitch bearing is to be located for an articulated blade if a pitch bearing is to be included; i.e., Loc. 22 (MFEA) \neq 0.0

  Note: Even if Loc. 22 (MFEA) = 0.0, the collective pitch (Loc. 11) is added to the sectional twist distribution of an articulated blade at and outboard of the blade section specified by NFEA.

- Loc. 30: Number of blade section (NCT), counting from the blade tip inboard, at the inboard end of which the control torque application point is to be located for an articulated blade if control torque is to be included; i.e., Loc. 23 (MCT) ≠0.0
- Loc. 31: Number of blade section (NCON), counting from the blade tip inboard, at which the pitch control structure restraint is to be applied to a flex-strap or bearingless blade if the effects of pitch control structure discontinuity unknowns are to be included; i.e., Loc. 24 (MCON) \neq 0.0
- Loc. 32: Logic control parameter (NBC), which specifies the type of blade root conditions at the shaft-rotor hub interface such that a value of 0.0 denotes cantilevered blade root conditions as in the case of an articulated rotor, a value of 1.0 denotes gimballed rotor blade root conditions, and a value of 2.0 denotes teetering rotor blade root conditions
- Loc. 33: Logic control parameter (MFUS), which equals 1.0 if a support structure is to be included and equals 0.0 if a support structure is not to be included

  Note: If a support structure is to be included Loc. 20 (NFSEC) must be 1.0 or greater.
- Loc. 34: Number of aerodynamic load point azimuthal steps in one blade revolution (NAS), used for the blade aerodynamics harmonic computations

  Note: NAS should be an integer multiple of the number of blades on the rotor and must be greater than 2\*NHC (Loc. 35) for the necessary number of harmonics to be determined. However, in that the representative capability of the harmonic analysis is dependent on the number of azimuthal steps, a value of at least 12.0 is recommended.
- Loc. 35: Maximum number of harmonics above and below the primary frequency to be included for interharmonic coupling (NHC)

  Important Note: The program is presently dimensional such that NHC cannot exceed 1.0. The

program should use NHC = 1.0 when the system has a forward velocity and/or an elastic support structure and/or an elastically supported control system. For cases where interharmonic coupling is not possible (simple axisymmetric problem NHC may be set equal to 0.0

- Loc. 36: Logic control parameter (NVI), which equals 1.0 if the radial and azimuthal induced velocity distribution as inputted in Locs. 2201 2800 is to be used, and equals 0.0 if the induced velocity distribution is to be taken from the blade section data (Locs. 201 2200) for each blade section and is assumed to be constant with azimuth
- Loc. 37: Logic control parameter (NSP), which equals 1.0 if control system equations are to be included and equals 0.0 if control system equations are not to be included
- \*\*Loc. 38: Maximum number of harmonics of the control system ring deflection above and below the primary frequency to be included for interharmonic coupling (MAXN)

  Note: If the control system ring is rigid, the value for MAXN need not be more than 1.0. If the control system ring is rigid and supported isotopically, MAXN should still be taken as 1.0 since cyclic deflection of the ring can still occur. Present program dimensions restrict MAXN to 1.0 unless there is either no support structure included (i.e., Loc. 33 (MFUS)=0.0) or no blade discontinuities.
- \*\*Loc. 39: Number of concentrated cyclic spring-damper units supporting the control system ring (NES)(azi-muthal and radial positions and stiffness and damping characteristics for these supports defined in Locs. 89 96 and 109 132)

  Note: Present program dimensions restrict the maximum number of spring-damper support units to no more than 4.

- \*\*Loc. 40: Logic control parameter (MSC), which equals 1.0 if a collective spring-damper unit supporting the control system base plate is to be included, in which case the stiffness and damping characteristics of the spring-damper unit are defined in Locs. 133 134; equals 0.0 if a collective spring-damper unit is not to be included
- \*\*Loc. 41: Mass of the control system ring, lb-sec<sup>2</sup>/ft
- \*\*Loc. 42: Radius of the control system ring, ft
- \*\*Loc. 43: Local torsional stiffness of a segment of the control system ring about its circumferential axis, lb-ft<sup>2</sup>
- \*\*Loc. 44: Local bending stiffness of a segment of the control system ring about a radially oriented axis, lb-ft<sup>2</sup>

- Loc. 45: Effective drive shaft torsional flexibility, rad/(ft-lb), defined as the reciprocal of kd where kd is the torsional stiffness of an effective torsional spring
- Loc. 46: Logic control parameter (NPRS), which equals 1.0 if control parameter input is to be printed as output and equals 0.0 if control parameter input is not to be printed
- Loc. 47: Not used
- Loc. 48: Number of starting eigenvalues
  (NEGN) to be considered for a particular case
  where a maximum of five starting values is
  allowed for a given case
- Loc. 49 Real part (growth rate, rad/sec) of the starting eigenvalues, where the number of array locations Loc. 53: to be defined is specified by Loc. 48 (NEGN) Note: As an example, if Loc. 48 is defined to be 2.0 only Loc. 49 and 50 need to be defined.

<sup>\*\*</sup>Note: If Loc. 37 (NSP) equals 0.0 a control system is not being included. Therefore, the control system information in Locs. 38 - 44 need not be included.

- Loc. 54 Imaginary part (frequency, rad/sec) of the startthru ing eigenvalues where the number of array loca-Loc. 58: tions to be defined is specified by Loc. 48 (NEGN) Note: As an example, if Loc. 48 is to be 2.0, only Loc. 54 and 55 need to be defined.
- Loc. 59: Percentage of a 1-percent increment of starting eigenvalue (IPCT) which is to be used to compute the second trial eigenvalue to be used in the next step in the iteration procedure (recommended value is 50.0, which results in a second trial eigenvalue of 1.005 times the starting eigenvalue)
- Loc. 60: Maximum number of iterations to be performed for each starting eigenvalue (NIT)
- Loc. 61: Number of repeatable significant figures (MER) required in consecutive trial eigenvalues for satisfactory convergence of the iteration procedure for each starting eigenvalue (a value of 7.0 is recommended)

  Note: Whether convergence has actually been obtained can be noted on comparison of the last two eigenvalues and their determinant values and the degree to which the shaft-rotor hub interface conditions are satisfied.
- Logic control parameter (NORM), which equals the Loc. 62: number of the unknown in the unshifted unknowns  $\left\{\overline{q}_{0}\right\}^{*}$  counting from the top, which is to be used as the basis for normalizing the mode shape (i.e., normalized to unity) Mode shapes may be normalized to any unknown expected to be non-zero in value. For normalization based on a specific blade tip unknown being set to unity, NORM = NSP\* (2\*MAXN+1) + 6\*MFUS + the location number of the specific unknown in the blade tip vector. In this expression the first and second terms represent the number of control system and support structure unknowns in the unshifted unknowns vector, respectively. NSP is contained in Loc. 37, MAXN is contained in Loc. 38, and MFUS is contained in Loc. 33. From the above

expression, values of NORM required for normalization based on various blade tip deflections for various system configurations are as shown in Table 1.

TABLE 1.			
VALUES OF NORM FOR NORMALIZATION TO VARIOUS BLADE TIP DEFLECTIONS FOR VARIOUS SYSTEM MODELS			
System	Flapwise	Edgewise	Torsional
Model	Deflection	Deflection	Deflection
MFUS=0, NSP=0		3	2
MFUS=1, NSP=0		9	8
MFUS=0, NSP=1*		4	3
MFUS=1, NSP=1*		10	9

<sup>\*</sup>MAXN taken as zero in value

If MAXN has been taken to have a value of one, the numbers in the last two rows of Table 1 would be increased by two. For normalization based on a support structure tip unknown the expression for NORM is similar to that for a blade tip unknown except that the term 6\*MFUS is not included. Thus, if the system model includes a support structure, MFUS=1, and has a free end, NFFB (Loc. 27)=1, the values of NORM for setting a support structure tip deflection to unity are obtainable by subtracting 6 from the value of NORM required for the same type of blade tip deflection. If the support structure is cantilevered (NFFB=0) the support structure tip unknowns are force and moment unknowns to which the mode shapes can be normalized if desired. It should be noted that the support structure mode shapes, when reactionless blade behavior is assumed can only be obtained if normalization is based on a support structure unknown.

Loc. 63: Logic control parameter (IREM), which equals the number of the unshifted equation to be removed from the matrix procedure to obtain correction values for updating the value of the unknowns (with one unknown being set to unity there is

one equation too many) The value IREM is dependent on the value of NORM (Loc. 62), particularly in the case of uncoupled modes. Basically, the value to take for IREM corresponds to the location number in the unshifted unknowns column vector of an unknown other than that being normalized to, which will also be non-zero in value. For example, if normalization is based on setting the blade tip flapwise deflection to unity, the blade tip flapwise slope will be non-zero such that IREM is taken as NORM + 1. Thus, on this basis, for tip flapwise or edgewise deflections (either blade or support structure) of unity use IREM = NORM + 1 and for a blade tip torsional deflection of unity use IREM = NORM + 5 if blade discontinuity equations are involved. For a blade tip torsional deflection of unity without discontinuity equations or a support structure tip torsion deflection of unity use IREM = NORM - 1. Relationships between NORM and IREM for normalization to support structure tip force or moment unknowns, if the support structure is cantilevered, can be obtained in a similar manner.

Note: If the system model has sufficient modal coupling, all modes except those corresponding to reactionless blade behavior when a support structure is included may be obtained by normalizing the blade tip flapwise deflection to unity. In order to avoid singular matrix difficulties with an articulated rotor using the previous criteria for NORM and IREM, a stiff elastic blade section, even if of short length, should be modeled inboard of the most inboard hinge or bearing of an articulated blade.

- Loc. 64: Logic control parameter (NEX), which has the same value as Loc. 63
- Loc. 65: Logic control parameter (NPS), which denotes the type of blade phasing to be used where 0.0 specifies the blades to be in an umbrella or collective mode, 2.0 specifies a reactionless or scissors mode, 1.0 specifies a forward cyclic mode, and -1.0 specifies a backward cyclic mode Note: The value of NPS is significant only

when the phasing option of the program is to be used; that is, when Loc. 18 (NBP) is non-zero.

- Loc. 66: Logic control parameter (NSCH), which equals 1.0 if the search option is to be used for estimating the starting eigenvalues and equals 0.0 if the search option is not to be used Note: If NSCH = 1, then the real and imaginary parts of the starting eigenvalue for the scanning procedure must be inputted in Loc. 49 and 54, respectively. These input values should represent the beginning of the range within which the starting eigenvalues for the iteration procedure are to be estimated.
- \*\*Loc. 67: Number of steps in growth rate to be considered if the search option is to be used
- \*\*Loc. 68: Number of steps in frequency to be considered if the search option is to be used (should not be greater than 25.0)
- \*\*Loc. 69: Stepsize of the growth rate increment if the search option is to be used
- \*\*Loc. 70: Stepsize of the frequency increment if the search option is to be used

Loc. 71 thru Loc. 76: Angular position,  $\phi_m$ , of the mth blade ahead of the reference blade position (fixed hub coordinate system x-axis) in the direction of rotor rotation at time = 0 for values of m from 1 to NB, sequentially, in radians Note: For a four-bladed rotor with equal azimuthal blade spacing the values for Loc. 71 - 74 would be 0.0,  $\pi/2$ ,  $\pi$ , and  $3\pi/2$ , respectively, assuming  $\phi$  to be 0.0 as is the normal case. When the blade phasing option is being used Loc. 71 must be defined to be 0.0. It is to be noted that due to present program dimensions only one

<sup>\*\*</sup>Note: If Loc. 66 (NSCH) = 0.0, the search option is not specified and the numbers in Locs. 67 - 70 need not be defined. If NSCH = 1, the ranges of growth rate and frequency should be selected such that no more than five starting eigenvalues are obtained.

blade can be considered unless the blade phasing option is used.

- Loc. 77

  thru

  cod attached to the mth blade for values of m

  Loc. 82: from 1 to NB, sequentially, ft/lb (inputted only for rotor systems having articulated type blades for flexstrap bearingless rotors see Locs. 135 140)
- Loc. 83 Damping coefficient to axial stiffness ratio of the form c/k associated with the control rod Loc. 88: attached to the mth blade,  $\tau_m$ , for values of m from 1 to NB, sequentially, sec (inputted only for rotor systems having articulated type blades for flexstraps or bearingless rotors, see Locs. 141 146)
- \*\*Loc. 89 Torsional stiffness of the jth torsional springthru damper unit counteracting local lateral (out of plane) control system ring rotation,  $k\theta_i$ , for Loc. 92: values of j from J. to NES, sequentially, ft-lb/rad Note: At the control system cyclic spring-damper support unit locations specified by Locs. 117 -120, torsional spring-damper units attaching the control system ring to ground such that local lateral ring rotations are restrained can be considered. Specifically, each of these torsional spring-damper units counteracts out-of-plane rotation of the local segment of the ring at their point of attachment about a radially oriented axis thru their point of attachment.
- \*\*Loc. 93 Torsional damping coefficient of the jth torthru sional spring-damper unit counteracting local
  lateral control system ring rotation, c0; for
  values of j from 1 to NES, sequentially,
  ft-lb-sec/rad

<sup>\*\*</sup>Note: If Loc. 37 (NSP) equals 0.0, a control system is not being included, so that the control system information in Locs. 89 - 96 need not be provided.

- Loc. 97 Effective torque arm length of the mth blade thru pitch arm, a<sub>m</sub>, for values of m from 1 to NB, Loc. 102: sequentially, as defined by Equation (8); positive if pitch arm is aft of blade shear center, ft (required only for articulated blades)
- Loc. 103 Rigid offset distance of mth control rod attachthru ment point from the circumferential axis of the Loc. 108: control system ring, d<sub>m</sub>, for values of m from 1 to NB, sequentially, ft (positive if control rod attachment point is located outward from the ring circumferential axis)
- \* \*Loc. 109 Torsional stiffness of the jth torsional springthru damper unit counteracting local control system Loc. 112: ring longitudinal (torsional) rotation,  $k\phi_{\dot{1}}$ , for values of j from 1 to NES, sequentially, ft-lb/rad Note: At the control system cyclic spring-damper support unit locations specified by Locs. 117 -120, torsional spring-damper units attaching the control system ring to ground such that local longitudinal ring rotations are restrained can be considered. Specifically, each of these torsional spring-damper units counteracts torsional rotation of the local segment of the ring at their point of attachment about the local segment's circumferential axis.
- \*\*Loc. 113 Torsional damping coefficient of the jth torthru sional spring-damper unit counteracting local Loc. 116: control system ring longitudinal (torsional) rotation, co, for values of j from 1 to NES, sequentially, ft-lb-sec/rad
- \*\*Loc. 117 Angle specifying azimuthal location of the jth thru control system cyclic spring-damper unit ahead Loc. 120: of the control system fixed coordinate system x-axis in the direction of rotor rotation,  $\chi_j$ , for values of j from 1 to NES, sequentially, radians

- \*\*Loc. 121 Linear stiffness of the jth cyclic springthru damper unit supporting control system ring, k;
  Loc. 124: for values of j from l to NES, sequentially,
  lbs/ft
- \*\*Loc. 125 Damping coefficient of the jth cyclic spring thru damper unit supporting the control system ring,
   Loc. 128: c<sub>j</sub>, for values of j from l to NES, sequentially,
   lb-sec/ft
- \*\*Loc. 129 Rigid offset distance of the jth cyclic springthru damper unit attachment point from the circumLoc. 132: ferential axis of control system ring, b;, for

  values of j from 1 to NES, sequentially, ft
  (positive if cyclic spring-damper unit attachment point is located inward from the ring
  circumferential axis)
- \*\*Loc. 133: Linear stiffness of the collective spring-damper unit supporting the control system base plate, K, lb/ft (required only when Loc. 40 (MSC) = 1.0)
- \*\*Loc. 134: Damping coefficient of the collective springdamper unit supporting the control system base plate, C, lb-sec/ft (required only when Loc. 40 (MSC) = 1.0)
- \*\*Note: If Loc. 37 (NSP) equals 0.0, a control system is not being included such that the control system information in Locs. 93 134 is not required.
  - Loc. 135 Reciprocal of the axial stiffness of the control thru rod attached to the mth blade for values of m Loc. 140: from 1 to NB, sequentially, ft/lb (required for flexstrap and bearingless rotors for rotors having articulated blades, see Loc. 77 82).
  - Loc. 141 Damping coefficient of the spring-damper representation of control rod attached to the mth blade

    Loc. 146: for values of m from 1 to NB, sequentially,

    1b-sec/ft (required for flexstrap and bearingless rotors-for rotors having articulated blades, see

    Locs. 83 88)

- Loc. 147 First of two angles,  $\phi_c$ , (in radians) needed to thru

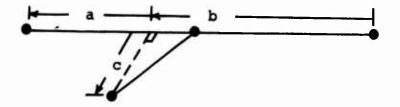
  define the orientation of the control rod of the
- define the orientation of the control rod of the mth flexstrap or bearingless blade with respect to its rotating hub coordinate system at the control rod-control system attachment point required for values of m from 1 to NB, sequentially, and depicted in Figure 16
- Loc. 153 Second of two angles,  $\phi_{\text{C}}$ , (in radians) needed to thru define the orientation of the control rod of the mth flexstrap or bearingless blade with respect to its rotating hub coordinate system at the control rod-control system attachment point required for values of m from 1 to NB, sequen-
- Loc. 159 Perpendicular distance (in feet) from the rotor thru disk plane to the control rod-control system

tially, and depicted in Figure 16

- Loc. 164: attachment point associated with the mth flexstrap or bearingless blade, required for values of m from 1 to NB, sequentially; positive in value if the control rod-control system attachment point is located on the fixed hub coordinate system -z-axis side of the rotor disk plane
- Loc. 165: Structural damping coefficient for the blade structural damping
- Loc. 166: Logic control parameter, which equals 1.0 if all shape vector information determined is to be outputted in punched form (in addition to printed form) and equals 0.0 if no punched shape vector output is to be generated
- Loc. 167: Fore and aft blade cyclic pitch, which equals the value of the blade cyclic pitch (in radians) when the blade is located in the fixed hub coordinate system -y-axis direction, i.e., located aft
- Loc. 168: Lateral blade cyclic pitch, which equals the value of the blade cyclic pitch (in radians) when the blade is located in the fixed hub coordinate system x-axis direction; i.e., located in the reference blade position

- Loc. 169: Logical control parameter (MLEL), which equals 1.0 if a lead-lag hinge is to be included for an articulated blade and equals 0.0 if a lead-lag hinge is not to be included
- Loc. 170: Number of blade section (NLEL) counting from the blade tip inboard, at the inboard end of which the lead-lag hinge is to be located for an articulated blade if a lead-lag hinge is to be included; i.e., Loc. 169 (MLEL) ≠ 0.0
- Loc. 171: Logical control parameter which equals 1.0 if the hlade section mass and inertia-related damping effects on the system behavior are not to be included and equals 0.0 if these damping effects are to be included Note: Normally a value of 0.0 would be used.
- Loc. 172: Logical control parameter (MCTY) used in conjunction with MFLEX (Loc. 25) = 1.0 such that when equal to 0.0 a flexstrap rotor system is to be considered and when equal to 1.0 a bearingless rotor system is to be considered Note: When MFLEX (Loc. 25) = 1.0, MCON (Loc. 24) is normally defined to be 1.0
- Loc. 173: Length of torque tube pitch control structure spur or extension shaft, ft, which is required for a bearingless rotor system
- Loc. 174: Flapwise bending stiffness of the torque tube pitch control structure spur about its local coordinate system y-axis, lb-ft<sup>2</sup>, which is required for a bearingless rotor system
- Loc. 175: Edgewise bending stiffness of the torque tube pitch control structure spur about its local coordinate system z-axis, lb-ft<sup>2</sup>, which is required for a bearingless rotor system
- Loc. 176: Steady blade torque (COE1) at the pitch control structure-blade attachment point not removed by the pitch control structure, ft-lb (applicable for articulated blades not having a pitch bearing, for flexstrap blades, and for bearing-less blades)

Loc. 177: An effective distance (COE2) which is used in conjunction with COEl (Loc. 176) to define the steady flapwise shear force acting on the blade as a result of the steady blade torque removed by the pitch control structure, ft (applicable to same blades specified for Loc. 176) Note: To provide clarification to the definition of this system parameter the following discussion is provided. In the case of a torque tube pitch control structure lying in the rotor disk plane, as depicted in the following sketch, the value of COE2 can be defined as equal to c (a+b)/a where, as depicted, c is the perpendicular distance from the control rod-pitch arm attachment point to the torque tube axis, a is the distance along the torque tube axis from the dropped perpendicular to the spur spherical bearing, and b is the distance along the torque tube axis from the dropped perpendicular to the torque tube-blade attachment point. This definition of COE2 is based on the torsional and



flapwise moment equilibrium equations about the torque tube axis and the spherical bearing, respectively. The above definition of COE2 is valid for a pitch arm oriented toward the blade leading edge if c is taken to have a negative value and for the dropped perpendicular intersecting the torque tube axis inboard of the spur spherical bearing if a is taken to be negative. For a torque tube pitch control structure not lying in the rotor disk plane the distances required can be determined from the projection of the three attachment points onto the disk plane.

In the case of an articulated or flexstrap rotor, a and b go to zero such that COE2 is equal to c.

- Loc. 178: Percentage of steady blade torque (COE3) in decimal form (i.e., less than 1.0) not removed by the pitch control structure in the case of an articulated blade having a pitch bearing (normally would be 0.0 in value for a frictionless pitch bearing)
- \*\*Loc. 179: Length of the flexstrap blade pitch arm along its coordinate system x-axis if Loc. 172 (MCTY) = 0.0 and length of the torque tube (from blade attachment point to pitch arm attachment point) if Loc. 172 (MCTY) = 1.0, ft
- \*\*Loc. 180: Product of Young's modulus and the average cross-sectional area (EA) of the flexstrap blade pitch arm if Loc. 172 (MCTY) = 0.0 and product of Young's modulus and the average cross-sectional area of the torque tube if Loc. 172 (MCTY) = 1.0, 1b
- \*\*Loc. 181: Flapwise bending stiffness of the flexstrap blade pitch arm about its coordinate system y-axis if Loc. 172 (MCTY) = 0.0 and of the torque tube about its coordinate system y-axis if Loc. 172 (MCTY) = 1.0, 1b-ft<sup>2</sup>
- \*\*Loc. 182: Edgewise bending stiffness of the flexstrap blade pitch arm about its coordinate system z-axis if Loc. 172 (MCTY) = 0.0 and of the torque tube about its coordinate system z-axis if Loc. 172 (MCTY) = 1.0, 1b-ft<sup>2</sup>
- \*\*Loc. 183 Three angles;  $\alpha$ ,  $\beta$ , and  $\gamma$ , respectively, (in thru radians) which define the orientation of the Loc. 185: flexstrap blade pitch arm (Loc. 172 (MCTY) = 0.0) or torque tube (Loc. 172 (MCTY) = 1.0) relative to the rotating hub coordinate system as depicted in Figure 12

<sup>\*\*</sup>Note: If a flexstrap or bearingless rotor is not to be considered the information of Locs. 179 - 185 is not needed.

Loc. 186: Torsional stiffness (GJ) of the torque tube if a bearingless rotor is to be considered, lb-ft<sup>2</sup>

Loc. 187: Length of bearingless blade pitch arm along its coordinate system x-axis, ft

Loc. 188 Not used thru
Loc. 190:

Loc 191 Three angles, a' 8'.

Loc. 191 Three angles,  $\alpha$ ,  $\beta$ , and  $\gamma$ , respectively, (in thru radians) which define the orientation of the Loc. 193: bearingless blade pitch arm relative to the torque tube coordinate system as depicted in Figure 13

Loc. 194: Not used

Loc. 195 Perpendicular distance (in feet) from the rotor thru disk plane to the mth bearingless blade spheri-Loc. 200: cal bearing-spur attachment point for values of m from 1 to NB, sequentially, and is positive in value if the spherical bearing is located on the fixed hub coordinate system -z-axis side of the rotor disk plane

	TABLE 2. CONTROL PARAMETER INPUT LOCATIONS						
					AM VARIA		
Loc.	program symbol	Loc.	program symbol	Loc.	program symbol	Loc.	program symbol
0002	ОМ	0030	NCT	0064	NEX	0135-	AMKC(I)
0003	SDVEL	0031	NCON	0065	NPS	0140	I=1,NB
0004	AIRD	0032	NBC	0066	NSCH	0141- 0146	CTAU(I) I=1,NB
0005	FVEL	0032		lt .		0147-	PHIC(I)
1			MFUS	0067	IG	0152	I=1,NB
0006	CHI	0034	NAS	0068	IF	0153- 0158	THEC(I) I=1,NB
0007	ZETA	0035	NHC	0069	STG	0159-	AL12(I)
0008	THC	0036	NVI	0070	STF	0164	I=1,NB
0009	PFC	0037	NSP	0071-	, ,	0165	SDCO
0010	PLC	0038	MAXN	0076 0077-	I=1,NB AKCI(I)	0166	PUNI
0011	COLL	0039	NES	0082	I=1,NB	0167	CYFA
0012	AG	0040	MSC	0083- 0088	TAU(I) I=1,NB	0168	CYLA
0013	GT	0041	SWM	0089-	AKT (J)	0169	MLEL
0014	GP	0042	SWR	0092 0093-	J=1,NES ACT(J)	0170	NLEL
0015	NPD	0043	SWGJ	0096	J=1,NES	0171	DACO
0016	NSK	0044	SWEI	0097- 0102	SMLA(I) I=1,NB	0172	MCTY
0017	NB	0045	TORFLX	0103-	DMS(I)	0173	AEXT
0018	NBP	0046	NPRS	0108 0109-	I=1,NB AKP(J)	0174	EYEX
0019	NBSEC	0047	not used	0112	J=1,NES	0175	EZEX
0020	NFSEC	0048	NEGN	0113- 0116	ACP(J) J=1,NES	0176	COEl
0021	MFLAP	0049-	SR(I),	0117-	ECHI(J)	0177	COE2
0022	MFEA	0053	I=1,NEGN SI(I),	0120 0121-	J=1,NES	0178	COE3
0023	MCT	0058	I=1,NEGN	0124	J=1,NES	0179-	PHOTT(I)
0024	MCON	0059	IPCT	0125-		0186 0187-	I=1,8
0025	MFLEX	0060	NIT	0128 0129-	J=1,NES BJ(J)	0194	PHWTT(I) I=1,8
0026	MAER	0061	MER	0132	J=1,NES	0195-	ALSTH(I)
0027	NFFB	0062	NORM	0133	CAPK	0200	I-1,NB
0028	NFLAP	0063	IREM	0134	CAPC		
0029	NFEA						

### Blade/Support Structure Section Input

As mentioned earlier, location numbers 201 - 2200 contain section input for blade and support structure sections. Each section has 50 locations associated with it. Thus, locations 201 - 250 are associated with the first section, locations 251 - 300 with the second section, and so on. The maximum number of sections is 40 and the 40th section would be associated with locations 2151 - 2200. However, it is not necessary that this many sections be used and in such case the locations corresponding to unused sections would be left with values of 0.0 as initialized by the program.

The order in which the particular sections are taken is very important. Section number 1 is always at the blade tip, section number 2 is the next inboard section on the blade, and so on until the hub section is reached. most inboard blade section corresponds to the rotor hub. The number of this section by definition is equal to The next section, number NBSEC+1, always is the first section of the support structure. This is the support structure section furthest from the rotor hub (at the support structure tip). This section is also allowed to have either free or cantilevered end conditions at its end most distant from the rotor hub. The next section, number NBSEC+2, is the next most distant section of the support structure, and so on. This numbering order continues until section number NBSEC + NFSEC is reached, which corresponds to the last section of the support struc-The total section data for all sections is placed in the storage array such that the section data is stored in the single array P(2000) of the labelled common PLOAD. Thus, each section is not denoted by an independent program name.

The definitions of the 50 input locations associated with each blade or support structure section are provided in the following discussion. In addition, for the more experienced HASTA program user these input locations and their corresponding mathematical symbols are given in Table 3 at the end of this discussion of section input data.

As described previously, each general section (blade or support structure) may consist of concentrated mass and

inertia, aerodynamics, torsional spring-damper units, an elastic section with centrifugal stiffening or localized elastic restraint (this localized elastic restraint is used for only one particular section for a flexstrap or bearingless rotor), bends in shear center axis and/or a rotation of local coordinates to account for blade twist and collective pitch, and rigid offsets in the shear center axis. Of the 50 locations provided for each section, the first seven are the section control indicators; M1, M2, M3, M4, M5, M6, and M7. Each of these control indicators specifies whether or not a particular transfer matrix is to be used for the section. The section control indicators and their related transfer matrices are as follows:

Location	Parameter	Related Transfer Matrix
one	Ml	Concentrated Mass and Inertia
two	M2	Bend
three	мз	Aerodynamics
four	M4	Elastic Section
five	<b>M</b> 5	Rigid Offset
six	М6	Torsional Stiffness
seven	м7	Elastic Restraint (for flexstrap or bearingless rotors only)

It is to be noted that the alpha location number used here is with regard to the position in the block of 50 locations given to each section. This convention will be followed throughout the remainder of this discussion. In using the control indicator a value of 0.0 indicates that the particular transfer matrix will not be used. For a blade section a control indicator value of 1.0 specifies that the particular transfer matrix is to be used. For a support structure section, a value of 2.0 specifies that the particular transfer matrix is to be used. For example, a blade section may have a concentrated mass and an elastic

length associated with it. Thus, M1 and M4 for that section would have a value of 1.0. If, in addition, the section includes aerodynamics, then M3 would be 1.0. The remaining values for M2, M5, M6, and M7 would be 0.0. For a support structure section with mass, an elastic length, and aerodynamics, the values of M1, M4, and M3 should be 2.0 and the values of M2, M5, M6, and M7 would be 0.0.

In developing the input values for the seven control indicators, there are two sets of special conditions. Only one set of conditions is in regard to the use of M7. blade section is allowed to have a non-zero value for M7 and all other control indicators for this section should be 0.0. Thus, a bend transfer matrix should be used in the next outboard section to align the local blade coordinate system of the section having non-zero M7 with the rotating hub coordinate system, as required in the program. A further condition is that the blade section having a non-zero value for M7 must be that specified by NCON (Loc. 31) if MCON (Loc. 24) equals 1.0. A support structure section is not allowed to have a non-zero value for M7. The second set of conditions is in regard to the first blade section (section number 1) and the first support structure section (section number NBSEC+1) when a support structure is included. These two sections must consist of only mass and inertia properties. Thus, only Ml can be non-zero for these two sections.

Of the remaining section array locations (locations eight thru fifty), locations fifteen thru seventeen must be defined for every section; whether or not other locations must be defined is dependent on the values for the section control indicators. This dependency is given below.

If a section has a non-zero Ml, locations eight thru fourteen for that section must be defined (only non-zero numbers need to be inputted).

If a section has a non-zero M2, no additional locations other than locations fifteen thru seventeen must be defined.

If a section has a non-zero M3, locations ten, eleven, and eighteen thru twenty-four must be defined.

If a section has a non-zero M4, locations twenty-five thru twenty-nine must be defined.

If a section has a non-zero M5, locations thirty-eight thru forty must be defined.

If a section has a non-zero M6, locations forty-four thru fifty must be defined.

If a blade section has a value of 1.0 for M7, no additional information other than that provided in array locations 2 thru 200 is required.

The various section properties and corresponding locations are described in the following:

Loc. Lumped mass of section, m, lb-sec<sup>2</sup>/ft eight:

Loc. Offset of the section center of gravity in nine: the local section y-axis direction from the local x-axis (shear center axis),  $\varepsilon_{ry}$ , ft (e.g., positive for a blade section if cg is forward of the local x-axis)

Loc. x-coordinate of the origin of the local ten: blade or support structure section coordinate system in the rotating hub or fixed support structure coordinate system as depicted in Figure 9 for a blade section, h<sub>rx</sub>, ft

Loc. y-coordinate of the origin of the local eleven: blade or support structure section coordinate system in the rotating hub or fixed support structure coordinate system as depicted in Figure 9 for a blade section, h.... ft

<sup>n</sup>ry, ft

Loc. Local blade or support structure section twelve: polar mass moment of inertia I, lb-sec2-ft

Loc. Local blade or support structure section thirteen: flapwise mass moment of inertia I, lb-sec<sup>2</sup>-ft

Loc. fourteen:

Local blade or support structure section edgewise mass moment of inertia I<sub>z</sub>, lb-sec<sup>2</sup>-ft

Note: The mass moments of inertia are with respect to axes passing thru the section center of gravity and parallel to the local section coordinate system axes.

Section locations fifteen thru seventeen are angles which describe the orientation of the local blade or support structure section coordinate system with respect to the rotating hub or fixed support structure coordinate system. These have been discussed in detail in the section of this report pertaining to coordinate systems and are depicted in Figure 10.

Loc. fifteen:

Local blade or support structure section lead-lag angle,  $\phi$ , positive for a right-handed presweep rotation about the reference coordinate system z-axis (for a blade, the outboard end of the section forward), rad

Loc. sixteen:

Local blade or support structure section coning angle,  $\theta$ , positive for a right-handed precone rotation about the preswept reference coordinate system y-axis (for a blade, the outboard end of the section in the -z-axis direction), rad

Loc. seventeen:

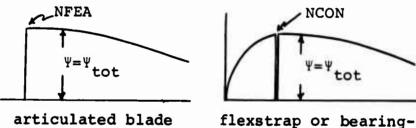
Local blade or support structure section pitch angle, \( \mathcal{Y} \), positive for a right-handed rotation about the preswept and preconed reference coordinate system x-axis (for a blade, leading edge up), rad

Note: The value read for a blade section can be taken as the total local section pitch angle (collective + twist contribution) with the collective pitch value of Loc. 11 equal to 0.0 or can be taken as only the local twist contribution. In the latter case this value is superimposed on the collective value of Loc. 11 in a manner dependend on the MFLEX (Loc. 25) and NFEA (Loc. 24) values (see Loc. 11). The twist contribution should include steady twist due to blade loads. As examples of the possibilities for the determination of Y input values,

Loc. 11 = 0.0 and Loc.  $11 \neq 0.0$  cases can be considered for articulated and flexstrap or bearingless blades. If Loc. 11 is 0.0 then the value of  $\Psi$  for a section should be inputted as the total of collective and twist contribution at the section such that the  $\Psi$  distribution over the blade span might be as shown in the following sketch, where NFEA (Loc. 24) and NCON (Loc. 31) denote location of pitch bearing and flexstrap or bearingless pitch control structure restraint respectively.

# Loc. 11 = 0.0

less blade



But if a collective input,  $\Psi_{\text{coll}}$ , is used, then the  $\Psi$  for each section should be defined by utilizing the expression  $\Psi = \Psi_{\text{tot}} - \Psi_{\text{coll}}$  each section, as depicted in the following sketch where  $\Psi$  of a section, if other than zero, is negative.

Loc. 11 =  $\Psi_{\text{coll}}$ NFEA

Vecoll

articulated blade

flexstrap or bearingless blade

It should be noted that at the flexstrap or bearingless pitch control structure restraint location,  $\Phi$ ,  $\Theta$ , and  $\Psi_{\text{tot}}$  must be zero for consistency with the pitch control structure restraint representations.

Section locations eighteen thru twenty-four describe the aerodynamics of the section and need not be inputted if M3 = 0.0

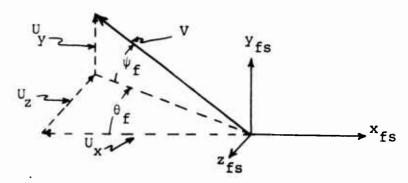
Loc. eighteen:

Aerodynamic table number (MTAB) which denotes the aerodynamic coefficient table to be used to determine the lift, drag, and moment coefficients and their slopes as a function of angle of attack and Mach number for this particular section The aerodynamic coefficient tables Note: are discussed in further detail in the presentation of their input. Basically, the program was developed to use up to five different spanwise airfoil shapes. representation of any of these shapes may involve the use of table look-up or analytical expressions for nonlinear aerodynamic coefficients. Thus, for a blade section, MTAB may equal any number from 1 to 5. However, for a support structure section, MTAB may also be equal to 6 and 7, where for MTAB = 6, the aerodynamic section is a NACA 0012 airfoil and for MTAB = 7, flatplate crossflow aerodynamics are used. Due to present program dimensions only one aerodynamic coefficient table corresponding to MTAB equal to 1 can be used. These dimensional restrictions can be easily removed if more than one set of aerodynamic coefficient data must be used. These dimensional restrictions do not affect the use of MTAB = 6 or 7.

Loc. nineteen:

Effective aerodynamic length of the blade or support structure section, La, ft

Locations twenty and twenty-one are required for a support structure sections only. These are the two angles which describe the velocity of the helicopter with respect to the fixed support structure coordinate system, as depicted in the following sketch.



Loc. twenty:

 $\psi_f$  = arcsin (U<sub>y</sub>/V) where U<sub>y</sub> is the climb rate and V is the resultant velocity of the helicopter, rad

Loc. twenty-one:

 $\theta_f$  = arctan  $(U_z/U_x)$  where  $U_z$  is the lateral velocity and  $U_x$  is the forward velocity of the helicopter, rad

Note:  $U_X$  is positive if the helicopter is moving forward (negative  $x_{fs}$  direction),  $U_Y$  is positive if the helicopter is climbing (positive  $y_{fs}$  direction), and  $U_Z$  is positive if the helicopter is moving laterally to the starboard (negative  $z_{fs}$  direction). In such case that V is zero, both  $\psi_f$  and  $\theta_f$  are indeterminant. In this case input these angles as zero. Similarly, if  $U_X = U_Z = 0$ , but V is not zero (i.e.,  $U_Y = V$ ) then input  $\psi_f = +\pi/2$  if  $U_Y$  is positive and  $\psi_f = -\pi/2$  if  $U_Y$  is negative. In either case input  $\theta_f$  as zero.

Loc. twenty-two:

Distance that the blade or support structure section shear center axis is forward of mid-chord along the local coordinate system y-axis,  $\delta$ , ft

Loc. twenty-three:

Chord length of the blade or support structure section, c, ft

Loc. twenty-four:

Local induced velocity of the blade section, v<sub>i</sub>, ft/sec (not required for a support structure section)

Note: This induced velocity needs to be inputted only when the control parameter NVI (Loc. 36) is 0.0. If NVI is greater than zero, the induced velocity as a function of radial and azimuthal position of the blade section inputted in locations 2201 - 2800 is used.

Locations twenty-five thru twenty-nine must be defined if M4 is non-zero.

Loc. twenty-five:

A parameter used in combination with the centrifugal force acting on a section to specify the centrifugal stiffening effects on the torsional stiffness of a flexible strap or beam section inboard of the flexstrap or bearingless pitch control structure restraint application; defined as the effective value of .5  $(EI_v + EI_z)A_s/(I_f+I_c)$ (in pounds) for the section where  $EI_{v}$  and EI, are the section flapwise and edgewise bending stiffness, respectively, A is the total cross-sectional area of the section, and  $I_f$  and  $I_c$  are the flapwise and edgewise area moments of inertia, respectively Note: Only required for sections in which this effect is significant. Not required for a support structure section.

Loc. twenty-six:

Elastic length of the blade or support structure section, L, ft

Loc.

Local blade or support structure section twenty-seven: torsional stiffness, EI, lb-ft2

Loc.

Local blade or support structure section twenty-eight: flapwise bending stiffness, EI, lb-ft2

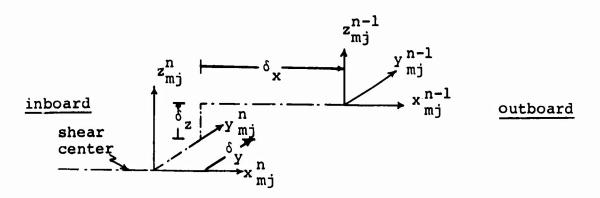
Loc. twenty-nine: Local blade or support structure section edgewise bending stiffness, EI, lb-ft2

Loc. thirty: Centrifugal force acting on the blade section that is estimated inside the program using mass distribution and rotational

speed, and for output purposes is stored in this location, lb (no input needed)

Locations thirty-one thru thirty-seven are not used.

Locations thirty-eight thru forty need only be described if M5 is non-zero. The pertinent parameters are depicted in the following sketch for a blade section where n and n-l superscripts denote a local coordinate system inboard and outboard of the rigid offset characteristics, respectively.



Loc. Rigid blade or support structure section thirty-eight: shear center axis offset in the local coor-

dinate system x-axis direction,  $\delta_{x}$ , ft

Loc. Rigid blade or support structure section thirty-nine: shear center axis offset in the local coordinate system y-axis direction,  $\delta_v$ , ft

Loc. Rigid blade or support structure section forty: shear center axis offset in the local coordinate system z-axis direction,  $\delta_z$ , ft

Locations forty-one thru forty-three are not used.

Locations forty-four thru fifty, which pertain to consideration of localized torsional spring-damper units in the blade or support structure section, need be described only when M6 is non-zero. Also, locations forty-four thru forty-nine cannot be defined non-zero if location fifty is non-zero.

Loc. forty-four:

Inverse of the localized torsional spring-damper unit stiffness about the local sec-

tion coordinate system x-axis,

 $K_{x}^{-1}$ , rad/(ft-lb)

Loc. forty-five:

Inverse of the localized torsional springdamper unit stiffness about the local sec-

tion coordinate system y-axis,

 $K_v^{-1}$ , rad/(ft-lb)

Loc. forty-six:

Inverse of the localized torsional spring-damper unit stiffness about the local sec-

tion coordinate system z-axis,

 $K_z^{-1}$ , rad/(ft-lb)

Loc. forty-seven:

Damper time constant (c/k) associated with the localized torsional spring-damper unit acting about the local section coordinate system x-axis,  $\tau_{\rm x}$ , sec

Loc. forty-eight:

Damper time constant (c/k) associated with the localized torsional spring-damper unit acting about the local section coordinate system y-axis,  $\tau_{_{\rm U}}$ , sec

Loc.
forty-nine:

Damper time constant (c/k) associated with the localized torsional spring-damper unit acting about the local section coordinate system z-axis,  $\tau_z$ , sec

Loc. fifty:

Control system spring constant, K<sub>s</sub>, which may be used to represent the applied control torque as a linear function of local torsional rotation. (However, use of the previously described representations of the control system effects are recommended instead)

TABLE 3. SECTION DATA INPUT LOCATIONS AND CORRESPONDING SYMBOLS								
Location	Symbol	Location	Symbol	Location	Symbol			
x* + 0001	Ml	x + 0018	MTAB	x + 0035	<b>†</b>			
x + 0002	M2	x + 0019	La	x + 0036	not used			
x + 0003	мз	X + 0020	Ψf	X + 0037				
X + 0004	M4	X + 0021	θf	X + 0038	δ <sub>x</sub>			
x + 0005	м5	X + 0022	δ	X + 0039	δ y			
x + 0006	М6	X + 0023	С	X + 0040	δ z			
x + 0007	м7	X + 0024	v <sub>i</sub>	X + 0041	<b>^</b>			
x + 0008	m	x + 0025	<sup>GJ</sup> cs	X + 0042	not used			
x + 0009	ε <sub>ry</sub>	X + 0026	<sup>L</sup> e	X + 0043				
x + 0010	h <sub>rx</sub>	X + 0027	EIx	X + 0044	K <sub>x</sub> -1			
x + 0011	h <sub>ry</sub>	X + 0028	EIy	X + 0045	K <sub>y</sub> -1			
X + 0012	ı,	X + 0029	EIz	X + 0046	K <sub>z</sub> <sup>-1</sup>			
x + 0013	I <sub>y</sub>	x + 0030	P <sub>T</sub>	X + 0047	τx			
X + 0014	Iz	X + 0031	<b>↑</b>	X + 0048	τ			
X + 0015	Φ	X + 0032	not	X + 0049	τz			
x + 0016	Θ	x + 0033	used	x + 0050	Ks			
x + 0017	Ψ	x + 0034	+					

<sup>\*</sup>X represents the last data input location of the previous section which is factorable by 50.

## Optional Induced Velocity Distribution Input

The computer program can use a rotor induced velocity distribution which varies both azimuthally and radially, determined by use of an independent analysis, instead of a radially varying distribution inputted through blade section data. The use of this optional induced velocity distribution is controlled by the parameter NVI (Loc. 36). If the value of this array location is equal to 1.0 this optional induced velocity distribution is used and must be defined for Locations 2201 - 2800. This set of induced velocities is stored in the array V(25,24) in common block The first index of this array corresponds to blade aerodynamic section number (radial position), and the second index corresponds to the azimuthal position of the The blade aerodynamic section numbers are determined in the same manner as the blade section numbers except only blade sections having aerodynamic characteristics included are counted. The induced velocity values for each aerodynamic blade section are those occurring at the radial position of the aerodynamic load (lumped mass) point on the section.

The induced velocities are inputted for each radial aerodynamic section going from the blade tip section to the most inboard blade aerodynamic section, while maintaining a fixed blade azimuthal position. Then, the induced velocities are inputted for each radial aerodynamic section, taken in the same order as above, at a fixed blade azimuthal position one azimuthal step in the direction of rotor rotation ahead of the previous azimuthal position. This process is repeated until the induced velocities at each blade aerodynamic section (radial position) and blade azimuthal position have been defined. Due to the dimensions of the induced velocity storage array, 25 input locations corresponding to aerodynamic radial position are reserved for each azimuthal position of the blade and up to 24 blade azimuthal positions are allowed, which are equally spaced azimuthally. The azimuthal blade positions allowed are dependent on the value of the control input parameter NAS (Loc. 34) and defined by  $\psi_k = 2\pi (1-1)/NAS$ is the kth azimuthal blade position, in radians. This azimuthal blade position is defined relative to the fixed hub coordinate system x-axis (reference blade position) and k is an integer having values of 1 through

NAS. Thus, location numbers 2201 - 2225 are associated with the blade azimuthal position denoted by  $\psi_1$ , location numbers 2226 - 2250 are associated with the blade azimuthal position denoted by  $\psi_2$ , and so on.

In general, the location number for the induced velocity of the nth aerodynamic radial position at the kth blade azimuthal location is defined as 2200 + 25(k-1) + n. Since k cannot be greater than NAS and n cannot be greater than the number of blade aerodynamic sections, the largest location number to be defined would be 2200 + 25(NAS-1) + the number of aerodynamic sections.

It should be noted that if the induced velocity distribution to be used does not vary azimuthally but is either uniform or only varies radially, this distribution can be more conveniently inputted by the definition of  $v_i$  (location twenty-four of the blade section data) with the logic control parameter NVI equal to 0.0.

## Aerodynamic Coefficient Input

The airfoil aerodynamic coefficient data is to be included for a case only when the control parameter MAER (corresponding to location 26) of the case is equal to 1 and must be included after the number 8 card following the storage array data for the case. This data, if required, is inputted with an entirely different format than that utilized for the previously discussed storage array data.

The aerodynamic coefficient data for an airfoil shape can consist of any of three types, corresponding to the form of representation to be used to determine the aerodynamic coefficients. The first type consists of data describing aerodynamic coefficients in a tabular form for a lower and upper range of angle of attack values, and of data defining coefficients to be used in a series representation of aerodynamic coefficients for angles of attack between the two tabular data ranges. For example, tabular data may be provided for angle of attack values of 0 to 20 degrees and 350 to 360 degrees, with series coefficient data provided for angle of attack values between 20 to 350 degrees. second type consists of only data defining coefficients to be used in a series representation of the aerodynamic coefficients of a symmetrical airfoil. The third type consists primarily of aerodynamic coefficient data in the C-81 computer program form.

Initially, the input data required for the first and second type of aerodynamic coefficient representation is presented. This is followed by a detailed discussion of the series representation used in both of these types of aerodynamic coefficient representation. The input data required for the third type of representation is then briefly discussed in regard to the modifications required, in that the C-81 aerodynamic table format has been fully documented elsewhere (e.g., Reference 3). All aerodynamic coefficient input is read in and stored in common block COEFFS for later use in subroutine ACOEFF.

Although the HASTA program is presently limited to the consideration of only one set of aerodynamic coefficient data due to dimensional restrictions, the program was developed to consider up to five different sets of aerodynamic coefficient data. Thus, the construction of the aerodynamic data described below will be based on five different sets:

First Card - Format 1415

NTAB, a number from one to five defining the number of airfoil aerodynamic coefficient data sets to be inputted.

Note: The following cards are included for each set of aerodynamic coefficient data.

Card #1 - Format 1415

ISER, a control parameter such that if equal to 0, the aerodynamic coefficient data consisting of both tabular and series coefficient data (corresponding to the first type of data) is to be inputted; if equal to 1, aerodynamic coefficient data consisting of only series coefficient data (corresponding to the second type of data) is to be inputted; and if equal to 81, aerodynamic coefficient data based on the C-81 aerodynamic table format is to be inputted (corresponding to the third type of data).

<sup>3.</sup> Davis, John M., ROTORCRAFT FLIGHT SIMULATION WITH AERO-ELASTIC ROTOR AND IMPROVED AERODYNAMIC REPRESENTATION, Volume II - User's Manual, Bell Helicopter Company; USAAMRDL-TR-74-10B, Eustis Directorate, US Army Air Mobility Research and Development Laboratory, Fort Eustis, Virginia, June 1974, AD 782756

Note: As an example, if aerodynamic coefficient data set number two is designated to read in only the series coefficients of the second type (i.e., ISER = 1), then any aerodynamic section with its section input variable MTAB (corresponding to location eighteen) = 2 will use the series representation with the inputted coefficients for determination of lift, drag, and moment coefficients.

#### Card # 2 - Format 1415

MT, a number from one to five assigned to this set of aerodynamic coefficient data to distinguish it from other sets such that the input between this card and the next ISEK card is associated with a data set designated by the number MT.

Note: Due to present program dimensional restrictions, MT must = 1.

An aerodynamic coefficient data set is constructed of the data necessary for the determination of the two-dimensional lift, drag, and moment coefficients about quarter chord (i.e., about a point on the airfoil chord located 1/4 chord-length aft of the leading edge of the airfoil). The data necessary for each of these three types of two-dimensional coefficients is presented in the following discussion in the required order of input. The data for each type of two-dimensional coefficient is constructed independent of the other two-dimensional coefficients.

#### Lift Coefficient Data:

Card #3.1 = Format 1415

NCCl (equivalent to NCC(MT,1)), number of series coefficients for lift coefficient determination where if ISER = 0 a value of 15 is required and if ISER = 1 a value of 20 is required

Cards #3.la - Format 5El4.7 (more than one card)

CCS(K,MT,1) for K = 1, NCC1, coefficients (constants) of the series representations for determination of lift coefficients (dependent on type of series to be used) such that Cols. 1-14 Cl<sub>1</sub>, the first constant 15-28 Cl<sub>2</sub>, the second constant 29-42 Cl<sub>3</sub>, the third constant 43-56 Cl<sub>4</sub>, the fourth constant 57-70 Cl<sub>5</sub>, the fifth constant

Next card

Cols. 1-14 Cl<sub>6</sub>, the sixth constant 15-28 Cl<sub>7</sub>, the seventh constant etc., until Cl<sub>NCCl</sub> has been reached where the form Cl<sub>k</sub> has been used to denote CCS(K,MT,1)

Note: Cards #3.2, etc., are not inputted if ISER = 1.

Card #3.2 - Format 1415

NMACHS (equivalent to NMACH(MT,1)), the number of Mach numbers involved in the lift coefficient table where NMACHS cannot be greater than 11

Card #3.2a - Format 7F10.0 (may be more than one card)

AMACH(K,MT,1) for K = 1, NMACHS, values of Mach numbers for the construction of the lift coefficient table such that

Cols.  $1-10~M_1$ , lowest Mach number  $11-20~M_2$ , next highest Mach number  $21-30~M_3$ , next highest Mach number  $31-40~M_4$ , next highest Mach number  $41-50~M_5$ , next highest Mach number etc., until  $M_{\rm NMACHS}$  has been reached where  $M_{\rm K}$  has been used to denote AMACH(K,MT,1) Note: The value of  $M_1$  should be zero and the highest Mach number should be equal to 1.0.

#### Card #3.3 - Format 14I5

NCL (equivalent to NCLS(1,MT,1)) - first index being the Mach number index), the number of angles of attack (with corresponding lift coefficients) for Mach number M<sub>1</sub> where NCL cannot be greater than 50 for any Mach number

Card #3.3a - Format 7F10.0 (may be more than one card)

ALPHS(1,K,MT,1) for K = 1, NCL - first index being the Mach number index, values of angles of attack, deg, for the first Mach number such that

Cols. 1-10  $\alpha_1$ , first angle of attack for  $M_1$  11-20  $\alpha_2$ , second angle of attack for  $M_1$  21-30  $\alpha_3$ , third angle of attack for  $M_1$  31-40  $\alpha_4$ , fourth angle of attack for  $M_1$  etc., until  $\alpha_{NCL}$  has been reached

where  $\alpha_K$  has been used to denote ALPHS(1,K,MT,1) Note: Normally the angle of attack distribution is such that it represents a lower and an upper range of angle of attack with a series representation utilized between the two ranges.

Card #3.3b - Format 7F10.0 (same number of cards as Card #3.3a)

CLDM(1,K,MT,1) for K = 1, NCL - first index being the Mach number index, values of the lift coefficient for the first Mach number and each angle of attack such that

Cols. 1 - 10 CL<sub>1</sub>, lift coefficient at  $M_1$ ,  $\alpha_1$  11 - 20 CL<sub>2</sub>, lift coefficient at  $M_1$ ,  $\alpha_2$  21 - 30 CL<sub>3</sub>, lift coefficient at  $M_1$ ,  $\alpha_3$  31 - 40 CL<sub>4</sub>, lift coefficient at  $M_1$ ,  $\alpha_4$  etc., until CL<sub>NCL</sub> has been reached

where  $CL_K$  has been used to denote CLDM(1,K,MT,1)

Card #3.4, Card #3.4a, and Card #3.4b are the next set of input cards; they are similar to Card #3.3, Card #3.3a, and Card #3.3b, respectively, except that the input numbers are those corresponding to M<sub>2</sub>.

Similar sets of cards are added corresponding to M<sub>3</sub> thru M<sub>NMACHS</sub> to complete the lift coefficient data required to construct an aerodynamic coefficient data set. It is not necessary to have the same number of or values of angles of attack for each Mach number, since NCL is read for each Mach number. However, the angle of attack defining the upper end of the lower angle of attack range and the angle of attack defining the lower end of the upper angle of attack range should be the same for all Mach numbers used in constructing an aerodynamic coefficient table, (e.g., lift coefficient table).

#### Drag Coefficient Data:

Input for the drag coefficient data is carried out in the same fashion as that for the lift coefficient data. Thus,

#### Card #4.1 - Format 1415

NCC1 (equivalent to NCC(MT,2)), the number of series coefficients for drag coefficient determination where if ISER = 0 a value of 10 is required and if ISER = 1 a value of 7 is required

Card #4.la - Format 5El4.7 (more than one card)

CCS(K,MT,2) for K = 1, NCC1, coefficients (constants) of the series representations for the determination of drag coefficients (dependent on type of series to to used)

Note: Cards #4.2, etc., for the drag coefficient table are not inputted if ISER = 1.

#### Card #4.2 - Format 1415

NMACHS (equivalent to NMACH(MT,2)), the number of Mach numbers involved in the drag coefficient table where NMACHS cannot be greater than 10

Card #4.2a - Format 7F10.0 (may be more than one card)

AMACH(K,MT,2) for K = 1, NMACHS, values of Mach numbers for the construction of the drag coefficient table where  $M_1$  should be zero and the highest Mach number should be 1.0

#### Card #4.3 - Format 1415

NCL (equivalent to NCLS (1,MT,2)) - first index being the Mach number index), the number of angles of attack (with corresponding drag coefficients) for Mach number M<sub>1</sub> where NCL cannot be greater than 15 for any Mach number

Card #4.3a - Format 7F10.0 (may be more than one card)

ALPHS(1,K,MT,2) for K = 1, NCL - first index being the Mach number index, values of angles of attack, deg, for the first Mach number

Card #4.3b - Format 7F10.0 (may be more than one card)

CLDM(1,K,MT,2) for K=1, NCL - first index being the Mach number index, values of the drag coefficients for the first Mach number and each angle of attack

Cards 4.3, 4.3a, and 4.3b are followed by similar sets of cards with values corresponding to drag coefficient table Mach numbers  $\rm M_2$  thru  $\rm M_{NMACHS}$  to complete the drag coefficient data required to construct an aerodynamic coefficient data set.

#### Moment Coefficient Data:

Input of the moment coefficient data is carried out in the same manner as that for the lift coefficient data or the drag coefficient data. These cards may be numbered starting with Card #5.1. For the moment coefficient data, if ISER = 0 a value of 22 is required for the NCCl card and if ISER = 1 a value of 16 is required. The moment coefficient data must correspond to the data necessary to define the two-dimensional moment coefficient about quarter chord (i.e., about a point on the airfoil chord line located a distance of 1/4 of a chordlength aft of the airfoil leading edge).

The construction of the preceding data completes the input necessary for the first data set, which is designated as the MTth set of aerodynamic coefficient data by the number inputted for MT.

The input of the next set of aerodynamic coefficient data (if NTAB>1) must be constructed in the same fashion as that given for the previous data set, starting with input for variable ISER, followed by input for MT, NCC(MT,1), ..... etc. The same procedure is repeated for the third, fourth, and fifth sets of data, if required. Thus, additional sets of data would be inputted in the form represented below.

Aerodynamic Coefficient Data Set No. 2 (Include only if NTAB>2):

Cards #6 Data set type card (either ISER = 0 or ISER = 1)

Cards #7 Data set identification card (MT = any number from 1 - 5 that has not been used for the other data sets)

Cards #8 Lift coefficient data

Cards #9 Drag coefficient data

Cards #10 Moment coefficient data

Aerodynamic Coefficient Data Set No. 3 (Include only if NTAB>3):

Cards #11 Data set type card (either ISER = 0 or ISER = 1)

- Cards #12 Data set identification card (MT = any number from 1 5 that has not been used for the other data sets)
- Cards #13 Lift coefficient data
- Cards #14 Drag coefficient data
- Cards #15 Moment coefficient data

Aerodynamic Coefficient Data Set No. 4 (Include only if NTAB>4):

- Cards #16 Data set type card (either ISER = 0 or ISER = 1)
- Cards #17 Data set identification card (MT = any number from 1 5 that has not been used for the other data sets)
- Cards #18 Lift coefficient data
- Cards #19 Drag coefficient data
- Cards #20 Moment coefficient data

Aerodynamic Coefficient Data Set No. 5 (Include only if NTAB = 5):

- Cards #21 Data set type card (either ISER = 0 or ISER = 1)
- Cards #22 Data set identification card (MT = any number from 1 5 that has not been used for the other data sets)
- Cards #23 Lift coefficient data
- Cards #24 Drag coefficient data
- Cards #25 Moment coefficient data

The series coefficients required for an aerodynamic coefficient data set are dependent upon the type of representation being utilized to determine the two-dimensional lift, drag, and moment coefficients and their slopes about airfoil quarter chord. For the first type of representation (tables plus series), ISER = 0, a series representation is utilized if the angle of attack  $\alpha$  is not in the ranges represented by the tabular data. For the second type of representation, ISER = 1, a series representation is always used. The various coefficients (constants) required for each of these series representations is presented in the following discussion where  $\text{Cl}_{K}$ ,  $\text{C2}_{K}$ , and  $\text{C3}_{K}$  correspond to lift, drag, and moment series constants, respectively.

