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EDITORIAL

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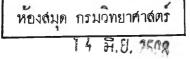
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Crystalline State of Cellulose in Fresh and Dried Mature Cotton Fiber from Unopened Bolls as Studied by X-Ray Diffraction*

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Synopsis

The crystal inity of cellulose in the undried cotton fiber, fresh from the unopened but mature boll, was studied by x-ray diffractometer methods and compared with the crystallinity cf portions of fibers from the same samples either dried directly or from which the water has been removed in various "indirect" ways calculated to better preserve the original structure including: (a) Solvent exchange, (b) freeze-drying, (c) drying above the critical temperature of liquids and (d) drying after the cellulose of the wet fiber has been crosslinked. The difference in crystallinity observed between directly and indirectly dried fibers indicates that a crystallization process must take place during the direct drying of the water-wet fiber. This crystallization process is promoted by the presence of water and inhibited or prevented when the fiber is dried indirectly. An increase of the degree of crystallinity due to wetting can be explained by assuming that the crystallization, which had been suppressed in the indirectly dried fiber takes place subsequently upon drying of the rewetted fiber. That the indirect methods preserve entirely or partially, such amorphous structure as is originally present is confirmed by the lower density and higher dyestuff accessibility of such fibers.

INTRODUCTION

The molecular structure—crystalline, paracrystalline, or amorphous in which cellulose occurs in cell walls is of importance for many problems. One of these is the molecular biology of cell elongation; another the explanation of the properties of fibers.

In connection with a theory of plastic surface growth of cell walls, Heyn,¹ in 1934 studied the walls of young elongating cells of *Avena* coleoptiles by x-ray diffraction, in order to obtain information about the organization of the cellulose molecules during the growth of the wall. From the undried fresh sample, a diffuse, halolike pattern characteristic of water was obtained. After drying, a diffraction pattern characteristic of cellulose was obtained. Although this finding raised the question whether or not cellulose is present only in an amorphous form in the fresh wall, no conclusion

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was drawn because it appeared possible that the cellulose diagram might be "masked" by the water halo or that the diffracted radiation from crystalline cellulose might be dissipated, (e.g., by multiple scattering by the water in the undried sample).

With regard to the properties of fibers it has been a question of long standing in what form cellulose occurs in undried cotton fiber, what happens during the drying of the fiber and how the circumstances of drying might affect the properties of the resulting product by altering the molecular aggregation. In connection with this problem Berkley and Kerr² investigated the structure of the undried, fresh cotton fiber with x-rays, using photographic methods. They obtained diagrams which gave no indication at all of the expected cellulose diagram but only two diffuse halos characteristic of water. Upon drying, the halos disappeared and at the same time the diagram of cellulose appeared just as in the 1934 case cited above. If, before drying, the cotton had been stretched (or excessively handled) in the wet state, a faint cellulose diagram appeared besides the halos. If a dried bundle of cotton was rewetted, the cellulose diagram remained present. From these experiments Berkley and Kerr concluded that in the undried cotton fiber of the ages studied cellulose occurs only in an amorphous structure. Their model of undried cotton fiber contains sets of long-chain cellulose molecules which upon drying bundle up at regular intervals into a permanent crystalline structure, leaving unordered material between the crystalline domains.

Preston³ has already pointed out that this interpretation of amorphous cellulose "cannot in the least be regarded as final," since the absence of an x-ray diagram does not necessarily imply the absence of crystalline regions (but only that these regions are small in size), and since the cellulose diagram of the fresh material may be "masked" by the water halos. It still remained to be explained then why in the rewetted fiber, the water halo does not mask the cellulose pattern.

Rånby and Katzmire,⁴ in a study of the cellulose during the development of the cotton fiber from the immature to the mature condition, using x-ray photographic methods, always found evidences of crystalline cellulose in the dried, mature cotton fiber, but could not be certain of its presence in the immature cotton fiber (20–25 days after flowering). They used fibers preserved in 50% alcohol which, after washing with distilled water, were dried in a vacuum over P_2O_5 or which were dried after solvent exchange from acetone to cyclohexane. They did not investigate never-dried material.

In small-angle x-ray studies of undried cotton fiber, Heyn^{5,6} found distinct evidence of the existence of regular discontinuities of a diameter of 50 A. which might correspond either to micelles of (fully crystalline) crystallites of cellulose or to intermicellar interstices of the same dimensions. (From x-ray data alone it is not possible to decide between these two possibilities, although the first appeared the simplest.) Both cases would be in disagreement with a continuous amorphous structure and rather suggest that some crystalline structure exists in undried cotton fiber. The question about the state in which cellulose occurs in elongating young cell walls and in undried secondary walls and what changes occur in crystallinity during drying thus remained undecided, although an amorphous structure in fresh walls and the occurrence of crystallization upon drying has been suggested by some of the studies made.

The present paper reports the results of x-ray diffractometer studies concerned with these problems. It was hoped that information might be obtained about the original undisturbed state of the molecules without interference by the presence of water on the existing cellulose diffraction pattern by using the following techniques. Fresh undried fibers, just removed from the unopened but relatively mature bolls, were air-dried normally and in special ways to preserve the original molecular organization as well as possible: Before drying, the water was replaced with nonpolar liquids or removed by freeze-drying or by drying the fiber after crosslinking the cellulose. In order to obtain information about the degree of dispersion, porosity, or collapse of the amorphous phase, measurements were also made of the density and accessibility of the fibers for dyestuffs. With these methods the effects of the condition of the amorphous phase of the various treatments could be followed to complement the x-ray data.

MATERIAL AND METHODS

After some initial experiments had been carried out with bolls grown by Mr. R. S. Orr of the Southern Regional Research Laboratory, cotton bolls, harvested just before opening, were received from the Agricultural Experiment Station at Mississippi State University.

The locks, collected from the fresh unopened bolls, were placed under water during the removal of the fiber from the seeds, or sampled in a moist chamber, to retain the normal moisture content. Care was taken not to exert the slightest tension on the fibers. A portion of the fibers from each boll was always dried directly in air to serve as a control.

Removal of Water

Liquid Exchange Method. In the liquid exchange the fibers were passed successively from the water-wet state of the boll through one of the following scries of liquids in each of which they remained for 2-12 hr.: (a) ethanol $\rightarrow 100\%$ ethanol \rightarrow ethyl ether; (b) Cellosolve (2-ethoxyethanol) \rightarrow ethyl ether; (c) 100% methanol \rightarrow benzene; (d) 75\% methanol $\rightarrow 100\%$ methanol $\rightarrow n$ -pentane; and (e) 100% methanol $\rightarrow n$ -pentane.

The *n*-pentane, ethanol, and methanol were carefully dried. It was assumed that in this way the last traces of water were removed from the fiber. From the last liquid of each series the fibers were dried in air at room temperature or in a vacuum desiccator at 60° C.

By replacing the reactive water by inert, especially nonpolar liquids and by removing these liquids, rather than water, from the fiber, it was expected that the molecular organization would remain better preserved. The best results were obtained with benzene and pentane. It is important that, according to nitrogen adsorption methods, these substances are known to preserve the largest internal surface of the fiber. They would, therefore, cause a smaller collapse of the molecular structure when used for drying than would polar liquids, such as water.

Liquids Above Critical Temperature. Another method followed was the one used by Kistler⁹ for the preparation of aerogels. The method consists in removing the final exchange liquid at a pressure greater than the critical vapor pressure and at a temperature above the critical temperature, so that the liquid is first transformed into a gas, and the liquid–gas interface is destroyed before the liquid is removed.

This precludes the action of a fluid-gas interface which, presumably, induces the collapse of the amorphous region during drying. *n*-Pentane, which has a critical temperature of 197°C. at a pressure of 33 atm., was used. It is interesting that after this high temperature treatment the cellulose was apparently undamaged. This can be understood because oxygen and water were absent. On the other hand, it has been shown^{10,11} that heat damage occurs between 260 and 300°C. and that the presence of oxygen and water greatly increases the effect.

Freeze-Drying. Freeze-drying has been found to be a useful method for retaining many fine structures of biological origin. The use of this technique to prepare amorphous sugars and other normally crystallizable substances is well known.^{12,13} The water-wet samples were placed in glass containers and were frozen in the wet state with standard equipment in a Dry Ice-acetone mixture at -70° C. or in liquid nitrogen; in the latter case *n*-pentane was used as an intermediary liquid to prevent formation of an insulating gas layer around the sample. After 24 hr. in a lyophilizer, the samples were dry.

Crosslinking

By crosslinking the cellulose in the undried fiber before removal of the water it was expected that the original state of the molecules would be reinforced and stabilized, and thus remain better preserved during the removal of the water.

The crosslinked material was prepared according to Goldthwait's procedure¹⁴ as modified by Reeves et al.,¹⁵ a solution of 19.5% or 9.5% hydrochloric acid and 7.4% formaldehyde in water was used. The undried fibers remained in this solution for 15–60 min., after which time they were washed and dried in air. Control experiments were also prepared with standard dry fiber.

Diffractometer Traces

The x-ray traces were obtained with a standard Norelco diffractometer with the use of nickel-filtered copper radiation and a pulse height analyzer for discrimination to provide a high degree of monochromatization. The incident x-ray radiation was carefully standardized by use of a brass standard. The same scaling multiplier and time factors (16-1-4) were used throughout this work. One unit of the graph is equivalent to 6 counts/sec.

The dry diffractometer specimens were prepared according to the method of Segal¹⁶ and of Nelson and Schultz.¹⁷ The fibers were first passed through a Wiley mill and pressed at 25,000 psi into flat platelets of 1×2 cm. with a dry weight of 100 mg. A few drops of a 1% solution of cellulose acetate in amyl acetate were added to the pellet for better coherence, after which it was pressed again to remove excess liquid. After drying, the pellet was pressed once more before being placed in the diffractometer. This method was found to give very reproducible results. Experiments with whole fibers mounted parallel in special holders gave comparable results, but at a lower intensity and with larger variation.

Density Measurements

The density measurements were carried out with a density gradient tube according to the technique of Orr¹⁸ with carbon tetrachloride and hexane as gradient liquids. The method was modified by deliberately omitting the boiling with xylene, intended to remove the trapped air. It was assumed that the bulk density so measured would be an indicator for differences in the degree of dispersion or contraction of the amorphous phase. Hermans and Weidinger¹⁹ similarly endeavored to calculate the proportion of crystalline and amorphous cellulose from density measurements. Whatever the correct explanation might be, the density measurements at least served as an indicator of changes in the noncrystalline portion of the fiber.

Differential Dye Test

This test was carried out according to the method of Goldthwait,^{20,21} as modified by Rebenfeld and Hong.²²

RESULTS

X-Ray Data

In all 160 x-ray diffractogram traces were prepared; only a few representative traces are presented in the figures.

Undried Fiber. Figure 1a is a trace of pure water in the sample holder. The maximum at $2\theta \ 21.3^{\circ}$ is from the covering polyethylene film. Figure 1b is a trace of a mature fiber recovered under water from a boll harvested before opening. Figure 1c is a trace of similar fiber collected from the boll in an atmosphere of 100% R. H., so as to maintain the same water content which existed in the living cell.

During the recording of the x-ray tracing, the original water content of these samples was maintained. The whole fibers were packed into a wet platelet of the standard size $(1 \times 2 \text{ cm.})$ in an aluminum sample holder, which, according to the method of Segal¹⁶ was subsequently closed off on the exposed side by a 0.5 mil polyethylene film,

The intensity of the 002, 101, and 101 peaks is lowest (10 units in Fig. 1b, and 17 units in Fig. 1c) in the wet samples. There is definite evidence of crystalline structure in spite of the almost complete absorption of diffraction by the large amount of water present. In parallel experiments it was shown that ground, highly crystalline cellulose, when saturated with water also gave diffractograms with similarly reduced intensities.²³

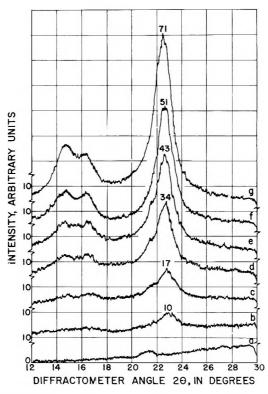


Fig. 1. Diffractometer traces of: (a) pure water in the sample holder; (b) water-wet fiber; (c) same fiber sampled at 100% R.H.; (d) same fiber compressed in wet state at 25,000 psi; (e) same fiber dried overnight at room temperature and humidity; (f) same fiber passed and then dried at room temperature and humidity; (g) a Deltapine control, dry.

Air-Dried Fiber. Figure 1d is a trace of the first platelet (Fig. 1b) after it had been pressed again with a pressure of 25,000 psi. Figure 1e is a trace of the same platelet dried overnight in air, at room temperature; Figure 1f is a trace of a commercial cotton, variety Deltapine, several years old, prepared in the standard way by passing the fibers through a Wiley mill and adding a slight amount of cement to the platelet for coherence.

The intensity of the 002, 101, and $10\overline{1}$ peaks is highest in the commercial sample (71 units) and medium in the samples which were pressed (34 units in Fig. 1*d*), or dried overnight (43 units in Fig. 1*e*) or pressed and dried

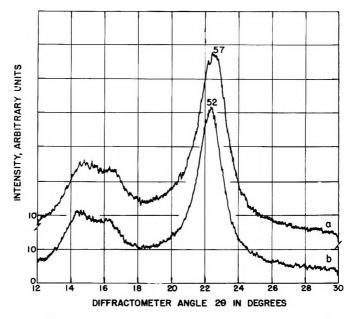


Fig. 2. Diffractometer traces of: (a) fiber dried from benzene; (b) same fiber, control, dried overnight from water.

(51 units in Fig. 1f). An increased definition and separation of the 101 and 10 $\overline{1}$ peaks is also observed.

Whereas in the wet samples the main peak is located at 23° , in the dry samples it is located at 22.5° .

Figures 5b and 5c below also illustrate the distinct decrease in intensity of the 002 peaks of fibers dried only overnight at room conditions as compared with those of fibers stored for a longer period under room conditions (Deltapine standard).

Effect of Stretching of the Undried Fiber. Stretching of the fiber in water before drying was always found to result in slightly higher diffraction peaks in the dried samples as compared to unstretched samples, regardless of what the subsequent preparation has been.

Fiber Dried After Liquid Exchange. Fibers dried from ether after the water had been first exchanged by alcohol or Cellosolve, did not give a tracing greatly different from that of the directly air-dried fibers.

The diffractometer traces of fibers dried from benzene, (Fig. 2), however, differed in various ways from those dried from water. In the first place the 002 peak intensity was lower, and a less clear definition and separation of the 101, $10\overline{1}$ peaks was observed. In the second place a much higher background was present between the 002 and 101 peaks. In the benzene-dried samples the intensity of the background at a position of $2\theta = 18-19^{\circ}$ measured 14 units (Fig. 2a), against 10 units in a comparable sample dried overnight from the water wet state in air and which had a similar intensity of the 002 peak (Fig. 2b).

Fiber Dried From Liquids Above Critical Temperature. Figure 3 shows diffractograms of amorphous cellulose and of fiber dried from pentane above the critical temperature (197°C.).

The maximum of the diffractogram of amorphous cellulose (ball-milled cotton) is located between 22 and 18°, at about $2\theta = 20^{\circ}$, just between the position of the 002 and 101 peaks of crystalline cellulose. This position corresponds with the location of greatest broadening (and resulting shift) of the 002 peak. The Deltapine control had an intensity of the 002 peak

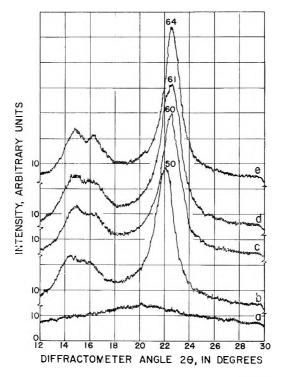


Fig. 3. Diffractometer traces of: (a) amorphous cellulose prepared by ball-milling; (b) fiber dried above critical temperature from pentane; (c) same, after 30 hr. at room temperature and humidity; (d) same, dried from pentane in vacuum desiccator at 33°C.; (e) Deltapine control.

of 65 and a background of 10 units (Fig. 3e). In the pentane-dried samples the background was 12 and 13 units, respectively, Fig. 3b and 3d). Lastly, in the pentane samples the 002 peak was broadened on the side toward the smaller angle. This broadening went hand in hand with a slight shift of the 002 peak toward a lower angle. This broadening will be explained in the discussion in relation to the following experimental data.

Freeze-Dried Fiber. The freeze-dried samples (Fig. 4a) show the same features as the pentane and benzene-dried samples. The 002 peak is still lower than those (about 50–55 units), if the pre-drying has taken place thoroughly by liquid nitrogen. The composite features indicate the lowest

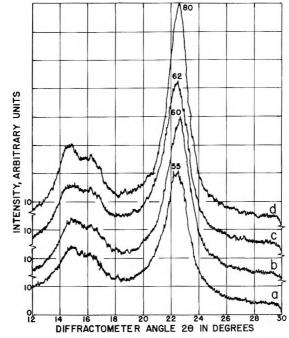


Fig. 4. Diffractometer traces of: (a) freeze-dried fiber, prefrozen in liquid nitrogen; (b) same, after 24 hr. at room temperature and humidity; (c) freeze-dried fiber, prefrozen in a Dry Ice-acetone mixture and thereafter kept for 24 hr. at room temperature and humidity; (d) same fiber as in (a) but rewetted in water and dried at room temperature overnight.

degree of crystallinity of all samples studied (with the exception of the freeze-dried, crosslinked samples of Fig. 5a, to be discussed below).

After storing of the samples for 24 hr. the intensity of the 002 peak was increased to 62 units (Fig. 4c).

If a freeze-dried sample is rewetted in water and dried overnight at room temperature, a most striking effect is observed. The intensity of the 002 peak (Fig. 4d) increases to 80 units, which is even higher than that of the Deltapine standard. Also the 101 peak increases in intensity, and a better separation occurs into 101 and $10\overline{1}$ peaks; the background is greatly reduced. These component features indicate a high degree of crystallinity.

Crosslinked Fiber. The x-ray traces of crosslinked fiber (Fig. 5) show about the same features as those of the freeze-dried materials. A very high background intensity is observed, 15 units (Fig. 5a) against 11 units for the controls which had been dried directly during the same time, (Fig. 5b); all samples show the same intensity of the 002 peak.

Crosslinked, Freeze-Dried, and Benzene-Exchange, Freeze-Dried Fiber. The diffractograms of the fibers freeze-dried after crosslinking or liquid exchange into benzene are given in Figure 6.

In the crosslinked and freeze-dried sample (Fig. 6a), a very low 002 peak intensity of 51 is observed and a 101 peak height of 20 units against a

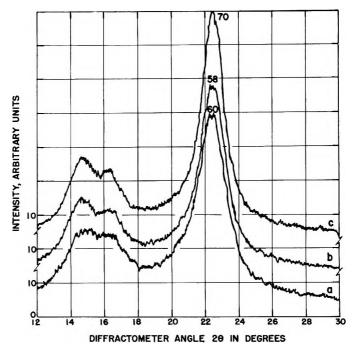


Fig. 5. Diffractometer traces of: (a) fiber crosslinked with formol and dried overnight at room temperature and humidity; (b) noncrosslinked control dried overnight at room temperature and humidity; (c) Deltapine control.

background intensity of 14 units. Figure 6c is a diffractogram of a Deltapine control traced at the same intensity setting of the 002 peak but showing a background of only 8° . Figure 6b shows a noncrosslinked control dried overnight from water. The clear definition of peaks and the lower background in Figures 6b and 6c which are in strong contrast to the features of the crosslinked fiber indicate a lower crystallinity than in any of the other samples.

The benzene-exchanged, freeze-dried sample (Fig. 6d) shows the same features as that in Figure 6a, though to a smaller extent.

It was shown in parallel experiments that "cement-treated" samples gave almost identical curves, except at a slightly higher level.

Density Data

The results of the density measurements are given in Table I.

The value (1.214) reported in the table for freeze-dried cotton is the lowest ever reported for cotton. The subsequent increase of the density of the freeze-dried cotton can be explained by a steady penetration of the liquid into the amorphous portions of the fiber, probably replacing entrapped air (the amount of entrapped air might serve as a measure of the porosity). In the stretched fiber this penetration is apparently faster, perhaps as a result of ruptures in the outer and inner layers or of the forma-

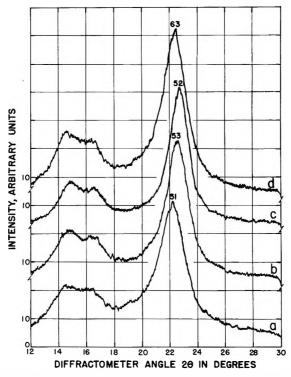


Fig. 6. Diffractometer traces of noncemented samples of: (a) formol-crosslinked and freeze-dried fiber; (b) control dried overnight at room temperature and humidity; (c) Deltapine control, traced at same intensity for 002 peak; (d) fiber freeze-dried after benzene liquid exchange.

TABLE I

Density Measuremen	ts with	Cotton	Fiber	from	Which	Water	Has	Been	Removed	in
Various Ways (Measured after 24 hr.)										

Fiber	Density, g./cc.
Normal, air-dried from water	1.550
Amorphous, ball-milled	1.505
Benzene, air-dried	1.510
Pentane-dried, above critical	
temperature	1.407
Freeze-dried	1.214 - 1.240
Freeze-dried, after 48 hr.	1.282
Freeze-dried after 7 days	1.504
Freeze-dried, stretched	1.504 - 1.529
Crosslinked	1.520

tion of irregular crevices in the amorphous portions during the collapse of the fiber.

The density value of the pentane "critically dried" fiber (1.407) is also a very low one. The density value of crosslinked fiber (1.520) corresponds very well with the one (1.525) reported by Reeves et al.¹⁵

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Differential Dye Results

The benzene- and pentane-dried samples after dyeing all showed a very high accessibility, as indicated by a brilliant green color, whereas the samples directly air-dried from the same bolls exhibited a red color, indicating a more compact structure.

DISCUSSION

From the above experiments, the following conclusions may be drawn regarding the state of cellulose in the fresh but mature, undried fiber and the extent of crystallization of cellulose during drying.

Since the diffractograms of the undried fiber always show some cellulose diffraction pattern, it must be concluded that crystalline cellulose does always occur in the mature fresh fiber. These observations do not support the hypothesis of Berkley and Kerr,² according to whom cellulose would occur only in the amorphous form in the undried fiber. That these authors did not find any indication of a cellulose pattern in the diagram of undried cotton fiber (except after stretching) may probably be ascribed to their technique. Not only did they use the photographic recording method, but also they probably did not use monochromatized radiation. It is well known that the x-ray scattering effect by water is greatly increased when nonmonochromatized radiation is used. In the present study, a more highly monochromatized radiation was achieved than by the authors by use of the pulse height analyzer in addition to the nickel filter and the focusing effect, inherent to the diffractometer setup. The use of such discrimination and of a reflection technique should reduce the amorphous scattering of water.

In the experiments of Berkley and Kerr² the much stronger water scattering may have easily "masked" or dissipated the diffraction effect by cellulose, particularly when the crystallinity was still low, as in the undried fiber. After the crystallinity had increased as a result of stretching, or as a result of direct drying (see conclusions below) the scattering by water was found no longer to mask the diffraction effect. The experimental observations of these authors may thus be explained without assuming an allamorphous structure in the fresh fiber.

The reason for the use of indirect methods to remove the water in the present experiments has already been briefly mentioned in the introduction. Following modern views, the presence and removal of water would promote the crystallization of cellulose by enabling the formation of hydrogen bonds between hydroxyls between and within the cellulose molecules. The presence of a liquid-gas interface would moreover promote the "collapse" of the amorphous regions of the molecules into a denser arrangement, inducive to crystallization. In the absence of either water (pentane- and benzene-drying) or of an interface (freeze-drying and "critical temperature evaporation"), or after reinforcement of the molecules by crosslinking, the further collapse and crystallization would be inhibited and the original

organization of the molecules in the fresh fiber might be expected to be maintained to a great extent. The density values and the differential dye tests show that a greater porosity and dyestuff accessibility results from these treatments, features which may be explained by a better preservation and a lower degree of collapse of the amorphous phase.

The experiments show that with samples from which the water has been removed in this indirect way, x-ray diffractograms with lower peak height, larger width, and higher background are obtained as compared to those from the directly dried samples. All of these features indicate that a lower degree of crystallinity exists in the indirectly dried than in the directly dried fibers. Since the indirect drying methods tend to preserve the amorphous structure better than the direct drying methods, it may be concluded that a greater extent of crystallization must occur during direct drying of the water-wet fiber than when the water is removed indirectly. This is in accordance with the modern views outlined above, according to which the presence of water and its gradual removal would induce crystallization and its absence suspend this process. The results with the rewetted, freeze-dried fiber are in agreement herewith. After rewetting the freeze-dried fiber and subsequently drying it from the waterwet state, the degree of crystallinity is found to be increased far above that of the freeze-dried material. It appears as if after freeze drying the secondary crystallization process takes place only after rewetting of the fiber and subsequent direct drying from the water-wet state. In how far the indirect methods prevent any crystallization to take place at all cannot be decided from the data available. The fact that no completely amorphous structure was ever observed after indirect water removal is at least in agreement with the above findings concerning the presence of crystallinity in the undried fiber.

The results show that a further crystallization of cellulose, beyond the original crystallinity in the wet fiber, takes place during the drying from water and that this process, moreover, continues for some time afterwards; this is indicated by the still larger degree of crystallinity of old material which had been stored for some time.

An interesting observation is the unilateral broadening and slight shift of the 002 peak, described in the experimental part. This shift may be explained in the preset case by a superposition of an amorphous background above the ordinary diffraction pattern. The trace of amorphous cellulose has a maximum just between the two peaks (Fig. 4a). Its super position, therefore, will result indeed in a shift of the 002 peak toward a smaller angle. This shift has to be explained, therefore, by a decrease of crystallinity rather than by an increase of spacing in the microcrystallites.

It should be emphasized, finally, that the present experiments were carried out with mature cell walls of cotton of which the major portion consists of secondary wall material. The question as to whether elongating primary walls (e. g., coleoptiles) contain cellulose in a crystalline form is not answered by the present findings.

ห้องสมุด กรมวิทยาศาสตร์

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Use of a company and/or product name by the Department does not imply approval or recommendation to the exclusion of others which may also be suitable.

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Résumé

On a étudié, par des méthodes de diffraction aux rayons-X, la cristallinité de la cellulose dans la fibre de coton non-sèchée, à partir directement de la balle non ouverte mais mûre et les résultats obtenus ont été comparés avec la cristallinité de portions de fibres obtenues à partir des mêmes échantillons séchés directement ou bien dont l'eau a été enlevée de différentes manières 'incirectes' de façon à préserver le mieux possible la structure générale. Ces différentes manières comprennent: (a) échange de solvant, (b) lyophilisation, (c) séchage audessus de la température critique des liquides et (d) séchage après que la cellulose de la fibre mouillée soit pontée. La différence de cristallinité observée entre les fibres séchées directement et indirectement indique qu'un processus de cristallisation peut avoir lieu pendant le séchage direct de la fibre mouillée d'eau. Ce processus de cristallisation est favorisé par la présence d'eau et inhibé ou empêché lorsque la fibre est séchée indirectement. Une augmentation du degré de cristallinité due au mouillage peut être expliqué en admettant que la cristallisation, qui avait été supprimée dans la fibre séchée indirectement, a lieu ultérieurement par séchage de la fibre remouillée. Le fait que les méthodes indirectes préservent entièrement ou partiellement telle structure amorphe présente originellement, est confirmé par la densité plus faible et par l'accessibilité plus élevée aux colorants de telles fibres.

Zusammenfassung

Die Kristallinität von Zellulose in der ungetrockneten Baumwollfaser, frisch aus der ungeöffneten, aber reifen Kapsel, wurde mit Röntgenbeugungsmethoden untersucht und mit der Kristallinität von Teilen der Fasern aus der gleichen Probe verglichen, die entweder direkt getrocknet wurden oder aus denen das Wasser auf verschiedenen "indirekten" Wegen entfernt worden war, die eine bessere Erhaltung der ursprünglichen Struktur gewährleisten sollten. Dazu gehören (a) Lösungsmittelaustausch, (b) Gefriertrocknung, (c) Trocknung oberhalb der kritischen Temperatur von Flüssigkeiten, (d) Trocknung nach Vernetzung der feuchten Faser. Der beobachtete Unterschied in der Kristallinität zwischen dizkekt und indirekt getrockneten Fasern zeigt, dass während der direkten Trocknung der feuchten Faser ein Kristallisationsprozess stattfinden muss. Dieser Kristallisationsprozess wird durch die Gegenwart von Wasser begüngstigt und wird bei indirekter Trocknung der Faser verhindert. Eine Zunahme des Kristallinitätsgrades durch Befeuchtung kann durch die Annahme einer Kristallisation, welche in der indirekt getrockneten Faser unterdrückt worden war, beim darauffolgenden Trocknen der wiederbefeuchteten Faser erklärt werden. Dass die indirekten Methoden zur Gänze oder zum Teil die ursprünglich vorhandene amorphe Struktur erhalten, wird durch die niedrigere Dichte und die höhere Farbstoffaufnahme solcher Fasern bestätigt.

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Heterogeneous Polymer Systems. I. Polymeric Oil-in-Oil Emulsions

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Synopsis

A novel class of emulsions has been introduced. Emulsions of this class comprise two immiscible polymer solutions and a graft copolymer as an emulsifying agent. The name polymeric oil-in-oil emulsions (POO emulsions) has been suggested for the new emulsions. The concept has been verified with several systems of polymer solutions. The polymers used here are poly(ethyl acrylate), poly(methyl methacrylate), polystyrene, polyvinyltoluene, poly-*p-tert*-butylstyrene, and a styrene/acrylonitrile copolymer.

INTRODUCTION

A wide variety of definitions of the term emulsions exists in the literature. According to Becher,¹ "an emulsion is a heterogeneous system, consisting of at least one immiscible liquid intimately dispersed in another in the form of droplets, whose diameter, in general, exceeds 0.1μ . Such systems possess a minimal stability, which may be accentuated by such additives as surface-active agents, finely divided solids, etc."

Two types of emulsion are known: An emulsion of oil droplets in a continuous phase of water, and an emulsion of water droplets in a continuous phase of oil. The terms oil and water, as used in the literature, denote nonpolar and polar liquids in general. The question can be asked: Do these two emulsion types represent a limit, or are other emulsion types possible?

If "immiscible oils" or "immiscible waters" could be found, the possibility would arise that not one, but three classes of emulsions could be made, namely oil-oil (0/0) emulsions, oil-water (O/W) emulsions, and water-water (W/W) emulsions. Each of these three classes of emulsions would then consist of two emulsion types, depending on which phase is the continuous and which is the disperse phase (Fig. 1). Within each class, the two emulsion types should be invertible, as oil-in-water emulsions can be inverted into water-in-oil emulsions and vice versa.²

Of the three conceivable classes of emulsions, only the combination oilin-water or, in more general terms, the combination nonpolar-polar, is described in the literature. The combination oil-oil or nonpolar-nonpolar and the combination water-water or polar-polar have been either not recognized or not seriously considered.

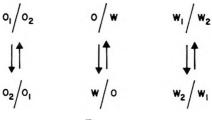


Figure 1.

The purpose of this paper is the verification of the existence of oil-in-oil emulsions. A mechanism of stabilization of oil-in-oil emulsions will be proposed in a subsequent paper, and water-in-water emulsions will be discussed in a future paper in this series.

RESULTS AND DISCUSSION

Principles of POO Emulsions

A general access to heterogeneous liquid systems consisting of two or more immiscible oils or waters is given when polymer solutions rather than low molecular weight materials are employed. Dobry and Boyer-Kawenoki³ have shown that solutions of two polymers in one solvent separate into two phases. Other authors⁴⁻⁷ have confirmed the generality of the occurrence of phase separation of polymer solutions, and Scott⁸ has presented a thermodynamic treatment of the phenomenon. Systems with more than two phases can be obtained when more than two polymers are dissolved in one solvent.

Novel types of emulsions can be made with immiscible polymer solutions, namely oil-in-oil and water-in-water emulsions, if emulsifiers active in such systems can be found. It is conceivable that even a series of emulsions can be made which represents a gradual transition from entirely nonpolar oil-in-oil emulsions to very polar water-in-water emulsions. A series of this type would involve nonpolar polymers like polystyrene, polymers of medium polarity such as polyacrylates, polymethacrylates and polymeric alcohols like poly(vinyl alcohol), and highly polar polymers like polyclectrolytes. Indeed, the possibilities for making emulsions of this new type seem to be as wide as the field of polymer chemistry. Since the new emulsions are based on polymer solutions, the terms polymeric oil-in-oil emulsions (POO emulsions) and polymeric water-in-water emulsions (PWW emulsions) are proposed for these systems.

There are two major differences between polymeric emulsions and conventional emulsions: (1) the two phases of POO and PWW emulsions are of equal or similar polarity, while the phases of conventional emulsions are of opposite polarity; (2) the immiscibility of the two liquids employed in POO and PWW emulsions is a consequence of the incompatibility of the solutes, while the immiscibility of the liquids employed in conventional emulsions is a consequence of the incompatibility of the solvents (oil and

water). In POO emulsions, the solvent is the same in both phases, and the interface is comparable (for illustrative purposes) to a semipermeable membrane in osmosis: i.e., the solvent can pass freely between the phases; the solutes cannot.

One prerequisite for the preparation of oil-in-oil emulsions is fulfilled. Immiscible oils are now generally available because of the phenomenon of phase separation of polymers in solution. In order to prepare POO emulsions, another prerequisite must be fulfilled as well: emulsifiers must be found which are active in such systems. Since POO emulsions, by definition, consist of nonpolar, organic phases, a nonionic mechanism of stabilization has to be expected. This speculation suggests the use of polymeric materials which are similar to nonionic surfactants, i.e., materials which contain chains of different structure in the same molecule. Graft and block copolymers are polymeric materials which are formally similar to nonionic surfactants, and—without any implication as to their mechanism of stabilization—the idea to try graft and block copolymers as POO emulsifiers seems attractive, particularly since Bartl and von Bonin⁹ have successfully used a styrene-grafted poly(ethylene oxide) as an emulsifier in waterin-oil emulsions.

In Situ Generation of the Second Phase

Conventional oil-water emulsions are made by agitating a mixture of oil, water, and an emulsifier. Another possibility of making an emulsion exist in the case of POO-emulsions. There, an emulsion can either be made by agitating a mixture of two immiscible polymer solutions with a POO emulsifier or by polymerizing a solution of a polymer in another monomer and thus creating the second phase *in situ* in a finely dispersed form. The latter method is particularly attractive, since formation of graft copolymer by chain transfer to the dissolved polymer occurs during the polymerization, if the chain transfer constant is of sufficient magnitude. A system should result in which the components of the graft copolymer are identical with the homopolymers in the two phases, thus assuring complete compatibility of each branch of the graft copolymer with the corresponding homopolymer. This compatibility aspect becomes important when the homopolymers are themselves random copolymers.

The partial polymerization of any solution of a polymer in another monomer should lead to the *in situ* formation of a polymeric oil-in-oil emulsion, provided that the dissolved polymer and the formed polymer are incompatible (which is usually the case) and that both polymers are soluble in the monomer which serves as the solvent. The emulsion stability would depend on the amount of graft copolymer formed during the polymerization.

The preparation of POO emulsions by *in situ* formation of the second phase and of the POO emulsifier will be illustrated here with the use of combinations of polystyrene with poly(methyl methacrylate), poly(ethyl acrylate), polyvinyltoluene, poly-*p-tert*-butylstyrene, and a styrene/acrylo-nitrile copolymer as examples.

The polymerization of a 6% solution of poly(ethyl acrylate) in styrene may serve as a typical example for the observations made during such a heterogeneous polymerization. The initial solution of poly(ethyl acrylate) is water-clear. It is homogeneous, i.e., it contains only one phase, since only one polymer is present. The system is still homogeneous after a minute amount of the styrene has been polymerized to polystyrene, since phase separation does not occur before a certain threshold value of composition which is called the "critical point." After this point, two phases coexist which are solutions of both polymers, poly(ethyl acrylate) and polystyrene, in styrene. In one phase, which will be called the poly(ethyl acrylate) phase, poly(ethyl acrylate) prevails, and in the other phase, which will be called the polystyrene phase, polystyrene prevails. As the polymerization proceeds and more polystyrene is formed, the amount of polystyrene in the poly(ethyl acrylate) phase decreases, and the amount of polystyrene in the polystyrene phase increases. After a certain degree of conversion has been reached, there is practically only one polymer in each phase, so that the system consists then of a poly(ethyl acrylate) solution in styrenc and a polystyrene solution in styrene. More detailed information on phase equilibria of two polymers in one solvent can be found in the literature on phase separation cited above and in Tompa's book on polymer solutions.¹⁰

Since the compositions of the two phases change as the polymerization proceeds, the refractive indices of the two phases also change, which behavior leads to a change in the appearance of the samples from water-clear to slightly hazy, turbid, and opaque. Occasionally, when the refractive indices of all constituents are practically identical, no haze or opacity can be observed. Such systems should not be mistaken for homogeneous systems, even if they look water-clear. A good phase contrast microscope often makes two phases visible in systems which appear entirely clear to the naked eye. Even if the phase separation cannot be made visible at all, the necessity of its occurrence can still be concluded from the bulk of experimental evidence, according to which polymers of sufficiently different structure are only very rarely compatible. The first occurrence of opacity in a polymerization does not necessarily indicate the critical point. However, the point of first opacity is often very near the critical point.

The first samples of a series taken during a polymerization occasionally separate into two liquid layers after a relatively short time because not enough graft copolymer has been formed after this polymerization time to give sufficient emulsion stability. In order to avoid confusion with the phenomenon of phase separation, this phenomenon of separation into two layers will be called here "demixing" (from the German *entmischen*), since this term is commonly used in the German literature on emulsions (e.g., by E. Manegold).¹⁶ Demixing does not coincide with coagulation; it is a consequence of coagulation.

Another important phenomenon occurring during a heterogeneous polymerization is the change of the phase volume ratio as a function of the degree of conversion of the system. The phase volume ratio Ψ is defined

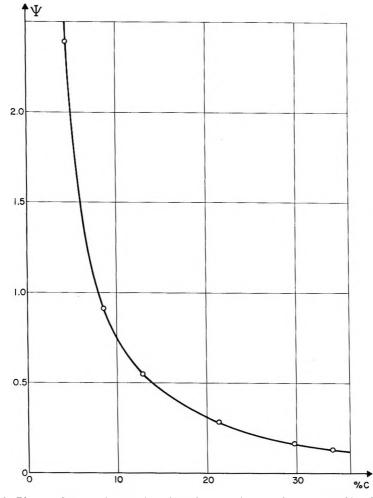


Fig. 2. Phase volume ratio as a function of conversion for the system 6% poly(ethyl acrylate)-polystyrene-styrene.

here as $\Psi = A/B$, where A is the volume of the phase of the polymer which was initially dissolved in the monomer and B is the volume of the polystyrene phase. The phase volume ratio could be measured as a function of degree of conversion, if the samples taken during the polymerization would readily demix. However, many POO emulsions are so stable that complete coagulation can be achieved only after long centrifugation times in an ultracentrifuge. A simpler way of obtaining a phase volume ratio curve is the preparation of a series of solutions, the compositions of which correspond to the compositions of samples taken during a polymerization, except that the graft copolymer, i.e., the POO emulsifier, has been omitted. Such solutions demix readily, since they are not emulsified, and an "approximate" phase volume ratio can be measured. The phase volume ratio obtained by this method is called approximate, because a certain error will be

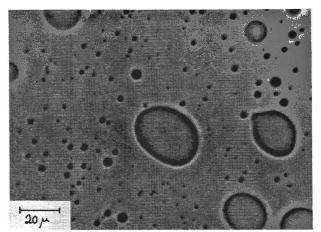


Fig. 3. 6% Poly(ethyl acrylate) in styrene, polymerized to 6.3% conversion: before the inversion point.

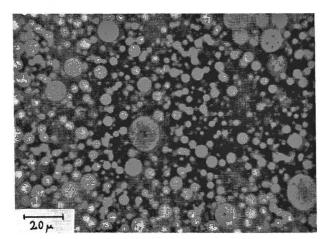


Fig. 4. 6% Poly(ethyl acrylate) in styrene, polymerized to 24.4% conversion: after the inversion point.

introduced by the omission of the graft copolymer. However, this error should be small, since the amount of graft copolymer formed during the polymerization is usually rather small.

The approximate phase volume ratio has been plotted in Figure 2 for the system poly(ethyl acrylate)-polystyrene-styrene as a function of the degree of conversion C. Before the critical point, the system is homogeneous, and no phase volume ratio exists. At the critical point, the polystyrene phase comes into existence. As the polymerization proceeds, the volume of the polystyrene phase increases and, consequently, the phase volume ratio decreases, because styrene (solvent) is transformed into polymer which, in turn, draws other solvent from the poly(ethyl acrylate) phase until the osmotic equilibrium is reached. This behavior has definite consequences with respect to the structure of the POO emulsion. Since

the polystyrene phase is, at first, very small, it is naturally the disperse phase of the POO emulsion. As the polymerization proceeds and the volume of the polystyrene phase increases at the expense of the volume of the poly(ethyl acrylate) phase (Fig. 2), a point is finally reached at which the polystyrene phase becomes too large to be disperse and the poly(ethyl acrylate) phase becomes too small to be continuous. At this point, a phase inversion occurs. After the inversion point, the poly(ethyl acrylate) phase is disperse, and the polystyrene phase is continuous. During the polymerization of a 6% solution of polyethylacrylate in styrene, the phase inversion cccurs at 10% conversion. Figure 3 shows the emulsion state before the inversion point, and Figure 4 shows the emulsion state after the inversion point. In both phase contrast photomicrographs, the poly-(ethyl acrylate) phase is white, and the polystyrene phase is black.

The occurrence of phase inversions in oil-water emulsions has been described at length in the literature,^{1,2} and a relation between the emulsion state and the phase volume ratio has been pointed out by several authors. A phase volume theory of the emulsion state based on purely stereometric grounds was proposed by Ostwald.¹¹ Sherman¹² has shown that the phase volume ratio at which inversion occurs can be a function of the emulsifier concentration. A dependency of the phase inversion point on the concentration of the POO emulsifier seems to exist also in POO emulsions. In several POO emulsion systems, a shifting of the inversion point to higher phase volume ratios (lower degrees of conversion) has been observed to occur when the concentration of the POO emulsifier is decreased.

In the polymerization of a 6% solution of poly(methyl methacrylate) in styrene, all samples before 13.5% conversion were water-clear, so that no phase contrast could be obtained under the microscope. The phase inversion must have occurred in this region, because the poly(methyl methacrylate) phase was the disperse phase after this region. The samples at conversions higher than 13.5% were opaque and looked very similar to the samples obtained during the polymerization of the poly(ethyl acrylate) solu-Since poly(methyl methacrylate) has no activated C—H bonds, it tion. should have a lower chain transfer constant than poly(ethyl acrylate), which has C—H bonds activated by the ester carbonyls. Therefore, less grafting should occur *ceteris paribus* on the poly(methyl methacrylate) than on the poly(ethyl acrylate) and, consequently, the POO emulsion stability in the poly(methyl methacrylate) system should be lower than in the poly(ethyl acrylate) system, which is indeed the case. In the poly(methyl methacrylate) system, all samples taken during the polymerization demixed within three to four weeks, while the samples of the poly(ethyl acrylate) system were stable for at least half a year. The droplets in the former system were larger than the droplets in the latter system. The observation has usually been made that the average drop size in POO emulsions increases as the concentration of the POO emulsifier and the emulsion stability decrease.

Polymeric oil-in-oil emulsions are, by definition, emulsions of phases with similar polarity. The question arises: How similar can the polymers in the



Fig. 5. 10% Polystyrene in *p-tert*-butylstyrene, polymerized to 5.3% conversion: before the inversion point.



Fig. 6. 10% Polystyrene in *p-tert*-butylstyrene, polymerized to 7.8% conversion: at the inversion point.

two phases be and still permit an emulsion to be made? In pursuit of this question, three POO emulsions have been prepared, the components of which have very similar structures.

The three systems are: polystyrene-poly-*p*-tert-butylstyrene-*p*-tertbutylstyrene, polystyrene-polyvinyltoluene-vinyltoluene, and polystyrenestyrene/acrylonitrile copolymer-styrene/acrylonitrile. Phase separation occurs in each system. POO emulsions have been prepared by polymerization of 10% solutions of polystyrene in *p*-tert-butylstyrene, in vinyltoluene, and in a 75/25 styrene/acrylonitrile mixture. The same observations have been made in these systems as in the systems described above. All samples taken during the polymerization were opaque POO emulsions. Phase inversions took place during each polymerization. As typical examples, photomicrographs of samples taken during the polymerization of the solution of polystyrene in *p*-tert-butylstyrene are shown here. Figure 5 shows

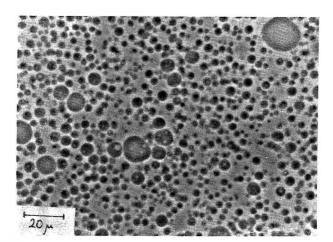


Fig. 7. 10% Polystyrene in *p-tert*-butylstyrene, polymerized to 13.3% conversion: after the inversion point.

the system before the inversion point, Figure 6 shows the system at the inversion point, and Figure 7 shows the system after the inversion point. The polystyrene phase is black, and the poly-*p*-tert-butylstyrene phase is white in these pictures. Multiple emulsions can be observed in Figures 6 and 7 and also in Figure 4. The occurrence of multiple emulsions after the phase inversion point is a phenomenon generally observed in POO emulsions. The same phenomenon has been observed after phase inversions in oil-water emulsions.^{2,13} The phase inversion occurred at about 8% conversion in the system containing poly-*p*-tert-butylstyrene, at about 14% conversion in the system containing the styrenc/acrylonitrile copolymer. The samples taken at less than 15% conversion demixed gradually over a period of half a year. The samples taken at conversions higher than 15% were stable for more than half a year. (Further polymerization of the solvent-monomers was inhibited with benzoquinone in all samples.)

Occurrence of POO Emulsions in the Literature

Although the existence of POO or PWW emulsions has hitherto apparently not been recognized, many authors have probably prepared materials which actually were POO emulsions but were not recognized as emulsions, since the true nature of such systems is revealed only when a phase contrast microscope is employed. The unusually high stability of many POO emulsions might often have disguised even the heterogeneous nature of the systems so effectively that they were mistaken for homogeneous systems. Occasionally, a so-called "compatibilization" of polymers by graft copolymers is mentioned in publications. In such publications, compatibilization apparently means making a heterogeneous two-polymer system homogeneous by blending in a graft copolymer, in the same manner as a heterogeneous system consisting of benzene and water is made homogeneous by adding methanol. However, the literature on phase separation and polymer incompatibility cited above and phase separation experiments which will be reported later suggest that a compatibilization of this type is not possible in heterogeneous polymer systems.

Recently, Hughes and Brown¹⁴ have studied the influence of styrenegrafted poly(ethyl acrylate) on the phase separation of poly(ethyl acrylate) and polystyrene in a common solvent. The authors grafted a poly(ethyl acrylate) latex with styrene and obtained a mixture of the graft copolymer with the two corresponding homopolymers. The graft copolymer was isolated from this mixture by a solvent extraction procedure. The authors obtained two distinct liquid layers when they dissolved pure poly(ethyl acrylate) and pure polystyrene in mutual solvents. When they dissolved their graft copolymer-homopolymer mixture in the same solvents, they no longer obtained two liquid layers, but solutions which they described Then, the authors isolated the graft copolymer from their as turbid. mixture and dissolved it together with pure poly(ethyl acrylate) and pure polystyrene in the same solvents. Again, the authors obtained turbid solutions which did not give two liquid layers. From these experiments, Hughes and Brown concluded that a property of the graft is its ability to "compatibilize" poly(ethyl acrylate) and polystyrene in common solvents and that for the grafts and inixtures containing them, the two-phase separation could not be obtained.

Since Hughes and Brown had apparently prepared a POO emulsion rather than a homogeneous system, their experiments were repeated. The turbid solutions which Hughes and Brown had obtained, when graft copolymer was present in their system, were investigated with a phase contrast microscope. As expected, these turbid solutions were not homogeneous systems, but POO emulsions.

Observations which should be mentioned here were made by Bristow⁵ and Merrett.¹⁵ Bristow observed that "an interpolymer (prepared by mastication) caused a marked reduction in the speed of phase separation" in phase equilibrium studies in polymer–polymer–solvent systems. Merrett found that colloidal suspensions of solid polymer particles in organic solvents can be stabilized by graft copolymers, one component of which is identical with the polymer in this organic latex.

Direct Emulsification with Radiation Graft Copolymer

Phase-separating solutions of two polymers in one solvent usually demix within a few hours to give two liquid layers. POO emulsions can be prepared from such systems by adding small amounts of suitable graft copolymers. Such POO emulsions are stable for several days, weeks, or months, depending on the nature of the polymers involved. Preliminary experiments can be reported here, which were carried out in order to study the possibility of making POO emulsions with graft copolymers obtained by γ -radiation grafting.

In order to prepare graft copolymers by this method, 20% solutions of polymers in monomers were irradiated in screw-cap bottles which were completely filled, thus excluding air almost entirely. The irradiations were

carried cut with a Co⁶⁰ source at room temperature at a dose rate of 100 krad/hr., doses ranging from 0.25 to 4.00 Mrad being used. A linear dependency of the degree of conversion of the samples on the radiation dose was observed, and a phase inversion occurred after irradiation with 1.5 Mrad (20.6% conversion) during the irradiation of a 20% solution of poly(methyl methacrylate) in styrene.

While all samples of this series were still liquid after irradiation, all samples irradiated with doses higher than 0.75 Mrad were solid in a series of 20% solutions of polystyrene in methyl methacrylate. The POO emulsifier activity of the irradiated poly(methyl methacrylate) solutions in styrene was tested by adding 2% of these samples to a two-phase system obtained by dissolving 6% poly(methyl methacrylate) and 20% polystyrene in 74\% benzene. (The 2% of emulsifier solution is based on the total two-phase mixture.) After agitating on a laboratory shaker, the samples were allowed to stand for observation. While the control sample with no emulsifier demixed within 8 hr., the samples with emulsifier demixed within a period of 75 hr., the demixing times depending on the radiation dose which the emulsifier solution had received.

The emulsifier activity of the samples obtained by irradiation of 20% solutions of polystyrene in methyl methacrylate was tested by adding 5% of these samples to two-phase ssytems obtained by dissolving 6% polystyrene and 20% poly(methyl methacrylate) in 74% benzene. The control sample with no emulsifier demixed within 6–7 hr. The samples with emulsifier demixed over a period of 5 to 6 weeks. The individual demixing times were again a function of the radiation dose which the emulsifier had received.

EXPERIMENTAL

Poly(ethyl acrylate) was prepared by emulsion polymerization according to the method described by Hughes and Brown.¹⁴ Poly(methyl methacrylate) (du Pont Lucite) and polystyrene (Dow Styron 638) were molding grade production materials which were used without purification. The *tert*-butylstyrene was the *para* isomer; the vinyltoluene was a mixture of isomers (60% meta + 40% para).

In order to prepare POO emulsions by in situ generation of the second phase, mass polymerizations of 6% or 10% solutions of polymers in monomers were carried out in a 3-liter resin flask equipped with stirrer, reflux condenser, and thermocouple. The polymerizations were carried out under nitrogen with a stirrer speed of 60 and 0.03% Bz₂O₂ as initiator. The temperature was 75°C. when acrylonitrile was present and 90°C. in all other cases. Samples were taken every 15 min. The solids contents of the samples were determined on a moisture balance. The conversion C was calculated from the solids contents S by the formula:

$$C = (S - P) / [1 - (P/100)]$$

where P is the concentration of the dissolved polymer. S, P, and C are given in per cent, but the percentages of S and P are based on the entire system, while the conversion C is based on the monomer only.

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The emulsion state of the samples was investigated by using a dark phase contrast microscope. In this type phase contrast microscope, the phase with the lower refractive index appears white. Refractive index measurements must accompany all investigations of POO emulsions in order to establish which is the disperse phase and which is the continuous phase. Refractive index measurements have also been used to confirm that the phase inversions observed are not optical illusions caused by a crossover point of the refractive index curves.

The author wishes to thank Mr. H. L. Garrett for preparing the phase contrast photomicrographs, Mr. P. A. Traylor for his general advice and assistance of the microscopic work, and Dr. S. G. Turley for reading the manuscript. Dr. T. Gillespie and Dr. A. M. Schwartz (Harris Research Laboratories) contributed to this work by their combined interest and stimulating discussions. Special thanks are due Dr. H. Keskkula for suggesting the field of research.

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Résumé

On présente une nouvelle classe d'émulsions. Les émulsions de cette classe sont composées de deux solutions de polymères non-miscibles et d'un copolymère greffé comme émulsifiant. Le nom Polymeric Oil-in-Oil Emulsion (POO-emulsions) a été suggéré pour les nouvelles émulsions. On a vérifié ce système avec plusieurs solutions de polymères. Les polymères employés ici sont le polyacrylate d'éthyle, le polyméthacrylate de méthyle, le polystyrène, le polyvinyltoluène, le poly-*p-tert*-butylstyrène et un copolymère styrène/acrylonitrile.

Zusammenfassung

Eine neue Klasse von Emulsionen ist eingeführt worden. Emulsionen dieser Klasse bestehen aus zwei nichtmischbaren Polymerenlösungen und einem Pfropfcopolymeren als Emulgator. Der Name Polymere Oel-in-Oel Emulsionen (POO-Emulsionen) wird für die neuen Emulsionen vorgeschlagen. Das Konzept ist an mehreren Systemen von Polymerenlösungen verifiziert worden. Die hier benützten Polymeren sind Polyäthylacrylat, Polymethylmethacrylat, Polystyrol, Polyvinyltoluol, Poly-*p-tert*-butylstyrol und ein Copolymerisat von Styrol und Acrylnitril.

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Probabilistic Considerations of the Tacticity of Optically Active Polymers

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Synopsis

The probability theory of Markov chains used in the characterization of stereoregular polymers is extended to optically active high polymers. The degree of tacticity is expressed in terms of the transition probabilities for chain growth which is asymmetric with respect to selection of monomer unit configurations. The variation of the Bovey tacticities with the probability parameters is illustrated for the case of asymmetric, simple Markov chains. The relations between tacticity and configurational asymmetry of optically active polymers are discussed.

I. INTRODUCTION

In a previous communication,¹ we have dealt with the nonstationary process of linear copolymer chain growth on the basis of the Markov statistics and concluded that the copolymer composition tends to be anisometric with respect to the component monomers in its stationary limit, whenever the transition probabilities associated with the propagation step of copolymerization do not satisfy the stochastic reversibility. Thus for the occurrence of the so-called asymmetric polymerizations, whether asymmetric induction or selection, it is necessary only that in the chain propagation step the two conditional probabilities of persistence of the ultimate unit configurations, D and L, be unequal (DD \neq LL).

The above inequality for asymmetric polymerization can obtain when the selection of monomer unit configurations is governed by the statistics of either "asymmetric" Markov chains $(LD \neq DD \neq LL \neq DL)^1$ or Bernoulli trials $(LD = DD \neq LL = DL)^2$ In the case of asymmetric-selection polymerization, the probability parameters can be evaluated from the reactivity ratios of the enantiomorphic monomers, which in turn are obtainable, at least in principle, by the usual copolymerization technique. On the other hand, in the case of asymmetric-induction polymerization, in which adding monomer has no asymmetric carbon, it is impossible to decide the statistical scheme only from the data for the degree of configurational asymmetry induced in the high polymers.

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In the present study, we consider quantitatively the relations between tacticity and configurational asymmetry of optically active high polymers in the stationary limit. Basically, the treatment is an extension of various statistical theories³⁻⁵ of polymer tacticity to cover the asymmetric Markov process, including the Bernoullian statistics as a special case. The relations obtained should be useful for discriminating between the two statistical schemes and for characterizing stereoregular asymmetric polymers.

II. GENERAL CONSIDERATIONS

We will be concerned with the polymer chain growth in which a chainend sequence consisting of k monomer units selects a monomer unit configuration under the influence of those k units, thereby forming a new monomer unit sequence of the length k in the chain end. We refer to these terminal sequences before and after the monomer addition as the states iand j, respectively. Each step of monomer addition is subject to the competition of the two possible elementary reactions, e.g.,

$$\textbf{mDLD} + \textbf{M} - \overbrace{\qquad \rightarrow \text{ mLDL}}^{\rightarrow} \textbf{mLDL}$$
State $i(k = 3)$ States $j(k = 3)$

If the conditional probability, p_{ij} , of the transition from the state *i* to the state *j* is independent of the extent of polymerization, then the chain growth can be described by the statistics of the Markov type with a $2^k \times 2^k$ stochastic matrix **P**, whose *i*th column and *j*th row elements are p_{ij} .⁴ The transition probabilities are expressible in terms of the rates of the competing elementary reactions and are subject to the restriction:

$$\sum_{j=1}^{m} p_{ij} = 1$$

 $i = 1, 2, \dots, m$
 $m = 2^{k}$ (1)

Consider an interior sequence of k monomer units in a linear polymer molecule, the molecular weight of which is so great that the effect of initiation is negligibly small. We denote by $F_i^{(k)}$ the probability that the interior sequence be in the state *i*. The Markov process of chain growth is then represented by a set of simultaneous linear equations:

$$\sum_{i=1}^{m} p_{ij} F_i^{(k)} = F_j^{(k)}$$

$$j = 1, 2, \dots, m \qquad (2)$$

The probability $F_{i}^{(k)}$ is given by a nonvanishing root of eqs. (2), which is normalized in such a way that

$$\sum_{i=1}^{m} F_{i}^{(k)} = 1 \tag{3}$$

The mathematical procedure for obtaining the above probability is formally identical with that used for calculating the fraction of a given monomer in a copolymer formed from 2^{k} component monomers under the influence of the terminal unit alone. The result is^{1,4}

$$F_{i}^{(k)} = \psi_{i} / \sum_{j=1}^{m} \psi_{j}$$
(4)

Here ψ_i is the *i*th component of the unnormalized eigenvector corresponding to the unit eigenvalue of **P**, and is obtainable¹ as the minor determinant of the *i*th column and *i*th row element in the singular determinant (5):

D =	$p_{11} - 1$	p_{21}			p_{m1}	(5)
	p_{12}	$p_{22} - 1$,	p_{m2}	
		•			•	
		•				
		•			•	
	•	•				
	· ·	•				
	p_{1m}	$p_{2\pi}$		p_{π}	m-1	

Replacing ψ_i and ψ_j with the corresponding diagonal minors D_{ii} and D_{jj} , we can rewrite eq. (4) as

$$F_{i}^{(k)} = D_{ii} / \sum_{j=1}^{m} D_{jj}$$
(6)

That is, the distribution of sequence states in a polymer chain is equal to the fractional distribution of the diagonal minors derived from the singular determinant (5).

Finally, the polymer tacticity can be expressed in terms of pertinent sequence distributions and, eventually, as the function of the transition probabilities alone. In the next section, the tacticity and configurational asymmetry of a polymer chain will be calculated for the cases of asymmetric Markov chains with k = 1 and 2. The cases in which k is greater than 2 will not be treated because they are of little practical significance.

III. RELATIONS BETWEEN TACTICITY AND ASYMMETRY

A. Simple Markov Chains (k = 1)

In a simple Markov chain, only the terminal unit of the chain is responsible for the transition probability. We denote by p_{DD} and p_{DL} the conditional probabilities that in the propagation step a growing polymer carrying a terminal unit D selects the D and L configurations, respectively. Similar transition probabilities corresponding to persistence and alternation of the terminal unit L on propagation will be respectively denoted by p_{LL} and p_{LD} . The fractions, $F_{D}^{(1)}$, and $F_{L}^{(1)}$, of D and L configurations existing in a high polymer are calculated from eq. (6), giving

$$F_{\rm D}^{(1)} = (1 - p_{\rm LL})/(2 - p_{\rm LL} - p_{\rm DD}) = p_{\rm LD}/(p_{\rm LD} + p_{\rm DL})$$
 (7a)

$$F_{\rm L}^{(1)} = (1 - p_{\rm DD})/(2 - p_{\rm LL} - p_{\rm DD}) = p_{\rm DL}/(p_{\rm LD} + p_{\rm DL})$$
 (7b)

The degree of configurational asymmetry, ω_D , which may be defined as the excessive fraction of D configurations in a high polymer chain, is expressed as

$$\omega_{\rm D} = F_{\rm D}^{(1)} - F_{\rm L}^{(1)} = (p_{\rm LD} - p_{\rm DL})/(p_{\rm LD} + p_{\rm DL})$$
(8)

In eqs. (7) and (8), p_{LD} and p_{DL} cannot both be zero.

The degrees of polymer tacticity have been defined in two ways. One is the Natta tacticity,⁶ which is defined as the fractions of the two adjacent monomer configurations (dyad) that are isotactically bonded (DD or LL) or syndiotactically bonded (DL or LD) in a chain. The other class of tacticities, proposed by Bovey and Tiers,⁷ is concerned with the sequences of three consecutive monomer configurations (triad). These triads are said to be isotactic if they are in the DDD or LLL configuration, syndiotactic if they are in the DLD or LDL configuration, and heterotactic if they consist of one isotactic bond and one syndiotactic bond, i.e., DDL, DLL, LDD, or LLD.

In conformity with the definitions stated above, Natta's isotacticity I_0 and syndiotacticity S_0 of asymmetric polymers may be formulated as

$$I_{0} = F_{\rm D}^{(1)} p_{\rm DD} + F_{\rm L}^{(1)} p_{\rm LL}$$

= 1 - 2p_{\rm LD} p_{\rm DL} / (p_{\rm LD} + p_{\rm DL}) (9)
$$S_{0} = F_{\rm D}^{(1)} p_{\rm DL} + F_{\rm L}^{(1)} p_{\rm LD}$$

$$= 2p_{\rm LD}p_{\rm DL}/(p_{\rm LD} + p_{\rm DL}) \tag{10}$$

In a similar fashion, Bovey's isotacticity I, syndiotacticity S, and heterotacticity H are calculated, giving

$$I = F_{\rm D}^{(1)} p_{\rm DD}^{2} + F_{\rm L}^{(1)} p_{\rm LL}^{2}$$

$$= 1 + p_{\rm LD} p_{\rm DL} - 4 p_{\rm LD} p_{\rm DL} / (p_{\rm LD} + p_{\rm DL}) \qquad (11)$$

$$S = F_{\rm D}^{(1)} p_{\rm DL} p_{\rm LD} + F_{\rm L}^{(1)} p_{\rm LD} p_{\rm DL}$$

$$= p_{\rm LD} p_{\rm DL} \qquad (12)$$

$$H = F_{\rm D}^{(1)} (p_{\rm DD} p_{\rm DL} + p_{\rm DL} p_{\rm LL}) + F_{\rm L}^{(1)} (p_{\rm LL} p_{\rm LD} + p_{\rm LD} p_{\rm DD})$$

$$= 4 p_{\rm LD} p_{\rm DL} / (p_{\rm LD} + p_{\rm DL}) - 2 p_{\rm LD} p_{\rm DL} \qquad (13)$$

These five tacticities are not mutually independent. First, it is apparent that I + S + H = 1 and $I_0 + S_0 = 1$. Second, from eqs. (9)-(13), it can readily be verified that

$$I_0 = I + H/2$$

 $S_0 = S + H/2$ (14)

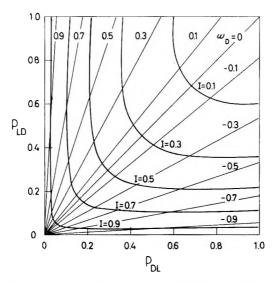


Fig. 1. Contour diagram of the degrees of isotacticity I (curves) and configurational asymmetry ω_D (straight lines) as functions of the alternation probabilities for a polymer formed by the simple Markov mechanism.

Therefore, any two of the Bovey tacticities define the third as well as I_0 and S_0 . Further, those two Bovey tacticities just suffice to make possible the evaluation of the two independent probability parameters, $p_{\rm LD}$ and $p_{\rm DL}$, which completely characterize the polymer molecules formed by the asymmetric, simple Markov mechanism. The Bernoullian case needs no separate consideration, since it is no more than a special case of Markov chains, in which $p_{\rm LD} + p_{\rm DL} = 1$.

It is worthwhile to note here that the Bovey tacticities of an asymmetric polymer can be related with its Natta tacticities and the (degree of) configurational asymmetry by

$$I = I_0^2 + p_{\rm LD} p_{\rm DL} \omega_{\rm D}^2 \tag{15}$$

$$S = S_0^2 + p_{\rm LD} p_{\rm DL} \omega_{\rm D}^2 \tag{16}$$

$$H = 2I_0 S_0 - 2p_{\rm LD} p_{\rm DL} \omega_{\rm D}^2 \tag{17}$$

The second terms in the right-hand sides of eqs. (15)-(17) represent the departure of the Bovey tacticities from the one-parameter theory⁷ in which the statistics of selection of tactic *bonds* is assumed to be Bernoullian.

In Figure 1 the (degree of) isotacticity I calculated from eq. (11) is illustrated in the form of a contour diagram with $p_{\rm LD}$ and $p_{\rm DL}$ as variables. A family of straight lines radiating from the origin shows the dependence of the configurational asymmetry $\omega_{\rm D}$ upon the two parameters.

On the basis of Figure 1 several points can clearly be stated, although some of them may have been obvious qualitatively. In the first place, the isotacticity of a polymer tends to become large when either one of the two alternation probabilities is sufficiently small. In other words, when one persistence probability (either p_{DD} or p_{LL}) is large, the other probability has little effect on the isotacticity.

Second, a set of p_{DL} and p_{LD} may be determined uniquely from known values of I and ω_D of high polymers. This may serve as a resolution of the statistics governing asymmetric polymerization.

Third, although the isotacticity of a polymer must be large if the polymer has an appreciably high configurational asymmetry, the converse is not necessarily true. For instance, when I is as great as 0.9, ω_D can take on any value (including zero) between 0.932 and -0.932, depending on the asymmetry of the mode of chain propagation. Nonetheless, large configurational asymmetry is possible only for highly isotactic polymers since the greater the I value, the greater is the maximum possible value of $|\omega_D|$. These mutual relations between I and ω_D are quantitatively represented by the inequalities:

$$2\omega_{\rm D}^2/(1+|\omega_{\rm D}|) \le I \le 1$$
 (18)

or rather

$$0 \le |\omega_{\rm D}| \le (I + \sqrt{I^2 + 8I})/4 \tag{19}$$

which can be derived from eqs. (8) and (11) under the restriction that $0 < p_{\rm LD} + p_{\rm DL} \leq 2$.

Figures 2 and 3, respectively, demonstrate the dependences of syndioand heterotacticities of polymers on the probability parameters. Either may provide a check on the parameters obtained from the experimental values of I and $\omega_{\rm D}$ with the aid of Figure 1 and on the applicability of the case k = 1.

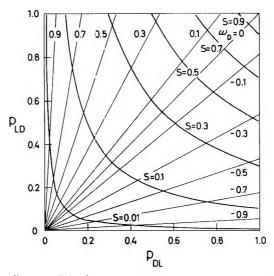


Fig. 2. Contour diagram of the degrees of syndiotacticity S(curves) and configurational asymmetry ω_D (straight lines) as functions of the alternation probabilities for a polymer formed by the simple Markov mechanism.

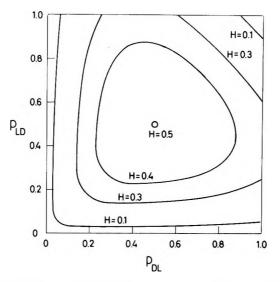


Fig. 3. Contour diagram of the degree of heterotacticity H as a function of the alternation probabilities for a polymer formed by the simple Markov mechanism.

It can be seen from Figure 2 that high syndiotacticity will be imparted to a polymer only when both alternation probabilities are so large that the polymer has no appreciable asymmetry. The degree of heterotacticity attains a maximum value 0.5 when $p_{\text{DD}} = p_{\text{DL}} = p_{\text{LD}} = p_{\text{LL}} = 1/2$, as can be seen in Figure 3.

In principle, comparisons of the above theoretical results with observations may be attempted for polymers, for which the configurational asymmetry can be measured. Although the tacticity measurements by the NMR technique have been reported for polymers of methyl methacrylate,⁷ α -methylstyrene,⁸ styrene,⁹ propene,¹⁴ and methyl vinyl ether,¹⁰ no tacticity data are available as yet for those polymers having optical activity.

B. Markov Chains with Penultimate Effects Included (k = 2)

When the configuration of the penultimate monomer unit also affects the selection of the configuration of adding monomer, there are eight possible elementary reactions of the type:

$$mXY + M \rightarrow mYZ$$

with instantaneous probabilities of transition p_{xyz} , where X, Y, and Z stand for either D or L. Since these eight parameters are subject to the four stochastic restrictions

$$p_{\rm XYD} + p_{\rm XYL} = 1 \tag{20}$$

only four of them are independent. Here we will choose p_{DDD} , p_{LLL} , p_{DLD} , and p_{LDL} as the independent parameters.

The fractions, $F_{XY}^{(2)}$, of the dyads XY existing in a polymer are equal to

the relative magnitudes (normalized to unity) of the diagonal minors of the 4×4 determinant

$$D = \begin{vmatrix} p_{\text{DDD}} - 1 & 0 & 1 - p_{\text{LDL}} & 0 \\ 1 - p_{\text{DDD}} & -1 & p_{\text{LDL}} & 0 \\ 0 & p_{\text{DLD}} & -1 & 1 - p_{\text{LLL}} \\ 0 & 1 - p_{\text{DLD}} & 0 & p_{\text{LLL}} - 1 \end{vmatrix}$$
(21)

where the dyads DD, DL, LD, and LL correspond to the rows from the top to the bottom, respectively. The results are

$$F_{\rm DD}^{(2)} = (1 - p_{\rm LLL})(1 - p_{\rm LDL})/A$$
 (22a)

$$F_{\rm LL}^{(2)} = (1 - p_{\rm DDD})(1 - p_{\rm DLD})/A$$
 (22b)

$$F_{\rm DL}^{(2)} = F_{\rm LD}^{(2)} = (1 - p_{\rm LLL})(1 - p_{\rm DDD})/A$$
 (22c)

where

$$A = (1 - p_{\text{LLL}})(1 - p_{\text{LDL}}) + (1 - p_{\text{DDD}})(1 - p_{\text{DLD}}) + 2(1 - p_{\text{LLL}})(1 - p_{\text{DDD}})$$
(23)

The expressions (22) are identical with those given by Miller³ and by Price.⁴

The fractional distributions, $F_{\rm D}^{(2)}$ and $F_{\rm L}^{(2)}$, of the D and L configurations are given by

$$F_{\rm D}^{(2)} = F_{\rm DD}^{(2)} + F_{\rm LD}^{(2)}$$
(24a)

$$F_{\rm L}^{(2)} = F_{\rm LL}^{(2)} + F_{\rm DL}^{(2)}$$
(24b)

respectively. The configurational asymmetry of a polymer is then expressed as

$$\omega_{\rm D} = F_{\rm D}^{(2)} - F_{\rm L}^{(2)} = F_{\rm DD}^{(2)} - F_{\rm LL}^{(2)}$$
(25)

which does not vanish unless the following relation holds:

$$(1 - p_{\text{LLL}})/(1 - p_{\text{DDD}}) = (1 - p_{\text{DLD}})/(1 - p_{\text{LDL}})$$
 (26)

Obviously, the Natta tacticities are

$$I_0 = F_{\rm DD}{}^{(2)} + F_{\rm LL}{}^{(2)} \tag{27}$$

$$S_0 = F_{\rm DL}{}^{(2)} + F_{\rm LD}{}^{(2)} = 1 - I_0 \tag{28}$$

while the tacticities consistent with Bovey's definition are

$$I = F_{\rm DD}{}^{(2)}p_{\rm DDD} + F_{\rm LL}{}^{(2)}p_{\rm LLL}$$
(29)

$$S = F_{\rm DL}{}^{(2)}p_{\rm DLD} + F_{\rm LD}{}^{(2)}p_{\rm LDL}$$
(30)

$$H = F_{\rm DD}{}^{(2)}p_{\rm DDL} + F_{\rm DL}{}^{(2)}p_{\rm DLL} + F_{\rm LD}{}^{(2)}p_{\rm LDD} + F_{\rm LL}{}^{(2)}p_{\rm LLD}$$

= 1 - I - S (31)

Again, the relations (14) hold, whether the Markov process under consideration is symmetric or not.

Thus we have only three independent physical quantities, ω_D , *I*, and *S*, related to four unknown parameters. In order to characterize the polymer, therefore, at least one more independent piece of experimental information is required.

IV. DISCUSSION

So far, considerations have been confined to the characterization of an asymmetric polymer which is formed at a single type of catalytic site. The situation becomes a bit more complex when one considers the possibility that a catalyst provides more than one type of active site participating in the propagation reaction, thus giving mixtures of polymer chains of various stereospecific properties. For instance, the fact that the formation of stereoregular polymer is often accompanied by the formation of a certain amount of amorphous polymer emphasizes the importance of this possibility. In the case where there are only two types of catalyst present, one giving amorphous and the other giving crystalline polymer, separation of the two polymer fractions permits the application of the theory to each fraction separately.

In discussing the mechanism of stereoregular polymerization by heterogeneous catalysts, Schuerch¹² first suggested the possibility that in some cases of catalysis giving isotactic polymer the propagation reaction at a particular catalytic site conforms to asymmetric statistics favoring either D or L configuration and that the entire sample of catalyst contains equal numbers of left- and right-handed sites. In the polymerization of *racemic* monomers, then, a "quasi-*racemic*" mixture of optically active polymer chains would be formed. If the quasi-*racemic* polymer formed could be optically resolved, it would be possible to characterize each of the quasienantiomorphic polymers by the present theory. Probably, the argument can be extended to include the situation that a catalyst may carry equal numbers of left- and right-handed sites with various abilities of stereoregulation.

In considering the possibility of Schuerch's "dual-site" mechanism, the experimental results of the copolymerization between D- and L-propylene oxides conducted recently by Tsuruta et al.¹³ are interesting. The enantiomeric monomer mixtures were copolymerized at various feed ratios by use of an optically inactive, yet stereospecific, catalyst (ZnEt₂—ROH). Optical activity of the gross polymer obtained was found to be proportional to that of the monomer feed, and the unreacted monomer mixture had the same optical activity as did the feed mixture. These results indicate that the apparent monomer reactivity ratios are $r_D = r_L = 1$ and, hence, that the chain growth as a whole obeys the Bernoullian statistics. Further, the polymer was fractionated with a solvent into crystalline and amorphous parts, which respectively showed higher and lower optical activities than would be expected from the observed mode of monomer consumption, i.e., the overall polymerization behavior obeying the Bernoullian statistics. These observations seem to be explainable only by assuming the presence

of equal numbers of D- and L-catalyst sites, each biased to select one configuration. Perhaps, the tacticity-asymmetry relations can be analyzed by the present theory when tacticity data become available.

Conceivably, there are some cases of asymmetric polymerization where the Markovian statistics breaks down. For example, the statistics is non-Markovian when a given catalytic site exists in more than one reactive state in dynamic equilibrium during the growth of a chain as in the mechanism proposed by Coleman and Fox¹⁴ for homogeneous anionic polymerization. The results of the present asymmetry considerations are, of course, not applicable to such non-Markovian processes.

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Résumé

On étend la théorie des probabilités des chaînes de Markov, utilisée pour la caractérisation des polymères stéréoréguliers, aux hauts polymères optiquement actifs. On exprime le degré de tacticité en fonction de la probabilité de transition d'une chaîne en croissance assymétrique, en tenant compte du choix de la configuration de l'unité monomérique. La variation de tacticité selon Bovey avec les paramètres de probabilité, est illustrée par des chaînes de Markov simples et assymétriques. On discute les relations entre la tacticité et l'assymétrie configurationnelle des polymères optiquement actifs.

Zusammenfassung

Die zur Charakterisierung von stereoregulären Polymeren angewendete Wahrscheinlichkeitstheorie von Markov-Ketten wird auf optisch aktive Hochpolymere ausgedehnt. Der Taktizitätsgrad wird durch die Übergangswahrscheinlichkeit für das Kettenwachstum, welche in Bezug auf die Auswahl der Monomerbausteinskonfiguration unsymmetrisch ist, ausgedrückt. Die Abhängigkeit der Taktizität nach Bovey von den Wahrscheinlichkeitsparametern wird für den Fall von asymmetrischen, einfachen Markov-Ketten gezeigt. Die Beziehungen zwischen Taktizität und Konfigurationsasymmetrie von optisch aktiven Polymeren werden diskutiert.

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Branching in Poly(butadiene-co-styrene). I. Branching Determined by Viscometry and Ultracentrifugation

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Synopsis

A sample of poly(butadiene-co-styrene), SBR, was divided into twelve fractious by precipitation from a dilute benzene solution. The intrinsic viscosities $[\eta]$ and weights of all the fractions were measured, and the sedimentation coefficients s_0 were determined for the nine fractions of highest molecular weight. From the values of $[\eta]$ and s_0 the number of crosslinks per molecule m, was calculated for each fraction. The results indicated that only the four fractions of highest molecular weight contained crosslinked molecules. The number of crosslinks per weight-average primary (prior to crosslinking) molecule for the entire sample, δ_0 , was obtained from the weights of the fractions and the values of m. By use of various theories, values of δ_0 of 0.78, 0.56, and 0.38 were obtained. From the values obtained for $[\eta]$ and s_0 and the pycnometric partial specific volume of the polymer in benzene, the molecular weights M of the nine fractions of highest $[\eta]$ were calculated. The molecular weights of the remaining fractions were calculated from the relation between M and $[\eta]$ obtained by others. A molecular weight distribution curve was established and used to obtain $\delta_0 \leq 0.36$.

INTRODUCTION

If poly(butadiene-co-styrene), SBR, is polymerized at a high temperature or to a high conversion, some of the polymer molecules will be branched. The occurrence of branching is revealed by the formation of an insoluble gel under certain polymerization conditions. Branching may involve either trifunctional or tetrafunctional units. Tetrafunctional branching is generally called crosslinking. According to the experimental results of Morton,¹ almost all the branching in SBR arises from crosslinking. Cragg and co-workers^{2,3} have examined the relative amounts of crosslinking in SBR polymerized under various conditions, and concluded that the Huggins' constant⁴ increases with the extent of crosslinking.

In the present paper a quantitative determination is made of the degree of crosslinking and the distribution of the crosslinks in a sample of SBR. Similar studies have been made by Thurmond and Zimm⁵ on polystyrene, by Guillet⁶ on polyethylene, and by Senti et al.⁷ on dextran.

To determine the number of crosslinks per molecule it is necessary to know the ratio of the intrinsic viscosity of the molecule to that of a linear molecule of the same molecular weight. In the present work, a relation between the intrinsic viscosity and the sedimentation coefficient is proposed to obtain this ratio. This method, in conjunction with several theories, can be used to estimate the degree of crosslinking in fractions of a sample of SBR. By using the weights of the fractions together with the degree of crosslinking in each fraction, the amount of crosslinking in the unfractionated sample can be calculated. From the experimentally determined molecular weight distribution another estimate can be made of the amount of crosslinking in the unfractionated sample. The results of these two methods have been compared with those obtained from a study of the radiolysis of SBR reported in another paper.⁸

THEORETICAL

The sedimentation coefficient s_0 is related to the molecular weight M and the molecular frictional coefficient f_0 , by the Svedberg equation:⁹

$$s_0 = M(1 - v_0 \rho_0) / N f_0 \tag{1}$$

In this equation ρ_0 is the density of the solvent and v_0 is the polymer partial specific volume. Flory has derived the relation¹⁰

$$f_{0} = \eta_{0} P'(\overline{S_{0}}^{2})^{1/2}$$
(2)

where η_0 is the solvent viscosity, P' is a "universal" constant, and $(\overline{S_0}^2)$ is the mean-square radius of gyration at the theta temperature. Another relation from the treatment of Flory^{*} is

$$[\eta] = \phi'[(\overline{S_0^2})/M]^{3/2}M^{1/2}$$
(3)

where ϕ' is also a "universal" constant. The ratio $(\overline{S_0}^2)/M$ is also a constant for a given polymer-solvent system.

The ratio of the mean-square radius of gyration of a branched molecule to that of a linear molecule of the same molecular weight is denoted by g, where g has been related¹³ to m, the number of cross-links per molecule.

It has frequently been assumed^{6,10} that eqs. (2) and (3) may be written for branched molecules in the form

$$(f_0)_{\rm br} = \eta_0 P'(\overline{S_0^2})^{1/2} g^{1/2}$$
(4)

$$[\eta]_{\rm br} = \phi[(\overline{S_0^2})/M]^{3/2} M^{1/2} g^{3/2}$$
(5)

Equation (5) indicates that

$$[\eta]_{\rm br}/[\eta]_{\rm lin} = g^{3/2} \tag{6}$$

Stockmayer and Fixman¹⁴ suggested that the effective hydrodynamic radius of a polymer molecule is less sensitive to branching than is the radius of gyration. They derived the relation

$$(f_0)_{\rm br} = P' \eta_0 (\overline{S_0^2})^{1/2} h \tag{7}$$

* The treatment of Flory is not entirely correct. Krigbaum and Carpenter,¹¹ for instance, found that ϕ' , decreases as the "goodness" of the solvent increases. Several theories¹² maintain that the chief reason for the discrepancy between Flory's theory and experiment is due to his assumption that the polymer segment density is Gaussian at all temperatures. Despite these objections Flory's theory is used here.

where h is the ratio of the effective hydrodynamic radius of a branched molecule to that of a linear molecule of the same molecular weight. They related h to g, and found that h is less sensitive to branching than is $g^{1/2}$. In view of the general experimental validity of eqs. (2) and (3) for linear polymers, they assumed that the ratio of effective hydrodynamic radii of branched to linear polymers obtained for the friction coefficient could also be used to discuss viscosity. This assumption leads to

$$[\eta]_{\rm br} = \phi' [(\overline{S_0}^2)/M]^{3/2} M^{1/2} h^3$$
(8)

and

$$[\eta]_{\rm br}/[\eta]_{\rm lin} = h^3 \tag{9}$$

Zimm and Kilb¹⁵ have recently derived the relation

$$[\eta]_{\rm br} / [\eta]_{\rm lin} = g^{1/2} \tag{10}$$

Equations analogous to eqs. (4) and (5) can be written

$$(f_0)_{\rm br} = \eta P'_{\rm br} (\overline{S_0}^2)^{1/2} g^{1/6}$$
(11)

$$[\eta]_{\rm br} = \phi'_{\rm br} [(\overline{S_0}^2)/M]^{3/2} M^{1/2} g^{1/2}$$
(12)

where P'_{br} and ϕ'_{br} might vary. The theories of Bueche¹⁶ and of Kotliar and Podgor¹⁷ are in good agreement with the last relation. Furthermore, the results of two investigations^{18,19} on monodisperse polystyrene support the Zimm and Kilb theory.

On combining eqs. (1), (2), and (3) for linear polymers one obtains

$$(s_0)_{\ln}[\eta]_{\ln^{1/3}}/M^{2/3} = (\phi')_{\ln^{-1/3}}(P')_{\ln^{-1}}(1 - v_0\rho_0)/\eta_0 N$$
(13)

where the subscript (lin) has been added to denote linearity. The term $(\phi')_{\text{lin}}^{1/3}(P')_{\text{lin}}^{-1}$ has been found experimentally to have the value 2.5×10^6 for linear flexible chain molecules.

For branched molecules, each of the three sets of eqs. (1), (4), and (5); (1), (7), and (8); and (1), (11), and (12) leads to

$$(s_0)_{\rm br}[\eta]_{\rm br}^{1/3}/M^{2/3} = (\phi')_{\rm br}^{1/3}(P')_{\rm br}^{-1}(1 - v_0\rho_0)/\eta_0 N$$
(14)

According to the theories of Flory and of Stockmayer and Fixman

$$(\phi')_{\rm br} = (\phi')_{\rm lin}$$

and

$$(P')_{\rm br} = (P')_{\rm lin}$$

Experiments with branched and linear dextrans⁷ indicate that the product $(\phi')^{1/4}(P')^{-1}$ is unaffected by branching. This finding leads to the assumption that

$$(\phi')_{\ln^{1/3}}(P')_{\ln^{-1}} = (\phi')_{br}(P')_{br}^{-1}$$

when interpreting results by using the Zimm and Kilb theory. If the value of M is the same in eqs. (13) and (14), then

$$(s_0)_{\rm lin}[\eta]_{\rm lin}^{1/3} = (s_0)_{\rm br}[\eta]_{\rm br}^{1/3}$$
(15)

At temperature greater than the theta temperature, eqs. (2) and (3) for linear molecules become 10

$$f_0 = [\eta_0] P'(\overline{S_0^2})^{1/2} \alpha \tag{16}$$

and

$$[\eta] = \phi'[(\overline{S_0}^2)/M]^{3/2}M^{1/2}\alpha^3 = KM^a$$
(17)

where α is the excluded volume factor and K and a are constants. On combining eqs. (1), (15), and (17), the excluded volume factor α cancels out and eq. (13) results. It can be assumed that α also cancels out in the case of branched molecules. Equations (6), (9), and (10) are strictly valid at the theta temperature only, but experimental evidence^{5,19} indicates that the use of temperatures above the theta temperature leads to negligible errors.

Eliminating M between eqs. (13) and (17) leads to

$$(\mathfrak{s}_0)_{\mathrm{lin}} = K_{\mathfrak{s}}[\eta]_{\mathrm{lin}}^{\gamma} \tag{18}$$

where K_s and γ are constants and

$$\gamma = (2 - a)/3a$$

Schumaker¹⁹ has derived a similar equation. Substituting eqs. (18) into eqs. (15) gives

$$K_{s}[\eta]_{\text{lin}}^{(3\gamma+1)/3} = (s_{0})_{\text{br}}[\eta]_{\text{br}}^{-1/3}$$
(19)

If γ , K_s , $(s_0)_{\rm br}$ and $[\eta]_{\rm br}$ are known, the value of $[\eta]_{\rm lin}$ can be obtained from this equation. From the ratio $[\eta]_{\rm br}/[\eta]_{\rm lin}$ a value of g can be calculated by using eqs. (6), (9), or (10). From g the number of crosslinks per molecule, m, can be obtained by using the Zimm and Stockmayer relation.¹³ The weight-average number of crosslinks per molecule, m_w , for the entire sample can be calculated from the weights of the fractions and the values of m for each fraction. The number of crosslinked units per weight-average primary molecule δ_0 is related^{5,14,15} to m_w by

$$m_{\omega} = \delta_0 / (1 - \delta_0) \tag{20}$$

There are several advantages to this method of finding g over that employing the molecular weight. In a sample containing highly crosslinked molecules there is likely to be some microgel. Even a very small amount of microgel will have a major effect on the accuracy of lightscattering experiments,²¹ but will have an insignificant effect in ultracentrifugation. Equation (4), (7), or (11) in conjunction with eq. (1) indicates that $(s_0)_{br}$ is greater than $(s_0)_{1in}$ while $[\eta]_{br}$ is less than $[\eta]_{1in}$. Therefore, the effect of branching is more pronounced when the quantities $[\eta]$ and s_0 are employed rather than $[\eta]$ and M.

EXPERIMENTAL

The SBR sample, obtained from the Polymer Corporation, Sarnia, Ontario, was prepared by emulsion polymerization and contained impurities of fatty acid soap, fatty acid, and Polygard antioxidant. The conversion was $70 \pm 2\%$. The manufacturers estimated that the styrene content was 28.7% and that 20% of the polybutadiene portion was vinyl-1,2, 7\% was cis-1,4, and 73\% was trans-1,4. According to Binder²² these values indicate that the polymerization temperature was about 5°C.

Reagent grade benzene and methanol obtained from Fisher Scientific Company were used as received. The antioxidant N-phenyl- β -naphthylamine, was obtained from Eastman Organic Chemicals.

Fractionation

The fractionation technique employed was almost identical to that developed by Cragg.²³ A solution of 15 g. of SBR in 1500 ml. of benzene was prepared in a 3-liter stoppered separatory funnel maintained at 25° C. in a constant temperature bath. A precipitant of 50% methanol in benzene was added to the solution with vigorous stirring until the solution became so turbid that the stirrer shaft was not visible in the illumination of a 100-w. light bulb held behind the bath. The temperature of the bath was increased very slowly with stirring, until the cloudiness just disappeared. At this point heating was stopped, and the bath was allowed to cool to 25° C. Stirring was then stopped, and the polymer phase allowed to precipitate for 24 hr. At the end of this period the precipitate was drawn off into a stoppered 100-ml. flask. A small amount of antioxidant was added and the volume made up to 100 ml. by the addition of benzene. The weight of each fraction was obtained by a freeze-drying technique. Twelve fractions were obtained in this manner.

Viscosity

A modified Ubbelohde viscometer, designed by Craig and Henderson²⁴ for a negligible kinetic energy correction, was used to measure the intrinsic viscosity of each fraction at 25 ± 0.05 °C. Dust was removed from the solvent, benzene, and from the solution by filtration through sintered glass. The validity of the method of dilution was established by the determination of the solids content after the final dilution.

To detect any dependence of viscosity on shear rate a four-bulb viscometer was also employed. This viscometer was a modified form of the suspended-level dilution capillary viscometer of Schurz and Immergut.²⁵

Partial Specific Volume

Fourteen density determinations were made over the concentration range 35.9-2.60 g./l. in a 25-ml. pycnometer, and the partial specific volume was calculated by Kraemer's formula.⁹

Ultracentrifugation

Sedimentation velocity measurements were made in a Spinco Model E ultracentrifuge equipped with Schlieren optics employing a Wolter phase plate as the opaque element. Throughout the experiments the rotor

temperature was maintained at $25 \pm 0.5^{\circ}$ C., the rotor speed was 59,000 rpm, and the phase plate angle was either 50° or 60°. Standard doublesector cells were used with solvent in one channel and solution in the other. In each sedimentation study about 12 photographs were taken at 16-min. intervals starting at some suitable time after the rotor had attained the desired angular velocity. Each fraction was examined at several concentrations between 0.7 and 0.1 g./100 ml. of solution. However, a few experiments were made at higher concentrations.

RESULTS

Fractionation

The weight of polymer in each fraction is given in Table I. These fractions are numbered according to the order in which they were precipitated. The sum of the weights is 11.76 g. After the withdrawal of the last fraction a small amount of polymer and impurities having a total weight of 1.47 g. remained in solution. Approximately 88% of the original 15 g. of sample can thus be accounted for. The amount of impurities in the starting material was determined by the standard method²⁶ and accounts for 6.73% of the sample. Therefore about 3% of the polymer remains in solution. Since the moisture content of the SBR was negligible, the loss in material must be related to adsorption of some of the polymer on the sides of the separatory funnel, and to errors in the pipet deliveries arising from the high viscosity of the polymer solution.

From the weights and intrinsic viscosities of the fractions the intrinsic viscosity of the unfractionated polymer was calculated to be 2.55. This value is slightly greater than 2.31 found by the direct measurement of the $[\eta]$ of the unfractionated polymer. This discrepancy indicates a loss of low molecular weight material during fractionation.

Viscosity

Linear plots of the reduced viscosity, η_{sp}/c , against concentration c were used to determine the intrinsic viscosity $[\eta]$ of the fractions. No shear rate effect was found, even for the fractions of highest $[\eta]$. The results of Table I show that $[\eta]$ steadily decreases from fractions 1 to 12.

Values of the Huggins' constant, k', given in Table I, were calculated from the slopes of the η_{sp}/c versus c plots by using the equation

$$\eta_{sp}/c = [\eta] + k'[\eta]^2 c \tag{21}$$

An accurate value of k' could not be calculated for fraction 12 because of major scatter in the plot of η_{sp}/c versus c. For fractions with high intrinsic viscosities k' tends to increase with $[\eta]$.

Another method of calculating $[\eta]$ employs a plot of $\ln \eta_\tau/c$ versus c, where η_τ is the relative viscosity. Values of $[\eta]$ obtained by this method were in good agreement with those obtained from plots of η_{sp}/c versus cfor fractions with k' < 0.30. For fractions with higher k' values, plots of

	Weight,			$s_0 \times 10^{13}$,		
Fraction	g.	$[\eta], \mathrm{dl.}/\mathrm{g.}$	k', g./dl.	sec.	$k_s/[\eta]$	$M imes 10^{-3}$
1	0.477	5.38	0.742	4.63	2.24	1,168
2	1.120	5.13	0.593	4.41	2.29	1,058
3	0.777	4.30	0.414	3.39	2.15	656
4	0.765	3.65	0.341	2.85	2.06	464
5	0.862	3.18	0.333	1,91	1.28	238
6	1.310	2.59	0.274	1.65	1.47	174
7	1.254	2.19	0.248	1.44	1.50	128
8	1.294	1.81	0.244	1.29	1.69	99.2
9	1.360	1.48	0.289	1.21	1.97	81.9
10	1.385	1.10	0.267			57.7
11	0.980	0.786	0.237			36.9
12	0.190	0.632				27.6

 TABLE I

 Solution Properties and Molecular Weights of the Fractions

 $\ln \eta_{\tau}/c$ versus c were nonlinear and on extrapolation to zero concentration gave higher values of $[\eta]$ than those obtained by the first method. Mac-Farlane and McLeod²⁷ have explained this disagreement, and have shown that plots of η_{sp}/c versus c give the correct values of $[\eta]$.

Ultracentrifugation

Single symmetrical peaks were obtained for all the fractions. Unfortunately, peak movement could not be accurately measured for fractions 10, 11, and 12 because the peaks were too small and blurred. The maximum-ordinate sedimentation coefficient s was obtained from linear plots of log X_m versus time, where X_m is the distance of the maximum ordinate from the center of the rotor.²⁸

Since the density and viscosity of benzene are sensitive to pressure, the value of the sedimentation coefficient will depend on pressure. A correction for this effect has been proposed by Oth and $Desreux^{29}$ in the equation

$$s_p = s(1 - \mu P) \tag{22}$$

where s_p is the sedimentation coefficient uncorrected for pressure, s is the value at one atmosphere pressure, P is the pressure at that point in the cell at which s_p was measured, and μ is a factor which depends on the sensitivity of the solvent viscosity and density to pressure. The value of μ was calculated from the data of Baldwin and Van Holde.³⁰ It was found that $(1 - \mu P) = 1.04 \pm 0.01$.