Lift Coefficient Series Representation (ISER = 0):

This representation is used when the condition  $\text{Cl}_1 < \alpha < \text{Cl}_2$  is satisfied, where  $\text{Cl}_1$ , which must be  $\geq 0$ , is the maximum value of the angle of attack, deg, for which the lower angle of attack range of the lift coefficient tabular data can be used and  $\text{Cl}_2$  is the minimum value of the angle of attack, deg, for which the upper angle of attack range of the lift coefficient tabular data can be used. If the maximum value of the angle of attack

be used. If the maximum value of the angle of attack in the lower range of the tabular data is not the same for all Mach numbers of the table, then the lowest maximum angle of attack defining the lower angle of attack range of all Mach numbers must be used for Cl<sub>1</sub>.

Similarly, if the minimum value of the angle of attack in the upper range of the tabular data is not the same for all Mach numbers, then the highest minimum angle of attack defining the upper angle of attack range of all Mach numbers must be used for Cl<sub>2</sub>.

As an aid to defining in series form the lift coefficient as a function of angle of attack  $\alpha$ , two intermediate functions can be defined. These functions are in general form:

$$L1(x) = C1_3 + C1_4x + C1_5x^2 + C1_6x^3 + C1_7x^4$$

$$L2(x) = C1_8 + C1_9x + C1_{10}x^2$$

Then, the series representation for the two-dimensional lift coefficient CL for various ranges of angle of attack is defined as:

CL = 
$$\text{Cl}_{11}\text{Ll}(\alpha)$$
 for  $\text{Cl}_{1}<\alpha \le 90^{\circ}$   
CL =  $\text{Cl}_{12}\text{Ll}(\alpha)$  for  $90^{\circ}<\alpha \le 160^{\circ}$   
CL =  $\text{Cl}_{12}\text{L2}(\alpha)$  +  $\text{Cl}_{13}(\alpha-160)/20$  for  $160^{\circ}<\alpha \le 180^{\circ}$   
CL =  $\text{Cl}_{14}\text{L2}(\Delta)$  +  $\text{Cl}_{13}(200-\alpha)/20$  for  $180^{\circ}<\alpha \le 200^{\circ}$   
CL =  $-\text{Cl}_{14}\text{Ll}(\Delta)$  for  $200^{\circ}<\alpha \le 270^{\circ}$   
CL =  $-\text{Cl}_{15}\text{Ll}(\Delta)$  for  $270^{\circ}<\alpha < \text{Cl}_{2}$   
where  $\Delta = 360^{\circ} - \alpha$ .

Drag Coefficient Series Representation (ISER = 0):

This representation is used when the condition  $C2_1 < \alpha < C2_2$  is satisfied, where the  $C2_1$  and  $C2_2$  angles, deg, are based on the upper and lower angle of attack limits of the lower and upper angle of attack ranges for the drag coefficient tabular data, respectively, in the same manner as the  $C1_1$  and  $C1_2$  angles were determined. As an aid to defining in series form the drag coefficient as a function of the angle of attack  $\alpha$ , two intermediate functions can be defined. These functions in a general form are:

D1(x) = 
$$C2_3 + C2_4x + C2_5x^2 + C2_6x^3 + C2_7x^4$$
  
D2(x) =  $C2_8 + C2_9x + C2_{10}x^2$ 

The series representation for the two-dimensional drag coefficient CD for various ranges of angle of attack is defined as:

CD = D1(
$$\gamma$$
1) for C2<sub>1</sub>< $\alpha \le 90^{\circ}$   
CD = D1( $\gamma$ 2) for 90°< $\alpha \le 166^{\circ}$   
CD = D2( $\alpha$ ) for 166°< $\alpha \le 180^{\circ}$ 

$$CD = D2(\Delta) \qquad \text{for} \quad 180^{\circ} < \alpha < 194^{\circ}$$

CD = D1(
$$-\gamma$$
2) for 194°< $\alpha$ <270°

CD = D1(
$$\gamma$$
3) for 270° $\leq \alpha < C2_2$ 

where

$$\gamma 1 = \alpha + (15 - C2_1)(90-\alpha)/(90-C2_1)$$

$$\gamma 2 = 180 - \alpha$$
, and

$$\gamma 3 = 360 - \alpha - (345-C2_2)(\alpha-270)/(C2_2-270)$$
.

Moment Coefficient Series Representation (ISER = 0):

This representation is used when the condition  $\text{C3}_1 < \alpha < \text{C3}_2$  is satisfied where the  $\text{C3}_1$  and  $\text{C3}_2$  angles, deg, are based on the upper and lower angle of attack limits of the lower and upper angle of attack ranges for the moment coefficient tabular data, determined in the same manner as the  $\text{Cl}_1$  and  $\text{Cl}_2$  angles were determined. As an aid to defining in series form the moment coefficient about airfoil quarter chord as a function of the angle of attack, five functions can be defined. These functions in a general form are:

$$M1(x) = C3_{3}(30-x)/14 + C3_{4} + C3_{5}x + C3_{6}x^{2} + C3_{7}x^{3}$$

$$M2(x) = C3_{8} + C3_{9}x + C3_{10}x^{2} + C3_{11}x^{3} + C3_{12}x^{4}$$

$$M3(x) = C3_{13} + C3_{14}x + C3_{15}x^{2} + C3_{16}x^{3}$$

$$M4(x) = C3_{17} + C3_{18}x + C3_{19}x^{2} + C3_{20}x^{3} + C3_{21}x^{4}$$

$$M5(x) = C3_{22}(\alpha - 330)/(C3_{2} - 330) - C3_{4} - C3_{5}x$$

$$- C3_{6}x^{2} - C3_{7}x^{3}$$

The series representation for the two-dimensional moment coefficient about the airfoil quarter chord for various ranges of angle of attack is then defined as:

CM = M1(
$$\alpha$$
) for C3<sub>1</sub>< $\alpha \leq 30^{\circ}$ 

$$CM = M2(\alpha) \qquad \text{for} \qquad 30^{\circ} < \alpha \le 150^{\circ}$$

$CM = M3(\alpha)$	for	150°<α <u>&lt;</u> 168°
$CM = M4(\alpha)$	for	168°<α <u>&lt;</u> 180°
$CM = -M4(\Delta)$	for	180° <a<192°< td=""></a<192°<>
$CM = -M3(\Delta)$	for	192° <u>&lt;</u> α<210°
$CM = -M2(\Delta)$	for	210° <u>&lt;</u> α<330°
$CM = M5(\Delta)$	for	330° <u>&lt;</u> α <c3<sub>2</c3<sub>

For the first type of aerodynamic coefficient representation (tabular plus series form) the angle of attack  $\alpha$  has the units of degrees, and the coefficients required in the series representation are based on this fact. For the second type of aerodynamic coefficient representation, the angle of attack  $\alpha$  has the units of radians in regard to the symmetrical airfoil series representation and, thus, the series coefficients for this type must be based on this fact. In addition to the condition that ISER = 1 for the second type (series only), the value of  $\text{Cl}_1$  must be less than zero.

If the combination of ISER = 1 and Cl  $_1 \geq 0$  is used, the program will terminate execution. Since a symmetrical airfoil is being represented, only the expressions for the lift, drag, and moment coefficients about quarter chord for  $\alpha$  between 0 and  $\pi$  radians are required to define the necessary constants. If  $\alpha$  is greater than  $\pi$  the aerodynamic coefficients are determined using the expressions, with  $\alpha$  being redefined as  $2\pi\text{-}\alpha$  and the sign changed on the two-dimensional aerodynamic coefficients, as required.

Lift Coefficient Representation (ISER = 1, Cl<sub>1</sub><0):

As an aid to defining the lift coefficient the following terms can be defined:

$$SQT = \sqrt{1-M^2}$$

$$LL = Cl_2(1-M)(1+Cl_3)$$

$$LM_1 = [(1-M)Cl_8 + (Cl_9M + Cl_{10})\alpha]/(Cl_{11} + Cl_{12}M)$$

$$LM_2 = (Cl_{13}\sin\alpha + Cl_{14}\sin2\alpha + Cl_{15}\sin3\alpha + Cl_{16}\sin4\alpha)$$

where M is the Mach number. The term LL, with  $\text{Cl}_3 = 0$ , is the angle in radians at which the lift coefficient curve normally becomes nonlinear. The purpose of  $\text{Cl}_3$  is to

allow extension of the normal range of linear aerodynamics to a higher angle of attack. The representation for the two-dimensional lift coefficient for various angle of attack ranges is defined as:

CL = 
$$\text{Cl}_7 \alpha/\text{SQT}$$
 for  $0 \le \alpha \le \text{LL}$   
CL =  $\text{LM}_1/\text{SQT}$  for  $\text{LL} \le \alpha \le \text{Cl}_4$   
CL =  $\text{LM}_2/\text{SQT}$  for  $\text{Cl}_4 \le \alpha \le \text{Cl}_5$   
CL =  $(\text{Cl}_{17} + \text{Cl}_{18} \alpha)/\text{SQT}$  for  $\text{Cl}_5 \le \alpha \le \text{Cl}_6$   
CL =  $(\text{Cl}_{19} + \text{Cl}_{20} \alpha)/\text{SQT}$  for  $\text{Cl}_6 \le \alpha \le \pi$ 

Drag Coefficient Representation (ISER = 1, Cl<sub>1</sub><0):</pre>

As an aid to defining the drag coefficient the following terms can be defined:

$$DM_1 = C2_3 + C2_4 \cos \alpha + C2_5 \cos 2\alpha + C2_6 \cos 3\alpha + C2_7 \cos 4\alpha$$

The representation for the two-dimensional drag coefficient for various angles of attack ranges is defined as:

$$CD = C2_1 + C2_2\alpha^2 \quad \text{for} \quad 0 \le \alpha \le LL$$

$$CD = DM_1/SQT \quad \text{for} \quad LL < \alpha < \pi$$

Moment Coefficient Representation (ISER = 1, Cl<sub>1</sub><0):

As an aid to defining the moment coefficient the following terms can be defined:

$$MM_{1} = C3_{6}(C3_{7} - (\alpha + C3_{8})/C3_{9})$$

$$MM_{2} = C3_{1}\sin\alpha + C3_{2}\sin2\alpha + C3_{3}\sin3\alpha + C3_{4}\sin4\alpha$$

$$- .25(LM_{2}\cos\alpha + DM_{1}\sin\alpha)$$

where the first four terms of the last expression above define the moment coefficient about midchord. The representation for the two-dimensional moment coefficient for various angles of attack ranges is defined as:

CM = 0 for 
$$0 \le \alpha \le C1_4$$
  
CM = MM<sub>2</sub>/SQT for  $C1_4 < \alpha \le C1_5$   
CM = C3<sub>5</sub>/SQT for  $C1_5 < \alpha \le C1_6$   
CM = MM<sub>1</sub>/SQT for  $C1_6 < \alpha \le \pi$ 

For this type of aerodynamic coefficient representation the lift, drag, and moment coefficient slopes are normally determined by use of analytical expressions obtained by taking the derivative of the expressions for the two-dimensional aerodynamic coefficients with respect to  $\alpha$ , such that additional constants are not required to define the slopes. However, this is not the case for the moment coefficient slope for  $\text{Cl}_4 < \alpha < \text{Cl}_5$  where the moment coefficient

expression directly uses the values obtained for CL and CD for the lift and drag contribution to the moment coefficient about quarter chord. In this case, the moment coefficient slope expression, which is obtained by taking the derivative with respect to  $\alpha$  of the moment coefficient expression with the lift and drag coefficient effects represented in series form, requires the definition of additional constants. These constants can be defined in terms of previously defined constants as:

$$C3_{10} = C3_{1} - C1_{14}/2 - C2_{3}/4 - C2_{5}/4$$

$$C3_{11} = 2C3_{2} - C1_{13}/4 - 3C1_{15}/4 - C2_{4}/4 - C2_{6}/4$$

$$C3_{12} = 3C3_{3} - C1_{16} - C2_{7}/4$$

$$C3_{13} = 4C3_{4}$$

$$C3_{14} = 3(C1_{14} + C2_{5})/4$$

$$C3_{15} = C1_{15} + C2_{6}$$

$$C3_{16} = 5(C1_{16} + C2_{7})/4$$

The modification required to the C-81 format aerodynamics data table for use in the HASTA program is discussed below. Initially, the table identification card and the title and control card are removed from an existing C-81 data deck such that only a basic lift coefficient table, drag coefficient table, and a moment coefficient table (in that order) remain. Six cards must be added to the front of the resulting C-81 deck. These are, in terms of previously defined data cards,

- First Card Format 1415 (NTAB)
- Card #1 Format 1415 (ISER)
- Card #2 Format 1415 (MT)
- 4. Card #3.1 Format 1415 (NCC1)
- 5. Card #3.la Format 5E14.7 (CCS(K, MT,1))
- 6. Card #3.2 Format 1415 (NMACHS, NCL)

which must be added in the order listed. For C-81 format tables ISER (Card #1) must be equal to 81. The First Card and Card #2 are as previously defined. NCCl (Card #3.1) is defined equal to 2 and CCS (1, MT, 1) and CCS (2, MT, 1) (Card #3.la) are defined equal to 180.0 and -180.0, respectively, corresponding to the highest and lowest angle of attack included in the lift coefficient table. integer values corresponding to the number of Mach numbers involved in the lift coefficient table and the number of angles of attack involved in the same table, in the order mentioned, must be provided on Card #3.2 instead of the previously defined value. After the last card of the lift coefficient table but before the first card of the drag coefficient table, three cards must be added in the following order: Card #4.1 (NCC2), Card #4.1a (CCS (1, MT, 2), CCS (2, MT, 2)), and Card #4.2 (NMACHS, NCL). These three cards are identical in concept to Cards #3.1, #3.1a, and #3.2 except that they are defined in regard to the drag coefficient table. In fact, NCC2 must be defined as 2 and CCS (1, MT, 2) and CCS (2, MT, 2) must be defined as 180.0 and -180.0, respectively. Similarly, after the last card of the drag coefficient table but before the first card of the moment coefficient table, three cards containing NCC3; CCS (1, MT, 3) and CCS (2, MT, 3); NMACH and NCL must be added. These are defined as 2; 180.0 and -180.0;

the number of Mach numbers involved in the moment coefficient table and the number of angles of attack involved in the same table, respectively.

If more than one C-81 data set is to be used the additional sets would be constructed in the same manner but without the First Card, which contains NTAB, and added to the back of the first set. In fact, the three different types of aerodynamic coefficient representations can be utilized for one case by noting that the departure path of input generation is initiated at Card #1 (ISER).

#### DESCRIPTION OF PROGRAM OUTPUT

The output obtained from the execution of the program is dependent upon the type of run, the type of data included in the input deck, and the program options activated by the various input parameters. This output may consist of both printed and punched output. For purposes of discussion the output can be divided into several basic output groups, which are discussed individually in the following sections. Each of these groups may not be outputted or may have various parts which may or may not be outputted depending on the values used for the input parameters. The dependency of output on input parameters is also presented in the discussion of the various output groups.

The general sequence in which the basic output groups are outputted (overall output flow) for a general computer run can be represented by the following steps where the output is in printed form unless otherwise noted:

- 1. Output of storage array data
- 2. Output of program control parameters
- 3. Output of aerodynamic coefficient tables
- 4. Output of sectional aerodynamic coefficients and steady loads
- 5. Output of section data
- 6. Output of search option information, if used
- 7. Output of iteration scheme steps

- 8. Shape vector output (printed)
- 9. Shape vector output (punched)
- 10. Output groups 7, 8, and 9 are repeated for each additional starting eigenvalue inputted or obtained from use of the search option for the first system configuration (case) of a computer run
- 11. Output specified by 1 10 is repeated for each additional system configuration (case) of a computer run

where output groups 1 - 9 are the basic output groups that will be discussed in the following sections.

## Output of Storage Array Data

The first numerical output for a case of a run consists of the printout of the basic input deck, which defines values for variables of the 2800-element storage array. output is preceded by a title heading, PRINTOUT OF INPUT DATA, and by column headings of the form LOC NUM VAL1 VAL2 VAL 3 VAL4 VAL5. The numerical printout of all storage location input cards follows this last heading in the same order in which they are read. Each printed line consists of the initial storage array location number (under LOC), the number of variable values on the card to be read (under NUM), and up to five variable values, depending on the value of NUM (under VAL1, VAL2, VAL3, VAL4, and VAL5, as required). The variable values are printed in a 5 (Gl4.5,4X) format to aid in the determination of whether or not these values are properly aligned on the input cards.

The main reason for this output is to allow the input data to be easily checked to ascertain whether or not all of these data cards are properly punched. It should be noted that number 8 and number 9 punched control cards are not included in this output. For cases in a run other than the first case, this output may be short since only a few modification cards may need to be inputted.

### Output of Program Control Parameters

The next group of output for a case of a run, which may be printed, is that pertaining to the program control parameters. The output of this group is preceded by the heading, HELICOPTER AEROELASTIC STABILITY ANALYSIS INPUT PARAMETERS, and consists of one page of output. This output is not printed if the input number in Location 46 (corresponding to NPRS) of the control parameter input is equal to 0.0.

The first four lines of this output contain the values of various important integer parameters. The first line prints out the parameters NB, NBP, NBSEC, NFSEC, NBC, NHC, NFFB, and NAS - corresponding to the input in Locations 17, 18, 19, 20, 32, 35, 27, and 34, respectively. It should be noted that the integer parameters are obtained by truncation of the corresponding input numbers in floating point form. The second line contains the values of parameters NFLAP, NFEA, NCT, NCON, NES, MAXN, and FUA - corresponding to the input in Locations 28, 29, 30, 31, 39, 38, and 16, respectively. Also in this line, the value of parameter NSY which is always equal to 100 - is printed. The next two lines provide the values of parameters NEGN, IPCT, NIT, MER, NORM, IREM, NEX, NPS, IG, IF, NLEL and MCTY - corresponding to input in Locations 48, 59, 60, 61, 62, 63, 64, 65, 67, 68, 170, and 172, respectively.

The next four lines of this output give the general description of the rotor configuration being considered. This output is self-explanatory, in that 17 short statements, which can be thought of as questions regarding the configuration, are followed by "yes" or "no" answers. For example, if ARTICULATED SYS NO is printed, the configuration has a flex-strap or bearingless rotor system with or without the effect of constraint unknowns included - depending on whether CONSTRAINT APP is followed by YES or NO, respectively. The "yes" or "no" answers are based upon particular input parameters. For example: BLADE PHASING YES corresponds to NBP input (in Location 18) being non-zero; DISK PLAN CALC YES corresponds to NPD (input in Location 15) being non-zero; and COLL SPRING IN is followed by YES when the input in Location 40 (MSC) is 1.0.

The statements answered by YES or NO are FLAP HINGE, CONTROL TORQUE EQ, PITCH BEARING, ARTICULATED SYS, CONSTRAINT

APPlied, FUSELAGE, BLADE PHASING, AERODYNAMICS, GIMBALLED SYSM., VARIABLE OUTPUT, DISK PLANE CALCUlations, FUSELAGE AERO., SWASHPLATE IN, COLLective SPRING IN, VI (induced velocity) DISTribution USED, SEARCH OPTION, SHAPE PUNCHED, and LEAD-LAG HINGE. Lower case letters contained above have been added for clarification of the statements and are not included in the output. It should be noted that GIM-BALLED SYSM. YES corresponds to either a gimballed or a teetering rotor system, with the specific type determined by the value printed for NBC.

The next set of output in this group consists of seven lines of output describing ROTOR SPEED, VEL. OF SOUND, AIR DENSITY, CRAFT VEL., ANGLE CHI, ANGLE ZETA, THETA GRAV., PSI GRAVITY, COEF. C(K), DELTA3, ALPHA1, COLL. ANGLE, GR RATE STEP, FREQ. STEP, GRAV. ACC., SHAFT FLEX., STR. DAMPING, F/A CYCLIC, LONG CYCLIC, DAMPING OUT, SPUR LENGTH, SPUR EIY, SPUR EIZ, COE1, COE2, and COE3 - corresponding to input in Locations 2, 3, 4, 5, 6, 7, 13, 14, 8, 9, 10, 11, 69, 70, 12, 45, 165, 167, 168, 171, 173, 174, 175, 176, 177, and 178, respectively.

The next few lines of output give the information regarding the control rod and its attachment to the blade. If the rotor configuration is an articulated rotor system (MFLEX=0) this output consists of the parameters PHIM(MS), AKCI(MS), TAU (MS), SMLA (MS), and DMS (MS) for values of MS from 1 to NB - corresponding to input in Locations 71-76, 77-82, 83-88, 97-102, 103-108, respectively. But if the rotor configuration is a flexstrap rotor system (MFLEX = 1 and MCTY = 0), this output describes the parameters PHIM(MS), AMKC(MS), CTAU(MS), PHIC(MS), THEC(MS), AL12(MS), and ALSTH(MS), for values of MS from 1 to NB - corresponding to input in Locations 71-76, 135-140, 141-146, 147-152, 153-158, 159-164, and 195-200, respectively, and the eight parameters of the PHOTT(I) array corresponding to Locations 179-186. If the rotor configuration is a bearingless rotor system (MFLEX = 1 and MCTY = 1) the same parameters described for a flexstrap configuration are described plus the eight parameters of the PHWTT(I) array corresponding to Locations 187-194.

Information concerning the control system ring and its support system is printed next if there is a control system included (NSP  $\neq$  0). The first line of this part of the output describes the control system ring; torsional stiffness, bending stiffness, mass, and radius; in that order. The next output consists of the spring-damper unit support

parameters ECHI(J), AK(J), AC(J), and BJ(J) for values of J from 1 to NES - corresponding to the input in Locations 117-120, 121-124, 125-128, and 129-132, respectively. In the last line of this part of the output, the collective spring-damper unit parameters CAPK and CAPC are printed, which correspond to the input in Location 133 and 134, respectively. It should be noted that these last two parameters are outputted independent of the value of MSC, which specifies whether or not the collective base plate support exists.

The last lines of output on this page depict the starting eigenvalues (both real and imaginary parts) for the normal iteration procedure and correspond to input in Locations 49-58. One eigenvalue is printed on each line, such that the number of lines printed is equivalent to the values of parameter NEGN. If the search option is employed, only one eigenvalue is outputted, corresponding to the starting eigenvalue for the range of search.

## Output of Aerodynamic Coefficient Tables

If C-81 aerodynamic coefficient tables are inputted into the computer program, these tables, including the cards denoting the number of Mach numbers and angles of attack, are printed out essentially the same as inputted. The only difference is that the angle of attack value is outputted in a lX, F 6.1 format instead of F7.3 (as inputted) to avoid dropping the first character of the angle of attack value. It is to be noted that if several aerodynamic coefficient data tables are inputted only those of the C-81 format will be outputted. Preceding this output is a message FOR ISER EQUAL 1 ONLY CCS ARRAYS ARE INPUTTED which is printed if ISER is equal 1 or 81. If ISER is equal 81 this message should be ignored.

### Output of Sectional Aerodynamic Coefficients and Steady Loads

This output follows the previous group and consists of the printout of two groups of intermixed output. The first group consists of the steady forces and moments acting on the next inboard section from the section for which they are outputted. Prior to the first force and moment output the title STEADY FORCES AND MOMENTS is outputted followed by the heading SECTION, N, VY, VZ, T, MZ, MY spaced such that

the corresponding values fall directly underneath. The positive direction of these variables corresponds to that defined for similar variables in the blade shape vector. The information is outputted for every blade section. The second group consists of the aerodynamic variables for each aerodynamic load point position. This output is not printed out if aerodynamics are not included; that is, if the input variable MAER (Location 26) is equal to zero. The size of this output for each aerodynamic blade section is dependent on the number of azimuthal steps (NAS) used for representing the blade aerodynamics. The aerodynamic variables printed for each blade aerodynamic section at various azimuthal positions of the reference blade and for each fuselage aerodynamic section are, in the order of printing: angle of attack (ALPHZ), Mach number (AMACZ), lift coefficient (CSUBL), drag coefficient (CSUBD), pitching moment coefficient (CSUBL), lift curve slope (CLALP), drag .urve slope (CDALP), and pitching moment curve slope (CMALP) where the aerodynamic coefficients printed are two-dimensional. The heading, AERO COEFFICIENTS, and the column headings corresponding to the variables specified above in parentheses precede the numerical output in tabular form. This aerodynamic output for a blade section precedes that of the blade section steady loads and moments.

The order in which these numbers are outputted for a blade section will be briefly noted. The first line of aerodynamic output is for the blade aerodynamic section at the first azimuthal position (reference position) of the blade (corresponding to  $\psi_1$  which equals zero). The next line of aerodynamic output is for the blade aerodynamic section at the next azimuthal position of the blade (corresponding to  $\psi_2$ which equals  $2\pi/NAS$ ). Additional lines are printed corresponding to the stepped azimuthal positions of the blade aerodynamic section until all azimuthal positions have been considered. It should be noted that aerodynamic coefficients are printed only for those blade sections having aerodynamics associated with them. Similar aerodynamic coefficient information for support structure aerodynamic sections is outputted (there being only one line per support structure aerodynamic section).

## Output of Section Data

The input for the blade and support structure sections is printed on the next four pages of output in the form of four tables. The numbers printed in these tables correspond to that stored in locations 201 - 2200 as described in the section pertaining to blade/support structure section input. Preceding the first table, the heading, SECTION INPUT DATA, is printed followed by another heading specifying the order of the application of structural sections of the blade and fuselage - which is 'ORDER OF SECTIONS: BLADE TIP (SECTION 1) TO HUB, THEN FROM FREE END OF FUSELAGE (SECTION 1) TO HUB'.

On the first page of this output, the section number, the values of parameters M1 - M7 which denote the transfer matrices associated with a section, and the values of the parameters m,  $\epsilon_{ry}$ ,  $h_{rx}$ ,  $h_{ry}$ ,  $I_{x}$ , and  $I_{y}$  for each section are outputted under similar column headings. Section parameters described on page two for each section are, in order:  $I_z$ ,  $\Phi$ ,  $\Theta$ ,  $\Psi$ ,  $L_a$ ,  $\psi_f$ ,  $\theta_f$ , and  $\delta$ , where these parameters are outputted under similar column headings. Page three of the output describes c, v<sub>i</sub>, xxxx (GJcs), L<sub>e</sub>, EI<sub>x</sub>, EI<sub>y</sub>, EI<sub>z</sub>, and  $\boldsymbol{P}_{\boldsymbol{T}}$  for each section where these parameters are outputted under similar column headings.  $P_{\mathbf{T}}$  is the steady centrifugal force acting on the section due to rotation of the blade and depends upon the magnitude and distribution of masses outboard of the blade section. It may be noted that  $P_{_{\mathbf{T}}}$  for fuselage sections is zero. The fourth group of output describes, in order:  $\delta_x$ ,  $\delta_y$ ,  $\delta_z$ ,  $N_0$ ,  $Vy_0$ ,  $Vz_0$ ,  $K_x^{-1}$ ,  $K_y^{-1}$ ,  $K_z^{-1}$ ,  $\tau_x$ ,  $\tau_y$ ,  $\tau_z$ , and  $K_s$  for each section with the values given under column headings similar to the variables. The values for  $N_0$ ,  $Vy_0$ , and  $Vz_0$  will always be 0.0 since these are the steady forces now determined internally in the program.

This tabular form of output of blade and support structure section data provides a convenient form for checking the sectional input to ascertain if the blade and support structure representation is as desired.

## Output of Search Option Information

This set of output provides information regarding the value of the final matrix determinant for each trial eigenvalue specified in the use of the search option procedure by input of the initial stability and frequency values, the size of the stability and frequency steps, and the number of stability and frequency steps.

For each trial eigenvalue, a set of three numbers in double precision (first and last numbers being complex) are printed, which are components of the resulting final governing matrix determinant. The numbers printed with descriptive labels are the program variables in the order DTPHAS, DTLG10, and DPIVOT: where the determinant  $\overline{\Delta}$  is defined as

# $\overline{\Delta} = DTPHAS*DPIVOT*10$ (DTLG10)

The quantity DTLG10 is representative of a factor removed from the determinant in the process of reducing the determinant matrix to the one which has diagonal elements with a complex absolute value of 1 and DTPHAS and DPIVOT are complex numbers resulting from obtaining the determinant of this resultant matrix.

This information is followed by the output of the trial (initial) search option eigenvalue and the value of the determinant with descriptive labels. It is to be noted that due to size limitations, a factor (multiples of 10\*\*20) is removed from the calculation of the determinant to prevent overflow problems. Thus, for purposes of output the matrix determinant is defined by the equation

# $\overline{\Delta} = DTPHAS*DPIVOT*10$ (DTLG10-IFAC\*20.)

where IFAC is the integer number of times 20 can be divided into DTLG10. Thus, a factor 10\*\*(IFAC\*20.) has been removed from the determinant before printout. When the above information has been outputted for all trial eigenvalues the possible starting eigenvalues that are obtained will be used in the iteration procedure. However, if there are not any possible starting eigenvalues in the region scanned, then a message that there are no eigenvalues in that region is outputted.

The main purpose of the output provided for the search option procedure is to allow the user to ascertain if possible

roots may have been missed or if there may be an eigenvalue in a neighboring area based on trends observed in the determinant values as a function of stability and frequency values.

## Output of Iteration Scheme Steps

This set of output is the pertinent information regarding the iterational procedure such that the program behavior from one iteration to the next can be observed.

The first line that is printed under this group of output by the program is as follows:

#### XXX VALUES OF UPDATED LAMBDA MATRIX

where in place of the xxx the actual number of values is printed. The numbers printed after this heading are the trial eigenvector quantities which are the approximations to the non-zero solution unknowns. It is to be noted that these are initially assumed to be unity and are updated by the correction quantities after each iteration and printed. Once the program has converged to an eigenvalue, there should be no significant change in these quantities. fore, the printout of this information provides an additional check on the program convergence to an eigenvalue. The initial set of trial eigenvector quantities is followed by the printout of the three determinant components, DTPHAS, DTLG10, and DPIVOT, for the starting eigenvalue. The functionality of these variables was discussed in detail in the previous output section. After the output of this information on the first iteration (ITI = 0), the initial eigenvalue and corresponding modified (i.e., a factor removed as discussed in the previous section) determinant value are printed.

The updated LAMBDA MATRIX for the second iteration (ITI = 1) is then printed, followed by the listing of determinant components (DTPHAS, DTLG10, and DPIVOT) for the second trial eigenvalue. The eigenvalue and modified determinant value on the second iteration are not printed, but are outputted as the LAST values on the third iteration.

The output for each iteration above the second iteration (ITI > 1) has the following form:

- 1. Updated LAMBDA MATRIX is printed.
- The three determinant components (DTPHAS, DTLG10, and DPIVOT) are listed.
- 3. The three numbers describing the last modified determinant value, current modified determinant value, and eigenvalue convergence are printed.
- 4. The three numbers stating the last eigenvalue, current eigenvalue, and next eigenvalue are printed.

The three determinant components (2.) correspond to the CURRENT eigenvalue and determinant. The heading LAST refers to the values on the previous iteration. The NEXT eigenvalue is based on the interpolation of CURRENT and LAST values. It is to be noted that the possibility of the value of IFAC changing from one eigenvalue to another has been compensated for in the interpolation scheme. The convergence value is based on the change of eigenvalue from the current eigenvalue to the next eigenvalue relative to the current eigenvalue. Also, it may be noted during successive iterations that the normalized quantity in the updated LAMBDA MATRIX remains equal to one.

As the program iterates to a solution eigenvalue, the current modified determinant value will become smaller and approaches zero in the limit (at an eigenvalue). Furthermore, the difference between the current eigenvalue and the next eigenvalue, as predicted by the program, will approach zero. The last iteration will show eigenvalue convergence being less than (.1) \*\* MER, indicating that the eigenvalue has converged to within the prescribed accuracy. (Note that MER is the input parameter in Location number 61.) If this is not so, then the program ran out of iterations (prescribed in the input by NIT). As an example, consider the following sample printout of the last step of an iteration where the following is outputted:

LAST DETERMINANT VALUE =-0.688730D-06-0.344391D-06
CURRENT DETERMINANT VALUE =-0.570891D-09 0.161642D-09
EIGEN VALUE CONVERGENCE = 0.104667E-08

LAST EIGEN VALUE =-0.250890D 02 0.177439D 03 CURRENT EIGEN VALUE =-0.250888D 02 0.177439D 03 NEXT EIGEN VALUE =-0.250888D 02 0.177439D 03 Here, it is obvious that the eigenvalue has converged to a value of (-25.0888+177.439i), rad/sec, and the last eigenvalue convergence is less than (.1)\*\*MER where MER is taken as 7.

After the program has converged to an eigenvalue, or if it has reached its upper limit on the number of iterations, then the following title for the shape vector output group (discussed in next section) is printed out:

# AEROELASTIC STABILITY STATE VECTORS

## Shape Vector Printed Output

The shape vectors for the blades and fuselage are computed and printed after the eigenvalue has converged to a solution eigenvalue or the maximum number of iterations allowed has occurred. The shape vectors are printed out after the last iteration whether or not convergence has been obtained because quite often, even though the eigenvalue convergence is not within the prescribed accuracy, the convergence may be very close to that desired and the shape vectors may be quite satisfactory if they satisfy the boundary or matching conditions at the hub. It should be noted that the degree to which the boundary conditions are satisfied and the degree of convergence obtained determine the validity of the results of a run. The main reason a converged eigenvalue for a specific case may not be obtained before the number of allowed iterations has occurred is that the starting eigenvalue may not be sufficiently close to an actual solution eigenvalue of the system of interest. Quite often fairly good guesses are needed to assure that the starting eigenvalues converge to the proper solution eigenvalues.

The printout of the swashplate (control system) displacements and the shape vectors (or mode shapes) of the blades and support structure will be presented assuming  $\pm 1/\text{rev}$  interharmonic coupling (NHC = 1) to be involved in the program run. The swashplate ring deflections, if NSP  $\neq$  0, are printed out following a general heading, SWASHPLATE DEFLECTIONS, and separated into sets corresponding to a particular shifted frequency by headings of the form, p PER REV., where p goes from a value of +NHC to -NHC. It should be noted that a positive value of p corresponds to an upward

shift in the frequency (for example, if p is equal to +1 the output corresponds to behavior at 1/rev above that of the frequency obtained on solution). Under each of these headings are printed the corresponding p/rev frequency shifted Fourier spatial harmonics of the swashplate motion in the order of the harmonics going from +NMAX to -NMAX, where the particular spatial harmonic is specified (with the opposite sign) in the printout. Thus, for NHC = 1, the swashplate information is printed out in the following order:

- 1. +NMAX to -NMAX spatial harmonics of
   swashplate displacement for p = 1
   corresponding to a +1/rev motion rela tive to the main frequency
- 2. +NMAX to -NMAX spatial harmonics of
   swashplate displacement for p = 0
   corresponding to a motion at the
   main frequency
- 3. +NMAX to -NMAX spatial harmonics of swashplate displacement for p = 1 corresponding to a -1/rev motion relative to the main frequency

The next set of output is the printout of the blade shape vectors. The shape vector printout for NHC = 1 can be listed in the order of output as

- 1. heading, BLADE 1 +1 PER REV SHAPE VECTOR (LOCAL AXIS SYS.)
- 2. +l/rev mode shapes for blade
   number l in the local section coordinate
   systems where k is -l but motion is
   l/rev above the main frequency
- 3. heading if NPD is 1 (corresponding to input Location 15), DISK PLANE AXIS SYSTEM
- 4. +1/rev mode shapes for blade number 1, if NPD is 1, in the disk plane axis system (rotating hub coordinate system) where k is -1 but motion is 1/rev above main frequency

- 5. heading if NPD is 1 (corresponding to input Location 15), DISK PLANE AXIS SYSTEM POLAR COORDINATES AMPLITUDE AND PHASE ANGLE
- 6. +1/rev disk plane mode shapes for blade number 1, if NPD is 1, in polar form, where motion is 1/rev above main frequency
- 7. steps 1 thru 6 are repeated for blade number 2 (only if NB > 2), blade number 3 (only if NB > 3), etc.
- 8. steps 1 thru 7 are repeated for the blade mode shapes at the main frequency (p = 0)
- 9. steps 1 thru 7 are repeated for the blade mode shapes 1/rev below the main frequency (p = -1)

The blade shape vectors are printed out for all the blade sections with four sets of three columns each for the local coordinate system values and disk plane values with the sets in the following order:

- radial, inplane, and vertical blade deflections
- torsional, vertical bending, and inplane bending slopes
- 3. radial, inplane shear, and vertical shear forces
- 4. torsional, vertical bending, and inplane bending moments

Each column has a descriptive heading specifying the variable listed in the column and the positive convention of the variable. The state variable values for a blade section are the values of the variables acting on the outboard end of the next inboard section. If NHC is equal to zero only 0/rev shape vectors are involved and printed.

The blade shape vector output is followed by the printout of the support structure mode shapes if the configuration includes a support structure (i.e., MFUS = 1 corresponding to input Location 33). This printout can be listed in the order of output as

- 1. heading, +1 PER REV SHAPE VECTORS ON THE FUSELA. STRUCTURE (LOCAL AX)
- 2. +1/rev mode shapes for the support
  structure in local section coordinate
  systems where k is -1 but motion is
  1/rev above the main frequency
- 3. heading if NPD is 1 (corresponding to input Location 15), FUSELAGE REFERENCE AXIS SYSTEM
- 4. +1/rev mode shapes for the support structure relative to the fixed support structure coordinate system where motion is 1/rev above main frequency
- 5. heading if NPD is 1 (corresponding to input Location 15), FUSELAGE REFERENCE AXIS SYSTEM POLAR COORDINATES
- 6. +1/rev mode shapes for the support structure relative to the fixed support structure coordinate system in polar form, if NPD is 1, where motion is 1/rev above main frequency
- 7. steps 1 thru 6 are repeated for the support structure mode shapes at the main frequency
- 8. steps 1 thru 6 are repeated for the support structure mode shape 1/rev below the main frequency

The support structure shape vectors are also printed out for all support structure sections with four sets of three columns each for the local coordinate system values and fixed support structure coordinate system values, with the sets in the following order:

- axial, vertical, and lateral support structure deflections
- 2. torsional, lateral bending, and vertical bending slopes
- axial, vertical shear, and lateral shear forces
- 4. torsional, lateral bending, and vertical bending moments

Each column has a descriptive heading specifying the variable listed in the column and the positive convention of the variable. It should be noted that in these headings the notation, INPLANE, has been used to denote the lateral direction. The positive convention for the twist in the reference axis system is for the top of the structure to the left. Basically, the variable values outputted for a support structure section are the values for the variables acting on the hubward end of the section in the positive axis directions. For both the support structure and blade mode shape output, the section numbers are also printed in an adjacent column to allow easy association of results with the section to which they correspond. If NHC is equal to zero only the 0/rev shape vectors are printed.

The printout of the blade shape vectors and the support structure shape vectors, if a support structure is modelled, is the last printed output associated with the results obtained for a given starting eigenvalue. From this shape vector output the convergence of the eigenvalue could be verified, if desired. Normally, when the program converges to an eigenvalue, all of the boundary conditions at the hub are satisfied. One of these boundary conditions can be easily checked from the printed output. The blade deflection denoted by UBZ at the blade root (hub section) of each blade in the local coordinate system (or disk plane, since the variable values at hub section should be independent of coordinate system) should be equal to the support structure deflection denoted by UBX at the last section (hub section) of the support structure in the local support structure axis system. The remaining blade root variables and support structure variables at the hub may also be checked for matching of boundary conditions, but the equations describing the hub boundary conditions involve combinations of -1/ rev,

0/rev, and +1/ rev frequency-shifted shape vectors due to the transformations from the blade rotating system to hub fixed system and vice versa.

## Shape Vector Punched Output

The computer program provides the blade and support structure state variable information in punched card form if IPU (corresponding to array Location 166) is equal to 1. punched output includes all state variables (shifted and unshifted) determined for all blade sections of all blades and all support structure sections. The punched data is generated with the use of a (I5, 3(1X,2(1PE12.4))) format such that each card contains the section number and three state variable values in the same order as they are printed. For every row of printed state variable output a punched card containing the same information is generated. order in which the state variable information is punched coincides with the order in which all of the blade and support structure state variables are printed. This program capability was added to allow the state variable information to be available after a run for subsequent use.

## SAMPLE INPUT

## Bearingless Rotor Case

2011	1.0				
2514	1.0	1.0	0.0	1.0	
3014		1.0	0.0	1.0	
3514		1.0	0.0	1.0	
4014		1.0	0.0	1.0	
4514	1.0	1.0	0.0	1.0	
5014	1.0	1.0	0.0	1.0	
5514	1.0	1.0	0.0	1.0	
6014		1.0	0.0	1.0	
6514		1.0	0.0	1.0	
7014		1.0	0.0	1.0	
7514		1.0	0.0	1.0	
8014	1.0	1.0	0.0	1.0	
8514	1.0	1.0	0.0	1.0	
9014	1.0	1.0	0.0	1.0	
9515		1.0	0.0	1.0	1.0
					• • •
10023		0.0	1.0		
-	1.0				
	1.0				
11514	1.0	1.0	0.0	1.0	
12014	1.0	0.0	0.0	1.0	
12514		0.0	0.0	1.0	
	1.0	0.0	0.0	1.0	
				=	
	1.0	0.0	0.0	1.0	
14014		0.0	0.0	1.0	
14514	-	0.0	0.0	1.0	
15014	1.0	0.0	0.0	1.0	
15514	1.0	0.0	0.0	1.0	
	1.0	0.0	0.0	1.0	
16514		1.0	0.0	1.0	
	1.0	•••	• • •	•••	
		44804	101 17000	LARBI	09/1944
2085		-,61591	193.37000	.60591	.024216
	.0083197	-,61591	183.70150	.60591	048432
3085	.0080135	<b>61591</b>	174.03300	. 60591	.048432
3585	.0080135	61591	164.36450	.60591	.048432
4085	.0078979	61591	154.69600	.60591	.048432
4585	-	-,61591	145,02750	.60591	.048432
5085		-,61591	135.35900	.60591	.048432
			125.69050		
5585	.0077380	61591		.60591	,048432
6085	.0077380	61591	116.02200	.60591	.048432
6585	.0077380	61591	106,35350	.60591	.048432
7085	.0134267	61591	96.68500	.60591	.053236
7585	.0077380	-,61591	87.01650	.60591	.048432
8085	.0089997	18618	77.34800	.60591	045456
8585	.0116129	01591	67.67950	.60591	.031485
					019826
9085	.0129953	11217	58.01100	.60591	
9585	,032923	0.0	51.47500	0.0	.047785
11585	.0089010	0.0	48.34250	0.0	.034662
12085	.0057872	0.0	43.50825	0.0	.030318
12585	.0020748	0.0	38.67400	0.0	.012693

```
13085 .0020594
                     0.0
                                      33.83975
                                                   0.0
                                                                   .010097
13585 .0020897
                     0.0
                                      29.00550
                                                   0.0
                                                                   .007622
14085 .0021199
                     0.0
                                      24,17125
                                                   0.0
                                                                   .007141
14585 .0022519
                     0.0
                                      19,33700
                                                   0.0
                                                                   .007547
15085 .0044613
                     0.0
                                      14.50275
                                                   0.0
                                                                   .013266
15585 .0154515
                     0.0
                                       9.66850
                                                   0.0
                                                                   .026028
16085 .0444968
                                       4.83425
                     0.0
                                                   0.0
                                                                   .382518
16585 .0260251
                     0.0
                                       0.0
                                                   0.0
                                                                   .340449
 2141 .024216
 2641 .048432
 3141 .048432
 3641 .048432
 4141 .048432
 4641 .048432
 5141 .048432
 5641 .048432
 6141 .048432
 6641 .048432
 7141 .053236
 7641 .048432
 8141 .045456
 8641 .031485
 9141 .019826
 9641 .067785
11641 .034662
12141 .030318
12641 .012693
13141 .010097
13641 .007622
14141 .007141
14641 .007547
15141 .013266
15641 .026028
16141 .382518
     .340449
16641
 2764 9,6685
                      .1360000E+07
                                                    .5940000E+08
                                     .2380000E+07
 3264 9,6685
                      .1360000E+07
                                                    .5940000E+08
                                     .2380000E+07
 3764 9,6685
                      .1360000E+07
                                     .2380000E+07
                                                    .5940000E+08
 4264 9,6685
                      .1360000E+07
                                     .2380000E+07
                                                    .5940000E+08
 4764 9,6685
                      .1340000E+07
                                                    .5940000E+08
                                     .2380000E+07
 5264 9,6685
                      .1360000E+07
                                     .2380000E+07
                                                    .5940000E+08
 5764 9,6685
                      .1360000E+07
                                     .2380000E+07
                                                    .5940000E+08
 6264 9,6685
                      .1360000E+07
                                     .2380000E+07
                                                    .5940000E+08
 6764 9,6685
                      .1360000E+07
                                     .2380000E+07
                                                    .5940000E+08
7264 9.6685
                      .1360000E+07
                                                    .5940000E+08
                                     .2380000E+07
7764 9,6685
                      .1361000E+07
                                                    .5940000E+08
                                     .2380000E+07
                      .1538300E+07
 8264 9,6685
                                     .2550300E+07
                                                    .5887500E+08
                      .2175500E+07
                                                    .5496800E+08
 8764 9,6685
                                     .3974100E+07
                      .3596600E+07
 9264 9,6685
                                     .5684300E+07
                                                    .5047400E+08
                      .4533300E+07
9764 6.5360
                                                    .6460600E+08
                                     .1076800E+08
```

```
.1182500E+08
10264 2.4750
                                      .1574600E+09
                                                     .3953500E+09
                      .3929400E+08
11764 0.6575
                                      .1210700E+09
                                                    .6106000E+09
12264 4.83425
                      .4210500E+06
                                      .1588500E+08
                                                    .1371800E+09
                      .5850400E+05
                                      .5273700E+07
                                                    .4555200E+08
12764 4.83425
                      .4905900E+05
                                      .5869500E+07
13264 4,83425
                                                    .3737800E+08
                      .4942800E+05
13764 4.83425
                                                    .3734500E+08
                                      .7047600E+07
14264 4.83425
                      .4998300E+05
                                                    .3740700E+08
                                      .8321000E+07
14764 4.83425
                      .5000000E+05
                                                    .3870500E+08
                                      .9934100E+07
15264 4.83425
                      .7208000E+05
                                      .1474200E+08
                                                    .4924300E+08
                      .3156800E+06
15764 4.83425
                                                    .8572300E+08
                                      .2848200E+08
                      .2375500E+07
                                                    .1788100E+09
16264 4,83425
                                      .4689400E+08
16764 4.83425
                                      .3999100E+09
                      _4777400E+08
                                                    .1346800E+10
 9891 .60591
       .1668200E+08
12251
12751
       .7044400E+07
13251
       .6361000E+07
13751
       .6419300E+07
14251
       .6488600E+07
14751
       .6874800E+07
15251
       .9400200E+07
       .1620300E+08
15751
16251
        .2698000E+08
      44.5059
   21
  151 1.0
  173
     1.0
                     4.0
                                    31.0
  242 1.0
                     1.0
  311 19.0
  461 1.0
  595 50.0
                     15.0
                                    7.0
                                                   5.0
                                                                  6.0
  641 6.0
       .6035700E-03
 1351
 1471 -. 785398
 1531 .390008
 1724 1.0
                     2.58226
                                      .2000000E+07
                                                     .2000000E+07
                     -263.08173
 1763 0.0
                                    0.0
                      .2585000E+07
                                      .1593000E+07
 1794 39,00573
                                                     .6930000E+06
 1834 3,1415927
                      .0736455
                                    0.0
                                                    .2681840E+07
 1871 7.43277
 1912 1.064508
                     -_0101443
  121 386.088
12021 1.0
100111.0
115410.0
125211.0
130211.0
135211.0
140211.0
145211.0
150211.0
155211.0
```

A to Little to files

```
160211.0
 9581.0308687
10081.0046190
11581.0066174
1010148.3425
1060148.3425
1110148,3425
09623.077161
                     0.0
                                    .077161
11623.025285
                     0.0
                                    .025285
10161-.01309
11661-.01309
106010 0
102643,1325
                      .1385800E+08
                                     .1481100E+09
                                                    .4269400E+09
117640.0
                      0.0
                                     0.0
                                                    0.0
01791 38,41774
01841 .088644
1591 10.56
 1951 3.06
2531 1.0
 3051 1.0
 3531 1.0
4051 1.0
4531 1.0
5031 1.0
5531 1.0
6031 1.0
6531 1.0
7031 1.0
7531 1.0
8031 1.0
8531 1.0
2682 1.0
                     9.6685
3182 1.0
                     9,6685
3682 1.0
                     9,6685
4182 1.0
                     9.6685
4682 1.0
                    4.6685
5182 1.0
                    9,6685
5682 1.0
                    9.6685
6182 1.0
                    9.6685
5682 1.0
                    9,6685
7182 1.0
                    9,6685
7682 1.0
                    9,6685
8182 1.0
                    9,6685
8682 1.0
                    8.34075
2722 3,26591
                    10.64
3222 3,26591
                    10.64
3722 3.26591
                    10.64
4222 3.26591
                    10.64
4722 3.26591
                    10.64
5222 3,26591
                    10.64
```

```
5722 3,26591
                     10.04
 6222 3,26591
                     10.64
 6722 3,26591
                     10.64
 7222 3,26591
                     10.64
 7722 3.26591
                     10.64
 8222 3,26591
                     10.64
 8722 3.26591
                     10.64
                      .1146300E-06
   32
       .1340300E+05
   63 1,570796
                     0.0
                                    . 8
  261 1.0
  341 16.0
 2741 513.97
 3241 513,97
 3741 513.97
 4241 513.97
 4741 513.97
 5241 513.97
 5741 513,97
 6241 513.97
 6741 513,97
 7241 513.97
 7741 513.97
 8241 513.97
 8741 513,97
 1672 .001641
                     .005009
 2111-0,1853881E+01
 2611-0,1713217E+01
 3111-0,1571979E+01
 3611-0,1429330E+01
 4111-0.1284368E+01
 4611-0,1136753E+01
 5111-0.9864085E+00
 5611-0.8338016E+00
 6111-0,6797164E+00
 6611-0.5250247E+00
 7111-0.3709548E+00
 7611-0,2189657E+00
 8111-0,7083029E-01
 8611 0,7135791E-01
 9111 0.2053451E+00
 9611-0.3157269E+00
10111-0.2750667E+00
10611-0.2750667E+00
11111-0.2750667E+00
11611-0,2750667E+00
12111-0.2211854E+00
12611-0.1673041E+00
13111-0.1237797E+00
13611=0.8025533E=01
14111-0,5228527E-01
```

```
14611-0.2431520E-01
15111-0,1341677E-01
15611-0,2518338E-02
16111-0.1259169E-02
 2153-0.1454767E-01-0.2782708E-01 0.9605795E-01
 2653-0,1454767E-01-0,2782708E-01 0,1027852E+00
 3153-0.1460704E-01-0.2841647E-01 0.1093680E+00
 3653-0,1475289E-01-0,2965435E-01 0.1158658E+00
 4153-0,1499213E-01-0,3192549E-01 0,1223182E+00
4653-0.1526636E-01-0.3422624E-01 0.1267245E+00
 5153-0,1554871E-01-0,3638931E-01 0,1350722E+00
 5653-0,1578262E-01-0,3811616E-01 0,1413519E+00
6153-0,1593547E-01-0,3933148E-01 0,1475481E+00
 6653-0,1599818E-01-0,3991526E-01 0.1536441E+00
 7153-0,1593390E-01-0,3986597E-01 0.1596156E+00
 7653-0.1571872E-01-0.3908069E-01 0.1653896E+00
8153-0,1532025E-01-0,3751607E-01 0,1711283E+00
8653-0.1470527E-01-0.3519034E-01 0.1771091E+00
9153-0,1365723E-01-0,3221410E-01 0,1833672E+00
 9653-0,1297938E-01-0,3163933E-01 0,2288158E+00
10153-0,1297938E-01-0,3163933E-01 0,2285851E+00
10653 0.0
                    0.0
                                  0.0
11153 0.0
                                  0.0
11653-0,1297938E-01-0,3163933E-01 0.2285851E+00
12153-0.1114528E-01-0.2767443E-01 0.2341551E+00
12653-0,1114528E-01-0,2767443E-01 0,2413099E+00
13153-0.9003095E-02-0.2246325E-01 0.2455308E+00
13653-0.9003095E-02-0.2246325E-01 0.2497092E+00
14153-0.5785745E-02-0.1481477E-01 0.2431120E+00
14653-0,5785745E-02-0,1481477E-01 0,2365021E+00
15153-0,2254416E-02-0,6113276E-02 0,2246698E+00
15653-0.2254416E-02-0.6113276E-02 0.2115865E+00
16153-0,5209367E-03-0,1703219E-02 0,2106684E+00
1761 157.0
 611 7.0
 371 1.0
 381 1.0
 395 3.0
                                   .015
                                                  6.1
                                                                .1000000E+19
 441 .1000000E+10
 971 6,5
1173 0.0
                    2.094395
                                  4.188790
                    .2359423E+05 .2359423E+05
01213 .2359423E+05
1331 7363,5766
1351
      .3846154E-05
 623 8.0
                    9.0
                                   9.0
 601 12.0
2161 -. 03061
2661 -,03061
3161 -, 031258
3661 -,032839
```

```
4161 -,035118
 4661 -. 037649
 5161 -. 040028
 5661 -. 041928
 6161 -. 043264
 6661 -. 043907
 7161 -. 043853
 7661 -. 042989
 8161 -. 041268
 8661 -. 038709
 9161 -. 035435
 9661 -. 034803
10161 -. 034803
11661 -. 034803
12161 -. 030441
12661 -. 030441
13161 -. 024709
13661 -, 024709
14161 -,016297
14661 -. 016297
15161 -. 00672
15661 -.00672
16161 -. 00187
  351 0.0
  651 2.0
  481 1.0
  491 -14.6
  541 48.6
    8
    1
   81
    1
    5
180.
                  -180.
   11
         39
                                                                         0.85
                                0.5
                                                 0.7
                                                         0.75
                                                                 0.8
       0.
                0.3
                        0.4
                                        0.6
       0.9
                1.
                .04
        .04
                                         .04
                                                                         .04
-180.
                        .04
                                .04
                                                 .04
                                                         .04
                                                                 .04
       .04
                .04
       . 65
                                                                         .45
                .65
                                                 .65
-174.
                                         . 65
                        .65
                                ,65
                                                         . 65
                                                                 . 65
        .65
                . 65
-170.
                                                 .65
                                                                 .65
        . 65
                .65
                        .65
                                .65
                                         .65
                                                                         .65
                                                         .65
        .65
                .65
                                                                 .62
                                                                         .62
-166.
        .62
                                .62
                                         .62
                                                 .62
                                                         .62
                .62
                        .62
        .62
                .62
                                                 .865
                        .865
                                .865
                                        .865
                                                         .865
                                                                 .865
                                                                         .865
-133.
        .865
                .865
        .865
                .865
       . 635
                        .635
                                        .635
                                                 .635
                                                         .635
-113.
                .635
                                 .635
                                                                 .635
                                                                         .635
       ,635
                .635
                        -.89
       -.89
                                                                         -. 89
-58.
                -.89
                                -.89
                                        -.89
                                                -,89
                                                         -.89
                                                                 -.89
```

	89	89							
-38,	-1.14	-1.14	-1.14	-1.14	-1.14	-1.14	-1.14	-1.14	-1.14
	-1.14	-1.14				B		47.	- <b>-</b>
-20.	98	-1.03	-1.07	-1.13	-1.14	868	86	845	74
-15.	-1.01 -1.165	-1.34	-1.285	-1,23	-1.13	88	892	827	685
-15.	-1.01	-1.34	-19503	-1,53	-1113	<b>4</b> 600	- 0 7 2	021	A*002
-13,5	-1,22	-1.28	-1.33	-1.26	-1,12	88	885	814	677
	-1.01	-1.34	• •	• • •		•	•	• - •	
-12,	-1,095	-1.15	-1.2	-1.14	-1.092	86	877	791	655
	-1.01	-1.25					_		• -
-9.5	89	93	97	-,93	-1.05	83	85	77	62
_ c _ c	- 947	-1.1	51	- 66	_ 505	64	688	65	58
-5,5	-, 47 -, 41	493 61	m*31	55	585	. 04	000	05	- 30
-4.	-,312	•.33	335	36	39	41	5	475	28
	- 55	43	-,000						
-2.	1	107	105	115	12	12	127	16	165
	085	185							
-1.	0.0	0.0	0.0	0.0	.01	.025	.015	.05	005
0 0	015	06	4.3	4.7	4 /1	. 7	6.0	2.11	<b>A</b> 6
0.0	.11	.11	.12	.13	.14	.17	.19	.24	.06
2.	.32	.332	.35	.375	.41	.475	.485	.37	.208
	.39	.3	• 30	, , , ,	•			• • •	
3.	425	.443	.467	. 5	.547	.62	. 5	.415	. 26
	.52	.426							
4.	.53	.55	.58	.65	.68	.675	.57	.475	.28
4	.63	.545		040	0.1	747	4 -		• >
6.	.742 .92	.772	.815	.868	.91	.767	.67	•51	.32
8.	95	995	1.035	1,115	.995	.856	.732	.545	. 355
	1.19	1.03	.,			• (1)	• • • • •		•
10.	1.165	1.22	1.26	1.27	1.075	.942	.791	.58	.393
	1.19	1.095							_
11.	1.268	1.328	1.38	1.278	1.092	.985	.825	. 6	.413
	1.19	1.095	4 /19	1 25		4 028	422	4.4.	423
12.	1.375	1.44	1.42	1,25	1.113	1.028	.852	.615	.432
13.	48	1,55	1.395	1,225	1.13	1.069	.885	.633	. 45
	1,19	1.095	• • • •	.,					
13,5	1.53	1.6	1.27	1.207	1.141	1.09	. 9	.641	.461
	1.19	1.095					20 2	_	75.4
14.	1,585	1.095	1.14	1.19	1.15	1,112	.913	. 65	. 47
15	1.19	1.095	4	1 102			0 # 4	444	лО
15.	.915	.962	1.	1.192	1.17	1,155	.946	. 468	.49
20.	1.	1.05	1.09	1,2	1.26	1.367	1.1	.76	.59
	1.19	1.095	• • • •					., .	• • •
38.	1,135	1,135	1.135	1.135	1.135	1.135	1.135	1.135	1.135

58,	1.135 .89 .89	1.135 .89 .89	.89	.89	.89	.89	.89	.89	.89
113.	635	635	635	-,635	635	-,635	635	635	635
133.	-,635 -,865	635 865	-,865	-,865	-,865	-,865	865	865	865
158.	865 -1.	865	-1.	-1.	-1.	-1.	-1.	•1.	-1.
166.	-1. 72	-1. 72	-,72	72	72	-,72	72	·.72	72
170.	72 82	72 82	82	-,82	-,82	•,82	82	-,82	82
180.	82	82	.04	.04	.04	.04	.04	.04	.04
2	.04	.04							
180.	45	-180	•						
	0.0	0.4	0.5	0.6	0.65	0.7	0.75	0.8	0.85
-180.	.015	.015	.015	.015	.015	.015	.015	.015	.015
-175.	04	04	.04	.04	.04	.04	.04	.04	.04
-170.	.11	11	.11	•11	.11	.11	.11	•11	.11
-164.	55	55	.55	.55	.22	.22	.22	.22	.55
-155.	.51 .51	.51	.51	.51	.51	.51	.51	.51	.51
-130.	1.08	.51 1.08 1.08	1.08	1.08	1.08	1.08	1.08	1.08	1.08
-100.	1.51	1.51	1.51	1.51	1.51	1.51	1.51	1.51	1.51
<b>-90</b> .	1.56	1.56	1.56	1.56	1.56	1.56	1.56	1.56	1.56
<b>-80</b> .	1.51	1.51	1.51	1,51	1.51	1.51	1.51	1.51	1.51
-60.	1.24	1.24	1.24	1.24	1.24	1.24	1.24	1.24	1.24
-40.	9	9	. 9	. 9	. 9	. 9	. 9	. 9	. 9
-25.	51 51	.51 .51	.51	.51	.51	.51	.51	.51	.51
-8.	0205	0205 2175	.067	.136	.1375	.1405	.144	.17	.1818
-6.	0154 138	.0154	.03	.075	.0765	.079	.087	.115	.127
-4.	.0112	.1062	.0115	.0141	.0163	.0182	.0287	•06	.0715

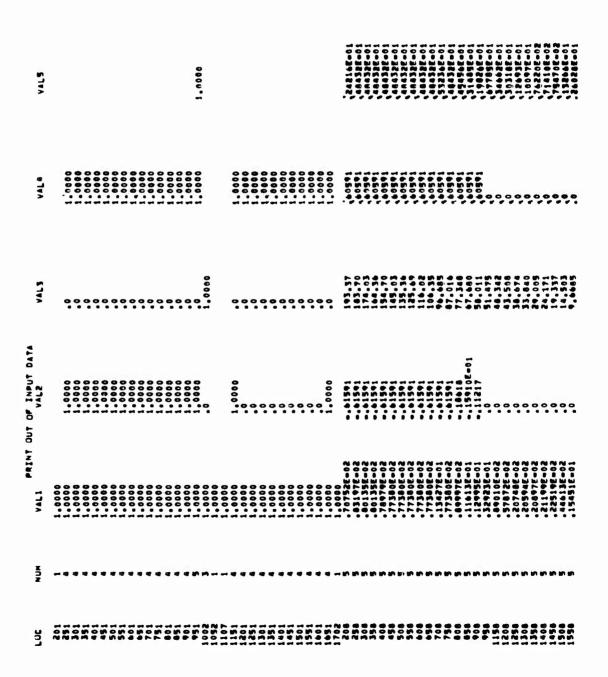
-3.	.0107	.0107	.01095	.0123	.01335	.01445	.0117	.0322	.0448
	.0625	.089							
-2.	.0104	.0104	.0104	.0105	.0104	.0107	.011	.0137	.0284
	.0425	.0715							
-1.	.0105	.0105	.0103	.01035	.01035	.0105	.0104	.0177	.0373
	.0512	.0812							
0.	.0106	.0106	.0102	.0102	.0103	.0103	.0131	.0287	.0445
	.06	.091	-						
1.	.0105	.0105	.0103	.01035	.01075	.0119	.0217	.0474	.0631
•	.079	.1105	•						
2.	0104	.0104	.0104	.0105	.0112	.0186	.0384	.0659	.082
-,	0975	1293			•	-		_	
3.	0106	0106	.0107	.0118	.015	.0298	. 0569	.0848	.101
J.	1165	1485			••••	• • • • • • • • • • • • • • • • • • • •			•
4	0108	.0108	.011	.0131	.0236	.0484	.0755	.1035	.1195
4.		.167	. 0	.0131	.0230				
	.135		.01175	.0191	.0345	.067	.0944	.122	.1383
5.	.0114	.0114	.01113	• 01 41	.0343				
4	.153	.186	0125	.0293	.053	.086	.113	.141	.157
6.	.012	.012	.0125	.0273	.033	.000		• 1 - 1	• 1 3 .
_	.172	.205	4477	0/136	.072	.1047	.1319	.16	.176
7.	.01265	.01265	.0133	.0426	.012	.1047	. 1317	• 10	. 170
	.1915	.223		014	0005	1275	IEAR	.1788	. 195
8.	.0135	.0133	.0153	.061	.0905	.1235	. 1505	.1/80	.173
	.21	.2425			4.000		4 4 0 7	400	.2135
9.	.0137	.0137	.0212	.0798	.1092	.1422	. 1693	.198	. 6133
	. 556	.261	- 4			4445	4.4.	-4-	273
10.	.0153	.0153	.03	.0983	.1275	.1607	.188	.217	. 232
	.248	. 28							
11.	.0175	.0175	.0483	.118	.1465	.179	.207	.236	.2505
	. 500	.299							
12.	.0205	.0205	.067	.1357	.105	.1985	.225	.256	.27
	.285	.318						_ = =	
13.	.0282	.0282	.0858	.1545	.1835	.217	.244	.275	.289
	.304	.3365						_	
15.	.0465	.0465	.1233	.192	.221	.254	.281	.3135	.3265
	. 34	.374							
30.	. 66	. 66	.66	.66	.66	.66	.66	.66	.66
_	. 66	.66							. • .
50.	1.07	1.07	1.07	1.07	1.07	1.07	1.07	1.07	1.07
	1.07	1.07							
80.	1.5	1.5	1.5	1.5	1.5	1.5	1.5	1.5	1.5
Ť	1.5	1.5							
90.	1.56	1,56	1.56	1,56	1.56	1.56	1.56	1.56	1.56
	1.56	1.56	-						
100.	1.51	1.51	1.51	1.51	1.51	1.51	1.51	1.51	1.51
* - 5 <b>*</b>	1.51	1.51		-					•
120.	1.23	1,23	1.23	1,23	1.23	1.23	1.23	1.23	1.23
	1,23	1.23	• • •		<del>-</del>				
140.	.89	.89	.89	.89	.89	.89	.89	.89	.89
	89	.89	•	-	*	-	•		
	/								

155.	.5	•5 •5	. 5	.5	.5	.5	. 5	•5	. 5
104.	.55	.55	.55	.22	.22	.22	.22	.22	. 22
170.	.11	.11	.11	.11	.11	.11	.11	•11	.11
175.	.04	.04	.04	.04	.04	.04	.04	.04	.04
180.	015 015	015	.015	.015	.015	.015	.015	•015	.015
180									
180.	44	=18	0.						
	0.9	0.4	0.5	0.6	0,65	0.7	0.75	0.8	0.85
-180.	04	04 04	04	04	04	04	04	04	-104
-172.	.37	.37	.37	.37	.37	.37	. 37	.37	.37
-168.	35 35	.35	.35	.35	.35	. 35	.35	.35	.35
-164.	.39	.39	.39	.39	.39	.39	.39	.39	.39
-150.	42	.42	.42	. 42	.42	.42	.42	. 42	.42
-150.	445 445	.445	.445	.445	.445	.445	.445	. 445	.445
-130.	.575 .575	.575 .575	.575	.575	.575	.575	.575	.575	.575
-115,	.6	.6	.6	.6	.6	.6	.6	. 6	.6
-90.	.55 .55	•55 •55	.55	•55	.55	.55	.55	.55	.55
-60.	. 4	. 4	. 4	• 4	. 4	. 4	. 4	. 4	. 4
-40.	.26	. 26	. 26	.26	.26	.26	.26	.26	.26
-30.	.18	.18	. 18	.18	.18	.18	.18	.18	.18
-16.	.105	.105		.105		-			
-4.	0075	0075	0065	0105	015	018	0175	.0238	.009
-3.	007	=.007 =.002					0189		.0055
-2,	007 031	0065 0095					01		
-1.	0075 03	0075	0075	0084	0084	0105	009	012	-:0275
0.0							008		

```
-.0435 -.057
       -.0085 -.0085 -.0083 -.009 -.0088 -.0075 -.0125 -.0505 -.0235
1.
       -.05
               -. 0615
              -.009
                      -.0087 -.009 -.0085 -.007 -.025 -.0515 -.037
2.
       -.009
       -.0505 -.068
       -.0093 -.0093 -.009 -.0076 -.006 -.011
                                                   -.0415 -.0525 -.0375
3.
       -.051
              -.072
               -.0095 -.0095 -.006 -.0035 -.0225 -.0525 -.057 -106
4.
       -.01
       -.0655 -.0745
              -.009
       -.01
                      -.009 -.0024 -.005 -.04
5.
                                                    -.0605 -.076 -.084
       -.0825 -.0805
6.
       -.0115 -.0075 -.0085 0.
                                     -.015
                                           -.0505 -.067 -.083 -.0975
       -.0935 -.085
7.
       -.013
              -.0045 -.0078 .0005
                                     -.031
                                            -.058 -.0755 -.0785 -.09
       -.099
              -.091
       -,015
                                     -.0425 -.077
8.
              -.0005 -.007
                            -.011
                                                   -.082 -.089 -.097
              -.096
       -.104
              .006
9.
       .006
                             -.0223 -.0525 -.082
                                                            -.094 -.102
                      -.006
                                                   -.089
       -.1088 -.1009
              .0125
10.
       .0125
                             -.0315 -.0624 -.0869 -.096
                                                            -. 0989 -. 1068
                      -.003
       -. 1137 -. 1058
       .0135
                      .001
11.
              .0135
                              -.0415 -.0723 -.0918 -.101
                                                            -.1028 -.1118
       -.1186 -.1106
                      .0035
       .0035
                             -.0514 -.0822 -.0966 -.1058 -.1087 -.1167
12.
              .0035
       -.1235 -.1155
13.
       -.0185 -.0185 -.005 -.0613 -.0922 -.1017 -.1107 -.1137 -.1215
       -.1285 -.1205
14.
       -.0435 -.0435 -.0565 -.0612 -.1023 -.1065 -.1157 -.1186 -.1266
       ·.1335 -.1255
       -,102
              -.102
                      -.0885 -.0912 -.1122 -.1165 -.1252 -.1285 -.1365
16.
              -.1354
       -.143
       -.175
              -.175
                      -.175
25.
                             ·.175
                                     -.175
                                            -.175 -.175
                                                            -.175 -.175
       -.175
              -.175
                      -.29
       -.29
                                     -.29
                                             -.29
40.
              -.29
                              -.29
                                                    -.29
                                                            -.29
                                                                   -.29
       -,29
              -.29
       -,43
              -.43
                      -. 43
                              -.43
                                     -.43
                                             -.43
60.
                                                    -.43
                                                            - . 43
                                                                   -.43
       -,43
              -.43
       -.58
90.
              -.58
                      -.58
                              -.58
                                     -.58
                                             -.58
                                                    -.58
                                                            -.58
                                                                   -.5A
       -,58
              -.58
115.
       -,63
              -.63
                      -.63
                              -.63
                                     -.63
                                             -,63
                                                    -,63
                                                            -.63
                                                                   -.63
       -,63
              -.63
       .,555
140.
              . 555
                      -.555
                              -.555
                                     -.555
                                            -,555
                                                    -.555
                                                            -.555
                                                                   -.555
       .555
              -.555
160.
       -.43
              -.43
                      -.43
                              -.43
                                     -.43
                                             -,43
                                                    -.43
                                                            -.43
                                                                   -.43
       -,43
              -.43
       -.38
                      -.38
168.
              -.38
                              -.38
                                     -.38
                                            -.38
                                                    -.38
                                                            -.38
                                                                   -.38
       -,38
              -.38
              -.39
                                                    -.39
172.
       -,39
                      -.39
                              -.39
                                     -.39
                                            -,39
                                                            -.39
                                                                   -.39
       -,39
              -.39
       -,28
176.
              .. 28
                      -,28
                              -.28
                                     -,28
                                            -,28
                                                    -.28
                                                            -.28
                                                                   -.28
```

## SAMPLE OUTPUT

## Bearingless Rotor Case

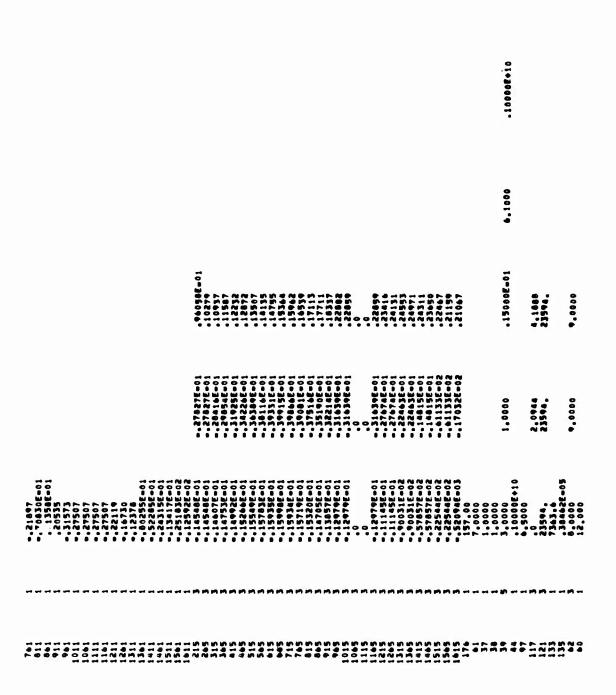


BEST MARINE

••	
**************************************	
•••	
<b>8) 8)</b> என்ன என்ன என்ன என்ன என்ன என்ன என்ன என்	

```
....
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 20000E-07
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ........
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              .14011E+0+
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        .77161E-01
.25265E-01
                                                                                                                                                                                                                                                          7.0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 . 2583
. 2583
. 2583
. 7384
. 7384
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 1018
. 
                                                                                                                                                                                                                                                          15.000
1.0000
```

```
653
                       1.0000
703
                        1.0000
                        1.0000
753
803
                        1.0000
            1
853
             1
                        1.0000
                                            9,6685
             2
                        1,0000
865
                                            9.6685
318
            5
                        1.0000
368
            2
                       1.0000
                                            9,6685
418
             S
                       1.0000
                                            9.6685
            2
                       1,0000
                                            9.6685
468
                       1.0000
            2
                                            9,6685
518
568
             2
                        1.0000
                                            9,6685
             2
618
                        1.0000
                                            9.6685
                                            9.6685
            2
                        1,0000
668
718
                                            9,6685
            2
                       1.0000
            5
                                            9.6685
768
                       1.0000
                                            9.6685
818
            5
                       1.0000
            5
                       1.0000
                                            8.3407
868
            2
                       3,2659
                                            10.640
272
            5
                        3,2659
                                            10,640
322
372
             5
                        3,2659
                                            10.640
                                            10.640
422
            2
                        3.2659
                        3,2659
472
             2
                                            10.640
            2
                        3,2659
                                            10.640
522
                        3,2659
572
                                            10.640
             2
                       3,2659
                                            10.640
955
             2
                       3,2659
                                            10.640
672
722
             2
                        3,2659
                                            10.640
             2
772
                        3,2659
                                            10.640
                                            10.640
                       3,2659
             5
955
872
                        3,2659
            5
                                            10.640
                        13403.
                                            .11463E-06
             2
  3
                                                                 .80000
             3
  6
                        1.5708
                                             . 0
                        1.0000
 56
             1
                       16.000
 34
            1
                       513.97
513.97
274
             1
324
                        513.97
374
             1
424
                        513.97
             1
474
                        513.97
             1
524
                        513.97
574
                       513.97
                        513.97
624
            1
674
                        513.97
                        513.97
724
                        513.97
774
             1
824
                        513.97
             1
874
                        513.97
                                            .50090E-02
                        .16410E-02
167
                      -1,8539
             1
211
105
                      -1,7132
             1
311
                      -1.5720
                      -1,4293
361
411
                      -1.2844
             1
461
                      -1,1368
            1
                      -. 98641
511
                      -,83380
561
                      -.67972
611
             1
661
                      -.52502
             1
                      -.37095
711
```



```
216
              1
                         -. 30610E-01
 266
              1
                         -. 30610E-01
 316
               1
                         -.31258E-01
 366
              1
                         -.32839E-01
 416
              1
                         -.35118E-01
 466
                         -. 37649E-01
              1
 516
              1
                         -.40028E-01
 566
              1
                         -. 41928E-01
 616
              1
                         -. 43264E-01
 666
              1
                         -.43907E-01
 716
              1
                         -. 43853E-01
 766
              1
                         -.42989E-01
 816
              1
                         -.41268E-01
 866
              1
                         -. 38709E-01
 916
              1
                         -. 35435E-01
 966
              1
                         -. 34803E=01
1016
              1
                         -.34803E-01
1166
              1
                         -.34803E-01
1216
              1
                         -.30441E-01
1266
              1
                         -.30441E-01
1316
              1
                         -. 24709E-01
1366
              1
                         -. 24709F-01
1416
              1
                         -.16297E-01
1466
              1
                         -.16297E-01
1516
              1
                         -.67200E-02
1566
              1
                         -.67200E-02
1616
              1
                         -.18700E-02
                          . 0
  35
              1
                          2.0000
  65
              1
  48
              1
                          1,0000
  49
              1
                         -14,600
  54
              1
                          48.600
```

MELICOPTER AERDELASTIC STABILITY ANALYSIS INPUT BARAMETERS

OO AKE BE COLORED BE C			
TOO LOOP TO COO COO COO COO COO COO COO COO COO	CRAFT VEL. COLL. ANGLE B SHAFT FLEX. B DAMPING CCT B COR!		
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		CONTRACTOR	POPPER DE LE COMPANION DE LE C
MATANA BANA BANA BANA BANA BANA BANA BANA	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	FTA 628V. B 0.0 PHAI C 0.0 PHAI A C 0.0 NG CYCLIC B 0.005009 NG CYCLIC B 0.005009 UN EIZ 0.789880 THECCI;	
### ##################################	ALPHAI GRAV, ACC, B LONG CYCLIC B BPUR EIZ	A1 ACC	
HUTH RHWI Ph 4IP		1638	90 BLB1
0 % > 0	00	0.000000000000000000000000000000000000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
ONO 2 > 2 2	FREG SATEP F/A CYCLIC SPUR EIY COES	**************************************	50 60 00 00 00 00 00 00 00 00 00 00 00 00
7 4 6 4 7 4 6 4		68 ARRENTE 8 0.0 PARCA BYTE 8 0.0 PARCA CYCLI BYTE CARLO COLO PARCA CYCLI COLO PARCA CYCLI COLO COLO COLO COLO COLO COLO COLO C	TARCO MIRE OF TA
# # #   O   O   O   O   O   O   O   O	0.0 2.58220 2.58220	0.25.00 2.5822 0.25.00E	20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00 20.00
			0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
2	SPUR LENGTH	BATA: DAMPING COE2 CENGTH COE2 CALLACTI B 0.0	## 100 E

STARTING EIGENVALUE 1 # .0.1440600E+02 0.4840001E+02

FOR ISER EQUAL 1 ONLY CCS ARRAYS ARE INPUTTED 39 11 0.3000 0.4000 0.5000 0.6000 0.7000 0.7500 0.8000 0.8500 0.0 0,9000 1,0000 -180.0 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 -174.0 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 -170.0 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 0.6500 -166.0 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 0.6200 -133.0 0.8650 0.8650 0.8650 0.8650 0.8650 0.8650 0.8650 0.8650 0.8650 0.8650 0.8650 **-113.0 0.6350 0.6350 0.6350 0.6350 0.6350 0.6350 0.6350 0.6350 0.6350** 0.6350 0.6350 **-58.0-0.8900-0.8900-0.8900-0.8900-0.8900-0.8900-0.8900-0.8900-0.8900** -0.8900-0.8900 -38.0-1.1400-1.1400-1.1400-1.1400-1.1400-1.1400-1.1400-1.1400-1.1400-1.1400 -1.1400-1.1400 -20.0-0.9800-1.0300-1.0700-1.1300-1.1400-0.8660-0.8600-0.8450-0.7400 -1.0100-1.3400 -15.0-1.1650-1.2250-1.2850-1.2300-1.1300-0.8800-0.8920-0.8270-0.6850 -1.0100-1.3400 -13.5-1.2200-1.2800-1.3300-1.2600-1.1200-0.8800-0.8850-0.8140-0.6770 -1.0100-1.3400 -12.0-1.0950-1.1500-1.2000-1.1400-1.0920-0.8600-0.8770-0.7910-0.6550 -1.0100-1.2500 -9.5-0.8900-0.9300-0.9700-0.9300-1.0500-0.8300-0.8500-0.7700-0.6200 -0.9470-1.1000 -5,5=0.4700=0.4930=0.5100=0.5500=0.5850=0.6400=0.6880=0.6500=0.5800 -0.4100-0.6100 -4.0-0.3120-0.3300-0.3350-0.3600-0.3900-0.4100-0.5000-0.4750-0.2800 -0.2200-0.4300 -2.0-0.1000-0.1070-0.1050-0.1150-0.1200-0.1200-0.1270-0.1600-0.1650 -0.0850-0.1850 0.0100 0.0250 0.0150 0.0500-0.0050 0.0 -1.0 0.0 0.0 0.0 -0.0150-0.0600 0.0 0.1100 0.1100 0.1200 0.1300 0.1400 0.1700 0.1900 0.2400 0.0400 0.1100 0.0600 2.0 0.3200 0.3320 0.3500 0.3750 0.4100 0.4750 0.4850 0.3700 0.2080 0.3900 0.3000 3.0 0.4250 0.4430 0.4670 0.5000 0.5470 0.6200 0.5000 0.4150 0.2600 0.5200 0.4260 4.0 0,5300 0,5500 0,5600 0,6200 0.6800 0,6750 0,5700 0,4750 0,2800 0,6300 0,5450 0.7420 0.7720 0.8150 0.8680 0.9100 0.7670 0.6700 0.5100 0.3200 0.9200 0.7870 8.0 0.9500 0.9950 1.0350 1.1150 0.9950 0.8560 0.7320 0.5450 0.3550 1.1900 1.0300 10.0 1.1650 1.2200 1.2600 1.2700 1.0750 0.9420 0.7910 0.5800 0.3930 1,1900 1,0950 11.0 1.2680 1.3280 1.3800 1.2780 1.0920 0.9850 0.8250 0.6000 0.4130 1,1900 1,0950 12.0 1.3750 1.4400 1.4200 1.2500 1.1130 1.0280 0.8520 0.6150 0.4320 1,1900 1,0950 13.0 1.4800 1.5500 1.3950 1.2250 1.1300 1.0690 0.8850 0.6330 0.4500

```
1.1900 1.0950
  13.5 1.5300 1.6000 1.2700 1.2070 1.1410 1.0900 0.9000 0.6410 0.4610
       1.1900 1.0950
  14.0 1.5850 1.0950 1.1400 1.1900 1.1500 1.1120 0.9130 0.6500 0.4700
       1.1900 1.0950
  15.0 0.9150 0.9620 1.0000 1.1920 1.1700 1.1550 0.9460 0.6680 0.4900
       1.1900 1.0950
  20.0 1.0000 1.0500 1.0900 1.2000 1.2600 1.3670 1.1000 0.7600 0.5900
       1,1900 1,0950
  38.0 1.1350 1.1350 1.1350 1.1350 1.1350 1.1350 1.1350 1.1350 1.1350
       1.1350 1.1350
  58.0 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900
       0.8900 0.8900
 113.0-0.6350-0.6350-0.6350-0.6350-0.6350-0.6350-0.6350-0.6350-0.6350-0.6350
      -0.6350-0.6350
 133.0-0.8650-0.8650-0.8650-0.8650-0.8650-0.8650-0.8650-0.8650-0.8650-0.8650
      -0.8650-0.8650
 150.0-1.0000-1.0000-1.0000-1.0000-1.0000-1.0000-1.0000-1.0000-1.0000-1.0000
      -1.0000-1.0000
 166,0-0.7200-0.7200-0.7200-0.7200-0.7200-0.7200-0.7200-0.7200-0.7200-0.7200
     -0.7200-0.7200
 170.0-0,8200-0,8200-0,8200-0,8200-0,8200-0,8200-0,8200-0,8200-0,8200-0,8200
      -0.8200-0.8200
 180.0 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400
      0.0400 0.0400
 11
      45
      0.0
              0.4000 0.5000 0.6000 0.6500 0.7000 0.7500 0.8000 0.8500
      0,9000 1,0000
-180.0 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150
      0.0150 0.0150
-175.0 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400
      0.0400 0.0400
-170.0 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100
      0.1100 0.1100
-164.0 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200
      0.2200 0.2200
-155.0 0.5100 0.5100 0.5100 0.5100 0.5100 0.5100 0.5100 0.5100 0.5100
      0.5100 0.5100
-130.0 1.0800 1.0800 1.0800 1.0800 1.0800 1.0800 1.0800 1.0800 1.0800
       1.0800 1.0800
-100.0 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100
       1,5100 1,5100
-90.0 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600
       1,5600 1,5600
-80.0 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100
      1,5100 1,5100
-60.0 1.2400 1.2400 1.2400 1.2400 1.2400 1.2400 1.2400 1.2400
       1.2400 1.2400
-40.0 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000
      0,9000 0,9000
0.5100 0.5100
 -8.0 0.0205 0.0205 0.0670 0.1360 0.1375 0.1405 0.1440 0.1700 0.1818
      0.1930 0.2175
 -6.0 0.0154 0.0154 0.0300 0.0750 0.0765 0.0790 0.0870 0.1150 0.1270
      0.1380 0.1615
 -4.0 0.0112 0.0112 0.0115 0.0141 0.0163 0.0182 0.0287 0.0600 9.0715
      0.0830 0.1062
  -3.0 0.0107 0.0107 0.0109 0.0123 0.0133 0.0144 0.0117 0.0322 0.0448
      0.0625 0.0890
```

```
-2.0 0.0104 0.0104 0.0104 0.0105 0.0104 0.0107 0.0110 0.0137 0.0284
     0,0425 0,0715
 -1.0 0.0105 0.0105 0.0103 0.0104 0.0104 0.0105 0.0104 0.0177 0.0373
     0.0512 0.0812
 0.0 0.0106 0.0106 0.0102 0.0102 0.0103 0.0103 0.0131 0.0287 0.0445
     0.0600 0.0910
 1.0 0.0105 0.0105 0.0103 0.0104 0.0107 0.0119 0.0217 0.0474 0.0631
     0.0790 0.1105
 2.0 0.0104 0.0104 0.0104 0.0105 0.0112 0.0166 0.0384 0.0659 0.0820
     0.0975 0.1293
 3.0 0.0106 0.0106 0.0107 0.0118 0.0150 0.0298 0.0569 0.0848 0.1010
     0,1165 0,1485
 4.0 0.0108 0.0108 0.0110 0.0131 0.0236 0.0484 0.0755 0.1035 0.1195
     0.1350 0.1670
 5.0 0.0114 0.0114 0.0118 0.0191 0.0345 0.0670 0.0944 0.1220 0.1383
     0.1530 0.1860
 6.0 0.0120 0.0120 0.0125 0.0293 0.0530 0.0860 0.1130 0.1410 0.1570
     U.1720 0.2050
 7.0 0.0127 0.0127 0.0133 0.0426 0.0720 0.1047 0.1319 0.1600 0.1760
     0.1915 0.2230
 8.0 0.0133 0.0133 0.0153 0.0610 0.0905 0.1235 0.1505 0.1788 0.1950
     0.2100 0.2425
 9.0 0.0137 0.0137 0.0212 0.0798 0.1092 0.1422 0.1693 0.1980 0.2135
     0.2290 0.2610
 10.0 0.0153 0.0153 0.0300 0.0983 0.1275 0.1607 0.1880 0.2170 0.2320
     0.2480 0.2800
 11.0 0.0175 0.0175 0.0483 0.1180 0.1465 0.1790 0.2070 0.2360 0.2505
     0.2660 0.2990
 12.0 0.0205 0.0205 0.0670 0.1357 0.1650 0.1985 0.2250 0.2560 0.2700
     0.2850 0.3180
 13.0 0.0282 0.0282 0.0858 0.1545 0.1835 0.2170 0.2440 0.2750 0.2890
     0.3040 0.3365
 15.0 0.0465 0.0465 0.1233 0.1920 0.2210 0.2540 0.2610 0.3135 0.3265
     0.3400 0.3740
 30.0 0.6600 0.6600 0.6600 0.6600 0.6600 0.6600 0.6600 0.6600 0.6600
     0.6600 0.6600
 50.0 1.0700 1.0700 1.0700 1.0700 1.0700 1.0700 1.0700 1.0700 1.0700
     1,0700 1,0700
 80.0 1.5000 1.5000 1.5000 1.5000 1.5000 1.5000 1.5000 1.5000 1.5000
     1,5000 1,5000
 90.0 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600 1.5600
     1.5600 1.5600
100.0 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100 1.5100
     1,5100 1,5100
120.0 1.2300 1.2300 1.2300 1.2300 1.2300 1.2300 1.2300 1.2300 1.2300
     1,2300 1,2300
140.0 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900 0.8900
     0.8900 0.8900
155.0 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000 0.5000
     0.5000 0.5000
164.0 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200 0.2200
     0.2200 0.2200
170.0 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100 0.1100
     0.1100 0.1100
175.0 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400 0.0400
     0.0400 0.0400
180.0 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150 0.0150
     0.0150 0.0150
     44
11
     0.0
            0.4000 0.5000 0.6000 0.6500 0.7000 0.7500 0.8000 0.8500
```

```
0.9000 1.0000
-180.0-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400
      -0.0400-0.0400
-172.0 0.3700 0.3700 0.3700 0.3700 0.3700 0.3700 0.3700 0.3700 0.3700
       0,3700 0,3700
-160.0 0.3500 0.3500 0.3500 0.3500 0.3500 0.3500 0.3500 0.3500 0.3500
       0.3500 0.3500
-164.0 0.3900 0.3900 0.3900 0.3900 0.3900 0.3900 0.3900 0.3900 0.3900
       0.3900 0.3900
-156.0 0.4200 0.4200 0.4200 0.4200 0.4200 0.4200 0.4200 0.4200 0.4200 0.4200
       0.4200 0.4200
-150.0 0.4450 0.4450 0.4450 0.4450 0.4450 0.4450 0.4450 0.4450 0.4450
       0.4450 0.4450
-130.0 0.5750 0.5750 0.5750 0.5750 0.5750 0.5750 0.5750 0.5750 0.5750
       0.5750 0.5750
-115.0 0.6000 0.6000 0.6000 0.6000 0.6000 0.6000 0.6000 0.6000 0.6000
       0.6000 0.6000
 ■90.0 0.5500 0.5500 0.5500 0.5500 0.5500 0.5500 0.5500 0.5500 0.5500
       0.5500 0.5500
 -60.0 0.4000 0.4000 0.4000 0.4000 0.4000 0.4000 0.4000 0.4000 0.4000 0.4000
       0.4000 0.4000
 -40.0 0.2600 0.2600 0.2600 0.2600 0.2600 0.2600 0.2600 0.2600 0.2600
       0.2600 0.2600
 -30.0 0.1800 0.1800 0.1800 0.1800 0.1800 0.1800 0.1800 0.1800 0.1800
       0.1800 0.1800
 -16.0 0.1050 0.1050 0.1050 0.1050 0.1050 0.1050 0.1050 0.1050 0.1050
       0.1050 0.1050
  -4.0-0.0075-0.0075-0.0065-0.0105-0.0150-0.0180-0.0175 0.0238 0.0090
       0.0200 0.0050
  -3.0-0.0070-0.0070-0.0067-0.0091-0.0112-0.0150-0.0189 0.0090 0.0055
      -0.0060-0.0020
  -2.0-0.0070-0.0065-0.0070-0.0075-0.0075-0.0120-0.0100-0.0130 0.0040
      -0.0310-0.0095
  -1.0-0.0075-0.0075-0.0075-0.0084-0.0084-0.0105-0.0090-0.0120-0.0275
      -0.0300-0.0350
   0.0-0.0080-0.0080-0.0080-0.0090-0.0090-0.0090-0.0090-0.0080-0.0330-0.0215
      -0.0435-0.0570
   1.0-0.0085-0.0085-0.0083-0.0090-0.0088-0.0075-0.0125-0.0505-0.0235
      -0.0500-0.0615
   2.0-0.0090-0.0090-0.0087-0.0090-0.0085-0.0070-0.0250-0.0515-0.0370
      -0.0505-0.0680
   3,0-0,0093-0,0093-0,0090-0,0076-0,0060-0,0110-0,0415-0,0525-0.0375
      -0.0510-0.0720
   4.0-0.0100-0.0095-0.0095-0.0060m).0035-0.0225-0.0525-0.0570-0.0600
      -0.0655-0.0745
   5.0-0.0100-0.0090-0.0090-0.0024-0.0050-0.0400-0.0605-0.0760-0.0840
      -0.0825-0.0805
   6.0-0.0115-0.0075-0.0085 0.0
                                   -0.0150-0.0505-0.0670-0.0830-0.1975
      -0.0935-0.0850
   7.0-0.0130-0.0045-0.0078 0.0005-0.0310-0.0580-0.0755-0.0785-0.0900
      -0.0990-0.0910
   8.0-0.0150-0.0005-0.0070-0.0110-0.0425-0.0770-0.0820-0.0890-0.0970
      -0.1040-0.0960
   9.0 0.0060 0.0060=0.0060=0.0223=0.0525=0.0820=0.0890=0.0940=0.1020
      -0.1088-0.1009
  10.0 0.0125 0.0125-0.0030-0.0315-0.0624-0.0869-0.0960-0.0989-0.1068
      -0.1137-0.1058
  11.0 0.0135 0.0135 0.0010-0.0415-0.0723-0.0918-0.1010-0.1028-0.1118
      -0.1186-0.1106
  12.0 0.0035 0.0035 0.0035-0.0514-0.0822-0.0966-0.1058-0.1087-0.1167
```

6

```
-0.1265-0.1205
 14.0-0.0435-0.0435-0.0565-0.0612-0.1023-0.1065-0.1157-0.1166-0.1266
     -0.1335-0.1255
 16.0-0.1020-0.1020-0.0865-0.0912-0.1122-0.1165-0.1252-0.1265-0.1365
     -0.1430-0.1354
 25.0-0.1750-0.1750-0.1750-0.1750-0.1750-0.1750-0.1750-0.1750-0.1750
     -0.1750-0.1750
 40.0-0.2900-0.2900-0.2900-0.2900-0.2900-0.2900-0.2900-0.2900-0.2900
     -0,2900-0,2900
 60.0-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300
-0.4300-0.4300

90.0-0.5800-0.5800-0.5800-0.5800-0.5800-0.5800-0.5800-0.5800

-0.5800-0.5800
115,0-0,6300-0,6300-0,6300-0,6300-0,6300-0,6300-0,6300-0,6300-0,6300
     -0.6300-0.6300
140.0-0.5550-0.5550-0.5550-0.5550-0.5550-0.5550-0.5550-0.5550-0.5550
     -0.5550-0.5550
160.0-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300-0.4300
+0,4300-0,4300
165.0-0,3800-0,3600-0,3600-0,3600-0,3600-0,3600-0,3800-0,3800
-0.3800-0.3600
172.0-0.3900-0.3900-0.3900-0.3900-0.3900-0.3900-0.3900-0.3900
     -0.3900-0.3900
176.0-0.2800-0.2800-0.2800-0.2800-0.2800-0.2800-0.2800-0.2800-0.2800
     -0,2800-0,2800
180.0-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400-0.0400
     -0.0400-0.0400
                                  STEADY FORCES AND MOMENTS
  SECTION
                             VV
                                            VZ
                                                                          MZ
                                                                                         MY
```

0.27087E+04 +0.33871E+01 +0.85743E+02 0.48235E+02

0.16685E+04

13.0-0.0185-0.0185-0.0050-0.0613-0.0922-0.1017-0.1107-0.1137-0.1215

-0,1235-0,1155

		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
COEFFICIENTS	91444444444444444444444444444444444444	
AERO		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
		777 748 748 748 748 748 748 748 748 748
		40000000000000000000000000000000000000

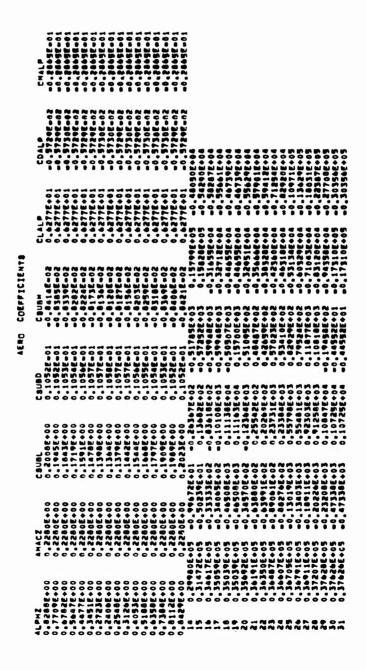
	C C C C C C C C C C C C C C C C C C C	
COEFFICIENTS		
AERO		
		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0

			36.04
			3E+03 +0.67823E+04
COEFFICIENTS	00000000000000000000000000000000000000	danseradone m hobbedendenden hobbedendendenden hommendendendende	C
A.E. R.O.			E-03 -00-34380E-03
		e du de e	+O1 CPIRAGES
			*03 *0*/3300E*01
			1.12110

COEFFICIENTS	
AERO	

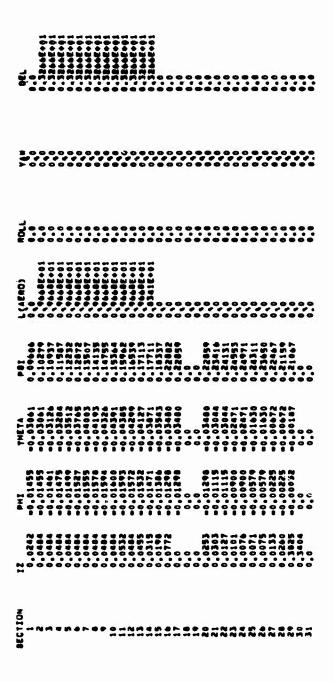
COEFFICIENTS		2
AERO	DESCRIPTION OF THE PROPERTY OF	00000000000000000000000000000000000000

			8E+04
			E+05 =0.45844E+04
COEFFICIENTS		COEFFICIENTS	E+03 0.15040E+05
AERO		AERO	+02 =0,45351E+03
			.02 -0.42038E+02
	# # # # # # # # # # # # # # # # # # #		5 -0.173136+02
			13 0.28425E+05



ORDER OF SECTIONS: BLADE TIP(SECTION 1) TO HUB, THEN FROM FREE END OF FUSELAGE (SECTION 1) TO HUB SECTION INPUT DATA

12	•	•	- c	Ö	<b>6</b> .	Č	0	•	•	·	•	•	C	•	•	•	c	•	c	•	•	•	•	. c	•	0	C	c	•	c	c	0
**	7000				0 0 0	9000	0.048	0.048	0.048	0.048	0.00	0.053	0.048	0.045	0.031	0.020	0.077	0.0	0.0	0	0.025	0.030	0.013	0,010	0.00	0.007	0.00	0.013	0.026	0.383	0.340	0.0
> 0 7				10.0		100	-1.137	40.00	.0.834	-0.480	-0.525	-0.371	-0.21	0.071	6.071	0.205	-0.316	00.875	-0.274	-0.275	-0.275	-0.221	-0.167	-0.124	00.00	-0.052	-0.024	-0.013	200.00	100.0-	0.0	0.0
×	101.170	181.702	110		700	154.696	145.027	135,350	125.691	116.022	104.354	96.685	87.016	77.348	67.680	58.011	51.475	46.342	48.342	48.342	48.342	43.508	30.674	33.640	20.005	24.171	19.337	14.503	9.668	4.834	0.0	0.0
F.8 V	414	414	414				-0.414	.0.616	-0.616	-0.616	-0.616	-0.616	-0-616	-0.186	-0.01	.0.112	0.0	0.0	0.0	0.0	0.0	0.0	0.0	c • 0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
r	0.00708	6 . 0 . 0			100000	000000	0.00174	0.00774	0.00774	0.00774	0.00774	0.01543	0.00774	000000	0.01161	0.01300	0.03087	0.00462	0.0	0.0	0.00662	0.00574	0.00201	902000	0.00200	0,00212	0.00225	0.00446	0.01545	0.04450	0.02603	••
7.	0.0	0				0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	••	0.0	0.0	0.0
î	0.0	0	0		•		0		0.0	0.0	0.0	0.0	0.0	0.0	0.0	•	0.0	0.0	•	0.0	0.0		0.0	•	•	0.0	0.0	•	•	0.0	0	••
I	0.0	0.0	0		•		0.0	0.0	0.0	.0	0.0	0.0	0.0	•	0.0	0.0	•	••	0.0	0.0	0.0	0.0	••	0	0.0	0.0	0.0	0.0	•	0.0	0.0	0
Ŧ	0.0	0.1	0 - 1				•	0.	•	••	••	•	•		•	••	•	•	•	0.0	0.0	:	•	-	•	•	- -	••	-	•		•
ř	0.0	1.0	0			•	0		:	1.0	1.0	0.	0.1	1.0		•	0.0	0.0	•	0.0	0.0	0.0	•	•	•	•	0.0	••	•	0.0	0	•
ĩ	9	1.0	9.1			•	0.	-0		•		•		•	·:	0.	•	•		•		-	•	-	~	-	-	-	: :	•		
ī	1.0	0	0.1					0	:		1.0			•	••	••	••	•	•	••	•	•			•	•	•	••	•	•	•	•
SECTION		~	-	•		n .	• 1	-	•	•	2	-	~	2	=	5	-	14	=	=	0	2	25	2	2	S:	2	~	2	2	e i	=



SECTION D	DEL 4 D	) Y 130	OFL Z	21.002	VVeRTC	VZebie	1/4 %	***		•			
	_				0.0						2	-	•
~											0	0	
			•	•	•	•	•	0.0	0			0	
•		•		0.0	0.0	•	0.0	0.0	••	6	0	0	
•		6.0	0.0	0.0	0.0	0.0	0.0	0.6	0.0			•	
•		0.0	0.0	0.0	0.0	0.0	0.0						
•		0.0	0.0	0.0	0.0	0.0							
•		0.0								•			
•									•			0	
•					•			0.0	•	6	6	c c	
• (		0.0	0	0		•	0.0	0.0	••	6	6.0	0.0	
2		٥.	0.0	••	0.0	0	••	0.0	0.0	0.0	0.0	0.0	
=		0.0	0.0	0.0	6.0	0.0	0.0	0.0	0.0	0	0	0	
~		٠.	0.0	0.0	0.0	0.0	0.0	0.0	0.0	•	c		
2		0.0	0.0	0.0	0.0	0.0	0.0						
=		0.0	0.0	0.0	0.0	0	0						
		0.0	0.0								•		
•		0.406							•				
=													
::											0.0	0	
								0.0	0.0	•	0.0	0.0	
.;		•			0.0	0.0	9	0.0	•	•	0.0	0.0	
5:			0.0	0	0		0	0.0	•••	0.0	0.0	0.0	
3:		0			0.0	•		0.0	0.0	e,	6	0.0	
3:		0.0	0	•	0	•	•	0.0	0.0	0	0.0	0.0	
2		0.0	0.0		•	0.0	0.0	0.0	0.0		0.0	0,0	
2		0.0	••	0.0	••	0.0	0.0	0.0	0.0		0	0.0	
2			0.0	0.0	••	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
~		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0	0.0	
2		0.0	0.0	0.0	•••	0.0	0.0	0.0	0.0	0.0		0	
2		0.0	0.0	0.0	0.0	0.0	•	0.0	0.0	0			
2		0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0				
=	••	0.0	0.0	0.0	•••	0.0	0.0	0.0	0.0		0.0	0	
					S VALUES	1 OF UPDA1	TED LAMB	IS VALUES OF UPDATED LAMBDA MATRIX					
1.00000+00	0.0	1.1	1.00000+00	••	-	1.00000+00	0.0	1.00000+00	0.0	1,000	000000	٥٠٥	
1.00000+00	0.0	:	1.00000+00	0.0	=	1.00000+00	0.0	1.00000+00		000	00+00		
1.00000001	0.0	:	1.00000+00	•	-	1.00000+00	0.	1.00000+00	0.	1.000	1.00000001	0	
OTPHAS .			0.00050	0.44654653857014645+00	404D+00		-	-0.82799737627064620-0	10-0299				
DOLADY		•	0.100636132370760+02 -0.20062092642177360-02	9264217	7300-02		-	-0.36429403227446988-02	500-05				
INITIAL EIGENVALUE		-14.60	•	•	30	DETERMINANT .		3861D+16 4127D+16	•:•				

15 VALUES OF UPDATED LAMBDA MATRIX

```
0.0 5.42100-20 0.0 1.62830-19 0.0 3.38610-21 8.64890-03 1.91890-03 -7.3860-09 1.1860-08 -1.3860-09 1.1860-08 1.1860-08 5.7.8600-09 1.81800-01 1.1860-09 1.8680-09 1.1860-09 1.1860-09 1.1860-09 5.0880-19 1.1860-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.8880-09 1.88
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            6.2884D=03 -7.9165D=04 7.9382D=04 2.5174D=04
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  LABT EIGEN VALUE 8-0,1867300-02 0,8884300-02 CURRENT EIGEN VALUE 8-0,1861110-02 0,8024070-02 NEXT EIGEN VALUE 8-0,1462250-02 0,8028130-02
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     LAST DETERMINANT VALUE m 0,1250200-19-0,1240-55-18
CURRENT DETERMINANT VALUE m 0,125020-13 0,2159260-13
ELEN VALUE CONVERGENCE m 0,29087965-03
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      LAST EIGEN VALUE mes,1461110+02 0.4020070+02 CURRENT EIGEN VALUE mes,1462250+02 0.4028130+02 NEXT EIGEN VALUE mes,1462220+02 0.4028120+02
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    -0.21252728436244860-02
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                -0,200081+0+8534+950+00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              LAT DETERMINANT VALUE mo.202300-16-0.2280098-16-CURRENT DETERMINANT VALUE mo.20200-16-0.128809-18-0.128809-18-0.128809-18-0.128809-18-0.128809-18-0.128809-18-0.128809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.18809-18-0.1880
                                                                                                                                                                                                                                                                                                                                                                                                 -0.12338508902127470+00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          0.10209905842844905-64
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              -0.19430333640850910+00
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        0.14740782545402400-05
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           15 VALUES OF UPDATED LANDDA HATRIX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             15 VALUES OF UPDATED LAMBDA MATRIX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       VALUES OF UPDATED LAMBDA MATRIX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 .
                                                                                                                                                                                                                                                                                                                                                                                       0.00235886644258430+00
0.18091561807308190+02
=0.21208492199500950=02
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0.180863151868340+02
0.18086315186880030+02
0.1008403723818000033
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    0.98014069703080888400
0.18090108279282128+02
=0.18933488627147980=09
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ..
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ..
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         DTPHAS B
DTLG19 B
DPIVOT B
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    07610 0
07610 0
                                                                                                                                                                                                                                                                                                                                                                             076448 .
07610 .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        :
```

4

```
0.955210896371380-09
                                                                                                                                                                       LAST DETERMINANT VALUE 8-0,18428-20-13 0,21652-0-13 CURRENT DETERMINANT VALUE 8 0,1462450-10 0,8008020-00 E1GEN VALUE CONVERGENCE 8 0,5062006-00
                                                                                                                                                                                                                                                                   LAST EIGEN VALUE m-8,1442250+02 0.4428130+02
CURRENT EIGEN VALUE m-8,1468220+02 0.4428120+02
NEXT EIGEN VALUE m-0,1462220+02 0.4428120+02
                                                                               .0.1982001708786012D+00
                                                                            0.1804888418073150+02
0.1804888418873150+02
0.180581588787888888
                                                                        DTEMAS S
DTLEIO S
DPIVOT S
```

AEROELAGTIC GTABILITY GTATE VECTORS

SAASHPLATE DEFLECTIONS

	<b>.</b>	(LOCAL AXTS SYS.)	UZ. VERT. DEFL. (+. URMARD)		ellechontelos el. Molfred
2 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 O PER REV SMAPE VECTOR(LNCAL AXTS SYS.)	UV. INPLANE DEFLY (+, ROTATION DIR.)	1	SE TON THE TANK THE T
		BLADE :	UX, RADIAL DEFL. (+, GUTBOARD)	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	-
			SECTION		35.0

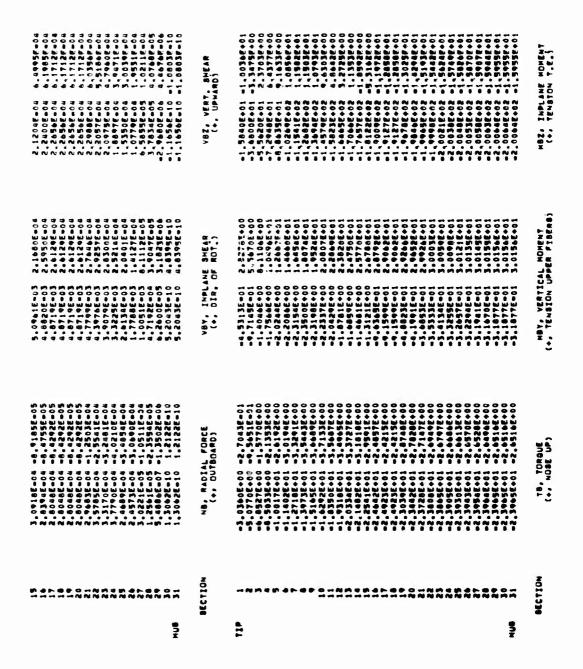
1

-

2 2 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	A TENED ON THE PROPERTY OF THE PROPERTY ON THE	11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	0.000000000000000000000000000000000000	
	S.1070E-07 -1.2435E-05 1.3062E-10 1.2122E-10 1.3062E-10 1.2122E-10 N. AXIAL FURCE (+, RADIAL DUTBURD)	### ### ##############################
	BUNNO BUNDO	- N M 경 M 용 C

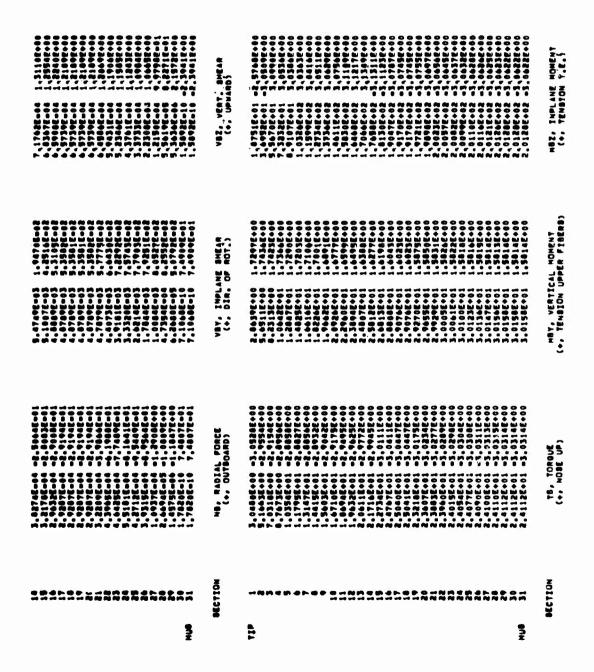
-1.9339E 02 -2.2617F 01 -1.9407E 02 -2.25617F 01 -1.9407E 02 -2.2503F 01 -1.959ZF 02 -2.1902F 01 -1.959ZF 02 -2.1902F 01 -1.064F 02 -1.595SF 01	4 Z. CHORDEIGE HOMBET (++TENGION 7.E.)	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1
2.52676.01 2.58226.01 2.585786.01 2.585786.01 2.61556.01 3.615586.01		
-4.9897E+01.2 -4.9811E+01.2 -4.5014E+01.2 -4.5014E+01.2 -4.2792E+01.2 -4.1877E+01.3	I V. FLABILOE MOMENT (+) TENSION UPPER FIDERS)	
-2.8645E+01 -3.3277E+00 -2.710/E+01 -3.097E+00 -2.7206E+01 -3.097E+00 -2.5310E+01 -2.8276E+00 -2.5311E+01 -2.8276E+00 -2.4306E+01 -2.8276E+00 -2.430E+01 -2.8516E+00 -2.3985E+01 -2.8516E+00	T, TIRQUE (+) NUSE UP)	9. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5.
# IN 4 F 0 0 0 10 P P P P P P P P P P P P P P P	SECTION	

<b>3</b> £C 11UN	UBK, RADIAL DEFL	L DEFL.	UBY, INPLANE DEFL. (+, ROTATION DIR.)	UBZ, VPRT, DEFL. (*, UPHARD)
-	3,72186-02		1.5902E-02 1.2792E-01	-1.0024E+00 1.2295F=02
~ .	3.53565-02	3.6396E=04	1.6100E=02 1.1888E=01	
•	30 8 30 8 30 8 30 8 30 8 30 8 30 8 30 8			-8.8025E-01 2.1262F-02
	ACTOR C		1.0303E-04 1.017@E-01	NOTATION NOTES OF THE PARTY OF
•	2.6862E-02	7.8096F=05		
•	2.43926-02			MODELPOOP TO TOTAL PROPERTY OF
•	2.1801E-02	2.8414E-04		SOURCE OF THE STATE OF THE STAT
•	1.9146E=02	3.8386E-04	53436-02	POSENCOPY RE TO LOCOTO
01	1.64785-02	4.55576.64	4746E=02	10 mm
=	1.36495-02	4.6296E-04		TO SECTION
~	1.1322E-02	4.52236-04		-3,3062E=01 -1,1921E=02
=	8.040SE=03	3.7229E=04		-2,7391F-01 -1,2622F-02
<u>.</u>	6.830SE-03			
51	4. ** 545E = 03			
•	3.3954E=03	3.6489E=04		-1.3570F-01 -0.0564F-03
<u> </u>	2.65475=03		.2768E-03	
2:	2.65475-03		.2768E-03	
2,	2.85475-03	5.1137E=04	.2748E+03	
2 :	2.8547E-03		.2768E-03	
	C.1314E=03	*	. C. 163E=03	9.7074E-02 -6.9476F
:2	9.3570E=04	1.0833E+04	10012/2000 00012/2000 P	NOTES NOTES OF SOUTH
*	4.9306E-04	5.7024E=05	2182E-03	-2 8046
52	2.5279E=04	2.91126-05		
*	7.4284E-05	A.3447E-06		1.1932F-02
۲,	2.7477E-05	3.0331E-06	. 4020E-04	
	2.3562E=00	2.3624E=07	8.2734E=05 1.2267E=04	1.4851E-03
9	1.6626E-10	1.51946-10	1921F=06 2-922F=0	#081400000000000000000000000000000000000
ž	1.66262-10	1.51946-10	.1941E=09 2.9429E=0	+1, 4256fa08 +1,3161fa08
SECTION	a market			
		UPWARD)	(+ TW DORNEARD)	C.FOR PO. BEG BEF .+)
-	40.740.4	40-145-5		
~	8.9207E-04		6-3010E03 0-9150F004	
-	8.8458E=04			
•	8.6631E-04		•	
•	8.4000E=04		-4.1071	
• •	0.0714E-04	1.13046-04	.4233E-03	4.4163F-05 8.034SF-04
- 4		60-2/9276	. 3952E = 03	
•	6.7767E=04	1.8855F=05	A DECEMBER OF THE DESCRIPTION	6.6495E-05 7.7840F-04
0.7	D-25346-04	A. 6481F=06		
=		-2.0918E-05		CONTRACTOR -
21	.0736E-04	-6.1082E-0		100
2	#023E-04	-8.8452E-05	.7472E-03	•