Plots of 1/s versus concentration c gave straight lines, as is illustrated in Figure 1 for fraction 4. The sedimentation coefficient at zero concentration s_0 was obtained by extrapolation, and k_s was calculated by using the equation

$$1/s = (1/s_0)(1 + k_s c) \tag{23}$$

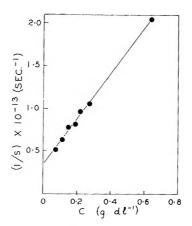


Fig. 1. Dependence of the sedimentation coefficient on concentration for fraction 4.

Values of s_0 and $k_s/[\eta]$ are given in Table I. The value of s_0 steadily increases with intrinsic viscosity, whereas $k_s/[\eta]$ increases in an irregular manner.

Because the peaks were somewhat blurred, only Gralen's method³¹ could be used to estimate the polydispersity of each of the fractions. The ratio of the area under the sedimentation curve to the maximum ordinate, X_m , was plotted against X_m for a particular concentration to give a straight line. Extrapolation of a plot of the slopes of these lines versus concentration gave the slope at zero concentration. This slope has been related to the ratio of the weight-average molecular weight \overline{M}_w to the number-average molecular weight M_n . For all the fractions $\overline{M}_w/\overline{M}_n$ was found to be 1.03 \pm 0.01. This represents an unexpectedly low degree of poly-dispersity considering that only twelve fractions were obtained.

Molecular Weight

The molecular weights of the first nine fractions were calculated by using eq. (13) or (14). As eq. (15) indicates, both equations give the same value of M. The results are presented in Table I. The partial specific volume v_0 was found to be 0.995 \pm 0.005 at 25°C. The viscosity of the solvent η_0 was 6.024 mpoises and its density ρ_0 was 0.8735 g./ml., both at 25°C. These values together with $(\phi')^{1/4}(P')^{-1} = 2.5 \times 10^6$ were used in calculating M.

Values of M for the last three fractions were calculated from

$$[\eta] = 2.95 \times 10^{-4} M^{0.71} \tag{24}$$

This equation was determined³² for fractions of "cold" SBR. In a following section it is shown that the molecules of the last three fractions are linear; therefore, eq. (24) can be used to calculate their molecular weight. If the molecules were branched, M determined by using eq. (24) would be less than the true value.

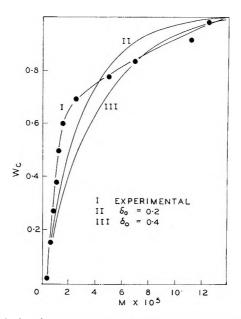


Fig. 2. Theoretical and experimental molecular weight distribution curves.

From the values of M and the weights of the fractions, the molecular weight distribution curve given in Figure 2 was established. For comparison, Kilb's³³ theoretical distribution curves are shown for several values of δ_0 , the number of crosslinked units per weight average primary molecule. Neither of the theoretical distributions agree with the experimentally determined distribution: they indicate less low molecular weight and less high molecular weight material than is found experimentally.

A value of the ratio $\overline{M}_w/\overline{M}_n = 2.84$ was calculated from the expression

$$\frac{\overline{M}_w}{\overline{M}_n} = \frac{\sum (dW_c/dM)M \sum (dW_c/dM)/M}{\sum (dW_c/dM)^2}$$
(25)

where W_c is the cumulative weight.

Degree of Crosslinking

Figure 3 shows the plot of $\log s_0$ versus $\log [\eta]$ for the nine fractions of highest molecular weight. The results for five of these fractions can be fitted to a straight line described by the equation

$$s_0 = 0.944 \, [\eta]^{0.61} \tag{26}$$

Therefore, in eq. (18), $K_s = 0.944$ and $\gamma = 0.61$. By using these values in eq. (19) together with the appropriate values of s_0 and $[\eta]$, the ratios $[\eta]_{br}/[\eta]_{1in}$ for each of the four fractions of highest molecular weight were obtained. Values of g were calculated according to the three theories represented by eqs. (6), (9), and (10). The three series of m values given in Table II were then obtained by using the Zimm and Stockmayer theory.¹³

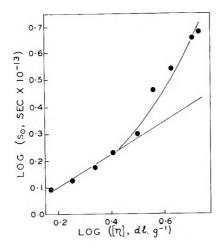


Fig. 3. The dependence of the sedimentation coefficient at zero concentration, s_0 , on $[\eta]$.

From the results given in Table II it is evident that the branching frequency, represented by the ratio m/M, increases with molecular weight as predicted by theory.³³ Three values of the weight-average number of crosslinks per molecule, m_w , were calculated by using the appropriate values of m and the weights of the fractions. The value of m_w calculated by the Zimm-Kilb theory, eq. (10), is about six times greater than that based on Flory's theory, eq. (6), and about three times greater than that based on the Stockmayer-Fixman theory, eq. (9). Finally, three values of δ_0 , given in Table II, were obtained by substituting m_w into eq. (20).

		m				
Fraction	$[\eta]_{ m br}/[\eta]_{ m lin}$	Zimm-Kilb	Stockmayer-Fixman	Flory		
1	0.544	21.3	6.4	2.7		
2	0.558	19.0	5.9	2.5		
3	0.661	8.4	3.8	1.7		
4	0.712	5.4	2.9	1.3		
5	1.000	0	0	0		
w		3.58	1.26	0.55		
		0.78	0.56	0.38		

TABLE II Degree of Crosslinking in Each Fraction

Another value of δ_0 was calculated from the relation 33

$$\overline{M}_{w}/\overline{M}_{n} = \left[2 - (\delta_{0}/2)\right]/(1 - \delta_{0})$$
(27)

From the experimentally determined result of $\overline{M}_w/\overline{M}_n = 2.84$, the value $\delta_0 = 0.36$ was obtained. This method of calculating δ_0 is valid only if the primary molecular weight distribution is the "most probable." If it is broader, δ_0 will be overestimated.

DISCUSSION

One of the most frequently used branching parameters is Huggins' constant, k'. There is, however, considerable doubt as to whether an increase in k' does actually indicate the occurrence of branching and not simply an increase in polydispersity³⁴ or in molecular orientation.³⁵ In the present study a change in shear rate had no effect on k', and therefore the latter possibility can be excluded. According to Cleverdon,³⁶ the degree of polydispersity of the fractions increases with the relative molecular weight, and so the increase in k' that we observe might result from a change in polydispersity. However, the value of k' for the unfractionated polymer is 0.42 which is less than for the four fractions of highest molecular weight. In this particular study, therefore, the increase in k' can be attributed to branching. The corresponding increase in m, the number of crosslinks per molecule, supports this conclusion.

Others^{18,13} have also found that k' increases with branching; however, experiments have been reported 37,38 in which k' is independent of branching. Manson and Cragg³⁷ have suggested that only certain types of branching affect k' and that branching which has only a small influence on the segment density distribution of the molecule will have no effect on k'. Apparently the type of branching which occurs in SBR has a large influence on the segment density distribution.

Wales and Van Holde⁴⁰ have used the theories of Burgers³⁹ and of Flory¹⁰ to derive the relation

$$k_s/[\eta] = 1.66$$

From the derivation this relation should be valid for both linear and branched molecules; however, its validity, even for linear molecules, is in doubt.⁴¹ Wales and Van Holde⁴⁰ claim that k_s is characteristic of the low molecular weight components of a sample. Therefore, considering that $[\eta]$ is characteristic of the high molecular weight components, $k_s/[\eta]$ should decrease with increasing polydispersity. The high molecular weight fractions are expected to be more polydisperse than the low molecular weight fractions, and so the increase in $k_s/[\eta]$ with molecular weight cannot be due to polydispersity. Although the effect of branching on k_s has not been examined theoretically, the results of Moore et al.⁴² indicate that k_s is less for a branched molecule than for a linear molecule of the same molecular weight. The large values of $k_s/[\eta]$ found in the present work suggest that branching decreases $[\eta]$ to a greater extent than it does k_s .

A quantitative estimate of the degree of branching in a particular sample of SBR is the main concern of this investigation. To make this estimate the following four assumptions had to be made: (1) molecular nonlinearity is the result of crosslinking, not trifunctional branching; (2) if the crosslinks were destroyed a "most probable" molecular weight distribution would result; (3) the crosslinks occur at random; and (4) the fractions are monodisperse. As previously mentioned, Morton's results indicate that crosslinking is the chief cause of molecular nonlinearity.

The analysis of Booth and Beason⁴³ shows that the primary molecular weight distribution of SBR is only slightly broader than the "most probable" type. Flory¹⁰ claims that a small amount of nonrandom cross-linking might occur, but only to a significant extent at conversions greater than that used in preparing the present sample.

The fourth assumption, that the fractions are monodisperse, is definitely not valid. Both theoretically and experimentally it has been shown that the degree of polydispersity increases with the relative molecular weight of the fractions.³⁶ It is not known whether branched molecules differ in solubility from linear molecules of the same molecular weight. If there is a solubility difference the polydispersity of the high molecular weight fractions might be greater than that occurring in the fractionation of linear molecules.

From Gralen's method the degree of polydispersity in the fractions is found to be very low; $\overline{M}_w/\overline{M}_n \simeq 1.03$. There are several reasons for regarding these results sceptically. One of the assumptions in this method is that no diffusion occurs; but Eriksson⁴⁴ has shown that a correction must be made for diffusion. The extent of such a correction for the present system is unknown. According to several experiments⁴⁵ on other polymers, the dependence on concentration of the slope of (area/ X_m) versus X_m increases with decreasing concentration. Therefore, by the failure to use sufficiently low concentrations the value of the slope at zero concentration would be too small. This underestimation would give a value of M_w/M_n which is less than the true value.

The effect of polydispersity on the experimentally determined molecular weight distribution and the values of m and δ_0 will depend on the molecular weight distribution of the fractions, on how the molecular weight distribution changes with the molecular weight of the fractions, and on how the branched molecules are distributed in the fractions.* Without this information it is impossible to estimate the nature of the errors in either the molecular weight distribution or in the values of m and δ_0 . The large discrepancy between the theoretical and the experimental molecular weight distribution curves shown in Figure 2 is probably due to polydispersity of the fractions. Apparently, this polydispersity causes the experimentally determined molecular weight distribution to overestimate the amount of low and high molecular weight material. If another method, light scattering, for example, was used to measure the molecular weight, the nature of the errors in the molecular weight distribution might be radically different. Even if the molecular weight distribution is subject to a very large error, the values of m or δ_0 might be subject to a very much smaller error.

A following paper⁸ describes the changes in solubility and swelling

^{*} The results of Thurmond and Zimm⁵ for crosslinked polystyrene have been used to test the validity of several theories.^{5,14,16} Unfortunately, only nine fractions were collected and therefore the importance of polydispersity is greater than in the present case.

resulting from the exposure of SBR to γ -radiation. The results strongly indicate that $\delta_0 \simeq 0.9$. If this is the correct value, it can be concluded that δ_0 based on the experimentally determined molecular weight distribution is too low, and that the three theories represented by eqs. (6), (9), and (10) overestimate the effect of branching on intrinsic viscosity. Of the three theories that of Zimm and Kilb gives the most accurate value of δ_0 ; however, because the effect of polydispersity of the fractions is unknown the validity of even this theory is not definitely established.

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Résumé

Un échantillon de poly(butadiène-co-styrène), SBR, a été divisé en douze fractions par précipitation à partir d'une solution benzénique diluée. Les viscosités intrinséques, $[\eta]$ et les poids de toutes les fractions ont été mesurés, et les coefficients de sédimentation, se, ont été déterminés pour les neuf fractions possédant les poids moléculaires les plus élevés. A partir des valeurs de $[\eta]$ et de s_o , le nombre de ramifications par molécule, m, a été calculé pour chaque fraction. Les résultats indiquent qu'il n'y a que les quatre fractions de poids moléculaires les plus élevés qui contiennent des molécules ramifiées. Le nombre de ramifications par molécule primaire de poids moyen (avant la ramification) pour l'échantillon entier, d_o , a été obtenu à partir des poids des fractions et des valeurs de m. En utilisant diverses théories, on a obtenu des valeurs de d_a de 0.78, 0.56 et 0.38. A partir des valeurs obtenues pour $[\eta]$ et s_o et du volume spécifique partiel pycnométrique du polymère dans le benzène, on a calculé les poids moléculaires, M, des neuf fractions possédant une $[\eta]$ le plus élevé. On a calculé les poids moléculaires des fractions restantes par la relation entre M et $[\eta]$ obtenue par d'autres méthodes. On a dressé une courbe de distribution du poids moléculaire et on l'a utilisée pour obtenir de $\leq 0.36.$

Zusammenfassung

Eine Poly(butadien-co-styrol)-Probe, SBR, wurde durch Fällung aus einer verdünnten Benzollösung in zwölf Fraktionen zerlegt. Die Viskositätszahl, $[\eta]$, und das Gewicht aller Fraktionen wurden gemessen und für die neun Fraktionen mit dem höchsten Molekulargewicht der Sedimentationskoeffizient s_0 bestimmt. Aus den Werten von $[\eta]$ und s_0 wurden für jede Fraktion die Zahl der Vernetzungsstellen pro Molekül, m, berechnet. Die Versuchsergebnisse zeigen, dass nur die vier Fraktionen mit dem höchsten Molekulargewicht vernetzte Moleküle enthalten. Die Zahl der Vernetzungsstellen pro Gewichtsmittel des primären (vor der Vernetzung) Moleküls dür die gesamte Probe, δ_0 , wurde aus den Fraktionsgewichten und den m-Werten erhalten. Nach verschiedenen theoretischen Ansätzen wurden δ_0 -Werte von 0,78, 0,56, und 0,38 erhalten. Aus den erhaltenen $[\eta]$ -und s_0 -Werten sowie dem pyknometrischen, partiellen spezifischen Volumen des Polymeren in Benzol wurden die Molekulargewichte, M, der neun Fraktionen mit dem höchsten $[\eta]$ -M-Beziehung erhalten. Eine Molekulargewichtsverteilungskurve wurde aufgestellt und damit $\delta_0 \leq 0,36$ erhalten.

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Branching in Poly(butadiene-co-styrene). II. Radiation-Induced Branching Examined by Viscometry

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Synopsis

The dependence of intrinsic viscosity on radiation dose has been examined for poly-(butadiene-co-styrene) irradiated *in vacuo* and for mixtures of this polymer and Nphenyl- β -naphthylamine irradiated in air and *in vacuo*. If no correction is made for crosslinking in the unirradiated polymer, theories examined appear to overestimate the increase in intrinsic viscosity. However, if it is assumed that in the unirradiated polymer the number of crosslinked units per weight-average primary molecule δ_0 is 0.65, the results agree with the theory of Spiro which uses the Stockmayer-Fixman relation between intrinsic viscosity and branching. The dose required for incipient gelation, R_{ρ} , was determined for the various samples. These results were used together with the number-average molecular weight of the unirradiated polymer and with assumed values of δ_0 to calculated values of G_z , the number of crosslinks formed per 100 e.v. of radiation energy absorbed by the sample. Good agreement with solubility and swelling results, reported elsewhere, was obtained if $\delta_0 = 0.9$.

INTRODUCTION

Any one or any combination of the following reactions might occur on irradiating a polymer: degradation, crosslinking, cyclization, endlinking, and crosslinking by a chain reaction. The composition and environment of the polymer determine which of these reactions will occur. The nature of the changes in solution properties produced by irradiation aids in distinguishing between these possible reactions. In a forthcoming paper¹ the radiation-induced changes in solubility and swelling of SBR are examined, and it is concluded that at doses several times greater than the dose for incipient gelation R_g , only crosslinking or endlinking occurs. On studying the molecular weight changes caused by irradiating polystyrene of various molecular weight distributions Spiro has concluded that no endlinking occurs.² In the present work it is assumed that this conclusion is applicable to SBR.

This paper deals with the radiation-induced changes in the intrinsic viscosity of pure poly(butadiene-co-styrene) and the same polymer containing various amounts of N-phenyl- β -naphthylamine. The viscosity results are compared to those predicted by Katsuura,³ Kilb,⁴ Kotliar,⁵ and Spiro.⁶

In interpreting the results it was necessary to consider that the unirradiated polymer contained crosslinked molecules. The extent of this crosslinking has been investigated elsewhere.^{1,7}

EXPERIMENTAL

Materials

The SBR sample was obtained from Polymer Corporation, Sarnia, Ontario. It was prepared by emulsion polymerization at approximately 5°C. and contained impurities of fatty acid soap, fatty acid, and Polygard antioxidant. The molecular weight distribution and extent of crosslinking of this same sample were investigated in a previous paper.⁷

Reagent grade benzene and methanol (Fisher) were used in all the experiments. The antioxidant N-phenyl- β -naphthylamine was obtained from Eastman Organic Chemicals and will be denoted by B.

Sample Preparation

The impurities in the SBR were separated from the poly(butadiene-costyrene) by precipitating the polymer with methanol from a dilute solution of SBR in benzene. The concentration of methanol needed for complete precipitation of the polymer was sufficiently low that all the impurities remained soluble. To avoid oxidation the entire purification was accomplished in a nitrogen atmosphere. Upon precipitating the polymer, the supernatant liquid was withdrawn and the polymer redissolved in benzene. Following reprecipitation and removal of the supernatant liquid, the polymer was washed with methanol. The purified polymer was dissolved in benzene and a known quantity of antioxidant, B, added. The solution was frozen, placed in a vacuum desiccator and freeze-dried. From the weight of dry polymer plus B and the known weight of B the percentage of B in the polymer was calculated. The samples were stored at 0°C. in a vacuum and in the dark.

Irradiation Technique

Samples were placed in Pyrex tubes and evacuated at 1 μ for at least two days to ensure the removal of all the benzene. At a pressure of 0.1 μ the tubes were sealed and irradiated in a Co⁵⁰ gamma-cell manufactured by Atomic Energy of Canada Limited. The electron densities and electron fractions of the polymer and antioxidant were used in calculating the dose received by the samples. In making these calculations the value of wfor air was taken as 34 e.v. The dose rate varied from 6.0 to 5.2 Mrad/hr. during the period of experimentation. The pure polymer was irradiated *in vacuo*, and the polymer containing antioxidant, B, was irradiated both *in vacuo* and in air.

Determination of R_{g} and $[\eta]$

The dose for incipient gelation R_g was determined by noting the dose required to cause a benzene solution of the irradiated polymer to block a sintered glass filter. This method was subject to several possible sources of error. A small quantity of gel might block such a small fraction of the area of the sintered glass that its presence might not be detected. Furthermore, if a small amount of gel is present in the form of small aggregates it might pass through the pores of the filter. At doses only slightly less than R_g the intrinsic viscosity of some of the molecules is very high; therefore, slow filtration might be caused by this high viscosity rather than by the presence of gel. Because of these possible sources of error the accuracy of R_g is probably only about 10% and the precision 5%.

The intrinsic viscosities of samples were determined as previously described.⁷

RESULTS

Dose for Incipitant Gelation, R_{g}

The values of R_{g} obtained by the filtration technique are given in Table I. They refer to the dose adsorbed by the entire sample, not simply by the pure polymer. A discussion of the effect of antioxidant and of air on R_{g} will be given in a future paper.⁸

 G_z is defined as the number of crosslinks formed per 100 e.v. of radiation energy absorbed by the sample. This quantity is related to R_g and the weight-average molecular weight of the unirradiated polymer, \overline{M}_w , by⁹

$$G_x = 0.48 \times 10^6 / R_g \overline{M}_w \tag{1}$$

The number-average molecular weight of the unirradiated polymer, \overline{M}_n , is related to \overline{M}_w by⁹

$$\overline{M}_{w}/\overline{M}_{n} = [2 - (\delta_{0}/2)]/(1 - \delta_{0})$$
⁽²⁾

where δ_0 is the number of crosslinked units per weight-average primary molecule. (Two crosslinked units are equivalent to a crosslink, and primary molecules result from the breaking of the crosslinks.) By osmometry^{*} it was found that $\overline{M}_n = 89,900$. However, the correct value of δ_0 is in doubt.

In a previous investigation⁷ the molecular weight distribution of the polymer was determined, and from this distribution it was estimated that δ_0 = 0.36. In the same investigation, values of δ_0 were calculated from the solution properties and weights of the fractions in conjunction with several theories. Flory's theory¹⁰ gave $\delta_0 = 0.38$, the theory of Stockmayer and Fixman¹¹ gave $\delta_0 = 0.56$, and the theory of Zimm and Kilb¹² gave $\delta_0 =$ 0.78. A study¹ of the effect of radiation on the solubility of the polymer

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* The osmotic pressure data were supplied by the Pulp and Paper Research Institute of Canada.

indicated that $\delta_0 = 0.9$. Three of these possible values of δ_0 have been used in eq. (2) to give values of \overline{M}_w which in turn have been substituted into eq. (1) with the various values of R_g to give three series of G_x values. The complete results are presented in Table I. As δ_0 increases G_x decreases: for the pure polymer $G_x = 9.41$ if $\delta_0 = 0.0$, but $G_x = 1.72$ if $\delta_0 = 0.9$.

		G_x , crosslinks/100 e.v. absorbed				
В, %	R_{g} , Mrad	,	$\delta_0 = 0.78,$ $\overline{M}_w = 2.4 \times 10^5$			
0	0.20	9.41	3.33	1.72		
0.5	0.54	3.49	1.24	0.64		
2.1, 5.3	0.69	2.73	0.96	0.50		
7.1, 11.3	0.69	2.73	0.96	0.50		
60.0	1.00	1.88	0.67	0.35		
0ª	1.69	3.18	1.13	0.59		
2.7ª	0.53	1.00	0.36	0.18		

	TABLE I	
Dependence of R_g , G_x ,	and \overline{M}_w on δ_0 and	Content of Antioxidant B

* Irradiated in air.

If \overline{M}_w is determined experimentally it is not necessary to know δ_0 to calculate G_x because the product $R_g \overline{M}_w$ is independent of δ_0 . However, the determination of \overline{M}_w by light scattering is often unreliable,¹³ particularly for branched polymers.¹⁴

Intrinsic Viscosity

An investigation was made of the possible errors in $[\eta]$ arising from microgel, oxidation, and filtration. Samples irradiated to doses near but less than R_q were analyzed for microgel by shaking the solutions with finely

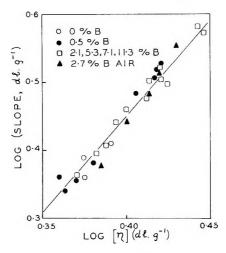


Fig. 1. Plot of log of the slope of η_{sp}/c versus c as a function of $[\eta]$.

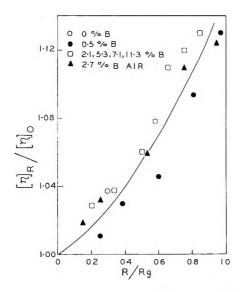


Fig. 2. The dependence of $[\eta]_{R}/[\eta]_{0}$ on R/R_{g} .

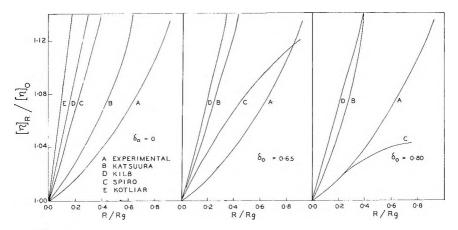


Fig. 3. A comparison between the theoretical and experimental dependence of $[\eta]_R/[\eta]_0$ on R/R_{ϱ} .

divided calcium sulfate.¹⁵ No microgel was detected. To remove small particles of dust, the solutions were filtered through sintered glass prior to viscosity measurements. Even for samples irradiated to doses close to R_g the intrinsic viscosity was unaffected by filtration. Although SBR is readily oxidized, an increase in the oxygen content of the polymer (determined by Alfred Bernhardt, Max Planck Institute) from 0.12% to 0.46% had no effect on the change in $[\eta]$ caused by irradiation. One week of exposure to air at room temperature was required to increase the oxygen content of the pure polymer to 0.46%. The pure polymer samples studied for radiation effects were never exposed to air for longer than ten minutes.

Values of $[\eta]$ were obtained from linear plots of η_{sp}/c versus concentration c, as has previously been described.⁷ In Figure 1 the log of the slopes of the plots of η_{sp}/c versus c are plotted against the corresponding $[\eta]$ values for all the samples examined. The straight line obtained can be fitted to the equation

$$\eta_{sp}/c = [\eta] + k'[\eta]^2 c \tag{3}$$

where

$$k' = 0.223 \ [\eta]^{0.75} \tag{4}$$

The Huggins' constant,¹⁶ k' has generally been found to be independent of $[\eta]$ for linear polymers.

Figure 2 shows the effect of irradiation on the intrinsic viscosity for doses up to R_q . The intrinsic viscosity of the unirradiated polymer is denoted by $[\eta]_0$ and that of the irradiated polymer by $[\eta]_R$. The scatter of the points is probably the result of errors in R_q , rather than of errors in $[\eta]$ or R. Figure 3 compares the results with theory for three assumed values of δ_0 . When δ_0 is zero, all four theories predict much higher values of $[\eta]_R/[\eta]_0$ than are obtained experimentally. This same discrepancy exists for three of the theories when $\delta_0 = 0.65$ or 0.80; but the theory of Spiro⁶ is in good agreement with experiment at $\delta_0 = 0.65$ and even underestimates $[\eta]_R/[\eta]_0$ at $\delta_0 = 0.80$.

All theories have been applied assuming the exponent in the Mark-Houwink relation is 0.68. This value is close to that of 0.71 determined¹⁷ for "cold" SBR. According to the theories differences of this magnitude are insignificant. A further assumption is that crosslinking alone occurs on irradiation.

DISCUSSION

Huggins' constant k' is one of the most frequently reported but least understood parameters in the treatment of the solution properties of polymers. Among the factors attributed to an increase in k' are an increase in molecular orientation,¹⁸ in branching,¹⁹ and in polydispersity.¹⁰ For certain polymers an increase in one of these variables definitely causes an increase in k', but for other polymers no such relation is observed. In a previous investigation⁷ it was concluded that branching in SBR increases k'. Therefore, the increase in k' found in the present work and expressed by eq. (4) can be assumed to reflect branching and possibly other factors.

The applicability of eqs. (1) and (2) and of the four theories represented in Figure 3 involves several assumptions concerning the effect of the radiation on the polymer and the properties of the unirradiated polymer. One of these assumptions is that branching in the unirradiated polymer must be caused by crosslinking imposed randomly upon a "most probable" molecular weight distribution. According to Morton,²¹ almost all the branching in SBR is caused by crosslinking. Booth and Beason²² have

shown that the primary molecular weight distribution in SBR is only slightly broader than the "most probable" type. The occurrence of a small amount of nonrandom crosslinking in SBR has been suggested by Flory,¹⁰ but it is only significant at conversions greater than that used for the present polymer sample.

The validity of assuming that only crosslinking occurs on irradiation has already been discussed. The absence of degradation has been established for high dcses; however degradation might occur at low doses. In the present paper it is assumed that degradation is absent at all doses. Solubility results¹ have indicated that SBR irradiated in air undergoes a small amount of degradation with a ratio of scissions to crosslinks of 0.25. Figure 2 shows that, within experimental error, this amount of degradation does not affect the shape of the plot of $[\eta]_R/[\eta]_0$ versus R/R_g . This insensitivity is consistent with theory and has been thoroughly investigated by Kilb.²³

The final assumption, that the crosslinking caused by the irradiation occurs at random, is valid for polystyrene and for polybutadiene, and since styrene units in SBR are distributed at random it is likely that crosslinking will occur at random.¹⁰ Witt's solubility²⁴ results support the occurrence of random crosslinking, since the shape of his plots of sol fraction versus dose are independent of the styrene content of SBR.

Witt²⁴ also found $G_x = 1.70$ for SBR containing 28% styrene and $G_x = 1.15$ for 38% styrene. He obtained \overline{M}_w by light scattering and therefore did not need δ_0 to calculate G_x . However, light scattering generally gives a value of \overline{M}_w which is high; therefore, Witt's G_x values are probably low. The present sample contained 28.7% styrene, and on the basis of Witt's results G_x should be slightly less than 1.70. Table I gives $G_x = 1.72$ for $\delta_0 = 0.90$ and $G_x = 3.33$ for $\delta_0 = 0.56$. Assuming Witt's results are correct it can be concluded that $\delta_0 = 0.90$. This is the same result as obtained from solubility data.¹

The theories which predict the dependence of intrinsic viscosity on dose are very complicated. Any such theory must consider the following problems.

(1) For the relation between the number of crosslinks per molecule m and the ratio of the radius of gyration of a crosslinked molecule to that of a linear molecule of the same molecular weight, denoted by g, theories have been proposed by Kataoka²⁵ and by Zimm and Stockmayer.²⁶ For a given value of g, Kataoka predicts a higher value of m.

(2) For the relation between g and the ratio of the intrinsic viscosity of a crosslinked molecule to that of a linear molecule of the same molecule weight, $[\eta]_{36}/[\eta]_{1in}$, four main theories have been proposed. Those of Flory,¹⁰ Katsuura,³ Zimm and Kilb,¹² and Stockmayer and Fixman¹¹ are represented by eqs. (5), (6), (7), and (8), respectively,

$$[\eta]_{\rm br} / [\eta]_{\rm lin} = g^{3/2} \tag{5}$$

$$[\eta]_{\rm br} / [\eta]_{\rm lin} = g^{2-a} \tag{6}$$

$$[\eta]_{\mathrm{br}}/[\eta]_{\mathrm{lin}} = g^{1/2}$$

$$\tag{7}$$

$$[\eta]_{\rm br}/[\eta]_{\rm lin} = h^3 \tag{8}$$

where a is the exponent in the Mark Houwink equation and h is a function of g.

(3) Theories treating the problem of the effect of crosslinking on the molecular weight distribution have been proposed by Kotliar,⁵ Kilb,⁴ Schultz,²⁷ Zimm and Stockmayer,²⁶ Katsuura,³ and Spiro.⁶

Considering that one theory from each of the three groups must be used in calculating the dependence of $[\eta]_R/[\eta]_0$ on R/R_g there are forty-eight possible combinations and therefore this number of possible theories relating these two ratios. The four combinations considered in the present work have been derived in detail and have received some experimental support. Of these four only that derived by Katsuura uses the relation between g and m proposed by Kataoka. To relate g to $[\eta]/[m]_{\text{lin}}$ Katsuura used eq. (6), Kotliar used a relation similar to eq. (7), Kilb used eq. (7), and Spiro used eq. (8). The four combinations involve different theories for relating crosslinking to changes in molecular weight distribution; however, the theories employed by Kilb and Spiro are almost identical.

As Figure 3 shows, only Spiro's theory agrees with the present experimental results. The major difference between this theory and the others is that it involves the Stockmayer-Fixman relation, eq. (8). The use of this relation leads to the prediction that the ratio $[\eta]_R/[\eta]_0$ is almost independent of dose when the extent of crosslinking is great. The other relations lead to the prediction that $[\eta]_R/[\eta]_0$ increases approximately exponentially with extent of crosslinking. The results of the present work suggest that the Stockmayer-Fixman relation is correct. Furthermore, the result $\delta_0 = 0.65$ agrees well with $\delta_0 = 0.56$ calculated from the solution properties of the fractions⁷ as interpreted by the Stockmayer-Fixman relation. On the other hand, solubility results¹ strongly support $\delta_0 = 0.9$; this is close to the value 0.78 obtained using the Zimm-Kilb relation to interpret the fraction data. The Stockmayer-Fixman relation might be correct only at high extents of crosslinking, and another relation such as that proposed by Zimm and Kilb might be correct at lower values.

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Résumé

On a examiné la dépendance de la viscosité intrinsèque vis-à-vis de la dose de radiation pour le poly(butadiène-co-styrène) irradié sous vide et pour des mélanges de ce polymère et de N-phényl- β -naphthylamine irradiés à l'air et sous vide. Si aucune correction n'est faite pour le pontage dans le polymère non-irradié, les théories examinées paraissent surestimer l'augmentation de la viscosité intrinsèque. Cependant si on admet que dans le polymère non-irradié, le nombre d'unités pontées par molécule primaire de poids moyen, δ_o , est 0.65, les résultats concordent avec la théorie de Spiro qui utilise la relation de Stockmayer-Fixman entre la viscosité intrinsèque et la ramification. La dose requise pour le début de gélification, R_o , a été déterminée pour divers échantillons. Ces résultats ont été utilisés en combinaison avec le poids moléculaire moyen en nombre du polymère non-irradié et avec les valeurs admises de δ_o pour calculer les valeurs de G_x , le nombre de ramifications formées par 100 e.v. d'énergie de radiation absorbée par l'échantillon. Une bonne concordance avec les résultats, relatés ailleurs, de solubilité et de gonflement, rapportés ailleurs, a été obtenue si $\delta_o = 0.9$.

Zusammenfassung

Die Abhängigkeit der Viskositätszahl von der Strahlungsdosis wurde an Poly(Butadien-co-Styrol) bei Bestrahlung im Vakuum und an Mischungen dieser Polymeren mit *N*-Phenyl- β -naphthylamin bei Bestrahlung in Luft und im Vakuum untersucht. Ohne Anbringung einer Korrektur für die Vernetzung im unbestrahlten Polymeren scheinen die überprüften Theorien eine zu grosse Zunahme der Viskositätszahl zu liefern. Bei Annahme einer Vernetzungszahl pro Gewichtsmittel des Primärmoleküls, δ_o , im nich bestrahlten Polymeren von 0,65 stimmen die Ergebnisse jedoch mit der Theorie von Spiro überein, welche die Beziehung von Stockmayer-Fixman zwischen Viskositätszahi und Verzweigung benützt. Die zum Eintritt der Gelbildung erforderliche Dosis, R_o , wurde an den veschiedenen Proben bestimmt, zusammen mit dem Zahlenmittel des Molekulargewichts des nicht bestrahlten Polymeren und mit angenommenen Werten für δ_o wurden diese Ergebnisse zur Berechnung von G_x -Werten, der Zahl der pro 100eV in der Probe absorbierten Strahlungsenergie gebildeten Vernetzungsstellen benützt. Mit $\delta_o = 0,9$ wurde gute Übereinstimmung mit an anderer Stelle mitgeteilten Löslichkeits- und Quellungsergebnissen erhalten.

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Branching in Poly(butadiene-co-styrene). III. Radiation-Induced Branching Examined by Solubility and Swelling

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Synopsis

The dependence of solubility and swelling on radiation dose has been examined for pure polymer and polymer containing varying amounts of the antioxidant N-phenyl- β -naphthylamine. Degradation did not occur when samples were irradiated *in vacuo* but in the presence of air degradation was initiated and crosslinking was retarded. During irradiation *in vacuo* the antioxidant interacted with the polymer and prevented the formation of a large number of crosslinks. An analysis of the solubility data indicated that there were 0.9 crosslinked units per weight-average primary molecule in the unirradiated polymer, and that 1.59 crosslinks were formed in the pure polymer on the absorption of 100 e.v. of radiation energy (i.e., $G_x = 1.59$). These values are consistent with the swelling data but not with the experimentally determined molecular weight distribution.

INTRODUCTION

Solubility and swelling determinations have frequently been used to study the effect of radiation on polymers. Witt¹ examined the dependence of solubility on dose for SBR samples containing different percentages of styrene. For a sample of the same composition as that used in the present work, Witt found G_x , the number of crosslinks formed per 100 e.v. absorbed, to have a value of 1.71. In the present paper values of G_x are determined by methods different from those used by Witt. The present techniques and their results are compared and evaluated.

In studies of the solubility and swelling changes produced by irradiation, the effect of crosslinking in the unirradiated polymer is frequently ignored. In the present work the importance of preirradiation crosslinking is examined, and estimates are made of the number of crosslinked units per weight-average primary molecule δ_0 in the unirradiated polymer. The values found for δ_0 are compared with those obtained by other methods.^{2,3}

In the present investigation the effects of air and of the presence of the additive N-phenyl- β -naphthylamine on the polymer irradiation process have been examined by solubility and swelling techniques.

EXPERIMENTAL

The materials, the purification methods, and the irradiation techniques employed have previously been described.^{2,3}

Solubility

The determination of the percentage of irradiated polymer soluble in benzene was simple and accurate. A known weight of small pieces of irradiated polymer, generally about 0.3 g., was placed in 25 ml. of benzene for 24 hr. The solution was then decanted into a 100-ml. volumetric The procedure was repeated three times, the gel washed with flask. small amounts of benzene, and the final solution made up to 100 ml. A dilute solution of the antioxidant N-phenyl- β -naphthylamine (denoted by B) was used in the extraction of the pure polymer. The solids content of 25 or 50 ml. of the final benzene solution was found by freeze-drying. In calculating the percentage of soluble polymer a correction was made for the presence of the antioxidant, B. This technique could be applied with satisfactory reproducibility if more than 50% of the sample were gel. Below 50% the gel tended to break into small pieces which passed over into the solution during decantation, even when a copper 100 mesh filter was employed. Consequently, only the results for gel contents greater than 50% are reported.

Baskett's⁴ method was used to determine the minimum value of the ratio of the number of scissions to the number of crosslinks, p_0/q_0 . A sample was irradiated to a high dose, extracted, and the gel divided into several portions. Each portion was irradiated to a different dose and the gel content measured.

Swelling

Upon separating the gel from the sol the degree to which the gel swelled in benzene was determined. The benzene not incorporated into the gel was decanted off, and the particles of swollen gel were rolled on a paper towel for about 1 min. to remove any surface benzene. The particles were then quickly transferred to a weighed stoppered bottle and their weight determined. Because the weight of dry gel was known from solubility experiments, the benzene associated with the gel could be found.

This very practical technique was subject to two obvious sources of error. If the drying process were too prolonged some of the benzene contributing to the swelling might be lost during the drying of the gel, and if too rapid, some excess benzene would remain in the gel. To determine the importance of these possible errors in the drying technique, the method of Flory⁵ for the determination of the extent of swelling in a saturated benzene atmosphere was applied to several samples of widely differing degrees of swelling. This rather complex method gave results within 2% of the paper towel method.

In preliminary experiments it was found that the degree of subdivision of the sample and the time of extraction, beyond 24 hr., had no effect on the extent of swelling. Bardwell⁶ made a thorough study of these effects and reached the same conclusion. In the light of his results no further study was deemed necessary.

RESULTS

Solubility

Figure 1 shows the dependence of $S + \sqrt{S}$ on 1/R, where S is the sol fraction and R the dose. According to Charlesby,⁷ if the initial molecular weight distribution is of the "most probable" type and if the unirradiated polymer consists of only linear molecules, the data should fit the equation

$$S + \sqrt{S} = (p_0/q_0) + (0.48 \times 10^6/G_x \ \bar{M}_{n_0}R) \tag{1}$$

In this equation p_0/q_0 is the ratio of the number of scissions to the number of crosslinks, R is the dose in megarads, \overline{M}_{n_0} is the number-average molecular weight of the unirradiated linear polymer, and G_x is the number of crosslinks formed per 100 e.v. of energy absorbed. The plots of Figure 1 do not obey this equation since, as previous investigations² showed, the unirradiated polymer contains crosslinked molecules. The extent of this crosslinking may be expressed as the number of crosslinked units per weight-average primary (prior to crosslinking) molecule, denoted by the symbol δ_0 . This degree of crosslinking may also be expressed as an equivalent specific dose of radiation, R_0 . If the experimentally determined dose for incipient gelation is R_q and if $p_0/q_0 = 0$, then

$$\delta_0 = R_0 / (R_0 + R_g) \tag{2}$$

The solubility data will obey eq. (1) if a specific value of R_0 is added to R. At high values of R this correction will have a very small effect. Therefore the intercept with the ordinate will be unaffected by R_0 , and it may be concluded that for samples irradiated *in vacuo* $p_0/q_0 = 0$. For samples irradiated ir. air, however, p_0/q_0 is greater than zero.

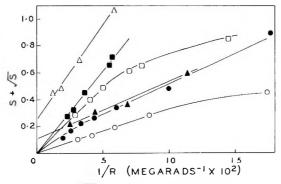


Fig. 1. Dependence of $S + \sqrt{S}$ on 1/R: (O) 0% B; (\bigcirc) 0.5% B; (\square) 2.1, 5.3, 7.1, and 11.3% B; (\blacksquare) 60.0% B; (\blacktriangle) 0% B, irradiated in the presence of air; (\triangle) 2.7% B, irradiated in the presence of air.

Solubility Following S	Second Irradiation (Initial	Solubility was 5.20%
R, Mrad	<i>S</i> , %	$S + \sqrt{S}$
25.2	0.28	0.0081
42.2	0.315	0.0087
122.0	0.568	0.0132

TABLE I

Table I shows the data used in estimating p_0/q_0 by Baskett's method. Unfortunately, the doses employed were not sufficiently high to give a constant value of $S + \sqrt{S}$. It can be concluded, however, that p_0/q_0 is greater than 0.01. The actual value of p_0/q_0 cannot be much greater than this; otherwise the plots of $S + \sqrt{S}$ versus 1/R would not extrapolate to an approximately zero intercept.

From the slopes of the plots of Figure 1 measured at high doses, values of G_x were calculated from eq. (1). As the results of Table II show, the value of G_x calculated in this manner is almost independent of δ_0 . To correct for crosslinks in the unirradiated polymer it was necessary to add R_0 to the dose, and to calculate \overline{M}_{n_0} by using eq. (3).⁷

$$\bar{M}_n = \bar{M}_{n_0} / (1 - \delta_0 / 4) \tag{3}$$

In this equation \overline{M}_n is the number-average molecular weight of the crosslinked unirradiated polymer. A value of $\overline{M}_n = 89,900$ was obtained by osmometry. Table II also gives the values of G_x previously calculated³ from R_g , \overline{M}_n , and assumed values of δ_0 . In contrast to G_x calculated by using eq. (1), G_x calculated by this method is highly dependent on δ_0 . The two methods give approximately the same results for irradiation *in* vacuo when $\delta_0 = 0.9$.

Figure 2 gives plots of sol fraction versus R/R_{g} for samples irradiated in vacuo. Except for the case of 0.52% antioxidant content, all the data fit one curve. A comparison of this curve with theoretical curves indicates that $\delta_{0} = 0.9$. The theoretical curves were obtained using Charlesby's theoretical curve⁷ of sol fraction versus R/R_{g} for $\delta_{0} = 0$.

	G_x calcul	lated from δ_0 , \bar{N}	G_x calculated from δ_0 , \overline{M}_n and the plot of $S + \sqrt{S}$ versus $1/R$		
B, %	$\delta_0 = 0$	$\delta_0 = 0.8$	$\delta_0 = 0.9$	$\delta_0 = 0$	$\delta_0 = 0.8$
0	9.41	3.33	1.72	1.62	1.59
0.5	3.49	1.24	0.64	0.97	0.94
2.1, 5.3	2.73	0.96	0.50	0.59	0.56
7.1, 11.3	2.73	0.96	0.50	0.59	0.56
60.0	1.88	0.67	0.35	0.46	0.43
()a	3.18	1.13	0.59	1.16	1.10
2.7ª	1.00	0.36	0.18	0.41	0.39

TABLE IIDependence of G_x on % B and on the Method of Calculation

* Irradiated in air.

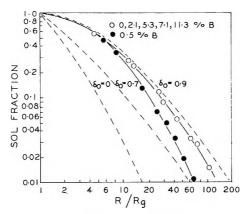


Fig. 2. Comparison between theoretical and experimental dependence of S on R/R_g : (O) 0, 2.1, 5.3, 7.1, and 11.3% B; (\bullet) 0.5% B.

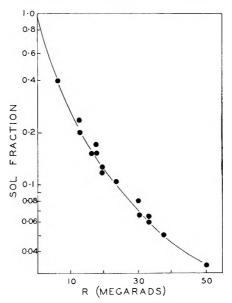


Fig. 3. Plot of log S vs. R for samples containing 2.1, 5.3, 7.1, and 11.3% B.

Values of sol fraction from his curve were plotted against $[(R/R_g) - \delta_0]/(1 - \delta_0)$, where R/R_g is also from the Charlesby curve.

Pearson⁸ has suggested that chain reaction crosslinking occurs when butadiene polymers are irradiated. The method of Charlesby for the detection of this type of reaction has been applied to the present results. Figure 3 shows the required plot of log S versus dose for samples containing 2.1, 5.3, 7.1, and 11.3% antioxidant. A similar plot is obtained for pure polymer. The average slope between S = 0.2 and S = 0.8 was determined and together with the previously determined values of R_g substituted into eq. (4).

$$i = [d(\log S)/dR] R_g (\overline{M}_w/\overline{M}_n)$$
(4)

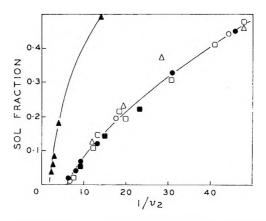


Fig. 4. Dependence of S on $1/v_2$: (O) 0% B; (\bigcirc) 0.5% B; (\square) 2.1, 5.3, 7.1, and 11.3% B; (\blacksquare) 60.0% B; (\blacktriangle) 0% B, irradiated in the presence of air; (\triangle) 2.7% B, irradiated in the presence of air.

The average number of links formed per chain reaction is equal to (1 - i)/i. If $\delta_0 = 0$, then $\overline{M}_w/\overline{M}_n = 2$. Substitution into eq. (4) leads to i = 0.5, and therefore a chain reaction does not occur. If a correction is made for δ_0 values greater than zero, the likelihood of a chain reaction is reduced since *i* increases. This increase occurs because \overline{M}_{n_0} is less than \overline{M}_n , while the slope is unaffected by R_0 , and $R_g \overline{M}_w = (R_g + R_0) \overline{M}_{w_0}$.

Swelling

Figure 4 shows the dependence of the volume fraction of polymer v_2 in the swollen gel on the sol fraction, S. The dependence is identical for all the samples with one exception; pure polymer irradiated in air gives higher v_2 values.

According to Flory¹⁰ the average molecular weight between crosslinks, \overline{M}_{cq} , is related to v_2 by the expression

$$\frac{M_{co}}{(1-2\overline{M}_{co}/\overline{M}_{nv_0})} = \frac{-\rho_p V_1 \left(v_2^{1/3} - 2v_2/f_n\right)}{\chi v_2^2 + \ln\left(1-v_2\right) + v_2}$$
(5)

In this equation ρ_p is the density of the polymer, V_1 is the molar volume of the solvent, χ is the interaction coefficient between the polymer and the solvent, f_n is the functionality of the branching (in the present case $f_n =$ 4), and \overline{M}_{nn_p} is the primary number-average molecular weight of the molecules in the gel. This equation includes the correction for "free ends" given by Flory.¹⁰ The value of \overline{M}_{nn_p} is calculated from eqs. (3) and (6) as:

$$\bar{M}_{n_{0_2}} = \bar{M}_{n_0} \left(1 + \sqrt{S} \right) \tag{6}$$

Equation (5) has been found to underestimate the value of M_{cg} .^{11,12} This discrepancy has been attributed, in part, to chain entanglements which result in physical crosslinks, to steric hindrance, and to changes in

 χ . Blanchard and Wooton¹³ have proposed that the first two factors may be corrected for by the expression

$$\overline{M}_{cg} = \omega_s + \gamma_1 F \left(1 - 2\overline{M}_{cg} / \overline{M}_{n_{0g}} \right) \tag{7}$$

In this equation γ_1 is an entanglement factor and ω_s a steric hindrance factor. Furthermore,

$$\gamma_1 = 1 + \sigma \bar{M}_{cg} \tag{8}$$

where σ is a constant for a given polymer-solvent system. Using Mullins' results¹² for natural rubber in *n*-decane, Blanchard and Wooton¹³ found $\omega_s = 0$ and $\sigma = 0.414 \times 10^{-4}$. In the present work these results have been assumed to be valid for SBR in benzene.

Kraus¹⁴ has studied the dependence of χ , the interaction coefficient, on v_2 for polybutadiene in *n*-heptane. He found that

$$\chi = 0.37 + 0.52v_2 \tag{9}$$

It has been assumed that this equation is also valid for the present system. To find the importance of the correction, calculations have been made using $\chi = 0.38$ for all values of v_2 . This is the average of the values 0.38 and 0.40 obtained by French and Ewart¹⁵ and by Bristow,¹⁶ respectively. These two values support the validity of eq. (9), since $\chi = 0.36$ was found for completely soluble polymer and $\chi = 0.40$ for $v_2 = 0.181$.

Upon obtaining \overline{M}_{cq} , the crosslinking density for the gel, q_q , and for the entire sample, q, was calculated. The crosslinking density is defined as the proportion of main chain units crosslinked. Flory¹⁰ gives the relation

$$\overline{M}_{cg} = w/(q_g + w/\overline{M}_{n_{0g}}) \tag{10}$$

where w is the average weight of the monomer units in the polymer, 68.6 in the present work. Combining eq. (10) with the relation⁷

$$q_g = q(1+S) \tag{11}$$

gives

 $q = \left[(1 - M_{cg} / \bar{M}_{n_{0g}}) w \right] / \left[(1 + S) M_{cg} \right]$ (12)

To calculate the values of q given in Table III, seven widely distributed values of v_2 and S from the main curve of Figure 4 were used. Figure 5 shows the dependence of q on dose for samples containing 2.1, 5.3, 7.1, and 11.3% B. For pure polymer the dependence would be identical but the doses would be lower by a constant factor. In correcting for δ_0 , eq. (3) was used, and R_0 was added to the dose. The result of Figure 5 shows that this correction has only a small effect. However, on correcting for the dependence of χ on v_2 it is found that q is reduced by approximately 30%. A similar reduction in q is obtained on correcting for chain entanglements.

Values of q may also be calculated from the relation⁷

$$q = RG_x w / 0.48 \times 10^6 \tag{13}$$

				Crosslinking density $q imes 10^4$				
				$\delta_0 = 0$	$\delta_0 = 0.8$	$\delta_0 = 0.8$	$\delta_0 = 0.8$	
				$\chi = 0.38$	$\chi = 0.38$	$\chi = 0.37 +$	$\chi = 0.37 +$	
	$R + R_{0}$,					$0.52v_{2}$	0.52i	
R, Mrad	Mrad			$\sigma = 0$	$\sigma = 0$	$\sigma = 0$	$\sigma = 4.14 \times$	
$(\delta_0 = 0)$	$(\delta_0 = 0.8)$	$1/v_{2}$	S, $%$				10-	
4.6	7.36	52	48.0	4.0	4.80	4.80	3.08	
6.4	9.16	36	38.0	5.5	6.38	6.38	3.76	
10.7	13.46	22	24.0	10.0	10.2	9.28	4.82	
22.5	25.26	12	10.0	25.5	26.9	22.9	10.7	
42.0	44.76	8	4.0	53.5	56.2	39.0	19.6	
50.0	52.76	7.2	3.0	65.0	66.4	45.9	24.2	
62.0	64.76	6.5	2.0	81.5	84.2	53.8	24.9	

TABLE III
Dependence of the Crosslinking Density q on Dose, and the Effect
of Correcting for Chain Entanglements and Changes in χ

The plots in Figure 5 show that q calculated by using $G_x = 0.50$ or 0.96 is in better agreement with q from swelling data than if $G_x = 2.73$ is used. As Table II shows, $G_x = 2.73$ was calculated for $\delta_0 = 0.0$, while $G_x = 0.96$ and 0.50 were calculated for $\delta_0 = 0.8$ and 0.9, respectively. If the corrections for chain entanglement and changes in χ are valid, the swelling results indicate that G_x is less than 0.50 and δ_0 is greater than 0.9.

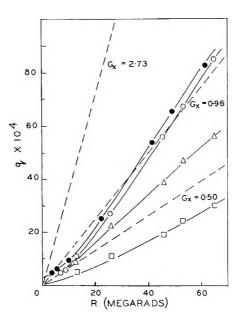


Fig. 5. Crosslinking density q as a function of $R: (\bullet)$ uncorrected; (O) corrected for δ_0 ; (Δ) corrected for δ_0 and χ ; (\Box) corrected for δ_0 , χ , and chain entanglements.

DISCUSSION

There are several assumptions implicit in the analysis of the solubility and swelling results given here. It is assumed that any branching present in the unirradiated polymer is caused by randomly occurring crosslinking imposed on a molecular weight distribution which is approximately of the "most probable" type. It has previously been shown² that these conditions are fulfilled for the SBR system studied. It is further assumed that the radiation causes neither endlinking nor cyclization. Spiro¹⁷ has developed a method, based on changes in molecular weight distribution, to distinguish between endlinking and crosslinking. An application of this method to polystyrene revealed that no endlinking occurred. The results of Spiro and the general improbability of an endlinking reaction support the assumption that endlinking is absent in the present case. Saito¹⁸ has considered the effect that cyclization would have on the dependence of sol fraction on dose. According to his analysis, cyclization in the absence of degradation but in the presence of crosslinking would result in a plot of log S versus log (R/R_a) which would be convex to the R/R_a axis. However, if δ_0 is greater than zero, the resulting concavity might mask the effect of cyclization. However, since the importance of cyclization increases with dose, an inflection point in the plots of log S versus log (R/R_a) might be expected. These plots are given in Figure 2 and show no points of inflection. This does not prove that cyclization is absent; but when the lack of evidence for cyclization in any polymer system is also considered, the assumption that cyclization is absent seems justified.

Figure 1 indicates that degradation occurs only when the polymer is irradiated in air. Even though the method of Baskett⁴ indicates that $p_0/q_0 = 0.01$ for irradiation *in vacuo*, the true value might be zero because of the possibility of degradation by oxidation. The solubility results of Witt¹ also indicate that no degradation occurs. Contrary to this, Anderson¹⁹ found p_0/q_0 to be considerably greater than zero; however, the stress relaxation technique used by Anderson to detect scission measures instantaneous scissions in addition to permanent scissions.

In a previous paper³ it was shown that the presence of air during irradiation increases R_{ρ} . This increase must be caused partly by the occurrence of scissions, and might also be caused by a reduction in crosslinking. If the subscript *a* denotes degradation, then according to Schultz et al.²⁰

$$R_g/R_{g_a} = (q_{0_a} - p_{0_a}/2)/q_0 \tag{14}$$

If it is assumed that $q_{0_a} = q_0$ then for q_{0_a}/p_{0_a} values obtained from Figure 1, a value of $R_g/R_{g_a} = 0.90$ is obtained for the 2.7% B sample and 0.95 for the pure polymer. However, the experimental ratio R_g/R_{g_a} is 0.41 for the 2.7% B sample and 0.37 for the pure polymer. Therefore, on irradiating the polymer in air, not only is degradation initiated, but crosslinking is retarded. The plots of Figure 4 show the degree of swelling of pure polymer irradiated in air to be much less than for polymer irradiated in vacuo or for polymer containing B irradiated in air. Apparently, the pure polymer is oxidized to such an extent that it no longer swells as much as unoxidized material. Oxidation probably changes both χ and the polymer density. In a following paper²¹ the amount of oxidation is examined by infrared spectroscopy, and it is shown that a polymer containing B is only slightly oxidized. This explains why swelling behavior is unaffected by the air if B is present.

The results of Table II indicate that a large reduction in G_x is produced by the addition of a small amount of B. The number of crosslinks prevented by B can be calculated at any dose and for any composition. Figure 2 shows that the plots of sol fraction versus R/R_s for samples containing 2.1, 5.3, 7.1, and 11.3% B coincide with the plot for the pure polymer, provided irradiation is *in vacuo*. If the effect of B in retarding crosslinking were not constant. the plots would not coincide. For example, the sol fraction for samples containing 0.52% B tends to decrease more rapidly with R/R_q than for the other samples. This must occur because the protective effect of B is decreasing with increasing dose and therefore R_{q} is also decreasing. The effective or instantaneous value of R_{q} will be that which makes R/R_g at a given sol fraction equal to R/R_g for pure polymer at the same sol fraction (or for polymer containing more than 2%B). At a sol fraction of 0.01, which corresponds to a dose of 50 Mrad, the effective value of R_{g} for a polymer containing 0.52% B is 0.454. This is considerably lower than the value of 0.54 found for R_{g} by filtration technique.² For $R_g = 0.454$ and an assumed value of δ_0 , the number of crosslinked units per weight-average primary molecule, δ , may be calculated for R = 50 Mrad from eqs. (2) and (15).

$$\delta = (R + R_0) / (R_g + R_0) \tag{15}$$

Thus for a polymer containing 0.52% B, a value of $\delta = 22.9$ is found if $\delta_0 = 0.8$. For pure polymer, $R_{\varrho} = 0.20$, and for the same values of δ_0 and R, δ is found to be 50.8. On correcting for dilution in a sample containing 0.52% B the value of δ should be $50.8 \times 0.9948 = 50.6$, provided there is no interaction between B and polymer. These results indicate that B prevents the formation of 50.6 - 22.9 = 27.7 crosslinked units. On the other hand, if $\delta_0 = 0.9$, the number of crosslinked units prevented is 14.0. In a following paper²¹ these results are compared to the amount of B destroyed at R = 50 Mrad.

Values of δ_0 and G_x have been estimated in this report and also in two previous reports^{2,3} by several different methods. A summary and evaluation of these methods and their results will now be given. Four methods have been used to calculate δ_0 .

(1) The unirradiated polymer was divided into twelve fractions, and the weights, intrinsic viscosities, and sedimentation coefficients of these

fractions were measured. The data were interpreted by several theories, 22,23 and the two most reliable theories gave $\delta_0 = 0.56$ and 0.78.

(2) Using the same data mentioned above the molecular weight distribution of the unirradiated polymer was established. This distribution indicated that $\overline{M}_w/\overline{M}_n = 2.84$ and $\delta_0 = 0.36$.

(3) According to the theory²⁴ of Spiro, the manner in which the intrinsic viscosity increases with dose indicates that $\delta_0 = 0.65$ in the present system.

(4) From the log-log plot of sol fraction versus R/R_{σ} it was estimated that $\delta_0 = 0.9$. This is considered the most reliable value of δ_0 because it is based on well established theory and the experimental technique is the simplest and most accurate.

Two methods have been used to calculate G_x .

(1) From the R_g value, the number-average molecular weight of the unirradiated polymer, and the experimentally determined ratio $\overline{M}_w/\overline{M}_n$, it was estimated³ that $G_x = 9.41$ for the pure polymer irradiated in vacuo.

(2) From the plot of $S + \sqrt{S}$ versus 1/R and the number-average molecular weight of the unirradiated polymer it was estimated that for $\delta_0 =$ 0.0 and 0.8 the respective values of G_x would be 1.62 and 1.59. These values are in good agreement with $G_x = 1.71$ obtained by Witt.¹ They are probably more reliable than $G_x = 9.41$ because sol fraction and \overline{M}_n are more accurately determined than R_g and $\overline{M}_w/\overline{M}_n$.

If the experimentally determined molecular weight distribution is narrower than the true distribution, and if $\overline{M}_w/\overline{M}_n = 15.5$, rather than 2.86, a value of $\delta_0 = 0.9$ is obtained. If this value of δ_0 is now combined with R_g and \overline{M}_n , a value of $G_x = 1.72$ is found. The agreement of these values with δ_0 and G_x calculated by the most reliable methods strongly suggests that the experimentally determined molecular weight distribution is, indeed, much narrower than the true one. The theories used to interpret the solution properties of the fractions appear to overestimate the effect of crosslinking on intrinsic viscosity; however, the polydispersity of the fractions might be the cause of this discrepancy. As previously noted,³ three of the chief theories which relate intrinsic viscosity to R/R_g appear to overestimate the increase in $[\eta]$, whereas the theory of Spiro²⁴ underestimates this increase.

The swelling results are difficult to interpret because the validity of the corrections for chain entanglements and for changes in χ with v_2 are not well established. Furthermore, no correction is made for the excluded volume effect which might be important.²⁵ Swelling results for other polymers have generally been found to overestimate G_x if none of these corrections is made. Therefore, the results presented in Figure 5 indicate that G_x for samples containing 2.1-11.3% B is less than 0.96. The corresponding value of G_x for the pure polymer is 3.33. These values were calculated from δ_0 assumed to be 0.8 and R_g and \overline{M}_n . Therefore, the swelling results indicate that δ_0 is greater than 0.8. These limiting values of δ_0 and G_x are consistent with $\delta_0 = 0.9$ and $G_x = 1.59$.

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Résumé

On a étudié la dépendance de la solubilité et du gonflement vis-à-vis de la dose de radiation dans le cas d'un polymère pur et un polymère contenant différentes quantités d'un antioxydant, la N-phényl- β -naphthylanine. Aucune dégradation n'a lieu lorsque les échantillons sont irradiés sous vide, mais en présence d'air, la dégradation est initiée et le pontage est retardé. Pendant l'irradiation sous vide, l'antioxydant réagit avec le polymère et empêche ainsi la formation d'un grand nombre de pontages. Une analyse des résultats de solubilité montre qu'il y a 0.9 unités pontées par rapport au poids moyen des molécules primaires dans le polymère non-irradié, et que 1.59 ponts sont formés dans le polymère pur par absorption d'une énergie de radiation de 100 e.v. (c.a.d. $G_x =$ 1.59). Ces valeurs concordent avec les résultats obtenus à partir des études du gonflement, mais non avec la distribution du poids moléculaire déterminé expérimentalement.

Zusammenfassung

Die Abhängigkeit der Löslichkeit und Quellung von der Strahlungsdosis wurde an reinem Polymeren und an solchem mit wechselndem Gehalt an N-Phenyl- β -Naphthylamin als Antioxydans untersucht. Bei Bestrahlung der Proben in Vakuum trat kein Abbau auf, in Gegenwart von Luft jedoch wurde der Abbau initiiert und die Vernetzung verzögert. Während der Bestrahlung in Vakuum reagierte das Antioxydans mit dem Polymeren und verhinderte die Bildung einer grossen Zahl von Vernetzungsstellen. Eine Analyse der Löslichkeitsdaten zeigte, dass im unbestrahlten Polymeren 0,9 vernetzte Bausteine pro Gewichtsmittel des Primärmoleküls vorhanden waren und dass im reinen Polymeren bei der Absorption von 100eV Strahlungsenergie 1,59 Vernetzungsstellen gebildet werden (d.h. $G_x = 1,59$). Diese Werte sind mit den Quellungsdaten konsistent, nicht aber mit der experimentell bestimmten Molekulargewichtsverteilung.

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Branching in Poly(butadiene-co-styrene). IV. Retardation of Radiation-Induced Branching

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Synopsis

The composition and yield of the evolved gas and the resulting changes in infrared and ultraviolet spectra have been examined for the irradiation of poly(butadiene-costyrene). Apart from crosslinking, the major changes which occurred during the reaction were the evolution of hydrogen and the destruction of vinyl groups. For every 100 e.v. of radiation energy absorbed 0.45 molecules of hydrogen were evolved, $G(H_2) =$ 0.45, and 6.1 vinyl groups were destroyed, G(-vinyl) = 6.1. These results have been compared with the yield of crosslinks, $G_x = 1.60$. Addition of N-phenyl- β -naphthylamine to the polymer reduced the gas yield to a greater extent than predicted by the "mixture law" (which states that the yield of a product from component X is directly proportional to the electron fraction of X). Over the additive concentration range of 2-11%, the gas yield was constant. This behavior is identical to that found previously for the crosslink yield. An explanation of these results has been given which involves the occurrence of processes which exhibit a negative deviation from the mixture law together with processes which exhibit a positive deviation. The destruction of the additive during the irradiation of a sample containing initially 0.52% additive has been determined. The results indicate that the additive protects the polymer mainly by charge transfer or excitation energy transfer.

INTRODUCTION

It has frequently been observed that the yields of some of the products resulting from irradiation of hydrocarbon mixtures are less than would be expected if the absorption of energy by each component were directly proportional to its electron fraction.^{1,2} This discrepancy has been attributed to interactions between the components. In solutions of alkanes the interaction appears to be mainly physical in nature, i.e., chemical bonds are neither formed nor broken.² In other systems, such as the vapor-phase radiolysis of mixtures of cyclohexane and benzene, the interaction is mainly chemical in nature. In this paper a study is made of the interaction between a low molecular weight compound, N-phenyl- β -naphthylamine, denoted B, and a polymer, poly(butadiene-co-styrene).

In a previous paper⁴ it was found that for a concentration of the low molecular weight compound, B, of 2% the yield of crosslinks is much less than would be expected on the basis of electron fraction. Over the range 2-11% B, however, the yield of crosslinks is constant. In the present in-

vestigation the dependence of total gas yield on concentration of B has been examined, and compared with the dependence of crosslink yield.

Dyne and Denhartog^{2,5} have studied the nature of the interaction between liquid hydrocarbons by determining the isotopic composition of the hydrogen yield, and Charlesby and Lloyd⁶ have studied the nature of the interaction between anthracene and silicone by following the reduction in anthracene concentration on irradiation. It is essentially this latter technique which has been employed for the present system.

The changes in the degree of unsaturation resulting from irradiation have frequently been studied for both hydrocarbons and polymers. In the present work changes in unsaturation have been examined by infrared and ultraviolet spectroscopy and by mass spectrometry. These changes have been compared with the corresponding amount of crosslinking.

EXPERIMENTAL

The methods employed in the preparation and irradiation of samples have been described elsewhere.⁴ Reagent grade toluene was obtained from Fisher Scientific and the anhydrous ethanol from Consolidated Alcohols.

Gas Analysis

The total amount of gas evolved on irradiation was measured in a calibrated manifold containing a McLeod gauge. Gas yields were measured for samples containing various amounts of B and for doses up to 45 Mrad. The composition of the gas evolved from the pure polymer was determined by mass spectrometry.

Infrared and Ultraviolet Spectroscopy

A solution technique could not be used to obtain the infrared spectrum of irradiated polymer because of the insolubility of the polymer. Consequently, a thin film of unirradiated polymer was formed between two sodium chloride plates, and its spectrum was measured on a Perkin-Elmer Model 21 spectrophotometer before and after irradiation *in vacuo*.

The high sensitivity of sodium chloride to moisture made it necessary to employ a different technique⁷ for samples irradiated in air. A concentrated solution of polymer in benzene was placed in a glass ring floating on mercury. On evaporation of the benzene a thin circular film of polymer remained attached to the sides of the ring. This same technique was used to prepare films for ultraviolet spectroscopy.

Destruction of Additive

The concentration of the additive B was obtained by extracting a sample with a solvent which dissolves B, but not polymer, and determining the concentration of B in the solvent by ultraviolet spectroscopy. The effect of irradiation was studied for doses up to 50 Mrad.

A 1.8-g. sample of polymer containing 0.52% B was cut into 1 mm. cubes and refluxed in 50 ml. of ethanol-toluene azeotrope, (ETA) containing 7 parts of ethanol to 3 parts of toluene. After 4 hr. of refluxing the solution was cooled and the supernatant decanted into a volumetric flask. This extraction was repeated four times. The volume of the combined supernatants was made up to 250 ml. by washing the extracted polymer with ETA. Aliquots of this solution were diluted to give a concentration suitable for ultraviolet spectra measurements. A Beckman Model DK-1 spectrophotometer was used and the peak at 308 m μ was attributed to *N*-phenyl- β -naphthylamine, B. This technique is essentially the same as the standard method⁸ for the determination of the antioxidant content of SBR.

RESULTS

Gas Analysis

Figure 1 shows the dependence of gas yield Y on dose R. For samples containing 50% B there is a nonlinear relation between Y and R, but for all other B concentrations this relation is linear. The number of molecules of gas evolved per 100 e.v. of energy absorbed by the sample, G_{g} , was calculated from these results. Table I and Figure 2 show the dependence of G_{g} on B concentration. The number of crosslinks formed per 100 e.v. of energy absorbed, G_{x} , which was determined previously,⁴ is also given in Table I and Figure 2. The value of G_{g} for the sample containing 60% B is not shown in the figure because of its extreme dependence on dose. It appears that G_{g} and G_{x} are independent of additive concentration over the range 2.1–11.3% B.

The dashed line in Figure 2 represents the "mixture law"² which states that the yield of a radiolytic product which arises from a particular compound is directly proportional to the electron fraction of the compound. Lamborn and Swallow⁹ claim that in certain systems energy absorption is

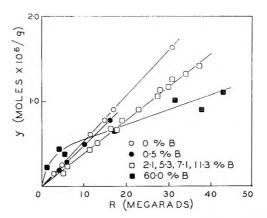


Fig. 1. Gas yield as a function of dose and additive concentration.

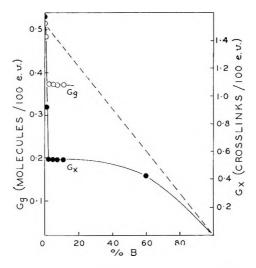


Fig. 2. Dependence of G_g and G_z on percentage B.

not directly proportional to electron fraction. However, recent experimental evidence supports the premise of direct proportionality.¹⁰ In the present system the electron density of the polymer is approximately equal to that of the additive, and therefore the mixture law may be expressed in terms of weight fraction rather than electron fraction. Figure 2 shows that G_x and G_g are less than predicted by the mixture law. The extent of this negative deviation reaches a maximum at 2% B. The value of $G_g =$ 1.8, which was obtained at low doses for the polymer containing 60% B, represents a large positive deviation.

The composition of the gas formed on irradiation of the pure polymer to a dose of 31 Mrad was 87.1% hydrogen, 4.7% ethylene, and 8.2% high mass number constituents. Therefore, since $G_g = 0.52$ for pure polymer, $G(H_2) = 0.452$, $G(C_2H_4) = 0.0244$, and G(higher mass number) = 0.0427.

Changes in the Spectra

The infrared spectrum of pure polymer was measured before and after irradiation *in vacuo* to a dose of 150 Mrad. The only change was a decrease in the peak associated with vinyl groups¹¹ at 912 cm.⁻¹. The absorbance of this peak decreased from 0.561 at R = 0 to 0.357 at R = 150 Mrad. According to the composition of the polymer determined by the manufacturers, the vinyl content of the unirradiated polymer is 15.5%. From this value and the change in absorbance it is calculated by Beer's law that after a dose of 150 Mrad, 36.3% of the vinyl groups initially present have been destroyed. This suggests that G(-vinyl) is 6.1.

Infrared spectral measurements showed that after a dose of only 10 Mrad the pure polymer irradiated in air is greatly oxidized. Pure polymer exposed to air alone for the same period as required for a dose of 100 Mrad was only slightly oxidized. When samples containing 2.7% B were ir-

radiated in air, however, the extent of oxidation was only slightly greater than that in the absence of radiation.

Irradiation of the pure polymer *in vacuo* to a dose of 100 Mrad produced a large increase in the ultraviolet absorption of the polymer. An even larger increase was noted when air was present during irradiation.

Destruction of B

Figure 3 shows the dependence on dose of the weight fraction Q of soluble B in samples which contained 0.52% B before irradiation. From the plot it is seen that at doses above 5 Mrad, Q decreases linearly with dose, while below 5 Mrad the rate of decrease is greater the lower the dose.

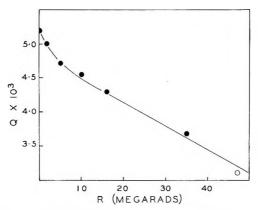


Fig. 3. Weight fraction of soluble additive as a function of dose for samples containing 0.52% soluble additive prior to irradiation.

The material balance for the irradiation of a mixture of polymer, P, and additive, B, is

$$B_0 + P_0 = B_R + B_D + B_{DG} + P_R + P_{DG}$$
(1)

In this equation B_0 and P_0 are the respective weights of additive and polymer in the unirradiated sample. All the symbols of the right-hand side of this equation represent weights in the irradiated sample. $B_{\rm R}$ is the weight of soluble additive, $B_{\rm D}$ is the weight of additive attached to the polymer, and $B_{\rm DG}$ the weight of additive decomposed to gas or to fragments which do not absorb in the same ultraviolet region as the pure antioxidant. $P_{\rm R}$ and $P_{\rm DG}$ are the weights of polymer extracted and decomposed to gas, respectively. The number of molecules of additive which are destroyed or become attached to the polymer per weight-average primary (prior to crosslinking) molecule is

$$D = [(B_{\rm D} + B_{\rm DG})(N/217)](\bar{M}_{w_0}/P_0N)$$
(2)

where 217 is the molecular weight of the antioxidant, N is Avogadro's number, and \overline{M}_{w_0} is the weight-average molecular weight of the primary molecules. Before irradiation

$$Q_0 = B_0 / (B_0 + P_0) \tag{3}$$

and after irradiation

$$Q_{\rm R} = B_{\rm R}/(B_{\rm R} + P_{\rm R} + B_{\rm D}) \tag{4}$$

Substituting the relation

$$B_{\rm D} + B_{\rm DG} = B_0 - B_{\rm R} \tag{5}$$

and eqs. (3) and (4) into eq. (2) leads to

$$D = (\overline{M}_{w_0}/217) \left\{ [Q_0/(1-Q_0)] - [Q_R(B_R + P_R + B_D)/P_0] \right\}$$
(6)

If it is assumed that $P_{\rm R} = P_0$ and $B_{\rm D} = 0$, then eq. (6) becomes

$$D = (\overline{M}_{w_0}/217) \left\{ [Q_0/(1 - Q_0)] - [Q_R/(1 - Q_R)] \right\}$$
(7)

Because of the assumptions, D calculated by eq. (7) will be slightly greater than the true value.

The value of \overline{M}_{w_0} must first be obtained before D can be calculated. The primary molecular weight distribution of the unirradiated polymer is only slightly broader than the "most probable" type; therefore, \overline{M}_{w_0} is approximately twice as large as the number-average molecular weight of the primary molecules, \overline{M}_{n_0} .¹² The number of crosslinked units per weight-average primary molecule, δ_0 , is related to \overline{M}_{n_0} by the expression¹³

$$\bar{M}_n = \bar{M}_{n_0} / (1 - \delta_0 / 4) \tag{8}$$

where \overline{M}_n is the number-average molecular weight of the crosslinked molecules. By osmometry it was found that $\overline{M}_n = 89,900$, and previous investigations⁴ indicate that δ_0 is between 0.8 and 0.9. Substitution of these values into eq. (8) gives two values of \overline{M}_{n_0} which in turn lead to two values of \overline{M}_{w_0} . Using these values in eq. (7) together with Q values obtained from Figure 3 gives D = 1.32 for a dose of 50 Mrad and for $\delta_0 = 0.8$, and D =1.27 for the same dose but with $\delta_0 = 0.9$.

DISCUSSION

The relative amounts of crosslink formation, gas evolution, and vinyl group destruction which occur on irradiating the pure polymer suggest what groups of the polymer chain are affected and how they are affected. In SBR only the butadiene units need be considered because they are much more sensitive to radiation than are the styrene units since $G_x = 3.2$ for polybutadiene¹⁴ and $G_x = 0.045$ for polystyrene.¹⁵ The G value for gas other than hydrogen is only 0.067. The processes which produce this gas are relatively unimportant compared to those which lead to crosslink formation, hydrogen evolution, and vinyl group destruction, since $G_x = 1.60$, $G(H_2) = 0.45$ and G(-vinyl) = 1.25.

These three major processes are closely related to each other. It was previously shown that only crosslinking occurs on irradiation and that this

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E , %	G_{g} , molecules of gas/100 e.v. absorbed by sample	G_x , crosslinks/100 e.v. absorbed by sample	
0	0.52	1.59	
0.5	0.48	0.94	
2.1	0.38	0.56	
5.3	0.38	0.56	
7.1	0.38	0.56	
11.3	0.38	0.56	
60.3	1.8 ⁿ	0.43	
	$0.25^{\rm b}$		
100.0	0.04°	0.00	
	0.02^{d}		

TABLE I Dependence of G_x and G_g on Additive Concentration

^a For R = 0.

^b For R = 40 Mrad.

^c For R = 6 Mrad.

⁴ For R = 54 Mrad.

crosslinking does not involve a chain reaction.⁴ Therefore, the two basic processes involving polymer molecules P are

 $P + P \longrightarrow PP$ $P + P \longrightarrow PP + H_2$

There may be several intermediate steps possibly involving ions, radicals, and excited molecules. Since $G(H_2) = 0.45$ and $G_x = 1.60$, the ratio of the yields of the first process to the second process is 2.55. Depending on the specific reactions involved, the first process may result in the destruction of one or two vinyl groups, and the second process may result in the destruction of two vinyl groups, or, no destruction may occur. These qualifications are based on the consideration that the destruction of a vinyl group represents the formation of two new single bonds. The high value of G(-vinyl) relative to G_x and $G(H_2)$ might be caused by a reaction between adjacent vinyl groups on the same molecule. Considering that $G(H_2) = 0.45$ this reaction must lead to very little hydrogen evolution.

Kuz'minskiĭ et al.¹⁶ found that the unsaturation in SBR had been reduced by 80% after a dose of 150 Mrad. Turner¹⁷ claims that the chemical method used by them to measure the degree of unsaturation overestimates the amount of destruction. The results of the present work tend to support Turner's criticism, since infrared analysis indicates that only 36% of the unsaturation is destroyed after 150 Mrad.

On exposing natural rubber to γ -radiation, Evans et al.⁷ observed considerable diene formation. The increase in the ultraviolet absorption obtained in the present work might also be due to diene formation. If two vinyl groups react with each other to give a crosslink and hydrogen, a diene would be formed.

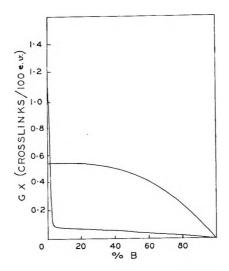


Fig. 4. Theoretical dependence of G_x on additive concentration.

The changes in the infrared spectrum of the polymer when irradiated in air are similar to those observed by others in the absence of radiation. Apparently the radiation accelerates the rate of oxidation but does not introduce new oxidation reactions. Dole et al.¹⁸ have suggested a large number of complicated reactions which probably occur during radiationinduced oxidation. Solubility results previously reported⁴ for irradiation in air indicate that the ratio of scissions to crosslinks is 0.10 for pure polymer and 0.25 for polymer containing 2.7% B, but because thick samples were used the true values of these ratios is probably considerably greater. The solubility results also indicated that the presence of air not only initiates scission but retards crosslinking as well. Infrared analyses show that B is very efficient in protecting the polymer from radiation-induced Bauman and Born¹⁹ have suggested the reactions responsible oxidation. In contrast to the present results, Field et al.²⁰ found for this protection. that when the polymer was exposed in air to ultraviolet radiation the presence of B increased the amount of oxidation.

The results of Figure 2 indicate that B and the polymer interact so that both G_x and G_0 are less than predicted by the mixture law. In a previous investigation⁴ it was found that after a sample containing initially 0.52%B was irradiated to 50 Mrad, B had prevented the formation of 27.9 crosslinked units per weight-average primary molecule if $\delta_0 = 0.8$ and 14 if $\delta_0 =$ 0.9. In the present investigation it is found that after the same sample has received the same dose of 50 Mrad, 1.32 molecules of B have become attached to the polymer or have decomposed per weight-average primary molecule if $\delta_0 = 0.8$, and 1.27 if $\delta_0 = 0.9$. Therefore, the ratio of crosslinked units prevented to molecules of B attached to the polymer or decomposed is 21.3 for $\delta_0 = 0.8$ and 10.6 for $\delta_0 = 0.9$. There are several reasons for the probably overestimation of the extent of attachment and decomposition of B and therefore for the probable underestimation of this ratio. Incomplete evacuation or a post-irradiation reaction would result in the attachment of B to the polymer. If some of the polymer dissolves in the azeotrope underestimation will result. The assumptions involved in calculating eq. (7) will lead to an underestimation of this ratio.

The large number of crosslinked units prevented for each molecule of B destroyed is incompatible with a radical scavenging mechanism. If it is assumed that each crosslinked unit corresponds to a radical, a molecule of B must scavenge at least 10.6 radicals: this is highly unlikely. A small amount of radical scavenging probably does occur; but most of the protection must be due to charge transfer or excitation energy transfer.

The effect of B on G_x and G_q over the entire concentration range is given in Figure 2. Values of G_{g} for the sample containing 60% B are not shown in this figure but are given in Table I. At a concentration of 60% B the solubility limit of B in the polymer is definitely exceeded. The very high G_q values for this sample and the dose dependence of G_q is probably related to this and to secondary reactions involving the scavenging of hydrogen; however, no definite explanation can be given. Over the range 2-11% B the values of G_g and G_x are constant. It might be suggested that only one process is responsible for the formation of crosslinks and gas, and that G_g and G_x are the same at 11% as at 2% B since the solubility limit of B in the polymer is 2%. However, the results of Angert and Kuz'minskii indicate that the solubility limit is in excess of 10% B. Furthermore, even if the solubility limit were 2% B, the value of G_{ρ} would decrease by 0.03 units and that of G_x by 0.05 units over the range 2-11% B because of the dilution of the polymer by B. This argument refutes other explanations involving the occurrence of only one process.

For simplicity we can assume that there are two processes involved, although there might be more. The large deviation from the mixture law produced by 2% B indicates that one of these processes is reduced by B. Even if this process were completely retarded by a concentration of 2% B and the other process were unaffected by B, there would still be a reduction in G_x and G_g over the range 2-11% B since the concentration of polymer is being reduced. The independence of G_g and G_x over the range 2-11% B indicates that the second process exhibits a positive deviation from the mixture law. Figure 4 shows one possible manner in which two such processes could be affected by B to give a plot similar to that of Figure 2.

The two processes could involve ions exclusively or excited molecules exclusively. However, because radiation produces both ions and excited molecules and because B affects the processes differently, it is likely that one mechanism involves ions and the other excited molecules. Since B is a secondary amine and therefore a good electron donor, it would prevent the ionic process by replacing electrons lost by polymer molecules. This implies that the reaction which exhibits a negative deviation from the mixture law is ionic. The other process which involves excited molecules exhibits a positive deviation from the mixture law because of the transfer of excita-

Kinetics of Styrene Polymerization Catalyzed by Rhenium Pentachloride

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Synopsis

Polystyrene of high molecular weight was obtained in a good yield by the polymerization of styrene catalyzed by rhenium pentachloride in benzene or benzene-ethylene dichloride solution. The mechanism of this polymerization reaction was studied by kinetic and spectroscopic measurements. Experimental results were well explained by assuming that a π -complex between rhenium pentachloride and monomer initiates the cationic polymerization in the case of benzene solution and that $^+CH_2CH_2Cl$ initiates the cationic polymerization in the presence of ethylene dichloride.

INTRODUCTION

It has been reported that rhenium halides act as Lewis acids¹ and are effective as polymerization catalysts.^{2,3} In the present study, styrene was polymerized by using rhenium pentachloride, and polystyrene of high molecular weight was obtained in a good yield. The mechanism of this polymerization reaction was studied under various experimental conditions by using kinetic and spectroscopic measurements.

EXPERIMENTAL

Sample

Commercial styrene was washed twice with 20% aqueous sodium hydroxide, washed twice with 20% aqueous sodium bisulfite, washed thoroughly with water, then dried over calcium chloride and distilled at reduced pressure. A distillate boiling at 39° C./10.5 mm. Hg was used for the experiment. Commercial ethyl monochloroacetate was completely dried over calcium chloride and distilled at reduced pressure. A distillate boiling at 44° C./13 mm. Hg was used for the experiment. Commercial benzene was washed twice with concentrated sulfuric acid and then washed thoroughly with water, allowed to stand for 24 hr. over calcium chloride, and distilled over sodium metal. A distillate boiling at 80° C./760 mm. Hg was used. Commercial ethylene dichloride was dried completely over calcium chloride and distilled. A distillate boiling at 83.7° C./760 mm. Hg was used. Commercial rhenium pentachloride was completely purified by

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repeated sublimation at a high vacuum. All of these samples were purified or distilled again immediately before each run.

Procedure

A 100-ml. three-necked flask with a mercury-seal stirrer was used. Into this flask, desired quantities of solvent and monomer were introduced under an atmosphere of purified nitrogen gas. The mixture was kept at a constant temperature ($\pm 0.05^{\circ}$ C.) in a thermostat. A solution of rhenium pentachloride in ethyl monochloroacetate was added rapidly under the nitrogen atmosphere. At definite time intervals after the addition of the catalyst, aliquots of the reaction mixture were removed with a syringe previously filled with nitrogen and were poured into methanol to precipitate polymer. The obtained polymer was dissolved in toluene, precipitated twice with methanol, washed completely with methanol, and dried at reduced pressure.

The molecular weight of the polymer was determined by using an Ostwald viscometer at 30°C. for toluene solutions and also by using a vapor pressure osmometer (Mechro.ab, Model 30-1 A) at 20°C. for benzene solution. Molecular weight was calculated from the viscosity measurement, by using the equation:⁴

$$[\eta] = 1.2 \times 10^{-4} M^{0.7}$$

Visible and ultraviolet absorption spectra for the reaction system were measured by a Cary 14 spectrometer.

RESULTS

Rate of Polymerization

Except in special cases, all measurements were conducted by dissolving a desired quantity of rhenium pentachloride in 5 ml. cf ethyl monochloro-acetate and adding this solution to the polymerization system to give a total volume of 50 ml.

The variations of yield with time at various concentrations of catalyst are shown in Figures 1–3, benzene being used as a solvent and the initial concentration of monomer being kept constant. The variations of yield with time at various concentrations of monomer with benzene as a solvent and a constant initial concentration of catalyst are shown in Figures 4–6.

Each of the rates of polymerization obtained from the curves in Figures 1–6 reaches a stationary value with time. An example is shown in Figure 7. It is obvious from the figure that the rate of polymerization increases with polymerization time and that it becomes stationary at the time τ . As shown in Figure 8, the stationary rates R_s obtained from Figures 1–6 satisfy the relationship:

$$R_{s} = k[C]_{0}[M]_{s}^{2.8}$$
(1)

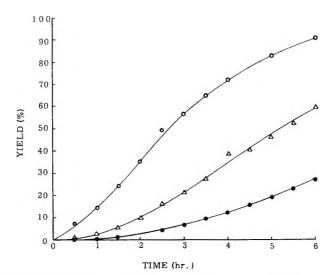


Fig. 1. Time-conversion curves of polymerization at various catalyst concentrations: (O) 3.300 mmole/l.; (Δ) 2.200 mmole/l.; (\bullet) 1.100 mmole/l. Reaction temperature: 0°C., styrene concentration: 5.228 mole/l.

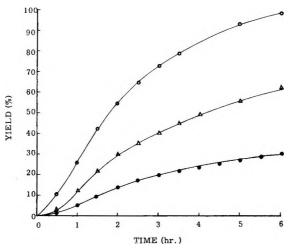


Fig. 2. Time-conversion curves of polymerization at various catalyst concentrations: (O) 1.100 mmole/l.; (Δ) 0.550 mmole/l.; (\bullet) 0.275 mmole/l. Reaction temperature: 10°C., styrene concentration: 5.228 mole/l.

Here, $[M]_s$ is stationary concentration of monomer and $[C]_0$ is initial concentration of catalyst which is used as an approximate value of the stationary state concentration of catalyst. Values of the rate constant k obtained from the straight lines of Figure 8 are plotted against 1/T as shown in Figure 9. From this plot, an activation energy of 29.1 kcal./mole is obtained. Also, as shown in Figure 10, values of τ obtained from Figures 1-6 satisfy the relationship:

$$1/\tau = k_{\tau} [C]_{0} [M]_{0}^{1.8}$$
(2)

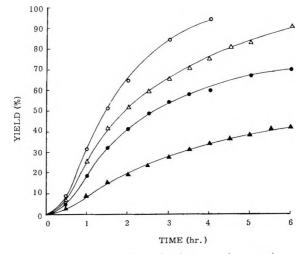


Fig. 3. Time-conversion curves of polymerization at various catalyst concentrations: (O) 0.330 mmole/l.; (Δ) 0.220 mmole/l.; (\bullet) 0.165 mmole/l.; (Δ) 0.110 mmole/l. Reaction temperature: 20°C., styrene concentration: 5.228 mole/l.

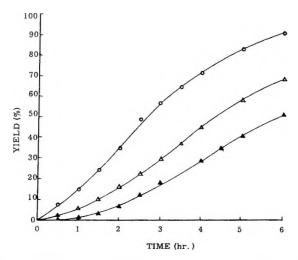


Fig. 4. Time-conversion curves of polymerization at various monomer (styrene) concentrations: (O) 5.228 mole/l.; (Δ) 3.485 mole/l.; (\bullet) 2.614 mole/l. Reaction temperature: 0°C., catalyst concentration: 3.300 mmole/l.

An Arrhenius plot of k_{τ} is shown in Figure 11 and an activation energy of 28.7 kcal./mole is obtained.

Degree of Polymerization

The variation of the degree of polymerization P with time is shown in Figure 12, where the change of yield with time is shown for comparison. It is obvious that the degree of polymerization attains a constant value at the stationary state. The relation between the degree of polymerization

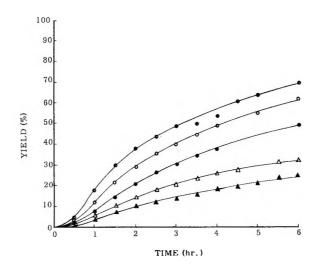


Fig. 5. Time-conversion curves of polymerization at various monomer (styrene) concentrations: (①) 6.099 mole/l.; (\bigcirc) 5.228 mole/l.; (\bigcirc) 4.357 mole/l.; (\triangle) 3.485 mole/l.; (\triangle) 2.614 mole/l. Reaction temperature: 10°C., catalyst concentration: 0.550 mmole/l.

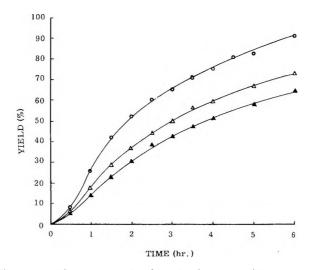


Fig. 6. Time-conversion curves of polymerization at various monomer (styrene) concentrations: (O) 5.228 mole/l.; (Δ) 3.485 mole/l.; (Δ) 2.614 mole/l. Reaction temperature: 20°C., catalyst concentration: 0.220 mmole/l.

and the initial concentration of monomer is shown in Figure 13, where the concentration of catalyst was kept constant. These measurements were conducted for system of styrene-benzene-ethyl monochloroacetate-catalyst where 5 ml. of ethyl monochloroacetate was used for the total volume of 50 ml. In order to determine the effect of ethyl monochloroacetate on the degree of polymerization, various quantities of ethyl monochloroacetate were

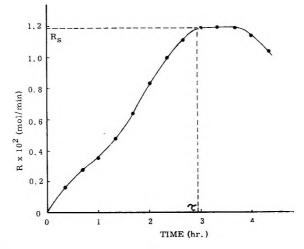


Fig. 7. Polymerization rate dependence on the reaction time. Reaction temperature: 0°C., catalyst concentration: 2.200 mmole/l., monomer concentration: 5.228 mole/l.

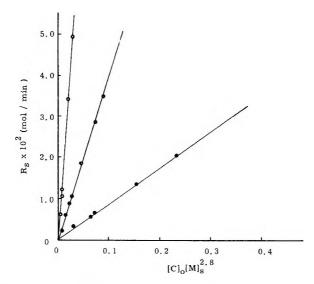


Fig. 8. Changes of polymerization rate with $[C]_0[M]_s^{2.8}$ at various temperatures: (\bullet) $0^{\circ}C.$; (\bullet) $10^{\circ}C.$; (O) $20^{\circ}C.$

used for 45 ml. of styrene without benzene and the concentration of catalyst was kept constant; results are shown in Figure 14.

Spectroscopic Measurements

Since color of the polymerization system changed from dark green to yellow brown during the polymerization, spectroscopic measurements were conducted at 20°C. to examine the change of visible and ultraviolet absorption during the polymerization. Also, spectra of the catalyst-benzene

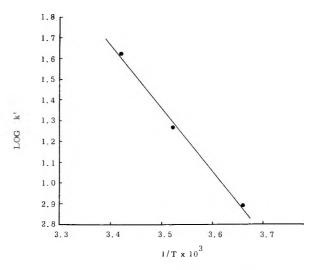


Fig. 9. Arrhenius plot of log k vs. 1/T.

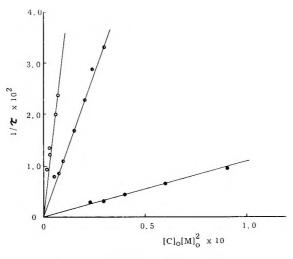


Fig. 10. Change of $1/\tau$ with $[C]_0[M]_0^2$.

and catalyst-ethyl monochloroacetate-benzene systems were examined as shown in Figures 15 and 16. In the catalyst-benzene system, the first absorption occurs at 3120 A. and the second absorption at 3550 A. By adding ethyl monochloroacetate, the first absorption shifts to 3220 A. and the second to 3600 A. As shown in Figure 17*a*, immediately after addition of styrene to the mixture of catalyst, ethyl monochloroacetate, and benzene, the first absorption moves to 3250 A. but the second does not change. Also, new peaks appear at 3050 and 2999 A. After 30 min. of mixing, as shown in Figure 17*b*, intensities of these new peaks increase, and those of absorptions at 3250 and 3600 A. decrease. Two hours after mixing, when

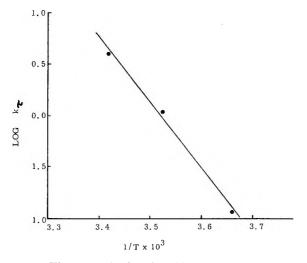


Fig. 11. Arrhenius plot of log $k\tau$ vs. 1/T.

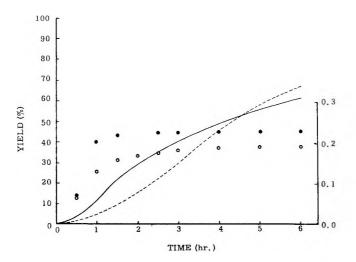


Fig. 12. Changes of intrinsic viscosity and conversion with polymerization time: (——) conversion and (\bullet) viscosity with polymerization at temperature of 10°C., monomer concentration of 5.228 mole/l., catalyst concentration of 0.550 mmole/l.; (---) conversion and (\bigcirc) viscosity with polymerization at temperature of 0°C., monomer concentration of 3.485 mole/l., catalyst concentration of 3.300 m mole/l.

the polymerization is supposed to be almost over, the new peaks at 2999 and 3050 A. disappear, as shown in Figure 17c.

In order to check whether the shift of the absorption spectra caused by the addition of ethyl monochloroacetate is due to the formation of a new bond, NMR and infrared spectra of a solution of rhenium pentachloride in ethyl monochloroacetate were measured. No evidence for the formation of a new bond was obtained.

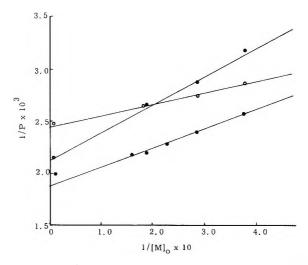


Fig. 13. Dependence of 1/p on the initial monomer concentrations: $(\oplus) 0^{\circ}$ C., catalyst concentration: 3.300 mmole/l.; $(\bullet) 10^{\circ}$ C., catalyst concentration of 0.550 mmole/l.; $(O) 20^{\circ}$ C., and catalyst concentration of 0.220 mmole/l.