DISK PLANE AXIS SVSTEM - POLAR COGROINATES

UBZ, VERT, DEPL.	C
PL. UBY, IMPLANE DEFL.	DE
UBX, RADIAL DEFL. (+, QUTBOARD)	
96C710W	



### SUMMARY OF PREDICTED HODES DAMPING FREG CONVERGENCE PREDOMINANT RAD PER SEC PER REV CRITERIA SATISFIED

YES

1.1073

0.4928120+02

HODE TYPE

VERTICAL

HODE

1 -0,1402220+02

### ADDITIONAL SAMPLE CASES

### Sample Input (Flexstrap Case)

```
21125.66
  3113400.0
  41.000000115
  81.8
 1511.0
 1711.0
 1814.0
 19125.0
 2011.0
 2411.0
 2511.0
 2611.0
 31116.0
 3311.0
 3418.0
 3750.0
                   0.0
                                  3.0
                                                                .0285
                   9.0000000E+149.0000000E+14
 4233.44
 451.0000086
 4611.0
 4812.0
 492-28.0
                   2.4
 542175.00
                   204,40
 59150.0
 60110.0
 6117.0
 62111.0
 63112.0
 64112.0
 6512.0
11740.0
                   2.0944
                                  4.1888
12149.0000000E+169.00000000E+169.0000000E+169.0000000E+16
13316700.0
1351.00000134
1471.35457
1531,81211
159111.22
17926,128824
                   100000000.
181220000000,0
                   20000000.0
                   -.025075
18322.789096
20111.0
2085.000244
                   -. 9324
                                  60,75
                                                 -4.4074
                                                                .000628
2135
                   .000628
                                                 -.01619
                                  -,15212
                                                                .0853
25141.0
                                                 1.0
                   1.0
                   -,9556
                                                 -4.1277
                                                                .003953
2585,001538
                                  58,925
                                                  -.01619
                   .003953
                                                                .0901
2635
                                  -,15212
                   281000.0
                                  341000.0
                                                 20200000.0
27641.846
                                                 1.0
                                  1.0
30141.0
                   1.0
                   -.9889
                                  56,325
                                                                .002573
                                                 -3.7291
3085,001001
                   .002573
                                                                .0969
3135
                                  -.15212
                                                 -.01619
                   301000.0
                                                18200000.0
32642,63
                                      460000.0
```

```
1.0
35141.0
                                                    1.0
                    1.0
3585,000901
                       -.8727
                                    54,275
                                                                   .002592
3635
                     002592
                                    -,15212
                                                    -.01619
                                                                    .1023
37642.074
                    323000.0
                                    588000.0
                                                    16100000.0
40141.0
                    1.0
                                    1.0
                                                    1.0
                    -.7444
4085.001103
                                    51.775
                                                                   .003967
                                                    -3.0315
4135
                    .003967
                                    -.15212
                                                    -.01619
                                                                   .1088
42642.529
                    343000.0
                                    711000.0
                                                     15600000.0
45141.0
                    1.0
                                    1.0
                                                    1.0
4585.001551
                    -. 8101
                                    48.15
                                                    -2.4758
                                                                   .006338
                    .006338
4635
                                    -.15212
                                                     -.01619
                                                                   .1183
47643.667
                    373000.0
                                    816000.0
                                                    16600000.0
50141.0
                    1.0
                                    1.0
                                                    1.0
5085,001472
                    -.8627
                                    44.0
                                                    -1.8396
                                                                   .006488
                    .006488
5135
                                    -.15212
                                                    -.01619
                                                                   .1292
                                    894000.0
52644.198
                     411000.0
                                                    17800000.0
55141.0
                                    1.0
                                                    1.0
                    1.0
5585,001499
                    -. 9245
                                                                   .007059
                                    40.0
                                                    -1.2264
                    .007059
                                    -.15212
5635
                                                    -.01619
                                                                   .1396
57644.047
                    451000.0
                                    975000.0
                                                    19200000.0
60141.0
                                    1.0
                    1.0
                                                    1.0
6085.001527
                    -. 9847
                                                                   .007629
                                    36.0
                                                    -0.6132
6135
                    .007629
                                    -.15212
                                                    -.01619
                                                                   .1501
62644.047
                    490000.0
                                    1060000.0
                                                   20500000.0
65141.0
                                    1.0
                    1.0
                                                   1.0
                    -1.0558
6585,001554
                                                                   .0082
                                    32.0
                                                    -0.000
6635
                                    -,15212
                    .0082
                                                   -.01619
                                                                   .1606
67644.047
                    529000.0
                                     1140000.0
                                                        21800000.0
70141.0
                                    1.0
                    1.0
                                                    1.0
7085,001472
                    -1.1153
                                                                   .008149
                                    28,137
                                                      .5922
7135
                    .008149
                                    -.15212
                                                    -.01619
                                                                    .1707
72643.908
                                    1210000.0
                    568000.0
                                                   23100000.0
75141.0
                    1.0
                                    1.0
                                                   1.0
7585.001954
                    -1,2778
                                    24.775
                                                   1.1076
                                                                   .008158
                    .008158
7635
                                    -.15212
                                                   -.01619
                                                                    .1791
77643.401
                                        1290000.0
                    603000.0
                                                   24200000.0
80141.0
                                    1.0
                    1.0
                                                   1.0
8085.002596
                    -1.4803
                                   22,275
                                                   1.4909
                                                                   .010329
8135
                                    -.15212
                    .010329
                                                   -.01619
                                                                   .1860
82642.529
                    796000.0
                                    1690000.0
                                                    38000000.0
85141.0
                                    1.0
                    1.0
                                                   1.7208
                    -1.4089
                                   20,775
8585,002912
                                                                   .007789
                    .007789
                                   -.15212
8635
                                                                   .1900
                                                   -.01619
87641.518
                    1120000.0
                                    2370000.0
                                                   64300000.0
90141.0
                                   1.0
                    1.0
                                                   1.0
9085.002694
                    -1.19
                                   19.9
                                                    1.855
                                                                   .006852
                                   -.15212
9135
                    .006852
                                                   -.01619
                                                                   .1923
                    4340000.0
9264.885
                                   5270000.0
                                                    97900000.0
95211.0
95711.0
```

```
100141.0
                     1.0
                                    1.0
                                                    1.0
10085.007778
                     -1.15
                                    17.275
                                                    2.2574
                                                                   .034386
10135
                     .034386
                                    -.15212
                                                    -.01619
                                                                   .1991
102642.656
                     2240000.0
                                    806000.0
                                                        19900000.0
105121.0
                     1.0
105421.0
                     1.0
10585,001255
                     0.0000
                                    14.0
                                                     2.9289
                                                                   .004421
10635
                     .004421
                                                    -.01619
                                                                   0.000
107642,929
                                    500000.0
                     101000.0
                                                    14000000.0
108912.28374
110141.0
                        1.0
                                                    1.0
11085.002
                     0.0000
                                    11,381
                                                                   .00066
11143,00066
                                     -.01619
112642.619
                     60000.0
                                    45000.0
                                                     15400000.0
115111.0
115411.0
11585,0012
                     .000
                                    9.0
                                                                   .000676
11643,000676
                                    -.01619
117642.381
                     60000.0
                                    45000.0
                                                     18200000.0
120111.0
120411.0
12085,00053
                                    7.0
                                                                   .000692
12143,000692
                                    -.01619
122642.0
                     60000.0
                                        45000.0
                                                   20700000.0
125111.0
125411.0
12581,0005
126015.0
12621,000896
12641.000896
12661-,01619
127642.0
                    60000.0
                                    140000.0
                                                     21800000.0
130141.0
                    1.0
                                                   1.0
13061,000085
131012.671
13121.000086
13141,000086
132642.329
                    60000.0
                                    66500.0
                                                    22200000.0
133111.0
135411.0
13581,001
136011.342
13623,001
                                    .001
137641.392
                    10000000.0
                                    66500.0
                                                    29200000.0
140411.0
142641.342
                    9.00000000E+169.00000000E+169.0000000E+16
 31912.9916
 36912.2974
 41913.0926
 46912.9159
```

```
51913.1052
56914.0393
61914.0393
66913.9696
71913.6475
76912.96
81912.02
86911.1992
91911.7672
101913.6228
                                    603.7
 32232,9692
                     8.05
                                    603.7
                     8.2
 37233.0340
                                    603.7
                     8.4
42233.1122
                                    603.7
 47233.2247
                     8.65
                                    603.7
                     9.0
 52233.3543
                                    603.7
                     9.25
 57233.4821
                                    603.7
                     9.6
 62233.6060
                                    603.7
 67233.7319
                     9.86
                                    603.7
                     10.18
 72233.8539
                                    603.7
                     10.4
 77233.9587
                                    603.7
 H2234.0388
                     10.6
                                    605.7
                     10.72
 87234.0846
                                    603.7
                     10.85
 92234.1113
                                    603.7
102234.1952
                     11.0
 31011.0
 36811.0
 41811.0
 46811.0
 51811.0
 56811.0
 61811.0
 66611.0
 71811.0
 76811.0
 81811.0
 86811.0
 91811.0
101811.0
145112.0
                      .1144
 2162-.02013
                      .1192
 2662-,02013
                      .126
 3162-.02013
                      .1314
  3662-,02013
                      .1379
 4162-,02013
                      .1474
  4662-.02015
                      .1583
  5162-.02013
                      .1687
  5662-.02013
                      .1792
  6162-,02013
                      .1897
  6662-,02013
                      .1998
  7162-,02013
```

```
7662-,02013
                     .2082
 8162-,02013
                     .2151
                     .2191
 8662-,02013
 9162-,02013
                     .2214
10162-,02013
                     2882
10661-.02013
11161-.02013
11661-,02013
12161-.02013
12661-.02013
    1
    1
   15
7,4254402E-06-8,2868165E-0999,79237
19.0
                                               P15PP880.0
                                                               -1.5350914E-03
                                               -1.202794
                                                                0.0036020154
                               0.0
                                               1.0
                                                                1.0
1.0
               1.0
  10
                      0.4
0.0
           0.3
                                 0,505
                                            0.555
                                                        0.618
                                                                   0.68
0.75
           0.82
                      1.0
                                 340.
                                            350.
                                                        360.
0.0
                      20.0
           12.7
.19
                                                        .19
                                 -1.0
                                            -.85
           1,5
                      1.1
  12
                                 13.
                                                                   20.
                      11.
                                                        15.
0.0
           8.
                                            14.
           350.
                      354.
                                 356.
                                            360.
340.
                                            1.63
.205
           1.09
                      1.39
                                 1.58
                                                        1.48
                                                                   1.18
                      -.45
-1.0
           -,7
                                 -.24
                                             .205
 12
                      10.
0.
340.
           8.
                                 11.
                                                                   20.
                                            11.8
                                                        13.
           350.
                      354.
                                 356.
                                            360.
           1.15
                                                                   1.07
                      1.36
                                 1.45
                                            1.5
                                                        1.43
.22
                      -.444
                                            .22
-1.0
           -.73
                                 -,25
   12
0.
                      11.
                                 12.
                                                                   20.
                                            12.5
                                                        12.7
           9.
           350.
340.
                      354.
                                 356.
                                            360.
. 25
           1,365
                      1.565
                                            1.65
                                                        1.51
                                                                   1.2
                                 1.64
                      -.45
                                 -.25
           -,71
                                            .25
-1.0
   13
0.
340.
                      10.
                                            12.
           8.
                                 11.
                                                        13.
                                                                   20.
           350.
                      352.
                                  354.
                                            356.
                                                        360.
                                 1.495
                                            1.48
                                                        1.36
           1,3
                                                                   1.25
.26
                      1.48
                                 -.46
           -,69
                                            -.255
                                                        .26
                      -.61
-1.
   15
0.
                      6.
340.
                                 7.
350.
                                            8.
352.
                                                        9.
354.
                                                                   10.
                                                                   356.
           20.
360.
                                 1.19
                                            1.24
                                                        1.27
                                                                   1.33
.285
           . 7
                      1.1
                                            -.62
1.34
           1.3
                      -1.0
                                 -.67
                                                        -.47
                                                                   -.27
```

```
.285
 12
           3.
                                              10.
                       3,7
                                  6,
355,
                                                         14.
                                                                     20.
            350.
340.
                       354.
                                              360.
.305
            .75
                       . 8
                                  .96
                                              1.18
                                                         1.33
                                                                     1.48
-1.
            -,67
                       -.53
                                              .305
                                  -.42
0.
           2.
352.
                                  10.
                                              15.
                                                                     340.
                       6.
353.
                                                         20.
350.
                                                                     359.
                                                         356.
360.
                                              1.35
.36
            .56
                       .86
                                                         1.5
                                  1.11
                                                                     -1.
                                                         .. 35
-.7
            -,67
                       -.67
                                              -.49
                                                                     .23
                                  -.61
.36
 13
0.
                                             8.
356.8
                                                                     20.
           1.
350.
                                                         15.
                       2.
                                  6.
355.4
340.
                       354.
                                                         360.
            . 3
                      . 4
                                  .79
. 16
                                              .97
                                                         1.4
                                                                     1.56
                                  -.19
                                                         .16
            -.68
                       -.44
                                              -.33
-1.
0.
           2.5
                      340.
                                  360.
0.
                      -2.5
                                  0.
                                                0.10546602
13.0
                354.0
                                -1.0783242
                                                                -0.0022458297
2.5438880E-05-1.0989072E-075.5012552
                                                -0.060345598 0.00016618434
0.0
           0.3
                      0.4
                                  0.6
                                              0.7
                                                         0.8
                                                                      1.0
 15
0.0
                      2.
                                  3.
354.
                                              4.
356.
                                                                    8.
359.
           1.
                                                         6.
358.
10.
360.
                                                         .009
            .0085
.008
                       .009
                                  .009
                                              .0085
                                                                     .0115
.013
            .017
                       .03
                                  .011
                                                         .0086
                                              .01
                                                                     .0085
.008
 15
0.0
                      2.
           1.
                                  3.
354.
                                                         6.
358.
                                             356.
                                                                    359.
10.
                      14.
360.
                      .009
.008
            .0085
                                  .009
                                              .0085
                                                         .0088
                                                                     .0106
.013
           .017
                      .03
                                  .011
                                              .008
                                                         .0086
                                                                     .0085
.008
 15
0.0
                      2.
                                  3.
354.
                                                                    8.
359.
                                              4.
                                                         6.
358.
           12.
                                             356.
10.
360.
                                                         .009
.0075
                      .0075
                                             .008
                                                                     .01145
           .0075
                                  .0076
.0145
                                                         .0075
           . 057
                      .08
                                  .016
                                             .0082
                                                                    .0075
.0075
 15
                      2.
0.0
           1.
                                  3.
354.
                                             4.
356.
                                                        358.
                                                                    8.
359.
10.
```

340						
360.	0.00					
.008	.008	.008	.0088	.0087	.021	.08
.08	.14	.18	.058	.0139	.0085	.0085
.008						
15						
0.0	1,	2.	3.	4.	6.	8.
10.	12.	14.	354.	356.	358.	359.
360.		-			• • •	
.0105	.0155	.03	.06	.07	. 1	.13
.14	.26	.27	.08	.02	.009	.009
0105		• • •	• • •		,007	
15						
0.0	1.	2.	3.	4.	4	
10.	iz.				6.	8.
-	15.	14.	354.	356.	358.	359.
360.	095					
.07	.075	.08	.09	•1	. 15	. 2
. 3	. 3	.3	.09	.06	. 05	.05
.07						
15		-				
0.0	1.	2.	3.	4.	6.	8.
10.	12.	14.	354.	356,	358.	359.
360.		1				
.21	.21	.24	. 25	. 26	. 3	.34
. 35	. 35	. 35	. 25	. 2	. 18	.18
.21						-
52						
13.0	352.0	•	.0545	0.22140	169 0.	037698898
0.0014700	305 -2.19	80119E-050	16285396	-0.0143		2695044E-04
		13282E-09-		0.05152	0503 4	2809828E-04
		9316 -		0.00110		7548054E-06
	0E-08.0045					/ 3444 345 800
6						
0.0	0.3	0.45	0.67	0.75	1.	
14	<b>V</b> , <i>J</i>	V, 43	0.01	0.73		
0.	2,	n	4		4.0	4.4
12.	14.	4. 352.	6.	8.	10.	11.
03			354.	356.	358.	360.
	035		039	049	545	057
058	06	005	015	0215	026	03
14	3			_		
0.	2.	4.	6.	8.	10.	11.
12.	14.	352.	354.	356,	358.	360.
03	035	039	039	049	0545	057
058	06	005	015	0215	026	03
14	_					
0.	Š.	4.	6.	8,	10.	11.
12.	14.	352.	354.	356,	358.	360.
03	035	039	045	049	049	05
05	06	005	022	0215	026	03
14		-	-	-	•	-
0.	2.	4.	6.	8.	10.	11.
		-	-	_		

12. =.037 =.145	14. 0435 15	352. 05 006	354. 0915 024	356. 108 032	358. •.09	360.
0. 12. 12 17	2. 14. •.122	4. 352. 12	6. 354. 14	8. 356. •.15	10. 358. 16	037 11. 360. 17
14 0, 12, 09	2. 14. 169	4. 352. 233 .094	6. 354. 29	8. 356. 4	10. 358. •.5 •.037	11. 360. •.5

# Sample Results (Flexstrap Case)

0.20967105714891940502 -0.314357858000880405805	LAST DETERNIMANY VALUE = 0.00050000000000000000000000000000000	LAST EIGEN VALUE med.2300735002 0.1700002005 Current eigen value med.2300045000 0.170007000 Next eigen value med.23000000000000000000000000000000000000	15 VALUEB OF UPDATED LAMBDA MATRIX	3.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0	0.8994650573400660-00 .0.4369926479836040-00 0.20967166148569020-02 .0.43696261298759675967	LABY DETERNIMANY VALUE see, 26566600000 0.12655500000 CURRENT DETERNIMANY VALUE see, 271700000000 0.1265550000 EIGEN VALUE CONVERGENCE s 0.20032828000	RO-GLOGOLI"O RO-GROOPER"O BUTTA NUCLE NUCLE BOTTA NUCLE NUCL	15 VALUES OF UPDATED LAMBDA MATRIX	0.0 0.0 0.0 0.0 2.0 0.0 0.0 0.0 0.0 0.0	0.20467146066119340502 0.20467166066119340502 0.3181914713334120512	CHART DETERMINANT VALUE see 1277700-see.0.5590010 CHARENT DETERMINANT VALUE see 1.000700-10 CIGEN VALUE CONVERGENCE s 0.52035000-10	CO-COCCOCT C RO-COCCCC C-C DOTAL RELEGATION OF TACOCCOCCCC COLUMN AND EN TOTAL COCCCCCCC COCCCCCCCCCCCCCCCCCCCCCCCCC
				000					•••			
07610 . 001707 .				1.00000	075848 0 075810 0 091407 0				000000000000000000000000000000000000000	075610 075610 091707		

AEROELABTIC STABILITY STATE VECTORS

BLADE 1 O PER REV SHAPE VECTURILICAL AXIS SYS.)

•	BECTION	UK, RADIAL	06#1.		
		(+, OUTBOARD)	BOARDS	C+* ROTATION DIR.	(ORTHAN *+)
41		2.0403E-02	1.3228E=02	-3.3274E=01 -2.7312E=01	0.00000.10
	~	2.0403E-02	1. 3228E-02		49,4838F-01 -8,7804F-04
	•	2.0403E-02	1.3228E-02	-3.1363E-01 -2.4552E-01	-5.0434F-0
	∢ (	2.0403E-02	1.32285-02	-3.0421E-01 -2.3277E-01	
	<b>.</b>	2.0403E=02	1.32285-02		
	••	2.0403E=04	1.32285-02		
		2.0403E-02	1.32285.02		
		20.020.02	1.3668506		
	• •	20 20 20 20 20 20 20 20 20 20 20 20 20 2	1.36605=06		
	2 -	A. 040 ST BOR	I . MACON .	•	-4.7656F=01 -2.5596F=02
		2 04046 G	1. SCHOOL SCHOOL		20 - 20 - 20 - 20 - 20 - 20 - 20 - 20 -
		2.04016-02	12286-02		
		2.0401F=02	1 3238F 02	•	NOTIONS NOTION OF THE PROPERTY OF
		2.0401F=02	1.12285-02		
		1.798RE-02	7.055560	からしまるとのでは、 かっしょうかってい	
		2.0403E-02	1.52285.02		Manager of the Manager of
			1,01225-04		
	•	99756-04	40.04004		
			TO LEAD TO		MONAGAN (* 1003CAC*10
	: ~		10 PART 0 11		
	: ~		101111111111111111111111111111111111111	ACTION OF THE STATE OF THE STAT	NOTARCHE OF REPARKS OF
	2	505E-15	2.1477Fe14		SOUNDAME OF THE PROPERTY OF
	*	6.7585E-15	2-1977E=14		11125-03
	<b>~</b>	6.7585E-15	2.1477Fe1a	06716	
	;				eles/o/get1 elegiblesi
•	9ECT10*	H	Teller		
		80% **)	NOSE UP)	CARDO AVIA	
					ייי פרפייב רביים
- 1		4.7757E-02	S. 6858E-03	1.62485-02 -7.24845-04	
	~	4.7730E-02	3.6709E=03		
	~	4.746SE=02	3.52576-03		
	◀ (	4.7311E-02	3.49496-03		
	<b>.</b>	4.7162E=02	3.5181E-03		-7.0516E-03 -6.1053E-03
	••	4.7032E-02	N. BERUREON		-7.2006E=03 -6.0203E=03
		4.06785-02	5.8678E-05		-7.3626E-03 -5.900BF-03
	•	20-32-06			47.5084E+03 45.7345E+05
		8.0000E-04	40 10 10 10 10 10 10 10 10 10 10 10 10 10		-7.6456E-03 -5.5255E-03
	2:	20-18000°	4.7542F=05		-7.7634E-03 -5.2791E-03
		30 10 10 10 10 10 10 10 10 10 10 10 10 10	5.15016-05	•	-7.9114E=03 -4.9963E=05
	= :	20-26000	S. 3391E-03		-6.0174E-03 -4.7260E-03
	23	20026000	7.0407600	Z.3047E=0Z 0.6Z44E=04	
		2002500	2047BB446		
		20-10-07-07-07-07-07-07-07-07-07-07-07-07-07	SOURCE OF THE PARTY OF THE PART		
		3.0479E=04	POPULATION OF		
		20032617.		2.8349E+02 5.9315E+03	
		****		4.101er=04 3.1114F=03	-1.4373E-03 -2.6431E-03

# DEST AVAILABLE COPY

A C 1	22 The Abelian State of the Ab	, ,,,,,,,	
1. 7 PETATE OF 2. 10 SAME OF S	MU ANAROGO	7.77	TEANSTORM   CONTRACTORM   CO
3. 10.10.10.10.10.10.10.10.10.10.10.10.10.1	4. ** ** ** ** ** ** ** ** ** ** ** ** **	1. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.	7.012
6 0 - 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	24 24 25 24 25 25 25 26 26 26 26 26 26 26 26 26 26 26 26 26	108 08 08 08 08 08 08 08 08 08 08 08 08 0	

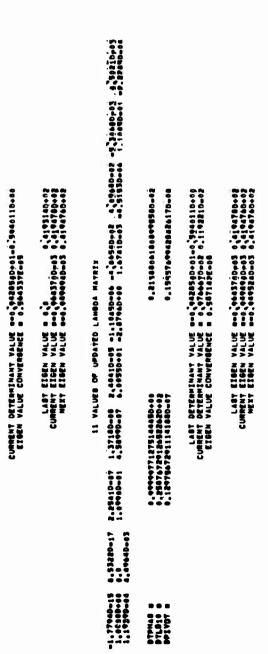
1.0911R+03 1.210311R+03 1.21031R+03 1.21031R+03 1.20031R+03 1.30031R+03 1.300

----

### Sample Input (Articulated Case)

```
0002140.0
001511.0
                    4.0
001721.0
001917.0
002111.0
0.122500
                    1.0
002816.0
002924.0
                    3.0
003711.0
                   1.0
003923.0
                                              E+11.10
                                                             E+11
                                    .10
004140.1
                    0.9
004511.0
004811.0
0054141,7228
                                   7.0
0059350.0
                    10.0
                                    7.0
                    7.0
006236.0
                E-06
00771.1
00971-.5
                    2.0943951
                                   4.1887902
011730.0
                E+17.9
                                              E+17
                               E+17.9
01213.9
                E+05
01331.6
016921.0
                    5.0
020111.0
                    0.005
                                    10.0
020830.25
021210.5
021410.5
                                    0.05
02153-,015
                    -.02
025411.0
                                    0.05
02653-.015
                    -.02
                               E+09.1
                                              E+09.1
                                                             E+09
027649.1
                     . 1
030211.0
                    -.02
03152-,015
035111.0
03652-.015
                    -.02
040211.0
04161-.02
045211.0
 50411.0
                                                              E+12
                                              E+12.1
                               E+12.1
05264.9
                     . 1
    9
```

### Sample Results (Articulated Case)



BEST A ....... COPY

APROFLASTIC STABILLTY STATE VECTORS

SHABHPLATE DEPLECTIONS

O PER REV.

w( 0)==0.17794D=14 0.85323D=16

O PER REV SHAPE VECTORILOGAL AXIS SYS.

BLADE 1

SECTION

-1

64. Meetreon e. Montreeon 1. Meetreon e. Montreeon 1. Meetreon e. Montreeon 1. Meetreon e. Montreeon e. Montr PHI Z. CHORDNISE SUPPE (+, BLADE LEAD) V Z. PLAPHISE SHEAR (+, UPHARD) UZ. VERT. DEPL 1.75676 1.7566601 1.7566601 1.7566601 1.7567601 1.7567601 1.7567601 PHI Y, FLABMISE BLODE (+, FLAP DOWN) V V. CHORDWISE SHEAR (+, TGHARD L.E.) UY, INPLANE DEFL. 22.6240E+011.1266E+00 22.6240E+011.1266E+00 22.6240E+011.1266E+00 23.6240E+011.1266E+00 24.6240E+011.1266E+00 25.6240E+011.1266E+00 26.6240E+011.1266E+00 26.6240E+00 26.62 N. AXIAL FORCE (+, RADIAL GUTBOARD) UK, PADIAL DEFL. (+, DUTBOARD) PHI K, THIST (+, NOBE UP)

-4,5797E+00 3,9653E+00

M Z. CHORDETEE MOMENT (+.TENSTON T.E.)

H Y. PLAPHISE HOMENT (+, TENSION UPPER FISERS)

2.1411E-01 -1.8160E-01 2.3413E-04 2.8314E-05

-1. 0029E+00 5.2003E=01

-11

T, TOROUE (+, NOSE UP)

SECTION

5 T

41.

SECTION

2

SECTION

41

1,10020000 1,4191000 1,10020000 1,4191000 1,1711000 1,4004000 1,1711000 1,4004000 1,1711000 1,4004000

2.3595E=04 2.9879E=09 2.3595E=04 2.9876E=08 2.3597E=04 2.9891E=09 3.3597E=04 2.9891E=09 5.9630E+03 47.98381E=01

3.4204E406 44.1010E407 1.166E407 4.601E409 1.106E607 4.601E409 1.0396E407 4.2727E408

### Sample Input (Gimballed Case)

```
0002140.0
001511.0
001721.0
                     4.0
001916.0
0.122200
                     1.0
002924.0
                     3.0
0.115200
003711.0
003923.0
                     1.0
                                               E+11.10
                                                               E+11
                                    .10
004140.1
                     0.9
004611.0
004811.0
00541255,2501
                                    7.0
0059350.0
                     10.0
                                    7.0
006236.0
                     7.0
00771.1
                E-06
00971-.5
                     2.0943951
                                    4.1887902
011730.0
                                               E+17
01213.9
                E+17.9
                                E+17.9
01331.6
                E+05
020111.0
                                    10.0
020830.25
                     0.005
021210.5
021410.5
                                    0.05
02153-.015
                     -.02
025411.0
                                    0.05
02653-.015
                     -.02
                                               E+07.4
                                                               E+07
                     . 1
                                E+07.4
027649.1
030211.0
03152-.015
                     -.02
035111.0
                     -.02
03652-.015
040211.0
045411.0
                                                               E+13
04764.9
                                E+12.1
                                               E+12.1
                     . 1
    9
```

# Sample Results (Gimballed Case)

AEROELASTIC STABILITY STATE VECTORS SHASHPLATE DEFLECTIONS

9	1X18 8VS.)	CENTROL	10000000000000000000000000000000000000		PHI Z. CHORDWIGE SLIPE (4. BLADE LEAD)	ACCOMPAND	V Z. PLAPETOR BHRAR (+. CPRERD)		T. C. CLORDELAGG, MORENT (+, TEASTON T.E.)	######################################
O PER REV. M( O)==0.54070D=03=0.51631D=04	O PER REV SHAPE VECTORILDEAL AKID SYS.)	UV, INPLANE DEFL. (+, ROTATION DIR.)	*** S1986 ** O. 7 ** B1876 ** S*** S*** S*** S*** S*** S*** S***	2.41664.00 4.01487.00 2.21687.00 4.01487.00 2.2687.11 4.52797.13	HI A' PLAPHINE GLOPE (+, PLAPHINE GLOPE	1.62618601 = 1.6261888100 1.377088606 = 1.2966811 1.377088606 = 48.286788106 1.377088606 = 48.286708106 1.37708806 = 48.286708106 1.37708806 = 48.28680806 1.28677815	V V. CHORDWING BHEAR (+) TOWARD L.M.)	*2.3500E+02 1.2148E+03 *2.3500E+02 1.2148E+03 5.859E+02 1.213E+05 5.859E+02 1.213E+03 5.878E+02 1.213E+03 5.878E+02 1.213E+03	T Y. PLAPHING ROIDST (+) TRANSION UPPER FIGURE)	
	BLADE 1	UX, RADIAL DEFL. (+, OUTBDARD)	1.2926E-08 -6.7366E-10 1.2926E-08 -6.7366E-10 1.2926E-08 -6.7366E-10	6.5001Ee12 1.7197Ee13 6.5001Ee12 1.7197Ee13 6.5001Ee12 1.7197Ee13	TONE OF COLUMN	6.24666102 11.089966102 1.10116703 1.084066102 1.10116703 1.084066103 9.0046610 9.99966111 1.87406608 82.18046611	* AKTAL PORCE (+, RADIAL DUTBOARD)	13.9228E+02 1.7751E+02 13.9228E+02 1.7751E+02 13.9228E+02 1.7751E+02 13.9228E+02 1.7751E+02 15.4573E+01 1.9854E+02	T, TOROUE (+) MOSE UP)	SW. USCOPERATION OF STREET
		SECTION	-NIN	# # # # # # # # # # # # # # # # # # #	SECTION.	NMene	9EC110W		SEC TION	

# Sample Input (Teetering Case)

0002140.0				
001511.0				
001721.0	2.0			
001916.0				
0.155500	1.0			
002924.0	3.0			
0.5212.0				
003711.0				
003923.0	1.0			
004140.1	0.9	.10	E+11.10	E+11
004611.0	· •	•		-
004811.0				
00541255.2501				
0059350.0	10.0	7.0		
006236.0	7.0	7.0		
00771.1	E-06	. •		
00971-5				
011730.0	2.0943951	4.1887902		
01213.9	E+17.9	E+17.9	E+17	
01331.6	E+05			
020111.0				
020830.25	0.005	10.0		
021210.5				
021410.5				
02153015	02	0.05		
025411.0				
02653=,015	02	0.05		
027649.1	. 1	E+07.4	E+07.4	E+07
030211.0				
03152015	02			
035111.0				
03652015	02			
040211.0				
045411.0				_
C4764.9	.1	E+12.1	E+12.1	E+12
8				
9				

# Sample Results (Teetering Case)

0.2999280003 0.2999800003 0.2999900003 671094820002 1.12000004 671094820000 0.2999900003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003 0.299990003			1.310AD-09	
	CORRENT EIGEN VALUE = 0.0	TABLUS OF TOTALES OF TARGET LANGOA MATRIX   ***O*******************************	.UES OF UPDATED LAMBDA MATRIX 7.562500-00 1.78050-04 -1.51970-02 7.81480-02 -2.98180-05 7.66200-00 7.47500-01 1.19500-03 1.12200-04 00 -0.80620491894021835-10	LAST DETERMINANT VALUE ==0.356456D=04 0.223170D=05 CURRENT DETERMINANT VALUE ==0.2370556=09 EIGEN VALUE =00.2370556=09 LAST EIGEN VALUE ==0.4458600=03 0.29479D=03 NEXT EIGEN VALUE ==0.4458600=03 0.29479D=03

AEROELABTIC STABILITY STATE VECTORS

STATE VECTORS SHABHPLATE DEFLECTIONS O PER REV.

BLADE 1 O PER REV SHAPE VECTOR(LOCAL AXIS SYS.)

H( 0)==0.596220=03=0.559810=04

				Control and a second a second and a second a	
	8EC710N	UX, RADIAL DEFL. (+, OUTBOARD)	DEFL. GARD)	UY, INPLANE DEPLY (+, ROTATION DIR.)	LZ - CERT (SE
2	~ N F		16 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	#1.5157E=02 7.8127E=02 #9.525E=03 2.925E=03	
3			6. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4. 4.		TO THE STATE OF TH
	<b>36</b> C710N	PHE X THE (+) NOBE CP)	F C C C C C C C C C C C C C C C C C C C	(+, FLAPWING GLOPE (+, FLAPWING GLOPE	PHI Z. CHORDWISE SLAPE (+, BLADE LEAD)
=	~ @ FA		10.70000 10.12260 10.12260 10.12260	1.949.00000 1.04990000 1.949900000 1.949900000 1.949900000 1.949900000 1.94990000000000000000000000000000000000	SOURCE OF THE CONTROL
3	•••	14.00000 14.00000 14.00000 14.00000 14.00000	1.0102810 -2.0838610 -7.1875615	1.3772E406 - 5.2854E400 1.3772E406 - 5.2854E600 2.4466E411 - 5.1462E413	•
	8EC710N	N, AXIAL PORCE (+, RADIAL GUTBOARD)	FORCE IUTBOARD)	V V. CHORDETSE SHEAR (+, TOMARO L.E.)	V Z. PLAPHIBE BREAR (+. UPHARD)
Ė	₩ <b>8) I</b> PI <b>4</b>	83.4223E+02 83.4223E+02 83.4223E+02	1.77616+02 1.77616+02 1.77616+02		11.
5			1. 445400	5.8946F+02 1.4151E+03 5.8749E+02 1.2104E+03 5.8749E+02 1.2104E+03	11.8842M+08 6.0984M+01 11.8847M+08 6.8MOUM+01 11.8847M+08 6.8MOUM+01
	<b>B</b> ECT10N	T, TORDUE (+, NOSE UP	0.0E 	H V. FLAPHING MOMENT (+, TENNION UPPER FINERS)	1 Z. CHORDEHOR FORENT (+, TENBION T.E.)
=	N:M <b>4</b>	19.12.13.13.13.13.13.13.13.13.13.13.13.13.13.	7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243 7.243	1.1700E801 89.29826E801 1.4892E801 81.38460E801 1.489546-00 81.58650E901 1.4865E908 81.58650E903	60.17778+01 8.300+08+08 8.18788+01 1.11788+08 8.18788+08 1.11788+08
5	<b>.</b>		-2,3150E+02 -2,3150E+02		U. 1101R+03 1. 1196R+04 U. 64849R+04

## Sample Input (Rigid Case)

```
0002140.0
001511.0
001711.0
001914.0
002511.0
004611.0
004811.0
00541255,2501
                                   7.0
0059350.0
                    10.0
006235.0
                    6.0
                                   6.0
020111.0
020830.25
                                   10.0
                    0.005
021210.5
021410.5
                                   0.05
02153-.015
                    -.02
025411.0
02653=,015
                    -.02
                                   0.05
                               E+07.4
                                             E+07.4
                                                             E+07
027649.1
                    . 1
030211.0
035411.0
                                                            E+12
03764.9
                    . 1
                               E+12,1
                                             E+12.1
    9
```

# Sample Results (Rigid Case)

0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.0	1,31280-02 1,00800+00 C.0			
1.00280-07 -3.27590-10 -4.31020-04 1.94910-09 -1.51920-02 7.82040-02 -2.54740-03 1.31170-02 1.00000-06	2 - O - O 2	UTPMAS = 0.99999255081188300+00 0.38998342896815870622 DTG10 = -0.23103837535608320+00 0.85026714988294730612	LAST DETERMINANT VALUE & 0.2016370=07 0.2674000-09 CURRENT DETERMINANT VALUE & 0.1645030-10 0.3280020-12 EIGEN VALUE CONVERGENCE & 0.135659E-09	LAST ELGEN VALUE ==0.2505055.0 = 3UJAV VALUE ==0.2560505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.296050505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.2960505.0 0.29605.0 0.2960505.0 0.2960505.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.29605.0 0.296

NEXT EIGEN VALUE ==0.337005D=03 0.256578D=03

AEROELABTIC STABILITY STATE VECTORS

		PLADE 1	O PER REV BHAPE VECTOR(LOCAL AXIS BVS.)	XI B BVB.
	9EC110N	UX, RADIAL DEPL. (+, GUTBGARD)	UV, INPLANE DEPL' (+, ROTATION DIR.)	UZ, VERT, DEFL.
41.	on <b>(1)</b> y	1.2926E-08 -6.746E-10		
5	••	5.2760E-20 -5.2030E-20	4.6479E-10 4.6147E-10 4.6479E-10 62.6579E-17	10.2442010 N.40401000114.485020114 14.545020114
	9EC110N	PEN Nº TENDO (+) NOSE CP)	C+, PLAPHINE BLOPE	PHI Z, CHORDWISE SLAPE (+, SLADE LEAD)
41.	~ <b>8</b> 4	-0.3100E-04 1.4462E-05	1.6461E=01 = 1.4043E=07 1.3780E=00 = 1.8843E=11	-2.5424C-03 1.3126C-02
2	•	• •	1.37722mbb -5.2629Embb 2.8064E-11 -6.5027E-15	
	9CC110N	N, AXIAL FORCE (+, RADIAL DUTEGARD)	V V. CHORDWINE BHEAR (+, TOWARD L.E.)	V Z. FLAPHISE BHEAR (4. UPHARD)
Ė	<b>∞ N</b> (			• •
\$	•	-3.5155K+01 1.455K+02 -5.5155K+01 1.455K+02	5.6714E+02 1.2123E+05 5.6714E+02 1.2123E+05	11. Pastone o abouteon
	9ECT10N	7, TORBUE (+, NOBE UP)	T V. PLAPEISE HORBNT (+, TENSION UPPER FIBERS)	H Z. CHOBONISE HOMENT (+, TENSION T.E.)
41.	<b>0</b> 1	-1,-0927K+02 2,1307K+00	5.4693E=02 -5.2909E=01	
2	•	2,0356503 -2,36216-02	1.6042E+08 +5.856E+02 1.6042E+08 +6.1376E+02	5.64848+03 1.31798+04 9.64848+03 1.82648+04

## PROGRAM LISTING

Program Components Page														Page				
Main P	ro	gra	am															290
ACOEFF		٠.											٠					327
AERO .	į										•	•	•	•		Ĭ	•	322
BAERO						·	Ĭ		Ī	·	•	i		·		•	•	316
BARRAY	•	•	•	•		•		•	•	•	•	•	•	•	•	•	•	333
BEND .	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	367
BLARO	·	•	•	•	·	·	•		•	•	•	•	•	•	•	•	•	372
BMASS	•	•	•		•	•		•		•	•	•	•	•	•	•	•	363
CDOT .	Ċ	i		•		•	•	•	•	•	•	•	•	•	•	•	•	410
DCMAT	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	391
ELAST	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	369
EPSOLN	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	363
EXCHI		•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	404
EXPON	•	•	٠	•	•	•	•	•	•	•	•	•	•	•	•	•	•	393
FAERO	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	320
FMASS	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	٠	365
FUARO	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	371
LOADIN	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	302
MLCC 2	•	•	٠	•	•	•	•	•	•	•	•	•	•	•	•	•	•	
	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	360
MLRC2	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	359
POLAR	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	409
RCDOT										•			٠			•	•	411
RIGID	•											•		•	•			368
ROWSUM		•													•			412
SARRAY											•			•	•	•		352
SECPAR			•		•				•	•								303
SETUP	•								•			•		•	•			295
SOLVE												•					•	388
STIFF		,																366
SUBMA			•															374
SUBMB																		376
SUBMF																		387
SUBMG													•	•				383
SWA .																		394
SWAPS																		390
SWB .	•					-						•						396
TABLU	•	•	•	•	·	•	•	•	•	•	•						Ċ	325
TKNS .	•	•	•	•	•	•	•	•	•	•	•	•	•			•		361
TIT AT	•	•	•	•	•		•	•	•	•	•	•	•	•	•	•		403
17117 0	•		•	•	•	•		•	-	-	-	•	-	-			-	401
ZLN .	•	•	•	•	•	•	•	•	•	•	•	•	•	•		•	•	399
ZTEGI	•	•	•	•	•	•	•	•	•	•	•	•			•	•	•	405
Overlay	, ,	• :+-	·	•	124	•	•	•	•	•	•	•	•	•			•	413
Overra	Y =	لا ر	. uc		7 T C	-	•	•	•	•	•	•	•	•	•	•	•	-17

```
MAINLINE PROGRAM FOR HELICOPTER AEROELASTIC STABILITY
C
      ANALYSIS
      REAL+8 DFAC, FACL, FACC, DIFF, CX, PFC, PLC
      REAL+8 ARRAY(3)
      DATA BYES/'YES '/, BNO/' NO '/
      DATA ARRAY/'INPLANE', 'VERTICAL', 'TORSION '/
      CUMPLEX EGNS(5), START, EC(25), EC2(25)
      COMPLEX GXJ, GYJ, GZJ
      CUMPLEX+16 CMS, CM1, CS1, CS2
      COMPLEX+16 EPS(63), ALM(63)
      COMPLEX#16 DUMMC
      COMPLEX+16 AMA(2550)
      COMPLEX+16 EGNN, EGNL, REML, EGNC, REMC, DETSV, FACT
      CUMPLEX+16 EGNSL (5), ENGCH
      DIMENSION CONV(5), PENOM(5)
      DIMENSIUN NBIGMD(5)
      DIMENSION Y(100), 3D(4000), CX(75)
      DIMENSIUN DETR(25), DETR2(25), AFA(240)
      COMMON/RNAM/CS(4,6), SN(4,6)
      COMMON/RNAM1/CSA(4,24), SNA(4,24)
      COMMUN/8TAB/CPSI(24,6), SPSI(24,6)
      COMMON/ROTF/OM1, OM2, OMT
      COMMON/CALM/ALM
      COMMON/EPSA/EPS
      COMMON/AMAT/AMA
      CUMMON/FUSA/AFA
      CUMMON/SUB/Y
      CUMMUN/SAIN/SD
      COMMUN/FREF/CMS, CM1, C81, C82
      COMMUN/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
     1 MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NPEA, NCT, NCON, NFFB,
     2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
     31REM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
     4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXC8B, MXCPM, MXCPK, MXSMB,
     SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
     6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
      COMMON/PLOAD/STOR,OM,SDVEL,AIRD,FVEL,CHI,ZETA,THC,AFO,APO,COLL,AG,
     1GT,GP,APD,ASK,BN,BPN,BNS,FNS,FLAPH,FEAM,CTM,CONM,AFLEX,AERM,
     2AFFB, FLAN, FEN, CTN, CON, BCT, FUSM, ASN, CNH, VIN, BPC, SPH, ESN, SCC, HMA,
     45RA, SHTS, SWBS, TFX, PRS, RT, EGNM, SR(5), SI(5), PCTI, ANIT, ERM, ANDR, AREM
     SANEX, PNS, SCHN, AIG, AIP, STG, STF, PHIM(6), AKC(6), ATAU(6), TAK(4), TAC(4)
     6, SMA(6), DB8(6), PAK(4), PAC(4), ECHI(4), AKE(4), ACE(4), BJE(4), CAKE,
     TCACE, STKC(6), BTAU(6), PHIC(6), THEC(6), BL12(6), SDCO, PUNI,
     SCYFA, CYLA, CELM, CELN, DACO, CTYM, AEXT, EYEX, EZEX, CDE1, CDE2, CDE3,
     9PHOTT(8),PHWTT(8),CLESP(6),P(2000),V(25,24)
      COMMON/DAMCO/OMDA
      COMMON/ISUMA/NBGMD
      COMMON/NLEAD/MLEL, NLEL, MCTY
      COMMON/QVTEM/QXJ,QYJ,QZJ
      COMMON/CPARS/ALSTH(6)
```

```
CUMMUN/TAER/THCK, THC1, THC2
     COMMON/SPAR/AKCI(6), TAU(6), SMLA(6), DMS(6), AK(4), AC(4), BJ(4),
    1 CAPK, CAPC
     CUMMON/CPAR/AMKC(6),CTAU(6),AL(6,6),AL12(6)
     CUMMUN/SWASH/SWGJ, SWEI, SWM, SWR
     CUMMON/SPARI/AKT(4), ACT(4), AKP(4), ACP(4)
     COMMON/CFLEX/CX
     CUMMUN/SHAFT/TURFLX
     CUMMUN/COUP/PFC, PLC
     COMMON/DTERM/DFAC
     CUMMUN/REMA/DETSV
     COMMON/IPCH/IPU
     CUMMUN/FGRAV/FGRA
     ICNT=0
     CM1=DCMPLX(0.D0,1.D0)
1931 CUNTINUE
     CALL SETUP (EGNS, ICNT)
     IF(NSCH.LT.1) GD TO 50
     IB=0
     IC=0
     ID=0
     IE=0
     MUDERO
     START=EGNS(1)
     CRSSREAL (START)
     CISHAIMAG(START)
     DO 20 I=1, IF
     CI=CIS+(I=1) *STF
     DO 10 J=1, IG
     CR=CRS+(J=1) *STG
     CMS#CR+CI*CM1
     DU 6 K#1, MXQ
   6 ALM(K)=DCMPLX(1.D0,0.D0)
     CALL BARRAY
     CALL SARRAY
     CALL EPSOLN
     CALL SOLVE
     PRINT 943, CMS, DETSV
     RESKI #DETSV
     DUMMC=DETSV+DCMPLX(0.D0,=1.D0)
     RESI1#DUMMC
     IF(J.GT.1) GO TO 3
   2 RESRZERESR1
     RESIZ=RESI1
     GO TO 10
   3 IF((RESI1+RESI2).GT..0) GU TO 2
     IF(RES12.EQ.0.0) GO TO 2
     R1=ABS(RESI1)
     R2=ABS(RESI2)
     CR=CR=STG+R1/(R1+R2)
```

```
RESRERESR2+(RESR1=RESR2)+R2/(R1+R2)
    IF(I.EQ.IH) GO TO 5
    IB=I
    IC=IC+1
    EC(IC)=CR+CI+CM1
    DETR(IC)=RESR
    GO TO 2
 5 ID=ID+1
    EC2(ID) = CR+CI + CM1
    DETR2(ID)=RESR
    GD TO 20
 10 CUNTINUE
20 CUNTINUE
    IF(IC.LT.2) GO TO 28
    DU 23 K=2,1C
    CRUSS=DETR(K=1) *DETR(K)
    IF(CRUSS.GT.O.) GU TO 23
    IE=IE+1
    RIMABS(DETR(K-1))
    R2=ABS(DETR(K))
    EGNS(IE)=EC(K-1)+(EC(K)-EC(K-1))+R1/(R1+R2)
 23 CONTINUE
    IF(ID.LT.2) GO TO 27
    DU 26 K=2, ID
    CROSSMOETR2(K-1)+DETR2(K)
    IF(CRUSS.GT.O.) GU TO 26
    IE=IE+1
    R1=ABS(DETR2(K=1))
    R2=ABS(DETR2(K))
    EGNS(IE) = EC2(K-1)+(EC2(K)-EC2(K-1))+R1/(R1+R2)
 26 CUNTINUE
 27 NUGNSHIE
    GU TO 29
 28 NDGNS=0
 29 CONTINUE
    IF (NUGNS.ER.O) GO TO 40
    GO TO 30
40
    WRITE(6,944)
    GU TO 1931
    NOGNSENEGN
50
 30 DD 99 L#1, NUGNS
    CONV(L)#2.0
    00 115 K=1, MXQ
    EPS(K)=DCMPLX(0.DU,0.D0)
115 ALM(K)=DCMPLX(1.D0,0.D0)
    MUDE=0
    ITI=0
 74 DO 105 K=1,MX0
    ALM(K) = ALM(K) + EPS(K)
    CMMM#CDAHS(ALM(K))
```

```
IF (CMMM .GT. 0.1E-25) GU TO 105
     ALM(K) #DCMPLX(0.D0,0.D0)
 105 CONTINUE
     WRITE(6,929) MXQ
     WRITE(6,930) (ALM(K),KH1,MXU)
     IF(ITI.GT.1) GO TO 77
     IF (ITI.EQ.1) GO TO 75
     CMS=EGNS(L)
     GU TO 80
  75 CMS=(1+IPCT+.0001) +EGNS(L)
     GU TU 80
  77 CMSBEGNN
  80 CONTINUE
     IF (MODE, EQ. U) GU TO 8850
     WRITE(6,941)
8850 CALL BARRAY
     NBIGMO(L) #NBGMD
     CALL SARRAY
     IF (MODE, EQ. 1) GO TO 99
     CALL EPSULN
     CALL SOLVE
     IF(ITI.EU.O) PRINT 943, CMS, DETSV
     IF(NIT.NE.O) GO TO 8851
     MUDE=1
     WHITE (6,941)
     CALL BARRAY
     NBIGMD(L) = NBGMD
     CALL SARRAY
     GU TO 99
8851 IF (ITI.GT.1) GO TU 93
     IF(ITI.EQ.1) GO TU 92
     EGNLECMS
     REML=DET8V
     FACLEDFAC
     GO TO 98
  92 EGNC#CMS
     FACT=DCMPLX(1.Do,0.Do)
     REMC=DETSV
     FACCEDFAC
     IF (FACC, EQ. FACL) GD TO 65
     DIFF#FACL-FACC
     IF (DIFF.LE.O. ODO) DIFF == UIFF
     IF (DIFF.GT.70.00) STOP
     FACTEDCMPLX(10.DO++(FACL-FACC),0.DO)
  65 EGNNEEGNC-REMC+(EGNC-EGNL)/(REMC-REML+FACT)
     GU TO 98
  93 EGNL#EGNC
     EGNC=CMS
     REMLEREMO
     FACL=FACC
```

```
FACT=DCMPLX(1.000,0.00)
    REMC=DETSV
    FACC=DFAC
    IF(FACC, EQ. FACL) GO TO 66
    DIFFEFACLEFACC
    IF (DIFF.LE.O.DO) DIFF == DIFF
    IF (DIFF.GT.70.DO) STOP
    FACT=DCMPLX(10.00++(FACL-FACC),0.00)
 66 EGNN=EGNC-REMC+(EGNC-EGNL)/(REMC-REML+FACT)
    ER#CDAHS((EGNN-EGNC)/EGNC)
    WRITE(6,934) REML, REMC, ER
    WRITE(6,935) EGNL, EGNC, EGNN
    IF((FR-.1**MER).GT.0.) GO TO 95
    CUNV(L)=0.0
 94 MUDE=1
    EGNSL (L) =EGNC
    ENGCHEEGNC+DCMPLX(0.D0,-1.D0)
    RENGCHBENGCH
    PENUM (L) = RENGCH/OM
    GU TO RO
 95 IF(ITI.EQ.NIT) GO TO 94
 98 ITI=ITI+1
    GO TO 74
 99 CUNTINUE
    WRITE(6,946)
    DU 950 LEI, NOGNS
    CON=BYES
    IF(CONV(L).GT.1.0) CONBBNU
    MTYPE=NBIGMD(L)
950 WRITE(6,948) L,EGNSL(L),PENDM(L),CON,ARRAY(HTYPE)
929 FURMAT (3(/),41x,14, VALUES OF UPDATED LAMBDA MATRIX!/)
930 FURMAT(10(1PE12.4))
934 FORMAT(2(/),41x, LAST DETERMINANT VALUE =1,2E13.6/
   1 38x, CURRENT DETERMINANT VALUE #1,2813.6/40%, TEIGEN VALUE CONVERG
   2ENCE =1, E13.6)
935 FURMAT(2(/),47x, LAST EIGEN VALUE #1,2E13.6/
   1 44x, CURRENT EIGEN VALUE =1,2E13.6/
   2 47x, 'NEXT EIGEN VALUE #1,2E13.6)
941 FORMAT(1H1,53x, 'AEROELASTIC STABILITY'/58x, 'STATE VECTORS')
943 FORMAT('O INITIAL EIGENVALUE . ', 2612.4,' DETERMINANT . '.
   1 2612,4)
944 FORMAT( / 10 NO EIGENVALUE FOUND IN THIS AREA!)
                                      0 F
                                            PREDICTED
946 FORMAT(1H1,20x,18 U M M A R Y
                                                                  M O D
   1 E 81//T7, "MODE", T15, "DAMPING", T32, "FREQ IN", T49, "FREQ", T66, "CONVE
   2RGENCE', TOB, 'PREDOMINANT'//T32, 'RAD PER SEC', T49, 'PER REV', T66, 'CR
   SITERIA SATISFIED', T88, 'MODE TYPE'/)
948 FURMAT(T7, 14, T15, 2(E13.6, 4x), F8.4, T72, A4, T90, A8)
    ICNT=1
    GU TO 1931
    END
```

```
SUBROUTINE SETUP (EGNS, ICNT)
   REAL DAT(2800)
   REAL+8 PLC, PFC
   COMPLEX EGNS(5)
   COMPLEX#16 AMA(2550)
   COMMON/AMAT/AMA
   COMMON/ROTF/OM1,OM2,OMT
   COMMON/FWYEL/FVLT,FVLP,FVLA,8CHI,CCHI
   COMMON/SWASH/SWGJ, SWEI, SWM, SWR
   COMMON/COUP/PFC.PLC
   COMMON/RNAM/C8(4,6),8N(4,6)
   COMMON/RNAM1/C8A(4,24),8NA(4,24)
   COMMON/STAB/CPSI(24,6), SPSI(24,6)
   COMMON/SPAR/AKCI(6), TAU(6), SMLA(6), DMS(6), AK(4), AC(4), BJ(4),
  1CAPK, CAPC
   COMMON/SPAR1/AKT(4),ACT(4),AKP(4),ACP(4)
   COMMON/CPAR/AMKC(6), CTAU(6), AL(6,6), AL12(6)
   COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
  1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
 ZNAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
 4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXC88, MXCPM, MXCPK, MX8M8,
 SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
  ANEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
   COMMON/PLOAD/STOR, OM, SOVEL, AIRD, FVEL, CHI, ZETA, THC, AFO, APO, COLL, AG,
  1GT, GP, APD, ASK, BN, BPN, BNS, FNS, FLAPM, FEAM, CTM, CONM, AFLEX, AERM,
  ZAFFB, FLAN, FEN, CTN, CON, BCT, FUSM, ASN, CNH, VIN, SPC, SPH, ESN, SCC. WMA.
 48RA, 8WTS, SWBS, TFX, PRS, RT, EGNM, 8R(5), 8I(5), PCTI, ANIT, ERM, ANOR, AREM,
  SANEX, PNS, SCHN, AIG, AIF, STG, STF, PHIM(6), AKC(6), ATAU(6), TAK(4), TAC(4)
  6,8MA(6),DBS(6),PAK(4),PAC(4),ECHI(4),AKE(4),ACE(4),BJE(4),CAKE,
  7CACE, STKC(6), BTAU(6), PHIC(6), THEC(6), BL12(6), SDCO, PUNI,
  BCYFA, CYLA, CELM, CELN, DACO, CTYM, AEXT, EYEX, EZEX, COE1, COE2, COE3,
  9PHOTT(8), PHWTT(8), CLESP(6), P(2000), V(25, 24)
   COMMON/DAMCO/OMDA
   COMMON/NLEAD/MLEL, NLEL, MCTY
   CUMMON/CPARS/ALSTH(6)
   CUMMON/AMASI/GCTCP
   COMMON/SHAFT/TORFLX
   COMMON/IPCH/IPU
   CUMMON/FGRAV/FGRA
   DATA AND/IND 1/, AYES/'YES 1/
   EQUIVALENCE (STOR, DAT(1))
   NSY#100
   OD85=TAGN
   IF(ICNT.GT.O)GO TO 10
   DU S IMI, NDAT
 5 DAT(1)=0.0
10 CALL LOADIN(DAT)
   NBSEC=BNS+.1
   NFSECHFNS+.1
```

```
NB=BN+.1
NBP=HPN+.1
MFLAPSFLAPM+.1
MFEA=FEAM+.1
MCTECTM+.1
MFLEX=AFLEX+.1
MCON#CONM+.1
MLEL=CELM+.1
MAERMAERM+.1
MFUS=FUSM+.1
NBC=BCT+.1
NFLAPEFLAN+.1
NFEASFEN+.1
NCT=CTN+.1
NCON=CON+.1
NLELECELN+.1
NFFBRAFFB+.1
NASHASN+.1
NHC=CNH+.1
NVIEVIN+.1
NSP#SPC+.1
MAXNESPH+.1
NESEESN+ . 1
MSC=SCC+.1
NEGN#EGN#+.1
IPCT=PCTI+.1
NITEANIT+.1
MERBERM+.1
MCTY=CTYM+.1
NORMBANOR+.1
IREMMAREM+.1
NEXMANEX+.1
NPS=PNS+.1
IF(PNS.LT..O)NPS=PNS-.1
NSCH=SCHN+.1
IGBAIG+.1
IFMAIF+.1
NPRS=PRS+.1
NPDEAPD+.1
NSKEASK+.1
IPU=PUNI+.1
PFC=AFO
PLCMAPO
```

00000

DU 20 I=1,NEGN A#\$R(I)

```
8=SI(I)
20 EGNS(I) = CMPLX(A,B)
   SWGJ=SWTS
   SWEISSWBS
   SHMBWMA
   SWRESRA
   TURFLXMTFX
   I=6
   DO 30 MS=1.NB
   DO 25 L=1,1
   ARGEL*PHIM(MS)
   CS(MS,L)=COS(ARG)
25 SN(MS,L)=SIN(ARG)
   AKCI(MS) = AKC(MS)
   TAU(MS)=ATAU(MS)
   CTAU(MS)=BTAU(MS)
   SMLA(M8) = SMA(MS)
   AMKC(MS)=STKC(MS)
   AL12(MS) mBL12(MS)
   ALSTH(MS)=CLESP(MS)
   PHI=PHIC(MS)
   THE STHEC (MS)
   CPHI=COS(PHI)
   SPHI=SIN(PHI)
   CTHE=COS(THE)
   STHE=SIN(THE)
   AL(1,MS)=CPHI+CTHE
   AL (4, MS) ==SPHI
   AL (3, MS) =-STHE
   AL(2,MS)=SPHI+CTHE
   AL(5,MS)=CPHI
   AL (6, MS) = CTHE
30 DMS(MS)=DBS(MS)
   IF(NSP.EQ.O)GO TO 45
   1=24
   DO 40 MS=1, NES
   00 35 L=1,I
   ARGAL + ECHI (MS)
   CSA(MS,L) #CUS(ARG)
35 SNA(MS,L)=SIN(ARG)
   AK (MS) MAKE (MS)
   AC(MS) =ACE(MS)
   AKT(MS)=TAK(MS)
   ACT(MS) = TAC(MS)
   AKP(MS)=PAK(MS)
   ACP(M8) =PAC(M8)
40 BJ(MS)=BJE(MS)
   CAPKECAKE
   CAPCACE
   IF (MAXN.GT.1) GU TO 45
```

```
IF (SWEI.NE. 0.0) GO TO 45
   SWEI=1.0
   SWGJ=8WEI
   IF(SWR.EQ.0.0) SWR=1.0
45 NCUL 3=6
   NFP1#NHC+1
   MXSMI=2+NHC+1
   MXT2P1=(2+MAXN+1) +NSP
   MXKQ=12+MXSMI
   NCSB=1
   MXCPL#MXSMI*MXSMI
   MXCSB=12*NCSB
   MXCPM=12*NCOLS
   MXCPK=MXCPL+MXCPM
   MXSMB#MXCSB*MXCPL
   NEBCHMXCPM*MXSMI
   NESBC=MXCSB+MXSMI
   MFASBENCSB+MXCPL
   MXFAB=NCOLS*MXCPL
   NFUS=6+MFUS
   NRBDANCOLS+MCT+MFEA+MFLAP+MLEL
   IF(MFLEX.EQ.0) GO TO 49
   NRBU=NCOLS+3*MCON
   IF(MCTY.EQ.1) NRBD#NCOLS+6*MCUN
49 NRIFCENFUS+MXT2P1+NB+NRBD
   MXUMNRIFC+MXSMI
   NEIFCHNRIFC *MXT2P1
   NEISCENRIFC + NFUS
   NEITC=NRIFC*NRBD
   MXTKN#NRIFC*NRIFC
   AMSCHAYES
   ANVIRAVES
   AMFL=AYES
   ACTT=AYES
   AFEABAYES
   BFLEXMAND
   ACONBAYES
   AFUS=AYES
   ASCHMAYES
   ANPDEAYES
   ANSKEAYES
   ANSPRAYES
   AAER=AYES
   APRL=AYES
   APRS AYES
   ANBPRAYES
   AIPUBAYES
   AMLEBAYES
   IF (MLEL, EQ. 0) AMLEMANU
   IF (MFLAP.EQ.O) AMFLEAND
```

```
IF (MCT.EQ. 0) ACTTEANU
    IF (MFEA, EQ. 0) AFEABAND
    IF (MFLEX.EQ. 0) BFLEXMAYES
    IF (MCON, EQ. 0) ACONBANO
    IF (MFUS, EQ. 0) AFUSHAND
    IF (NSCH. EQ. 0) ASCHRAND
    IF (NPD.EQ. 0) ANPDWANU
    IF (NSK.EG.O) ANSKRAND
    IF (NSP.EQ. 0) ANSPEAND
    IF (MAER, EQ. 0) AAERBAND
    IF (NBC.EQ. 0) APRLMAND
    IF (NPRS, EQ. 0) APREMAND
    IF (NBP.EQ. 0) ANBPEANO
    IF(NVI.EQ.O)ANVIWAND
    IF (MSC.EQ.O) AMSCHAND
    IF (IPU, EQ. 0) AIPURANO
    IF(NPRS.EQ.O)GO TO 70
    WRITE(6,900)
    HRITE (6,902) NB, NBP, NBSEC, NFSEC, NBC, NHC, NFFB, NAS,
   INFLAP, NFEA, NCT, NCUN, NES, MAXN, NSY, NSK
    WRITE(6,903) NEGN, IPCT, NIT, MER, NORM, IREM, NEX, NPS,
   1IG, IF, NLEL, MCTY
    WRITE(6,905) AMPL, ACTT, AFEA, BFLEX, ACON, AFUB, ANBP,
   1AAER, APRL, APRS, ANPD, ANSK, ANSP, AMSC, ANVI
    HRITE(6,906) ASCH, AIPU, AMLE
    WRITE(6,907) OM, SOVEL, AIRD, FVEL, CHI, ZETA, GT, GP,
   1THC, AFO, APO, COLL
    WRITE(6,908)STG,STF,AG,TORFLX,SDCO,CYFA,CYLA,DACO,AEXT,EYEX.EZEX.
   1CUE1, COE2, COE3
    DU 55 I#1,NB
    IF (MFLEX.NE.O) GO TO 56
    WRITE(6,909)I, PHIM(I), I, AKCI(I), I, TAU(I), I, SMLA(I), I, DMS(I)
    GU 10 55
 56 WRITE(6,920) I, PHIM(I), I, AMKC(I), I, CTAU(I), I, PHIC(I), I,
   1THEC(1), I, AL12(1), I, ALSTH(1)
55 CONTINUE
    IF (MFLEX.EQ. 0) GO TO 57
    WRITE(6,915)PHOTT(1),PHOTT(2),PHOTT(3),PHOTT(4),PHOTT(5),PHOTT(6),
   1PHOTT(7),PHOTT(8)
    IF(MCTY.EQ.O) GO TO 57
    WRITE(6,916)PHWTT(1),PHWTT(2),PHWTT(3),PHWTT(4),PHWTT(5),PHWTT(6),
   1PHWTT(7),PHWTT(8)
 57 CUNTINUE
    IF(NSP.EQ.O)GO TO 65
    WRITE(6,910)SWGJ,SWEI,SWM,SWR
    DU 60 I=1.NES
 60 WRITE(6,911)I, ECHI(I), I, AK(I), I, AC(I), I, BJ(I)
    WRITE(6,912)CAPK,CAPC
65 WRITE(6,913)
    WRITE(6,914)(I,EGNS(I),I=1,NEGN)
```

```
70 DM1#DM
      MO*MO=SMD
      FGRAMAG
      GCTCP#CUS(GT) +COS(GP) +AG
      MO+0.S=TMU
      IF (DACD.GT.0.0) OMTHO.0
      UMDA=UM+8DCU
      NFF=2+MXSHI
C
      IF (MAER, EQ. 0) GO TO 80
      CALL TABLU
      DU 75 Km1, NAS
      DU 75 Lai, NFF
      ARG=L+((K-1)+3.1415926+2.0/NAS)
      CPSI(K,L)=CUS(ARG)
   75 SPSI(K,L)#SIN(ARG)
      SCHI=SIN(CHI)
      SZET=SIN(ZETA)
      CZET=COS(ZETA)
      CCHI CUS(CHI)
      FVLT#FVEL#8CHI#CZET
      FVLP#FVEL + CCHI + CZET
      FVLA=FVEL+8ZET
   BO CALL SECPAR
      IF(MFU8.EQ.0) GU TO 85
      IF (MAER.EQ. 0) GU TO 85
      IF(NSK,EQ.O) GO TO 85
      CALL FAERU
   85 CONTINUE
  900 FURMAT(1H1, T37, 'HELICUPTER AEROELASTIC STABILITY ANALYSIS INPUT PA
     1RAMETERS 1//)
                                                              = ',13,3X,
                                           = ',13,'
                                                       NBSEC
                                    NBP
  902 FURMAT(9x, 'NB
                         m ',13,'
                                . 1,13,1
                                                   = ',I3,'
                                                               NFFR # 1,
     1'NFSEC # 1,13,1
                         NBC
                                            NHC
                                                    NFEA = 1,13,3%,
                   = ',13,/,9x,'NFLAP = ',13,'
     213,1
             NAS
     3'NCT
              # ',I3,'
                         NCON # ',13,'
                                            NES
                                                    = ',13,'
                                                               MAXN
                                      · ',13)
                    = 1,13,1 FUA
     413,
             NSY
                                           m 1,13,1
                                                              = ',13,3X,
                        = ',13,'
                                  IPCT
                                                       NIT
  903 FURMAT(9X, INEGN
     1 INER
             - 1,13,1
                         NORM = 1,13,1
                                           IREM # ',13,'
                                                               NEX
                                        = 1,13,1
                                                   15
                   = ',13,/,9x,'IG
     213,1
             NPS
                                   . ',13)
          NLEL
                 # ', 13, ' MCTY
                                     1,44,1
                                              CONT TORQUE EQ
  905 FURMAT(/, 11x, FLAP HINGE
     1 1
                                    ARTICULATED SYS 1, A4,
                           1,44,1
          PITCH BEARING
     21
                                                        1,44,
                           ',A4,/,11x,'FUSELAGE
          CONSTRAINT APP
                                                     1 . 44 .
                                    AERODYNAMICS
     3'
          BLADE PHASING
                           1,44,1
     41
          GIMBALLED SYSM. ',A4,'
                                    VARIABLE OUTPUT 1,44,/,8x,
     5'
                                                    1,44,
          DISK PLANE CALC ', A4, '
                                    FUSELAGE AERO.
          SWASHPLATE IN
                           1,44,1
                                    COLL SPRING IN
                                                    1.44.
     71
          VI DIST USED
                           1,44)
                                   1,44,1
                                            SHAPE PUNCHED
  906 FORMAT(11x, SEARCH OPTION
                                                             1,44,
          LEAD-LAG HINGE ', 44)
```

3-12 .45

on 197 inches the Control of Section Sections

```
907 FORMAT(/,9x, 'ROTOR SPEED = ',F12.6,' VEL OF SOUND = ',F12.6,
                                    CRAFT VEL.
       AIR DENSITY # ',E12.5,'
                                                 = 1,F12,6,/,6x.
  1 1
                                    ANGLE ZETA
                                                 = 1,F12.6,
  21
                     = 1,F12.6,1
        ANGLE CHI
       THETA GRAV.
                    # 1,F12,6,1
                                    PSI GRAVITY = 1, F12.6, /, 6x.
  31
                                                 # 1,F12.6,
                     # 1,F12,6,1
                                    DELTAS
  41
       COEF. C(K)
                                    COLL. ANGLE # 1,F12.6)
                     # ',F12,6,1
  51
        ALPHA1
                                                        = 1,F12,6,
908 FORMAT (9x, 'GR RATE STEP = 1,F12.6, FREQ. STEP
  11
       GRAV. ACC. # 1, F12.6, 1 SHAFT FLEX. # 1, £12.5, /, 9X,
  2'STR. DAMPING = 1, F12.6, 1 F/A CYCLIC = 1, F12.6,
      LUNG CYCLIC # 1 ,F12.6,1
                                    DAMPING OUT = ',F12.6,/,9x,
  4'SPUR LENGTH = ',F12.6,' SPUR EIY
                                              = ',E12.5,
  51
       SPUR EIT
                     # 1,E12,5,1
                                   COEI
                                                  ■ ',E12.5,/,9X,
                  = ',E12.5,' COE3
                                              # ',E12.5,/)
  PICOES
909 FORMAT(10x, 'PHIM(', 11, ') # ', F11.7, ' AKCI(', 11, ') # ', F11.7,
  1' TAU(',I1,') # ',F11.7,' BMLA(',I1,') # ',F11.7,
  2' DMS(',11,') = ',F11.7)
920 FORMAT(8x, 'PHIM(', 11, ') #', F10, 7, ' AMKC(', 11, ') #', E11, 5,
  1' CTAU(',11,') #',F10.7,' PHIC(',11,') #',F10.7,
  2' THEC(',11,') =',F10.7,/,6x,' AL12(',11,') =',F10.7,
   3' ALSTH(',11,') =',F10,7,/)
910 FORMAT(/,8x, SWASHPLATE , TORSIONAL STIFF. = ',E12.5,
  1', BENDING STIFF. = ',E12.5,', MASS = ',F10.5,
  2', RADIUS = ',F6.3,/)
911 FURMAT(19x, 'ECHI(', 11, ') = ', F12, 8, ' AK(', 11, ')
  1' AC(',11,') = ',F12.6,' BJ(',11,') = ',F12.7)
FORMAT(43x,'CAPK = ',F12.2,' CAPC = ',F12.6)
912 FURMAT(43x, CAPK
915 FURMAT(//)
914 FORMAT(40x, 18TARTING EIGENVALUE 1,11, 1 = 1,2E14.7)
915 FORMAT(/,9x, 'EL #1, F12.6, ' EAC # 1, E12.5, ' E1YY # 1, E12.5,
  11
                            ALP #1, $12.6, /, 9x, 'BET #1, $12.6,
       EIZZ = ',E12.5,'
  21
        GAM = ', F12.6, '
                            GJTT = ',E12.5,/)
                                                      ETYP # 1.E12.5.
916 FORMAT(/, 9X, 'PLEN B', F12.6,' EACP # ', E12.5,'
  11
       EIZP # 1,E12.5,1
                           ALPP #1, F12.6, /, 9x, 'BETP #1, F12.6,
        GAMP . ',F12.6,'
                            GJTP = ', E12, 5, /)
    RETURN
    END
```

```
SUBROUTINE LOADIN(X)
C
      DIMENSION T(5), X(1)
C
      IPPP = 0
    1 READ(5,10) K, J, (T(L),L=1,5)
   10 FURMAT(14, 11, 5E14.7)
      IF(J.EQ.6) GO TO 6
      IF(J.EQ.8) GD TO 8
      IF(J.EQ.9) GO TO 9
IF(IPPP.NE.0) GO TO 11
      WRITE (6, 45)
   45 FURMAT(1H1)
      WRITE(6,25)
      IPPP # 1
   11 DU 12 L=1,J
      N = K + L - 1
   12 X(N) # T(L)
      WRITE(6,55) K, J, (X(M),MMK,N)
   55 FORMAT(11x, 14, 8x, 11, 5x, 5(G14,5,4x))
      GO TU 1
    6 WRITE (6,35)
   35 FORMAT(5x, 'ERROR - INVALID CARD')
      60 TO 9
   25 FORMAT(T41, PRINT OUT OF INPUT DATA
                                              '/11x, 'LOC', 8x, 'NUM',
     1 9x, 'VAL1', 14x, 'VAL2', 14x, 'VAL3', 14x, 'VAL4', 14x, 'VAL5'/)
    8 RETURN
    9 CALL EXIT
      END
```

```
SUBROUTINE SECPAR
      REAL 80(4000)
      REAL Y(100)
      REAL 8A(3,3), SAT(3,3), BC(3), SBT(3,3)
      REAL+8 CX(75)
      COMMON/SAIN/SD
      COMMON/SUB/Y
      CUMMUN/CFLEX/CX
      COMMON/ROTF/OH1, OM2, OMT
      COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
     1 MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
     2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
     3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
     4NFP1, MXSMI, MXT2P1, MXKU, MXCPL, MXCSB, MXCPM, MXCPK, MXSMR,
     SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
     SHEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MUDE
      COMMON/PLOAD/STOR, OM, SDVEL, AIRD, FVEL, CHI, ZETA, THC, AFO, APO, COLL, AG,
     1GT, GP, APD, ASK, BN, BPN, BNS, FNS, FLAPM, FEAM, CTM, CONM, AFLEX, AERM,
     2AFFB, FLAN, FEN, CTN, CON, BCT, FUSM, ASN, CNH, VIN, SPC, SPH, ESN, SCC, WMA,
     48RA, SHTS, SHBS, TFX, PRS, RT, EGNM, SR(5), SI(5), PCTI, ANIT, ERM, ANOR, AREM
     SANEX, PNS, SCHN, AIG, AIF, STG, STF, PHIM(6), AKC(6), ATAU(6), TAK(4), TAC(4)
     6, SMA(6), DBS(6), PAK(4), PAC(4), ECHI(4), AKE(4), ACE(4), BJE(4), CAKE,
     7CACE, STKC(6), BTAU(6), PHIC(6), THEC(6), BL12(6), SDCO, PUNI,
     SCYFA, CYLA, CELM, CELN, DACO, CTYM, AEXT, EYEX, EZEX, COE1, COE2, COL3,
     9PHUTT(8), PHWTT(8), CLESP(6), P(2000), V(25,24)
      COMMUNINCEAD/MLEL, NLEL, MCTY
C
      COMMON/FWVEL/FVLT, FVLP, FVLA, SCHI, CCHI
      CUMMUN/AMASI/GCTCP
      CUMMON/FAIRS/ARVZ, ARVY, ARMO
      COMMUN/IARST/ILL, JSECK
      ILL=0
      TEMPNHO.0
      TEMVYBO.0
      TEMVZ#0.0
      TEMPTRO. 0
       TEMMZ#0.0
      TEMMYBO. 0
      WRITE(6,954)
  954 FURMAT(//,34x,'STEADY FORCES AND MOMENTS',/,4x,'SECTION',5x,'N',
     113x,'vy',12x,'vZ',12x,'T',13x,'MZ',12x,'MY',//)
      DO 30 Ja1, NSY
   30 Y(J)=0.0
       IF (CUE2.NE.0.0) GU TO 98
      CUEZ#1000.
       WRITE(6,917)
  917 FORMAT(//,10X, 'CHE2 WAS O, HESET TO 1000, IF USED',//)
   98 CONTINUE
      MC=0
      NTOT=NBSEC+NFSEC
```

```
DO 60 JEI, NTOT
   JSECK#J
   IF(J.NE.(NBSEC+1)) GO TU 32
   TEMPNEO. 0
   TEMVY=0.0
   TEMVZ=0.0
   TEMPT=0.0
   TEMMZ=0.0
   TEMMY=0.0
32 IB=(J=1) *50
   M1=P(IB+1)+.1
   M2=P(IB+2)+.1
   M3=P(IB+3)+.1
   M4=P(IB+4)+.1
   M5=P(IB+5)+.1
   M6=P([8+6)+.1
   M7=P(IB+7)+.1
   Y(1)=M1
   Y(2)=M2
   Y(3)=M3
   Y(4)=M4
   Y(5)=M5
   Y(6)=M6
   Y(7)=M7
   P15=P(IB+15)
   P16=P(18+16)
   P17=P(18+17)
   IF(J.GT.NBSEC) GD TD 33
   IF (MFLEX.EQ. 1)P17#P17+CULL
   IF (MFLEX.EQ.O.AND.J.LE.NFFA)P17=P17+COLL
33 Y(11)=SIN(P15)
   Y(12)=COS(P15)
   Y(13)=SIN(P17)
   Y(14)=CUS(P17)
   Y(15)=SIN(P16)
   Y(16)=C()8(P16)
   Y(18) = Y(12) * Y(15)
   Y(19)=Y(12)*Y(16)
   Y(20) = Y(16) + Y(13)
   Y(21)=Y(16) *Y(14)
   Y(22)=Y(11)*Y(15)
   Y(23) = Y(11) * Y(16)
   Y(24) = Y(11) *Y(14) +Y(18) *Y(13)
   Y(25) = Y(12) + Y(14) + Y(22) + Y(13)
   Y(26)=Y(11)*Y(13)+Y(18)*Y(14)
   Y(27) == Y(12) + Y(13) + Y(22) + Y(14)
   GU TU 15
34 IF (M1.EQ.0) GO TO 35
   Y(8)==P(18+8)
   Y(9)=P(1B+9)
```

```
P10=P(IB+10)
 P11=P(IB+11)
 P12==P(18+12)
 Y(10) = P(18+13)
 P14==P(IB+14)
  IF (M1 .EQ. 2) GO TO 1
  Y(17) = 0 M2 + Y(16) + Y(16)
 Y(28) = 0 M 2 + Y(15) + Y(21)
  Y(29) = UM2 + Y(15) + Y(20)
 Y(30) = DM2 + Y(20) + Y(21)
 C2TS2P=Y(20)*Y(20)
 C2TC2P=Y(21)*Y(21)
 32T=Y(15)*Y(15)
  Y(31)=0M2*(C2T32P+32T)
  Y(32)=DM2*(C2TC2P+92T)
  Y(33) = Y(8) * Y(9)
 EP2M=Y(33)*Y(9)
 CZMX=P14-P12
  Y(34)=P12+EP2M
  Y(35) =P14+EP2M
 CXMYPE=Y(34)=Y(10)
 CZMYPE=Y(35)=Y(10)
 02ME#Y(33)+0M2
  TDTVY=02ME*(P10*Y(24)+P11*Y(25))
  TDTVZ=02ME*(P10*Y(26)+P11*Y(27))
  TDTN=U2ME+(P10+Y(19)+P11+Y(23))
  Y(36) = OMT*Y(20)*(Y(34) + Y(35) = Y(10))/2.0
  Y(37) = OMT+Y(21) + (CZMX=Y(10))/2.0
  Y(38) = OMT + Y(15) + (CZMX + Y(10))/2.0
  Y(39) = CXMYPE + Y(28)
  Y(40) #CXMYPE+DM2+(S2T-C2T82P)+TDTVY
  Y(41)=CXMYPE*Y(30)=TDTVZ
  Y(42) = CZMYPE * Y(28)
  Y(43) #CZMYPE+DM2+(CZTC2P-C2T82P)+TDTVY
  Y(44)=CZMYPE+Y(29)+TDTN
  Y(45) = CZMX \star Y(29)
  Y(46) == CZMX*Y(30)
  Y(47) == CZMX+OM2+(C2TC2P=32T)
  TEHX#Y(8)+OM2+P10
  TEHY#Y(8)+0M2+P11
  TEMPN#TEMPN#Y(33) *Y(29) #TEHX*Y(19) #TEHY*Y(23) #Y(8) *GCTCP*Y(15)
  TEHVY=TEMVY=Y(33)+Y(32)-TEHX+Y(24)-TEHY+Y(25)+Y(8)+GCTCP+Y(20)
  TEMVZ@TEMVZ+Y(33)*Y(30)~TEHX*Y(26)~TEHY*Y(27)+Y(8)*GCTCP*Y(21)
  TEMPT=TEMPT+CZMYPE+Y(30)=TDTVZ+Y(33)+GCTCP+Y(21)
  TEMMZ=TEMMZ+CXMYPE+Y(29)+TDTN+Y(33)+GCTCP+Y(15)
  TEMMY#TEMMY+CZMX#Y(28)
  GO TO 35
1 Y(8)=Y(8)
  P120-P12
  Y(10) == Y(10)
```

```
P14=-P14
   Y(33) = Y(8) + Y(9)
   Y(34)=P12+Y(33)*Y(9)
   Y(35) = P14 + Y(33) * Y(9)
35 IF (MAER.EQ. 0) GO TO 36
   IF (M3.NE.1) GO TO 36
   ILL=ILL+1
   CALL HAERU
   TEMPTHTEMPT+ARMU
   TEMVZ#TEMVZ+ARVZ
   TEMVY=TEMVY+ARVY
   GU TU 36
 2 IF (M2 .EQ. 0) GO TO 6
   IF (J.Eu. 1) Gn Tn 5
   IF (J, EQ. (NASEC+1)) GO TO 5
 3 SA(1,1)=Y(19)
   SA(1,2)=Y(23)
   SA(1,3) = Y(15)
   SA(2,1)=Y(24)
   SA(2,2)=Y(25)
   SA(2,3)=Y(20)
   SA(3,1)=Y(26)
   SA(3,2)=Y(27)
   SA(3,3)=Y(21)
   Y80*(5-L)=I
   SAT(1,1)=80(I+19)
   SAT(1,2)=SD(I+24)
   SAT(1,3)=SD(I+26)
   SAT(2,1)=SD(I+23)
   SAT(2,2) #80(1+25)
   SAT(2,3)=SD(1+27)
   SAT(3,1)=-SD(1+15)
   SAT(3,2)=SD(I+20)
   SAT(3,3)=SD(I+21)
   DU 4 I=1,3
   DU 4 N=1.3
   IND=59+3*(I=1)+N
   Y(IND)=0.0
   DO 4 K=1,3
 4 Y(IND)=Y(IND)+SA(I,K)+SAT(K,N)
   ASTENSTEMPN
   ASTVYETEMVY
   ASTVZ#TEMVZ
   ASTETATEMPT
   ASTMZ#TEMMZ
   ASTMY#TEMMY
   TEMPN= Y(60) +ASTEN+Y(61) +ASTVY+Y(62) +ASTVZ
   TEMVY# Y(63) #ASTEN+Y(64) #ASTVY+Y(65) #ASTVZ
   TEMVZ= Y(66) *ASTEN+Y(67) *ASTVY+Y(68) *ASTVZ
   TEMPT# Y(60) *ASTET+Y(62) *ASTMZ+Y(61) *ASTMY
```

```
TEMMY# Y(63) *ASTET+Y(65) *ASTMZ+Y(64) *ASTMY
      GU TU 6
    5 M2=0
       2M=(2)Y
       WRITE (6,902)
    6 IF (M4.EQ.0) GU TO 18
       STGJ=P(IB+27)
       STEIY=P(18+28)
       STEIZ=P(IB+29)
       Y(54) = TEMPN
       Y(55)=TEMVY
       Y(56)=TEMVZ
       Y(57)=TEMPT
       Y(58)=TEMMZ
       Y(59) TEMMY
      IF (M4. EQ. 2) GO TO 13
       SLEN = - P(18+26)
      SLEN2#SLEN+SLEN
      CFORCETEMPN
       IF (J .EQ. 1) GO TO 14
0000000
      P(18+30) = CFURC
      TOTTEO.
       IF(P(IR+25).LT.0.001) GO TO 39
       IF(CFURC.EG.O.)GO TO 39
       TDTT=(STEIY+STEIZ)+CFORC/(2.0*P(IB+25))
   39 CONTINUE
       GAMZ==SLEN#SQRT(CFURC/STEIZ)
       GAMY==SLEN+SQRT(CFORC/STEIY)
      NTEU
       GAMBGAMZ
       STEI=STEIZ
    9 GAMZ#GAM#GAM
       IND=70+NT+6
       IF (GAM .LT..02) GO TO 10
       SGAMESINH (GAM)
       CGAM=COSH(GAM)
       Y(IND) = SLEN + SGAM / GAM
       Y(IND+1) = SLEN2 * (CGAM-1.0) / (GAM2 * STEI)
       Y(IND+2) = SLEN+SLEN2+(SGAM-GAM)/(GAM+GAM2+STEI)
       Y(IND+3)=CGAM
       GO TO 11
   10 GAM4=GAM2+GAM2
```

TEMMZ= Y(66) \*ASTET+Y(68) \*ASTMZ+Y(67) \*ASTMY

```
Y(IND) = SLEN+(1. + GAM2/6.+GAM4/120.)
   Y(IND+1) = SLEN2+(.5+GAM2/24.+GAM4/720.)/STEI
   Y(IND+2)=SLEN+SLEN2+(1./6.+GAM2/120.+GAM4/5040.)/STEI
   Y(IND+3)=1.0+GAM2/2.+GAM4/24.
11 IF(NT. EQ. 1) GO TO 12
   GAMBGAMY
   STEI=STEIY
   GU TO 9
12 Y(69)=SLEN/(STGJ+TUTT)
   Y(74)=Y(70)/STEIZ
   Y(75)=SLEN
   Y(80)=Y(76)/STEIY
   Y(81)=SLEN
   TEMMZ=-SLEN*TEMVY+TEMMZ
   TEMMY#SLEN*TEMVZ+TEMMY
   GO TO 18
13 SLEN = P(IB+26)
   SLEN2=SLEN*SLEN
14 Y(69) = 8LEN/STGJ
   Y(70)=9LEN
   Y(71)=8LEN2*.5/STEIZ
   Y(72) = SLEN2 + SLEN/(6. + STEIZ)
   Y(73)=1.0
   Y(74)=SLEN/STEIZ
   Y(75) = 3LEN
   Y(76)=SLEN
   Y(77) =SLEN2+.5/STEIY
   Y(78)=SLEN2+SLEN/(6.+STETY)
   Y(79)=1.0
   Y(BU)=SLEN/STEIY
   Y(81)=SLEN
   TEMMZ==SLEN+TEMVY+TEMMZ
   TEMMY=+SLEN+TEMVZ+TEMMY
   GO TO 18
15 IF (M5.EQ.0) GO TO 2
   (4E+41)4==(58)Y
   Y(83) = P(18+39)
   Y(84)==P(IB+40)
   IF (M5 .EQ. 1) GO TO 16
   Y(82)=-Y(82)
   Y(83)==Y(83)
   Y(84) = -Y(84)
16 Y(85)=Y(84) +TEMVZ+Y(83) +TEMVY
   Y(86) == Y(82) + TEMVZ
   Y(87)==Y(82)+TEMVY
   Y(88) # #Y(84) *TEMPN
```

CC

```
Y(89) = Y(83) + TEMVY+Y(82) + TEMPN
   Y(90) == Y(84) + TEMVY
   Y(91)=-Y(83)+TEMPN
   Y(92)==Y(83) *TEMVZ
   Y(93) = Y(82) + TEMPN+Y(84) + TEMVZ
   TEMPT#+TEMVY*Y(84)=TEMVZ*Y(83)+TEMPT
   TEMMZ==TEMVY+Y(82)+TEMPN+Y(83)+TEMMZ
   TEMMY=+TEMVZ+Y(82)=TEMPN+Y(84)+TEMMY
   GO TO 2
17 IF(M6.EQ.0) GU TO 34
   Y(94)=-P(18+44)
   Y(95)=-P(IB+45)
   Y(96) == P(18+46)
   Y(97)=P(18+47)
   Y(98)=P(18+48)
   Y(99)=P(18+49)
   Y(100)==P(18+50)
   IF(M6.EQ.1) GO TO 34
   Y(94)==Y(94)
   Y(95)==Y(95)
   Y(96)==Y(96)
   Y(100) =- Y(100)
   GU TO 34
18 IF(M7.EQ.0) GO TO 17
   Y(4)=1.
   MC=MC+1
   IF(MC .EQ. 1) GO TO 19 WRITE (6,903)
   STOP
19 ELEPHOTT(1)
   EAC=PHUTT(2)
   EIYY=PHOTT(3)
   EIZZ=PHOTT(4)
   ALP=PHOTT(5)
   BET#PHOTT(6)
   GAMSPHOTT(7)
   GJTT=PHOTT(8)
   ELSO=EL*EL
    ELCU=ELSO+EL
    IF(MCTY.GT.O) GO TO 70
   CK1=3.0+EIYY/ELCU
    CK2=3.0+EIZZ/ELCU
    CK3=EAC/EL
    CK4=-CK1+EL
    CK5=CK2+EL
    CK6=CK1+EL80
    CK7#CK2+EL80
    GO TO 71
70 ALPPEPHNTT(5)
```

C

1

```
BETPEPHWTT(6)
   GAMP=PHWTT(7)
   SALESIN (ALPP)
  CAL=COS(ALPP)
   SHE=SIN(HETP)
  CREECUS(RETP)
   SGA=SIN (GAMP)
  CGA=CUS(GAMP)
   SAT(1,2)==SAL+CGA+CAL+SHE+SGA
   SAT(1,3) =+ SAL+SGA+CAL+SHE+CGA
   SAT(2,2)=+CAL+CGA+SAL+SBE+SGA
   SAT(2,3) == CAL+SGA+SAL+SBE+CGA
   SAT(3,2)=CBE+SGA
   SAT(3,3)=CBE+CGA
   SAT11#8AT(3,2)*8AT(1,3)#8AT(3,3)*8AT(1,2)
   (S,S)TAR*(E,E)TAR=(E,S)TAR*(S,E)TAR=SSTAR
   (S,1) TAR + (E, S) TAR + (1, 3) + SAT(1, 2)
   AXTN=AEXT/EL
   AXPEL=AEXT+EL
   PHLEN=PHHTT(1)
   TUS1=1.5+(1.+2.*AXTN)/EL
   AXTE2#AEXT+PHLEN+SAT22
   TUSZ=EL/3.=.5*PHLEN*SAT22
   TUS3#.25+AXTE2
   TUS4==.5*EL+PHLEN*SAT22
   TUP1=TUS1+PHLEN
   TUP2=TUS1 *AXTE2
   TUP3=,5+1,5*AXTN
   TUP4=TUP3+AXTE2
   TUPS=EL-PHLEN+SAT22
   AXTEL AXTNAAXTNAAXTN
   AXTZZ#AXTE1*(EIZZ/EZEX)
   AXTYY=AXTE1*(EIYY/EYEX)
   AXTEIM1.+3.+AXTN+(1.+AXTN)
   AXTE2#AXTZZ+AXTE1
   AXTE1=AXTYY+AXTE1
   CK1=3. *EIYY/(AXTE1*ELCU)
   CK2#3.*EIZZ/(AXTE2*ELCU)
   CK3=0.0
   CK4=-CK1+AXPEL
   CK5=CK2+AXPEL
   CK6==CK4*AXPEL
   CK7#+CK5*AXPEL
71 SALESIN(ALP)
   CAL=COS(ALP)
   SBE=SIN(RET)
   CBE=CUS(BET)
   SGA=SIN(GAM)
   CGAMCOS(GAM)
   CASB=CAL+SBE
```

```
SASBESAL + SBE
   SA(1,1)=CAL+CBE
   SA(1,2)==SAL+CGA+CASB+SGA
   SA(1,3)#SAL+SGA+CASB+CGA
   SA(2,1)=SAL+CBE
   SA(2,2)=CAL+CGA+SASB+SGA
   SA(2,3)==CAL+SGA+SASB+CGA
   SA(3,1)=-SRE
   SA(3,2) mCBE+SGA
   SA(3,3)=CBE+CGA
   DU 20 K=1,75
50 CX(K)=0.00
   DO 24 I=1.3
   BC(1) == SA(I,1) +CK3
   BC(2)==8A(I,2)+CK2
   BC(3) = -SA(I,3) *CK1
   IXXEO
   IF (I .EQ. 2) IXX=5
   IF (I .EQ. 3) IXX=9
   DO 21 NEI.3
   IXABIXX+N
   DO 21 Km1.3
21 CX(IXA)=CX(IXA)+BC(K)+SA(N,K)
   BC(2)==SA(1,3)+CK4
   BC(3)=-SA(1,2)*CK5
   IXX=IXX+3
   DU 22 N=1.3
   IXABIXX+N
   DU 22 K#2,3
22 CX(IXA) mCX(IXA) +BC(K) +SA(N,K)
   BC(2)==SA(I,2)*CK6
   BC(3) = -8A(1,3) + CK7
   IXX=IXX+3+(5=I)
   DO 23 N#1.3
   IXABIXX+N
   DO 23 K=2,3
23 CX(IXA)mCX(IXA)+BC(K)+8A(N,K)
24 CONTINUE
   IF (MCTY_EQ.O) GO TO 17
   CK1==1.0
   CK3==TUP1+SAT11/AXTE2
   CK4==(AXTZZ+TUP2)/AXTE2
   CK5#TUP1*8AT33/AXTE1
   CK6==(AXTYY+TUP2)/AXTE1
   DO 72 I=1,3
   IXX=21+(I-1)+3
   BC(1)==SA(I,1)*CK1
   BC(2)=-SA(I,1)+CK3-SA(I,2)+CK4
   BC(3)==8A(I,1)+CK5=8A(I,3)+CK6
   DU 72 Na1,3
```

```
IXABIXX+N
  DO 72 K=1,3
72 CX(IXA)=CX(IXA)+BC(K)+SA(N,K)
  CK1#-PHLEN+SAT33
  CK2#=PHLEN+SAT11
  CK3=(AXTYY-TUP3)+PHLEN+SAT33/AXTE1
   CK4=(AXTYY+TUP5+TUP4)/AXTE1
   CK5=(AXTZZ-TUP3) +PHLEN+SAT11/AXTE2
   CK6==(AXTZZ+TUP5+TUP4)/AXTE2
   DO 73 1=1.3
   IXX=30+(I=1)*3
   BC(1) == SA(1,2) +CK1 = SA(1,3) +CK2
   BC(2)=-SA(I,1)+CK3-SA(I,3)+CK4
   BC(3)==8A(I,1)+CK5=8A(I,2)+CK6
  DU 73 N=1.3
   IXA=IXX+N
   DU 73 K=1.3
73 CX(IXA) #CX(IXA) +BC(K) +SA(N,K)
   ICCP=0
   CK1=PHLEN+SAT11
   CK2=PHLEN+SAT22
   CK3=PHLEN+SAT33
   CK4=TUS1/AXTE1
   CK5=-TUS1/AXTE2
   DU 74 I=1,3
   DU 74 N=1.3
74 SAT(I,N)=0.0
   SAT(1,1)=1.0
   SAT(2,1) == CK1 + CK5
   SAT(3,1)=-CK3+CK4
   SAT(2,2)==CK2+CK5+(AXT2Z+AEXT+TUB1)/AXTE2
   SAT(3,3)=CK2*CK4+(AXTYY+AEXT*TUS1)/AXTE1
65 IXX=39+ICCP+9
   DU 75 I=1,3
   DU 75 N=1.3
   3BT(N, I)=0.0
   DU 75 Km1.3
75 SHT(N,I) = SRT(N,I) + SAT(K,I) + SA(N,K)
   DU 76 N#1.3
   IXAT=1XX+(N=1)*3
   DU 76 I=1.3
   IXA=IXAT+I
   DO 76 K=1.3
76 CX(IXA)=CX(IXA)+SA(I,K)+SBT(N,K)
   ICCP=ICCP+1
   IF(ICCP.GT.3) GU TU 90
   DU 78 I=1,3
   00 78 Na1,3
78 SAT(I,N)=0.0
   IF (ICCP.GT.1) GO TO 79
```

```
CK4=(AXTZZ=TUP3)/AXTE2
   CK5=(AXTYY-TUP3)/AXTE1
   SAT(2,1) =- CK3+CK5
   SAT(3,1) == CK1 + CK4
   SAT(1,2)=CK3
   SAT(3,2)=-CK2*CK4+EL*(AXTZZ+AXTN*TUP3)/AXTE2
   8AT(1,3) =CK1
   SAT(2,3) =CK2+CK5=EL+(AXTYY+AXTN+TUP3)/AXTE1
   GU TO 85
79 IF(ICCP.GT.2) GO TO 80
   CK4=-TUS1/AXTE1
   CK5=TUS1/AXTE2
   SAT(2,1) == CK1 + CK5
   SAT(3,1) =- CK3+CK4
   SAT(2,2) == CK2+CK5+(1,+1,5+AXTN)/AXTE2
   8AT(3,3) =CK2+CK4+(1.+1.5+AXTN)/AXTE1
   GD TO 85
80 CK4mEL*((AXTYY*TUS4+TUS3)/AXTE1)/EIYY
   CK5=-EL+((AXTZZ+TU84+TUS3)/AXTE2)/EIZZ
   CK6m-EL+((.25+AXTZZ)+CK1/AXTE2)/EIZZ
   CK7==EL*((.25+AXTYY)*CK3/AXTE1)/EIYY
   SAT(1,1)=-CK3+CK7=CK1+CK6+EL/EAC
   SAT(2,1) == CK1 + CK5
   8AT(3,1)=-CK3+CK4
   SAT(1,2)==CK2+CK6+ELSG+(CK1+(AXTN/4=+AXTZZ/2=)/AXTE2)/EIZZ
   SAT(2,2)=CK3+CK3+EL/GJTT=CK2+CK5+ELSQ+((AXTZZ+TU82+AXTN+TU93)/AXTE
  12)/EIZZ
   SAT(3,2) mck3*ck1*EL/GJTT
   8AT(1,3)=CK2+CK7-EL8Q+(CK3+(AXTN/4.-AXTYY/2.)/AXTE1)/EIYY
   SAT(2,3) =CK1+CK3+EL/GJTT
   8AT(3,3)=CK1+CK1+EL/GJTT+CK2+CK4+EL8Q+((AXTYY+TU82+AXTN+TU83)/AXTE
  11)/EIYY
   GO TO 85
90 CONTINUE
   CX(64)==CX(64)
   CX(65)==CX(65)
   CX(66)=-CX(66)
   60 TO 17
36 IF(J.GT.NBSEC) GO TO 93
   IF(MFLEX.GT.0) GO TO 43
   IF(MFLAP.EQ.O) GO TO 37
   IF(J.EG.NFLAP) TEMMY=0.0
37 IF(MLEL, EQ. 0) GO TO 38
   IF(J.EQ.NLEL) TEMMZ#0.0
36 IF(MFEA, EQ. 0) GO TO 41
   IF (J.EQ.NFEA) TEMPTHO. 0
41 IF(MCT.EQ.0) GO TO 93
   IF(J.NE.NCT) GO TO 93
   IF (MFEA.EQ.O) GO TO 91
   TEMPTATEMPT+COE3
```

```
GO TO 93
 91 TEMVZ=TEMVZ-(COE1-TEMPT)/COE2
    TEMPTACOE1
    GU TU 93
 43 IF(MCON, EQ. 0) GO TO 93
    IF (J.NE.NCUN) GO TO 93
    TEMVZ=TEMVZ=(COE1=TEMPT)/COE2
    TEMPT#COE1
 93 CUNTINUE
    Y(48) #TEMPN
    Y(49)=TEMVY
    Y(50) TEMVZ
    Y(51)=TEMPT
    Y(52)=TEMMZ
    Y(53) TEMMY
    WRITE(6,953) J, TEMPN, TEHVY, TEMVZ, TEMPT, TEMMZ, TEMMY
953 FURMAT(5x,15,6(2x,E12.5))
 25 DO 50 L=1,NSY
    M=(J=1)+N8Y+L
 50 8D(M)=Y(L)
    DO 55 1=1,NSY
 55 Y(1)=0.0
 60 CUNTINUE
    DO 200 KK#1,4
    K=0
    DO 201 ISE1, NTOT
    185=18
    IF (IS.GT.NBSEC) ISSEIS-NBSEC
    GO TO (301,302,303,305),KK
301 IF (IS .EQ. 1) WRITE (6,501)
    WRITE (6,502) 188, (P(L+K), L=1,13)
    GO TO 202
302 IF (18, Eq. 1) WRITE (6,503)
    WRITE (6,504) 185, (P(L+K), L=14,17), (P(L+K), L=19,22)
    SO TO 202
303 IF (18. EQ. 1) WRITE (6,505)
    WRITE(6,506) 188, (P(L+K), L=23,30)
    GO TO 202
305 IF (IS. EQ. 1) WRITE (6,508)
    WRITE (6,509) ISS, (P(L+K), L838,50)
202 K#K+50
201 CUNTINUE
200 CUNTINUE
501 FORMAT(1H1,//, T58, SECTION INPUT DATA ,//, T18, ORDER OF SECTIONS:
   IBLADE TIP (SECTION 1) TO HUB, THEN FROM FREE END OF FUSELAGE (SECTI
   20N 1) TO HUB',///,T16, '85CTION M1
                                            MZ
                                                  MS
                                                         M4
                                                               MS
                                                                      MA
       M7',7%,'M',8%,'ERY',7%,'HRX',6%,'HRY',7%,'IX',8%,'IY')
```

C

```
502 FORMAT(17x,12,5x,7(f3,1,3x),F10,5,2x,f4,3,2(2x,f7,3),3x,f8,3,3x,
   1F8.3)
503 FORMAT(1H1,8(/), T16, 'SECTION', 6x, 'IZ', 9x, 'PHI', 8x, 'THETA', 7x, 'P8I'
   1,7x,'L(AERO)',6x,'RULL',9x,'YAH',11x,'DEL')
504 FORMAT(17x,12,6x,F10,4,3x,3(F8,5,3x),4(E11,4,2x))
505 FORMAT(1H1,8(/),T10,'SECTION',3X,'CHORD',9X,'IND. VEL',6X,'XXXX',1 10X,'L(ELA)',8X,'(GJ)T',9X,'(EJ)Y',9X,'(EJ)Z',9X,'(P)T')
506 FORMAT(10x,12,4x,8(E11,4,3x))
                                                                        NoRIG
508 FORMAT(1H1,8(/),T4,'SECTION',2X,'DEL X
                                                      DEL Y
                                                                DEL Z
                                                                    TAU X TAU Y
                                                      1/KZ
   1VY=RIG VZ=RIG
                        1/KX
                                       1/KY
   Z TAU Z
                 KIT
509 FURMAT(6x,12,4x,6(F7,4,1x),3(E11,4,1x),3(F7,4,1x),E11,4)
902 FORMAT(20x,'BEND NOT ALLOWED AT BLADE TIP OR FUSELAGE FREE END')
903 FORMAT(10x, ONLY 1 CONSTRAINT SECTION ALLOWED, JOB ABORTE'S
    RETURN
    END
```

```
SUBROUTINE BAERO
    REAL SD(4000)
    REAL Y (100)
    REAL+8 TC(34)
    REAL SPSI(24,6), CPSI(24,6)
    COMPLEX EXPF
    COMPLEX+16 AMA(2550)
    COMMON/SAIN/SD
    COMMON/SUB/Y
    COMMON/AMAT/AMA
    COMMON/STAB/CPSI, SPSI
    COMMON/TAER/THCK, THC1, THC2
    COMMON/AERZ/RCD2, RC2D2, PRC2D4, PRC3D6, CD4MD, AZER
    COMMON/AER3/OFYDP, DFZDP, DMDP, DFYDYY, DFZDYY, DMDYY, DFYDYZ,
       DFZDVZ, DMDVZ, CAPFY, CAPFZ, CAPM, VLLY, VLLZ, CAPP, ATAB
    COMMON/ROTF/OM1, OM2, OMT
    COMMON/FHVEL/FVLT, FVLP, FVLA, SCHI, CCHI
    COMMON/INTER/NSY, NRSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
   1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
   2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
   3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSS,
   4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXCSB, MXCPM, MXCPK, MXSMB,
   SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
   6NEISC, NEITC, MXTKN, NFF, HINPN, MAXPN, IBF, MODE
    COMMON/NLEAD/MLEL, NLEL, MCTY
    COMMON/PLOAD/STOR, OM, SOVEL, AIRD, FVEL, CHI, ZETA, THC, AFO, APD, COLL, AG.
   1GT, GP, APD, ASK, BN, BPN, BNS, FNS, FLAPM, FEAM, CTM, CONM, AFLEX, AERM,
   2AFFB, FLAN, FEN, CTN, CON, BCT, FUSH, ASN, CNH, VIN, SPC, 8PH, ESN, SCC, HMA,
   48RA,SWTS,SWBS,TFX,PRS,RT,EGNM,SR(5),SI(5),PCTI,ANIT,ERM,ANOR,AREM,
   SANEX, PNS, SCHN, AIG, AIF, STG, STF, PHIM(6), AKC(6), ATAU(6), TAK(4), TAC(4)
   6,8MA(6),DB8(6),PAK(4),PAC(4),ECHI(4),AKE(4),ACE(4),BJE(4),CAKE,
   7CACE, STKC(6), BTAU(6), PHIC(6), THEC(6), BL12(6), SDCD, PUNI,
   SCYFA, CYLA, CELM, CELN, DACO, CTYM, AEXT, EYEX, EZEX, COE1, COE2, COE3,
   9PHOTT(8),PHWTT(8),CLESP(6),P(2000),V(25,24)
    CUMMON/IARST/ILL, JSECK
    COMMON/FAIRS/ARVZ, ARVY, ARMO
    WRITE(6,101)
101 FURMAT(1H1,//,T58, 'AERO CUEFFICIENTS',//,
   1T8, 'ALPHZ', 9X, 'AMACZ', 9X, 'CSUBL', 9X, 'CSUBD'
   2,9X,'CSUBM',9X,'CLALP',9X,'CDALP',9X,'CMALP')
    IF(ILL.GT.1) GO TO 5
    DO 12 I=1,2550
 12 AMA(I) #DCHPLX(0.D0,0.D0)
  5 PINU=3,141592654
    NAMA=34+MXSMI
    THEKETHE
    I=JSECK
    ARVZ=0.0
    ARVY#0.0
    ARMOSO.0
```

```
C
      MAMA=(ILL-1) +NAMA
C
      IB=(I-1)+50
C
      P19=P(IB+19)
      P22=P(IB+22)
      P23=P(18+23)
      CD4=P23/4.0
      RCD2=AIRD+P23/2.0
      RC2D2#RCD2*P23
      PRC204mPINO*RC202/2.0
      CD4MD=CD4-P22
      PRC3D6mPRC2D4+CD4
      THC1=1.0+THCK
      THC2=(1.0-THCK)/4.0
      ATABEP(IB+18)
      TFAC=1.0
000000
      OM15#UM1*Y(15)
C
      UMD15=P22+0M15
      OMHY#OM1*P(IB+11)
      DMHX=UM1*P(IB+10)
      CAPP==UM15
      VELIKEP(IB+24)
      APSI=P(1B+17)
      IF(MFLEX.EQ.1) APSIBAPSI+COLL
      IF (MFLEX.EQ.O.AND.I.LE.NFEA) APSIMAPSI+COLL
      DO 24 K=1,NAS
       IF(NVI.GT.O) VELIKEV(ILL,K)
       881K=8PSI(K,1)
      CSIK=CPSI(K,1)
       TPSINCYLA+CSIK-CYFA+SSIK
       STPSC=SIN(TPSI)
       CTPSC=COS(TPSI)
       TPSI=TPSI+APSI
       STPS#SIN(TPSI)
       CTPS#CDS(TPSI)
       FCY1#=Y(11) +CTP8+Y(18) +8TP8
       FCY2# Y(12)*CTP8+Y(22)*STP8
       FCY3# Y(11) +8TP8+Y(18) +CTP8
       FCY4==Y(12) +STPS+Y(22) +CTPS
```

```
UM20=UM1+Y(16)+STPS
UM21=UM1+Y(16)+CTP8
1)MD20=P22+()M20
UMD21=P22+0M21
BVLI=FVLT+SSIK=DMHY+FVLA+CSIK
BVLJ=FVLT+CSIK+OMHX-FVLA+SSIK
BVLK=FVLP+VELIK
VLLY=BVLI*FCY1+BVLJ*FCY2+BVLK*Y(16)*STPS
VLZM=BVLI*FCY3+BVLJ*FCY4+BVLK*Y(16)*CTPS
VLLZ=VLZM+OMD15
VLXM=BVLI+Y(19)+BVLJ+Y(23)=BVLK+Y(15)
VLLX=VLXM+OMD21
AZERESDVEL
CALL AERO(1, TFAC)
DYPTHUFYDP
DZPT=DFZDP
DYYTEDFYDVY
DZYT=DFZUVY
DYZT=DFYDVZ
DZZT=DFZOVZ
CFYTECAPFY
CFZT=CAPFZ
DFYDP=DYPT+CTPSC=UZPT+STPSC
DFZDP#DZPT*CTPSC+DYPT*STPSC
DFYDVY=DYYT+CTPSC-DZYT+STPSC
DFZDVY=DZYT+CTPSC+DYYT+STPSC
DFYUVZ#DYZT*CTPSC=DZZT*STPSC
DFZDVZ#DZZT*CTPSC+DYZT*STPSC
CAPPY=CFYT+CTPSC=CFZT+STPSC
CAPFZ=CFZT+CTPSC+CFYT+STPSC
TC(1)=DMDVZ*P22=DMDP
TC(2)=DMDVY
TC(3)=DMDVZ
TC(4)==DFYDVZ*P22+DFYDP
TC(5)=DFYDVY
TC(6) == DFYDVZ
TC(7)=+DFZDVZ+P22=DFZDP
TC(8)=-DFZDVY
TC(9)=DFZDVZ
TC(10)=CAPFY
TC(11)==CAPFZ
TC(12)=DMDVZ+DM20=DMDVY+DM21
TC(13)=DMDVZ+VLLY=DMDVY+VLZM
TC(14) = DMD VZ + DM15
TC(15) = DMD VZ + OMD 20 + DMD VY + VL XM = DMDP + OM20
TC(16) #DMD VY*OM15
TC(17)==DMDVZ+VLLX+DMDP+OM21
TC(18) GCAPM
TC(19) == OFYDVZ +UM20+DFYDVY+QM21
TC(20) == DFYDVZ + VLLY + DFYDVY + VLZM = CAPFZ
```

```
TC(21)==DFYDVZ*UM15
      TC(22)==DFYDVZ+OMD20=DFYDVY+VLXM+DFYDP+OM20
      TC(23) m - DFYD VY * UM15
      TC(24) #DFYDVZ+VLLX-DFYDP+OM21
      TC(25) == CAPM
      TC(26) = DFZDVZ+OM20= DFZDVY+OM21
      TC(27)=DFZDVZ+VLLY=DFZDVY+VLZM=CAPFY
      TC(28)=DFZDVZ+OM15
      TC(29) #DFZDVZ+DMD20+DFZDVY+VLXM=DFZDP+DM20
      TC(30)=DFZDVY+UM15
      TC(31)==DFZDVZ+VLLX+DFZDP+OM21
      TC(32)==CAPM
      TC(33)=CAPFY
      TC(34)=-CAPFZ
      ARVZMARVZ+CAPFZ*P19
      ARVY#ARVY+CAPFY#P19
      ARMUMARMU+CAPM*P19
      DU 20 NN=1, MXSMI
      NIENN-NFP1
      NEIABS(N1)
      AECPSI(K,N)
      B=SPSI(K,N)
      IF (N1.GT.0) GO TU 21
      IF (N1.LT.0) GO TU 22
      EXPF=CMPLX(1.0,0.0)
      GU TO 23
   21 EXPFECMPLX(A,-B)
      GU 10 23
   22 EXPF=CMPLX(A,6)
   23 IAMMMAMA+(NN=1)+34
      DO 20 J=1,34
   20 AMA(IAM+J) =AMA(IAM+J) =P19+TC(J) +EXPF
   24 CUNTINUE
   26 CONTINUE
      HAMPEMAMA+1
      JEMAMA+NAMA
      DU 28 IMMAMP, J
   28 AMA(I)=AMA(I)/NAS
      WRITE(6,703)(AMA(IN),IN=1,204)
C 703 FURMAT(8F10.6)
      ARVZ=ARVZ/NAS
      ARVY=ARVY/NAS
      ARMOBARMU/NAS
      RETURN
      END
```

```
SUBHOUTINE FAERU
  DIMENSION SD(4000), Y(100), AFA(240)
  COMMUN/FUSA/AFA
  CUMMUN/SAIN/SD
  COMMON/SUR/Y
  CUMMUN/AER2/RCD2, RC2D2, PRC2D4, PRC3D6, CD4MD, AZER
  CUMMUN/AER3/DFYDP, DFZDP, DMDP, DFYDVY, DFZDVY, DMDVY, DFYDVZ,
      DFZDVZ, DMDVZ, CAPFY, CAPFZ, CAPM, VLLY, VLLZ, CAPP, ATAB
  COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
  1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
 2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 31HEM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
 4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXC8B, MXCPM, MXCPK, MX8MB,
  SNEBC, NESHC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXO, NEIFC,
 6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
  COMMON/NLEAD/MLEL, NLEL, MCTY
  COMMON/PLOAD/STOR, OM, SOVEL, AIRD, FVEL, CHI, ZETA, THC, AFO, APO, COLL, AG,
  1GT,GP,APD,ASK,BN,BPN,BNS,FNS,FLAPM,FEAM,CTM,CONM,AFLEX,AERM,
  2AFFB, FLAN, FEN, CIN, CUN, BCT, FUSM, ASN, CNH, VIN, SPC, SPH, ESN, SCC, HMA,
  48RA, SWTS, SWBS, TFX, PRS, RT, EGNM, SR(5), SI(5), PCTI, ANIT, ERM, ANOR, AREM,
  SANEX,PNS,SCHN,AIG,AIF,STG,STF,PHIM(6),AKC(6),ATAU(6),TAK(4),TAC(4)
  6, SMA(6), DBS(6), PAK(4), PAC(4), ECHI(4), AKE(4), ACE(4), BJE(4), CAKE,
  7CACE, STKC(6), BTAU(6), PHIC(6), THEC(6), BL12(6), SDCO, PUNI,
  SCYFA, CYLA, CELM, CELN, DAGO, CTYM, AEXT, EYEX, EZEX, CDE1, CDE2, CDE3,
  9PHOTT(8), PHWTT(8), CLESP(6), P(2000), V(25, 24)
   AZER#SDVEL
   IL=0
   DU 12 I=1,240
12 AFA(I)=0.
   PINU=3.141592654
   DO 26 Imi, NFSEC
   L=(I=1) *NSY+NBSEC*NSY
   Y(3)=8D(L+3)
   M3=Y(3)+.1
   IF (M3.NE.2) GO TO 26
   IL-IL+1
   IB=(I-1)+50+NB3EC+50
   DU 16 Jm1, N8Y
16 Y(J)=8D(L+J)
   ATABEP (18+18)
   MTABRATAB+.1
   TFACM1.0
   IF (MTAB, EQ. 7) TFACHO, 0
   P19#P(IB+19)
   P20#P(18+20)
   P21=P(18+21)
   P228P(18+22)
   P23=P(1B+23)
   CD4#P23/4.0
```

RCD2#AIRD#P23/2.0

```
RC2D2#RCD2#P23
   PRC2D4=PIND+RC2D2/2.0
   CD4MD=CD4+TFAC=P22
   PRC3D6=PRC2D4+CD4
   Y79==FVEL+CUS(P20)+COS(P21)
   Y80= FVEL+8IN(P20)
   Y81==FVEL+COS(P20)+SIN(P21)
   CAPPEO.
   VLLX=Y80+Y(23)=Y81+Y(15)+Y79+Y(19)
   VLLY=Y80*Y(25)+Y81*Y(20)+Y79*Y(24)
   VLLZ#Y80*Y(27)+Y79*Y(26)+Y81*Y(21)
   CALL AERO(2, TFAC)
   IBB#(IL=1)+16
   AFA(IBB+1)=CAPFY
   AFA(IBB+2)=CAPFZ
   AFA(188+3)=DMUP=P22+DMDVZ
   AFA(IBB+4)=VLLZ+DMDVY-VLLY+DMDVZ
   AFA(188+5) = DMDVY
   AFA(IUB+6)=VLLX
   AFA(IBB+7)=DMUVZ
   AFA(IHB+8)=DFYDP=P22+DFYDVZ
   AFA(IBB+9)=VLLZ*DFYDVY=VLLY*DFYDVZ=CAPFZ
   AFA(IBB+10)=DFYDVY
   AFA(IBB+11)=DFYDVZ
   AFA(IBB+12)=DFZDP=P22*DFZDVZ
   AFA(IB8+13)=VLLZ+DFZDVY=VLLY+DFZDVZ+CAPFY
   AFA(IBB+14)=DFZDVY
   AFA(IBB+15)=DFZDVZ
   AFA(IBB+16)=CAPM
   DO 20 K=1.5
20 AFA(IBR+K) #AFA(IBB+K) *P19
   DU 21 Km7,16
21 AFA(IBB+K)=AFA(IBB+K)+P19
26 CONTINUE
   RETURN
   END
```

```
SUBROUTINE AERO(IBW, TFAC)
    CUMMUN/TAER/THCK, THC1, THC2
    COMMON/AFR3/DFYDP, DFZDP, DMDP, DFYDVY, DFZDVY, DMDVY, DFYDVZ,
   10FZOVZ, DMDVZ, CAPFY, CAPFZ, CAPM, VLLY, VLLZ, CAPP, ATAB
    CHMMUN/AER2/RCD2, RC2D2, PRC2D4, PRC3D6, CD4MD, SDVEL
    MTABBATAS+.1
    PINU#3.141592654
    VZERUSBART (VLLY*VLLY+VLLZ*VLLZ)
    IF (VLLZ.LT.0.0) GO TO 20
    IF (VLLZ.GT.0.0) GD TU 30
    IF (VLLY.LT.0.0) GO TO 11
    ALPHZ=0.0
    GO TO 40
 11 ALPHZEPING
    GU TO 40
 20 IF (VLLY.LT.0.0) GO TO 21
    IF (VLLY.GT.0.0) GD TO 22
    ALPHZ#.5*PINO
    GO TO 40
 21 ALPHZAPINO-ATAN(ABS(VLLZ/VLLY))
    GU TU 40
 22 ALPHZEATAN(ABS(VLLZ/VLLY))
    GU TU 40
 30 IF (VLLY, LT. 0.0) GU TO 31
    IF (VLLY.GT.0.0) GO TO 32
    ALPHZ#1.5*PINO
    GU TU 40
 31 ALPHZEPINO+ATAN(ABS(VLLZ/VLLY))
    GU TO 40
 32 ALPHZ=2.0*PIND=ATAN(ABS(VLLZ/VLLY))
 40 CONTINUE
    AMACZ#VZERO/SOVEL
    AMACIE1.0/(1.0=AMACZ#AMACZ)
    AMACZR(2.0-AMACZ+AMACZ)+AMAC1
    IF (IBW.EQ.1.AND.VZERO.EQ.0.0) WRITE(6,101)
101 FURNATCIOX, IMPENDING DIVISION BY VZERO EQUAL ZERO!)
    IF (IBW.EQ.2) THC1=2.0
    IF(IBW.EQ.2) THC2=0.0
    TC2C1=PRC2D4+THC1
    TC3C1=PRC3D6+THC1
    TC3C2#PRC3D6*THC2*4.0
    IF (IBW, EQ, 1) GO TO 2
    IF (VZERO.NE.O.O)GO TO 2
    RCD2V=0.0
    TC3CM#0.0
    GO TO 3
 2 RCD2V#RCD2/VZERO
    TC3CM#TC3C2/VZERO
 3 RCYDZV#RCDZV#VLLY
   RCZD2V#RCD2V#VLLZ
```