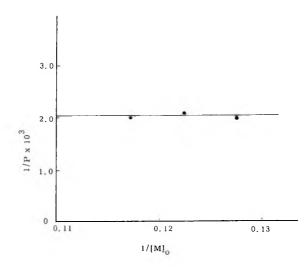


Fig. 14. Dependence of 1/p on the initial monomer concentration in the system without benzene. Reaction temperature: 10°C., catalyst concentration: 0.550 mmole/l.

Elementary Analysis

Results of elementary analysis of the polymer obtained are shown in Table I. Here, the molecular weight of the polymer calculated on the basis of the assumption that one polymer molecule contains one chlorine atom is compared with that obtained by vapor pressure osmometry.

The osmometric results are in sufficiently close agreement with the calculated molecular weights to indicate that each polymer molecule contains one chlorine atom.

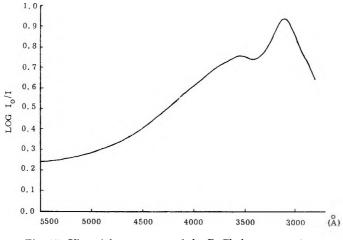


Fig. 15. Ultraviolet spectrum of the ReCl₅-benzene system.

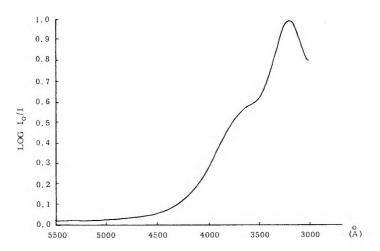


Fig. 16. Ultraviolet spectrum of the ReCls-ethyl monochloroacetate-benzene system.

TABLE I

No.	C, %	H, $\%$	Cl, %	Calc. M. W.	Measured M. W.
1	92.12	7.74	0.14	10,235	10,600
2	92.16	7.78	0.13	10,985	12,200

Effect of Ethylene Dichloride

Previously,³ it was found that ethylene dichloride promotes the polymerization of trioxane catalyzed by rhenium pentachloride. Therefore, the effect of the addition of ethylene dichloride was examined in the present case. The variations of yield with time at various concentrations of catalyst, monomer, and ethylene dichloride were measured as shown in

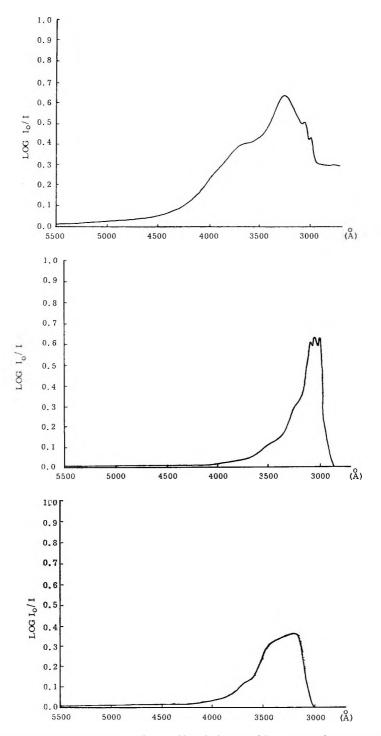


Fig. 17. Ultraviolet spectra of the ReCl₅-ethyl monochloroacetate-benzene-styrene system: (a) immediately after mixing; (b) 30 min. after mixing; (c) 2 hr. after mixing.

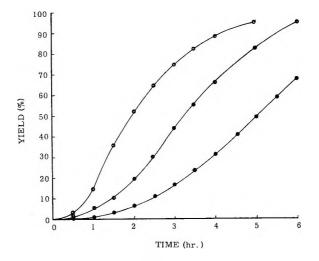


Fig. 18. Time-conversion curves of polymerization at 0°C. at various catalyst concentrations: (\oplus) 1.146 mmole/l.; (\oplus) 2.292 mmole/l.; (O) 4.584 mmole/l. Ethylene dichloride concentration: 4.234 mole/l., monomer concentration: 2.16 mole/l.

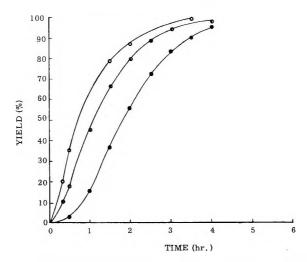


Fig. 19. Time-conversion curves of polymerization at 10°C. at various catalyst concentrations: (\bullet) 1.146 mmole/l.; (\bullet) 2.292 mmole/l.; (O) 4.584 mmole/l. Ethylene dichloride concentration: 4.234 mole/l., monomer concentration: 2.16 mole/l.

Figures 18–23. As shown in Figure 24, the stationary rate of polymerization R_s obtained from these figures is found to satisfy the eq. (3):

$$R_s = k' [E]_0^{0.5} [C]_0^{0.6} [M]_s^{1.8}$$
(3)

where, $[E]_0$ is the initial concentration of ethylene dichloride. The Arrhenius plot of k' is given in Figure 25, from which an activation energy of 13.6 kcal./mole is obtained. Also, the absorption spectrum of the ethylene dichloride-catalyst system is shown in Figure 26. Obviously, there

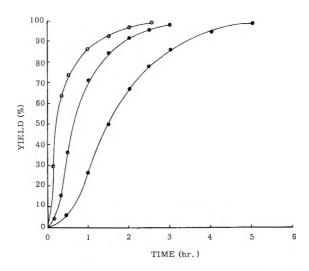


Fig. 20. Time-conversion curves of polymerization at 20°C. at various catalyst concentrations: (\bullet) 0.145 mmole/l.; (\bullet) 0.229 mmole/l.; (O) 0.342 mmole/l. Ethylene dichloride concentration: 4.234 mole/l., monomer concentration: 2.16 mole/l.

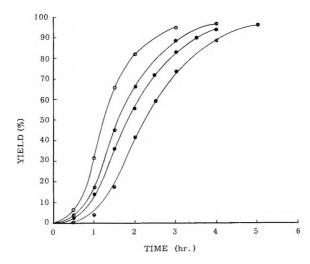


Fig. 21. Time-conversion curves of polymerization at various monomer concentrations: $(\odot) 1.57 \text{ mole/l.}$; $(\odot) 2.16 \text{ mole/l.}$; $(\odot) 2.67 \text{ mole/l.}$; (O) 3.46 mole/l. Ethylene dichloride concentration: 4.234 mole/l., reaction temperature: 10°C., catalyst concentration: 1.146 mmole/l.

is a new absorption at 3060 A. which was not observed in the systems not containing ethylene dichloride.

DISCUSSION

In order to explain the obtained results, the mechanism shown in eqs. (4)-(10) is proposed.

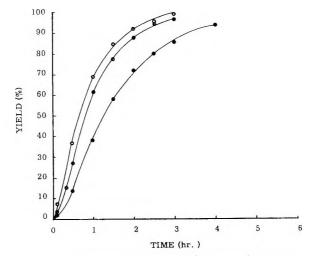


Fig. 22. Time-conversion curves of polymerization at various monomer concentrations: (\bullet) 0.77 mole/l.; (\bullet) 1.08 mole/l.; (O) 1.57 mole/l. Ethylene dichloride concentration: 4.234 mole/l., reaction temperature: 10°C., catalyst concentration: 1.46 mmole/l.

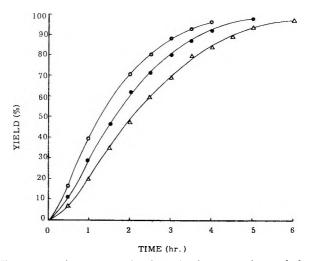


Fig. 23. Time-conversion curves of polymerization at various ethylene dichloride concentrations: (Δ) 2.17 mole/l.; (\odot) 4.234 mole/l.; (\bigcirc) 6.351 mole/l. Reaction temperature: 10°C., catalyst concentration: 1.15 mmole/l., monomer concentration: 2.16 mole/l.

Complex formation:

$$M + C \stackrel{k}{\rightleftharpoons} X \tag{4}$$

Initiation:

$$M + X \xrightarrow{k_i} XM^+$$
 (5)

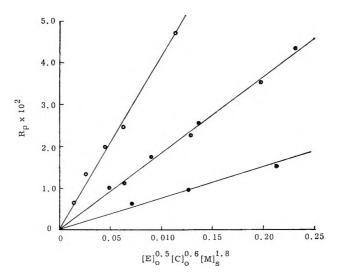


Fig. 24. Change of polymerization rate with $[E]_{0,5}[C]_{0,6}[M]_{a^{1,8}}$ at various temperatures: (•) 0°C.; (•) 10°C.; (•) 20°C.

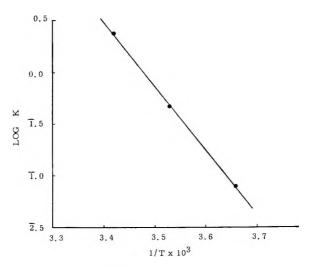


Fig. 25. Arrhenius plot of log k' vs. 1/T.

Propagation:

$$XM^{+} + M \xrightarrow{k_{p}} XM_{2}^{+}$$

$$\vdots$$

$$\vdots$$

$$(6)$$

$$XM_{-} + + M \xrightarrow{k_{p}} XM_{-} +$$

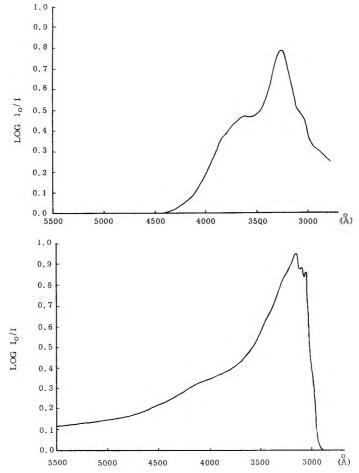


Fig. 26. Ultraviolet spectra of the systems (a) ReCl₅-ethylene dichloride; (b) ReCl₅-ethylene dichloride-styrene.

Termination:

$$XM_n^+ \xrightarrow{kt} XM_n \tag{7}$$

Transfer:

$$XM_n^+ + S \xrightarrow{ktrs} XM_n + S^+$$
 (8)

$$XM_{n}^{+} - S' \xrightarrow{ktrs'} XM_{n} + S'^{+}$$
(9)

$$XM_{n}^{+} + M \xrightarrow{\kappa \nu m} XM_{n} + M^{+}$$
(10)

Here, M is monomer, C catalyst, X complex between C and M, XM_n^+ growing cation, XM_n polymer, S benzene, and S' ethyl monochloroacetate.

For reaction (4), the following equilibrium equation is considered.

$$K = [\mathbf{X}]/[\mathbf{M}][\mathbf{C}] \tag{11}$$

In the stationary state, the total concentration of growing cations $\sum [XM_n^+]$ is considered to be a constant. Therefore,

$$\sum [XM_{n}^{+}]/dt = k_{i}[M]_{s}[X]_{s} - k_{T}[XM_{n}^{+}]_{s} = 0$$
(12)

Thus

$$\sum [\mathbf{X}\mathbf{M}_{n}^{+}]_{s} = (k_{i}/k_{T}) [\mathbf{M}]_{s} [\mathbf{X}]_{s}$$
(13)

$$k_T = k_t + k_{trs}[S] + k_{trs'}[S']$$
(14)

From eq. (11) and (13),

$$\sum [XM_{n}^{+}] = (Kk_{t}/k_{T}) [M]_{s}^{2} [C]_{s}$$
(15)

On the other hand, the stationary rate of polymerization R_s is given by

$$R_s = k_p [\mathbf{M}]_s \sum [\mathbf{X}\mathbf{M}_n^+]_s \tag{16}$$

By substituting eq. (15) into equation (16) we obtain

$$R_{s} = (Kk_{i}k_{p}/k_{T}) [C]_{s} [M]_{s}^{3}$$
(17)

If $[C]_s$ is equal to $[C]_0$, this equation is very similar to eq. (1). Also, an experimental activation energy of 29.1 kcal./mole is considered to be that of Kk_ik_p/k_T .

Next, the nonstationary state during the period τ will be considered. The rate of formation of growing cations is given by

$$d\sum[\mathbf{X}\mathbf{M}_{n}^{+}]/dt = k_{i}[\mathbf{X}][\mathbf{M}] - k_{T}[\mathbf{X}\mathbf{M}_{n}^{+}]$$
(18)

By integrating, we have

$$\sum [XM_n^+] = (k_i/k_T) [M]_0 [X]_0 (1 - e^{-kT_l})$$
(19)

The rate of polymerization is given by

$$-d[\mathbf{M}]/dt = k_p[\mathbf{M}]\sum[\mathbf{X}\mathbf{M}_n^+]$$
(20)

On integrating this, we have

$$\ln [\mathbf{M}]_{0} / [\mathbf{M}]_{s} = k_{p} \int_{0}^{\tau} \sum [\mathbf{X}\mathbf{M}_{n}^{+}] dt$$
(21)

Substituting this into eq. (19) yields

$$\ln [\mathbf{M}]_{0}[\mathbf{M}]_{s} = (k_{p}k_{i}/k_{T}) [\mathbf{M}]_{0}[\mathbf{X}]_{0} \int_{0}^{\tau} (1 - e^{-k_{T}t}) dt$$
$$= (k_{p}k_{i}/k_{T}) [\mathbf{M}]_{0}[\mathbf{X}]_{0}\tau + (k_{p}k_{i}/k_{T^{2}}) [\mathbf{M}]_{0}[\mathbf{X}]_{0}(e^{-k_{T}\tau} - 1)$$
(22)

Here, the magnitude of k_{τ} in the typical cationic polymerization of styrene is ca. 10^{-2} sec.⁵ and τ in the present experiment is 10^{3} - 10^{4} sec. Since the term, $e^{-k_{\tau}\tau}$ is far smaller than unity, this can be neglected. Thus,

$$\ln [M]_0 / [M]_s = (k_p k_i / k_T) [M]_0 [X]_0 [\tau - (1/k_T)]$$
(23)

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Also, $1/k_T$ may be neglected when compared with τ . Therefore,

$$\ln [M]_{0} / [M]_{s} = (k_{p}k_{i}/k_{T}) [M]_{0} [X]_{0} \tau$$
(24)

By substituting eq. (11) into this and rearranging, we have

$$1/\tau = (Kk_p k_t / k_T) [C]_0 [M]_0^2 \ln [M]_s / [M]_0$$
(25)

In the present experimental conditions, $\ln [M]_s/[M]_0$ is almost constant. Therefore, the following relationship is obtained.

$$1/\tau \propto (Kk_p k_i / k_T) [C]_0 [M]_0^2$$
 (26)

This almost agrees with eq. (2). Thus, the experimental activation energy of 28.7 kcal./mole for k_{τ} of the eq. (2) is considered to be equivalent to $Kk_{p}k_{t}/k_{T}$. In the discussion of eq. (17), a value of 29.1 kcal./mole was proposed for the activation energy of $Kk_{p}k_{t}/k_{T}$. Therefore, the mechanism above described is considered reasonable from the measurements of both the stationary polymerization rate and the time τ .

Then, the average degree of polymerization is given by eq. (27):⁶

$$1/P = (k_{trm}/k_p) + (k_{trs}[S]/k_p[M]) + (k_{trs}'[S']/k_p[M]) + (k_t/k_p[M])$$
(27)

When the total volume of the polymerization system is kept constant and only the ratio of styrene to benzene is changed, this equation becomes:⁷

$$1/P \left[(k_{trm} - bk_{trs} + ak_{trs} + k_s')/k_p \right] 1/[M]$$
(28)

Here,

$$k_{s}' = k_{t} + k_{trs}'[S'] - k_{trs}[S]$$

$$a = 1000d_{s}/W_{s},$$

$$b = d_{s}W_{m}/d_{m}W_{s}$$

and

$$C = d_s W_s'/d_s' W_s$$

where d_s , d_s' , and d_m are densities and W_s , W_s' , and $W_{m'}$ are molecular weights of benzene, ethyl monochloroacetate, and styrene, respectively. From the slopes and intercepts of Figure 13, values of $ak_{trs}/k_p + k_{s'}/k_p$ and $k_{trm}/k_p - bk_{trs}/k_p$ are obtained. Also, from Figure 14, it is obvious that $ak_{trs}/k_p + k_{s'}/k_p$ becomes zero for the system without benzene. In this system, bk_{trs}/k_p may be ignored. Therefore, k_{trm}/k_p can be calculated from

Temperature, °C.	k_{trm}/k_p	k_{trs}/k_p	
0	2.13×10^{-3}	$2.00 imes 10^{-4}$	
10	2.00×10^{-3}	0.95×10^{-4}	
20	2.47×10^{-3}	0.79×10^{-4} °	

TABLE II

the intercept of Figure 16. By substituting the value of k_{trm}/k_p into the value of $k_{trm}/k_p - bk_{trs}/k_p$, k_{trs}/k_p can be calculated as shown in Table II. These values of k_{trm}/k_p and k_{trs}/k_p are about one tenth of those obtained for the polymerization of styrene in benzene catalyzed by BF₃·OEt₂, SnCl₄, and TiCl₄.⁷ This suggests that rhenium pentachloride is a stronger Lewis acid than these catalysts.^{5b}

When ethyl monochloroacetate was added to the benzene-catalyst system, the absorption peaks moved toward the longer wavelength. This shift might be due to the polar effect of ethyl monochloroacetate as usually observed in the addition of polar solvent.⁸ Also, the shift of the second peak observed when styrene was added is considered to be due to the formation of a π -complex⁹ between styrene and rhenium pentachloride. Moreover, new peaks observed at 2999 A. and 3050 A. during the polymerization are considered to be due to the growing cation. Jordan et al.¹⁰ observed a new absorption at 4100-4200 A. in the polymerization of styrene catalyzed by $SnCl_4$ and $AlCl_3$ and claimed that this is an absorption by growing cation. However, Higashimura¹¹ observed an absorption at 4100 A. even in the system of polystyrene-SnCl₄-HCl and also found a new absorption at 3090 A. in the polymerization system. Thus, Higashimura proposed that the absorption at 3090 A. must be due to the existence of growing cation. The present results support his proposition. Taking into account these results, a more detailed mechanism is considered. Since the coordination number of rhenium is 6-8, π -complex formation between rhenium pentachloride and styrene is equally possible as in the case of SnCl₄ and styrene.¹² This process corresponds to the process of complex formation. Then, this complex forms a new π -bonding with another styrene monomer molecule and at the same time loses one chlorine atom. Thus, a carbonium ion and a chloride ion are formed. In this initiation process, the formation of new π -bond and the cleavage of Re-Cl occur and it requires a rather large activation energy. Therefore, it seems reasonable that the experimental activation energy is far larger than that of the usual cationic polymerization.^{5c} The cation formed reacts further with monomer to give a cation of higher degree of polymerization. This corresponds to the propagation process. Since a polymer molecule contains one atom of chlorine according to the elementary analysis, a growing cation is considered to recombine with Also, the polymer cation disappears on transfer with a chloride ion. monomer or solvent. The above explanation is summarized by eqs. (29)-(32).

$$\operatorname{ReCl}_{5} + \operatorname{St} \rightleftharpoons \operatorname{St} - - - - \operatorname{ReCl}_{5}$$

$$\tag{29}$$

$$St - - - - ReCl_5 + St \rightarrow St - - - ReCl_4St^+Cl^-$$
 (30)

$$---- \operatorname{ReCl}_{4}\operatorname{St}^{+}\operatorname{Cl}^{-} + \operatorname{St} \to \operatorname{St} - - - - \operatorname{ReCl}_{4}\operatorname{St}_{2}^{+}\operatorname{Cl}^{-}$$

$$(31)$$

$$\mathrm{St} - - - - \mathrm{ReCl}_{4}\mathrm{St}_{n-1}^{+}\mathrm{Cl}^{-} + \mathrm{St} \rightarrow \mathrm{St} \ldots \mathrm{ReCl}_{4}\mathrm{St}_{n}^{+}\mathrm{Cl}^{-}$$

 \mathbf{St}

$$\mathrm{St} - - - - \mathrm{ReCl}_{4}\mathrm{St}_{n} + \mathrm{Cl}^{-} \to \mathrm{St} \ldots \mathrm{ReCl}_{4}\mathrm{St}_{n}\mathrm{Cl}$$
 (32)

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When ethylene dichloride is added, the above scheme is not applicable for the results obtained. Kennedy et al.¹³ considered the formation of $[CH_3]^+AlCl_4^-$ from AlCl₃ and CH₃Cl for the polymerization of isobutene catalyzed by AICl₃ in methyl chloride. Also, the absorption at 3060 A. in Figure 26 suggests the existence of an intermediate complex between rhenium pentachloride and ethylene dichloride. Therefore, the present case is explained by assuming the same type of complex formation as shown in eqs. (33)–(36).

$$\operatorname{ReCl}_{5} + \operatorname{CH}_{2}\operatorname{Cl} - \operatorname{CH}_{2}\operatorname{Cl} \rightleftharpoons \operatorname{ReCl}_{5} \dots \operatorname{ClCH}_{2} - \operatorname{CH}_{2}\operatorname{Cl} \rightleftharpoons \operatorname{ReCl}_{6}^{-} + \operatorname{*CH}_{2}\operatorname{CH}_{2}\operatorname{Cl} \quad (33)$$

$$kt$$

$$^{+}CH_{2}CH_{2}Cl + St \xrightarrow{\sim} (CH_{2}CH_{2}Cl)St^{+}$$
(34)

 $(\mathrm{CH}_{2}\mathrm{CH}_{2}\mathrm{Cl})\mathrm{St}^{+} + \mathrm{St} \xrightarrow{k_{\mathcal{P}}} (\mathrm{CH}_{2}\mathrm{CH}_{3}\mathrm{Cl})\mathrm{St}_{2}^{+}$

$$(CH_2CH_2Cl)St_{n-1}^{+} + St \xrightarrow{kp} (CH_2CH_2Cl)St_n^{+}$$
(35)

$$(CH_2CH_2Cl)St_n^+ + ReCl_6^- \xrightarrow{\sim} (CH_2CH_2Cl)St_nCl + ReCl_5$$
 (36)

By applying stationary state approximation for this scheme, the stationary rate R_s is given by

$$R_{s} = (k_{t}k_{p}/k_{t})(K_{1}K_{2})^{0.5}[C]_{s}^{0.5}[C]_{s}^{0.5}[M]_{s}^{2}$$
(37)

If $[C]_s$ is equal to $[C]_0$ and $[E]_s$ equal to $[E]_0$, this equation is very similar to eq. (3). Therefore, the experimental activation energy of 13.6 kcal./ mole is that of $(k_i k_p/k_t) (K_1 K_2)^{0.5}$.

The authors wish to thank Dr. J. Tsuji and Mr. M. Morikawa for their advice, to Dr. K. Nukada and Mr. Y. Goto for the measurement of NMR spectra and to Messrs. K. Sugiyama and J. Takeda for their help in the experiment.

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Résumé

On a obtenu un polystyrène de haut poids moléculaire et avec un bon rendement, par polymérisation du styrène catalysée par le pentachlorure de rhénium, dans une solution de benzène ou de benzène-dichloro-éthylène. Le mécanisme de cette polymérisation a été étudié par des mesures cinétiques et spectroscopiques. On peut expliquer les résultats expérimentaux si on accepte qu'un complexe π entre le pentachlorure de rhénium et le monomère initie la polymérisation cationique dans le cas de la solution benzénique et que +CH₂CH₂Cl initie la polymérisation en présence de dichloro-éthylène.

Zusammenfassung

Hochmolekulares Polystyrol wurde in guter Ausbeute durch die Rheniumpentachlorid in Benzol oder Benzol-Äthylendichloridlösung katalysierte Polymerisation von Styrol erhalten. Der Mechanismus dieser Polymerisationsreaktion wurde durch kinetische und spektroskopische Messungen untersucht. Die Versuchsergebnisse lassen sich durch die Annahme, dass π -Komplexe zwischen Rheniumpentachlorid und dem Monomeren im Falle der Benzollösung die kationische Polymerisation starten und dass +CH₂CH₂Cl die kationische Polymerisation in Gegenwart von Äthylendichlorid anregt, gut erklaren.

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Shear Dependence of Viscosity–Molecular Weight Transitions. A Study of Entanglement Effects

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Synopsis

The flow behavior of concentrated polymer solutions covering molecular weights up to 150,000 were examined at shear rates up to 200,000 sec.⁻¹. The viscosity-molecular weight-shear rate results of previous workers recognizing only single critical molecular weight M^* , above which ordinary Bueche entanglements dominated the flow, were compared with our findings in which two distinct critical molecular weights, upper M^* and lower M^{**} exist. These results are compared with the theory, and new interpretations are presented.

INTRODUCTION

The viscosity of concentrated solutions of polymers has been the subject of many investigations. Typical systems reported include: cellulose nitrate,¹ polystyrene,² polyisobutylene,³ cellulose tributyrate,⁴ poly(methyl methacrylate),⁵ poly(vinyl alcohol),⁶ and many others.

It has been evident in all of these studies that the primary effect of shear is a breaking down of molecular interactions arising from chain entanglement and/or attractive forces between polar groups. Since chain entanglement is a function of both size and number of molecules, solute molecular weight and concentration are controlling factors. Bueche⁷ has shown that the low-shear viscosity η_0 of concentrated polymer solutions is proportional to molecular weight M below a critical value, M^* , whereas above M^* , it increases rapidly and becomes proportional to $M^{3.4}$.

With respect to concentration Ferry et al.⁸ and later Fox and Loshaek⁹ have shown empirically that the zero-shear viscosity is proportional to the fifth power of the concentration for M values above M^* .

Accordingly, the dependence of the zero-shear viscosity on concentration and molecular weight for values of molecular weight greater than M^* can be expressed by the equation:

$$\eta_0 \propto C^5 M^{3.4} \tag{1}$$

Porter and Johnson¹⁰ have discussed the effect of shear rate on the observed transitions in the viscosity as molecular weight is varied. Figure 1a shows their estimation of the viscosity behavior at low and high shear limits. The viscosity transition point is interpreted as reflecting the onset

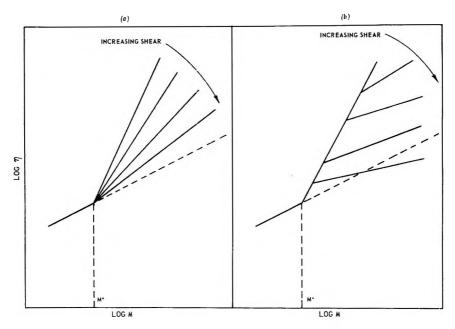


Fig. 1. Possible shear dependence of viscosity-molecular weight function of polymers.

of a network structure due to entanglement. Porter and Johnson state that "if the importance of imagined polymer entanglement becomes less with shear, then limiting high shear viscosity should increase with molecular weight in a way similar to that for simple molecules." The limiting Newtonian behavior can be approximated by extending the slope in Figure 1*a* for low molecular weights up into the non-Newtonian region. Further, this implies that the viscosity dependence on molecular weight varies smoothly from the 3.4 power at very low shear to the first power at very high shear rate.

Recently Schreiber et al.¹¹ have presented data on polyethylene over a wide molecular weight range $(M^* < M < 70M^*)$. A general representation of their findings is shown in Figure 1b. This figure also indicates that the critical molecular weight M^* for initial chain entanglement is independent of shear. However, it differs from Figure 1a in providing significant evidence that as shear is increased there is a sharp, shear-dependent transition in either the degree or type of entanglement. The molecular weight at which this second or β transition occurs is lower the higher the shear rate. Above this β transition, the molecular weight dependence falls to a fractional power, suggesting the involvement of segmental motion, and thus the flow is again non-Newtonian. Schreiber¹² has presented a qualitative view of molecular motion in the entangled state to account for his findings.

The purposes of our work are: (a) to elucidate the role of chain entanglements in the non-Newtonian flow of polymer solutions; (b) to gain a better understanding of the shear-rate dependence of the viscosity-molecular weight function for a relatively complex system, i.e., AN-MMA copolymer/ aqueous NaCNS solvent; (c) to check Bueche's theory of polymer entanglement and the various ways of representing as well as estimating the low- and high-shear viscosity limits.

EXPERIMENTAL

Materials

Several copolymers of acrylonitrile and methyl methacrylate (90/10) were prepared in a continuous reactor with a chlorate-sulfite redox system as catalyst. The weight-average molecular weight (\overline{M}_w) of the copolymers was determined by light scattering and covered a range between 20,000 and 156,000. Reagent grade sodium thiocyanate and deionized water were used to prepare 48% by weight aqueous NaCNS solvent which was subsequently used to prepare polymer solutions containing up to 13% by weight of polymer.

Apparatus and Procedure

An Ubbelohde glass viscometer was used for viscosity measurement at very low shear rate. The flow measurements at high shear rates were made by using the stainless steel capillary viscometer described earlier.¹³ End effect corrections were assumed to be negligible, since the capillary employed had a length/diameter ratio of 165. Kinetic energy corrections were applied at low concentrations.

Calculation of Viscosity

The values of the consistency variables, apparent shear rate D, and maximum shear stress at the capillary wall τ_w were calculated from the equations:

$$D = 4Q/\pi r^3 \tag{2}$$

and

$$\tau_w = \Delta P r / 2l \tag{3}$$

where Q is the volume flow rate in cubic centimeters/second, l is the capillary length in centimeters, r is the capillary radius in centimeters, and ΔP is the applied pressure in dynes/square centimeter corrected for kinetic energy loss. The apparent shear rate D was converted to maximum shear rate at the capillary wall, D_w by using the Rabinowitsch equation:

$$D_w = D(3 + \gamma)/4 \tag{4}$$

where γ is defined as $d \log D/d \log \tau_w$ at any D. The ratio of τ_w to D_w gives the viscosity at the wall in poises.

RESULTS AND DISCUSSION

Concentration and Molecular Weight Dependence of Viscosity at Low Shear Rates

The concentration dependence of specific viscosity at a constant temperature of 30°C. is shown in Figure 2, wherein the highest molecular weight polymer examined was 156,000 while the lowest one was 20,000.

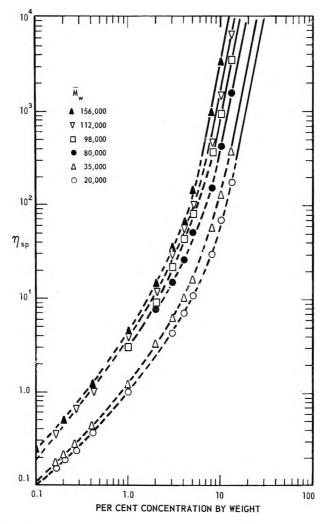


Fig. 2. Concentration dependence of low-shear specific viscosity at 30°C.

The results show that the specific viscosity rises exponentially with concentration. This effect is more pronounced and occurs at a lower concentration, the higher the molecular weight of the material. A twodecade change in concentration extends over nearly five decades of specific

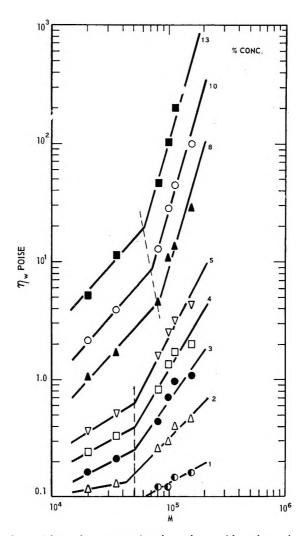


Fig. 3. Molecular weight and concentration dependence of low-shear absolute viscosity at 30 $^{\circ}\mathrm{C}.$

viscosity at high molecular weight level while the corresponding range at low molecular weight level is about three decades.

The solid lines in Figure 2 are drawn with a slope of 5, indicating that above a certain critical value C^* , specific viscosity $\eta_{sp} \propto C^5$. In our work, this appears to occur only at η_{sp} values greater than 300.

The molecular weight dependence of the low-shear absolute viscosity at 30° C. for solutions of various concentrations is shown in Figure 3. In accordance with the findings of other investigators, our system also shows an abrupt change of slope in the viscosity values above a certain critical molecular weight. This transition point is assumed to reflect Bueche entanglements.

The manner in which the slope of the viscosity-molecular weight relation depends on concentration is not very clearly understood. Examination of the data indicates that two broad categories can be formed: one including concentrations up through 5% and the other, concentrations of 8% and above. In the latter category, M^* , in agreement with theory, is inversely proportional to concentration (shown by the dotted line in Fig. Also, at high molecular weight the viscosity is proportional to the 3).theoretical 3.4 power of molecular weight. The agreement can be judged by noting that the experimental points fall on the straight lines which are drawn with a slope of 3.4. Since the viscosity measurements are accurate to $\pm 1\%$, the failure of the highest molecular weight value to fall on the lines of slope 3.4 suggests that this polymer sample may actually have had a molecular weight of 138,000 instead of 156,000 as shown. Below M^* , the slope is essentially equal to 1, indicating Newtonian behavior.

In the first category, the lines above M^* have also arbitrarily been drawn to pass through 138,000 at the highest molecular weight. However, M^* has lower values, and although it still appears to be roughly inversely proportional to concentration, the relation is by no means certain. Further, the slopes of the η_w -M plots deviate markedly from the theoretical values, decreasing gradually to 0.5 above M^* and to near zero below M^* at low concentration.

The reason for such a gradual change in the slopes both above and below M^* , and the deviations from a theoretical limiting value of unity is not clearly understood, since no permanent viscosity degradation is observed in this system.

Evaluation of M^*C^*

Examination of the slopes in Figures 2 and 3 makes it obvious that precise determination of M^* and C^* is difficult.

If the same results are plotted in accordance with eq. (1), it becomes possible to interrelate the dependence of viscosity on concentration and molecular weight by a single composite curve as shown in Figure 4. At high values of the abscissa, the curve has a linear portion with a slope of unity. For those combinations of M and C which lie on this straight line, the flow behavior is dominated by ordinary Bueche polymer entanglement, that is one polymer molecule has at least one other molecule so entangled with it that the two must move essentially as one. Deviation from the straight line indicates that eq. (1) is no longer valid, and the minimum values of M and C at which this occurs are designated as critical values M^* and C^* . Examination of Figure 4 suggests that eq. (1) is valid between the limits:

$$12.0 < (5 \log C + 3.4 \log M) < 13.5 \tag{5}$$

Ferry⁴ has suggested that the product CM be taken as a measure of the average number of Bueche entanglements per molecule, ξ . The average molecular weight between entanglements, M_{e_1} is M_{e_2}/ν_2 , where M_{e_2} is the

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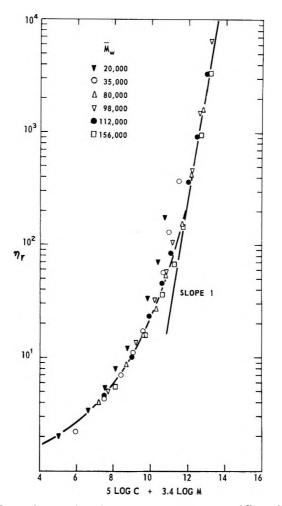


Fig. 4. Dependence of low-shear relative viscosity at 30° C. on $C^{5}M^{3.4}$.

value of M_e extrapolated to the hypothetical undiluted polymer in an uncrystallized state and ν_2 is the volume fraction of polymer and is equal to C/ρ , where ρ is the density of the undiluted polymer. In other words, the value of C/ρ represents the fraction of the volume occupied by the polymer at a given concentration. If we assume that at the onset of a continuous network, ξ is 2, then for a given polymer when $M = M^*$:

$$\xi = M/M_{e} = M/M_{ex} \nu_{2} = CM/\rho M_{ex} = 2$$
(6)

The experimental data can be used to check this assumption. Ferry¹⁰ has suggested that an estimate of M_{ex} can be obtained by plotting as abscissa log M + log C and as ordinate log η_{τ} - 1.6 log C, so that above CM^* all the data would coincide on a straight line of slope 3.4. It was found that the values of CM^* above 8500 \pm 2000 do fall on a straight line with slope of 3.4. This then, from eq. (6), corresponds to M_{ex} equal

to 3600. From Figure 4, we have $C^5M^{3.4} = 10^{12}$ as the point of deviation from a straight line with slope of unity. Thus, for a 10% (by weight) solution, M^* would be 71,000, and ν_2M^* would be 7500, and ξ would be close enough to the value 2. This treatment is valid only within the molecular weight range and concentrations examined. At very high concentrations and molecular weights, calculations of ξ do not come close to a value of 2, and therefore the general validity of the above treatment is questionable.

Shear Rate Dependence of Absolute Viscosity

The shear dependence of the viscosity-molecular weight function for concentrated macromolecular solutions is shown in Figures 5-8. At the

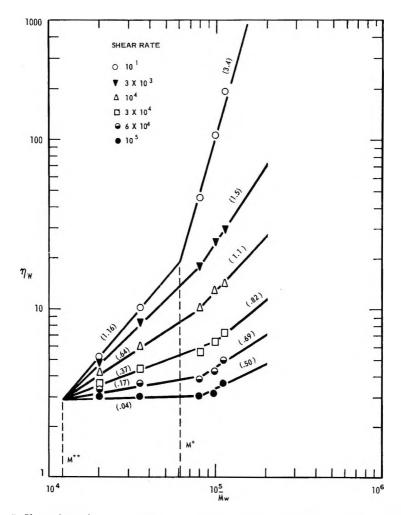


Fig. 5. Shear dependence of viscosity-molecular weight function for a 13% by weight solution at 30°C. Values in parentheses indicate the slopes of the lines.

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highest concentrations, the variation in viscosity with shear rates is very large. For example, at 13% by weight concentration, there is a 100-fold variation in viscosity when the shear rate is changed from 10^1 to 10^5 sec.⁻¹ while at 5% concentration the corresponding variation is only 7-fold.

Further, these solutions of AN-MMA copolymer in aqueous NaCNS seem to be unique, in that this is the first system that appears to possess two distinct critical molecular weights. Therefore, it is important to define the terminology that has been used to distinguish them.

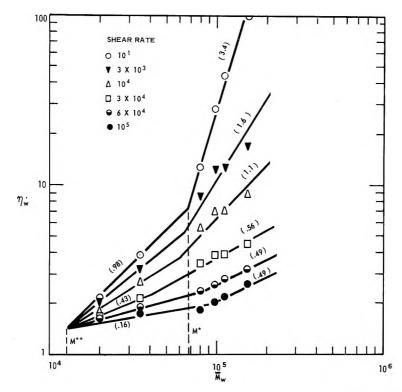


Fig. 6. Shear dependence of viscosity-molecular weight function for a 10% by weight solution at 30°C. Values in parentheses indicate the slopes of the lines.

 M^* refers to the critical molecular weight associated with Bueche-type chain entanglements. Thus, M^* is the molecular weight at which there exists an abrupt change in the slope $(dln\eta/dlnM)$. It is usually independent of shear, but experimental evidence has been presented by Schreiber¹¹ indicating a system wherein M^* appears first to increase with shear rate and then decrease at still higher shear rates, the smallest M^* value being at the lowest shear rate. M^{**} refers to the second critical molecular weight, and it is the highest molecular weight at which η appears to be independent of shear rate D. It is lower than M^* and has been assumed to be associated with entanglements arising from dipole-dipole interactions or hydrogen bonding.

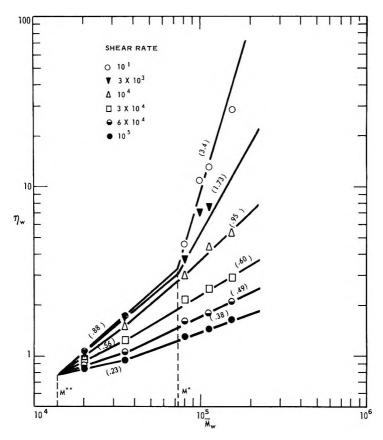


Fig. 7. Shear dependence of viscosity-molecular weight function for an 8% by weight solution at 30°C. Values in parentheses indicate the slopes of the lines.

There are three distinct regions which must be critically examined. These are: (a) a region above the upper critical molecular weight M^* ; (b) a region below M^* but greater than the lower critical molecular weight M^{**} ; and (c) a region below M^{**} .

In accordance with the Bueche⁷ theory of ordinary chain entanglements, the highest viscosity-molecular weight slope of 3.4 was obtained above M^* and at low shear rates. The limiting theoretical value below the transition M^* and at high shear rates may be unity for certain systems over a narrow molecular weight range. However, our findings are that the viscosity-molecular weight-shear function changes as follows.

(a) At molecular weights greater than M^* , the influence of ordinary chain entanglement diminishes at increased shear rates and ultimately attains a limiting value at high shear; simultaneously, the viscositymolecular weight function also attains a limiting slope of one half. Thus, in this region, the contribution to non-Newtonian viscosity comes from coupled or entangled chains and their deformation due to flow orientation at increased shear rates. Another novel observation in these results is

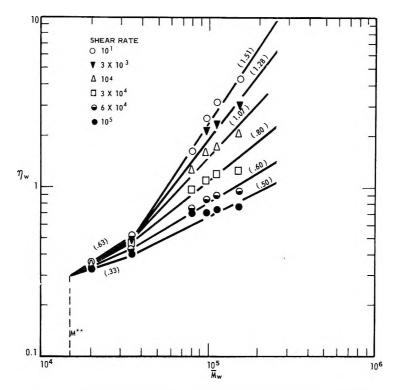


Fig. 8. Shear dependence of viscosity-molecular weight function for a 5% by weight solution at 30°C. Values in parentheses indicate the slopes of the lines.

that the various shear rate lines of the plot do not extrapolate to a common intersection point M^* , even though M^* remains essentially constant at all shear rates examined. This is indicated by the dotted line in the figures labeled M^* . The variation of the breakpoint from the dotted line position is indicative of the experimental precision at increased shear rate. Such behavior does not agree with those reported by other investigators, which is shown in Figure 1.

(b) At molecular weights lower than M^* but greater than M^{**} , the slopes of the viscosity-molecular weight lines decrease from 1.16 to near zero with increasing shear rates. Also, the limiting slope at high shear rate increases as the concentration is lowered from 13% to 5%, and it appears that a limiting slope of one-half will result in this region also at some lower concentration.

A qualitative explanation of this is that at higher concentrations there are a large number of strong secondary interactions which are associated with dipole-dipole interaction or hydrogen-bonding. These interactions result in a more stable quasi-lattice structure which has a different relaxation behavior than that existing at lower concentration.

The triangular area between the highest and lowest shear curves bounded by M^{**} and M^* also contracts as the concentration is lowered. It is believed that in this region, the contribution to non-Newtonian viscosity comes from entanglement arising from dipole-dipole interaction or hydrogen bonding. The fact that the lower critical molecular weight M^{**} occurs at such a low molecular weight signifies that in this system, non-Newtonian viscosity behavior is not due to deformation of individual molecules as expressed by Porter and Johnson¹⁴ in their general description of non-Newtonian flow.

Contrary to the behavior observed for M^* in (a) in this region, the plots in Figures 5-8 extrapolate to essentially a common value corresponding to a lower critical molecular weight M^{**} below which viscosity is expected to be independent of shear. The value of M^{**} was found to be inversely proportional to concentration in a manner similar to M^* . At very low molecular weight where $M < M^{**}$, any contribution of entanglement effects to non-Newtonian viscosity is absent, and the behavior should be Newtonian at attainable shear rates.

In this study, the molecular weight distribution is broad in all samples, and its effect on the exponents is not detectable. In general, the broader the molecular weight distribution in a given polymer, the more the viscosity will decrease with increasing shear rate.

Some scatter at high shear rates in the data at $M > M^*$ is observed and is believed to be due to the variations in the molecular weight distribution which causes differences in shear dependence. The limiting slope may also depend upon the polymer, the solvent, and the polymer-solvent system.

In studying the viscosity slope values, it was noticed that the slope of the line has in general the same value at a given shear rate, irrespective of the initial concentration of the polymer in the macromolecular solution. This behavior may be due to an important fundamental property of the macromolecule whereby the manner and rate of its deformation at a given shear rate are a characteristic of the polymer-solvent system and are independent of the initial concentration.

From the results of Figures 5-8, it appears that the critical molecular weights M^* and M^{**} are essentially independent of the velocity gradient.

The reduction in the value of the viscosity slopes is due to deformation and reduced intermolecular entanglement effects at increasing shear rate. At the limiting shear rates, the macromolecules are presumed to be in a well oriented, unentangled configuration.

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Résumé

Le comportement à l'écoulement de solutions concentrées de polymères de poids moléculaires allant jusqu'à 150.000, a été étudié à des vitesses de cisaillement allant jusqu'à 200.000 sec⁻¹. Les résultats de la viscosité/du poids moléculaire/de la vitesse de cisaillement, donnés par des auteurs antérieurs, qui admettant seulement un poids moléculaire critique M^* , au-dessus duquel les emmêlements ordinaires de Bueche dominent l'écoulement, sont comparés avec les découvertes qui montrent l'existence de deux poids moléculaires critiques différents, un M^* plus élevé et M^{**} plus bas. Ces résultats sont comparés avec la théorie, et de nouvelles interprétations sont présentées.

Zusammenfassung

Das Fliessverhalten von konzentrierten Polymerlösungen wurde im Molekulargewichtsbereich bis hinauf zu 150,000 bei Schubgeschwindigkeiten bis zu 200,000 sec⁻¹ untersucht. Die Viskositäts-Molekulargewichts-Schubgeschwindigkeitsergebnisse früherer Autoren, bei denen nur ein kritisches Molekulargewicht M^* auftrat, oberhalb welchem gewöhnliche Bueche-Verschlingungen das Fliessen bestimmten, wurden mit unseren Befunden verglichen, bei welchen zwei verschiedene kritische Molekulargewichte, oberes M^* und unteres M^{**} bestehen. Die Ergebnisse werden mit der Theorie verglichen und eine neue Interpretation wird gegeben.

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Aromatic Polypyromellitimides from Aromatic Polyamic Acids*

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Synopsis

Aromatic diamines react with pyromellitic dianhydride in solvents such as dimethylacetamide to form solutions of high molecular weight polyamic acids. These soluble polymers can be converted to insoluble aromatic polyimides. The aromatic polyimides exhibit zero strength temperatures above 700°C. and possess excellent thermal and oxidative stability. The stability characteristics of films and the relation of chemical structure to thermal and hydrolytic stability and to polymer properties such as crystallinity are described.

INTRODUCTION

We have been interested for some time in the possibilities of preparing intractable condensation polymers by conversion of a high molecular weight, tractable precursor. Most studies of condensation polymerization have been concerned with rather simple elimination reactions to form polymers which are rheologically manageable, thereby permitting formation of variously shaped objects. We wish to report the preparation and properties of a new group of condensation polymers, the aromatic polyimides, which are unusually high melting, intractable, insoluble, and possess outstanding thermal stability.

Earlier workers in this field prepared polyimides by polyamide-salt techniques.¹⁻³ Thus, pyromellitic dianhydride was reacted with ethanol to form the diester-diacid, which was treated with diamine to precipitate the monomeric diester-diacid salt. The salt was then heated to form a polymerizing melt, which, after dehydration and dealcoholation in the melt, formed the polyimide. Recently several du Pont patents⁴ and patent applications⁵ disclosing other synthetic routes have appeared and have been

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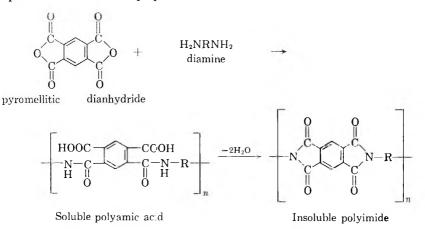
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cited in subsequent literature articles. $^{6-8}$ Published thermal stability data^{7,8} have confirmed our observations.