4

```
RCVD2=RCD2+VZERO
    IF(IBW.EQ.1) GO TO 5
    IF (MTAB.GT.5) GO TU 60
  5 ALPHZ=180. +ALPHZ/PIND
    IF (ALPHZ.GT.360.) ALPHZ=360.
    CALL ACOEFF (ALPHZ, AMACZ, CSUBL, CSUBD, CSUBM, CLALP, CDALP,
   1CMALP, MTAH)
    GU TO 70
 60 IF (MTAB.EQ.6) GQ TO 65
    CLALP=0.0
    CSUBL=0.0
    CSUBD=1.1
   CDALP=0.0
    GU TU 66
65 CLALP=5.73
    IF (ALPHZ.GT.PINO) ALPHZ#ALPHZ#2.*PINO
    CSUBLECLALP*ALPHZ
    CSUBD#.006+.13131*ALPHZ*ALPHZ
    CDALP=.26262*ALPHZ
    IF(ALPHZ.LT.O.)ALPHZ#ALPHZ+2.*PINU
 66 CMALPEO.
    CSUBMEO.
    ALPHZ=180.*ALPHZ/PIND
 70 CDTER=RCVD2+CSUBD
100 FURMAT(5x,8(E12.4,2x))
    WRITE(6,100)ALPHZ, AMACZ, CSUBL, CSUBD, CSUBM,
   1CLALP, CDALP, CMALP
    CLTER=RCVD2+CSUBL
    CHTER#RC202*AMAC2*CSUBM
    CMATE=RC2D2+CMALP
    VZCL=VLLZ*CSUBL
    VZCD=VLLZ*CSURD
    VYCL=VLLY*CSURL
    VYCD=VLLY*CSUBD
    FCSTL#VYCL*AMAC1+VLLZ*CLALP
    FCWKL=VZCL+AMAC1-VLLY+CLALP
    FCSTD#VYCD+AMAC1+VLLZ+CDALP
    FCWKD=VZCD+AMAC1-VLLY+CDALP
    DFYDP==TC2C1*VLLZ
    DFZDP#TC2C1*VLLY
    DMDP#CD4MD*DFZDP+TC3C2*VZERO+TC3C1*VLLY*TFAC
    DFYDVY==RCZD2V+FCSTL=RCYD2V+FCSTD=CDTER
    DFZDVY#RCYDZV*FCSTL*RCZDZV*FCSTD+CLTER+TC2C1*CAPP
    DMDVY#CMTER*VLLY+CMATE*VLLZ+CD4MD*DFZDVY
              -TC3CM+VLLY+CAPP-TC3C1+CAPP
    DFYDVZ=-RCZD2V*FCWKL-RCYD2V*FCWKD-CLTER
             -TC2C1+CAPP
    DFZDVZ#RCYD2V*FCWKL-RCZD2V*FCWKD-CDTER
    DMDVZ#CMTER+VLLZ-CMATE+VLLY+CD4MD+DFZDVZ
              -TC3CM+VLLZ+CAPP
   1
```

CAPFY==RCVD2+(VZCL+VYCD)+DFYDP+CAPP
CAPFZ=RCVD2+(VYCL=VZCD)+DFZDP+CAPP
CAPM=RC2D2+VZER0+VZER0+CSURM+CD4MU+CAPFZ
=CAPP+(TC3C2+VZER0+TC3C1+VLLY)
RETURN
END

```
SUBROUTINE TABLU
   COMMON/COEFFS/NTAB, NMACH(1,3), AMACH(11,1,3), NCL8(11,1,3),
   1ALPH8(11,50,1,3),CLDM(11,50,1,3),NCC(1,3),CC8(25,1,3)
  1 FORMAT(1415)
 2 FURMAT(7F10.0)
 3 FORMAT(5E14.7)
 11 FORMAT(7X,9F7.4)
 12 FURMAT(1F7.3,9F7.4)
 14 FURMAT(1X,F6.1,9F7.4)
    READ(5,1)NTAB
    WRITE(6,901)
901 FURMAT(1H1,58x, 'AERD TABLES',//)
    DO 10 MM=1,NTAB
    READ(5,1) ISER
    IF(ISER.GT.0) wRITE(6,900)
900 FURMAT(10x, FOR ISER EQUAL 1 UNLY CCS ARRAYS ARE INPUTTED!)
    READ(5,1)M
    DU 20 I=1,3
   READ(5,1)NCC1
   NCC(M,I)=NCC1
    READ(5,3)(CC8(K,M,I),K=1,NCC1)
    IF (ISER_EQ.81) GO TO 6
    IF(ISER, ER. 0)GD TU 5
   IF(CCS(1,M,1).GE.0.)STOP
    GO TO 20
  5 READ(5,1)NMACHS
    READ(5,2)(AMACH(K,M,I),K=1,NMACH8)
    NMACH(M,I)=NMACHS
    DU 30 J=1,NMACHS
    READ (5, 1) NCL
    NCLS(J,M,I)=NCL
    READ(5,2)(ALPHS(J,K,M,I),K=1,NCL)
 30 REAU(5,2)(CLDM(J,K,M,I),K=1,NCL)
    GD TO 20
  6 READ(5,1)NMACHS, NALF
    WRITE(6,1)NMACHS, NALF
    NMACH(M,I)=NMACHS
    NXLENMACHS
    IF (NMACHS.GE.10) NXL=9
    READ(5,11)(AMACH(K,M,I),K#1,NXL)
    WRITE(6,11)(AMACH(K,M,I),K=1,NXL)
    IF(NMACHS.GE.10) READ(5,11)(AMACH(K,M,I),K=10,NMACHS)
    IF (NMACHS.GE.10) WRITE (6,11) (AMACH(K,M,I),K=10,NMACHS)
    DO 7 J=1,NALF
    READ(5,12)ALP, (GLDM(K,J,M,I),K=1,NXL)
    WRITE(6,14) ALP,(CLDM(K,J,M,I),K=1,NXL)
    IF(NMACHS.GE.10)READ(5,11)(CLUM(K,J,M,I),K=10,NMACHS)
    IF(NMACHS, GE. 10) WRITE(6,11)(CLDM(K,J,M,I),K#10,NMACHS)
    DO 8 KEI, NMACHS
  B ALPHS(K,J,M,I) = ALP
```

7 CUNTINUE
DU 9 KR1, NMACHS
9 NCLS(K,M,I) RNALF
20 CUNTINUE
10 CUNTINUE
RETURN

END

```
SUBRUUTINE ACUEFF (ALPDD, AMACZ, CSUBL, CSUBD, CSUBM, CLALP, CDALP,
   1CMALP, MTAB)
   COMMON/COEFFS/NTAB, NMACH(1,3), AMACH(11,1,3), NCLS(11,1,3),
   1ALPHS(11,50,1,3),CLDM(11,50,1,3),NCC(1,3),CC8(25,1,3)
   ALPHZEALPDD
   PINU=3.141592654
   IF(CCS(1,MTAB,1)_LT.0.0) GU TU 410
   DU 400 L=1.3
   MME 1
   IMMTAB
    IF(CCS(2,I,L).GT.180.)GO TO 52
    IF(ALPHZ.GT.180.)ALPHZ#ALPHZ#360.
52 CONTINUE
   IF((ALPHZ.LE.CCS(1,I,L)).OR.(ALPHZ.GE.CCS(2,I,L))) GO TO 50
   GO TO 280
50 KSKIP=1
    IF(AMACZ.LT.AMACH(1,I,L)) GU TO 70
   GO TO 80
60 WRITE(6,901) ALPHZ,L
   MME2
    GO TO 370
 70 WRITE(6,902) AMACZ,L
    MME2
   GO TO 370
 BO NMACENMACH(I,L)
    IF (AMACZ.GT.AMACH(NMAC,I,L)) GO TU 260
 90 IF(ALPHZ.LT.ALPHS(1,1,1,L)) GU TO 60
   NCL=NCLS(NMAC,I,L)
    IF (ALPHZ.GT.ALPHS(NMAC, NCL, I, L)) GO TO 60
    IF(KSKIP.EQ.2) GO TO 160
    DO 150 KEI, NMAC
    IF(AMACZ.LT.AMACH(K,I,L)) GU TD 140
    IF (K.NE.NHAC) GO TO 150
140 IZ = K
    I1 = I2-1
    SGY = AMACH(I1,I,L)
    RM=(AMACZ=SGY)/(AMACH(I2,I,L)=SGY)
    GU TO 160
150 CONTINUE
160 NCLX=NCL8(I2,I,L)
    ALFWALPHZ
    NT=1
193 DO 190 LL=1,NCLX
    IF(ALF,LT,ALPH8(IZ,LL,I,L)) GO TO 180
    IF(LL.NE.NCLX) GO TO 190
180 J2=LL
    J14LL-1
    SGY=ALPHS(I2,J1,I,L)
    R2#(ALF-8GY)/(ALPH8(I2,J2,I,L)-8GY)
    SGY#CLDM(I2,J1,I,L)
```

## BEST AND COPY

```
IF (NT.EQ. 2) GO TO 192
   CL2#8GY+R2*(CLDM(12,J2,I,L)=8GY)
   PLF=CLOM(I2,1,I,L)
   GU TO 191
190 CUNTINUE
191 NT=2
    ALFEALF+1
    IF (ALF.GT.360.0) ALF#ALF=360.0
    IF(CCS(2,I,L).LE.180..AND.ALF.GT.180.)ALF#ALF-360.
    GU TU 193
192 SL2=8GY+R2*(CLDM(12,J2,I,L)=8GY)
    SLF=CLDM(I2,1,I,L)
    IF (KSKIP.EQ. 2) GO TU 270
    NCLY=NCLS([1,I,L)
    ALFSALPHZ
    NT=1
243 DE 240 LL=1, NCLY
    IF (ALF.LT. ALPHS(II.LL, I,L)) GU TH 230
    IF (LL. NE. NGLY) GO TO 240
230 J2=LL
    J1=LL-1
    SGY=ALPHS(I1, J1, 1, L)
    R1=(ALF-SGY)/(ALPHS(T1,J2,I,L)-SGY)
    SGY=CLDM(I1,J1,I,L)
    IF (NT.EQ. 2) GO TO 242
    CL1=SGY+R1*(CIDM(I1,J2,I,L)=SGY)
    QMG=CLUM(I1,1,I,L)
    GU TI1 241
240 CUNTIMUE
241 NT=2
    ALF=ALF+1
    IF(ALF.GT.360.0) ALF#ALF=360.0
    IF (CCS(2,I,L),LF.180..AND.ALF.GT.180.)ALF=ALF=360.
    GU TU 243
242 SL1=86Y+R1+(CLDM(I1,J2,I,L)=86Y)
    SMG=CLDM(I1.1.I.)
250 CLCX=CL1+RM*(CL2=CL1)
    DMDY=GMG+RM*(PLF=GMG)
    SLCX=SL1+HM*(SL2+SL1)
    SMDY=SMG+RM+(SL+=SMG)
    GO TO 390
SPU ISENHAC
    KSKIP=2
    GU TO 90
270 CLCX=CL2
    DMOY=PLF
    SLCX=SL2
    SMDY=SLF
390 IF(L-2) 391,392,393
391 CSUBL=CLCX
```

```
CLALPEIAO. /PINO*(SLCX=CLCX)
    GU TO 400
 392 CSUBDECLCX
     CUALPETRO. /PINO*(SLCX-CLCX)
     GU 111 400
393 CSUHMECLCX
    CMALPEISO. /PINO*(SLCX=CLCX)
400 CONTINUE
901 FURMAT(1H0,5X, COMPUTED ALPHA = 1,G12.4,
    1 UUTSIDE RANGE OF COEFFS = 1,12)
902 FURMAT(1H0,5X, COMPUTED MACH NO. = 1,G12.4.
   1 OUTSIDE RANGE OF CHEFFS = 1,12)
370 RETURN
240 ALFBALPHZ
    NTEL
    IF(L-2)600,700,800
600 DELBALF
    IF (ALF. GT. 1HO. O) DEL = 360. C-ALF
    TERM1=CCS(3,1,1)+CCS(4,1,1)+DEL+CCS(5,1,1)+DEL++2+
          CC4(6,1,1)+DEL++3+CC8(7,1,1)+DEL++4
    TERM2=CCS(A,I,1)+CCS(9,I,1)*DEL+CCS(10,I,1)*DEL**2
    IF (ALF.GT. 90.0) GU TO 610
    CLCxT=CCS(11,I,1)*TERM1
    60 TH 500
610 IF (ALF. GT. 160.0) GU TO 620
    CLCXT=CCS(12,I,1)*TERM1
    WILL TU 660
620 IF (ALF.GT.180.0) GI TH 650
    CLCxT=CCS(12,1,11+TERM2+CCS(13,1,11+(DEL=160.01/20.0
    Gir Til bon
650 IF (ALF.GT.200.0)GO TO 640
    CLCXT=-CCS(14,1,1) *TERM2+CCS(13,1,1) *(DEL-160.0)/20.0
    G() TU 660
640 IF (ALF. GT. 270.0) GO TO 650
    CLCXT==CCS(14,T,1) +TEHM1
    GU 111 660
650 CLCXT==CCS(15,I,1) *TERM1
660 IF (NT. FU. 1) CL( X=CLCXT
    SLCX=CLCXT
    IF (NT. E4.2) GH TH 390
    NIES
    ALFEALF+1
    IF (ALF.GT. $60.0) ALFEALF-360.0
    GU TH BOO
700 DELMALF
    IF (ALF. 61.90.0) GU TO 701
    XNUaDEL+(15.0-CCS(1,1,2))+((90.0-DEL)/(90.0-CCS(1,1,2)))
    GH TH 711
701 IF (ALF.GT.166.0) GU TO 703
    X110=180.0-ALF
```

```
GU TU 711
703 IF (ALF.GT. 1HO. 0) GO TO 705
    GI TO 713
705 IF (ALF.GF. 194.0) GO TO 707
    DEL=360.0-ALF
    Gir Tir 715
707 IF (ALF.GF.270.0) GU TH 709
    XNUEALF-180.0
    GU TU 711
709 XNU=360,0-ALF-(345,0-CC5(2,1,2))+((ALF-270,0)/
        (CCS(2,1,2)=270.0))
711 CLCXTBCC8(3,1,2)+CCS(4,1,2)*XNU+CC8(5,1,2)*XNU**2+
          CCS(A,I,2)*XNU**3+CCS(7,I,2)*XNU**4
   1
   GU TI) 799
713 CLCXT=CCS(A,I,2)+CCS(9,I,2)+DEL+CCS(10,I,2)*DEL**2
799 IF (NT.EU.1)CLCX=CLCXT
    SLCX=CLCXT
    IF (NT.EU. 2) GU TO 390
   NT#2
    ALFBALF+1
    IF(ALF.GT.360.0) ALF=ALF=360.0
    GO TU 700
800 DELMALF
    IF (ALF.GT.30.0) GU TO AU1
    CLCXT=CCS(3,1,3)+(30,=0EL)/14.0+CCS(4,1,3)+
          CCS(5,I,3)*DEL+CCS(6,I,3)*DEL**2+CCS(7,I,3)*DEL**3
   1
    GO TO 815
801 IF(ALF.GT.150.0) GP TU 805
802 CLCXT*CCS(8,1,3)+CCS(9,1,3)*DEL+CCS(10,1,3)*DEL**2+
   1
          CCS(11,I,3)*DEL**3+CCS(12,I,3)*DEL**4
   GU TU 815
803 IF(ALF.GT.168.0) GO TO 805
HOU CLCXT=CCS(13,1,3)+CCS(14,1,3)+DEL+CCS(15,1,3)+DEL++>+
          CC8(16,1,3)*DEL**3
    GO TO 815
805 IF(ALF.GT.1HO.0) GO TO 807
806 CLCXT*CCS(17,1,3)+CCS(18,1,5)+DEL+CCS(19,1,3)+DEL++2+
          CC8(20,1,3)*DEL**3+CC8(21,1,3)*DEL**4
    GO TO 815
BUT DELESON . OHALF
    IF(ALF.GE.192.0) GU TU 809
    GO TO 806
809 IF(ALF.GE.210.0) GD TU 811
    GO TO 804
811 IF(ALF.GE.330.0) GO TO 815
    GO TU 802
813 CLCXT=CCS(22,1,3) *(ALF=350.0)/(CCS(2,1,3)=330.0)=CCS(4,1,3)=
          CCS(5,I,3)*DEL=CCS(6,I,3)*DEL**2=CCS(7,I,3)*DEL**3
815 IF((ALF.GT.180.0).AND.(ALF.LT.330.0))CLCXT==CLCXT
A99 IF(NT.EQ.1)CLCX#CLCXT
```

```
SLCX=CICXT
    IF ("1. EU. 2) 611 711 390
    NI=5
    ALF=ALF+1
    IF (ALF. 67.360.0) ALF=ALF=360.0
    GO 10 800
410 IZMIAU
    Ç3Ua4=0.0
    CMALPED 0
    NEG=1
    ALF=ALPHZ
    SUT=SURT(1 .- AMACZ + AMACZ)
    L1=1. -AMACZ
    C2=CCS(2,1,1) *C1 *(1,+CCS(3,1,1))
    IF (ALF. LF. 180.) GU TO 412
    NF G==1
    ALF==4LF+360.
412 ALF=ALF+PIN(1/190.
    IF (ALF. GT. C2) GIJ TII 414
    CLALP=CCS(7,1,1)/SUT
    CSUBLECLALPALF
    CSUMD#CCS(1,1,2)+CCS(2,1,2)+ALF+ALF
    CDALP=2.0*CCS(2,1,2)*ALF
    GH 10 450
414 IF(ALF.GT.CCS(4,1,1)) GU TO 416
    C2=(CCS(11,1,1)+CCS(12,1,1)*AMACZ)*SQT
    CLALP=(CCS(9,1,1) *AMACZ+CCS(10,1,1))/CZ
    CSUBL=CLALP+ALF+C1+CCS(8,1,1)/CZ
    NTEI
    G(1 TI) 41A
416 IF (ALF.GT.CCS(5,1,1)) GO TO 420
    NTEU
418 SIESIN(ALF)
    SZESIN(2.0*ALF)
    83=SIN(3.0+ALF)
    S4=STN(4.0+ALF)
    C1=CUS(ALF)
    C2#CUS(2.0*ALF)
    C3=CUS(5.0+ALF)
    C4=C1)S(4.0+ALF)
    CSUBD=(CCS(3,1,2)+CCS(4,1,2)+C1+CCS(5,1,2)+C2
   1+CCS(6,1,2)+C3+CCS(7,1,2)+C4)/SUT
    CUALP=(-CCS(4,1,2)+91-2,+CCS(5,1,2)+92-3,+CCS(6,1,2)+S3
   1-4. *CCS(7, I, 2) *S4) /SOT
    IF (NT.GT.0) GO TO 450
   CSUBL=(CCS(13,I,1)*S1+CCS(14,I,1)*S2+CCS(15,I,1)*S3
   1+CCS(16, T, 1) +54)/SQT
   CLALP=(CCS(13,I,1)+C1+2,+CCS(14,I,1)+C2+3,+CCS(15,I,1)+C3
   1+4. *CCS(16, I, 1) *C4)/SQT
   CSUBM#(CCS(1,1,3) #81+CCS(2,1,3) #82+CCS(3,1,3) #83
```

```
1+CCS(4,1,3)+84)/SQT-,25+(CSUBL+C1+CSUBD+S1)
    CMALP#(CC8(10,1,3)+C1+CC8(11,1,3)+C2+CC8(12,1,3)+C3+CC8(13,1,3)+C4
   1+81+(CC8(14,I,3)+82+CC8(15,I,3)+83+CC8(16,I,3)+84))/9QT
    GO TO 450
420 IF(ALF,GT,CC8(6,I,1)) GU TO 422
    CLALP=CCS(18,1,1)/8QT
    CSUBL#CCS(17,1,1)/SGT+CLALP+ALF
    C8UBM#CC3(5, I, 3)/9QT
    NTEL
    GU TO 418
422 CLALP=CCS(20,1,1)/80T
    CSUBL=CCS(19,1,1)/SQT+CLALP+ALF
    CSUBM=CC8(6,1,3)+(CC8(7,1,3)=((ALF+CC8(8,1,3))/CC8(9,1,3)
   1))/301
    CMALPH-CC8(6,1,3)/(CC8(9,1,3)+5QT)
    NTEL
    GO TO 418
450 IF(NEG.GT.0) GO TO 370
    CSUBL = CSUBL
    CSUBME-CSUBM
    CDALPS-CDALP
    GD TO 370
    END
```

```
SUBROUTINE BARRAY
 INTEGER EM(6)
REAL+8 RREAL(144),CX,PLC,PFC
COMPLEX UBX(1,35,3), UBY(1,35,3), UBZ(1,35,3), PHIX(1,35,3),
1PHIY(1,35,3),PHIZ(1,35,3),AN(1,35,3),VY(1,35,3),VZ(1,35,3),
ZTEA(1,35,3), AMY(1,35,3), AMZ(1,35,3), QXJ, QYJ, QZJ
COMPLEX+16 CMS,CM1,CS1,CS2
CUMPLEX#16 R(144), T(72), B(648), SMLB(108), SMLC(108), SMLD(108)
COMPLEX#16 BSAVE(648), SMLBSV(108), SMLCSV(108), SMLDSV(108)
COMPLEXALS SHAPE(12), BLL, SMLBL, SMLCL, SMLDL, WSW
COMPLEX*16 EPS(63), ALM(63)
COMPLEX#16 CTB(54), FAB(54), FLB(54)
 COMPLEX#16 CTB1(9),CTB2(9),CTB3(9),FAB1(9),FAB3(9),FLB1(9),FLB2(9)
COMPLEX+16 D(144),C(144)
 COMPLEX+16 8MLE(108), SMLESV(108), F8B(54), SMLEL
 COMPLEX#16 F881(9),F882(9),F883(9),FA84(9),FL84(9),CT84(9)
 COMPLEX*16 SMLF(108), SMLG(108), SMLFSV(108), SMLGSV(108), SMLFL, SMLGL
 DIMENSION Y(100), 3D(4000), CX(75)
 COMMON/HARM/NHARM
 COMMUN/CALM/ALM
 COMMUN/EPSA/EPS
 COMMON/ARR/RREAL
 CUMMON/ARI/R
 COMMON/SUB/Y
 COMMON/SAIN/SD
 COMMON/ROTF/OM1, OM2, OMT
 COMMON/FREF/CM8, CM1, CS1, CS2
 COMMON/CFLEX/CX
 COMMON/COUP/PFC.PLC
 COMMON/818/B, SMLB, SMLC, SMLD, CTB, FAB, FLB, CTB1, CTB2, CTB3, FAB1, FAB3.
1FLB1,FLB2,SMLE,FSB,FSB1,FSB2,FSB3,FAB4,FLB4,CTB4,SMLF,SMLG
 CUMMUN/QVTEM/QXJ,QYJ,QZJ
 COMMON/ISUMA/NBGMD
 COMMON/NLEAD/MLEL, NLEL, MCTY
 COMMON/INTER/NBY.NBSEC,NFSEC,NB,NBP,MFLAP,MFEA,MCT,
1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
31REM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXC8B, MXCPM, MXCPK, MXSMB,
SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
 COMMON/IPCH/IPU
 DATA EM/1,15,29,42,57,70/
                   1/BTIPS/ITIP 1/BHUB/IHUB 1/
 DATA BLANKS/
 IL=0
 SPACEBBLANKS
 IWRITERO
 IF (MODE EQ. 1) IWRITE = 1
 NCCT#1
 NCFEAR1
```

```
NCFLP=1
   NCLEL=1
  NCACF=1
   NCACG=1
   ICTENCT
   IFEARNFEA
   IFLAMNFLAP
   ILEL NLEL
   IF (MCT_EQ_O) + CT=NHSFC+2
   IF (MFEA.EQ. U) NFEARNHSEC+2
   IF (MFLAP, EQ. 0) NFLAP=NHSEC+2
   IF (MLEL_EQ.O) NLEL=NRSEC+2
   IH=0
   IC=U
   IDEO
   IE=0
   IFF=0
   IGG=0
   MCACF=0
   MCACG=0
   DO 15 LET, MXSHH
   SMLE(L) #DCMPLx(0.U0,0.D0)
   SMLF(L)=DCMPLx(0.00,0.00)
   SMLG(L) #DCMPL X (0.00,0.00)
   SMLH(L)=DCMPLx(0.D0,0.D0)
   SMLC(L)=DCMPLx(0,U0,0,00)
15 SMLU(L)=DCMPLx(0,U0,0,D0)
   DU 55 K#1 MXCPK
55 B(K)=DCWb[X(0"D0'0"D0)
   D() 30 [=1, MXShI
   L=(I=1) *HxSMI+I
   LM1=(L-1) +MXCPM
   DU 31 M=1,6
   KELM1+EM(M)
31 B(K)=UCMPLX(1,000,0.00)
   IF (MFLEX.NE.O) GU TO 25
   IF (MLEL . ER . O) GH TH 26
   K=L+MXCSH=6
   SMLE(K) #DCMPLx(1.00,0.00)
26 IF (MFEA.ER.O) GO TO 23
   K=L+MXCSH=9
   KAEK+3
   SMLC(KA) #OCHPLX(PLC,0.00)
   SMLE(K) = DCMPLx(1.00,0.00)
23 IF (MFLAP.ED. 0) GI) TO 24
   KEL *MXC SB=2
   KABK-7
   SMLD(KA) #DCMPLX(PFC,0.U0)
   SMLU(K)=DCMPLx(1,000,0.00)
24 IF (MCT. EQ. 0) GO TO 30
```

K=L +MXCSH=A SMLB(K)=DCMPLx(1.00,0.00) G(1 T() 30 25 IF (MCUN\_EU. 0) GO TO 30 K=L+MXCSB=10 SMLH(K)=OCMPLX(CX(1),0,00) SMLC(K)=DCMPLx(CX(2),0.U0) SMLU(K)=DCMPLx(=Cx(3),0.D0) SMLE(K)=DCMPLX(=CX(22),0.00) SMLF(K)=DCMPLx(=Cx(25),0,00) SHLG(K)=UCMPLx(-Cx(2A).0.U0) SMEH(K)=DCMPLx(CX(4),0.00) Shic(K)=0CMPL $\times$ (C $\times$ (9),0.00) SHLD(K) #DCMPLx( #CX(13), 0, DO) SMLE(K)=DCMPLx(=Cx(31),0.00) SMLF(K)=DCMPLx(=CX(34),0.00) SMLG(K)=00MPLx(=0x(37),0,00) SHLB(K)=DCMPLx(Cx(h),0.00) SMLC(K)=UCMPLx(CX(111,0,00) SML()(K)=00MPLx(=0x(15),0.00) SMLE (K)=00MPL x (=0x(33),0.00) SMLF (K) #DCMPLx(-Cx(36),0,0) SML6(K)=0CMPLx(=CX(39),0,00) SMLB(K)=DCMPLx(=CX(2),0,00) SMLC(K)=0cMPLx(=CX(7),0,00) SMLU(K)=DCMPLx(CX(A),0.00) SHLE(K)=DCMPLx(CX(23),D.DU) SHLF (K)=DCMPLx(Cx(26),0,D0) SMLG(K)=DCMPLx(Cx(29),0,00) K=K+3 SML U(K) =DCMPL x(CX(5), U, DO) SMLC(K)=DCMPLx(Cx(10),0.D0) SMLU(K)=DCMPLx(-CX(14),0.00) SMLE(K)=FCMPLY(=FX(32),0.00) SMLF(K)=DCMPLx(=Fx(35),0,00) SMLG(K)=DCMPLx(=CX(3A),0,00) SMLB(K)=DCMPLx(Cx(3),0,00) SMLC(K)=DCMPLx(CX(H),0.00) Shin(K)=004Ptx(=0x(12),0,00) SHLE(K)=DCMPLX(=CX(24),0,00) SMLF(K)=DCMPLx(=CX(27),U.DO) SHLG(K)=DCHPLx(-Cx(3n),0,00) SO CUNTINUE IF (mine at a) an in 42 DO 40 THI MAKAB FSb(I) =UCMPLX(0,DU,U,U0)



```
FAB(1) #DCMPLX(0.DU,0.00)
   FLB(I)=0CMPLX(0.D0.0.D0)
40 CTH(I)=0CMPLX(0.00,0.00)
   DU 41 Tal, MFASH
   FSH1(I)=0CMPLx(0,00,0,00)
   FSH2(I)=OCMPLx(0.00,0.00)
   FSB3(1)=DCMPLx(0,00,0.00)
   FAH4(I)=DCMPLx(0.U0,0.D0)
   FLB4(1)=0CMPLx(0,00,0.00)
   CTH4(I)=DCMPLX(0,00,0.00)
   FAH1(I)=0C4PLY(0.00,0.00)
   FABS(1)=DCMPLx(0.00,0.00)
   CTH2(I) #DCMPLx(0.D0,0.D0)
   CTH3(I)=DCMPLx(0.U0,0.D0)
   PLH1(1)=DCMPLx(0.00,0.00)
41 FLH2(I)=DCMPLx(0.00,0.00)
42 DO 501 IS=1, MASEC
   ISMI=(IS=1)+HSY
   DI 50 L=1, NSY
   M=ISMI+L
50 Y(L)=50(4)
   IF (Y(5) . EQ. 0. ) GH TH AO
   CALL RIGID
   LG0=1
60 UU 79 JE1, MXSMI
   00 79 J=1, MXSMI
   L=(J=1) + "XSMI+I
   LM1=(L-1) +MXCPM
   LHM1=(L=1) *MXCSH
   DO 66 M#1, MXCPM
   KELM1+M
66 T(M) #B(K)
   CALL MLRC2 (RHEAL, T. NCULS)
   DO 70 ME1, MXCPM
   KELM1+M
70 8(K)=T(M)
   IF (NCACF.EQ.1) GO TO 83
   DU 81 ME1, MXCSB
   KELBM1+M
H1 T(M)=SMLF(K)
   CALL MLRC2 (RREAL, T, NCSH)
   DU 82 ME1. MXCSB
   KELBM1+M
82 SMLF(K)=T(M)
88 IF (NCACG.EQ.1) GO TO 88
   DO 84 ME1, MXCSB
   KELUM1+M
64 T(M) #SMLG(K)
   CALL MLHC2(RREAL, T, NCSB)
   DO 85 Mal, MXCSR
```

```
K=LHH1+M
   65 SMLG(K)=T(M)
   BB IF (NCLFL.ED.1) GO TO MY
       OU HE ME1, MXCSH
      Kal. HM1+M
   66 T(M)=SMLE(K)
       CALL NURCE (RREAL, T. NCS4)
       DU 87 4=1, MxCSR
      KELHM1+M
   87 SMLE (K)=T(")
   h9 IF (NCFFA, EQ. 1) GH TH 78
C
      DU 72 N=1, MXCSH
      K#L 0111+11
   12 T(M)=SMLC(K)
       CALL MLRC2 (RREAL, T, MCSH)
      DU 76 ME1, MXCSH
      K=LoM1+M
   76 SMLC(K)=1(M)
   7H IF (NCFLP.EN.1)GH TO 75
C
      DO 722 HaliMXCSH
      K=LHM1+M
  722 T(M)=SMLD(K)
       CALL MLRC2 (RRFAL, T. 1086)
       DIJ 762 M#1, MXCSR
       KEL dM1+M
  762 SMLD (K)=T(M)
   73 IF (NCCT_EQ.1)60 TO 79
C
       DII 723 ME1, MXCSH
       KaleM1+M
  723 T(M) = SHLH(K)
       CALL MLRC2 (RREAL, T, NCSH)
       DU 763 ME1, MXCSH
       KELHM1+M
  763 SMLb(K)aT(M)
   79 CONTINUE
       IF (LGU.E0.2) GO TU 100
       IF (LGU. EQ. 3) GO TO 120
   80 IF(Y(2),EQ.0.)GO TO 100
       CALL BEHD
       LG()=2
       GO TO 60
  100 IF (Y(4), Eq. 0.) Git TO 120
       CALL ELAST
       L60=5
       GO TO 60
  120 DU 200 I=1, MX9MI
       KSML=I-NFP1
```

## DEST AVAILABLE COPY

```
NSTEKSML
    CS1=CMS=CM1+NST+OM1
    CS2=CS1 *CS1
    IF (Y(6), EQ. 0.) GO TO 145
    CALL STIFF
    LGU=1
127 DU 404 J=1, MXSMI
    L=(J=1) * M X S M I + I
    LM1=(L=1) +MXCPM
    LHM1=(L-1) *MX(Sh
    DO 136 ME1, MXCPM
    K#LM1+M
136 T(M)=8(K)
    CALL MLCC2(R,T,NCULS)
    DU 137 MEL, MXCPM
    K=LM1+M
137 B(K)=T(M)
    IF (NCACF . F.Q. 1) GO TU 153
    DO 151 M=1.MXCSH
    K=L0/11+11
151 T(M)=5MLF(K)
    CALL MLCC2(R.T.NCSH)
    DO 152 M#1, MXCSH
    K=1.641+M
152 SMLF (K) = T (M)
153 IF (NCACG. EQ. 1) GO TO 156
    DU 154 MB1. MXCSH
    K=Lnd1+M
154 T(M)=SMLG(K)
    CALL MLCC2 (R.T.NCSH)
    DU 155 ME1, MXCSH
    K=LHM1+M
155 SALG(K)=T(M)
156 IF (NCLEL.ER.1) GO TO 135
    DO 131 M=1. MXCSH
    K=LMM1+M
131 T(M)=SMLE(K)
    CALL MUCCZ(H, T, NCSA)
    DU 132 M=1, MXC8H
    K=LHM1+M
132 SMLE(K)=T(M)
135 IF (NCFFA.EQ.1) GD TU 142
    DU 139 ME1, MXCSH
    K=LHM1+M
139 T(M)=SMLC(K)
    CALL MLCC2 (H, T, NCSH)
    DO 140 MEL.MXCSH
    KELHY1+M
140 SMLC(K)=T(M)
```

C

```
C
  142 IF (NCFLP.ER.1) GO TU 405
C
      DO 402 M=1, MXCSH
      KELBM1+M
  402 T(M)=SMLN(K)
      CALL MLCC2(R, T, NCSH)
      DU 403 ME1, HXCSH
      KELHM1+M
  403 SMLD(K)=T(M)
  405 IF (NCCT. EQ. 1) GU TO 404
C
      DU 407 ME1. MXCSH
      K=LHM1+M
  407 T(M)=SMLH(K)
      CALL MLCC2(R,T,NCSH)
      D(1 408 ME1, MXCSH
      KELDM1+M
  408 SHLH(K)=T(M)
  404 CUNTIMIL
      1 (LGH.GT.1) GH TU 200
  145 IF (Y(1).FN.O.)GO TO 200
      NHARMED
      CALL BMASS
      L611=2
      GU TH 127
  200 CONTINUE
      IF (MAER. FO. 0) GO TU 305
      IF (Y(3), FQ. U.) GO TO 305
      IL=IL+1
      IF ( -CACF . EQ. 1) GO TO 158
      DII 157 KEL PXSMH
      SALFSV(x)=SMLF(x)
  157 SMLF (K)=DCMPLX(0.00,0.00)
  15A IF (NCACG.EQ.1) GO TO 160
      UII 159 KE1, MXSMH
      SHLUSV(K)=SMLG(K)
  159 SMLG(K)=0CMPLx(U.00,0.00)
  160 IF (NCLFL.EQ.1) GO TO 2140
      DU 218 K#1, MXSMH
      SMLESV(K)=SMLF(K)
  214 SMLF (K)=DCMPLx(0.U0.0.D0)
 2140 IF (NCFFA.EQ.1) GO TO 2141
      DU 214 KM1. NXSMA
       SMLCSV(K)=SMLC(K)
  214 SMLC(N)=DCMPLx(0.00,0.00)
 2141 IF ("CFLP.EW.1)GO TO 2145
      UI 212 A=1, MX5MH
      SMLUSV(K)=SMLD(K)
  215 SWFF(K)=UCABFX(0.00'0'0'0')
```

## SIST AVAILABLE COPY

2143 IF (NCCT.EU.1)GU TU 2142 DU 216 KE1, MXSMH SMLBSV(K)=SMLH(K) 216 SMLh(K)=DCMPLx(0,00,0,00) 2142 DU 215 K=1, MXCPK HSAVE (K)=H(K) 215 H(K)=DCMPLX(0,D0,0,D0) NTIMS=MxSMI+1 DI) 300 NG=1,NFP1 NHARMEND-1 NTIMS=NTIMS=1 NSHF TENUENFP1-1 NHACK#1 217 CALL HLARD(C.D.IL) DO 250 JUST NTIMS NSHFT=NSHFT+1 NST=NSHFT IU=JU+NU=NRACK I=JU+NHACK=1 CS1=CMS+CM1+(IM1+NSHFT DU 220 M=1.144 220 R(M)=CS1+C(M)+D(M) DU 250 J=1, MXSMI L=(J=1) +MXSMI+I LU=(J=1) \*MXSMI+IQ LUM1=(LU=1)+MXCPM LM1=(L=1)+MXCPM LBQ=(LQ=1) \*MXCSB LB = (L=1) \*MXCSH DO 240 ME1, MXCPM K=LUM1+M 240 T(M)=BSAVE(K) CALL MLCC2(R,T,NCULS) DU 245 MHI, MXCPM KELM1+M 245 B(K) #T(M)+B(K) IF (NCACF.EQ.1) GO TO 163 DU 161 MMI, MXCSH KELBQ+M 161 T(M)=SMLFSV(K) CALL MLCC2(R,T,NCSB) DO 162 ME1, MXCSH KELH+M 162 SMLF(K)=T(M)+SMLF(K) 163 IF (NCACG.EQ.1) GO TO 166 DO 164 ME1, MXCSH K=LHQ+M 164 T(M)=SMLGSV(K) CALL MLCC2(R,T,NCSH)

DU 165 ME1. MXCSB

```
K=L+M
  165 SMLG(K)=1(M)+SMLG(K)
  166 IF (NCLEL . EQ. 1) GO TO 244
      DU 241 N=1, MXCSH
      KELHU+M
  241 T(M)=SMLESV(K)
      CALL MICCE (R.T. NCSH)
      DO 242 MMI.MXCSB
      KELH+M
  242 SHLE(K)=T(M)+SHLE(K)
  244 IF (NCFEA.EG.1) GO 10 249
Ç
¢
      DU 247 HE1. MXCSH
      KELHU+M
  247 T(M)#SMLCSV(K)
      CALL MLCC2(F,T,NCSP)
      DU 248 Mm1, MXCSH
      KEL H+M
  248 SMLC(K) = T(M) + SMLC(K)
  249 IF (NCFLP.ER.1)GO TO 251
C
C
      DII 595 WHI WXC8R
      KELHU+M
  262 T(M)=SMLDSV(K)
      CALL MLCC2(R,T,NCSH)
      DO 263 ME1. MXCSH
      K=LH+M
  263 SMLD(K)=T(M)+SMLD(K)
  251 IF (NCCT.ER.1)GU TU 250
C
C
      DO 272 M=1, MXCSB
      K=LBQ+M
  272 T(M)=SMLASV(K)
      CALL MLCC2(R,T,NCSH)
      DO 273 M=1, MXCSB
      KELB+M
  273 SMLH(K)=T(M)+SMLH(K)
  250 CUNTINUE
      IF(NO.LE.1) GO TO 300
      TF(NBACK.EQ.2) GO TO 300
      NHARMSONHARM
      NBACK=2
      NSHFT==NFP1
      GO TO 217
  300 CUNTINUE
  305 CONTINUE
      IF (MODE, EQ. 1) GO TU 350
```

```
IF (MFLEX.EQ.O)GO TO 481
    IF (MCUN.EQ. 0)GO TU 501
    IF (IS. NE. NCON) GO TO 500
    NCFEA=2
    NCFLP=2
    NCCT=2
    IF(MCTY.GT.O) GO TO 170
    DII 482 I=1, MXFAH
    K1=(I-1)+12+1
    K3=K1+2
    K5=K3+2
    K63K5+1
    K9=K6+3
    K0=K9+1
    CTR(I) = GX(1) *H(K1) + CX(2) *H(K5) = CX(3) *H(K9)
   1+CX(4)*H(K3)+CX(5)*b(K0)+CX(6)*b(K6)
    FAB(I)=CX(2)*H(K1)+CX(7)*H(K5)=CX(8)*H(K9)
   1+CX(9)*H(K3)+CX(10)*R(K0)+CX(11)*H(K6)
    FLH(1) #CX(3) #F(K1) +CX(8) #H(K5) -CX(12) #B(K9)
   1+CX(13)+B(K3)+CX(14)+B(K0)+CX(15)+B(K6)
482 CUNTINUE
    GU TU 501
170 NCLEL=2
    NCACFEZ
    NCACG=2
    DU 172 I=1. MXFAB
    K1=(1=1)+12+1
    K3=K1+2
    K5#K3+2
    K6=K5+1
    K9EK6+3
    KU=K9+1
    CTB(1)=CX(40)+B(K1)+CX(43)+B(K5)=CX(46)+B(K9)
   1+CX(49)*H(K3)+CX(52)*H(K0)+CX(55)*H(K6)
    FAB([) = CX(41) + H(K1) + CX(44) + H(K5) = CX(47) + H(K9)
   1+CX(50)*H(K3)+Cx(53)*B(K0)+CX(56)*B(Kb)
    FLB(1)=Cx(3)+H(K1)+Cx(B)+H(K5)=Cx(12)+B(K9)
   1+CX(13)+H(K3)+CX(14)+H(K0)+CX(15)+H(K6)
    FSH(I)=CX(42)+B(K1)+CX(45)+H(K5)=CX(48)+B(K9)
   1+CX(51)+H(K5)+CX(54)+H(K0)+CX(57)+B(K6)
172 CUNTINUE
    GO TO 501
481 IF(IS.NF.NLEL) GO TO 483
    NCLFF=5
    DO 314 1=1. MXFAH
    K=(1=1)+12+7
314 FSB(I)=B(K)
    IF(IS.LE.NFEA) GO TO 316
    DU 315 I#1, MFASH
    K=(1=1)+12+7
```

```
315 F582(I) = SMLC(K)
  316 IF(IS.LE.NCT) GO TO 318
      DU 317 I=1, MFASH
      K=(1-1) +12+7
  317 FSB1(I)=SMLH(K)
  318 IF (IS.LE.NFLAP) GU TO 483
      UU 319 I=1, MFASB
      K=(I=1)+12+7
  319 F583(I) = SMLD(K)
¢
  443 IF(IS.NE.NFEA) GO TO 326
      NCFEASS
      DU 320 I=1. MXFAH
      K=(I=1)+12+4
      KAEK+3
  320 FAH(I)#H(K)+H(KA)*PLC
      IF(IS.LE.NLEL) GO TO 303
      DO 302 I=1, MFASH
      K=(I=1)+12+4
      KABK+5
  302 FAB4(I) #SMLE(K)+SMLE(KA) *PEC
C
  303 IF (18.LT. NCT) GO TO 312
      DII 324 I=1, MFASH
      M=(I=1)+12+4
      KASK+3
  324 FAB1(I)=SHLH(K)+SMLH(KA)+PLC
C
  312 IF (IS.LE.NFLAP) GO TO 326
      DU 327 1=1, MFASB
      K=(I=1)+12+4
      KABK+3
  327 FAHS(I)=SMLD(K)+SMLD(KA)+PLC
C
C
  326 IF(18, NE, NCT) GI TU 330
      VCC1=5
      DI) 329 IS1. MXFAH
      K=(I=1)+12+3
  329 CTB(1)=b(K)
      DII 349 1=1. MFASH
      K=(I=1)+12+4
  349 CTH1(I)=SMLH(K)
      IF (15.LE.NLEL) GO TO 306
      UI 304 I=1, MFASH
      K=(I=1)+12+3
  3U4 CTH4(1)=SMLE(K)
  306 IF (IS.LE.NFEA) GO TU 331
      DO 353 I=1. HFASH
```

```
K#(1=1)+12+3
  333 CTH2(I)=SMLC(K)
C
  331 IF(18.LT.NFLAP) GU TO 330
      DI) 337 I=1, MFASH
      K = (1 - 1) + 12 + 3
  337 CTH3(I)=8MLD(K)
C
C
  330 IF (IS.NE.NFLAP) GU TO 500
      NCFLP=2
      DU 336 IR1, MXFAR
      K=(I=1) *12+11
      KARK-7
  356 FLB(I)#H(K)+H(KA)*PFC
      IF(IS.LE.NLEL) GO TO 308
      DO 307 I=1, MFASH
      K=(I=1)*12+11
      KARKA-7
  307 FLB4(I) #SMLE(K)+SMLE(KA)+PFC
C
  308 IF (18.LE.NFEA) GO TU 345
      DU 344 Im1, MFASH
      K#(I=1) +12+11
      KASK-7
  344 FLB2(I) #SMLC(K)+SMLC(KA)+PFC
C
  345 IF(IS.LT.NCT) G() TU 500
      DU 347 I=1, MFASB
      K=(I=1)+12+11
      KASK-7
  347 FLB1(I)=SMLB(K)+SMLB(KA)*PFC
      GU TO 501
C
C
C
  350 IF(MFLEX.EQ.O) GO TU 484
      IF(MCUN.ER.O) GO TO 487
      IF (IS.NE.NCON) GO TU 487
      NCFEA=2
      NCFLP=2
      NCCT=2
      MCT=1
      MFEA=1
      MFLAP#1
      MLEL=0
      18=1
      IC=1
      ID=1
      IF(MCTY.EQ.O) GO TO 487
```

```
MLEL=1
      MCACF=1
      MCACG=1
      It=1
      IFF=1
      IGG=1
      NCLEL=2
      NCACF=?
      NCAUG=2
      GU TU 487
  484 IF (IS. NE. NCT) GO TH 485
      NCCT=2
      In=1
  485 IF (IS.NE.NFEA) GO TO 486
      NCFL4=2
      IC=1
  406 IF (IS. NE. NFLAP) GO TO 488
      NOFLPEZ
      1021
  488 IF (IS. ME. NLEL) GO TO 487
      NCLELAZ
      IL=1
C
C
  487 CUNTINUE
      J2=HXCSH
      J3=MXCPM
      DU 502 MS=1,NH
      JIENFUS+(MS-1) +NRHD+MXT2P1
      DU 502 Imi, MXSMI
      DU 351 IR=1,12
  351 SHAPE(IR) =DCMPLX(0.00,0.00)
      DU 356 J=1, MX8MI
      JM1=J-1
      IMISI-1
      IJ1=JM1+NERC+J3+IM1
      IJ2=JM1+NESHC+J2+IM1
      IK1=JM1+NRIFC+J1
      DO 356 IR=1,12
      K=IJ1+IR
      L=IJ2+IR
      HLL=DCMPLX(0.D0,0.D0)
      DU 371 IT=1,6
      IN8=K+12+(IT=1)
      INL=IK1+IT
      BLL=BLL+H(INB) +ALM(INL)
  371 BLL=BLL+H(INB) *EPS(INL)
      INSCEL
      IF(IGG.EQ.0) GO TU 174
```

```
INLEIK1+NRBD
    BMLGL#BMLG(INSC) + ALM(INL)
    SMLGL=8MLGL+8MLG(INSC)+EPS(INL)
174 IF(IFF, EQ. 0) GO TO 176
    INL=IK1+NRBD=MCACG
    SMLFL=SMLF(INSC)+ALM(INL)
    SMLFL=SMLFL+SMLF(INSC) *EP8(INL)
176 IF(IE.EQ.O) GO TO 380
    INLHIK1+NRBD-MCACG-MCACF
    SMLEL=SMLE(INSC)+ALM(INL)
    SMLEL#8MLEL+8MLE(INSC) *EPS(INL)
380 IF(IB.EQ.0) GO TO 381
    INL=IK1+NRBD-MFEA-MFLAP-MLEL-MCACG-MCACF
    SMLBLESMLB(INSC) + ALM(INL)
    SHLBL#SMLBL+SMLB(INSC) *EP8(INL)
381 IF(IC.EQ.0)GO TO 382
    INLEIK1+NRBD=MFLAP=MLEL=MCACG=MCACF
    SMLCL#8MLC(INSC) + ALM(INL)
    SMLCL#SMLCL+8MLC(INSC)*EPS(INL)
382 IF(ID.EQ.0)GO TO 383
    INLEIK1+NRBD-MLEL-MCACG-MCACF
    SMLDL#SMLD(INSC) +ALM(INL)
    SMLDL#SMLDL+SMLD(INSC)#EP8(INL)
383 SHAPE(IR)#SHAPE(IR)+BLL=IB+SMLBL=IC+SMLCL=ID+SMLDL=IE+SMLEL
   1-IFF*SMLFL-IGG*SMLGL
356 CONTINUE
    UBX(M8, I8, I) = SHAPE(1)
    UBY(MS, IS, I)=SHAPE(5)
    UBZ(MS, IS, I) == SHAPE(9)
    PHIX(MS, IS, I) = SHAPE(3)
    PHIY(MS, IS, I) = SHAPE(10)
    PHIZ(MS, IS, I) = SHAPE(6)
    AN(MS, IS, I) #8HAPE(2)
     VY(MS, IS, I) == SHAPE(B)
     VZ(M8, I3, I) #8HAPE(12)
     TEA(MS, IS, I) = SHAPE(4)
     AMY(M8, IS, I) BHAPE(11)
     AMZ(MS, IS, I) #8HAPE(7)
502 CONTINUE
500 CONTINUE
501 CONTINUE
     IF (IWRITE, EG. 0) GU TO 971
     IF(N8P.EQ.0) GO TO 1051
     WRITE(6,1052)
     DU 1053 IXX#1,MX8MI
     IXM2#IXX=NHC=1
     SMXI-ESMXI
     WRITE(6,1055) IXM2
     DO 1053 IYY#1,MXT2P1
```

```
INLH(IXX-1) +NRIFC+IYY
       IEPHIYY-MAXN-1
       WSHREPS(INL)+ALM(INL)
       WRITE(6,1054) IEP, WSW
 1053 CONTINUE
 1051 CONTINUE
 1052 FORMAT(/55X, 'SWASHPLATE DEFLECTIONS!/)
 1054 FORMAT(/55X, 'w(1, 12, 1) = 1, 2E12.5)
 1055 FORMAT(//55x,12, PER REV. 1)
       DU 7000 IXU1, MXSMI
       DU 7000 MS#1.NB
       IXM2#IX=NHC-1
       IXM2==IXM2
       WRITE(6,1001) MS, IXM2
       WRITE (6,966)
       IJ=1
  968 DO 601 J=1,NBSEC
       IF(J.EQ.1) SPACE=BTIPS
       IF(J.EQ.NBSEC) SPACERBHUR
       WRITE(6,901) SPACE, J. UBX (MS, J. IX), UBY (MS, J. IX), UBZ (MS, J. IX)
       IF(IJ.NE.2) GO TO 390
       IF(IPU.EQ.1)WRITE(7,1111)J,UBX(M8,J,IX),UBY(M8,J,IX),UBZ(M8,J,IX)
  390 CUNTINUE
      SPACESBLANKS
      IF(IJ.EQ.3) GO TO 601
      QXJ=UBX(MS,J,IX)
      QYJ=UBY(MS,J,IX)
      QZJ=UBZ(MS,J,IX)
      IF(IJ.EQ.2) GD TO 603
      ISM1=(J-1)+N8Y
      DO 602 KB15,30
  602 Y(K)=SD(ISM1+K)
C
C
C
      (92) Y*[ZQ+(42) Y*[YQ+(91) Y*[XQm(XI, L, 2M) XBU
      UBY(MS,J,[X)=QXJ+Y(25)+QYJ+Y(25)+QZJ+Y(27)
      UHZ(MS,J,IX)=QXJ+(-Y(15))+QYJ+Y(20)+QZJ+Y(21)
      GD TU 601
  603 CALL POLAR
      LXD=(XI, L, SM)XBU
      UBY(MS,J,IX) =QYJ
      UBZ(M8,J,IX)=QZJ
  601 CONTINUE
      IF(IJ.GT.1) GO TO 604
      WRITE(6,950)
      GU TU 961
  604 WRITE (6,963)
  961 DU 951 Je1, NBSEC
      IF (J.EQ. 1) SPACE BTIPS
```

```
IF (J.EQ.NBSEC) SPACEBBHUB
      WRITE(6,901)SPACE, J, PHIX(MS, J, IX), PHIY(MS, J, IX), PHIZ(MS, J, IX)
      IF (IJ.NE.2) GO TO 391
      IF(IPU,EQ.1)WRITE(7,1111)J,PHIX(MS,J,IX),PHIY(MS,J,IX),PHIZ(MS,J,I
     1X)
  391 CONTINUE
      SPACE=BLANKS
      IF(IJ.EQ.3) GO TO 951
      QXJ=PHIX(MS,J,IX)
      GYJ=PHIY(MS,J,IX)
      QZJ=PHIZ(MS,J,IX)
      IF(IJ.EQ.2) GD TO 810
      ISM1=(J-1) +NSY
      DU 800 K=15.30
  800 Y(K)=SD(ISM1+K)
C
      PHIX(M8,J,IX)=QXJ+Y(19:+QYJ+Y(24)+QZJ+Y(26)
      PHIY(MS, J, IX)=QXJ*Y(23)+QYJ*Y(25)+QZJ*Y(27)
      PHIZ(MS,J,IX)=QXJ*(=Y(15))+QYJ*Y(20)+QZJ*Y(21)
      GU TU 951
  810 CALL POLAR
      PHIX(MS, J, IX) = QXJ
      PHIY(MS,J,IX)=QYJ
      PHIZ(MS,J,IX)=QZJ
  951 CUNTINUE
      IF(IJ.GT.1) GO TO 958
      WRITE(6,955)
      GU TO 956
  958 WRITE(6,964)
  956 DU 957 J#1,NBSEC
       IF (J.EQ.1) SPACE #BTIPS
      IF (J.EQ.NBSEC) SPACE BHUB
       WHITE(6,901)SPACE, J, AN(MS, J, IX), VY(MS, J, IX), VZ(MS, J, IX)
       IF (IJ.NE.2) GO TO 392
       IF(IPU.EU.1) WRITE(7,1111)J, AN(MS,J,IX), VY(MS,J,IX), VZ(MS,J.IX)
  392 CUNTINUE
       SPACEBBLANKS
       IF(IJ.EU.3) GO TO 957
       (XI, L, SM) MAELXD
      CXI, L, EM) YV=LYD
      QZJ=VZ(MS,J,IX)
       IF(IJ.EQ.2) GO TO 820
       ISM1=(J-1)+NSY
      DU 801 K=15,30
  801 Y(K)=SD(ISM1+K)
C
C
C
```

```
(AS) Y*LZD+(45) Y*LYD+(91) Y*LXD= (XI, L, 8M) NA
                  =QXJ*Y(23)+QYJ*Y(25)+QZJ*Y(27)
     VY(MS,J,IX)
                  #QXJ*(-Y(15))+QYJ*Y(20)+QZJ*Y(21)
     VZ(MS,J,IX)
    GU TO 957
820 CALL PULAR
     AN(MS,J,IX) = GXJ
     LYD=(XI,L,SM)YV
     VZ(MS,J,IX)=QZJ
957 CUNTINUE
     IF(IJ.GT.1) GU TO 970
     WHITE (6,959)
    GU TU 969
970 WRITE(6,965)
969 DU 960 J=1,NBSEC
     IF (J.EQ. 1) SPACE BTIPS
     IF (J.EQ.NBSEC) SPACE=BHUB
     WRITE(6,901)SPACE, J, TEA(MS, J, IX), AMY(MS, J, IX), AMZ(MS, J, IX)
     IF(IJ.NE.2) GO TO 393
     IF (IPU, EQ. 1) WRITE (7, 1111) J, TEA (MS, J, IX), AMY (MS, J, IX), AMZ (MS, J, IX)
393 CONTINUE
     SPACEBBLANKS
     IF(IJ.EQ.3) GO TO 960
     QXJ=TEA(MS,J,IX)
    QZJ=AMZ(MS,J,IX)
     CXI. (. SH) YMAELYD
     IF(IJ.EQ.2) GO TO 840
     ISMI=(J=1)+NSY
     DU 802 K#15,30
BOZ Y(K)=SD(ISM1+K)
     TEA(MS,J,IX) =QXJ+Y(19)+QYJ+Y(24)+QZJ+Y(26)
     AMY(M8,J,IX) #QXJ*Y(23)+QYJ*Y(25)+QZJ*Y(27)
     AMZ(MS,J,IX) =QXJ*(-Y(15))+QYJ*Y(20)+QZJ*Y(21)
     GD TD 960
840 CALL POLAR
     TEA(MS,J,IX)=QXJ
     LYG=(XI, L, EM)YMA
     AMZ(M8,J,IX)=QZJ
960 CUNTINUE
     IJ#IJ+1
9001 IF(NPD.EQ.0)GD TO 7000
     IF(IJ.GT.3) GO TO 7000
     IF(IJ.EQ.3) GO TO 850
     WRITE(6,1002)
     GO TO 830
850 WRITE(6,983)
830 WRITE(6,962)
     GD TO 968
```

1

CC

```
0000000000
 7000 CUNTINUE
       IENHC+1
       IF(NPD.GT.O) GO TU 516
       UBYM#CABS(UBY(1,1,1))
       UBZM=CABS(UBZ(1,1,1))
       PHIXMUCABS(PHIX(1,1,1))
       DO 511 IS=2, NBSEC
       UBYT#CABS(UBY(1, IS, I))
       UBZT=CABS(UBZ(1,18,1))
       PHIXT#CABS(PHIX(1, IS, I))
       UBYMBAMAX1 (UBYM, UBYT)
       UBZMWAMAX1(UBZM, UBZT)
  511 PHIXMWAMAX1(PHIXM, PHIXT)
       GO TO 520
  516 UBYM=UBY(1,1,1)
       UBZM#UBZ(1,1,1)
       PHIXMAPHIX(1,1,1)
       DO 512 13#2, NBSEC
       UBYTHUBY(1, IS, I)
       UBZT#UBZ(1,18,1)
       PHIXTOPHIX(1,18,1)
       UBYMAAHAX1 (UBYM, UBYT)
       UBZMWAMAX1 (UBZM, UBZT)
  512 PHIXMBAHAX1(PHIXM, PHIXT)
  520 PHIXMOPHIXM+5.73
       IF(UBYM.GT.UBZM) GO TU 524
       NBGMD=2
       IF(PHIXM.GT.UBZM) NBGMD#3
       GO TO 971
  524 NBGMD#1
       IF (PHIXM.GT. UBYM) NBGMD#3
  971 NCTHICT
       NFEARIFEA
       NFLAPRIFLA
       NLELHILEL
       RETURN
  901 FORMAT(3x, 44, 3x, 12, 3(9x, 2(1PE12.4)))
950 FORMAT(//, 78, 'SECTION', 728, 'PHI x, TWIST', 757, 'PHI y, FLAPWISE SLO
      1PE', T89, 'PHI Z, CHORDWISE SLOPE', /, T28, '(+, NOSE UP)', T60, '(+, FLA
      2P DOWN) 1, 793, 1 (+, BLADE LEAD) 1, //)
```

```
955 FORMATE
                   //, TB, 'SECTION', T27, 'N, AXIAL FORCE', T56, 'V Y, CHORDWI
    18E SHEAR', TOI, 'V Z, FLAPHISE SHEAR', /, T24, '(+, RADIAL OUTBOARD)', T
    259, 1(+, TOWARD L.E.) 1, 795, 1(+, UPWARD) 1,//)
959 FURMAT(//, T8, 'SECTION', T30, 'T, TORQUE', T57, 'M Y, FLAPHISE MOMENT',
    1790, 'M Z, CHORDWISE MOMENT', /, T28, '(+, NOSE UP)', T55, '(+, TENSION
    2UPPER FIBERS);, T90, (+, TENSION T.E.) 1,//)
1002 FORMAT(1H1,//,T49, DISK PLANE AXIS SYSTEM!,//)
962 FURMAT(TB, 'SECTION', T25, 'UBX, RADIAL DEFL.',
1 T58, 'UBY, INPLANE DEFL.', T92, 'UBZ, VERT. DEFL.',
    2,T28,'(+, DUTBOARD)',T58,'(+, RUTATION DIR.)',T95,'(+, UPWARD)',//
    3)
964 FURMATE
                   //, T8, 'SECTION', T26, 'NB, RADIAL FORCE', T58, 'VBY, INPLA
    INE SHEAR', 192, 'VBZ, VERT. SHEAR', /, 128, '(+, OUTBOARD)', 159, '(+, DI
                                        1.//)
    2R. UF ROT.)1,194,1(+, UPWARD)
965 FORMAT(//, T8, 'SECTION', T29, 'T8, TORQUE', T57, 'MBY, VERTICAL MOMENT'
    1, T91, 'MBZ, INPLANE MOMENT', /, T28, '(+, NUSE UP)', T55, '(+, TENSION U
    2PPER FIBERS)', T92, '(+, TENSION T.E.)',//)
966 FORMAT (T8, 'SECTION', T25, 'UX, RADIAL DEFL.', T58, 'UY, INPLANE DEFL.'
    1, 192, 'UZ, VERT. DEFL.', /, T28, '(+, OUTBOARD)', T58,
    2'(+, ROTATION DIR.)', T95, '(+, UPWARD)',//)
963 FORMAT(//, T8, 'SECTION', T28, 'PHIBY, TWIST', T54, 'PHIBY, VERT. BENDIN
    IG SLOPE', T87, 'PHIBZ, INPLANE BEND. SLOPE', /, T26, '(+, L.E. UPWARD)' 2, T59, '(+, TIP DOWNWARD)', T90, '(+, TIP DIR. OF ROT.)', //)
983 FORMAT (1H1, //, T39, 'DISK PLANE AXIS SYSTEM - POLAR COORDINATES! . / .
    1747, AMPLITUDE AND PHASE ANGLE 1,//)
1001 FURMATC
                 //, T45, 'BLADE', 12, 14, ' PER REV SHAPE VECTOR (LOCAL AXIS
    1848.) (,//)
1111 FURMAT(15.3(1x,2(1PE12.4)))
     END
```

```
SUBROUTINE SARRAY
   INTEGER EM(6), EE(6)
   REAL+8 RREAL(144)
   COMPLEX UBX(25,3), UBY(25,3), UBZ(25,3), PHIX(25,3), PHIY(25,3),
  1PHIZ(25,3),AN(25,3),VY(25,3),VZ(25,3),TEA(25,3),AMY(25,3),AMZ(28,3
  LZD, LYD, LXO, (S
   COMPLEX+16 CMS,CM1,CS1,CS2
   CUMPLEX+16 EPS(63), ALM(63), 8(216), R(144), T(72), QBAR(12), SLL
   DIMENSION Y(100), 8D(4000)
   COMMON/CALM/ALM
   COMMON/EPSA/EPS
   COMMON/381/8
   COMMON/ARR/RREAL
   CUMMON/ARI/R
   COMMON/ROTF/OM1,OM2,OMT
   CUMMON/FREF/CMS,CM1,CS1,CS2
   COMMON/SUB/Y
   COMMON/SAIN/SD
   COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
  1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
  2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
  31REM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
  4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXCSB, MXCPM, MXCPK, MXSMB,
  SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
  6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
   COMMON/NLEAD/MLEL, NLEL, MCTY
   COMMON/QVTEM/QXJ,QYJ,QZJ
   COMMON/IPCH/IPU
   DATA EM/2,16,31,44,59,72/
   DATA EE/1,15,29,42,57,70/
                     '/, STIPS/'TIP '/, BHUB/'HUB '/
   DATA BLANKS/
   IF (MFUS.EG. 0) GU TO 971
   MSCPK=MXCPM+MXSMI
   IWRITERO
   IF (MODE, EG. 1) INRITE=1
   IL=0
   SPACE=BLANKS
   DO 22 LE1, MSCPK
22 S(L)=DCMPLX(0.D0,0.D0)
   DO 30 Lm1, MX8MI
   LM1=(L-1)+MXCPM
   DD 30 Ma1,6
   KHLM1+EM(M)
   IF(NFFB.EQ.1) Kalmi+EE(M)
30 8(K) = UCMPLX(1.D0,0.D0)
   DO 500 ISE1, NESEC
   ISM1=(NHSEC+IS=1)+NSY
   DO 50 L=1.NSY
   M=ISM1+L
50 Y(L)=3D(M)
```

IF(Y(5), EQ. 0.) GO TO 80 CALL RIGID LGO=1 60 DU 75 I=1, MXSMI LM1=(I=1) +MXCPM DU 65 Mal, MXCPM KELM1+M 65 T(M)=S(K) CALL MLRC2(RREAL, T, NCOLS) DU 691 ME1, MXCPM KELM1+M 691 8(K) #T(M) 75 CONTINUE IF(LGU.EQ. 2) GO TU 100 IF(LGU.E0.3) GO TO 120 80 IF(Y(2), EQ. 0.) GO TO 100 CALL BEND L60=2 GU TU 60 100 IF(Y(4).EQ.O.) GO TO 120 CALL ELAST LGU = 3 GU TU 60 120 DU 200 I=1.MXSMI IM1=(I=1)+12 LM1=IM1+NC()LS KSML=I=NFP1 NSTEKSML CS1=CMS=CM1+NST+OM1 CS2#CS1\*CS1 IF (Y(6) . EQ. 0.) GO TO 148 CALL STIFF LGU=1 130 CUNTINUE DU 136 ME1, MXCPM KELM1+M 136 T(M)=S(K) CALL MLCC2(R,T,NCULS) DO 140 MM1, MXCPM KELM1+M 140 S(K)=T(M) IF (LGU.EQ. 2) GO TU 175 IF (LGU.ER.3) GO TU 200 148 IF(Y(1), Eq. 0.) GO TO 175 CALL PMASS LGU=2 GO TO 130 175 IF(Y(3),EQ.O.) GO TO 200 IL=IL+1 CALL FUARU(IL)

```
LGU=3
      GU TO 130
  200 CONTINUE
      IF (MUDE .ER. O) GU TH 500
      L1=MXCPM
      12=NRIFC
      J1=MXT2P1
      DO 499 I=1, MXSMI
      DG 250 L=1,12
      IM1=1-1
      KEL1 + IM1+L
      SLL=DCMPLX(U.DO,0.DO)
      00 252 17=1,6
      INB=K+12*([T=1)
      INL#J1+IZ#IM1+IT
      SLL=SLL+S(INB) +ALM(INL)
  252 SLL=SLL+S(INH) *EPS(INL)
  250 GHAR(L)#SLL
      UBX(IS, I) = OHAR(1)
      UHY(IS,I)=DHAR(5)
      UHZ(IS, I) ==UHAR(9)
      PHIX(IS, I) = (18AR(3)
      PHIY(IS, I) = QBAR(10)
      PHIZ(IS,1)=QBAR(6)
      AN(IS,I)=GBAR(2)
      VY(IS,I) == OHAR(A)
      VZ(IS,I)=QBAR(12)
      TEA(IS, I) = QBAR(4)
      AMY(IS,I)=QHAR(11)
      AMZ(IS, I) = QHAR(7)
C
 499 CUNTINUE
  500 CUNTINUE
C
      IF (IWRITE, EQ. 0) GO TO 971
      DU 7000 IXE1, MXSMI
      IXM2==IX+NHC+1
      WHITE (6,916) IXM2
      WRITE(6,917)
      IJ=1
  968 DD 503 J=1,NFSEC
       IF (J.ER.1) SPACE=BTIPS
       IF (J.EQ.NESEC) SPACE=HHUR
       WRITE(6,901) SPACE, J, UBX(J, IX), UBY(J, IX), UBZ(J, IX)
       IF (IPU.EQ.1) WRITE(7,1111) J. UBX(J.IX), UBY(J.IX), UBZ(J.IX)
      SPACEABLANKS
      IF (IJ.E0.3) GO TO 503
      (xI, t) xdu=txn
      (xI,L)YHU=LYD
      OZJEUBZ(J,IX)
```

```
IF(IJ.EQ.2) GO TO 702
      ISM1=(NBSEC+J-1)*N8Y
      DO 504 K=15,30
  504 Y(K) = 8D(ISM1+K)
C
CCC
      UBX(J,IX) = QXJ*Y(19)+QYJ*Y(24)+QZJ*Y(26)
      UBY(J, IX) #QXJ+Y(23)+QYJ+Y(25)+QZJ+Y(27)
      UBZ(J, IX) =QXJ+(=Y(15))+QYJ+Y(20)+QZJ+Y(21)
      GO TO 503
  702 CALL POLAR
      UBX(J,IX)=QXJ
      UBY(J,IX)=QYJ
      UBZ(J,IX)=QZJ
  503 CUNTINUE
      IF(IJ.GT.1) GO TO 703
      WRITE(6,950)
      GD TO 961
  703 WRITE(6,963)
  961 DU 951 J=1,NFSEC
      IF (J.EQ.1) SPACE=RTIPS
      IF (J.EQ.NFSEC) SPACEERHUB
      WRITE(6,901)8PACE, J, PHIX(J, IX), PHIY(J, IX), PHIZ(J, IX)
      IF(IPU.EQ.1)WRITE(7,1111)J,PHIX(J,IX),PHIY(J,IX),PHIZ(J,IX)
      SPACE=BLANKS
      IF(IJ.EQ.3) GO TO 951
      QXJaPHIX(J,IX)
      (XI, L) YIH9=LYD
      QZJ=PHIZ(J,IX)
      IF(IJ.E4.2) GO TO 704
      ISM1=(NBSEC+J=1)+NSY
      DU 800 K#15.30
  800 Y(K)=SD(ISM1+K)
C
      PHIX(J, IX) = QXJ + Y(19) + QYJ + Y(24) + QZJ + Y(26)
      PHIY(J, IX) = QXJ+Y(23) + QYJ+Y(25) + QZJ+Y(27)
      PHIZ(J, IX) = QXJ + (-Y(15)) + QYJ + Y(20) + QZJ + Y(21)
      GU TU 951
  704 CALL POLAR
      LXD=(XI, L)XIHQ
      LADM(XI'f) AIHd
      PHIZ(J, IX) = QZJ
  951 CUNTINUE
       IF(IJ.GT.1) GO TO 958
       WRITE (6,955)
      GU TO 956
  958 WRITE(6,964)
```

```
956 DU 957 J=1,NFSEC
      IF (J.EQ.1) SPACE=RTIPS
      IF (J.EG.NESEC) SPACE = BHUB
      WRITE(6,901)SPACE, J, AN(J, IX), VY(J, IX), VZ(J, IX)
      IF(IPU.EQ.1) WRITE(7,1111) J.AN(J.IX), VY(J.IX), VZ(J.IX)
      SPACEBHLANKS
      IF(IJ.EQ.3) GO TO 957
      QXJ=AN(J,IX)
      UYJ=VY(J.IX)
      QZJ=VZ(J,IX)
      IF (IJ.EQ.2) GO TO 705
      ISM1=(NBSEC+J=1)+NSY
      DO 801 K=15,30
  801 Y(K)=SD(ISM1+K)
C
C
C
                 (65) Y + (19) + (24) Y + (24) + (25)
      AN(J, IX)
                 =QXJ*Y(23)+QYJ*Y(25)+QZJ*Y(27)
      VY(J,IX)
                 \pi Q X J + (-Y(15)) + Q Y J + Y(20) + Q Z J + Y(21)
      VZ(J,IX)
      GU TU 957
  705 CALL POLAR
      LXD=(XI, L) NA
      UY(J,IX)=QYJ
      LZO=(XI,L)\V
  957 CUNTINUE
      IF(IJ.GT.1) GO TO 970
      WRITE (6,959)
      GD TO 969
  970 WRITE(6,965)
  969 DO 960 J#1, NFSEC
      IF (J.EQ.1) SPACE BTIPS
      IF (J.ER. NFSEC) SPACE RHUB
      WRITE(6,901)SPACE, J, TEA(J, IX), AMY(J, IX), AMZ(J, IX)
      IF(IPU.EQ.1)WRITE(7,1111)J, TEA(J,IX), AMY(J,IX), AMZ(J,IX)
      SPACEMBLANKS
      IF (IJ.EQ.3) GO TO 960
      QXJ=TEA(J,IX)
      (XI, L) YMAELYD
      QZJ=AMZ(J,IX)
      IF(IJ.ER.2) GO TO 706
      ISM1=(NBSEC+J-1)+NSY
      DU 802 K=15,30
  802 Y(K)=SD(ISM1+K)
       TEA(J, IX) = 0XJ+Y(19)+0YJ+Y(24)+0ZJ+Y(26)
       AMY(J, IX) =QXJ+Y(23)+QYJ+Y(25)+QZJ+Y(27)
       AMZ(J, IX) #QXJ+(-Y(15))+QYJ+Y(20)+QZJ+Y(21)
      GU TO 960
  706 CALL POLAR
       TEA(J, IX)=QXJ
```

```
AMY(J,IX)=QYJ
      AMZ(J,IX)=QZJ
  960 CONTINUE
      IJ=IJ+1
 9001 IF(NPD.EQ.0)GO TO 7000
      IF(IJ.GT.3) GO TO 7000
IF(IJ.EQ.3) GO TO 707
      WRITE (6,919)
      GO TO 708
  707 WRITE(6,920)
  708 WRITE(6,962)
      GO TO 968
C
C
C
C
Č
¢
C
 7000 CONTINUE
  971 RETURN
  901 FURMAT(3x, A4, 3x, 12, 3(9x, 2(1PE12, 4)))
  950 FURMAT(//, T8, 'SECTION', T28, 'PHI X, THIST', T57, 'PHI Y, INPLANE SLO
     1PE', TB9, 'PHI Z, VERTICAL SLOPE', /, T28, '(+, TOP LEFT)', T60, '(+, VEC
     2T. UP) ', T93, '(+, VECT. LEFT)',//)
                    //, TO, 'SECTION', T27, 'N, AXIAL FURCE', T56, 'V Y, VERTICA
  955 FURHATE
     IL SHEAR', T91, 'V Z, INPLANE SHEAR', /, T24, '(+, RADIAL TO TAIL )', T
     259, 1(+, UPWARDS)
                             ',T95,'(+, L.H.S.)',//)
  959 FORMAT(//, T8, 'SECTION', T30, 'T, TORQUE', T57, 'M Y, INPLANE MOMENT',
     1790, M Z, VERTICAL MOMENT',/,T28, (+,TOP LEFT)',T55, (+, TENSION
     2LHS FIRERS)', TOO, '(+, TENSION LOWER FIBS.)',//)
  962 FORMAT(//, T8, 'SECTION', T25, 'UBX, AXIAL DEFL.',
     1758, UBY, VERTICAL DEF. 1, T92, UBZ, INPL. DEFL. 1, /, T28,
     2'(+, TO TAIL )', T58, '(+, UPWARD
                                           DIR.)', T95, '(+, L.H.8.)',//)
  964 FURMAT(
                    //, T8, 'SECTION', T26, 'NB, AXIAL FORCE', T58, 'VBY, VERTI
     1C. SHEAR', T92, 'VRZ, INPL. SHEAR', /, T28, '(+, TO TAIL )', T59, '(+, UP
     2WARD)
                   1,194, (+, TO LEFT )1,//)
  965 FURMAT(//,T8,'SECTION',T29,'T8, TORQUE',T57,'MBY, INPLANE MOMENT'
     1, T91, MBZ, VERTIC. MOMENT', /, T28, '(+, TDP LEFT)', T55, '(+, TENSION L 2. H. S. FIHERS)', T92, '(+, TENSION LOWER FIBS, )', //)
  963 FURMAT(//,T8,'SECTION',T28,'PHIBX, TWIST',T54,'PHIBY, INPL' RENDIN
     IG SLUPE', TAT, 'PHIBZ, VERTIC. BEND. SLUPE', /, T26, 1(+, NOSE HPWARD) !
     2,159, 1(+, VECT. UPWARD)',190, 1(+, VECTOR LEFT SIDE)',//)
```

```
SUBROUTINE MLRC2(R,T,NCOLS)
    REAL +8 R(144)
    CUMPLEX#16 T(84), THLD(84)
    COMPLEX#16 RCDOT
    NCR#12*NCOLS
    DO 100 N#1.NCOLS
    11N1=(N-1)+12
    DO 100 Mm1,12
    MM1=(M-1)+12
    K=NN1+M
    LMEMM1+1
    LNENN1+1
100 THLD(K)=RCDUT(12,K(LM),T(LN))
    DU 200 I=1,NCR
200 T(I)=THLD(I)
    RETURN
    END
```

```
SUBROUTINE MLCC2 (R,T,NCDLS)
   COMPLEX+16 R(144), T(R4), THLD(84)
   COMPLEX#16 CDOT
   NCR#12*NCULS
   DU 100 NEI, NCOLS
   NN1=(N-1)+12
   UU 100 M=1,12
   MM1=(M-1)+12
   KENN1+M
   LM=MM1+1
   LNBNN1+1
100 THLD(K)=CDOT(12,R(LM),T(LN))
   DU 200 I=1.NCR
200 T(I)=THLD(I)
    RETURN
    END
```

```
SUBRUUTINE THUS(I.J)
   CUMPLEX*16 TKN(441)
   COMMONITKN1/TKN
   COMMON/INTER/NSY, NASEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
  1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
  2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
  3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB.
  UNFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXCSB, MXCPM, MXCPK, MXSMR,
  5NEBC, NESBC, MFASB, MXFAB, NFUS, NRBO, NRIFC, MXQ, NEIFC,
  SNEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
   COMMON/NLEAD/MLEL, NLEL, MCTY
   DU 5 L=1.MXTKN
5 TKN(L)=DCMPLX(0.D0,0.00)
   IF (MPUS, EU. 0) GO TO 6
   CALL SUBMA(I,J)
6 CALL SUBMB(I,J)
   CALL SUHMG(I,J)
   IF (NH.EN.1) GO TO 10
   CALL SUBMF(I,J)
10 IF(NBC.GT.O)CALL ZTEGI(I.J)
   IF (NSP.EQ.0) GO TU 20
   CALL SWA (I,J)
   CALL SMB(I,J)
20 CUNTINUE
   RETURN
   END
```

```
SUBROUTINE EPSOLN
  CUMPLEX+16 TKN(441)
  CUMPLEX#16 FTEMP(21)
  CUMPLEX*16 EPS(63)
  CUMPLEX+16 ALM(63)
  CUMMUN/TKN1/TKN
  COMMON/EPSA/EPS
  CUMMUN/CALM/ALM
  COMMON/INTER/NSY,NHSEC,NFSEC,NB,NBP,MFLAP,MFEA,MCT,
 1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
 2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSR.
 4NFP1, MXSMI, MXT2P1, MXKG, MXCPL, MXCSB, MXCPM, MXCPK, MXSMB,
 SNEBC, NESHC, MFASB, MXFAH, NFUS, NRBD, NRIFC, MXQ, NEIFC,
 6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
  COMMON/NLEAD/MLEL, NLEL, MCTY
  IREMISIREM
  REWIND 1
  WRITE (1) MXSMI, NRIFC, NHC, NURM, IREM1, NEX
  DU 2 I=1, MXSMI
  DU 3 K=1,NRIFC
3 FTEMP(K)=DCMPLX(0.D0,0.D0)
  DO 4 JE1, MXSMI
  CALL TKNS(I.J)
  WRITE(1)(TKN(IRITE), IRITE#1, MXTKN)
  DO 5 IG=1, NRIFC
  DU 5 IP=1.NRIFC
  KP=(IP-1) +NRIFC+IW
  IJE(J=1) *NRIFC+IP
5 FTEMP(IQ) =FTEMP(IU) =ALM(IJ) +TKN(KP)
4 CONTINUE
  DU 2 LB1.NRIFC
2 EPS(NRIFC+(I-1)+L)=FTEMP(L)
  REWIND 1
  RETURN
  END
```

```
SUBRUUTINE HMASS
   REAL Y(100)
   COMPLEX#16 CMS, CM1, CS1, CS2, TOMS
   CUMPLEX*16 CSTE
   CUMPLEX+16 A(144)
   COMMON/ARI/A
   CUMMUN/SUB/Y
   COMMON/ROTF/OM1, NM2, NMT
   CUMMUN/DAMCO/OMDA
   CUMMON/FREF/CMS.CM1,CS1,CS2
   CUMMUN/AMASI/GCTCP
   CN1#Y(33) +GCTCP
   CSTE=CS2
   CS2=CS2+DMDA+CS1
   TUMS=UMT+CS1
   DU 5 I=1.144
5 A(1)=DCMPLX(0.DU,0.D0)
   DU 11 T#1,144,13
11 A(I) = UCMPLX(1.D0, U.U0)
   A(13)=Y(A)+(CS2-Y(17))
   A(15)*Y(33)*(TOMS*Y(20)*Y(28))
   A(17) == Y(8) + (TDMS + Y(21) + Y(29))
   A(18)==Y(9)*A(13)
   A(21) = Y(8) * (70) * Y(20) = Y(28)
   A(37)=-Y(33)*(TUMS+Y(20)+Y(28))
   A(39)=Y(34)+CS2+Y(43)-Y(20)+CN1
   A(41)==Y(33) *(TOMS*Y(15)=Y(30))
   A(42)=Y(36)+CS1+Y(39)
  A(45)==Y(33)*(CS2=Y(31))
  A(46)=Y(37) *CS1+Y(45)
  A(73) =A(18)
  A(75)=-Y(36)+CS1+Y(42)
  A(77) ==Y(9) *A(17)
  A(78)=Y(35)+C32+Y(40)+Y(20)+CN1
  A(81)=A(15)
  A(82)==Y(3A) *C81+Y(46)
  A(85)==Y(8)+(TDMS+Y(21)=Y(29))
  A(87)#=Y(33)*(TOMS*Y(15)+Y(30))
  A(89)==Y(8)*(C82=Y(32))
  A(90)=-Y(9) *A(85)
  A(93)=Y(8)*(T()MS*Y(15)*Y(30))
  A(123)==Y(37)+C91=Y(44)=Y(15)+CN1
  A(126) = Y(38) + C81 + Y(41) + Y(21) + CN1
  A(130)=Y(10)*C82-Y(47)
  A(133)==Y(8)*(TUMS*Y(20)+Y(28))
  A(135)==A(45)
  A(137)=-Y(8)+(TOMS+Y(15)=Y(30))
  A(138)==A(37)
  A(141)==Y(A)+(CS2=Y(31))
  CS2=CSTE
  RETURN
  END
```

```
SUBROUTINE FMASS
   REAL Y(100)
   CUMPLEX#16 #(144)
   COMPLEX+16 CMS,CM1,CS1,CS2,WI,WII
   CUMMUN/FREF/CM3,CM1,CS1,CS2
   COMMON/ARI/W
   COMMUN/SUB/Y
   COMMON/FGRAV/FGRA
   WI=CS2+Y(8)
   WII=Y(9)+WI
   CN1=FGRA+Y(33)
   DO 10 1=1,144
10 W(I)=DCMPLX(0,D0,0,D0)
   w(13)=WI
   W(18) ==WII
   W(39) = C92 + Y(34) - CN1 + Y(25)
   W(45)==WII
   W(75) == WII
   w(78) = C82 + Y(35) = CN1 + Y(25)
   IW==(98)W
   W(123) = CN1 * Y(23)
   #(126) = CN1 #Y(27)
   W(130) = C82 + Y(10)
   w(135)=+WII
   W(141)==#I
   DO 20 I=1,144,13
20 W(I)=DCMPLX(1.000,0.00)
   RETURN
   END
```

SUBRUUTINE STIFF COMPLEX+16 SK(144) REAL Y(100) CUMPLEX#16 CMS,CM1,CS1,CS2 CUMMUN/ARI/SK CUMMUN/SUH/Y CUMNUN/FREF/CMS, CM1, CS1, CS2 DU 5 1=1,144 5 SK(I)=DCMPLX(0.U0,0.D0) IF (Y(100) .EQ. 0.0) GO TU 10 SK (39) = Y(100) GO TO 20 10 SK(28) #Y(94)/(1.+Y(97)\*CS1) SK(67) #Y(96) /(1.+Y(99) \*CS1) SK(119) EY(95)/(1.+Y(98)\*CS1) 20 DU 30 TE1,144,13 30 8K(I)=DCMPLX(1.DO,0.DO) RETURN END

```
SUBRUUTINE BEND
  REAL Y(100)
  REAL +8 8(144)
  CUMMUN/SUB/Y
  COMMON/ARR/B
  DO 5 I=1,144
5 B(I)=0.00
  B(1)=Y(60)
  B(5)=Y(61)
  B(9)=-Y(62)
  B(14)=Y(60)
  B(20)=-Y(61)
  B(24)=Y(62)
  B(27)=Y(60)
  B(30)=Y(62)
  B(34)=Y(61)
  B(40)=Y(60)
  B(43)=Y(62)
  B(47)=Y(61)
  B(49)=Y(63)
  B(53)=Y(64)
  B(57)==Y(65)
  B(63)=Y(66)
  B(66) = Y(68)
  B(70)=Y(67)
  B(76)=Y(66)
  B(79)=Y(68)
  8(83)=Y(67)
  B(86) #-Y(63)
  B(92)=Y(64)
  B(96)=-Y(65)
  B(97)=-Y(66)
  B(101)==Y(67)
  B(105) = Y(68)
  B(111) = Y(63)
  B(114)=Y(65)
  B(118) #Y(64)
  B(124)=Y(63)
  B(127)=Y(65)
  B(131)=Y(64)
  B(134)#Y(66)
  B(140) =-Y(67)
  B(144)#Y(68)
  RETURN
  END
```

```
SUBROUTINE RIGID
   REAL Y(100)
   REAL+8 R(144)
   COMMON/SUH/Y
   CUMMUN/ARR/R
   DO 5 L=1,144
5 R(L)=0.00
   DO 10 L=1,144,13
10 R(L)=1.00
   R(6)=-Y(85)
   R(10)=Y(84)
   R(44)=-Y(84)
   R(48)==Y(83)
   R(51)=-Y(84)
   R(54)=Y(82)
   R(74)=Y(83)
   R(80)=Y(82)
   R(99) =+Y(83)
   R(106)=Y(82)
   R(122)=-Y(A4)
  R(132)=Y(82)
  R(39)=Y(85)
  R(42) #Y(86)
  R(46)=Y(87)
  R(75)=Y(88)
  R(78)=Y(89)
  R(82)=Y(90)
  R(123)=Y(91)
  R(126)=Y(92)
  R(130)=Y(93)
  RETURN
  END
```

```
SUBROUTINE ELAST
       REAL Y(100)
       REAL+8 CX(75)
       REAL +8 E(144)
       COMMON/SUB/Y
       CUMMUN/CFLEX/CX
       COMMUN/ARR/E
C
      DU 5 I=1,144
    5 E(I)=0.00
      DU 8 K=1,144,13
    8 E(K)=1.00
      IF(Y(7),GT.,9)G0 TO 10
      E(28)=Y(69)
      E(30) #+ Y(69) + Y(59)
      E(34) == Y(69) + Y(58)
      E(42) =- Y(56) + Y(70) + . 5 + Y(55) + Y(77) + Y(57) + (1.0+ Y(73))
      E(43) =- Y(56) + Y(71) + . 5 + Y(55) + Y(77) + Y(57) + Y(74)
      E(44) = Y(56) *Y(72) + .5 *Y(55) *Y(77) *Y(57) *Y(71)
      E(46) == Y(76) + Y(55)
      E(47) == Y(77) + Y(55)
      E(48) == Y(78) + Y(55)
      £(54)=Y(70)
      E(55)=Y(71)
      E(56)=Y(72)
      E(66)=Y(73)
      E(67)=Y(74)
      E(68)=Y(71)
      E(78) =+Y(70) +Y(54)
      E(79)=+Y(71)+Y(54)+1.0
      E(80)=+Y(72)+Y(54)+Y(75)
     E(102) == .5*Y(77) *Y(57) *(1.0+Y(73))
      E(103)=-.5*Y(77)*Y(57)*Y(74)
      E(104) = -. 5 + Y(77) + Y(57) + Y(71)
     E(106) = Y(76)
     E(107)=Y(77)
     E(108) #Y(78)
     E(114) == .5 + Y(80) + Y(57) + (1.0+Y(73))
     E(115)=-,5*Y(80)*Y(57)*Y(74)
     E(116)=-.5+Y(80)+Y(57)+Y(71)
     E(118)=Y(79)
     E(119)=Y(80)
     E(120)=Y(77)
     E(126)=-,5*Y(54)*Y(77)*Y(57)*(1,0+Y(73))
     E(127) == .5+Y(54)+Y(77)+Y(57)+Y(74)
     E(128)=-,5*Y(54)*Y(77)*Y(57)*Y(71)
     E(130)=+Y(76)+Y(54)
     E(131)=+Y(77)+Y(54)+1.0
     E(132)=+Y(78)+Y(54)+Y(81)
     GU TU 15
```

```
10
      CONTINUE
      E(13)=CX(1)
      E(15)=CX(4)
      E(17)=CX(2)
      E(18)=Cx(6)
      E(21)=-CX(3)
      E(22)=Cx(5)
      E(37)=CX(4)
      E(39) = CX(16)
      E(41)=CX(9)
      E(42)=CX(18)
      E(45) == CX(13)
      E(46)=CX(17)
      E(73) #CX(6)
      E(75)=Cx(18)
      E(77)=CX(11)
      E(78)=Cx(21)
      E(81)=-CX(15)
      E(82)=CX(20)
      E(85)=-CX(2)
      E(87)==CX(9)
      £(89)==CX(7)
      E(90) == CX(11)
      £(93)=CX(8)
      E(94) == CX(10)
      E(121)=CX(5)
      E(123)=Cx(17)
      E(125)=Cx(10)
      E(126)=CX(20)
      E(129) =- CX(14)
      E(130)=CX(19)
      E(133) =CX(3)
      E(135) #Cx(13)
      E(157)=CX(8)
      E(138)=CX(15)
      E(141)=-Cx(12)
      E(142) =CX(14)
000000000
   15 RETURN
```

END

```
SUBROUTINE FUARO(IL)
   REAL Y(100), AFA(240)
   CUMPLEX#16 CMS,CM1,CS1,CS2
   CUMPLEX+16 C(144)
   COMMUN/SUB/Y
   C()MM()N/FUSA/AFA
   CUMMUNIARIIC
   CUMMON/FREF/CMS,CM1,CS1,CS2
   IPQ=16+(IL=1)
   DU 5 I=1,144
5 C(I)=UCMPLX(0.D0,0.D0)
   C(18) = AFA(IPQ+1)
   C(22) == AFA(IPG+2)
   C(39) = -(AFA(IPQ+3) + CS1 + AFA(IPQ+4))
   C(41) =-AFA(IPU+5) +CS1
   C(42) = AFA(IPQ+5) + AFA(IPQ+6)
   C(45) = AFA(IPQ+7) + C51
   C(46) = +AFA(IPQ+7) + AFA(IPQ+6)
   C(82) = AFA(IPQ+16)
   C(87)=AFA(IPQ+8)+CS1+AFA(IPQ+9)
   C(89) = AFA(IPQ+10) *CS1
   C(90) = AFA(IPQ+10) + AFA(IPQ+6)
   C(93) == AFA(IPQ+11) +CS1
   C(94)#+AFA(IPQ+11)+AFA(IPQ+6)
   C(126) = AFA(IPQ+16)
   C(135) =-AFA(IPG+12) +C81-AFA(IPG+13)
   C(137) = -AFA(IPQ+14) *CS1
   C(138) = AFA(IPQ+14) + AFA(IPQ+6)
   C(141) #AFA(IPQ+15) +C81
   C(142) = -AFA(IPQ+15) + AFA(IPQ+6)
   DU 8 I=1,144,13
B C(I) #DCMPLX(1.Do,0.Do)
   RETURN
   END
```

```
SUBROUTINE BLARD (AC, AD, IL)
    CUMPLEX+16 AC(144), AD(144)
   CUMPLEX+16 AMA(2550)
   COMMUN/AMAT/AMA
    CUMMON/HARM/NHARM
   COMMON/INTER/NSY, NASEC, NESEC, NB, NBP, MFLAP, MFEA, MCT,
   1MFLEX,MCON,MAER,MFUS,NBC,NFLAP,NFEA,NCT,NCON,NFFB,
   2NAS,NHC,NVI,NSP,MAXN,NES,MSC,NEGN,IPCT,NIT,MER,NORM,
   3IREM, NEX, NPS, HSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSR,
   UNFPI, MXSMI, MXT2PI, MXKQ, MXCPL, MXCSB, MXCPM, MXCPK, MXSMR,
   SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
  SNEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
   COMMUNINLEAD/MLEL, NLEL, HCTY
   DO 10 J=1.144
   AC(J)=DCMPLX(0.D0,0.D0)
 10 AD(J)=UCMPLX(0.D0,0.00)
    IPQ = 34 + (IL=1) + MXSMI + (NHC+NHARM) + 34
21 FURMAT (1H0,10E12.6)
   AC(39) # AMA(IPR+1)
    AC(41) = AMA(IPQ+2)
    AC(45) = AMA(IPQ+3)
    AC(87) = AMA(IPQ+4)
    AC(89) # AMA(IPQ+5)
    AC(93) # AMA(IPQ+6)
    AC(135) = AMA(IPG+7)
    AC(137) = AMA(IPR+8)
    AC(141) = AMA(IPR+9)
    IF (NHARM.NE.O) GO TO 9
    SET DIAGONALS = 1., CREATE MATRIX D.
 8 DU 101 I = 1,144,13
101 AD(1) #DCMPLX(1.D0,0.D0)
 9 \text{ AU(18)} = \text{AMA(IPG+10)}
    AD(22) = AMA(IPQ+11)
    AD(37) = AMA(IPQ+12)
    AD(39) # AMA(IPQ+13)
    AD(41) = AMA(IPG+14)
    AD(42) = AMA(IPQ+15)
    AD(45) = AMA(IPQ+16)
    AD(46) # AMA(IPQ+17)
    AD(82) = AMA(IPQ+18)
    AD(85) # AMA(IPG+19)
    AD(87) = AMA(IPQ+20)
    AD(89) = AMA(IPG+21)
    AD(90) = AMA(IPQ+22)
    AD(93) = AMA(IPQ+23)
    AD(94) = AMA(IPQ+24)
    AU(126) = AMA(IPR+25)
    AD(133) - AMA(IP9+26)
    AD(135) = AMA(IPQ+27)
    AD(137) = AMA(IPQ+28)
```

11

AD(138) = AMA(IP0+29) AD(141) = AMA(IP0+30) AD(142) = AMA(IP0+31) RETURN END

370

```
SUBROUTINE SUBMA(I,J)
     INTEGER IROW1(6)
     COMPLEX EX, EXPON
     CUMPLEX*16 CM1
     COMPLEX+15 3(216)
     COMPLEX+16 TKN(441)
     CUMMON/SS1/S
     CUMMUN/TKN1/TKN
     COMMON/INTER/NSY, NHSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
   1 MFLEX, MCON, MAFR, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB.
   ZNAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM.
   3 IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSR,
   UNFPI, MXSMI, MXT2PI, MXKU, MXCPL, MXCSB, MXCPM, MXCPK, MXSMA,
   SNEBC, NESBC, MFASH, MXFAB, NFUS, NKBD, NRIFC, MXQ, NEIFC,
   SNEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
    COMMUNINCEAD/MLEL, NLEL, MCTY
    DATA IRON1/2,4,7,8,11,12/
    CM1#DEMPLX(0.DO,1.DO)
    NMKEJOI
    MNBC=(1-NBC)+(2-NBC)/2
    NNBC=(1=NBC) +(1=NBC)
    IF (NMK.NE. 0) GO TO 225
    IMNU#(I=1) *12*NCOLS
    DO 210 IGHI, NCOLS
    DU 210 IP=1.6
    KT=NEIFC+(IG=1)+NRIFC+MXT2P1+IP
    KB=IMNC+(IQ-1)+12+IROw1(IP)
210 TKN(KT)=8(KH)
    DO 220 MS=1,NA
    DO 220 IGE1, NCOLS
    KH1=IMNC+(IQ=1)+12+3
    KT1=NEIFC+(IG-1)+NRIFC+HXT2P1+NFUS+NRHD*(MS-1)+4
    KH2=KH1-2
    KT2=KT1+1
220 TKN(KT2)#8(KH2)
    GU TU 240
225 IF (NMK.NE. 1) GU TO 226
    IF(I.EQ. MXSMI)GU TO 240
    INTE-1
    GU TH 230
226 IF (NMK. NE. -1) GO TO 240
    IF (I.EG. 1) GO TO 240
    INTE!
250 JMNC=(J-1)+12+NCDL8
    DU 235 MS=1.NH
    EX=EXPON(=INT,MS)
    DO 235 10=1, NCOLS
    KH=JMNC+(IG-1)+12
    K81=K8+10
    KBS=KB+9
```

```
KB3mKB+6
KB4mKB+5
KTmNEIFC+(IQ=1)*NRIFC+NFUS+MXT2P1+NRBD*(MS=1)
KT1mKT+1
KT2mKT+2
KT3mKT+3
KT4mKT+6
TKN(KT1)m=.5*(S(KB2)+INT*CM1*S(KB4))*EX
TKN(KT2)m=.5*(-S(KB3)+INT*CM1*S(KB1))*EX*NNBC
TKN(KT3)m=.5*(S(KB4)=INT*CM1*S(KB2))*EX
TKN(KT4)m=.5*(S(KB1)+INT*CM1*S(KB3))*EX*MNBC
CONTINUE
RETURN
END
```

```
SUBROUTINE SUBMB (I, J)
  INTEGER IROW3(2), IALP(6), IROWC(2)
  INTEGER P, Q
  REAL+8 CX
  COMPLEX EXPON
  COMPLEX+16 CM1
  CUMPLEX+16 B(648), SMLB(108), SMLC(108), SMLD(108)
  COMPLEX+16 CTR(54), FAB(54), FLB(54)
  CUMPLEX#16 CTB1(9),CTB2(9),CTB3(9),FAB1(9),FAB3(9),FLB1(9),FLB2(9)
  COMPLEX+16 TKN(441)
  COMPLEX+16 SMLE(108),F88(54)
  COMPLEX+16 FSB1(9),FSB2(9),FSB3(9),FAB4(9),FLB4(9),CTB4(9)
  CUMPLEX+16 SMLF(108), SMLG(108)
  DIMENSION CX(75)
  CDMMON/BTS/B, SMLB, SMLC, SMLD, CTB, FAB, FLB, CTB1, CTB2, CTB3, FAB1,
 1FAB3,FLB1,FLB2,SMLE,FSB,FSB1,FSB2,F8B3,FAB4,FLB4,CTB4,SMLF,SMLG
  COMMON/CFLEX/CX
  COMMON/SHAFT/TORFLX
  COMMON/TKN1/TKN
  COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
 1 MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NPEA, NCT, NCON, NFFB,
 ZNAS, NHC, NYI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 3IREH, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCDLS, NCSB,
 UNFP1, MXSMI, MXT2P1, MXKG, MXCPL, MXCSB, MXCPM, MXCPK, MXSMB,
 SNEBC, LESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC.
 6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
   COMMON/NLEAD/MLEL, NLEL, MCTY
   DATA IRUWC/1,0/
  DATA IROW3/12,7/
  DATA IALP/1,3,5,6,9,10/
  MCACFEO
  MCACGRO
   IF(MFU8.EQ.O) GD TD 65
   CHIADCHPLX(0.DO,1.DO)
  NMKBJ-I
  NUNDEO
   IF (NMK.EQ.O)NONO=1
   MNBC#(1-NBC) *(2-NBC)/2
   NNBC#(1=NBC) #(1=NBC)
  DO 10 GHI, NCOLS
  DO 10 Pe1,2
  L=(J=1)+NEBC+(I=1)+MXCPM+(Q=1)+12+IROH3(P)
   KTENEIFC+MXT2P1+NEI8C+(Q-1)+NRIFC+P
   LC#(J=1) +NCOL8+MX8MI+(I=1) +NCOL8+Q
10 TKN(KT)==B(L)+FLB(LC)+MFLEX+MCON+IROWC(P)
   IF(MFLEX.EQ.O) GO TO 11
   IF(HCON, EQ. 0) GO TO 29
  MCT#1
  MFEAB!
  MFLAPB1
```

```
MLEL#0
   IF(MCTY.EQ.O) GO TO 11
   MCACF#1
   MCACG=1
   MLEL=1
11 00 15 P=1,2
   L=(J-1) +NESBC+(I-1) +MXCSR+IROW3(P)
   KT=NEIFC+MXT2P1+NEISC+NCOLS+NRIFC+P
   IF (MCT.EQ. 0) GU TO 12
   TKN(KT) #SMLB(L) +CX(3) +MFLEX+IROMC(P) +NONO
   KT=KT+NRIFC
12 IF (MFEA, EQ. 0) GU TO 13
   TKN(KT) = SMLC(L) = CX(8) & MFLEX + IROWC(P) + NONO
   KT=KT+NRIFC
13 IF(MFLAP.EQ.O) GO TO 14
   TKN(KT) #SMLD(L)+CX(12) #MFLEX+IRUWC(P) #NONO
   KT=KT+NEIFC
14 IF (MLEL, ER. 0) GO TO 16
   TKN(KT)=SMLE(L)+CX(24)+MFLEX+IROWC(P)+NUNO
   KT#KT+NRIFC
16 IF (MCACF.EQ. 0) GO TO 17
   TKN(KT)#SMLF(L)+CX(27)*MFLEX#IROWC(P)*NONO
   KT=KT+NRIFC
17 IF(MCACG.EQ.O) GD TO 15
   TKN(KT)#SMLG(L)+CX(30)#MFLEX#IHUWC(P)#NONO
15 CUNTINUE
29 CONTINUE
   IF(I.EQ.1) GO TU 50
30 DO 31 9m1, NCOLS
   LM=(J-1) +NEBC+(I-2) +MXCPM+(Q-1)+12
   KTANEIFC+MXT2P1+NEISC+(G-1)+NRIFC+3
   LM1=LM+4
   LM2=LM+11
   TKN(KT)#TKN(KT)+.5*(B(LM1)=CM1*MNBC*B(LM2))*NNBC
   KT=KT+1
   LM3=LM+8
   LM4=LM+2
   TKN(KT)=TKN(KT)=.5+(A(LM3)=CM1+B(LM4))
   TKN(KT)=TKN(KT)=.5+(MNBC+B(LM2)+CM1+B(LM1))+NNBC
   KTEKT+1
31 TKN(KT)#TKN(KT)+.5+(B(LM4)+CM1+B(LM3))
   IF (MFLEX.ER. 1. AND. MCON. ER. O) GO TO 35
   LM=(J=1) +NESBC+(I=2)+MXCSB
   KT#NEIFC+MXT2P1+NEISC+NCOLS*NRIFC+3
   LM1BLM+4
   LM2=LM+11
   LM3=LM+8
   LM4=LM+2
   IF(MCT.EQ.0) GO TU 32
```

```
TKN(KT) #TKN(KT) = .5 * (SMLB(LM1) #CM1 *MNBC * SMLB(LM2)) *NNBC
   KT=KT+1
   TKN(KT)#TKN(KT)+.5+(SMLB(LM3)=CM1+SMLH(LM4))
   KT=KT+1
   TKN(KT)#TKN(KT)+.5*(MNBC*SMLB(LM2)+CM1*SMLB(LM1))*NNBC
   KT#KT+1
   TKN(KT)=TKN(KT)=_5+(SMLB(LM4)+CM1+SMLB(LM3))
   KT#KT+3+NRIFC
32 IF (MFEA.EQ.O) GU TO 33
   TKN(KT)=TKN(KT)=.5*(SMLC(LM1)=CM1*MNBC*SMLC(LM2))*NNBC
   KT=KT+1
   TKN(KT)=TKN(KT)+,5*(9MLC(LM3)=CM1*8MLC(LM4))
   KTSKT+1
   TKN(KT)=TKN(KT)+_5+(MNBC+SMLC(LM2)+CM1+8MLC(LM1))+NNBC
   KTEKT+1
   TKN(KT)=TKN(KT)=.5*(SMLC(LM4)+CM1+8MLC(LM3))
   KT#KT=3+NRIFC
33 IF (MFLAP_EQ.O) GU TO 34
   TKN(KT)=TKN(KT)=.5*(9MLD(LM1)=CM1*MNBC*SMLD(LM2))*NNBC
   KTEKT+1
   TKN(KT) # TKN(KT) + .5*(SMLD(LM3) = CM1 * SMLU(LM4))
   KTSKT+1
   TKN(KT)#TKN(KT)+.5*(MNBC*8MLD(LM2)+CM1*8MLD(LM1))*NNBC
   KT=KT+1
   TKN(KT)=TKN(KT)-.5*(9MLD(LM4)+CM1+8MLD(LM3))
   KTEKT-3+NRIFC
34 IF(MLEL_EQ.0) GU TO 36
   TKN(KT)mTKN(KT)m_5*(8MLE(LM1)=CM1*MNBC*SMLE(LM2))*NNBC
   KT#KT+1
   TKN(KT)mTKN(KT)+.5*(SMLE(LM3)=CM1*SMLE(LM4))
   KTSKT+1
   TKN(KT)=TKN(KT)+_5+(MNBC+SMLE(LM2)+CM1+SMLE(LM1))+NNBC
   KT=KT+1
   TKN(KT)#TKN(KT)=,5*(SMLE(LM4)+CM1*SMLE(LM3))
   KTEKT-3+NHIFC
36 IF(MCACF.EQ.O) GO TO 37
   TKN(KT)=TKN(KT)=.5*(SMLF(LM1)=CM1*MNBC*SMLF(LM2))*NNRC
   KT#KT+1
   TKN(K1)#TKN(K1)+.5+(8MLF(LM3)=CM1+8MLF(LM4))
   KT=KT+1
   TKN(KT)#TKN(KT)+.5*(MNBC+SMLF(LM2)+CM1*SMLF(LM1))*NNBC
   KT#KT+1
   TKN(KT)=TKN(KT)=.5+(SMLF(LM4)+CM1+SMLF(LM3))
   KTEKT-3+NRIFC
37 IF(MCACG.EQ.O) GO TO 35
   TKN(KT)#TKN(KT)=.5+(SMLG(LM1)=CM1+MNBC+SMLG(LM2))+NNBC
   KTHKT+1
   TKN(KT)mTKN(KT)+.5*(SMLG(LM3)=CM1*SMLG(LM4))
   KT#KT+1
   TKN(KT)=TKN(KT)+.5+(HNBC+SMLG(LM2)+CM1+SMLG(LM1))+NNBC
```

```
KTEKT+1
   TKN(KT)#TKN(KT)#.5*(SMLG(LM4)+CM1*8MLG(LM3))
35 CUNTINUE
50 IF(I.GE.MXSMI) GO TO 45
40 DU 41 Q=1,NCULS
   LP=(J-1) +NEBC+1+MXCPM+(Q-1)+12
   KTENEIFC+MXT2P1+NEISC+(Q-1)*NHIFC+3
   LP1=LP+4
   LP2=LP+11
   LP3=LP+B
   LP4mLP+2
   TKN(KT)#TKN(KT)+.5+(B(LP1)+CM1+MNBC+B(LP2))*NNBC
   KT#KT+1
   TKN(KT) = TKN(KT) = .5*(B(LP3) + CM1 + B(LP4))
   KT#KT+1
   TKN(KT)=TKN(KT)=.5+(MNBC+B(LP2)=CM1+B(LP1))*NNBC
   KTEKT+1
41 TKN(KT)=TKN(KT)+.5+(B(LP4)-GM1+B(LP3))
   IF (MFLEX.ER.1.AND.MCON.EQ.O) GO TO 45
   LP#(J=1) *NESBC+I*MXCSB
   KTENEIFC+MXT2P1+NEISC+NCOLS+NRIFC+3
   LP1=LP+4
   LP2=LP+11
   LP3=LP+R
   LP4=LP+2
   IF (MCT_EN_0) GO TO 42
   TKN(KT)=TKN(KT)=.5*(SMLB(LP1)+CM1*MNBC*SMLH(LP2))*NNBC
   KT=KT+1
   TKN(KT)=TKN(KT)+.5+(SMLB(LP3)+CM1+SMLB(LP4))
   KT=KT+1
   TKN(KT)=TKN(KT)+.5*(MNBC+SMLB(LP2)=CM1*SMLB(LP1))*NNRC
   KT=KT+1
   TKN(KT)=TKN(KT)=_5+(SMLB(LP4)=CM1+8MLB(LP3))
   KT#KT-3+NRIFC
42 IF (MFEA, EQ. 0) GO TO 43
   TKN(KT)#TKN(KT)#.5*(SMLC(LP1)+CM1*MNBC*SMLC(LP2))*NNBC
   KT#KT+1
   TKN(KT)*TKN(KT)+.5*(SMLC(LP3)+CM1*SMLC(LP4))
   KT#KT+1
   TKN(KT)=TKN(KT)+_5*(MNBC*8MLC(LP2)=CM1*8MLC(LP1))*NNBC
   KTBKT+1
   TKN(KT)=TKN(KT)=_5*(SMLC(LP4)=CM1*SMLC(LP3))
   KT#KT#3+NRIFC
43 IF(MFLAP, EQ. 0) GO TO 44
   TKN(KT)#TKN(KT)=.5*(SMLD(LP1)+CM1+MNBC+SMLD(LP2))*NNBC
   KT=KT+1
   TKN(KT)#TKN(KT)+.5*(SMLD(LP3)+CM1*SMLD(LP4))
   KT=KT+1
   TKN(KT) #TKN(KT)+.5+(MNHC+SMLD(LPZ)-CM1+SMLD(LP1))+NNRC
   KT=KT+1
```

```
TKN(KT)=TKN(KT)=.5*(SMLD(LP4)=CM1*SMLD(LP3))
    KT=KT=3+NRIFC
 44 IF (MLEL, EQ. 0) GO TO 38
    TKN(KT)=TKN(KT)=.5+(SMLE(LP1)+CM1+MNBC+SMLE(LP2))+NNBC
    KT#KT+1
    TKN(KT) = TKN(KT) + .5 * (SMLE(LP3) + CM1 * SMLE(LP4))
    KT=KT+1
    TKN(KT)=TKN(KT)+.5+(MNBC+SMLE(LP2)=CM1+SMLE(LP1))+NNBC
    KTEKT+1
    TKN(KT)aTKN(KT)-.5+(SMLE(LP4)-CM1+SMLE(LP3))
    KT=KT-3+NRIFC
 38 IF(MCACF.EQ.O) GO TO 39
    TKN(KT)=TKN(KT)=.5*(SMLF(LP1)+CM1*MNBC*SMLF(LP2))*NNBC
    KT#KT+1
    TKN(KT)=TKN(KT)+_*5*(SMLF(LP3)+CM1*SMLF(LP4))
    KT#KT+1
    TKN(KT)=TKN(KT)+.5+(MNBC+9MLF(LP2)=CM1+9MLF(LP1))+NNBC
    KT=KT+1
    TKN(KT) = TKN(KT) = .5 + (8MLF(LP4) = CM1 + 8MLF(LP3))
    KT#KT=3+NRIFC
 39 IF (MCACG.EQ. 0) GO TO 45
    TKN(KT)=TKN(KT)=.5+(SMLG(LP1)+CM1+MNBC+SMLG(LP2))+NNBC
    KT=KT+1
    TKN(KT)#TKN(KT)+.5*(SMLG(LP3)+CM1*SMLG(LP4))
    KT=KT+1
    TKN(KT)aTKN(KT)+_5*(MNBC+SMLG(LP2)=CM1*SMLG(LP1))*NNBC
    KTBKT+1
    TKN(KT)=TKN(KT)=.5*(SMLG(LP4)=CM1*SMLG(LP3))
 45 CUNTINUE
    IF (NBP.EQ.O) GO TO 100
    NPMK==NP8+NFP1=I
    INMK=IABS(NPMK)
    RINMK#1.0+INMK
    RFARRINMK/NBP
    NFA=INMK/NBP
    DIFMABS(RFA-1.0+NFA)
    IF(DIF.LT.(.05)) GO TO 70
    ISEXP=0
    GU TO 71
 70 ISEXPONBP
 71 IGMAXENRED
    DO 73 Pm1,6
    DU 73 QHI, IQMAX
    KTWNEIFC+MXT2P1+NEISC+(Q-1)*NRIFC+P
73 TKN(KT) #TKN(KT) #ISEXP
    GD TO 65
100 IF(NB,LT.2) GO TO 65
46 NMKEJOI
    DO 47 M8#2, NB
    DO 47 GB1, NRBD
```

```
DU 47 P=1.6
    KT=NEIFC+MXT2P1+NEISC+(Q=1)+NRIFC+P
    KT2=KT+(MS=1) *NEITC
    TKN(KT2) # TKN(KT) # EXPON(NMK, MS)
    IF (P.NE.2) GN TO 47
    DU 57 MM=1,NR
    IF (MS.GT.2) GO TO 56
    IF (Mm.EQ.1) GO TO 56
    KT4mKT+8+(MM=1)*NR8D
    TKN(KT4)=TKN(KT)+TURFLX
 56 CUNTINUE
    KT3=KT2+8+(MM-1)+NRUD
    TKN(KT3)#TKN(KT2)#TURFLX
 57 CUNTINUE
    TKN(KT2)=DCMPLX(0.D0.0.D0)
 47 CUNTINUE
 65 DO 110 KK=1,6
    DU 110 U=1.NCOLS
    L=(J-1)*NEBC+(I-1)*MXCPM+(Q-1)*12+IALP(KK)
    KTHNEIFC+NEISC+(Q-1)+NRIFC+MXT2P1+NFUS+KK
    IF (KK.EH.4.AND.MFUS.NE.O) GO TO 111
    TKN(KT)=8(L)
    GO TO 110
111 KTT#KT#8
    TKN(KT)=B(L)+TKN(KTT)+TORFLX
    TKN(KTT) = DCMPLX(0.D0,0.D0)
110 CUNTINUE
    IF (MFLEX, EQ. 0) GO TO 112
    IF (MCUN, EG. 0) GO TO 129
    MCT#1
    MFEA=1
    MFLAP=1
    MLEL=0
    IF(MCTY.EQ.O) GO TO 112
    MCACF=1
    MCACG#1
    MLEL=1
115 DO 151 KK=1,6
    L=(J=1) +NESBC+(I=1) +MXCSB+IALP(KK)
    KT=NEIFC+NEISC+NCULS+NRIFC+MXT2P1+NFUS+KK
    IF(MCT.EQ.0) GO TO 122
    TKN(KT) == SMLB(L)
    IF (KK. NE. 4) GO TO 113
    IF (MFUS.EQ.0) GU TO 113
    KTT=KT=8
    TKN(KT) == SMLB(L)+TKN(KTT) +TORFLX
    TKN(KTT)=DCMPLX(0,D0,0.D0)
113 KT#KT+NRIFC
122 IF (MFEA.EQ.0) GO TO 123
    TKN(KT)==SMLC(L)
```

```
IF (KK.NE.4) GO TO 114
    IF (MFUS, EQ. 0) GO TO 114
    KTT#KT-8
    TKN(KT) == SMLC(L)+TKN(KTT) #TURFLX
    TKN(KTT)=DCMPLX(0.D0,0.D0)
114 KT#KT+NRIFC
123 IF (MFLAP.EQ.0) GO TO 124
    TKN(KT) == SMLD(L)
    IF (KK.NE.4) GO TO 115
    IF (MFUS.EQ.0) GO TO 115
    KTT#KT#8
    TKN(KT) == SMLD(L)+TKN(KTT) +TURFLX
    TKN(KTT)=DCMPLX(0.D0,0.D0)
115 KT=KT+NRIFC
124 IF (MLEL.EQ.0) GO TO 125
    TKN(KT) #= SMLE(L)
    IF (KK.NE.4) GO TO 116
    IF (MFUS.EQ.0) GD TO 116
    KTT=KT-8
    TKN(KT) == SMLE(L)+TKN(KTT) +TORFLX
    TKN(KTT)=DCMPLX(0.D0,0.D0)
116 KT#KT+NRIFC
125 IF (MCACF.EQ.0) GO TO 126
    TKN(KT)==SMLF(L)
    IF (KK.NE.4) GU TO 117
    IF (MFUS.EQ.0) GO TO 117
    KYTEKT-8
    TKN(KT)==SMLF(L)+TKN(KTT)+TURFLX
    TKN(KTT) #DCMPLX(0.D0,0.D0)
117 KT=KT+NRIFC
126 IF (MCACG.EQ.0) GO TU 121
    TKN(KT) == SMLG(L)
    IF (KK.NE.4) GO TO 121
    IF (MFUS, EQ. 0) GU TU 121
    KTT=KT=8
    TKN(KT)==SMLG(L)+TKN(KTT) *TORFLX
    TKN(KTT) = DCMPLX(0.D0,0.D0)
121 CUNTINUE
129 CUNTINUE
    RETURN
    END
```

```
SUBROUTINE SUBMG(I,J)
 INTEGER P.Q
 REAL+8 CX
 COMPLEX+16 B(648), SMLB(108), SMLC(108), SMLD(108)
 COMPLEX*16 CTB(54), FAB(54), FLB(54)
 COMPLEX*16 CT81(9),CT82(9),CT83(9),FA81(9),FA83(9),FL81(9),FL82(9)
 COMPLEX#16 TKN(441)
 COMPLEX+16 SMLE(108), F88(54)
 COMPLEX+16 SMLF(108), SMLG(108)
 COMPLEX*16 F881(9), F882(9), F883(9), FA84(9), FL84(9), CT84(9)
 COMPLEX+16 YKM(3,6),CS1,CS2,CM1,CMS
 DIMENSION CX(75)
 DIMENSION AL536(6), AL436(6)
 COMMON/CPARS/ALSTH(6)
 COMMON/SPAR/AKCI(6),TAU(6),SMLA(6),DMS(6),AK(4),AC(4),BJ(4),
1CAPK, CAPC
 CUMMON/CPAR/AMKC(6),CTAU(6),AL(6,6),AL12(6)
 COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
3IREM, NEX, NP8, NSCH, IG, IF, NPRL, NPR8, NPD, NSK, NCOLS, NCSB,
4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXC8B, MXCPM, MXCPK, MX8MB,
SNEBC, NESBC, MFASB, MXFAB, NFUS, NKBD, NRIFC, MXQ, NEIFC,
6NEISC, NEITC, MXTKN, NFP, MINPN, MAXPN, IBF, MODE
 CUMMON/ROTF/OM1, OM2, OMT
 CUMMUN/FREF/CM8, CM1, C81, C82
 COMMON/TKN1/TKN
 COMMON/CFLEX/CX
COMMON/BTS/8, SML8, SMLC, SMLD, CTB, FAB, FLB, CTB1, CTB2, CTB3, FAB1, FAB3,
1FLB1,FLB2,8MLE,FSB,FSB1,FSB2,FSB3,FAB4,FLB4,CTB4,8MLF,SMLG
 COMMON/NLEAD/MLEL, NLEL, MCTY
NMK#J#I
NUNU#1
KSML#I-NFP1
CS1CMS-CM1+K8ML+DM1
 IF (NMK_NE_O) NONDEO
 IF(MFLEX.EQ.0) GO TO 100
 IF(MCUN.EQ.O) GO TO 900
M3#1
 OOS OF CO (O.TO.YTOM) TI
 YKM(I,M8)#AMKC(M9)/((1.+C81+CTAU(M8)#AMKC(M8)#AL(6,M9)#AL(6,M8)#
DO 300 Q#1,NRBD
KTHNEIFC+NEISC+(Q-1)*NRIFC+MXT2P1+NFUS+NCOLS
KUZENEIFC+NEISC+(Q=1)+NRIFC+MXT2P1+NFUS+5
KUX#KUZ=4
KPY#KUZ+1
KUYSKUZ-2
KPX#KUZ-3
IF(Q.GT.6) GO TO 301
L=(J-1) +NCOL S+MXSMI+(I-1) +NCOLS+G
```