This paper, which reviews activity in this laboratory over the last several years, describes the formation of polypyromellitimides by direct polymerization of pyromellitic dianhydride* and aromatic diamines in solvents such as dimethylacetamide or dimethylformamide to soluble, high molecular weight polyamic acids (also called polyamide acids). The polyamic acids are then dehydrated to polyimides of high molecular weight. The details of polymerization and the relationship of polyimide structure to properties as illustrated by specific diamines are included.



where R may be p-phenylene; m-phenylene; p,p'-biphenylene; 4,4'-diphenylene ether, sulfide, sulfone, methylene, and -isopropylidene.

EXPERIMENTAL

Reagents

Dimethylacetamide. du Pont technical grade material was distilled from phosphorus pentoxide at 30 mm. Hg.

Dimethylformamide. du Pont technical grade material was distilled from phosphorus pentoxide at 20 mm. Hg.

Diamines. Bis(4-aminophenyl) ether was purified by vacuum drying at 50°C. at ≤ 1 mm. Hg for 8 hr.

Bis(4-aminophenyl) sulfide was purified by decolorization of an aqueous solution of the dihydrochloride salt followed by precipitation with base and codistillation with dioctyl phthalate at ≤ 1 mm. Hg. White crystals of diamine which separated from the distillate on cooling were washed three times with petroleum ether and dried at ≤ 1 mm. Hg.

m-Phenylenediamine was purified by vacuum distillation.

Bis(4-aminophenyl) sulfone was best purified by recrystallization from an aqueous ethanol solution followed by vigorous vacuum drying.

* Polyimides derived from other dianhydrides will be described in future publications.

Pyromellitic Dianhydride. Technical grade material of the du Pont Explosives Department was sublimed through silica gel at 220-240°C. and 0.25-1 mm. mercury pressure.

Polymerizations

Typical Preparation of a Polyamic Acid. A 500-ml. flask fitted with mercury-seal stirrer, nitrogen inlet, drying tube, and stopper is carefully flamed to remove traces of water on the walls and is allowed to cool under a stream of dry nitrogen in a dry box. In the dry box 10.0 g. (0.05 mole) bis(4-aminophenyl) ether is added to the flask through a dried powder funnel, and residual traces are flushed in with 160 g. of dry dimethyl-acetamide. There is then added 10.90 g. (0.05 mole) pyromellitic dianhydride to the flask through a second dried powder funnel over a period of 2–3 min. with vigorous agitation. Residual dianhydride is washed in with 28 g. dry dimethylacetamide. The powder funnel is replaced by the stopper and the mixture is stirred for 1 hr. A small surge in temperature to 40°C. occurs as the dianhydride is first added, but the mixture rapidly returns to room temperature.

The above procedure yields a 10% solution which can be stirred without difficulty. In some cases the mixture becomes extremely viscous, and dilution to 5–7% solids may be required for efficient stirring. Polyamic acids so prepared exhibit inherent viscosities of 1.5–3.0 at 0.5% in dimethylacetamide at 30°C.

The polymer solutions may be stored in dry, sealed bottles at -15 °C. until needed.

Preparation of Polyamic Acid Films. Thin layers (10-25 mils) of polyamic acid solutions are doctored onto dry glass plates and dried for 20 min. in a forced draft oven (with nitrogen bleed) at 80°C. The resulting films are only partly dry and after cooling can be peeled from the plates, clamped to frames, and dried further *in vacuo* at room temperature.

Polyimide Conversion. Films of the polyamic acids which have been dried to a solids level of 65-75% are clamped to frames, heated in a forced draft oven to 300° C. for an additional hour. Further heating at 300° C. causes essentially no increase in the imide infrared absorptions at 5.63 and 13.85μ .

Property Measurement

Crease Test. A crease and bend test was used as a criterion of failure for films exposed in an oven with temperature control $\pm 3^{\circ}$ C. to 500°C. In the crease test, a narrow strip of the film was cut off and creased sharply between the fingers. In each case, several strips were cut from the sample and failure was recorded when more than half of the strips failed the test. The orders of stability as determined by this crease test correlated qualitatively with weight loss measurements.

Zero Strength Temperature. The du Pont Zero Strength Temperature Test was used to measure the temperature at which a polymer film (generally in the range of $20-75 \ \mu$ thick) failed under a tensile load of 1.4 kg./ cm.² (20 psi) 5 ± 0.4 sec. after contact with a preheated metal bar. This technique is relatively insensitive to film thickness within the range stated, and depending on sample uniformity, has the following precision: (1) about $\pm 5^{\circ}$ C. for Mylar polyester film (near 240°C.) (2) $\pm 15-20^{\circ}$ C. for poly-[N,N'(p,p'-oxydiphenylene)pyromellitimide] film (800–900°C.).

In practice, film strips 0.25 in. wide and 5 in. long are attached to a clamp at one end, and sufficient weight is attached to the other end to give a tensile load of 20 psi. The film strip is then contacted with a heated metal cylinder and a plot is made of the time required for failure (burning or melting through) versus the temperature of the cylinder. Measurements are made at several temperatures above and below that at which 5 sec. is required for failure, and a curve is drawn through the points. The zero strength temperature is then determined from the curve.

Van de Graaff Irradiation. The sample is moved under the electron beam 10 cm. below an aluminum window at a rate of 2.27 cm./sec. with a beam scanning width of 20 cm. For 2 M.e.v. electrons and a beam current of 250 μ amp., one pass gives a flux at the surface of 12.5 watt-sec./ cm.². For a material with a density of one and an electron range of 1 cm., the average dose per pass is 1.25 Mrads ($1.25 \times 10^8 \text{ ergs/g.}$).

Brookhaven Pile Exposure. Samples of film placed in the Brookhaven Pile were exposed to thermal neutrons, γ -rays, and other radiation. The flux in the pile is expressed in neutrons/cm.²/sec. (*nvt*).

Viscosity Measurements. Solution viscosities were measured on dilute solutions utilizing the indicated anhydrous solvents, concentrations, and temperatures. Dissolution (or dilution in the case of polyamic acid 10–15% solutions) was generally achieved by shaking at the temperature of measurement (30 or 15°C.). The work with fuming nitric acid requires cooling to minimize molecular weight degradation. The glass viscometers used were conventional Ostwald-Fenske types with capillaries sized to give flow times in the 40–120 sec. range, and bath temperatures were held to within $\pm 0.05^{\circ}$ C.

Thermogravimetric Analyses. Measurements of weight loss were conducted in a continuous-recording thermobalance, (Aminco Thermo-Grav), in controlled atmospheres. Temperature-programmed curves were obtained at slow rates (3°C./min.), while isothermal runs were made by preheating the chamber, then inserting the sample and holding to within $\pm 0.5^{\circ}$ C. The rate of gas flow was 100 cc./min.

X-Ray Measurements. Diffraction patterns were obtained on a General Electric XRD-5 diffractometer, utilizing nickel-filtered copper K α radiation (1.54 A.) at 50 kv. and 16 ma. and pinhole collimation. The flat-plate Laue photographs were obtained with a 2.5-cm. sample-to-film distance; a 1.25-mm (50 mils) specimen thickness and various appropriate exposure times were used.

Mechanical and Electrical Properties. These measurements were obtained by utilizing official ASTM methods (designation D-150-59 for the dielectric measurements and D-882-61T for the tensile properties). The electrical measurements utilizing an improved Schering Bridge and specimens were 25 μ (1-mil) films sprayed with silver paint electrodes to give precise areas in intimate contact. Tensile tests were conducted at strain rates in the range of 30-100%/min.

RESULTS AND DISCUSSION

Synthesis of Polyamic Acids

The preparation of polyamic acids is generally carried out by adding pyromellitic dianhydride to a solution or slurry of the diamine in a polar solvent such as dimethylacetamide or dimethylformamide. The polymerization may be conducted heterogeneously by addition of pyromellitic dianhydride as a solid or as a slurry in a relatively inert liquid such as acetone, γ -butyrolactone, or benzonitrile. The rate of reaction appears to be limited by rate of solution of pyromellitic dianhydride; normally 30-60

[React	tion of B	is(4-ami	nopheny	l) Ethe	r and Py	romellitic	Dianhyo	lride]
		amino- l) ether		nellitic lydride	Solids,	Temp.,	Time at temp.,	
Solvent	g.	Moles	g.	Moles	%	°C.	min.	$\eta_{\mathrm{inh}}{}^{\mathbf{a}}$
DMAc	10.00	0.05	10.90	0.05	10.0	25	120	4.05
DMAc	10.00	0.05	10.90	0.05	10.0	65	30	3.47
DMAc	20.00	0.10	21.80	0.10	10.6	85-88	30	2.44
DMAc	20.00	0.10	21.80	0.10	10.7	115-119	15	1.16
DMAc	20.00	0.10	21.80 ^b	0.10	10.3	125 - 128	15	1.00
DMAc	20.00	0.10	21.80°	0.10	15.7	135-137	15	0.59
N-Me capro- lactam	10.00	0.05	10.90	0.05	14.2	150-160	2	0.51
N-Me capro- lactam	10.00	0.05	10.90	0.05	12.9	175–182	1-2	Only partly soluble
N-Me capro- lactam	20.00	0.10	21.80	0.10	15	200	1	Insol.

TABLE I

Effect of Temperature of Polymerization on Inherent Viscosity of Polyamic Acid [Reaction of Bis(4-aminophenyl) Ether and Pyromellitic Dianhydride]

 $^{\circ}$ Determined at 0.5% concentration in the particular solvent at 30°C.

^b Increment of 0.35 g. pyromellitic dianhydride added before determination of η_{inh} . ^c Increment of 0.25 g. pyromellitic dianhydride and then 0.21 g. of bis(4-aminophenyl)ether added before determination of η_{inh} .

min. is adequate for laboratory-scale polymerization. Total solutes average 10-15%, although it has been possible to attain high molecular weight polyamic acids at concentration levels of 35-40%. At such high concentrations, the slurry method of addition enables the best mixing, and efficient cooling is required to compensate for the heats of reaction and stirring. When the solid pyromellitic dianhydride is added, a red-orange color is observed at the solid-liquid interface; this rapidly lightens to a lemon-

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yellow as the pyromellitic dianhydride dissolves and reacts with the diamine.

Best results are obtained from both types of procedure at temperatures of 15–75°C.; above 75°C. a decrease in the molecular weight of the polyamic acid becomes marked. Above 100°C. cyclization to imide is appreciable, causing eventual precipitation of polyimide as well as a lowered molecular weight of the polyamic acid (Table I). Above 150°C., the cyclization is so rapid that polyimide sometimes precipitates before all of the dianhydride can be added.

Conversion to Polyimide

Conversion of Polyamic Acid to Polyimide. Cyclization to polyimide may be carried out by heating a film of polyamic acid from 25 to 300°C. at a carefully controlled rate. As cyclization proceeds, the color of the polyamic acid darkens from a pale yellow to a deep yellow or orange.

Complete infrared spectra and ultraviolet spectra for poly[N,N'(p,p'-oxydiphenylene)pyromellitimide] are shown in Figures 1-4. (The instru-

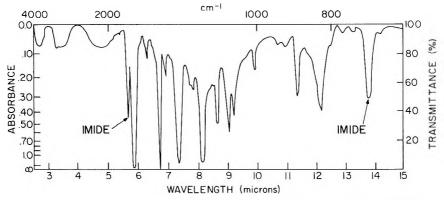


Fig. 1. Infrared spectrum of 0.1 mil poly[N,N'(p,p'-oxydiphenylene)pyromellitimide] (POP-PI) film. The film was heated to 300°C. over a period of 45 min., then held at 300°C. for 1 hr.

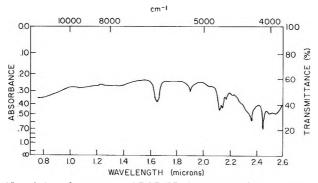
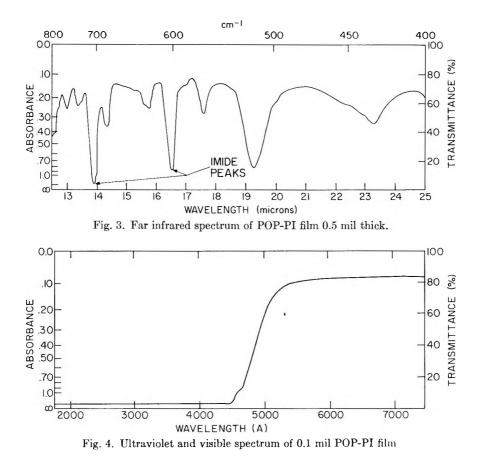


Fig. 2. Near infrared spectrum of POP-PI film 14 mils thick, scan 50 A./sec.



ments used were the Perkin-Elmer Model 21 with NaCl or KBr optics, and the Cary Model 14.) The cyclization can be followed spectrophotometrically⁹ (Fig. 1) by disappearance of the N-H band (3.08 μ) and ap-

	N, %	70
R	Calculated	Found
<u> </u>	9.7	$\begin{array}{c} 9.8\\ 9.5\end{array}$
	7.7	$\begin{array}{c} 7.9 \\ 7.7 \end{array}$
	7.4	$\begin{array}{c} 7.5 \\ 7.6 \end{array}$
	7.3	7.3
-<	6.5	$\begin{array}{c} 6.6 \\ 6.7 \end{array}$

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pearance of imide bands (5.63, 13.85 μ). Nitrogen analyses correspond to the converted ring structure (Table II).

Properties

Polyamic Acids. Polyamic acids are soluble in a variety of solvents, such as dimethylacetamide, dimethylformamide, dimethylsulfoxide, and

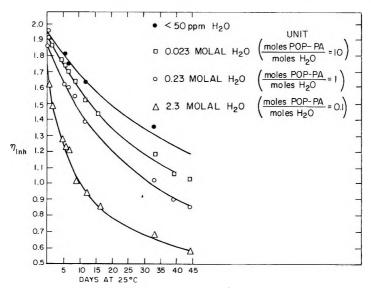


Fig. 5. Effect of added water on 0.23 molal POP-PA [polyamic acid from bis(4-amino-phenyl)ether and pyromellitic anhydride] solution in dimethylacetamide (DMAc).

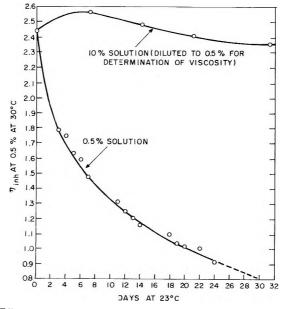


Fig. 6. Effect of concentration on stability of POP-PA in DMAc at 23°C.

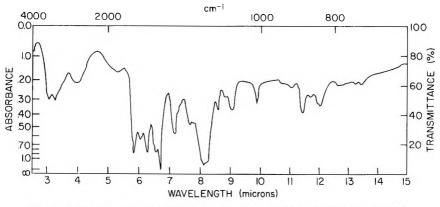


Fig. 7. Infrared spectrum of POP-PA film 0.1 mil thick, dried 2 hr. at 80°C.

tetramethyl urea. The amic acid polymer is sensitive to hydrolysis by water, similar to the monomeric phthalamic acids as previously noted by Bender¹⁰ (Fig. 5). The stability at 23° C. of the polyamic acids in solution is dependent upon the polymer concentration, dilute polymer solutions decreasing in viscosity much more rapidly than concentrated solutions (Fig. 6).

Films of polyamic acids containing 25-35% of residual solvent can be prepared by careful drying of cast solutions. These films on dissolving exhibit considerably lower inherent viscosities than the original polyamic acids (Table III). Polyamic acids have no true softening points, since dehydration occurs with heating to form polyimide; as noted above this can occur in solution at temperatures as low as 100 °C. The polymer, or

R	Solvent	η _{inh} solu- tion	Drying conditions	η _{inh} film
~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	Dimethylacetamide	$\begin{array}{c} 2.1\\ 2.1\end{array}$	30 min., 80°C. 30 min., 80°C. 5 days, 23°C.	1.3 1.3
<>- </td <td>Dimethylacetamide</td> <td>$\begin{array}{c} 1 &amp; 0 \\ 1 &amp; 2 \end{array}$</td> <td>10 min., 120°C. 30 min., 80°C.</td> <td>0.4 0.33</td>	Dimethylacetamide	$\begin{array}{c} 1 & 0 \\ 1 & 2 \end{array}$	10 min., 120°C. 30 min., 80°C.	0.4 0.33
	$\begin{array}{c} \textbf{Benzonitrile/di-}\\ \textbf{methylformamide}\\ (3/2) \end{array}$	1.0	15 hr., 25°C.	0.5
	Dimethylacetamide	1.3	6 hr., 70°C.	0.7
-CH2-CH2	Dimethylacetamide	2.3	20 min., 110°C.	0.5
-<->-s-<->-	Dimethylacetamide	1.2	30 min., 120°C.	0.5
-< <u>S0</u> 2-< <u>&gt;</u>	Dimethylacetamide	0.7	30 min., 120°C.	0.4

TABLE III

Decrease of Inherent Viscosity of Polypyromellitamic Acids During Film Casting and Drying (R = Diamine Component)

• POP-PA film is polyamic acid from bis(4-aminophenyl) ether and pyromellitic dianhydride.

film cast from solution, will not cyclize extensively until temperatures of 120–150 °C. are reached. A characteristic infrared spectrum of such a polyamic acid film from bis(4-aminophenyl) ether is shown in Figure 7.

**Polyimides.** A series of polypyromellitimides, some of which are summarized in Table IV, was prepared. Aromatic polypyromellitimides are extremely high melting, difficultly soluble polymers with outstanding resistance to heat, oxygen, and irradiation; their softening points, as determined by zero strength temperature of films, are normally well over 700°C. (in comparison, aluminum foil has a zero strength temperature of 550°C.). In contrast with polyamic acids, polyimides are colored compounds whose intensity of color depends upon the diamine component. The polyimide derived from bis(4-aminophenyl) sulfone is pale yellow; the polyimides from m-phenylenediamine, p-phenylenediamine, and bis(4-aminophenyl) ether are yellow to orange, while that based upon bis(4-aminophenyl)sulfide is deep red.

R	$\eta_{ ext{inh}}{}^{\mathbf{a}}$	Density
<i>m</i> -Phenylenediamine	>0.3	1.43
p-Phenylenediamine	0.5	1.41
p, p'-Biphenylenediamine	>0.3 ^b	1.43
Bis(4-aminophenyl)methylene	1.7	1.36
Bis(4-aminophenyl) isopropylidene	0.5	1.30
Bis(4-aminophenyl) thioether	>0.3 ^b	1.41
Bis(4-aminophenyl) ether	1.0ь	1.42
Bis(4-aminophenyl) sulfone	>0.3	1.43
Bis(3-aminophenyl) sulfone	0.5	

 TABLE IV

 Polypyromellitimide Films (R = Diamine Component)

* 0.5% in H₂SO₄.

^b Fuming HNO₃.

Thermal Stability. Thermal stability has been determined for polyimide films by weight loss measurements in air and helium atmospheres and by retention of film creasability upon heating in air. The data, summarized in Figures 8-10 and Table V, indicate that polyimides as a class possess outstanding thermal stability. When considered along with the retention of mechanical integrity as evidenced by zero strength temperatures in the metallic range, these stabilities become truly significant. Thus, the polypyromellitimide derived from bis(4-aminophenyl) ether showed isothermal weight loss in helium atmosphere of only 1.5% after  $\cdot 15$  hr. at 400°C., 3.0% after 15 hr. at 450°C., and 7% after 15 hr. at 500°C. In other weight loss measurements during constant rate of temperature increase  $(3 \, ^{\circ}C./min.)$  the polyimides derived from *m*-phenylenediamine, benzidine, and bis(4-aminophenyl) ether exhibited a 1-1.5% weight loss in the heating period to 500 °C. The thermogravimetric analyses are lent additional significance by the retention of film toughness after thermal aging summarized in Table V. Films derived from wholly aromatic poly-

			Zero strength tennoreture	Thermal :	Thermal stability in air ^a
R	Solubility	Crystallinity	competature, °C.	275°C.	300°C.
	Amorphous cone. H _a SO ₄ ; orystalline insol.	Crystallizable	006	>1 yr.	>1 mo.
$\Diamond$	Amorphous conc. H ₂ SO ₄ ; crystal- line insol.	<b>Crystallizes</b> readily	006	>1 yr.	
	Fuming HNO ⁵	Highly crystalline	>900	1	1 mo.
	Conc. H ₃ SO4	Slightly crystalline	800		7-10 days
CH ₃ CH ₃ CH ₃	Conc. H ₂ SO ₄	Orystallizable with difficulty	580		15-20 days
-C-s-C-	Fuming HNO ₃	Crystallizable	800	10-12 mos. (estimated)	6 weeks
	Fuming HNO:	Crystallizable	850	>1 yr.	>1 mo.
	Conc. H ₉ SO4	I	1	1	>1 mo.
Son-Son-	Conc. H ₂ SO ₄	Ţ	1	l	>ì mo.

Table V ovromellitimides (R =

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AROMATIC POLYPYROMELLITIMIDES

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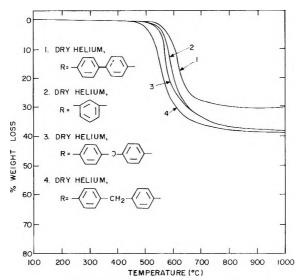
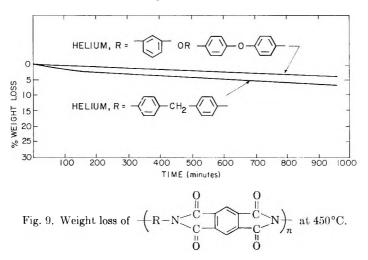


Fig. 8. Effect of diamine structure on weight loss of polypyromellitimides during constant rise in temperature (3°C./min.).



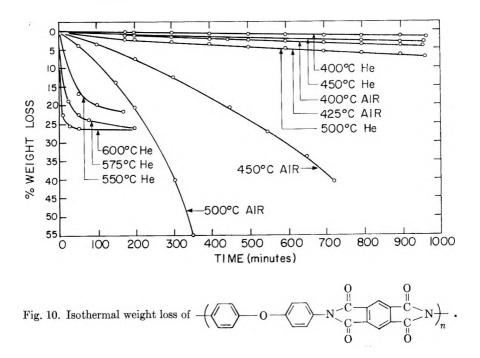
pyromellitimides retain toughness for months at elevated temperatures in air.

**Hydrolytic Stability.** The hydrolytic stability of the polypyromellitimides is, with certain exceptions, of a high order (Table VI) and may be considered quite unusual. The polypyromellitimides derived from bis(4-aminophenyl) ether and bis(4-aminophenyl) thioether, which already possess an outstanding level of thermal stability, retain toughness after one year and after three months respectively in boiling water. However, polyimides derived from diamines such as m-phenylenediamine and p-phenylenediamine exhibit poor hydrolytic stability, becoming embrittled after one week or less in boiling water.

R	Retention of film flexibility in boiling H ₂ O
	1 week
$\bigcirc$	1 week
0-0-	1 yr.
~	>3 mo.

TABLE VIHydrolytic Stability of Polypyromellitimides(R = Diamine Component)

**Radiation Resistance.** The data in Table VII indicate that films of the aromatic polypyromellitimides are outstandingly resistant to irradiation from high energy electrons and from thermal neutrons. Thus films of the polypyromellitimide from bis(4-aminophenyl)methane exhibit good mechanical and electrical properties after high energy electron exposure of over 10,000 Mrad in the Van de Graaff generator while films of polystyrene and poly(ethylene terephthalate) become embrittled after 500–600 Mrad. Films of the polyromellitimide from bis(4-aminophenyl) ether remain creasable after 40 days exposure to thermal neutrons at 175°C. in the Brookhaven pile.



	•			
Polymer film	Thickness, mils	Number passes	Dose, Mrad	Remarks
DDM-PIª	2.0	8000	10,000	Retains toughness, good electrical properties
Mylar ^b	2.0 - 3.0	200	240	Creasable
-	$\begin{array}{c} 2.0-3.0\ 3.0\end{array}$	500	600	brittle, yellow yellow, brittle
Polystyrene	1.2	500	600	Yellow, extremely brittle
Polyethylene	6-10	200	240	Very weak
(branched)	6-10			sticky gum

 TABLE VIIA

 Effect of Radiation on Polypyromellitimide Films

 (Exposure Van de Graaff 2 M.e.v. Electrons)

^a Polypyromellitimide from bis(4-aminophenyl)methane.

^b Du Pont's registered trademark for its polyester film.

(Thermal Neutron Degradation ^a )					
Polymer film	Thick- ness, mils	Exposure, days	Tempera- ture, °C.	Flux 10 ¹³ neutrons/ cm. ² /sec.	Remarks
POP-PI ^b	2-2.7	4()	50-75	0.4	Slightly darkened, brittle in spots
		40	175	0.5	Darkened, tough
		80	175	0.5	Darkened, brittle
Polystyrene	1.2	10	50 - 75	0.4	Yellow, very brittle
Polyethylene (branched)	3.0	10	50-75	0.4	Sticky, rubbery
	3.0	40	50 - 75	0.4	Brown varnish
Mylar ^o	3.0	10	50 - 75	0.4	Failed
	3.0	20	175	0.5	Yellow, brittle

TABLE VIIB Effect of Radiation on Polypyromellitimide Films (Thermal Neutron Degradation^a)

^a Courtesy of Brookhaven National Laboratory.

^b Polyimide from bis(4-aminophenyl)ether and pyromellitic dianhydride.

^c Du Pont registered trademark for its polyester film.

**Solution Properties.** The polyimides are insoluble in conventional solvents. Thus far, only fuming nitric acid has been found to be a general solvent for the species suitable for qualitative molecular weight evaluation at low temperature; concentrated sulfuric acid is effective for some polyimides. The stabilities of solutions of various polyimides in fuming HNO₃ and in concentrated  $H_2SO_4$  are summarized in Figures 11 and 12.

**Crystallinity.** Several of the polyimides are crystalline as made, for example, the polypyromellitimide from p-phenylenediamine (Fig. 13). Others are more or less ordered, depending on their structure. Thus, polypyromellitimides derived from m-phenylenediamine, bis(4-aminophenyl)methane, bis(4-aminophenyl)isopropylidene, bis(4-aminophenyl)

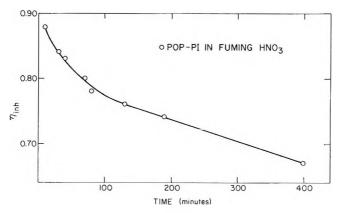


Fig. 11. Inherent viscosity vs. time for dilute solutions of polyimide; 15°C., 0.5 g. polymer/100 ml. solvent.

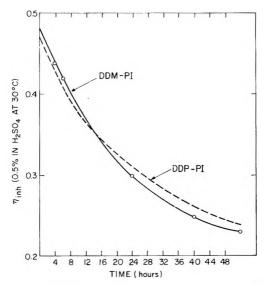


Fig. 12. Stability of polypyromellitimides in concentrated H₂SO₄; 30°C.

sulfide, and bis(4-aminophenyl) ether normally exhibit a low degree of order as prepared. High temperature treatment will cause crystallization of film derived from *m*-phenylenediamine and of films based upon bis(4-aminophenyl) ether (Fig. 14). Films, despite the slight weight loss upon heating noted previously, retain structural integrity for short exposures to 750-800 °C. in air; up to this temperature there appears, for the polymers studied, to be no evidence of crystal melting. These include the polypyromellitimide derived from bis(4-aminophenyl) ether, *m*-phenylenediamine, and *p*-phenylenediamine. No true second-order transition temperatures have been determined.

Mechanical and Electrical Properties. Polyimides, in addition to the outstanding permanence characteristics noted above, possess an excellent

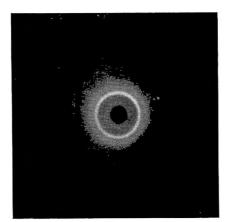
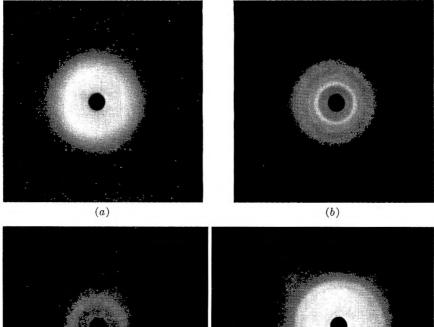
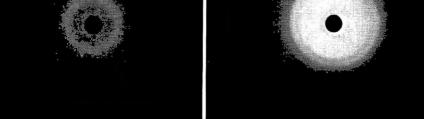


Fig. 13. Laue transmission x-ray diffraction pattern of unannealed poly(p-phenylene pyromellitimide) (filtered CuK $\alpha$  radiation).





(*c*)

(d)

Fig. 14. Laue transmission x-ray diffraction patterns of (a) polypyromellitimide from *m*-phenylenediamine, not annealed; (b) same, annealed 2 min. at 400°C.; (c) polypyromellitimide from bis(4-aminophenyl) ether, not annealed; (d) same, annealed at 400°C.

balance of mechanical and electrical properties. The films are stiff and strong and retain mechanical strength to high temperatures. The electrical properties of the various polyimides are all excellent and are summarized as a range characteristic for polyimides in Table VIII. A great deal of information has been obtained for H film, which is derived from bis(4-aminophenyl) ether. The data are summarized in Table IX.

The aromatic polypyromellitimides exhibit outstanding thermal stability

TABLE VIII

Electrical Properties of Polypyromellitimide Films (1-2 mil)					
	23°C.	150°C.	200°C.		
Dielectric constant (1000 cycles/sec.)	3.1-3.7	2.9-3.1	2.8-3.2		
Dissipation factor (1000 cycles/sec.)	0.0013-0.002	0.006-0.0014	0.0005-0.0010		
Volume resistivity (23°C., 50% R.H.), ohm-cm. Dielectric strength, v./mil	$10^{17}-5 imes10^{18}$ 4550–6900	>1015	10¹₄−10¹₅ 4600–5900		

TABLE IX Properties of H Film^a

Thermal stability in air ^b	
250°C.	10 yr. (extrapolated)
275°C.	1 yr.
300°C.	1 mo.
400°C.	1 day
Melting point, °C.	>900
Zero strength tempera-	815
ture, °C.	
Solvents	None
Density	1.42
Glass transition temp., °C.	>500
Tensile strength, psi	
4°K.	Flexible
25°C.	25,000
200°C.	17,000
300°C.	10,000
500°C.	4,000
Elongation, $\%$	
25°C.	70
200°C.	90
300°C.	120
500°C.	60
Tensile modulus	
25°C.	400,000
200°C.	260,000
300°C.	200,000
500°C.	40,000

^a Data of Tatum et al.¹¹

^b Retention of film flexibility.

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matched and supported by a unique property combination which has not been characteristic for other polymeric systems. In addition to thermal stability, the properties include outstanding radiation resistance, unusual resistance to solvent attack, film toughness and its retention under rigorous conditions of air aging, and a level of mechanical properties which make the films useful over a range from extremely low to extremely high temperatures.

Dr. Gordon D. Patterson, Jr. directed the analytical support for this work and contributed much valuable advice. Numerous helpful discussions were held with Professor George S. Hammond, California Institute of Technology.

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#### Résumé

Des diamines aromatiques réagissent avec le dianhydride pyromellitique dans des solvants tels que le diméthylacétamide pour former des solutions d'acides polyamiques de poids moléculaires élevés. Ces polymères solubles peuvent être transformés en polyimides aromatiques insolubles. Lés polyimides aromatiques présentent une force nulle à des températures situées au-dessus de 700°C et possèdent une stabilité thermique et une stabilité à l'oxydation excellentes. Les caractéristiques de stabilité des films et la relation entre la structure chimique et la stabilité thermique et hydrolytique et les propriétés du polymère telles que la cristallinité sont décrites.

#### Zusammenfassung

Aromatische Diamine reagieren mit Pyromellitdianhydrid in Lösungsmitteln wie Dimethylacetamid unter Bildung von Lösungen hochmolekularer Polyamidsäuren. Diese löslichen Polymeren können in unlösliche aromatische Polyimide umgewandelt werden. Die aromatischen Polyimide verlieren ihre Festigkeit erst oberhalb 700°C und besitzen ausgezeichnete thermische und oxydative Stabilität. Die Stabilitätscharakteristik von Filmen sowie die Beziehung der chemischen Struktur zur thermischen und hydrolytischen Stabilität und zu Polymereigenschaften wie Kristallinität wird beschrieben.

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# Viscosity Behavior of Branched and Linear Potassium Carboxymethyl Dextrans

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#### **Synposis**

Samples of branched and linear dextran of near identical intrinsic viscosities have been carboxymethylated to varying degrees and converted to the potassium salts. The reduced viscosity-concentration curves of the branched and linear carboxymethyl dextran polyelectrolytes of identical degree of substitution in aqueous potassium chloride solutions (0.001N and 0.0005N) were compared. Significant differences were observed to exist. At low degrees of substitution  $(0.06-0.20 \text{ carboxymethyl group per anhydro$ glucose unit) the branched macroion possessed larger reduced viscosities than did itslinear counterpart. At a higher degree of substitution (ca. 1.0 carboxymethyl groupper anhydroglucose unit) the reduced viscosity curves of the branched and linear macroions crossed. These differences were shown to be independent of shear rate, molecularweight and molecular weight distribution. It is concluded that branching is responsiblefor the differences in the reduced viscosity-concentration behavior of the branched andlinear potassium carboxymethyl dextran samples because of the higher charge densityin the branched macroion.

## Introduction

On the basis of theoretical calculations, Zimm and Stockmayer¹ concluded that the effect of branching on macromolecular extension should be to reduce the mean square radius. Thurmond and Zimm² compared the intrinsic viscosities of linear and branched polymer samples of identical molecular weight and showed that the predicted reduction in mean square radius is manifested in a lower intrinsic viscosity for the branched sample. This difference in intrinsic viscosities between branched and linear samples has been utilized in the development of a viscometric method of branch detection and estimation.²⁻⁶ Unfortunately the method is limited. Only in high molecular weight regions (>100,000) does a difference in intrinsic viscosity between linear and branched polymer samples exist.

It is incorrect to ascribe the disappearance of the difference between the intrinsic viscosities of the branched and linear polymer samples to the absence of branches in the low molecular weight region, since evidence exists to indicate otherwise. Senti and co-workers⁷ have shown that the amount of formic acid produced per anhydroglucose unit (AGU) in a branched dex-

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tran is independent of molecular weight from  $9.5 \times 10^6$  to  $1.8 \times 10^4$ , even though the intrinsic viscosity difference between branched and linear dextran samples apparently vanishes below a molecular weight of  $10^5$ . (The amount of formic acid produced can be related to the amount of branching in dextran samples.) This means, of course, that the branching frequency is identical throughout the entire molecular weight range, and some reason other than the absence of branches must be sought to explain the lack of a difference in intrinsic viscosity between linear and branched polymer samples at low molecular weights (<100,000).

On the basis of evidence presented by Trementozzi⁸ that long-chain branching increases with molecular weight for branched polyethylene samples (which had lower intrinsic viscosities than their linear homologs), it is not unreasonable to postulate that the same obtains with other branched polymeric systems and that the viscometric molecular weight method of branch detection and estimation can be applied only to polymer samples with long branches and that the method is insensitive to short branches.

In a study undertaken to develop a viscometric method which would not be insensitive to short branching, it was demonstrated⁹ that large viscosity differences between low molecular weight branched (short branches¹⁰) and linear dextran samples can be effected if the samples are first converted to sulfate macroions and then their reduced viscosity–concentration behavior determined in aqueous simple salt solutions (i.e., 0.001N KCl). To substantiate that the results obtained with the sulfate polyelectrolytes are not artifacts of the sulfate polyelectrolyte system and to extend the study to take into account the possible influence of such factors as molecular weight distributions, range of degree of substitution, and shear rate, we have studied the reduced viscosity–concentration behavior of linear and branched potassium carboxymethyl dextran polyelectrolytes.

#### Experimental

The branched and linear potassium carboxymethyl dextran polyelectrolytes studied were derived from the branched and linear dextran samples used in the preparation of branched and linear potassium dextran sulfate polyelectrolytes.⁹ The intrinsic viscosity of the branched dextran sample was  $0.15_7$  dl./g. and that of the linear sample  $0.16_4$  dl./g. The viscometry was also identical to that carried out in the previous study,⁹ i.e., same viscometer, solvent aqueous 0.001N or 0.0005N KCl,  $25^{\circ}$ C. Shear rate data were obtained with the aid of a variable shear viscometer.¹¹ The carboxymethyl dextran samples of low degree of substitution were prepared by reacting the dextran samples in aqueous sodium hydroxide with sodium monochloroacetate at 0°C. The sodium chloroacetate was prepared by the slow addition of monochloroacetic acid (3 times the stoichiometric amount required for complete substitution of the dextran) to 240 ml. of 20% (w/v) sodium hydroxide kept at 0°C. as the acid was added. Dextran (3 g.) dissolved in 90 ml. of the 20% sodium hydroxide was added to the 240 ml. of the sodium hydroxide-sodium chloroacetate solution.

Aliquots were withdrawn after 24-hr. periods and dialyzed against tap water until strong basicity in the dialyzing tap water was not detectable with litmus paper. Static dialysis against demineralized distilled water was continued for six changes (each change 4 liters). The solutions from the dialysis bags were then passed through potassium-charged cation-exchange resin (Dowex 50) and the potassium carboxymethyl dextran samples isolated by freeze drying. The highly substituted potassium carboxymethyl samples having  $\approx 1.0$  carboxymethyl group (CMG) per AGU were prepared at 18°C. via a two-stage carboxylation. Three linear dextran samples of molecular weight  $1.35 \times 10^5$ ,  $1.194 \times 10^5$ , and  $7.31 \times 10^4$  (determined with the aid of an ultracentrifuge by the Archibald method) were carboxymethylated to the same degree (0.80 CMG/AGU) at 18°C.

Sedimentation velocity coefficient distributions of the branched and linear dextran samples were obtained as described by Gupta, Robertson, and Goring¹² and also described in greater detail by Claesson and Moring-Claesson.¹³

## Results

The effect of shear rate D on the reduced viscosity,  $\eta_{sp}/c$ , of a branched potassium carboxymethyl dextran (PCMD) sample with 0.21 CMG per

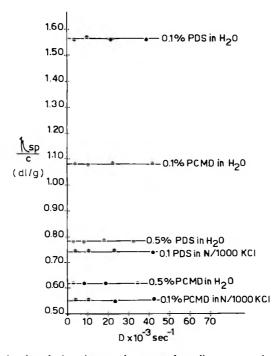


Fig. 1. Plots of reduced viscosity vs. shear rate for a linear potassium dextran sulfate (PDS) with 0.69 sulfate groups per anhydroglucose unit and a branched potassium carboxymethyl dextran (PCMD) with 0.21 carboxymethyl groups per anhydroglucose unit, both measured in a shear viscometer.¹¹

AGU at concentrations of 0.1% and 0.5% in water and 0.1% in aqueous 0.001N KCl as solvent is shown in Figure 1. Also in Figure 1 are the results of a shear study on linear dextran sulfate (0.69 sulfate groups/AGU) at the above concentrations and in the above solvents. It is evident

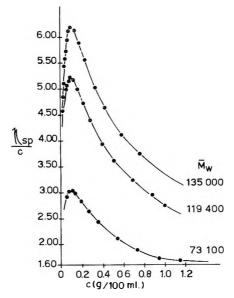


Fig. 2. Plots of reduced viscosity vs. concentration for linear potassium carboxymethyl dextrans of the same degree of substitution (0.80) but differing molecular weights. (The  $M_w$  is that of the parent dextran samples.)

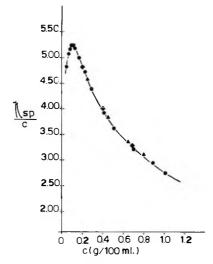


Fig. 3. Plots of reduced viscosity vs. concentration for linear potassium carboxymethyl dextrans of same degree of substitution but differing molecular weights normalized by the appropriate ratio of the reduced viscosities at the maxima: (**I**)  $M_{\rm w} =$ 135,000; (**O**)  $M_{\rm w} =$  119,400; (**A**)  $M_{\rm w} =$  73,100.

that the reduced viscosity is independent of shear rate, and, therefore, shear rate effects cannot be responsible for any differences in viscosity behavior for our polyelectrolyte systems.

In order to discover to what extent, if any, the differences in the reduced viscosity-concentration behavior of linear and branched polyelectrolyte samples might be due to differences in molecular weight or molecular weight

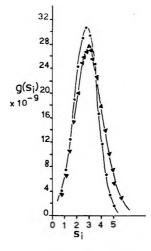


Fig. 4. The distribution function  $g(s_1)$  vs. the sedimentation velocity coefficient  $s_1$  for solutions of  $(\bullet)$  linear and  $(\blacktriangle)$  branched dextrans of concentration 0.42%.

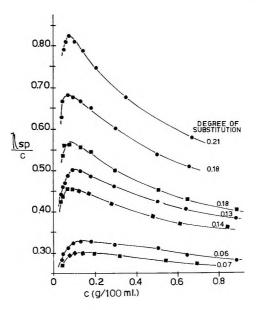


Fig. 5. Plots of reduced viscosity vs. concentration for potassium carboxymethyl dextrans of low degree of substitution in aqueous  $0.0005 \ N \ \text{KCl}$ : ( $\blacksquare$ ) linear polyelectrolytes; ( $\bullet$ ) branched polyelectrolytes.

distribution, reduced viscosity-concentration curves were obtained for three potassium carboxymethyl dextran samples substituted to essentially the same degree (0.82, 0.80, 0.82, CMG/AGU) but differing in molecular weight (parent dextran  $\overline{M}_w$  135,000; 119,400; 73,100). If there are no differences in the reduced viscosity-concentration curves for different molecular weight polyelectrolyte samples, then the molecular weight distribution of a polyelectrolyte sample (a spectrum of molecular weights) should not influence the reduced viscosity-concentration relationship. The reduced viscosity-concentration behavior of the different molecular weight

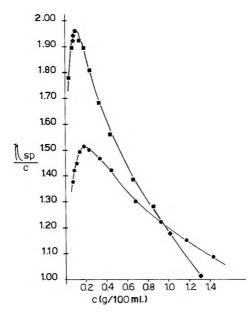


Fig. 6. Plots of reduced viscosity vs. concentration for highly substituted potassium carboxymethyl dextrans in aqueous 0.001 N KCl: ( $\bullet$ ) branched, 1.14 carboxymethyl groups per anhydroglucose unit; ( $\blacksquare$ ) linear, 1.22 carboxymethyl groups per anhydroglucose unit.

potassium carboxymethyl dextrans in 0.001N KCl are reproduced in Figure 2. On preliminary inspection, it appears that the curves all belong to the same family. In fact they do; any curve can be reduced to the other by an appropriate ratio of  $(\eta_{sp}/c) \frac{\max}{M_{w}(1)} / (\eta_{sp}/c) \frac{\max}{M_{w}(2)}$ . The coincidence of these curves is shown in Figure 3. This means that increasing the molecular weight only shifts the reduced viscosity-concentration curve to higher values of  $\eta_{sp}/c$ —a vertical shift with no horizontal shift.

It has been established indirectly⁹ and directly by proton magnetic resonance¹⁴ that very little or no degradation took place in the conversion of the linear and branched dextran samples to their respective potassium dextran sulfates. A comparison of the infrared spectra of branched dextran samples and their corresponding carboxymethyl derivatives indicated no branch degradation in the conversion. Therefore, the molecular weight distributions of the polyelectrolytes will be essentially the same as those of the parent dextran samples.

In Figure 4 are plotted the sedimentation velocity coefficient distributions for the linear and branched dextran samples used in preparing the polyelectrolytes (sulfate⁹ and carboxymethyl). It is evident from Figure 4 that there is very little difference between the distributions for the linear and branched parent dextrans and, therefore, no difference in molecular weight distribution that could be responsible for the differences in the viscosity behavior of the branched and linear potassium dextran sulfate⁹ and the branched and linear potassium carboxymethyl dextran samples.

The reduced viscosity-concentration curves for paired branched and linear potassium carboxymethyl dextran samples of low degrees of substitution (range 0.06 to 0.21 CMG per AGU) in 0.0005N KCl are shown in Figure 5. The reduced viscosity of the linear member of the pair is lower throughout the entire concentration range studied.

Differences in viscosity behavior were more marked when linear and branched potassium carboxymethyl dextran samples of much higher degree of substitution (linear sample 1.22 CMG/AGU and branched sample 1.14 CMG/AGU) were compared. Because of the higher degree of substitution, 0.001N KCL aqueous solutions were used as solvent. A crossover of the two curves is observed with these carboxymethyl dextran samples (Fig. 6).

## Discussion

Experimental results obtained in this reduced viscosity-concentration study with branched and linear potassium carboxymethyl dextran samples both confirm and supplement the findings of the viscosity study on the branched and linear dextran sulfate samples.⁹

With both polyelectrolyte systems it was observed that the reduced viscosity-concentration curves obtained for branched and linear polyelectrolyte samples (derived from parent dextran samples of near identical intrinsic viscosity) of the same degree of substitution (a degree of substitution near 1 ionogenic group per AGU) in the same solvent (i.e., aqueous KCl) were of the same general shape but nevertheless crossed one another. This crossover, it is evident, cannot be due to differences in molecular weight or molecular weight distribution, to differences in degree of substitution, or to differences in the ionic strength of the solvent. The crossover can only be due to the difference in branching of the samples.

An explanation of why branching causes a crossover of the reduced viscosity-concentration curves of branched and linear polyelectrolyte samples at high degrees of substitution (near 1 ionogenic group per AGU) and why at low degrees of substitution (in the range 0.06–0.21 ionogenic groups per AGU) this does not occur despite the fact that the branched polyelectrolyte has the higher reduced viscosity throughout the concentration range studied, is as follows. On the average, the contour length of the linear dextran macromolecule would be of the order of 240 AGU, since the weightaverage molecular weight of the sample was 40,000. The contour length of

the branched macromolecule of weight-average molecular weight 61,000 would be 148-178 AGU (assuming average branch lengths of 1.5-2 AGU). Consider now the consequences of (a) introducing charged sites—the same number per gram of macromolecule—onto the linear and branched macromolecules in solution, and (b) subsequent dilution of the solution. Because of branching, the local charge density will be greater in the branched than in the linear polyelectrolyte macromolecules and, therefore, the expansion of the branched macromolecules will be greater at the initial high concentration (ca. 1.0 g./dl.) of polyelectrolyte. Consequently  $\eta_{sp}/c$  for the branched polyelectrolyte solution will be greater than for the linear one at the same concentration. As the solutions are diluted, the branched and linear polyelectrolyte macromolecules expand further. Ultimately, the linear polyelectrolyte macromolecules should occupy the larger volume, partly because of their greater (average) contour length and partly because they would be less sterically hindered in achieving a "fuller extension." Thus at the high concentration,  $\eta_{sp}/c$  would be greater for the branched polyelectrolyte than for the linear one, but with sufficient dilution, the  $\eta_{sp}/c$  would become greater for the linear polyelectrolytes. In the lightly substituted branched and linear polyelectrolyte samples the charges are scattered much more thinly on the macromolecules. Nevertheless, in the coiled, branched polyelectrolyte macromolecules, the overall charge density is still greater than in the coiled linear polyelectrolyte macromolecules. Hence, relative expansion would again be greater for the branched polyelectrolyte macromolecules. With the low degree of substitution polyelectrolyte samples, however, the extent of possible expansion of the polyelectrolyte macromolecules is very small. At these small expansions, the restrictive factors to expansion such as steric hindrance and inherent inflexibility of the branch structure do not come strongly into play. Therefore, no crossover of the reduced viscosity-concentration curves is observed for polyelectrolyte samples of low degrees of substitution.

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#### Résumé

On a carboxyméthylé à différents taux des échantillons de dextrane ramifié et linéaire de viscosités intrinsèques presque identiques, et on les a transformés en sels de potassium. On a comparé les courbes de la viscosité réduite en fonction de la concentration pour les polyélectrolytes de carboxyméthyle-dextrane ramifié et linéaire possédant un degré de substitution identique, en solution aqueuse de chlorure de potassium  $(0.001 N \ge 0.0005$ N). On a observé des différences importantes. Pour un degré de substitution faible (0.06-0.20 groupe carboxyméthyle par unité d'anhydroglucose), le macroion ramifié possède une viscosité réduite plus grande que l'analogue linéaire. Pour un degré de substitution plus élevé (environ 1.0 groupe carboxyméthyle par unité d'anhydroglucose) les courbes de viscosité réduite des macro-ions ramifiés et linéaires se croisent. On a montré que ces différences sont indépendantes de la vitesse de cisaillement, du poids moléculaire et de la distribution du poids moléculaire. On en a conclu que la ramification est responsable des différences dans le comportement des échantillons de potassium carboxyméthyle-dextranes ramifié et linéaire, en ce qui concerne la viscosité réduite en fonction de la concentration, à cause de la densité de charge plus élevée dans le macro-ion ramifié.

## Zusammenfassung

Proben von verzweigtem linearem Dextran mit nahezu identischer Viskositätszahl wurden in verschiedenem Ausmass karboxymethyliert und zun Kaliumsalz umgewandelt. Die Kurven, reduzierte Viskosität gegen Konzentration, der verzweigten linearen Karboxymethyldextranpolyelektrolyte mit identischem Substitutionsgrad in wässriger Kaliumchloridlösung (0,001N und 0,0005N) wurden verglichen. Es bestanden signifikante Unterschiede. Bei niedrigem Substitutionsgrad (0,06-0,20 Karboxymethylgruppen pro Anhydroglukoseeinheit) besassen die verzweigten Makroionen eine höhere reduzierte Viskosiät als die linearen. Bei höherem Substitutionsgrad (zirka 1,0 Karboxylmethylgruppen pro Anhydroglukoseeinheit) kreuzten sich die reduzierten Viskositätskurven der verzweigten und linearen Makroionen. Dieser Unterschied erwies sich als unabhängig von der Schubgeschwindigkeit, dem Molekulargewicht und der Molekulargewichts verteilung. Man kommt zu dem Schluss, dass die Verzweigung wegen der höheren Ladungsdichte in den verzweigten Makroionen für die Unterschiede in der Abhängigkeit der reduzierten Viskosität von der Konzentration bei verzweigten und linearen Kaliumkarboxymethyldextranproben verantwortlich ist.

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# Analysis of Oligomerization Kinetics of Styrene on the Electronic Digital Computer

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### **Synopsis**

The mechanism of radical oligomerization by chain transfer reaction was studied in connection with the distribution of molecular weight of the obtained oligostyrene. In this case, the styrene–CCl₄ system was selected as model for this purpose. The kinetics of the chain transfer reaction is difficult to analyze because the concentrations of components in the system varies along with oligomerization. The rates of component reactions expressed by the simultaneous differential equations were solved by utilizing an electronic digital computer (IBM 650). Consequently, the analytical values and the experimental data showed good agreement, and the correlation among the coefficients of kinetic velocity in the system was clarified, yielding much information regarding the control of oligomerization.

## **INTRODUCTION**

The molecular weight distribution of a polymer is determined by the mechanism of polymerization, namely the type of polymerization and the velocity of each component reaction. Then, if the type of polymerization and an accurate molecular weight distribution are given, the velocity coefficient for each component reaction can be treated quantitatively. In addition, the accuracy of the distribution can be examined from the velocity coefficients thus obtained.

The types of radical polymerization have been studied thoroughly, and the relations between velocity coefficients for component reactions and the molecular weight distribution have also been formularized theoretically.¹ By means of this relation, the polymerization kinetics could be analyzed, although it has not been studied enough since many difficulties are involved in obtaining an accurate molecular weight distribution.

In view of this fact, the authors have studied lower polymerization by chain transfer reactions.² The products of this reaction have a molecular weight distribution just as high polymers do. Oligostyrene, as a typical case, has been fractionated effectively by means of elution column chromatography and the results of fractionation discussed.³ The mechanism of oligomerization by chain transfer reaction was formularized, and it was found that the molecular weight distribution is determined by the ratio of the molar concentration of the monomer to the chain transfer agent.

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Many assumptions must be introduced in order to solve all the component reactions because both the concentrations of the monomer and the chain transfer agent, and hence also their ratio, vary with the process of polymerization. An electronic digital computer was employed to solve the simultaneous differential equations for the velocity of all component reactions, in order to follow the changes of the reaction system accurately. The oligomerization of styrene was discussed by comparing the solution of these equations with the molecular weight distribution observed and the velocity of oligomerization.

# COMPONENT REACTIONS OF POLYMERIZATION AND THEIR RATE EQUATIONS

Oligomerization (telomerization) of styrene in carbon tetrachloride by chain transfer mechanisms can be divided into the component reactions of eqs. (1)-(5) which can be formulated in five steps.

Decomposition of initiator:

$$R-R \xrightarrow{k_d} 2R^* \tag{1}$$

Initiation:

$$\mathbf{R}^* + \mathbf{S} \xrightarrow{\kappa_0} \mathbf{S}^* \tag{2}$$

Chain growth:

Chain transfer:

Termination:

$$\mathbf{S}^* + ^*\mathbf{S} \xrightarrow{k'_{\circ}} \mathbf{S} \longrightarrow \mathbf{S}$$
(5)

where R-R denotes initiator, S is transfer agent (solvent), M is monomer,  $P_n$  is polymer molecule containing *n* units, R* is the primary radical from initiator, S* is the radical produced in transfer reaction with S, M* is a radical formed in transfer reaction with monomer molecule,  $M_n^*$  is a polymer radical containing *n* repeating units; the rate constants are:  $k_d$  the velocity coefficient for first-order decomposition of initiator,  $k_0$  the velocity coefficient for chain transfer to solvent S,  $k_n$  the velocity coefficient for reaction of  $M_{n-1}$  with monomer (velocity coefficient for propagation for each step),  $k'_n$  the velocity coefficient for chain transfer reaction of  $M_n^*$  to solvent S, and  $k'_0$  the velocity coefficient for termination by combination of two S* radicals.

In addition to the equations above many other processes are also conceivable in this system, but these additional reactions are considered to be of negligible importance, if any. The discussion of other reactions being omitted, the process explained by the preceding component reactions is limited to the so-called telomerization.

In the component reactions of polymerization [eqs. (1)-(5)], if the concentration of each component is denoted as follows, the concentration of each component in the system shown as a function of time and the rate of change of concentration may be expressed as shown in eqs. (6)-(14):  $C_{(RR)} = \text{concentration of RR}, C_R = \text{concentration of R}^*, C_S = \text{concentration of S}^*, C_M = \text{concentration of M}, C_n^* = \text{concentration of S}^*, C_M = \text{concentration of M}, C_n^* = \text{concentration of P}_n, C^* = \text{concentration of whole growing radicals}, C_{(RR)0} = \text{initial value of } C_{(RR)}, C_{M_0} = \text{initial value of } C_M, C_{S_0} = \text{initial value of } C_S, C = \text{concentration of whole polymer molecule}.$  These concentrations are in units of moles/liter or number of molecules.

$$dC_{(\mathbf{RR})}/dt = -k_d C_{(\mathbf{RR})_0} \tag{6}$$

$$dC_{\rm R}/dt = 2k_d C_{\rm (RR)} - k_0 f C_{\rm R} C_{\rm S}$$
⁽⁷⁾

$$dC_0/dt = k_0 f C_{\rm R} C_{\rm S} - k C_0 C_{\rm M} - k'_0 C_0^2 + C_{\rm S} (k' C^* - \alpha)$$
(8)

$$dC_{\rm M}/dt = -kC_{\rm M}(C_0 + C^* - C_n^*) \tag{9}$$

$$dC_{\rm S}/dt = C_{\rm S}(k_0 f C_{\rm R} + k' C^* - \alpha) \tag{10}$$

$$dC^{*}/dt = kC_{0}C_{M} - kC_{n}^{*}C_{M} - C_{S}(k'C^{*} - \alpha)$$
(11)

$$dC/dt = C_{\rm s}(k'C^* - \alpha) \tag{12}$$

$$dC_{1}^{*}/dt = k_{1}C_{0}C_{M} - k_{2}C_{1}^{*}C_{M} - k'_{1}C_{1}^{*}C_{S}$$

$$dC_{2}^{*}/dt = k_{2}C_{1}^{*}C_{M} - k_{3}C_{2}^{*}C_{M} - k'_{2}C_{2}^{*}C_{S}$$

$$dC_{3}^{*}/dt = k_{3}C_{2}^{*}C_{M} - k_{4}C_{3}^{*}C_{M} - k'_{3}C_{3}^{*}C_{S}$$

$$(13)$$

$$dC_{2}^{*}/dt = k_{2}C_{2}^{*}C_{M} - k_{2}L_{2}^{*}C_{M} - k'_{3}C_{3}^{*}C_{S}$$

$$\frac{dC_{1}/dt = k'_{1}C_{1}^{*}C_{8}}{dC_{2}/dt = k'_{2}C_{2}^{*}C_{8}} dC_{3}/dt = k'_{3}C_{3}^{*}C_{8}$$

$$(14)$$

$$dC_{n}/dt = k'_{n}C_{n}^{*}C_{8}$$

Here

$$\sum_{i=1}^{n} C_{i}^{*} = C^{*}$$

$$\sum_{i=1}^{n} C_{i} = C$$

$$k_{1} = k_{2} = k_{3} = \dots = k_{n} \equiv k$$

$$k'_{5} = k'_{6} = k'_{7} = \dots = k'_{n} \equiv k'$$

$$C^{*}(k' - k'_{1}) + C_{2}^{*}(k' - k'_{2}) + C_{3}^{*}(k' - k'_{3}) + C_{4}^{*}(k' - k'_{4}) = \alpha$$

The initiation efficiency of polymerization can be represented by the sum

$$f = f_1 + f_2 + f_3$$

where  $f_1$  is the efficiency of the radical formation by reaction (1), recombination of the radical being taken into consideration,  $f_2$  the efficiency of effective chain transfer to S in eq. (2), and  $f_3$  the efficiency that radical S* attacks monomer M in the first step of eq. (3), then the rate of formation of radical S* is obtained by multiplying  $k_0C_RC_S$  by f in eq. (8).

The velocity coefficients  $k_1-k_n$  of the propagation process, which actually are dependent on the chain length and have different values in the case where the degree of polymerization is low, are approximated by the chain length-independent coefficient k' in order to simplify the treatment. Instead the rate constants for chain transfer  $k'_1-k'_4$  are differentiated based on the relation of k'/k, considering the variation of k' with chain length, although the rate constants beyond  $k'_5$  are approximated by constants.

 $\alpha$  is a correction term for the deviation of  $k'_1 - k'_4$  from the mean value k'. The telomerization reaction can then be expressed in (2n + 7) simultaneous differential equations from eqs. (6)-(14) and analyzed by solving these simultaneous differential equations.

## CONCENTRATION OF THE COMPONENTS IN THE SYSTEM AND THE CALCULATION PROCEDURE

The Runge-Kutta method is used to obtain numerical solutions of the simultaneous eqs. (6)-(14). However it was shown to be impossible to solve these equations by the direct numerical calculation procedure with a computer because of too large errors and because the computer comes

to an overflow stop unless the time intervals on the calculation of the equations involving  $C_{\rm R}$ ,  $C_0$ ,  $C_i^*$ , and  $C^*$  are taken less than  $10^{-9}$  hr. This difficulty arises from the fact that the reaction rates are too large to be successfully analyzed even with the high speed of the computer.

Actually the calculation performed by setting very short time intervals, i.e.,  $10^{-9}$  hr., for the variations in the concentration  $C_{\rm R}$ ,  $C_0$ ,  $C_i^*$ , and  $C^*$ demonstrated that from any starting value the equation for the radicals converges to a fixed value, within the time range of  $10^{-6}-10^{-5}$  hr., which did not cause any observable change on  $C_{\rm (RR)}$ ,  $C_{\rm N}$ ,  $C_{\rm S}$ ,  $C_i^*$ , ..., etc. A short while after the beginning of the reaction, the radical concentrations of  $C_{\rm R}$ ,  $C_0$ , and  $C_i^*$  can be regarded as the stationary state is reached.

Then the preceding differential equations can be treated as follows. The left-hand sides of eqs. (7), (8), and (11) can be set to zero, yielding

$$C_{\rm R} = 2k_d C_{\rm (RR)0} e^{-k_d t} / k_0 f C_{\rm S} \tag{9'}$$

$$C_0 = (2k_d C_{(\rm RR)} e^{-k_d t} / k'_0)^{1/2}$$
(10')

$$C^* = (kC_0C_M + \alpha C_S)/k'C_S \tag{13'}$$

By using the generating function, the radical concentration  $C_n^*$  can be expressed as

$$G(\lambda) \equiv \sum_{n=1}^{N} C_n^* \lambda^n$$

in eq. (13). Thus

$$G(\lambda)/dt = k_1 C_0 C_M \lambda - k_2 C_1^* C_M \lambda - k'_1 C_1^* C_8 \lambda$$
  
+  $k_2 C_1 C_M \lambda^2 - k_3 C_2^* C_M \lambda^2 - k'_2 C_2^* C_8 \lambda^2$   
+  $k_3 C_2 C_M \lambda^3 - k_4 C_3^* C_M \lambda^3 - k'_3 C_3^* C_8 \lambda^3$ 

$$+ k_n C_{n-1} C_{\mathrm{M}} \lambda^n - k_{n+1} C_n^* C_{\mathrm{M}} \lambda^n - k'_n C_n^* C_{\mathrm{S}} \lambda^n = 0$$

If  $C_n^* \simeq C^*_{n-1}$ ,

$$G(\lambda) = kC_{\rm M}C_0\lambda/[(kC_{\rm M} + k'C_{\rm S}) - kC_{\rm M}\lambda]$$
  
=  $[1 - kC_{\rm M}\lambda/(kC_{\rm M} + k'C_{\rm S})]^{-1}kC_{\rm M}C_0\lambda/(kC_{\rm M} + k'C_{\rm S})$ 

If we define

$$kC_{
m M}/(kC_{
m M}\,+\,k'C_{
m S})\equiv\delta$$

the bracketed term in the preceding equation can be developed as follows:

$$(1 - \delta\lambda)^{-1} = 1 + \delta\lambda + (\delta\lambda)^2 + \dots$$

then,

$$G(\lambda) = C_1^* \lambda + C_2^* \lambda^2 + C_3^* \lambda^3 + \dots$$

If the coefficients of each  $\lambda$  term are determined,  $C_n^*$  can be obtained. As  $k'_1 \sim k'_4$  have been considered to be different, eqs. (13) and (14) will become as follows:

Here,  $\delta_n$  is expressed as follows:

 $\delta_{1} = kC_{M}/(kC_{M} + k'_{1}C_{S})$   $\delta_{2} = kC_{M}/(kC_{M} + k'_{2}C_{S})$   $\delta_{3} = kC_{M}/(kC_{M} + k'_{3}C_{S})$  $\delta_{4} = kC_{M}/(kC_{M} + k'_{4}C_{S})$ 

$$\delta_n = k C_{\rm M} / (k C_{\rm M} + k'_n C_{\rm S})$$

Equations (6)–(14) were reduced to the calculation of the stationary state in eqs. (7'), (8'), (11'), and (13') and to the numerical calculation of the simultaneous differential equations (6), (9), (10), (12), and (14). The calculation can be carried out easily by using a medium-scale electronic digital computer, as time intervals of 0.1-0.2 hr. suffice.

The calculated results for eqs. (6)-(14) for very small intervals  $(10^{-9}-10^{-7} \text{ hr.})$  from any initial values which converge to the eqs. (7'), (8'), (11'), (13'), and (14') within the short range of  $10^{-6}-10^{-5}$  hr. are shown in Figures 1, 2, and 3. It is clearly seen from these figures that when the initial concentrations  $C_{\rm R}$ ,  $C_0$ ,  $C_i^*$ , and  $C^*$  are taken to be zero or several times, even hundreds of times of the concentration of stationary state, they always converge to the same values, though the convergence processes are not monotonous, depending on their natures of equations of reaction velocity. This fact shows that the radical concentrations always

converge to the same value independent of the initial concentration  $C_{RR}$ ,  $C_M$ ,  $C_S$ , and  $C_i^*$ .

The time intervals taken in this calculation are 0.1–0.2 hr., and as the same results are obtained by using much smaller intervals, it is considered

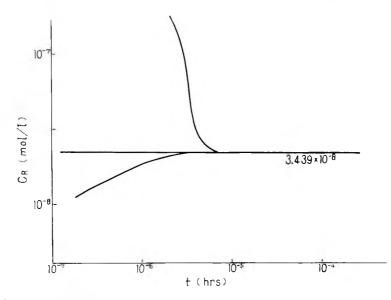


Fig. 1. Demonstration of a stationary state in the concentration of radicals in the system. Relation between the concentration of initiator radicals  $C_{\rm R}$  and the time of polymerization t. The calculations are shown for  $10^{-9}$  hr. time intervals.

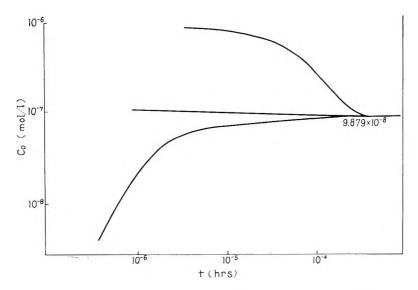


Fig. 2 Demonstration of a stationary state in the concentration of radicals in the system. Relation between the concentration of solvent radicals  $C_0$  and the time of polymerization t. The calculations are shown for  $10^{-7}$  hr. time intervals.

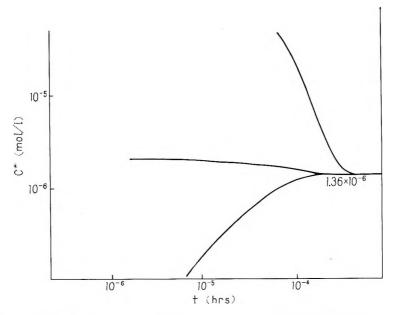


Fig. 3. Demonstration of a stationary state in the concentration of radicals in the system. Relation between the concentration of growing radicals  $C^*$  and the time of polymerization t. The calculations are shown for  $10^{-7}$  hr. time intervals.

that the assumption of the stationary state and the intervals taken are proper.

To apply the Runge-Kutta method, Gill's procedure was used; this had been developed for an electronic digital computer and proved to have following advantages: (1) fewer numbers of storage and instructions are required; (2) the results are sufficiently accurate; (3) a smaller execution time is involved.

In regard to differential equations, i = 1, 2, ..., n, the calculation procedure is as follows. Where j = 1, 2, 3, 4 in steps of the Runge-Kutta method,

$$dy_{ij}/dt = k_{ij} = f(y_{1,j-1}, y_{2,j-1}, \dots, y_{n,j-1})$$
(15)

$$y_{ij} = y_{i,j-1} + k[a_j(k_{ij} - b_j q_{i,j-1})]$$
(16)

$$q_{ij} = q_{i,j-1} + 3[a_j(k_{ij} - b_j q_{i,j-1})] - C_j K_{ij}$$
(17)

where the initial value  $q_{i0} = 0$ , and

$a_1 = 1/2$	$b_1 = 2$	$C_1 = 1/2$
$a_2 = 1 - \sqrt{1/2}$	$b_2 = 1$	$C_2 = 1 - \sqrt{1/2}$
$a_3 = 1 + \sqrt{1/2}$	$b_3 = 1$	$C_3 = 1 + \sqrt{1/2}$
$a_4 = 1/6$	$b_4 = 2$	$C_4 = k/2$

Equations (15)-(17) may be calculated by looping them, and the flow chart on the computer is shown in Figure 4. It has been shown that



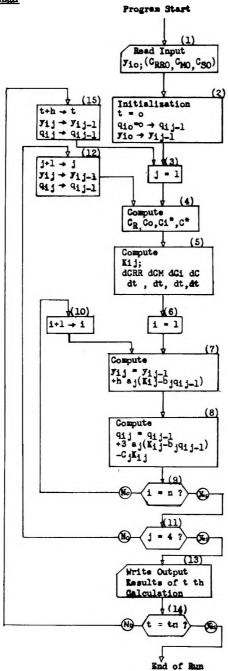


Fig. 4. Flow chart for the computer.

Runge-Kutta method is advantageous for the calculations by a computer of the kinetics models such as represented by the differential eqs. (6)-(14)and yields sufficiently accurate numerical solutions from a single starting value. The IBM 650 computer was employed, and 1.7 min. was required to calculate one interval of the Runge-Kutta method by floating point arithmetic. The calculation of the distribution of molecular weight, which is expressed by 33 variables of simultaneous differential equations, consumed about 10 min. for each interval. If a large-scale electronic computer had been employed, it would have required only a few seconds or less for the calculation.

## SELECTIONS OF THE VELOCITY COEFFICIENTS FOR THE COMPONENT REACTIONS AND THE SIMULATIONS

Oligomerization in this system can be analyzed by solving the eqs. (6)-(14). The velocity coefficients for the component reaction in polymerization in many cases have been measured by various methods, but

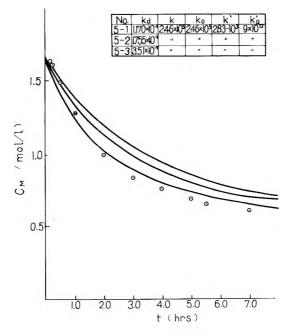


Fig. 5. Results of the simulations. Effects of the values of  $k_d$  on the relation between the concentration of monomer  $C_{\mathbf{M}}$  and the time of polymerization t: ( $\odot$ ) experimental values.

do not always agree with each other. As our main object was to compare the experimental data with the results of calculations based on the assumption of a given reaction scheme, the calculations were carried out by selecting suitable values for the rate constants from the available information.¹

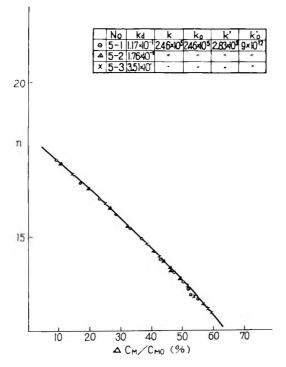


Fig. 6. Results of the simulations. Effects of the value of  $k_d$  on the relation between the conversion of monomer  $\Delta C_{M}/C_{M0}$  and the number-average degree of polymerization n.

The velocity coefficient for the decomposition of initiator,  $\alpha, \alpha'$ -azobisisobutylonitrile in this experiment, is expressed generally by the following equation:⁵

$$k_d = 10 \exp\{-\frac{30.7}{RT}\}$$
(18)

By inserting the reaction temperature,  $80^{\circ}$ C., into the equation above,  $k_a$  is found to be 0.351 (mole/l.-hr.), which was used in this calculation. The efficiency of the initiation reaction f, which is discussed in the paragraph dealing with the rate equations for the component reactions, was assumed to be 0.7 for the general case.

As data about the velocity coefficient for reactions (2) and (3) are scarce, it may be permissible to set  $k_0$  equal to k, considering the nature of the reaction. The characteristics of oligomerization (telomerization) are dependent on the fact that chain transfer to produce an oligomer occurs before the chain grows too long. In this case, as the chain length of the oligomer is so small compared with that of polymers, it would be desirable to consider that the velocity coefficients of propagation for monomer and *n*-mer take different values. Also, the same would be true for the process of termination. It is, however, a very complicated problem to treat both constants at the same time, and there has been no example of the treatment

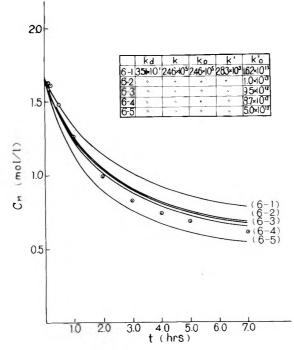


Fig. 7. Results of the simulations. Effects of the value of  $k'_0$  on the relation between the concentration of monomer  $C_M$  and the time of polymerization t for the case of k'/k = 0.0115: ( $\odot$ ) experimental values.

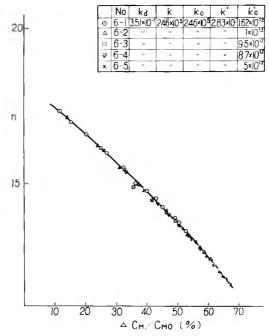


Fig. 8. Results of the simulations. Effects of the value of  $k'_0$  on the relation between the conversion of monomer  $\Delta C_{\rm M}/C_{\rm M0}$  and the number-average degree of polymerization *n*.

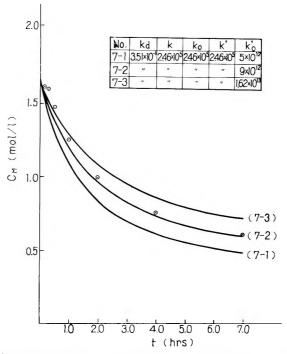


Fig. 9. Results of the simulations. Effects of the value of  $k'_0$  on the relation between the concentration of monomer  $C_M$  and the time of polymerization t for the case of k'/k = 0.01: ( $\odot$ ) experimental values.

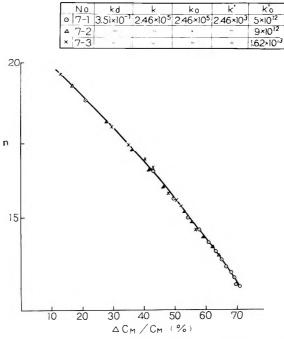


Fig. 10. Results of the simulations. Effects of the value of  $k'_0$  on the relation between the conversion of monomer  $\Delta C_M/C_{M0}$  and the number-average degree of polymerization *n* for the case of k'/k = 0.01.

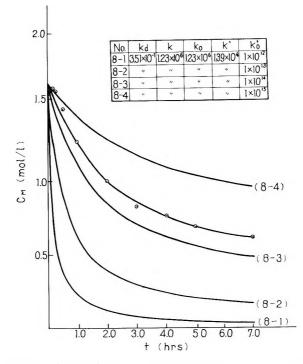


Fig. 11. Results of the simulations. Effects of the values of  $k'_0$ , k, and k' on the relation between the concentration of monomer  $C_{\mathbf{M}}$  and the time of polymerization t: ( $\odot$ ) experimental values.

of the variation of velocity coefficients with chain length of growing radicals; hence the constants for the propagation velocity were assumed to be independent of the chain length and the deviations corrected by including the variations into the rate constants for the chain transfer.

The value k was estimated to be  $2.46 \times 10^5$  by converting the value which was derived by Matheson and co-workers⁶ for polymerization of styrene to the value at 80°C., the effect of dilution also being considered.

As noted previously the velocity coefficients k are treated as single constant values regardless of the chain length, correction for the deviation caused by this assumption being included in k'.

Mayo⁷ obtained the value of k'/k experimentally for oligomers up to tetramer and assumed that k'/k to be constant in the range above pentamer. From this relation,  $k'_n$  is calculated by using the value of k previously determined.

In considering each component reaction determined in the precedingly section, the velocity coefficient for the chain termination  $k'_0$  was found to play an important role in the rate-determining steps of polymerization. If  $k'_0$  is small,  $C_0$  becomes larger, and the velocity of polymerization is promoted. It is one of the objectives of this study to estimate  $k'_0$ , which has not previously been known.

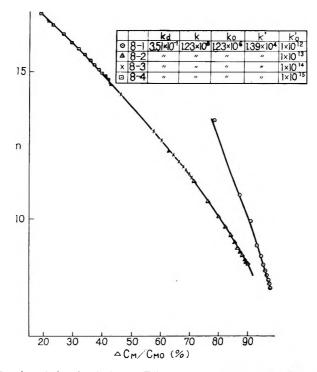


Fig. 12. Results of the simulations. Effects of the values of  $k'_0$ , k', and k on the relation between the conversion of monomer  $\Delta C_M/C_{M0}$  and the number-average degree of polymerization n.

In the computer analysis of the kinetics of component equations based on available information of the kinetics, the effects of the variation of the following coefficients on the rate of decrease of monomer concentration, the rate of polymerization, and mean degree of polymerization were investigated: (1) the velocity coefficient for decomposition of initiator  $k_d$ , (2) the velocity coefficient for propagation k, (3) the chain transfer constants k'/k, (4) the velocity coefficient for the termination reaction  $k'_0$ , and (5) determination of  $k'_0$ , corresponding to a proper value of coefficient.

The results of the simulation are shown in Figures 5-14, and the information obtained can be summarized as follows. (1)  $k_d$  determines the shape of the curve. (2) If  $k'_0$  is large, S* is consumed at the termination step rather than at the initiation step; thus the effective initiation decreases and the limiting conversion is reached leaving a large quantity of monomer intact. The estimated  $k'_0$  is about  $1.1 \times 10^{13}$ . (3) If the consideration is limited to the rate of monomer depletion, the change of k value does not necessarily determine the shape of the curve, and the experimental results may be explained properly by choosing an adequate value for  $k'_0$  in combination with k. (4) Even in the theoretical curve which best fits the experimental results, the rate of decrement of  $C_M$  is

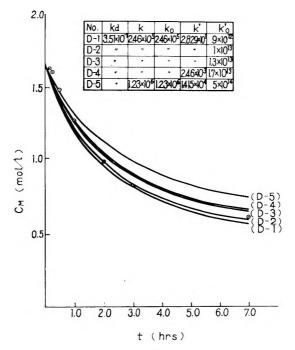


Fig. 13. Results of the simulations. Relation between the concentration of monomer  $C_{\rm M}$  and the time of polymerization t. Detailed calculations done by use of selected constants: ( $\odot$ ) experimental values.

greater than the experimental value. This discrepancy may arise from a time lag in the experiment until a given temperature is attained and/or the loss incurred in the operation because of its low yields. (5) Apart from minor discrepancies, the general features of the experimental curve

Exp. no.	Polymeri- zation time, hr.	Yield weight, g.	Chlorine content, %	Weight of styrene poly- merized, g.	Conversion in monomer X	Styrene concen- tration См, mole./1
	0.0			0.0	0.0	1.6733
1	0.167	0.5	3.68	0.480	$0.025_{0}$	1.632,
<b>2</b>	0.25	0.95	5.68	0.898	$0.047_{0}$	$1.597_{1}$
3	0.50	<b>2</b> . $2$	4.25	2.190	$0.114_{1}$	$1.488_{3}$
4	1.00	4.7	5.86	4.670	$0.243_3$	1.276,
5	2.0	7.7	5.90	7.651	$0.398_{5}$	$1.020_{4}$
6	3.0	9.7	7.22	9.625	0.5013	$0.849_{1}$
7	4.0	11.5	7.44	10.571	0.5515	$0.765_{0}$
8	5.0	12.3	8.92	11.201	$0.583_{s}$	$0.711_{3}$
9	7.0	13.7	10.66	12.133	$0.632_0$	$0.629_{5}$
10	10.0	14.2	10.70	12.522	$0.653_{9}$	0.6063

are fairly well explained by the theoretical value by choosing a suitable condition.

The experimental values for the reaction of this system are shown in Table I. Figures 15 and 16 show the results obtained by using the most probable values estimated from the simulation. The values of the chain transfer constants k'/k, 0.0115 and 0.010, derived for the case of high polymers will be examined in the following section.

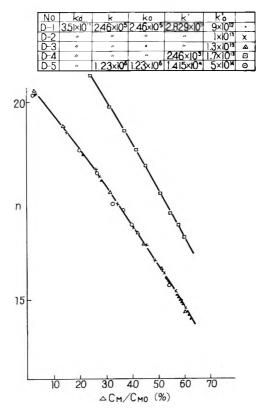


Fig. 14. Results of the simulations. Relation between the conversion of monomer  $\Delta C_{\rm M}/C_{\rm M0}$  and the number-average degree of polymerization. Detailed calculations done by use of selected constants.

As seen in Figures 15 and 16, the value 0.010 for k'/k gives 1.5–1.8 times larger degree of polymerization compared with experimental values at the same conversion, and the curve has also a slightly larger gradient. This suggests that k'/k lies in the range of 0.010–0.0115 if the calculation is correct. However it is difficult to determine whether a difference in the mean degree of polymerization of this extent is meaningful, as the accuracy of the measurement of molecular weight and other factors as well need to be taken into consideration. In this sense, the result of analysis of the kinetics seems to be more reliable.

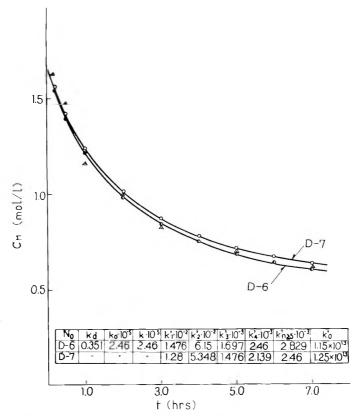


Fig. 15. Results obtained by using the most probable values estimated from the simulations. Relation between the concentration of monomer  $C_{M}$  and the time of polymerization  $t: (\triangle)$  experimental values.

As seen above, quite good agreement is obtained between experiment and the calculated results for the mean degree and rate of polymerization by taking suitable values for the rate constants of component reactions. This fact shows the usefulness of this model in elucidation of the reaction mechanism for oligomer formation.

The values of constants which satisfy the reaction conditions are summarized in Table II.

# MEAN MOLECULAR WEIGHT AND DISTRIBUTION FUNCTION Number-Average Molecular Weight

From the definition of number-average molecular weight, the following equation is derived;

$$\overline{M}_n = \sum M_n C_n / \sum C_n = \sum (nM_0 + M') \delta^n / \sum \delta^n$$
(19)

where  $M_n$  is the molecular weight of the *n*-mer,  $C_n$  is the concentration or number of molecules of *n*-mer,  $M_0$  is the molecular weight of monomer, and M is the molecular weight of the chain transfer agent.

					Most Probable Values	e values				
Vo.	$k_{d}$	$k_0 \times 10^{-5}$	$k \times 10^{-5}$	$k'_1 \times 10^{-2}$	No. $k_d = k_0 \times 10^{-5} = k \times 10^{-5} = k'_1 \times 10^{-2} = k'_2 \times 10^{-2} = k'_3 \times 10^{-3} = k'_4 \times 10^{-3} = k'_n \ge 5 \times 10^{-3} = k'_0 = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} = 10^{-3} $	$k'_{3} \times 10^{-3}$	$k'_{4} \times 10^{-3}$	$k'_n \ge 5 \times 10^{-3}$	k'0	k'/k
9-0	0,351	2.46	D-6 0.351 2.46 2.46	1.476 6.15	6.15	1.697	2.46		2.829 1.15×10 ¹³ 0.0115	0.0115
7-0	0.351	2.46	D-7 0.351 2.46 2.46 1.28	1.28	5.348	1.476	2.139	2.139 2.46 1.25 $\times$ 10 ¹³ 0.010	$1.25 \times 10^{13}$	0.010

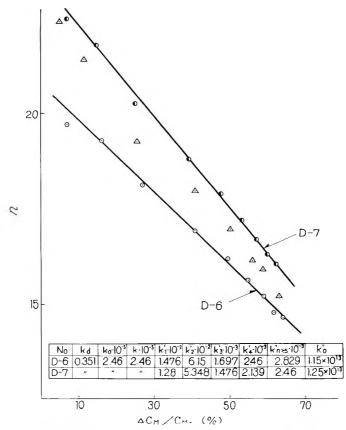


Fig. 16. Results obtained by using the most probable values estimated from the simulations. Relation between the conversion of monomer  $\Delta C_{\rm M}/C_{\rm M0}$  and the number-average degree of polymerization n: ( $\Delta$ ) experimental values.

As 
$$\delta < 1$$
,  $\sum \delta^n = \delta/(1-\delta)$ , eq. (19) can be converted to  
 $\overline{M}_n = [M_0 \delta/(1-\delta)^2 + M' \delta/(1-\delta)]/[\delta/(1-\delta)]$   
 $= M_0/(1-\delta) + M'$ 
(20)  
 $\overline{P}_n = 1/(1-\delta) + M'/M_0$ 
(21)

$$P_n = 1/(1 - 0) + M / M_0$$
 (2)

# Weight-Average Molecular Weight

Similarly to the case of number-average molecular weight, the following equations are derived.

$$\begin{split} \bar{M}_{w} &= \sum M_{n}^{2} C_{n} / \sum M_{n} C_{n} = \sum (nM_{0} + M')^{2} \delta^{n} / \sum (nM_{0} + M') \delta^{n} \\ &= (M_{0}^{2} \sum n^{2} \delta^{n} + 2M_{0} M' \sum n \delta^{n} + M'^{2} \sum \delta^{n}) / (M_{0} \sum n \delta^{n} + M' \sum \delta^{n}) \end{split}$$
(22)

where

$$\sum n^2 \delta^n = \delta(1 - \delta)/(1 - \delta)^3$$

and

$$\bar{M}_w = \frac{M_0(1+\delta) + 2M'(1-\delta) + (M'^2/M_0)(1-\delta)^2}{(1-\delta) + (M'/M_0)(1-\delta)^2}$$
(23)

$$\bar{P}_{w} = \frac{(1+\delta) + 2(M'/M_{0})(1-\delta) + (M'^{2}/M_{0}^{2})(1-\delta)^{2}}{(1-\delta) + (M'/M_{0})(1-\delta)^{2}}$$
(24)

If the degree of polymerization of oligomer is so high that M' can be regarded as negligible, the equation for  $\overline{P}_n$  can then be reduced to a simpler form, which is equal to that for high polymers. Since the ratio  $\overline{M}_w/\overline{M}_n$ which shows the inhomogeneity of the molecular weight distribution can be expressed as  $\overline{M}_w/\overline{M}_n = 1 + \delta$  for high polymers in general, and the extreme case where  $\delta$  approaches 1, then  $\overline{M}_w/\overline{M}_n \simeq 2$ . This, however, represents the case of polymerization in a solvent whose chain transfer constant is negligible, or the case where  $C_S/C_M$  is extremely small, but not the case of oligomerization.

#### **Molar Fraction Distribution Curve**

If  $N_n$  denotes the molar fraction of *n*-mer

$$N_n = C_n / \sum_{n=1}^{\infty} C_n = \delta^n / \sum \delta^n$$
(25)

$$N_n \simeq (1 - \delta)\delta^{n-1} \tag{26}$$

#### Weight Fraction Distribution Curve

If  $W_n$  shows the weight fraction of *n*-mer,

$$W_n = M_n C_n / \sum_{n=1}^{\infty} M_n C_n$$
(27)

In oligomers the endgroup cannot be neglected in determination of the molecular weight of *n*-mers. The molecular weight of the *n*-mer  $M_n$ , then, is expressed as the sum  $N_n = (nM_0 + M')$ , where M' and  $M_0$  denote molecular weights of end-groups and of monomer, respectively.

$$W_n = (nM_0 + M')C_n / \sum (nM_0 + M')C_n$$
  
=  $(nM_0\delta^n + M'\delta^n) / (\sum nM_0\delta^n + \sum M'\delta^n)$  (28)

Since  $\sum_{n=1}^{\infty} n\delta^n = \delta/(1 - \delta)^2$ 

$$W_n = (nM_0 + M')(1 - \delta)^2 \delta^{n-1} / [M_0 + M'(1 - \delta)]$$
(29)

The expression for the weight fraction distribution curve can be reduced to eq. (29). The value of n at which the curve reaches the maximum is obtained by differentiation of eq. (29).

$$\partial W_n / \partial n = (1/A) \delta^n (M_0 + n M_0 \ln \delta + M' \ln \delta) = 0$$
 (30)

Therefore,

$$n = -\left[ (1/\ln \delta) + (M'/M_0) \right]$$
(31)

If the degree of polymerization is sufficiently large to permit M' to be neglected, n can be expressed as follows by utilizing the relationship  $-\ln \delta \simeq (1 - \delta)$ ,

$$n = 1/(1 - \delta) \tag{32}$$

# **Integral Weight Distribution Curve**

The integral weight distribution function  $F_n$  is defined as

$$F_n = \int_0^n W_n dn \bigg/ \int_0^\infty W_n dn \tag{33}$$

From eq. (30),  $W_n$  is expressed as

$$W_n \simeq (1/A)\delta^n (nM_0 + M')$$

and

$$F_{n} = \frac{e^{n \ln \delta} (n \ln \delta - 1) + 1 + (M'/M_{0}) \ln \delta (e^{n \ln \delta} - 1)}{1 - (M'/M_{0}) \ln \delta}$$
$$= \frac{\delta^{n} (n \ln \delta - 1) + (M'/M_{0}) \ln \delta (\delta^{n} - 1) + 1}{1 - (M'/M_{0}) \ln \delta}$$
(34)

If M' can be neglected, eq. (34) is equal to the equation for high polymers

$$F_n = \delta^n (n + n\delta - 1) + 1 \tag{35}$$

# **Index Expression of Distribution Function**

The weight fraction and integral distribution curves are expressed in the form of an index,

$$\delta = kC_{\rm M}/(kC_{\rm M} + k'C_{\rm S}) = (1 + k'C_{\rm S}/kC_{\rm M})^{-1} = (1 + \xi)^{-1}; \ \xi \ll 1$$
(36)  
from  $e^x = 1 + x + x^2/2 + \dots \simeq 1 + x$ 

Then,

or

$$(1 + \xi)^{-1} = e^{-\xi} = \delta$$
  
(1 - \delta) = \xi(1 + \xi)^{-1} (37)

From eq. (29)

$$W_n = \frac{(nM_0 + M')}{M_0 + M'\xi e^{-\xi}} \,\xi^2 e^{-\xi(2+n-1)} = \frac{|n + (M'/M_0)|}{1 + (M'/M_0)\xi e^{-\xi}} \,\xi^2 e^{-\xi(n+1)}$$
(38)

Here, if the degree of polymerization n is large enough to permit M' to be regarded as approximately zero, then

$$W_n = n\xi^2 e^{-\xi(n+1)} \tag{39}$$

On the other hand,

$$\ln \delta = \ln (1 + \xi)^{-1} = - [\xi + (\xi^2/2) + (\xi^3/3) + \dots] \simeq -\xi$$

 $F_n$  is expressed as follows from eq. (34),

$$F_n = \frac{1 - (n\xi + 1)e^{-n\xi} - (M'/M_0)(e^{-n\xi} - 1)\xi}{1 + (M'/M_0)\xi}$$
(40)

If M' can be regarded to be zero as before,  $F_n$  becomes the distribution function for high polymers,

$$F_n = 1 - (1 + n\xi)e^{-n\xi} \tag{41}$$

By comparing the equation with the distribution function proposed by Palit,⁸

the eqs. (38) and (40) turn out to be identical because  $q = \xi$ , r = n from the definition in eqs. (39) and (41).

# RELATIONSHIP BETWEEN THE PER CENT CONVERSION AND THE DISTRIBUTION CURVE FOR OLIGOSTYRENE (EXPERIMENTAL)

## **Fractionation Samples**

The samples of oligostyrene, the products of the polymerization under the conditions shown in Table III at different conversions, were selected in proper intervals, yielding five samples of different per cent conversion

TABLE III

Polymerization System					
	Weight, g.	$\begin{array}{c} \text{Concentration,} \\ M \end{array}$	Volume, ml.	Concentration, mole/l.	Molar ratio
Styrene	19.20	0.1843	21.26	1.673	1.000
$\mathrm{CCl}_4$	141.79	0.9217	88.89	8.368	5.001
AIBN	1.51	0.0092		0.0837	0.050

TABLE IV Conversion and Fractional Samples

			Sample		
	F-1	F-2	F-3	F-4	F-5
Polymerization time, hr.	0.167	0.50	1.00	2.00	7.00
Yield of polymer, g.	0.5	2.2	4.7	7.7	13.7
Conversion of monomer, %	2.5	11.41	24.33	39.85	63.20
Expended sample, g.	2.0038	2.0061	2.0062	2.0002	2.0073

of monomer over the range of 3-70%. They were fractionated and the relationship between the conversion rate and molecular weight distribution was examined (Table IV).

The oligostyrene was fractionated by elusion column chromatography, and the molecular weight of each fraction was determined by measuring the viscosity according to eq. (43):^{2,9}

$$[\eta]_{\text{Benzene}}^{25^{\circ}\text{C}} = 3.77 \times 10^{-4} M^{0.62}$$
(43)

A detailed method of measurement of molecular weight distribution and its accuracy are given elsewhere.^{2,3,9}

#### Molecular Weight Distribution of Oligostyrene

Figure 17 shows an integral distribution curve which was obtained from the distribution function of the fractionated samples F-1-F-5. By differentiating the curve in Figure 17 graphically, the differential distribution curve in Figure 18 was obtained. Molar fraction distribution curves in the polymerization system are based on the distribution functions are shown in Figure 19. All these curves show a shift of the peak towards the lower molecular weight side with an increase of reaction time (as polymerization proceeds) and a tendency to converge to a certain value. This is explained by the fact that the rate of conversion decreases with increasing rate of polymerization toward the limiting value.

One of the features which should be noted in these distribution curves is the small difference in the widths of distribution curves even when the conversion rate is varied substantially. Whether this is due to experi-

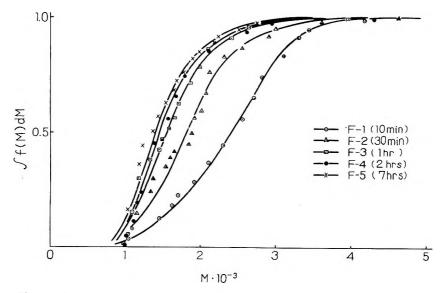


Fig. 17. Integral distribution curves of molecular weight. Oligostyrene samples were fractionated by elution column chromatography with MeOH-MEK as the developing agent, the composition being continuously varied.

mental errors or to an essential character of lower polymerization reactions should be studied further. It is conceivable that the number of moles of products having higher degree of polymerization which are produced at the initial stage of the polymerization is rather small compared with the

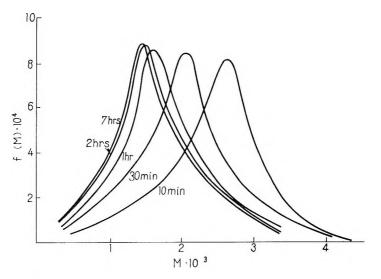


Fig. 18. Differential distribution curves of molecular weight. Obtained by graphical differentiation of the curve in Figure 17.

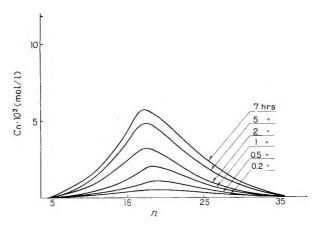


Fig. 19. Molar fraction distribution curves of oligostyrene in polymerization system.

total number of moles of the products at the end of the reaction and that the former do not therefore contribute properly to the measurements. The increase in the number of moles at the low degree of polymerization with the increase in per cent conversion is noticeable, and the shape of the curves is approximately of Gaussian type.

# MOLECULAR WEIGHT DISTRIBUTION OBTAINED BY ANALYSIS OF THE KINETICS

#### Estimation of Chain Transfer Constants and Parameter of Chain Transfer k'

The factors which govern the chain length of polymer in the system discussed here are the rate constants for propagation k and for the chain transfer k'. It is assumed, as stated previously, that the k value is a constant independent of degree of polymerization, but k' depends on it and is not a constant.