ŧ

```
TKN(KT+1)=-AL(1,MS)+CTB(L)=AL(2,MS)+FAB(L)=AL(3,MS)+FLB(L)
   TKN(KT+2)=AL(4,MS)+CTB(L)-AL(5,MS)+FAB(L)
   TKN(KT+3)==YKM(I,M3)+FLB(L)+(N3P=1)+TKN(KUZ)
  1=(TKN(KUX)=AL12(MS)*TKN(KPY))*AL(3,MS)/AL(6,MS)*AL(5,MS)
  2+(TKN(KUY)+AL12(MS)+TKN(KPX))*AL(3,MS)/AL(6,MS)*AL(4,MS)
   GD TO 300
301 IF(Q=8) 302,303,304
302 TKN(KT+1)=(AL(1,MS)+CX(1)+AL(2,MS)+CX(2)+AL(3,MS)+CX(3))+NOND
    TKN(KT+2)=(AL(4,M8)*CX(1)+AL(5,M8)*CX(2))*NUND
   TKN(KT+3)m+YKM(I,MS)+CX(3)+NONO+(NSP-1)+TKN(KUZ)
  1=(TKN(KUX)=AL12(M$)*TKN(KPY))*AL(3,M$)/AL(6,M$)*AL(5,M$)
  2+(TKN(KUY)+AL12(MS)*TKN(KPX))*AL(3,MS)/AL(6,MS)*AL(4,MS)
  3+AL (3, M8) /AL (6, M8) *AL (5, M8) *NONO
   GO TO 300
303 TKN(KT+1) #(AL(1, MS) *CX(2)+AL(2, MS) *CX(7)+AL(3, MS) *CX(8)) *NONO
    TKN(KT+2)#(AL(4,MS)+CX(2)+AL(5,MS)+CX(7))+NOND
    TKN(KT+3)=+YKM(I,MS)+CX(B)+NUND+(NSP+1)+TKN(KUZ)
  1-(TKN(KUX)-AL12(MS)*TKN(KPY))*AL(3,MS)/AL(6,MS)*AL(5,MS)
  2+(TKN(KUY)+AL12(MS)*TKN(KPX))*AL(3,M8)/AL(6,MS)*AL(4,M$)
   3-AL (3, MS) /AL (6, MS) +AL (4, MS) +NDNO
   GD TU 300
304 TKN(KT+1)==(AL(1,M8)+CX(3)+AL(2,M3)+CX(8)+AL(3,M8)+CX(12))+NDNO
    TKN(KT+2)==(AL(4,M3)+CX(3)+AL(5,M8)+CX(8))+NONO
    TKN(KT+3)=(-YKM(1,M3)*CX(12)+DCMPLX(1.D0,0.D0))*NONO+(N8P-1)*
   1TKN(KUZ)
   1-(TKN(KUX)-AL12(M3)+TKN(KPY))+AL(3,M8)/AL(6,M8)+AL(5,M8)
  2+(TKN(KUY)+AL12(MS)+TKN(KPY))+AL(3,MS)/AL(6,MS)+AL(4,MS)
300 CONTINUE
   GO TO 900
AL536(M8) #AL(5,M8) *AL(3,M8)/AL(6,M8)
   AL436(M8)=AL(4,M8)+AL(3,M8)/AL(6,MS)
   DD 250 GB1,NRBD
   KT#NEIFC+NEISC+(Q=1)+NRIFC+MXT2P1+NFU8+NCOL8
   KUZ=NEIFC+NEISC+(Q=1)*NRIFC+MXT2P1+NFU8+5
   KUXBKUZ-4
   KPYEKUZ+1
   KUYSKUZ-2
   KPXeKU2-3
   TKN(KT+1)=TKN(KUX)=ALSTH(MS)+TKN(KPY)
   TKN(KT+2)=TKN(KUY)+ALSTH(MS)+TKN(KPX)
    TKN(KT+3)=TKN(KUZ)
   IF (NONO.EQ. 0) GO TO 201
   IF(Q.LT.7) GO TO 201
   IF(0.67.9) GO TO 201
   IF(Q.EQ.7) TKN(KT+1)=TKN(KT+1)=DCMPLX(1.D0,0.D0)
   IF(Q.EQ.8) TKN(KT+2)=TKN(KT+2)=DCMPLX(1.D0.0.D0)
   IF(@.E@.4) TKN(KT+3) #TKN(KT+3) #DCMPLX(1.D0,0.D0)
201 IF(Q.GT.6) GO TO 205
   L=(J-1) +NCOL8+MX8M1+(I-1) +NCOL8+0
```

```
TKN(KT+6) #AL536(MS) *CTB(L) -AL436(MS) *FAB(L) -FSB(L) -
   1AL536(MS) + (TKN(KUX) - AL12(MS) + TKN(KPY))+
   2AL436(MS)*(TKN(KUY)+AL12(MS)*TKN(KPX))+(NSP=1)*TKN(KUZ)
    GU TD 250
205 LL1=58+(G=7)+3
    LL2=LL1+1
    LL3=LL1+2
    TKN(KT+6)==AL536(M8)+(TKN(KUX)=AL12(M8)+TKN(KPY))+
   1AL436(MS)*(TKN(KUY)+AL12(MS)*TKN(KPX))+(NSP=1)*TKN(KHZ)+
   2(AL536(MS)*CX(LL1)=AL436(MS)*CX(LL2)=CX(LL3))*NONO
    NOTE ELEMENTS 64,65,66 OF CX ARRAY CHANGED SIGN IN SECPAR
    IF (W.LT.10) Gn Th 250
    IF (NUND. EQ. 0) GO TO 250
    IF (W.GT.10) GO TO 210
    TKN(KT+4) =AL(1,MS)
    TKN(KT+5) =AL(4,MS)
    TKN(KT+6) #TKN(KT+6) + AL536(MS) * YKM(I, MS)
    GU TO 250
210 IF (W.GT.11) GU TO 220
    TKN(KT+4) =AL(2,MS)
    TKN(KT+5) = AL(5,MS)
    TKN(KT+b)=TKN(KT+b)=AL436(M5)*YKM(I,MS)
    GU TO 250
220 TKN(KT+4)=AL(3,M8)
    TKN(KT+6)=TKN(KT+6)=YKM(I,MS)
250 CUNTINUE
    GU TU 900
100 CONTINUE
    MS=1
    YKM(I,MS)=SMLA(MS)*(1+CS1*TAU(MS))
    DU 10 GE1, NCOLS
    KTHNEIFC+NEISC+(D+1)+NRIFC+MXT2P1+NFUS+7
    Lm(J=1) *NCOLS*MXSMI+(I=1) *NCOLS+Q
    IF (MCT.EQ.0) GO TO 20
    TKN(KT) = SMLA(MS) + CTB(L) + YKM(1,MS)
    KT=KT+1
 20 IF (MFE4.ER.O) GO TO 30
    TKN(KT)=FAB(L)
    KT=KT+1
 30 IF (MFLAP, EQ, 0) GO TO 31
    TKN(KT)=FLB(L)
    KT#KT+1
 31 IF (MLEL.EQ. 0) GO TO 10
    TKN(KT)=FSB(L)
 10 CUNTINUE
    KIENEIFC+NEISC+NCULS#NRIFC+MXT2P1+NFUS+7
    L=(J-1)*MXSMI+(I-1)*1
    IF (MCT.EW.O) GO TO 40
    TKN(KT) #AKCI(MS) #CTB1(L)
    KT1=KT+NRIFC
```

IF (MFEA.EQ.O) GO TO 32 TKN(KT1) #SMLA(MS) \*YKM(I, MS) \*CTB2(L) KT1=KT1+NRIFC 32 IF(MFLAP.EQ.O) GO TO 34 TKN(KT1)=SMLA(MS)+CTR3(L)+YKM(I,MS) KT1=KT1+NRIFC 34 IF (MLEL\_EQ.0) GO TO 36 TKN(KT1) = SMLA(MS) \*CTB4(L) \*YKM(I, MS) 36 KT=KT+1 40 IF (MFEA, EQ. 0) GO TO 50 KT2=KT+NRIFC .-IF (MCT.EQ.O) GO TO 42 TKN(KT)==FAB1(L) KT2#KT2+NRIFC 42 IF (MFLAP.ER.O) GO TU 44 TKN(KT2)==FAB3(L) KT2=KT2+NRIFC 44 IF(MLEL\_EQ.O) GO TO 46 TKN(KT2)==FAB4(L) 46 KTHKT+1 50 IF (MFLAP, EQ. 0) GO TO 56 KT1#KT IF(MCT.EQ.0) GO TO 52 TKN(KT)==FLB1(L) KT1=KT1+NRIFC 52 IF (MFEA.EG.0) GO TO 54 TKN(KT1)==FLB2(L) KT1#KT1+NRIFC 54 KT1mKT1+NRIFC IF (MLEL.EQ.O) GO TU 55 TKN(KT1)==FLB4(L) 55 KT#KT+1 56 IF (MLEL.EQ.0) GO TO 60 IF (MCT.EQ.0) GO TU 57 TKN(KT) == FSB1(L) KT#KT+NRIFC 57 IF (MFEA, EQ. 0) GO TO 58 TKN(KT)==FSB2(L) KT#KT+NRIFC 58 IF(MFLAP.EQ.0) GO TO 60 TKN(KT)#-F8B3(L) 60 CONTINUE 900 CUNTINUE RETURN END

1

```
SUBRUUTINE SURMF(1,J)
     INTEGER P.Q
    COMPLEX EXPON
    CUMPLEX+16 TKN(441)
    COMMON/INTER/NSY, NASEC, NESEC, NB, NBP, MFLAP, MFEA, MCT,
   1 MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
   ZNAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
   31REM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB.
   4NFP1, MXSMI, MXT2P1, MXKQ, MXCPL, MXCSB, MXCPM, MXCPK, MXSMB,
   SNEBC, NESHC, MFASH, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
   SNEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
    CUMMUN/TKN1/TKN
    CUMMUN/NLEAD/MLEL, NLEL, MCTY
    IF (NB.EQ.1)GD TO 586
    NMKBJeI
    DO 547 MS=2.NB
    DO 547 0=1, NRBD
    DU 547 P#1, NRBD
    KT=NEIFC+NEISC+(Q=1) +NRIFC+NFUS+MXT2P1+P
    KT2=KT+(MS=1)+(NEITC+NRBD)
547 TKN(KT2)=TKN(KT)+EXPON(NMK,MS)
586 RETURN
    END
```

```
SUBROUTINE SOLVE
      REAL *8 DTLG10, DFAC, FAC
      COMPLEXA: 6 ZERO, TWO, SUM, SWAP, DTPHAS, DPIVOT, DETSV
      CUMPLEX+16 EP8(63), FORCE(63), DB(63,63)
      COMMON/EPSA/EPS
      CUMMUN/REHA/DETSV
      COMMON/CDETRM/DPIVOT, DTPHAS, DTLG10, IDET
      COMMUNIDIERMIDEAC
      FACULO.DO
      TWO#DCMPLx(2.D0,0.D0)
      ZEROMDCMPLX(0,D0,0,D0)
      REWIND 1
      READ(1) MXSMI, NRIFC, NHC, NORM, IREM1, NEX
      NORDER#MX8MI*NRIFC
      DO 11 LEI, MXSMI
      INDWF#L+NRIFC
      IROWS=IROWF-NRIFC+1
      DO 11 KalamxSHI
      ICULF#K*NRIFC
      ICOLS=ICOLF-NRIFC+1
   11 READ(1)((DB(I,J),I=IRUMS,IRUMF),J=ICTLS,ICTLF)
      REWIND 1
      DO 12 I=1, NORDER
      IK=NURDER+1-I
   12 FURCE(IK) = EPS(IK)
      DU 200 J=1,45
C 200 WRITE(6,300)(DB(I,J),I=1,45)
C 300 FURMAT(5x,10012.4)
      IVET=1
      ISBLK#NHC+NRIFC
      ICOL=18BLK+NURM
      IROW=ISBLK+IREM1
      NEXCOL=ISBLK+NEX
      CALL SWAPS(DB, NORUER, ICOL, IRUM)
      SWAPSFORCE (IROW)
      FORCE (IRDW) = FORCE (NORDER)
      FORCE (NURDER) = SWAP
      N#NORDER-1
      CALL ERRSET(208,500)
      CALL DCMAT(DB, N, FURCE)
      CALL ERRSET(208,10)
      WRITE(6,102)DTPHAS,DTLG10,DPIVOT
  102 FURMAT(//2x, 'DTPHAS = ', 2040.16, /2x, 'DTLG10 = ',
     1D40,16,/2x,'DPIVOT # ',2D40,16)
      IFACODTLG10/FAC
      DFAC=IFAC+FAC
      DTLG10=DTLG10-DFAC
      DTPHAS=DTPHAS+DCMPLX(10.D0++DTLG10,0.D0)
      DETSV=DTPHAS*DPIVUT
      SUM#ZERO
```

```
DU 2 1=1.N
  IF(I.EQ.NEXCOL) GU TO 2
  SUM=SUM+DB(NORDER, I) +FORCE(I)
2 CONTINUE
  SUMEFORCE(NURDER)=SUM
  IF (CDARS (DB (NORDER, NEXCUL)) . NE. 0. DO) GU TO 5
  WHITE (6,6) NURDER, NEXCOL
               DB(',15,' ,',15,')
                                         IS ZERO')
6 FURMAT(10
  STUP
5 CONTINUE
  SUM#SUM/DH(NORDER, NEXCOL)
  FORCE (NEXCOL) = (SUM+FORCE (NEXCUL))/TWO
  FURGE (NORDER) #FORCE (ICOL)
  FURCE(ICOL)=ZERO
  DU & I=1, NORDER
3 EPS(I)=FORCE(I)
  RETURN
  END
```

SUBROUTINE SWAPS(DB, NORDER, ICUL, IROW)
COMPLEX+16 DB(63,63), SWAP
DO 1 I=1, NORDER
SWAP=DB(I, ICOL)
DH(I, ICOL)=DB(I, NORDER)
1 DH(I, NORDER)=SWAP
DO 2 I=1, NORDER
SWAP=DH(IROW, I)
DB(IROW, I)=DB(NORDER, I)
2 DB(NORDER, I)=SWAP
RETURN
END

```
SURROUTINE DCMAT(A,N,Y)
      REAL +8 ADET, AMAG, USIGN
      COMPLEX*16 A, Y, DDET, DPIVOT, TK, X
      COMPLEX+16 DAIJ, AMX, DONE, DYI, TEMP, DAKJ, DYK, DAKK, DAIK
     1, LINE, DPHAS
      DIMENSION ICHG(63), A(63,63), Y(63), X(63)
      COMMON /COETRM/ DPIVOT, DPHAS, ADET, IDET
      NUIME63
      ADET=0.DO
      DSIGN#1.DO
      DPHASEDCMPLX(1.000,0.00)
      NP1=N
      IF(IDET.EG.O) GO TO 650
      NP1=N+1
      DO 651 I=1,NP1
 651 X(I) = A(NP1, I)
 650 CUNTINUL
      DU 118 K=1.N
      AMX # A(K,K)
      IMXEK
      DU 100 I=K,N
      IF (CDAHS (A(I,K)) .LE. CDABS (AMX)) GO TO 100
      AMX = A(I,K)
      IMX=I
  100 CONTINUE
  102 IF (IMX.EQ.K) GO TO 106
      DU 104 J=1,NP1
      TEMPEA(K,J)
      A(K,J)=A(IMX,J)
  104 A(IMX,J) TEMP
      ICHG(K)=IMX
      TEMPAY(K)
      Y(K) = Y(IMX)
      Y(IMX)= TEMP
      DPHASE-DPHAS
      GO TO 108
  106 ICHG(K)=K
  108 CONTINUE
      DAKKHA(K,K)
  901 FURMAT(1x, 15, 2040, 16/)
      WRITE(6,1000) DAKK
C1000 FURMAT(5x, 'DAKK', 5x, 2020.10)
      AMAGECDABS(DAKK)
      IF (AMAG. NE. 0. DO) GO TO 6
      WRITE(6,7)
                   MATRIX IN DCMAT IS SINGULAR!)
    7 FURMAT(10
      STOP
    6 CONTINUE
      ADET=ADET+DLOG10(AMAG)
      DPHASEDPHAS*DAKK/AMAG
```

```
DUNE DCMPLX(1.DO, 0.DO)
      DAKKEDUNE/DAKK
      DU 110 J=1,NP1
  110 A(K,J) MA(K,J) DAKK
      A(K,K) BDAKK
      IF(IDET.EQ.0) GO TO 652
      TK=X(K)
      DU 653 J=K, NP1
  653 \times (J) = \times (J) = TK + A(K,J)
  652 CUNTINUE
      DYKEY(K)
      Y(K)=DYK+DAKK
      DO 114 I=1,N
      IF (I.EQ.K) GO TO 114
      DAIKEA(I,K)
      CALL ROWSUM(NP1, NDIM, A(I, 1), A(K, 1), DAIK)
      DO 112 J=1,NP1
C 112 A(I,J)=A(I,J)=DAIK+A(K,J)
      A(I,K)=DAIK
      DYI=Y(I)
      DYK#Y(K)
      A(I)=DAI=DVIK*DAK
  114 CONTINUE
      DO 116 I=1,N
  116 A(I,K)==A(I,K)+DAKK
      A(K,K)=DAKK
  118 CONTINUE
      DU 122 K=1,N
      LEN+1-K
      KI=ICHG(L)
      IF (L.EQ.KI) GU TU 122
      DU 120 I=1.N
      TEMP = A(I,L)
      A(I,L) = A(I,KI)
  120 A(I,KI) # TEMP
  122 CONTINUE
       IF (IDET.NE.O) DPIVOTEX(NP1)
  124 RETURN
      END
```

```
COMPLEX FUNCTION EXPON(L, MS)
C CREATE EXP(I+L+PHIM)
      DIMENSIUN CS(4,6), SN(4,6)
      COMMUN/RNAM/CS, SN
      IL=IABS(L)
      IF(L) 16,15,17
   15 EXPUNECHPLX(1.,0.)
      GO TO 18
   16 AECS(MS, IL)
      BESN(MS, IL)
      EXPUNECMPLX(A,=6)
      GO TO 18
   17 A=CS(MS,L)
      BESN(MS,L)
      EXPUNSCMPLX(A,B)
   18 CUNTINUE
      RETURN
      END
```

```
SUBRUUTINE SWA(I.J)
    INTEGER P.Q.OS
    COMPLEX EXPON
    CUMPLEX+16 CMS,CM1,CS1,CS2
    CUMPLEX#16 TKN(441)
    CUMPLEX#16 ZLN
    CUMPLEX+16 XNLG
    COMPLEX#16 YKM(3,4)
    CUMMON/SPAR/AKCI(6),TAU(6),SMLA(6),DMS(6),AK(4),AC(4),BJ(4),
   1CAPK, CAPC
    COMMON/INTER/NSY, NBSEC, NFSEC, NB, NHP, MFLAP, MFEA, MCT,
   1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
   2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NURM,
   3IREM, NEX, NP5, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSH,
   4NFP1,MXSMI,MXT2P1,MXKQ,MXCPL,MXCSH,MXCPM,MXCPK,MXSMB,
   5NEBC, NESBC, MFASH, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
   6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
    CUMMON/NLEAD/MLEL, NLEL, MCTY
    COMMON/ROTF/OM1, OM2, OMT
    COMMON/FREF/CMS, CM1, CS1, CS2
    CUMMUN/SWASH/SWGJ, SWEI, SWM, SWR
    COMMUNITANI/TKN
    KSML=I=NFP1
    IF(I.NE.J) GO TO 30
    DU 17 L=1.MXT2P1
    LS=L-MAXN-1
    LL=(L=1) *NRIFC+L
 17 TKN(LL) = ZLN(LS, I)
    DO 20 MS=1.NB
    DU 20 La1, MXT2P1
    LS=L=MAXN=1
    CFDL=1.0+DMS(MS)+(1.+(LS+LS-1)/(1.+LS+LS+SWGJ/SWEI))/SWR
    LL=(L=1)*NRIFC+MXT2P1+(MS=1)*NRBD+NCOL8+NFUS
    IF (MFLEX.EQ. 0) GO TO 21
    IF (MCUN.EQ.O) GO TO 20
    LL=LL+3
    IF(MCTY.GT.O) LL=LL+3
    TKN(LL) == EXPON(LS, MS) + CFDL
    GU TO 20
 21 LL=LL+MCT
    IF (MCT.EQ.0) GO TO 20
    CS1=CMS-CM1+KSML+DM1
    YKM(I,MS) #SMLA(MS) *(1+CS1 * TAU(MS))
    TKN(LL)=YKM(I,MS) *EXPON(LS,MS) *CFDL
20 CONTINUE
    GU TU 50
30 IMJ#I-J
    DO 18 La1, MXT2P1
    DO 18 GE1, MXT2P1
    IF(L.EQ.Q) GO TO 18
```

LMGEL-Q
IF(IMJ.NE.LMQ) GO TO 18
LS=L-MAXN-1
QS=Q-MAXN-1
LL=(L-1)\*NRIFC+Q
TKN(LL)\*XNLQ(I,LS,QS)
18 CUNTINUE
50 RETURN
END

```
SUBROUTINE SWB(I,J)
  INTEGER P.Q.QS
  REAL+8 CX(75)
  COMPLEX EXPON
  COMPLEX+16 ULN, 3(216)
  COMPLEX+16 TKN(441)
  COMPLEX#16 B(648), 8MLB(108), 8MLC(108), 8MLD(105)
  CUMPLEX+16 CTB(54), FAB(54), FLB(54)
  CDMPLEX+16 CT81(9), CT82(9), CT83(9), FA81(9), FA83(9), FL81(9), FL82(9)
  COMPLEX+16 SMLE(108),F88(54)
  CUMPLEX+16 8MLF(108), SMLG(108)
  CUMPLEX+16 F3B1(9),F8B2(9),F3B3(9),FAB4(9),FLB4(9),CTB4(9)
  CUMMON/BTS/B,SMLB,SMLC,SMLD,CTB,FAB,FLB,CTB1,CTB2,CTB3,FAB1,
 1FAB3,FLB1,FLB2,9MLE,FSB,FSB1,FSB2,FSB3,FAB4,FLB4,CTB4,SMLF,SMLG
  CUMMUN/SWASH/SWGJ, SWEI, SWM, SWR
  COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
 1 MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
 2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
 4NFP1, MX3MI, MXT2P1, MXKQ, MXCPL, MXC88, MXCPM, MXCPK, MX3M8,
 SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
 6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MUDE
  COMMUN/SPAR/AKCI(6), TAU(6), SMLA(6), DMS(6), AK(4), AC(4), BJ(4),
 1CAPK, CAPC
  CUMMON/CFLEX/CX
  CUMMUN/TKN1/TKN
  COMMUNINLEAD/MLEL, NLEL, MCTY
  CUMMUN/881/8
  NONU=1
  IMJ=I-J
  JMNC=(J-1)+12+NCOLS
  IF (MFLEX.EQ.O.AND.IMJ.NE.O) GU TO 23
  IF (MFLEX.EQ.O) GO TO 3
  IF (MCTY, EQ. 0) GO TO 3
  IF (IMJ.NE.O) GO TO 23
3 IF (IMJ.NE.O) NONDWO
  IF (NBP.EG.O) GO TU 13
  KSML#I=NFP1
  NPMK#=NPS=KSML
  DO 14 0=1, MXT2P1
  QS=Q=MAXN=1
  NMKUBNPMK-Q8
  IF (NMKQ, EQ. 0) GO TO 5
  RNMKQ#1.0*NMKQ
  RFABRNMKQ/NBP
  NFABNMKQ/NBP
  DIFERFA-1.0+NFA
  IF(DIF.GE.O.O) GO TO 2
  DIF =-DIF
2 IF(DIF.GT..05) GO TO 14
```

: 11

```
5 DFGR#1.0+DMS(1)+(1.+(G8+GS-1.)/(1.+G8+G5+SWGJ/8WEI))/SWR
    IF (MFLEX.EG. 0) GD TO 7
    IF (MCUN.EQ.O) GO TO 14
    IF(MCTY.GT.O) GO TO 6
    DO 8 IQ#1, NCOLS
   LL=NEIFC+NEISC+(IQ-1)+NRIFC+Q
   L=(J=1) +NCOLS+MXSMI+(I=1) +NCOLS+IQ
  A TKN(LL) == NBP+DFQR+FLB(L)
   LL=NEIFC+NEISC+NCULS+NRIFC+0
    TKN(LL)=+NBP+DFQR+CX(3)+NUND
    TKN(LL+NRIFC)=+NBP+DFGR+CX(6) *NUNO
    TKN(LL+NRIFC+2)==NBP+DFQR+CX(12)+NOND
    GU TO 14
  6 LLENEIFC+NEISC+NRIFC+NCULS+5+NRIFC+Q
    TKN(LL)==NBP+DFQR
    GO TO 14
  7 LL=NEIFC+NEISC+NRIFC+NCOLS+0
    IF (MCT.EQ.O) GO TO 14
    TKN(LL)==N8P*DFQR/SMLA(1)
14 CUNTINUE
    GO TO 23
 13 DU 21 MS=1,NB
    DU 21 PB1, MXT2P1
    USEP-MAXN-1
    DFGR=1.+DMS(MS)+(1+(QS+QS=1)/(1.+QS+QS+SWGJ/SWEI))/SWR
    IF (MFLEX.EQ.0) GO TO 22
    IF (MCON, EQ. 0) GO TO 21
    IF (MCTY.GT.O) GO TO 25
    DU 24 IGHI, NCOLS
    LLENEIFC+NEISC+(MS=1) +NEITC+(IG=1) +NRIFC+P
    L=(J=1) +NCOLS+MXSMI+(I=1) +NCOLS+IQ
 24 TKN(LL) == EXPON(-QS, MS) +DFQR+FLB(L)
    LL=NEIFC+NEISC+(MS=1) +NEITC+NCOLS+NRIFC+P
    TKN(LL) =+EXPON(=QS,MS)+DFQR+CX(3)+NONU
    LL=LL+NRIFC
    TKN(LL) =+EXPON(=QS,MS) +DFUR+CX(8) +NONO
    LL#LL+NRIFC
    TKN(LL) == EXPON(-QS, MS) + DFQR+CX(12) +NONO
    GU TU 21
 TKN(LL) == EXPON(=QS,MS) +UFQR
    GU TD 21
 22 LLENEIFC+NEISC+(MS=1) *NEITC+NRIFC*NCOLS+P
    IF (MCT.EQ.0) GO TO 21
    TKN(LL) ==EXPON(=QS,MS) *DFQR/SMLA(MS)
 21 CUNTINUE
 23 CONTINUE
    IF(MFUS,EU.O) GO TO 52
    JMI==IMJ
    DU 50 IPP=1, MXT2P1
```

LS=IPP=MAXN=1
IF(JMI.NE.LS) GO TO 50
DU 51 IGQ=1,NCOLS
LLP=JMNC+(IGQ=1)+12+1
LL=NEIFC+(IQQ=1)+NRIFC+IPP
51 TKN(LL)=ULN(LS,KSML)+S(LLP)
50 CUNTINUE
52 CUNTINUE
RETURN
END

```
COMPLEX FUNCTION ZLN+16(L3,I)
   REAL+8 C3.C4
   COMPLEX EXCHI
   CUMPLEX*16 CLNJ, C1, C2, C5, C6, C7, C8, C9, C10
   COMPLEX+16 CMS, CM1, C81, C82, VN, VN1, VN2
   CUMMUN/SWASH/SWGJ, SWEI, SWM, SWR
   COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
  1MFLEX,MCON,MAER,MFUS,NBC,NFLAP,NFEA,NCT,NCON,NFFB,
  2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM.
  3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
 4NFP1.MXSMI.MXT2P1.MXKQ.MXCPL.MXCBB.MXCPM.MXCPK.MXSMB.
  5NEBC.NESAC.MFASB.MXFAB.NPUS.NRBD.NRIFC.MXQ.NEIFC.
 SNEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
   CUMMON/SPAR/AKCI(6), TAU(6), SMLA(6), DMS(6), AK(4), AC(4), BJ(4),
  1CAPK, CAPC
   COMMON/NLEAD/MLEL, NLEL, MCTY
   CUMMUN/FREF/CMS, CM1, CS1, CS2
   COMMON/ROTF/OM1,OM2,OHT
   COMMON/SPAR1/AKT(4), ACT(4), AKP(4), ACP(4)
   RESWA
   KSML = I = NFP1
   CS1=CMS=CM1+KSML+UM1
   C32=C31 *C31
   C1=SWM+(C32-DMT+L3+CM1+C31-L3+L3+DM2)
   C2=DCMPLX(0,D0,0,D0)
   C9=UCMPLX(0,D0,0,D0)
   CFL=1.+(LS+L8-1)/(1+LS+LS+S+GJ/SHEI)
   CFLR=CFL/SWR
   DO 10 JJ=1.NE8
   CLNJ#AK(JJ)+C81+AC(JJ)=CM1+L8+DM1+AC(JJ)
   C2=C2+CLNJ
10 C9=C9+CLNJ+(1-BJ(JJ)+CFLR)
   C10=C2
   C38C3
   IF(MSC.EQ.O) GO TU 11
   C2=C10
   C5#CAPK+CAPC*(C81=CM1*L8*OM1)
   C6=DCMPLX(0.D0,0.D0)
   C7=DCMPLX(0.D0,0.D0)
   DO & JJ=1.NES
   CB#AK(JJ)+CB1+ AC(JJ)-CM1+L8+UM1+AC(JJ)
   C6=C6+C8+EXCHI(L8,0,JJ)+(1.-BJ(JJ)+CFLR)
 a C7=C7+C8*EXCHI(0,L8,JJ)*(1=BJ(JJ)*CFLR)
   C2=C9=C7*C6/(C5+C2)
11 IF(MAXN_EQ.1) GU TO 12
   KX=1-L8+L8
   C3#2.D0+3.141592654*L3*L3*KX*KX
   C4=R+R+R+(1./SWGJ+L8+L8/SWEI)
   C3=C3/C4
   ZLN=C1+C2+DCMPLX(C3,0.D0)
```

```
GO TO 13

12 ZLN=C1+C2

13 CUNTINUE

VN=DCMPLX(0.D0,0.D0)

VN1=DCMPLX(0.D0,0.D0)

VN2=DCMPLX(0.D0,0.D0)

DO 5 JJ=1,NES

VN=VN+AKT(JJ)+(CS1=CM1*LS*OM1)*ACT(JJ)

VN1=VN1+(AK(JJ)+(CS1=CM1*LS*OM1)*AC(JJ))*BJ(JJ)*(R=BJ(JJ)*CFL)

5 VN2=VN2+AKP(JJ)+(CS1=CM1*LS*OM1)*ACP(JJ)

ZLN=ZLN+(LS*LS*VN=VN1*CFL+CFL*CFL*VN2)/(R*R)

RETURN
END
```

```
COMPLEX FUNCTION XNLQ+16(I,L3,Q3)
   INTEGER QS
  COMPLEX EXCHI
  CUMPLEX*16 CS1,CS2,CM1,CMS,XN,XN1,XN2,XN3
  COMPLEXA16 C5, WN, WN1, WN2
  COMMON/SWASH/SWGJ, SWEI, SWM, SWR
  COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, HCT,
 1 MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
 2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 31REM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NC8B,
 ANELI, MXSHI, MXT2P1, MXKQ, MXCPL, MXCSB, MXCPM, MXCPK, MXSMB,
 5NEHC,NESHC,MFASH,MXFAB,NFUS,NRBD,NRIFC,MXQ,NEIFC,
 6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
  CUMMON/SPAR/AKCI(6), TAU(6), SMLA(6), DMS(6), AK(4), AC(4), BJ(4),
 1CAPK, CAPC
   CUMMUN/NLEAD/MLEL, NLEL, MCTY
  CUMMUN/FREF/CMS, CM1, CS1, CS2
   CUMMUN/RUTF/OH1, OM2, OMT
  CUMMUN/SPARI/AKT(4), ACT(4), AKP(4), ACP(4)
  KSML=I-NFP1
  CS1=CM8=CM1+K3ML+UM1
   IF(US.ER.LS) GO TO 15
   XNLG=DCMPLX(0.D0,0.D0)
   CFQ=1.+(Q3+Q3-1)/(1.+Q3+Q3+SWGJ/8WEI)
   CFL=1.+(LS*LS-1)/(1+LS*LS*SWGJ/SWEI)
   CFOR=CFG/SWR
   CFLK=CFL/SWR
   DO 10 JJ=1, NES
10 XNLU=XNLG+(AK(JJ)+(CS1-CM1+QS+OM1)+AC(JJ))+EXCHI(LS.QS.JJ)+
 1(1,-8J(JJ)*CFQR)
   IF (MSC.EQ.0) GO TO 16
   C5=CAPK+CAPC+(CS1=CM1+QS+UM1)
   XN1=DCMPLX(0.D0,0.D0)
   XN2=DCMPLx(0.00,0.00)
   XN3=DCMPLX(0.D0,0.D0)
   DO 12 JJ=1, NES
   XN=AK(JJ)+(CS1-CM1+QS+OM1)+AC(JJ)
   XN1=XN1+XN
   XN2=XN2+XN+EXCHI(L8,0,JJ)+(1.=8J(JJ)+CFLR)
12 XN3=XN3+XN+EXCHI(0,08,JJ)+(1.=BJ(JJ)+CFQR)
   XNLU=XNLQ=XN3+XN2/(C5+XN1)
   GO TO 16
15 XNLUEDCMPLX(0.D0,0.D0)
16 CONTINUE
   RESHR
   WN =DCMPLX(0.D0,0.D0)
   WN1=DCMPLX(0.D0,0.D0)
   WN2=DCMPLX(0.D0,0.D0)
   DU 5 JJ=1.NES
   wnmwn+(akt(JJ)+(cS1-cm1+QS+UM1)+ACT(JJ))+EXCHI(LS,QS,JJ)
```

```
WN1EWN1+(AK(JJ)+(C81-CM1+Q8+OM1)+AC(JJ))+BJ(JJ)+(R-BJ(JJ)+CFQ)+
1 EXCHI(L9,Q9,JJ)
5 WN2EWNZ+(AKP(JJ)+(C81-CM1+Q8+UM1)+ACP(JJ))+EXCHI(L8,Q8,JJ)
XNLQEXNLQ+(Q8+L8+WN-WN1+CFL+CFQ+CFL+WN2)/(R+R)
RETURN
END
```

```
COMPLEX FUNCTION ULN#16(LS.KSML)
  CUMPLEX*16 UN, UNN, UNC, CS1, C92, CMS, CM1
  COMPLEX EXCHI
  CUMMUN/SPAR/AKCI(6), TAU(6), SMLA(6), DMS(6), AK(4), AC(4), BJ(4),
 1CAPK, CAPC
  COMMON/ROTE/OM1, OM2, OM1
  CUMMUN/FREF/CMS, CM1, CS1, CS2
  CUMMON/SWASH/SWGJ, SWEI, SWM, SWR
  COMMON/INTER/NSY, NRSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
 1MFLEX, MCIIN, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
 2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
 3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSA,
 UNFP1, HXSH; , MXT2P1, MXKQ, MXCPL, MXCSB, MXCPH, MXCPK, MXSMA,
 SNEBC, NESHC, MFASH, MXFAB, NFUS, NRBU, NRIFC, MXQ, NEIFC,
 6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MUDE
  CUMMUN/NLEAD/HLEL, NLEL, MCTY
  UN =DCMPLx(0.D0,0.D0)
  UNN=DCMPL x (0.D0,0.D0)
  CFL=1.+(LS+LS=1)/(1+LS+LS+S+GJ/SHET)
  CFLH=CFL/SWR
  CS1=CMS=CM1+KSML+UM1
  DU 5 JJ=1, NES
  UNEUN+(AK(JJ)+(CS1-CM1*LS+OM1)+AC(JJ))+EXCHI(0,LS,JJ)+
 1(1.-BJ(JJ)*CFLR)
5 UNN=UNN+(AK(JJ)+(CS1-CM1+LS+(M1)+AC(JJ))
  IF (MSC, EQ, O) GO TU 6
  UNC#CAPK+(CS1=CM1+LS+OM1)+CAPC
  OF MENN+ANC\(AMC+HNN)
6 IF (MSC.EQ.O) ULNEUN
  RETURN
  END
```

```
COMPLEX FUNCTION EXCHI (L,0,J)
   INTEGER Q
   CUMMUN/RNAM1/CSA(4,24),8NA(4,24)
  LG=L-G
   ILQ=IA8S(LQ)
   IF(LU)16,15,17
15 EXCHI=CMPLX(1.0,0.0)
   GO TU 18
16 A=CSA(J,ILQ)
   BESNA(J, ILQ)
   EXCHI=CMPLX(A,-B)
   GO TO 18
17 A=CSA(J,ILQ)
   B=SNA(J, ILQ)
   EXCHI=CMPLX(A,B)
18 CONTINUE
   RETURN
   END
```

```
SUBROUTINE ZTEGI(1,J)
     INTEGER P.Q
     COMPLEX EXPON, EXPMI, EXPPI
     COMPLEX#16 CM1
     COMPLEX#16 B(648), SMLB(108), SMLC(108), SMLD(108)
     CUMPLEX+16 CTB(54), FAB(54), FLB(54)
     COMPLEX+16 CTB1(9),CTB2(9),CTB3(9),FAB1(9),FAB3(9),FLB1(9),FLB2(9)
     COMPLEX#16 SMLE(108),F88(54)
     COMPLEX+16 SMLF(108), SMLG(108)
     COMPLEX#16 FSB1(9),FSB2(9),FSB3(9),FAB4(9),FLB4(9),CTB4(9)
     COMPLEX+16 TKN(441)
     CUMMON/BTS/B, SMLB, SMLC, SMLD, CTB, FAB, FLB, CTB1, CTB2, CTB3, FAB1, FAB3.
    1FLB1,FLB2,SMLE,F8B,F8B1,F8B2,F8B3,FAB4,FLB4,CTB4,SMLF,SMLG
    CUMMON/TKN1/TKN
     COMMON/INTER/NSY, NBSEC, NFSEC, NB, NBP, MFLAP, MFEA, MCT,
    1MFLEX, MCON, MAER, MFUS, NBC, NFLAP, NFEA, NCT, NCON, NFFB,
    2NAS, NHC, NVI, NSP, MAXN, NES, MSC, NEGN, IPCT, NIT, MER, NORM,
    3IREM, NEX, NPS, NSCH, IG, IF, NPRL, NPRS, NPD, NSK, NCOLS, NCSB,
    4NFP1, MX8M1, MXT2P1, MXKQ, MXCPL, MXC8B, MXCPM, MXCPK, MX8MB.
    SNEBC, NESBC, MFASB, MXFAB, NFUS, NRBD, NRIFC, MXQ, NEIFC,
    6NEISC, NEITC, MXTKN, NFF, MINPN, MAXPN, IBF, MODE
     CUMMUN/NLEAD/MLEL, NLEL, MCTY
     CM1= DCMPLX(0,D0,1.D0)
     NMK= J-I
     KB= NEIFC+NEISC+MXT2P1+NFUS
     KBB= KB+NCOLS+NRIFC
     NMKP1=NMK+1
     NMKM1=NMK-1
     NPK==NP3=I+NFP1
     NBM1=(NB=1)+NRBD
     LSMA=(J=1)+NESBC+(I=1)+MXCSB
     LLAR=(J-1)+NEBC+(I-1)+MXCPM
     IF(MFLEX.EQ.0) GO TO 10
     WRITE(6,900)
     FORMAT(/, 9x, 'GIMBALLED OR TEETERING ROTOR, MFLEX MUST EQUAL ZERO')
900
     GU TO 90
  10 IF(NBC,EQ.2)GD TO 13
     IF (NBP.EQ. 0) GU TO 11
     IF(NBP.LE.2)GO TO 12
     GO TO 16
  11 IF(NB.GT.2)GO TO 16
  12 WRITE(6,901)
 901 FORMAT(/,9X, 'GIMBALLED ROTOR MUST HAVE MORE THAN THO BLADES')
     GD TD 90
  13 IF(NBP.EQ.O)GO TO 14
     IF (NBP.NE. 2) GO TO 15
     GO TO 16
  14 IF(NB,EQ.2)GO TO 16
  15 WRITE (6, 902)
 902 FORMAT(/, 9X, 'TEETERING ROTOR MUST HAVE THO BLADES')
```

```
60 TU 90
16 NE=2
   NA=1
   IF (NHC.EQ.1)GO TO 17
   NE = 1
   NAEU
17 N1==1
   NSEP
   DU 22 NN=1.NE
   IF (NN.FR.11GD TO 18
   N1=1
   NS=5
18 DO 19 0=1,NCOLS
   L3=LLAR+(Q=1)+12+3
   L10=L3+7
   KK#KB+(G=1)+NRIFC+N2
19 TKN(KK) #NA+B(L3)+N1+CM1+B(L10)
   L3=LSMA+3
   L10=L3+7
   KK#KBB+N2
   IF (MCT.ER.O)GO TO 20
   TKN(KK)==NA+SHLH(L3)=N1+CM1+SMLH(L10)
   KKEKK+NRIFC
20 IF (MFEA.EQ.O)GD TU 21
   TKN(KK) ==NA+SMLC(L3)=N1+CM1+SMLC(L10)
   KK=KK+NRIFC
21 IF(MFLAP, EQ. 0) GO TU 23
   TKN(KK)==NA+SMLD(L3)=N1+CM1+8MLD(L10)
   KKEKK+NRIFC
23 IF (MLEL, ER. 0) GO TO 22
   TKN(KK) ==NA+SMLE(L3)=N1+CM1+SMLE(L10)
22 CONTINUE
   IF (NBP.NE. 0) GO TO 40
   IF (NHC.EQ.2)G() TO 28
   DU 24 G=1, NRBD
   KT=KH+(U=1)*NRIFC+2
   KKSKT+4
   KSEKT+NBM1
   K6=KK+N8M1
   TKN(K2)==TKN(KT)
24 TKN(K6)=-TKN(KK)
   DU 25 M8=2,NB
   EXPMIMEXPON(NMKMI, MS)
   EXPPI=EXPON(NMKP1,MS)
   MSHIFT=(MS-1)+NEITC+(MS-2)+NRBD
   DD 25 Q=1,NRBD
   KT=KB+(Q=1)+NRIFC+2
   KKEKT+4
   K2=KT+M8HIFT
   K6=KK+MSHIFT
```

```
K22=K2+NRBD
   K66=K6+NRHD
   TKN(K2)==TKN(KT)+EXPP1
   TKN(K6) ==TKN(KK) +EXPM1
   TKN(K22) = TKN(K2)
25 TKN(K66) == TKN(K6)
   GU TO 100
28 DU 30 9=1, NCULS
   L11=LLAR+(0-1)+12+11
   KK=KB+(0-1) +NRIFC+NRAD+6
30 TKN(KK)=8(L11)
   L11=LSMA+11
   KK=KBB+NRBD+6
   IF (MCT.EU.O)GD TD 31
   TKN(KK)=-SMLB(L11)
   KKEKK+NRIFC
31 IF (MFEA, EQ. 0) GO TO 32
   TKN(KK)==SMLC(L11)
   KK=KK+NRIFC
32 IF (MFLAP.EG.O) GO TO 34
   TKN(KK)==SMLD(L11)
   KK=KK+NRIFC
34 IF (MLEL_EQ.0) GU TO 33
   TKN(KK)=-SMLE(L11)
33 EXPMIMEXPON(NMKM1,2)
   00 35 G=1.NRBD
   KT=KB+(Q=1)+NRIFC+6
   KK#KT+NEITC
35 TKN(KK) ==TKN(KT) +EXPM1
   DO 38 GE1, NRBD
   KT=KB+(Q=1)+NRIFC+NRRD+6
   KKEKT+NEITC
38 TKN(KK) #TKN(KT) #EXPM1
   GO TO 100
40 N1==1
   N2=P
   DO 50 NN=1,NE
   IF (NN.EQ. 1)GO TO 42
   N1=1
   N2=2
42 NPMKENPK+N1
   INMK=IABS(NPMK)
   RINMK#1.0+INMK
   RF A=RINMK/NBP
   NF ABINMK / NBP
   DIFEABS(RFA-1.0+NFA)
   IF (UIF.GT. (.05)) GU TO 50
   DU 44 GE1, NCULS
   L4=LLAR+(Q-1)+12+4
   KK=KB+(U=1)+NRIFC+N2
```

```
L11=L4+7
 44 TKN(KK) =NA+B(L4)+N1+CM1+B(L11)
    L4=LSMA+4
    KK#KBB+N2
    L11=L4+7
    IF (MCT.EQ. 0) GU TU 45
    TKN(KK)==NA+SMLH(L4)=N1+CM1+SMLH(L11)
    KKEKK+NRIFC
 45 IF(MFEA.EQ.O)GO TU 46
    TKN(KK) ==NA+SMLC(L4) =N1+CM1+SMLC(L11)
    KKEKK+NRIFC
 46 IF (MFLAP.EQ.O) GO TO 47
    TKN(KK)==NA+SMLD(L4)=N1+CM1+SMLD(L11)
    KK=KK+NRIFC
 47 IF (MLEL, EQ. 0) GO TO 50
    TKN(KK) == NA+SMLE(L4) =N1+CM1+8MLE(L11)
 50 CUNTINUE
    GO TO 100
 90 STOP
100 RETURN
    END
```

```
SUBRUUTINE POLAR
  CUMPLEX GXJ, GYJ, GZJ, GTX, GTY, DTZ
  COMMUNICATEM/OXJ. GYJ. GZJ
  DTX=GXJ+CMPLX(0.0,-1.0)
  DTY=0YJ*CMPLX(0.0,-1.0)
  DTZ=02J+CMPLX(0.0,-1.0)
  CXN=HXU
  DYREGYJ
  DZREGZJ
  DXI=DTX
  DYIEDTY
  DZI=DTZ
  IF (DXR.NE.O.O) GO TO 2
  IF(DXI.NE.O.O) GO TO 2
  DXA=0.0
  GU 10 3
2 DXAMATAN2(DXI,DXR)
3 IF(DYR.NE.O.O) GO TO 4
  IF(UYI,NE.O.O) GO TU 4
  DYABO. 0
  GU TO 5
4 DYAMATANZ(DYI, DYR)
5 IF (DZH.NE.O.O) GO TO 6
  IF(UZI.NE.O.O) GO TU 6
  DZA=0.0
  GU TU 7
6 DZABATANZ(DZI,DZR)
7 CONTINUE
  DXR=SGRT(DXR+DXR+DXI+DXI)
  DYR=SGRT(DYR+DYR+DYI+DYI)
  DZR=SURT(DZR+DZR+DZI+DZI)
  GXJ=CMPLX(DXR,DXA)
  QYJ=CMPLX(DYR,DYA)
  GZJ=CMPLX(DZR,DZA)
  RETURN
  END
```

\*FORTRAN CALLABLE COMPLEX FUNCTION TO ORTAIN DOT PRODUCTS.
\*ARGUMENT LIST IS (N,A,B), WHERE N IS THE DIMENSION OF THE VECTORS
\*A AND B. A IS PRESUMED SPARSE FOR MAXIMUM PROGRAM SPEED.
\*INTERMEDIATE RESULTS ARE CARRIED IN DOUBLE PRECISION AND THE
\*FUNCTION MAY BE DECLARED DOUBLE PRECISION COMPLEX, IF DESIRED.

```
SPACE 2
#INCR
          FQU
                 0
#COMPR
          EQU
                 1
#INDEX
          EOU
                 2
#N
          EQU
                 2
#A
          EQU
                 3
#B
          EQU
                 4
#MAXR
          FOU
          SPACE
#REAL
          EQU
                 0
                 2
#IMAG
          FOU
#ZERO
          EQU
                 4
#TEMP
          EQU
                 6
          SPACE 2
          DSECT
ARFAL
          DS
                 n
AIMAG
          DS
                 D
          DSECT
BREAL
          DS
                 n
BIMAG
          DS
                 D
          EJECT
CDOT
          CSECT
          SAVE
                 (2, #MAXR),,*
          USING COOT.15
          LM
                 #N, #B, 0(1)
          USING A.#A
          USING B.#B
                 #COMPR,0(#N)
          BCTR
                 #COMPR.O
          SLA
                 #COMPR.4
          LA
                 #INCR,16
          SR
                 #INDEX.#INDEX
          SDR
                 #REAL, #REAL
          SDR
                 #IMAG, #IMAG
          SDR
                 #ZERO.#ZERO
          SPACE 2
LOOP
          CD
                 #ZERO, A(#INDEX)
          BNE
                 CONTINUE
                 #INDEX, #INCR, LOUP
          BXLE
          RETURN (2, #MAXR)
EXIT
          SPACE
CONTINUE LD
                 #TEMP, AREAL (#INDEX)
                 #TEMP . BREAL ( #INDEX )
          MD
          ADR
                 #REAL, #TEMP
```

```
#TEMP, AIMAG(#INDEX)
         f D
                #TEMP, BIMAG(#INDEX)
         MD
          SDR
                #RFAL, #TFMP
                #TEMP, AREAL (#INDEX)
         1.0
         MD
                #TEMP.BIMAG(#INDEX)
          ADR
                #IMAG. #TEMP
         LD.
                *TEMP. ATMAG( #INDEX)
         MD
                #TEMP, BREAL (#INDEX)
          ADR
                #IMAG, #TEMP
         RXLF
                #INDEX, #INCR, LOOP
                FXIT
         SPACE 2
         LTORG
         END (Start of RCDOT)
*FORTRAN CALLARLE COMPLEX FUNCTION TO ORTAIN DOT PRODUCTS.
*ARGUMENT LIST IS (N.A.B), WHERE N IS THE DIMENSION OF THE VECTORS
*A AND B. A IS PRESUMED SPARSE FOR MAXIMUM PROGRAM SPEED.
*A IS A REAL VECTOR, WHILE B IS COMPLEX.
*INTERMEDIATE RESULTS ARE CARRIED IN DOUBLE PRECISION AND THE
*FUNCTION MAY BE DECLARED DOUBLE PRECISION COMPLEX, IF DESIRED.
         SPACE 2
#INCP
         EQU
                0
#C CMPR
         EQU
                1
#INDEXA
         EQU
#INDEXB
         FQU
                3
#N
         EQU
# 1
         FQU
                4
#B
         EQU
#MAXR
         EQU
                5
         SPACE
#REAL
         EQU
                0
#IMAG
         EQU
                2
#ZERO
         FQU
                4
#TEMP
         EQU
         SPACE 2
         DSECT
A
         DSFCT
BREAL
                D
         DS
RIMAG
         DS
                D
         EJECT
RCDOT
         CSECT
               (2.#MAXR)..*
         SAVE
         USING RCDOT, 15
                #N. #B. 0(1)
         USING A. #A
         USING B. #B
                #COMPR.O(#N)
         BCTR
               #COMPR.O
         SLA
               #COMPR.3
```

```
#INCR.8
         LA
          SP
                #INCEXA, #INDEXA
          SOP
                #RFAL, #RFAL
          SOR
                #IMAG. # IMAG
          SOR
                #7FRO.#ZERO
          SPACE 2
                #ZERO.A(#INDEXA)
LUGP
         CD
          BNF
                CONTINUE
          BYLE #INDEXA, #INCR, LCOP
          PETURN (2. #MAXR)
FXIT
          SPACE
                #INDEXP.O(#INDEXA, #INDEXA)
CONTINUE LA
         Lŋ
                #TEMP, A(#INDEXA)
                #TEMP.BREAL (#INDEXR)
         MD
          ADR
                #RFAL, #TEMP
         LD
                #TEMP.A(#INDEXA)
         MD
                #TEMP.BIMAG(#INDEXP)
         ADR
                #[MAG. #TEMP
          BXLE #INDEXA. #INCP. LODP
                FXIT
         SPACE 2
         LTORG
                       ___ (Start of ROWSUM)
         END __
*FORTRAN CALLABLE SUBROUTINE TO PERFORM MATRIX ROW OPERATIONS.
*ARGUMENT LIST IS (N.NOIM.A.B.X).
*THE ROW OPERATION A=A-X*R [S PERFORMED, WHERE A, B, AND X ARE
*DOUBLE PRECISION COMPLEX.
*NDIM IS THE COLUMN DIMENSION OF THE MATRICES. AND N IS THE NUMBER OF
*FLEMENTS TO BE OPERATED ON IN THE ROWS. THE INDEXING SCHEME IS
*THEREFORE 4(1)=4(1)-X*8(1), [=1,1+(N-1)*NDIM, NDIM
         SPACE 2
         FOU
#INCR
                0
#COMPR
         FQU
                1
                2
#INDEX
         EQU
         FOU
                1
#N
MICH
         EQU
                2
# 4
         EQU
                3
#8
         FQU
#X
         EQU
#MAXR
         FOU
         SPACE
#A TEMP
         EQU
                0
#RTFMP
         EOU
                2
#XRF4L
         EQU
#XIMAG
         EQU
         SPACE 2
         DSECT
AREAL
         ns
                D
AIMAG
         DS
                D
```

```
DSECT
BEFAL
          ns
                D
RIMAG
          rs
          FJECT
ROWSUM
          CSECT
          USING ROWSUM.15
                (14, #YAXR), *
          SAVE
          1. 14
                4N, 4X, 0(1)
          USING A. #A
          USING B. #R
                #NDIM,O(#NDIM)
          SLA
                UNDIM,4
                #COMPR.O(#N)
          BOTR
                #COMPR.O
                #COMPR-1, #NOIM
          MR
          LR
                #INCR.#NDIM
          SR
                #INDEX, #INDEX
          10
                #XRFAL, O( 4X)
          LD
                HYIMAG, R(HX)
          SPACE 2
          Ln
LOOP
                #ATEMP.BIMAG(#INDEX)
          MOR
                #ATEMP, #XIMAG
                #ATEMP, AREAL (#INDEX)
          40
          LD
                #RTEMP, RREAL (#[NDFY)
          MOR
                #STEMP, #XPFAL
          SOR
                #ATEMP. #BTEMP
          STD
                #ATEMP, AREAL (#INDEX)
         Ln
                #ATEMP, ATMAG (#INDEX)
         LD
                #BTEMP, BREAL (#INDEX)
          MOR
                #BTEMP, #XIMAG
          SDR
                #ATEMP. #BTEMP
                #BTEMP, RIMAG(#INDEX)
         LD
          MDR
                #BTEMP, #XRFAL
          SDR
                #ATEMP, #BTEMP
          STD
                #ATEMP, AIMAG (#INDFX)
         BXLF
                #INDEX. #INCR. LOOP
          SPACE
          RETURN (2, #MAXR),T
         LTORG
         FND
                                   (Start of Overlay Structure)
 OVERLAY ALPHA
 INSERT ART
 INSERT ARR
 INSERT COEFFS
 INSERT BTS
 INSERT SSI
 INSERT TKN1
OVERLAY BETA
 INSERT BAERO
 INSERT FAERO
```

INSERT ACRO INCERT ACOFFE INSERT SETUP INSERT SECPAR INSEPT IDADIN U IFAT TABLU CVERTAY BETA INSERT ELAST INSERT RIGID INSERT STIFF INSEPT BEND INSFOT MLPC2 INSEPT MLCC? INSEPT COOT INSERT ROOM OVERLAY GAMMA INSERT BARRAY INSERT RMASS INSERT BLARD OVERLAY GAMMA INSFRT SARPAY INSERT EMASS INSFOT FUARO OVERLAY PETA INSERT EPSOLN INSERT SURMA INSERT SURME INSERT CURME INSERT SUBMG INSERT TIEGT INSERT EXPON INSERT THMS INSERT SWA INSERT SWB INSEPT 71N INSERT XNLO INSEPT ULN INSEPT FXCHI CVERLAY ALPHA INSFOT SOLVE INSERT DOMAT INSTRT SWAPS INSERT ROWSHM INSERT FERSET FNTPY MAIN



## REFERENCES

- Sutton, Lawrence R. and Gangwani, Santu T., THE DEVELOPMENT AND APPLICATION OF AN ANALYSIS FOR THE DETERMINATION OF COUPLED TAIL ROTOR/HELICOPTER AIR RESONANCE BEHAVIOR, USAAMRDL-TR-75-35, Eustis Directorate, US Army Air Mobility Research and Development Laboratory, Fort Eustis, Virginia, August, 1975, AD A014989.
- Sutton, Lawrence R. and White, Richard P. Jr., THE DEVELOPMENT AND APPLICATION OF AN ANALYSIS FOR THE STABILITY BEHAVIOR OF BEARINGLESS MAIN ROTOR SYSTEMS, Letter Report SRL 14-77-3, RASA Division, Systems Research Laboratories, Inc., 1055 J. Clyde Morris Blvd., Newport News, Virginia.
- 3. Davis, John M., ROTORCRAFT FLIGHT SIMULATION WITH AEROELASTIC ROTOR AND IMPROVED AERODYNAMIC REPRESENTATION, Volume II User's Manual, Bell Helicopter Company; USAAMRDL-TR-74-10B, Eustis Directorate, US Army Air Mobility Research and Development Laboratory, Fort Eustis, Virginia, June 1974, AD 782756.