However, actually both k' and k depend upon the degree of polymerization, and in this sense the value of k' does not represent the rate constant for the propagation itself, but a kind of parameter which includes the deviation of k caused by the assumption of a constant.

In general, the chain length for the obtained polymer in the system is controlled by k'/k, hence if k is constant, the chain length can be determined by  $k'_n$ . So far, there has been no report on the measurement of k and k' for this oligomerization system, while there are a few reports on polymerization systems. The literature values do not agree exactly with each other but are of the same order as to exponent. The k values used here were obtained by converting the values derived by Matheson to the given temperature and examined by utilizing the chain transfer constant (k'/k) determined by Mayo. Mayo reported that the chain transfer constants for oligomers higher than the pentamer are constant but not those for lower degrees of polymerization than the tetramer.⁷ Then, from the results derived by Mayo et al. from the assumption that the velocity coefficients for propagation are independent of degree of polymerization  $k_n = k, k'$  values can be calculated, and of course  $k_{5 \leq n}$  is constant. By what group of numerical values  $k'_n$  is expressed can be determined, if simulations are carried out by projecting various conditions on an electronic digital computer.

#### **Velocity Coefficients Independent of Chain Lengths over Pentamer**

The calculation results for the case of a fixed value of the parameter  $k'_n$  above pentamer are represented in Figure 20. The results are different from the experimental data in Figure 19, in that the maximum value in Figure 20 exists at n = 4-5, and over wide range of polymerization degree the curve is monotonously decreasing. It is quite natural to take this type of distribution in order to approximate the mean degree of polymerization to the experimental value at the same time keeping the maximum at n = 4-5, although this does not fit the experimental facts at all.

This deviation from the experimental data can be ascribed to an error in the rate constants for the component reactions, as there is no method to measure the constant accurately in such a complicated system, thus making the use of approximate values inevitable. The rate constants for the component reactions depend on the degree of polymerization, and

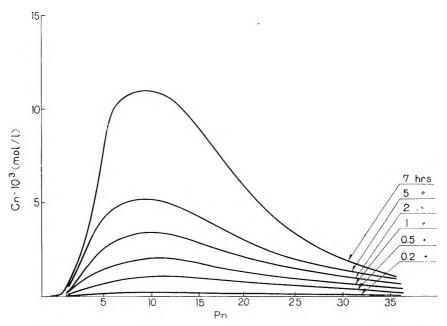


Fig. 20. Distribution curves obtained from analysis of kinetics. Molar distribution curves obtained from the results of calculations for the case of a fixed value in the parameter  $k'_n \geq 5$ .

this dependency can not be ignored in the discussion of the region of oligomer.

#### Estimation of the Proper Series for the Parameter $k'_n$

Strictly speaking, the rate constants for component reactions should be considered to be dependent on the degree of polymerization, and this is particularly the case in the region of low degrees of polymerization. Since it is too difficult to analyze and calculate the reactions including deviation of  $k_n$  from constant k, a condition has to be found that renders the calculation possible. For this reason, as described before, the chain propagation was treated as independent of chain length, with only the chain transfer dependent on chain length, which means that  $k'_1-k'_n$  are parameters of variation of rate constants, and in a polymerization system that the distribution of molecular weight of the oligomer resulting at any conversion depends predominantly on the factor  $k'_n$ , if  $k_i = k(i = 1 \sim n)$ .

Based on the  $k'_1-k'_4$  and  $k'_{5\leq n}$  obtained from the experimental value of chain transfer constant (k'/k), some series of  $k'_n$  were selected as models. In this case, it is important to select the series of  $k'_n$  which may be different from the reported value of  $k'_n$  that can explain the resultant distribution curves of molecular weight.

Six series of the models for  $k'_n$  were selected. The series K-1 is derived from Table V. Curves were selected for K-2 and K-3 by varying the gradient of K-1 adequately at  $k'_4$ .

Initia	l concentration $C_8/C_8$	$Y_{\rm M} = 5$
$k'_{1}/k = 0.0006$	$\delta_1 = 0.9970$	$M_0 = 104 (C_8 H_8)$
$k'_{2}/k = 0.0025$	$\delta_2 = 0.9877$	$M' = 154 \; (\mathrm{CCl}_4)$
$k'_{3}/k = 0.0069$	$\delta_3 = 0.9667$	$M'/M_0 = 1.48$
$k'_{4}/k = 0.0100$	$\delta_4 = 0.9534$	
k'/k = 0.0115	$\delta = 0.9456$	

TABLE V Chain Transfer Constants and Values of  $\boldsymbol{\delta}$ 

The K-4 series was obtained by gradual increase of the gradient at  $k'_{1}-k'_{2}$ , the K-5 series by directly increasing the gradient at  $k'_{4}$ , and the K-6 series by shifting K-5 parallel to the *n* axis to the position of  $k'_{n}$ , where number-average degree of polymerization of the products shows a suitable value. Six cases are displayed in Figure 21. These  $k'_{n}$  values are obtained by the method of least squares based on an arbitrary value of  $k'_{n}$ .

Distribution functions of each series from K-1 to K-6 are given by solving the simultaneous eqs. (6)-(14) by an electronic computer. The correct  $k'_n$  may be obtained by comparing the analytical results with the

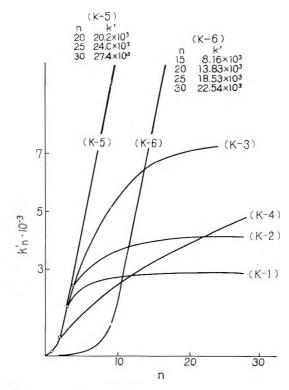


Fig. 21. Estimation of the proper series for the parameter  $k'_n$ . These  $k'_n$  values are obtained by the method of least squares based on an arbitrary value of  $k'_n$ .

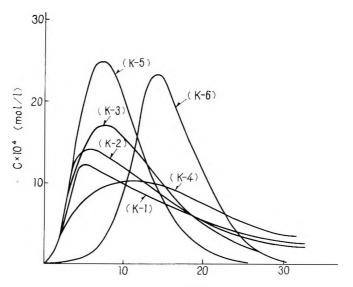


Fig. 22. Distribution curves in the polymerization system under given conditions corresponding to each series of  $k'_n$  for a polymerization time of 1 hr.

experimental values. The distribution curves under the given conditions corresponding to each series of  $k'_n$  for a polymerization time of 1 hr. are shown as Figure 22 for the convenience of comparison of mutual relations. It is of interest to examine the adequateness of the series in K-1-K-6, in connection with Figures 21 and 22.

#### Consideration of the Distribution Curve Obtained by Analysis of Kinetics

On comparing Figure 22 with the experimental Figure 19, the series K-3 and K-6 are found to fit the experimental distribution of  $k'_n$  more closely. The series K-3 is, as is clearly seen from Figure 21, a system in which  $k'_n$  increases with considerable gradient in the domain above tetramer, but its gradient decreases gradually and is roughly constant, at near  $k'_{20}$ . The K-6 series is obtained by shifting  $k'_1 - k'_4$  about 6 units along the n axis and by diverging to  $k'_n$  with the same gradient at the point of  $k'_4$ . This means that the parameter of chain transfer from  $k'_1$ to  $k'_5$  is nearly equal to zero, gradually increases beyond  $k'_5$  up to  $k'_{10}$ , and the gradient at  $k'_{10}$  is maintained above this point. Then, the parameter of chain transfer k' is negligible at the very initial stage of the reactions, but it increases constantly above decamer. In other words, the value of  $k'_n$  in the K-3 series, which has been discussed previously, does not converge at the point  $n \ge 4$ , but at a higher degree of polymerization, for example  $n \ge 20$ . In series K-6,  $k'_n \le 4$  can be neglected at the beginning of polymerization, but beyond  $n \geq 5$ , it increases gradually to infinity.

In the case of series K-6, this fact can be understood if we consider  $k'_n$  is a parameter involving the deviation caused by the assumption of  $k_n \equiv k$ .

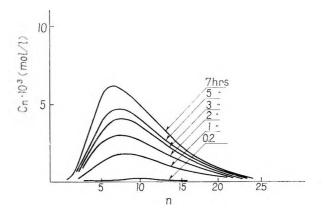


Fig. 23. Distribution curves in the polymerization system obtained by analysis of kinetics. The results obtained by using parameter series K-3 are shown.

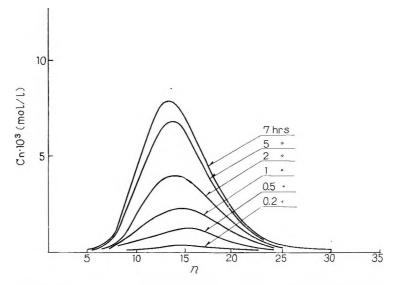


Fig. 24. Distribution curves in the polymerization system obtained by analysis of kinetics. The results obtained by using parameter series, K-6 are shown.

From these observations, the most probable series of  $k'_n$  is K-6, of course, the real value of  $k'_n$  would differ a little from this value, but they would have a similar character. From these results, information about the absolute values of rate constants for each component reaction were obtained, but a more important finding is that the common concept of independence of rate constants from degree of polymerization is not necessarily true. At least concerning the oligomer, it is clear that the dependence of reaction rate on the degree of polymerization should be considered.

The distribution curves of degree of polymerization derived by adapting analysis of the kinetics on the proper models K-3 and K-6 are shown in Figures 23 and 24, respectively. It is of interest to note that these two curves are similar to the experimental curves in their shape. The conclusion derived from these two curves is that the series of  $k'_n$  in K-6 shown in Figure 24 is more suitable for explaining the resulting products as to the variation of mean degree of polymerization with the degree of polymerization. This fact, however, does not necessarily indicate the correctness of parameters K-6, because the explanation is also possible with K-3 only by moving the curves parallel to the *n* axis. Thus, it can not be concluded at this stage which of the two models is more appropriate to explain the distribution of  $k'_n$ .

The essential differences between these two series lies in the question of whether  $k'_n$  is a convergent series or a divergent one. It is very difficult, however, to decide which is more meaningful in representing the actual phase. The results which have been derived by comparing the experimental results with analysis of the kinetics are summarized as follows: (1) the distribution of  $k'_n$  appears to increase continuously up to a larger value of n than has been supposed; (2) the k' values below  $k'_5$  are estimated to be smaller than those reported; (3) this discussion is valid only for the case when  $k'_n$  is treated as parameter in the sense as stated above; (4) those studies to determine more detailed  $k'_n$  value and micromechanisms of the reactions through these values in combination with experimental results are considered to be important.

The low polymer obtained by the telomerization has been said in general to have a wide distribution of molecular weight. However, it became evident after examining the distribution of molecular weight by fractionation that it had unexpectedly a narrow distribution. It is well known that in many cases the distribution pattern of the polymer is of Schultz type, in which a peak exists at relatively low degrees of polymerization. However, the distribution pattern of oligostyrene is, as seen from the results of measurements, relatively close to the Gaussian distribution, and is different from the distributions in high polymers.

So far there have been only a few reports on the distribution of the molecular weight of lower polymers and no established information in this regard. On the basis of the correct molecular weight distribution of oligostyrene some insight into the kinetics of polymerization would be obtained.

As has already been seen, the change of concentration of any component in this system was explained by detailed calculations with an electronic computer based on the chain transfer constants reported previously, and a probable value of the coefficient for the chain termination  $k'_0$  was estimated. But the concentration of obtained oligomer presented by eqs. (14') and (12), especially the change of the distribution of molecular weight with time, does not agree with the experimental value, the mean value being always smaller. It leads to a larger value of total moles of oligomer than in the experiment.

Apparently the too large values of the parameter  $k'_n$  which was used in the calculation seems to be solely responsible for this discrepancy. An adequate correction applied to  $k'_n$ , therefore, suffices to bring the calculated distribution closer to the observed values. As is clearly seen in Figure 21, the conventional treatment of  $k'_n$  constant above n = 5 is not valid, but  $k'_n$  has to be understood as a function of the degree of polymerization. This phenomenon is not limited to the case of oligostyrene, and apparently is common in the lower polymerizations of this kind. It is evident from this study that the  $k'_n$  value of low polymers is almost equal to zero up to  $n \simeq 5$  but increases gradually with polymerization degree.

Of course, such a view is based on the assumption that the measurement of the distribution of molecular weight is correct, and it is proved that a quite accurate measurement of molecular weight can be carried out by elution column chromatography. It is one of the very important characteristics that the distribution of molecular weight of oligomer is rather narrow in comparison with that of high polymer.

In fact, if the calculation is made with the use of a computer from this standpoint, the phenomenon can be explained easily.

## CONCLUSION

The detailed oligomerization kinetics of styrene was examined and a concept of the oligomerization, namely low polymerization, by radical mechanisms was established. An attempt was made to elucidate the reaction mechanisms of oligomerization with the aid of an electronic computer to follow the concentration change of components in the system along with the change in the degree of polymerization and with the distribution of molecular weight. The results may be summarized as follows.

(1) The rate equations for component reactions in the oligomerization consisting mainly of chain transfer reaction were established.

(2) The variation of concentration of multicomponents expressed as a function of time in the system are obtained by solving simultaneous differential equations with a medium-scale electronic digital computer (IBM 650) by utilizing Runge-Kutta method.

(3) A stationary state was reached within very short time of  $10^{-8}$ - $10^{-6}$  hr. When the initial value is zero, first the initiator radicals, next the solvent radicals, then finally the total concentration of radicals in the system reached a stationary state.

(4) Computer calculations indicate that the variation of concentration of radicals is almost constant at any point of time where the concentration of the feed components in the system (monomer, transfer agent, initiator) changes significantly. This fact suggests that a stationary state exists at any point of time independent of the rate of polymerization except at the initial and final stages of polymerization processes.

(5) By comparing molecular weight distributions obtained by analysis of the kinetics with the experimental data it is possible to discuss the change of concentration of the system, the rate of polymerization (i.e.,

conversion of monomer), and the number-average degree of polymerization of products quantitatively from the known velocity coefficients of component reactions and the distribution of molecular weight. The velocity coefficient for chain termination  $k'_0$  has also been estimated.

(6) The oligostyrenes have rather narrow molecular weight distributions in comparison with those of high polymers. The distribution curve which fits the experimental data was obtained by assuming the parameter  $k'_n$  to be dependent on the chain length and at the same time to increase with the degree of polymerization.

In this paper an attempt to elucidate the reaction kinetics of a complex system for oligomerization with an electronic computer was reported. The equations contain many variables which often differ greatly in magnitude, and this made the analysis difficult. This difficulty was avoided by utilizing the conditions of a steady state.

We are still a long way from treating chemical reactions quantitatively by simulation on a computer, but this method is very useful in elucidating the fine mechanism of a reaction if adequate values are supplied for the essential constants and parameters.

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#### Résumé

Nous avons étudié, en choisissant comme modèle le système styrène– $CCl_4$ , les mécanismes d'oligomérisation radicalaire par transfert de chaîne, en connexion avec la répartition des poids moléculaires de l'oligostyrène obtenu. La cinétique de la réaction de transfert de chaîne est difficile à analyser, parce que les concentration des composants dans le système varient suivant l'évolution de la réaction d'oligomérisation. Nous avons analysé, à l'aide du calculateur électronique digital IBM-650, l'importance des réactions composantes exprimées par les équations différentielles simultanées. Les valeurs analytiques et les données expérimentales sont en bon accord, et la corrélation entre les

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coefficients de vitesse cinétique dans le système a été éclaircie. On a obtenu de nombreuses informations concernant le contrôle de la réaction d'oligomérisation.

## Zusammenfassung

Der Reaktionsmechanismus der radikalischen Oligomerisation durch Kettenübertragung im als Modellsystem gewählten System Styrol-CCl4 wird in bezug auf die Molekulargewichtsverteilung des erhalten Oligostyrols untersucht. Da sich die Konzentration der Komponenten im System während der Oligomerisation verändert, ist die Kinetik der Kettenübertragungsreaktion schwer zu analysieren. Mit dem "Elektronendigitalrechner IBM 650" wurde die Geschwindigkeit der Elementarreaktionen, die in simultanen Differentialgleichungen mit mehreren Unbekannten vorliegen, erhalten. Die analytischen und experimentellen Werte können in gute Übereinstimmung gebracht werden. Der Zusammenhang zwischen den kinetischen Geschwindigkeitskoeffizienten im System wird geklärt, und damit werden neue Kenntnisse über die Oligomerisation gewonnen.

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# Scission Reactions in Some Vinyl and Vinylidene Polymers

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#### **Synopsis**

Rates of autocatalyzed oxygen absorption and chain scission were measured at 160 °C. and 1 atm. oxygen pressure for copolymers of ethyl acrylate-methyl methacrylate and ethyl acrylate-methyl  $\alpha$ -chloroacrylate. The crosslinked homopolymers of both the vinylidene-type monomers were very resistant to oxygen uptake and oxidative scission. Increasing amounts of ethyl acrylate in the copolymer systems increased the rate of oxygen absorption and chain scission. Slightly crosslinked poly(methyl methacrylate) containing 5% of dicumyl peroxide showed rapid chain scission at 140°C. in the absence of oxygen and negligible chain scission in the presence of oxygen. The same experiment carried out with poly(ethyl acrylate) shows the reverse behavior: crosslinking and little scission in the absence of oxygen and efficient chain scission in the presence of oxygen. Chemical mechanisms are presented to account for these results.

## Introduction

Chain scission is a most facile process when peroxide-initiated, radiationinitiated, or thermally induced degradations of vinylidene type polymers are conducted in the absence of oxygen at high temperatures. Recent studies of the dicumyl peroxide-initiated degradation of polyisobutylene^{1,2} have shown scission to be an efficient process; close to one scission is produced by each initiating radical. In the pyrolysis of poly(methyl methacrylate) and poly- $\alpha$ -methylstyrene it has been further demonstrated that an initial chain scission is followed by depropagation resulting in almost quantitative yields of monomer.³ It is well known that vinylidene polymers tend to degrade rather than crosslink when exposed to high energy radiation in the absence of oxygen.

Under similar conditions vinyl polymers give low yields of monomers;³ crosslinking accompanies and predominates over scission,⁴ and low ratios of scissions to initiating radicals are observed.⁵ Vinyl-type polymers will generally give crosslinked networks when exposed to high-energy radiation in the absence of oxygen, though some scission accompanies crosslinking.

In the presence of oxygen a striking reversal takes place for these two classes of polymers.

It has been shown that each initiating radical abstracting a tertiary hydrogen, produces one chain scission during the benzoyl peroxide-initiated oxidation of polypropylene and poly(ethyl acrylate).⁵ In this paper, by contrast, we show that oxygen actually inhibits chain scission during the dicumyl peroxide-initiated degradation of poly(methyl methacrylate).

Autoxidation studies at 160 °C. show that scission is rapid in poly(ethyl acrylate), a vinyl-type polymer. On the other hand it is very much slower in poly(methyl methacrylate) and in poly(methyl  $\alpha$ -chloroacrylate). Rates of oxidative scission in ethyl acrylate-methyl methacrylate and ethyl acrylate-methyl  $\alpha$ -chloroacrylate copolymers are consistent with earlier work,^{5,6} showing that it is the tertiary hydrogen along the polymer backbone that suffers the oxidative attack leading to scission. Free radical mechanism can be suggested to account for these results.

#### **Experimental**

Monomers (The Borden Chemical Co.) were freed of inhibitor by alkali and distilled water washings and were dried over magnesium sulfate. Solutions of 1 mole-% ethylene glycol dimethacrylate (EGDMA) in the monomers were prepared and to these was added less than 1% benzoin. Since the crosslinking agent may affect the rates of scission and oxygen uptake, all copolymers were prepared with 1 mole-% of crosslinking agent. Photopolymerizations were carried out between Pyrex glass plates, Teflon gaskets being used to keep the thickness of the sheets at 15 mils. A General Electric RS sunlamp was used as the light source as previously described.⁷ The films were swollen in acctone and dried in vacuo. The poly(methyl methacrylate) was annealed in vacuo for 6 hr. at 140°C. The poly(methyl  $\alpha$ -chloroacrylate) was similarly treated for 20 min.

The rates of chain scission were followed using the technique of stress relaxation.⁸ The amount of scission, the number of cuts/per cubic centimeter that have occurred up to time t was calculated from the equation:⁹

$$q(t) = -N_0 \ln (f_t/f_0)$$
(1)

where  $f_t/f_0$  is the ratio of stress on the sample at time t to that at time zero.  $N_0$  is the crosslink density as calculated from the equation of rubber elasticity.⁷ Oxygen was flushed through the relaxometer so that the rates of scission would be independent of oxygen pressure as previously shown.⁵

Oxygen absorption measurements were run with a 20-cc. cell attached to a single water-jacketed manometer-buret containing dioctyl phthalate as the indicating fluid. A constant-temperature bath kept the cell at 160  $\pm$  0.2°C. Calcium oxide was used to absorb volatiles.⁵ The rates of oxygen absorption were found to be independent of oxygen pressure at 1 atm. of oxygen. These rates were also found to be independent of sample thickness between 2 and 15 mils.

Densities were taken with a Weld pycnometer at room temperature. The values obtained were: poly(ethyl acrylate), 1.13 g./cc.; poly(methyl methacrylate), 1.19 g./cc.; poly(methyl  $\alpha$ -chloroacrylate) 1.40 g./cc.

Dicumyl peroxide (Borden), recrystallized from ethanol was incorporated into poly(methyl methacrylate) by swelling the sample in a concentrated peroxide-benzene solution for two days, followed by drying *in vacuo* for three days.

## Results

Figure 1 shows the data for  $f_t/f_0$  for the crosslinked ethyl acrylatemethyl methacrylate copolymers at 160°C. q(t) is obtained from eq. (1),

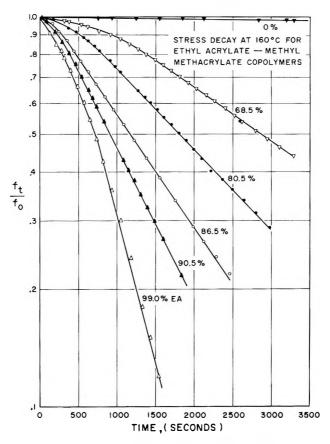


Fig. 1. Stress decay with time for ethyl acrylate-methyl methacrylate copolymers. Numbers indicate mole per cent of ethyl acrylate.

and it is clear that an apparent steady rate of scission is reached for all samples within 1 hr. Figure 2 shows data for the molecules of oxygen absorbed per cubic centimeter of polymer versus time for the ethyl acrylatemethyl methacrylate copolymer system. Once again it is clear that an apparent steady rate of oxygen absorption is reached within 1 hr. for all these copolymers.

Table I shows the steady rates of scission and oxygen absorption for all the copolymers and homopolymers. It is clear that the slightly crosslinked homopolymers of methyl methacrylate and methyl- $\alpha$ -chloroacrylate are

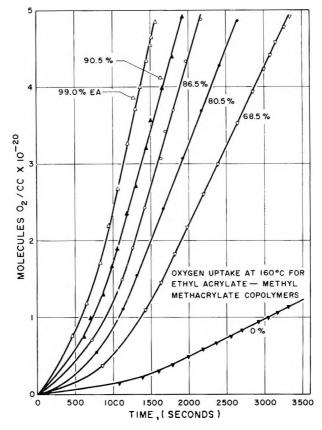


Fig. 2. Oxygen uptake with time for ethyl acrylate-methyl methacrylate copolymers. Numbers indicate mole per cent of ethyl acrylate.

comparatively very resistant to oxidation as measured by oxygen absorption or by chemical stress relaxation. Introduction of increasing amounts of ethyl acrylate into these polymers greatly increases the rate of oxygen absorption and of chain scission. As is evident from Table I, for a given mole per cent of ethyl acrylate, the methyl  $\alpha$ -chloroacrylate copolymers display higher rates of scission than do the methyl methacrylate copolymers. The rates of oxygen uptake for the two systems are comparable. Under equivalent conditions then,  $\epsilon$  methyl group along the polymer backbone inhibits the scission reaction to a greater degree than does chlorine.

The relative inertness of poly(methyl methacrylate) to oxidative scission is dramatized by the following experiment. Dicumyl peroxide (about 5 wt.-%) was incorporated into thin strip samples of slightly crosslinked poly(methyl methacrylate). Chemical stress relaxation measurements were carried out at 140°C., alternately under purified nitrogen and under oxygen. Relaxation of stress (caused by chain scission) occurred under nitrogen but not under oxygen, as can be seen in Figure 3. (Negligible rates occurred without dicumyl peroxide in both nitrogen and oxygen.)

	E A	EGDMA,	N₀, chains/cc.	dq/dt cuts/cc. sec.	$dO_2/dt$ , molecules
Copolymer	EA, mole- $\%$	mole-% ^a	$\times 10^{-19}$	$\times 10^{-16}$	cc. sec. $\times 10^{-17}$
EA-MMA	0.0	1.03	13.4	0.14	0.5
	68.5	1.08	8.6	2.8	2.0
	80.5	1.07	8.4	3.9	2.6
	86.5	1.27	8.0	5.4	3.4
	90.5	0.99	7.1	6.5	3.8
	99.0	1.00	7.1	12.3	4.6
EA-MCA	0.0	0.97	9.7	0.4	0.4
	67.1	1.04	9.3	4.1	2.3
	78.2	1.02	8.5	6.7	3.1
	85.8	0.98	8.0	8.0	3.6
	91.5	0.98	7.0	8.9	4.0
	96.0	0.98	7.0	11.1	4.4

TABLE I
Steady Rates in the Oxidation of Ethyl Acrylate-Methyl Methacrylate (EA-MMA)
and Ethyl Acrylate-Methyl Chloroacrylate (EA-MCA) Copolymers

^a Ethylene glycol dimethacrylate.

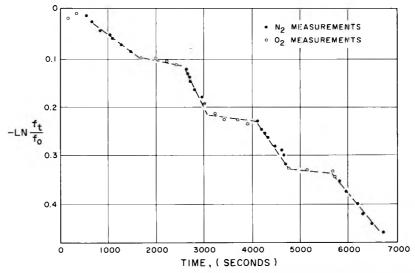


Fig. 3. Stress decay with time for poly(methyl methacrylate) with incorporated dicumyl peroxide. Relaxometer was flushed alternately as noted with nitrogen and oxygen.

Exactly the reverse is true for poly(ethyl acrylate).⁵ In the absence of oxygen, a free radical source causes crosslinking, but very little scission. In the presence of oxygen, scission without crosslinking is found.

# **Discussion of Possible Chemical Mechanisms**

To account for these observations it is possible to formulate a coherent set of chemical mechanisms. These of course must be viewed as any newly proposed mechanisms. They are tentative and are to be used as the basis for future experiments. It is highly likely that a combination of processes other than those advanced here could be written to explain the experimental observations. The following is what we feel at present is the simplest explanation.

All of the results of this study are consistent with the proposal that tertiary peroxy radicals are stable propagating species which terminate slowly in comparison with primary or secondary peroxy radicals.

Previous work on the initiated oxidation of poly(ethyl acrylate)⁵ has shown that scission and termination are concomitant processes, since scission produces primary peroxy radicals that terminate rather than continuing the kinetic chain by abstracting another tertiary hydrogen [eqs. (2)-(5)]:

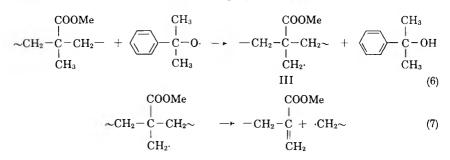
$$\sim CH_2 \xrightarrow{\downarrow} COOEt \qquad COOEt \\ \sim CH_2 \xrightarrow{\downarrow} C \xrightarrow{\downarrow} CH_2 \xrightarrow{$$

$$\cdot \mathrm{CH}_2 \sim + \mathrm{O}_2 \rightarrow \cdot \mathrm{OO-CH}_2 \sim$$
(4)

$$2 \cdot 00 - CH_2 \sim \rightarrow HOCH_2 \sim + 0 = CH \sim + O_2$$
(5)

Therefore, in poly(ethyl acrylate) oxidation and scission are rapid; the tertiary hydrogen is vulnerable to attack to produce a stable propagating tertiary peroxy radical (I) which can also react to give the precursor to scission, the tertiary alkoxy radical (II). Termination follows immediately.

In poly(methyl methacrylate) however, no tertiary peroxy radical can be formed. In the initiated degradation in the absence of oxygen, an alkyl radical (III) can be formed by hydrogen abstraction which can be the immediate precursor to scission [eqs. (6) and (7)]:



In the presence of oxygen, however, this radical will add oxygen to form a primary peroxy radical which will rapidly terminate with no attended scission [eqs. (8) and (9)].

$$\begin{array}{ccc} & & & & & & \\ & & & & & \\ & & & & \\ & \sim CH_2 - & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & &$$

$$2 \sim CH_{2} - CH_{2} \sim \rightarrow \sim CH_{2} - CH_{2} \sim + \sim CH_{2} - CH_{2} \sim + O_{2} \qquad (9)$$

$$CH_{2}OO \cdot CHO \qquad CH_{2}OH$$

Table I shows that scission is much lower in the methyl methacrylate copolymers than in the methyl chloroacrylate copolymers for a given ethyl acrylate concentration; this suggests that the methyl group on the polymer backbone serves to retard scission. A possible mechanism involves the formation of radical III as shown in eq. (10):

$$\begin{array}{ccc} \text{COOEt} & \text{COOMe} \\ \sim \text{CH}_2 & -\text{C} & -\text{CH}_2 & -\text{C} & \text{COOEt} & \text{COOMe} \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & &$$

The methyl group presents to the alkoxy radical a hydrogen that can be abstracted readily through a six-membered transition state. Kabasakalian and Townley¹⁰ have shown that when a six-membered transition state can be formed, hydrogen abstraction can complete favorably with the cleavage reaction. The methyl group at low concentrations should effectively block three potential scission sites, the position occupied and the two adjacent. At higher concentrations several methyl methacrylate units retard scission at overlapping sites reducing the effectiveness of a single unit. Such a reaction then can qualitatively explain the observed variation of the rate of scission with mole percent of ethyl acrylate in the copolymer.

The fact that oxygen absorption is not so affected at low methyl methacrylate concentrations can rule out the formation of radical III by a propagating peroxy radical.

In conclusion, it may be expected that for numerous polymers the paths to scission under oxygen may be quite different than in inert atmospheres, and that reversals in stability may be found for systems other than the vinyl and vinylidine polymers.

The financial support of the Textile Research Institute and the Army Research Office (Durham) is appreciated.

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### Résumé

Les vitesses d'absorption autocatalysée d'oxygène et de rupture de chaîne ont été mesurées à 160°C, et sous une pression d' une atmosphère d'oxygène pour les copolymères acrylate d'éthyle-méthacrylate de méthyle et acrylate d'éthyle- $\alpha$ -chloracrylate de méthyle. Les homopolymères pontés des deux monomères du type vinylidène résistaient très bien à l'absorption d'oxygène et à la rupture oxydante. Des quantités croissantes d'acrylate d'éthyle dans les copolymères augmentent la vitesse d'absorption d'oxygène et de rupture de la chaîne. Le polyméthacrylate de méthyle, contenant 5% de peroxyde de dicumyle, légèrement ponté, présente une rupture de chaîne rapide à 140°C en absence d'oxygène et une rupture négligeable en présence d'oxygène. La même expérience, effectuée avec le poly-acrylate d'éthyle, montre un comportement inverse: pontage et peu de rupture en absence d'oxygène et scission de chaîne en présence d'oxygène. On présente des mécanismes chimiques pour expliquer ces résultats.

### Zusammenfassung

Die Geschwindigkeit der autokatalysierten Sauerstoffabsorption und Kettenspaltung wurde bei 160°C und 1 Atmosphäre Sauerstoffdruck an Athylacrylat-Methylmethacrylat- und Äthylacrylat-Methyl- $\alpha$ -chloracrylatkopolymeren gemessen. Die vernetzten Homopolymeren der beiden Monomeren vom Vinylidentyp waren gegen Sauerstoffaufnahme und oxydative Spaltung beständig. Steigende Mengen von Äthylacrylat im Kopolymersystem erhöhten die Geschwindigkeit der Sauerstoffabsorption und Kettenspaltung. Schwach vernetztes Poly(methylmethacrylat) mit einem Gehalt von 5% Dicumylperoxyd zeigte bei 140°C in Abwesenheit von Sauerstoff rasche Kettenspaltug und in Gegenwart von Sauerstoff vernachlässigbare Kettenspaltung. Der gleiche Versuch mit Poly(äthylacrylat) liefert das umgekehrte Verhältnis: Vernetzung und geringe Spaltung in Abwesenheit von Sauerstoff und wirksame Kettenspaltung in Gegenwart von Sauerstoff. Zu Erklärung der Ergebnisse werden chemische Mechanismen aufgestellt.

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# Investigation of Thiazole Polymers for Heat-Resistant Fibers and Films

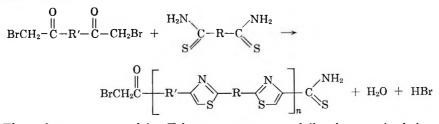
W. C. SHEEHAN and T. B. COLE, Southern Research Institute, Birmingham, Alabama, and L. G. PICKLESIMER, Aeronautical Systems Division, Wright-Patterson Air Force Base, Ohio

### **Synopsis**

Seventeen thiazole polymers were prepared by the polycondensation of his- $\alpha$ -bromoketones with dithioamides, and the polymers were investigated for preparing heat-resistant fibers and films. Tough fibers and films were made from four of the polymers; however, these polymers had low melting points (164–250°C.). All of the other polymers studied except these did not melt below 500°C., and they had excellent thermal stabilities, but they did not have good fiber- and film-forming properties because of their low molecular weights. All of the polymers prepared had some crystallinity. Two of the polymers were soluble in organic solvents; the others were soluble only in strong acids. Model compounds of four of the polymers were prepared, and the properties and structures of the compounds were compared with those of the polymers.

### **INTRODUCTION**

The condensation of halomethylketones and thioamides for preparing thiazoles is well known,¹ and the general reaction has been applied by Erlenmeyer et al.,²⁻⁹ by Mulvaney and Marvel,¹⁰ by Inoue et al.,¹¹ and by Longone and Un¹² to prepare thiazole polymers from bis- $\alpha$ -haloketones and dithioamides.



The polymers prepared by Erlenmeyer were not fully characterized, but those prepared by Inoue et al. and later by Mulvaney and Marvel, by condensing dithioadipamide, dithioterephthalamide, and dithioisophthalamide with p-bis(bromoacetyl) benzene, were reported to have a fair degree of thermal stability and to be soluble in strong acids. They had a number-average molecular weight of about 5000–6000, as indicated by endgroup analyses, but only the polymer obtained from dithioadipamide was film-forming. As a result of the work of Mulvaney and Marvel, thiazole polymers appeared to hold promise for the production of fibers and films of high thermal and chemical stability. The thiazole nucleus is remarkably resistant to drastic treatment with acids and bases, and it is not readily attacked by oxidizing agents.¹³ It remained to be shown, however, that the thiazole polymers could be made into fibers and films with desirable properties; and our work has been directed toward this goal. The three thiazole polymers described by Mulvaney and Marvel and fourteen thiazole polymers that have not been reported previously have been synthesized from bis- $\alpha$ -bromoketones and dithioamides and evaluated in our program. Model compounds of four of the polymers were prepared, and the properties and structures of the compounds were compared with those of the polymers.

# PREPARATION OF POLYMERS AND MODEL COMPOUNDS

Polymers were prepared by condensing  $bis-\alpha$ -bromoketones with aliphatic or aromatic dithioamides. The monomers that were used are listed in Table I, together with references to the methods of synthesis, the yields, and the melting or boiling points of the monomers and their precursors that were made. 2,2'-Dithiobiphenamide and dithiodipicolinamide were the only monomers made that have not been reported previously.

The polycondensations of the bis- $\alpha$ -bromoketones and dithioamides were carried out by dissolving equimolar amounts of the monomers in a solvent and stirring the solutions in the presence or absence of air with or without heating. Polymerizations were rapid; the polymers, with few exceptions, began to precipitate from solution shortly after reaction commenced. Polymerizations were carried out in acetic acid, acetone, dimethylformamide, or dimethylacetamide for 0.5–89 hr. and at temperatures ranging from 28 to 152°C.

Table II gives the repeating units of the polymers made and summarizes data on representative reaction conditions, yields, inherent viscosities, molecular weights, and colors of the polymers. Unless otherwise specified, no attempt was made to exclude air from the reaction mixture.

Inherent viscosities of the polymers in formic or sulfuric acid were used to indicate the relative molecular weights of the polymers. Thiazole polymers behave as polyelectrolytes in acids, the only effective solvents for most of the polymers, and the formation of salts in the acid solutions probably accounts for the unusually large differences in the inherent viscosities of a polymer determined in different acids.

Number-average molecular weights of 800–80,000 were indicated by bromine endgroup analyses for some of the polymers that had been exhaustively purified by extraction and reprecipitation. These values are questionable because of the difficulties of analyzing for small quantities of bromine and because of the difficulties of removing the hydrogen bromide liberated by the monomer during the polymerization and possibly attached to the nitrogen atom of the thiazole ring, without removing the active bromine on the polymer chain end.

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	Method of		Melting
	synthesis	Yield,	or boiling
Monomers and precursors	(ref.)	%	point, °C."
Dithiooxamide	Fro	m Eastmar	Chemical Co.
Dithiomalonamide	8	51	210 (dec.)
Dithiosuccinamide	9	41	143 (dec.)
Dithioadipamide	14	54	175-178 (dec.)
Dithiosebacamide	15	38	153 (dec.)
Dithioterephthalamide	14	75	266-272 (dec.)
Dithioisophthalamide	14	73	198-200 (dec.)
4,4'-Dithiodiphenamide	16	80	282-283 (dec.)
Dithiodipicolinamide ^b		85	233–235 (dec.)
2,2'-Dithiodiphenamide ^c		93	195–196 (dec.)
Perfluorosuccinodithioamide	$\mathbf{F}_{1}$	rom Penins	ular Chemical
		Researc	ch, Inc.
p-Bis(bromoacetyl)benzene	17	85	167–173 (dec.)
$p$ -Bis( $\alpha$ -bromopropionyl)benzene	18	49	119-120
4,4'-Bis(bromoacetyl)diphenyl ether	19	30	109-110
Isophthalamide	14	81	277 - 280
Isophthalonitrile	14	41	156 - 158
4,4'-Dicyanodiphenyl	20	27	236 - 237
Dipicolinamide	21	94	320
Dipicolinonitrile	22	38	125 - 127
2,2'-Diphenamide	23	70	215
2,2'-Dicyanodiphenyl	24	86	170
p-Dipropionylbenzene	25	19	97-98
p-Propylpropionphenone	25	88	143-145/18 min.
			Hg
4,4'-Diacetyldiphenyl ether	26	77	105-107

### TABLE I Methods of Synthesis, Yields, and Melting and Boiling Points of Monomers and Precursors

^a Uncorrected.

^b Anal. Calc.: C, 42.62%; H, 3.58%; N, 21.30%; S, 32.50%. Found: C, 42.53%; H, 3.63%; N, 21.14%; S, 32.20%.

^c Anal. Calc.: C, 61.78%; H, 4.45%; N, 10.29%; S, 23.53%. Found: C, 61.69%; H, 4.65%; N, 10.17%; S, 23.50%.

Light-scattering techniques were tried for determination of the molecular weights of several polymers that were soluble only in strong acids, but they were unsatisfactory because of the color and fluorescence of the acid solutions. However, the weight-average molecular weight of polymer XV, which was soluble in organic solvents, was determined in dimethylformamide by light scattering and found to be 7800. This polymer had an inherent viscosity in formic acid of 0.59 dl./g. and a number-average molecular weight of 40,000 based on bromine analysis.

Polymers IV, and VI, and VII were the first polymers that we prepared. They were prepared initially by the procedures reported by Mulvaney and Marvel.¹⁰ Polymer IV was originally prepared by mixing hot acetic acid solutions of the monomers and stirring the mixture overnight at 60°C. Since the temperature of the monomer solution at the time of mixing was

		List of Folymers and Summary of Folymerization Experiments Reaction conditions	Reaction conditions	zauon Ex	herman				
Polymer	Repeating unit	Solvent	Total monomer concn., mole/1.*	Temp., Time, Yield, °C. hr. %	Time, hr.	Yield, $\%$	Inherent viscosity, dl./g. in solvent ^b	Molecular weight, number- average ^e	Color
I		Acetic acid DMF Acetone	0.200 0.200 0.200	60 35	18 23 64	0 58 23	0 21, S.A. 0 29, S.A.	5,100	Red-brown Red-brown
п		Acetic acid Acetic acid DMF	0.098 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0.200 0	118-90 60 35	$\begin{array}{c} 0.5\\ 22\\ 16\\ 16\end{array}$	31 75 63	0.06, S.A. 0.13, S.A. 0.24, S.A.		Red Red Yellow
Η	Chen Charles - S	Acetic acid DMF	0.105 0.105	60 60-48	18 18	20 45	0.87, F.A. 0.81, F.A.	36,300	36,300 Pale yellow Pale yellow

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# THIAZOLE POLYMERS

$\operatorname{Tan}$	$\mathrm{Tan}$	$\operatorname{Tan}$	$\operatorname{Tan}$	$\operatorname{Tan}$	Pale yellow	Pale yellow	2	Gray	$\mathbf{Y}$ ellow	Yellow	$\operatorname{Brown}$	Yellow	Yellow	Yellow	$\mathbf{Yellow}$	$\mathbf{Y}\mathbf{ellow}$	$\mathbf{Y}$ ellow	(continued)							
									80,000			42,000							1,660						
0.74, F.A.	1.81, F.A.	1.26, F.A.	0.37, F.A.	3.80, F.A.	3.96, F.A.	3.07, F.A.	3.30, F.A.	0.89, F.A.	2.51, F.A.	2.41, F.A.	3.66, F.A.	1.78, F.A.	0.73, F.A.		0.14, S.A.	0.15, S.A.	0.19, S.A.	0.20, S.A.	0.12, S.A.	0.16, S.A.	0.20, S.A.	0.27, S.A.	0.30, S.A.	0.24, S.A.	
47	64	75	62	70	44	53	25	35	72	35	46	100	54	9	43	87	79	56	87	68	44	66	86	77	
20	16	16	16	18	16	16	89	16	18	16	16	18	18	c	3	9	18	4.5	16	64	64	64	9	72	
60	60 - 48	09	09	80 - 60	85-57	88 - 50	35	70	32	33	сс СС	60	60	-	118	100	100	152	152	152	38	28	100	100	
0.078	0.078	0.092	0.232	0.078	0.089	0.097	0.088	0.078	0.086	0.080	0.086	0.060	0.060		0.110	0.079	0.079	0.200	0.180	0.700	0.064	0.031	0.079	0.079	
Acetic acid							DMF		Acetone			Acetic acid	DMF		Acetic acid	DMF					Acetone		DMA		
	S. S.																								
IV												٨			IΛ										

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		Reaction co	Reaction conditions	nditions					
Polymer	Repeating unit	Solvent	Total monomer concn., mole /1.ª	Temp., °C.	Time, hr.	Yield $\%$	Inherent viscosity, dl./g. in solvent ^b	Molecular weight, number- average ^e	Color
ШЛ		Acetic acid DMF	0.100 0.017	$\frac{118}{152}$	18 18	54 75	0.11, S.A. 0.17, S.A.	2,300	Maroon Yellow
ΠΙΛ		DMF	0.079	50 100	18 6	86 88 88	0.10, S.A. 0.19, S.A.	1,030	Yellow Yellow
ÏX		DMA DMF«	0.0700	100	6 6–96	80 80- 87	0.26, S.A. 0.22-0.52, S.A.		Light tan Light tan
X		DMA	0.079	100	9	76	0.13, S.A.	4,700	Yellow
IX	IV-VI Copolymer	DMF	0.059	152	68	72	0.34, S.A.		Red-brown
ПХ		DMA	0.079	100	9	78	0.22, S.A.	2,850	Yellow
IIIX	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	DMA	0.079	100	9	09	0.49, S.A.	7,260	Light tan

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XIV		DMA	0.079	100	9	73	0.33, S.A.	5,700	5,700 Yellow	
XV		DMA	0.079	100	9	85	0.59, F.A.	40,000 White	White	
ΙΛΧ		DMF	0.079	100	9	67	0.08, S.A.	815	815 Yellow	
IIAX		I	1	I	I	66	0.06, S.A.		Yellow	
	COOH COOH									1

^a Equimolar concentrations of the monomers were used.

^b Measured at a concentration of 0.5 g, of polymer in 100 ml. of sulfuric acid (S.A.) or formic acid (F.A.) at 25°C. Inherent viscosities in formic acid are about 4 times as high as the inherent viscosities in sulfuric acid as determined with Polymer IV. The exact relationships is  $\log X = 1.78 \log y +$ 0.54; when X is  $\eta_{inh}$  in formic acid, and y ks  $\eta_{inh}$  in sulfuric acid.

* Based on bromine analysis, assuming one bromine atom per chain.

^d Reactions were carried out under nitrogen for 6, 24, 48, and 96 hr.

not reported by Mulvaney and Marvel, we investigated the effect of this temperature on the inherent viscosity of the polymer and, as shown in Table II, found that higher molecular weight products were obtained with an initial reaction temperature of 80-88 °C. than with an initial and sustained reaction temperature of 60 °C. Polymer IV was later prepared in acetone and in dimethylformamide at room temperature with inherent viscosities as high as those obtained in hot acetic acid. An experiment was made to determine the effect of reaction time on the inherent viscosity of polymer IV prepared in dimethylformamide at 30 °C. with a total monomer concentration of 0.21 mole/l. Samples taken at various times had the following inherent viscosities in formic acid: 3 hr., 1.07; 7 hr., 1.18; 11 hr., 1.24; 23 hr., 1.27; 30 hr., 1.17; 54 hr., 1.33; 120 hr., 1.18.

Polymers VI and VII were originally prepared by refluxing a dimethylformamide solution of the monomers overnight, but in later work different reaction times, temperatures, and solvents were investigated. The results showed that the inherent viscosities of polymer VI were apparently independent of reaction times (4.5–64 hr.) and reaction temperatures (28– 152°C.). Both polymers were obtained in hot acetic acid, and polymer VI was also obtained in acetone at room temperature and in dimethylacetamide at 100°C. Polymer VI having the highest inherent viscosity was obtained in dimethylacetamide.

Polymers II, III, and V were prepared by mixing acetic acid solutions of the monomers at 80°C. or above and stirring the mixtures overnight at 60°C. Each of these polymers was also prepared in hot dimethylformamide. Polymer I could not be prepared in hot acetic acid solution, but it was obtained in hot dimethylformamide and in acetone at room temperature.

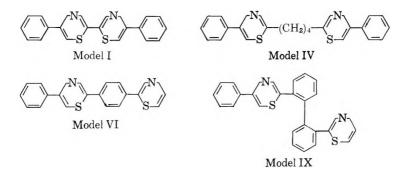
Polymer IX was prepared by heating a dimethylacetamide solution of the momomer (0.079 mole/l.) at 100°C. for 6 hr. The polymer was completely soluble in highly polar organic solvents and had an inherent viscosity in sulfuric acid of 0.26 dl./g. Increasing the monomer concentration to 0.79 mole/l. and carrying out the polymerizations under nitrogen for 6, 24, 48, and 96 hr. gave polymers that were only partially soluble in dimethylformamide. The soluble fractions constituted about 75% of the total weights of the polymers, and they had inherent viscosities in sulfuric acid in the range of 0.22–0.24 dl./g. The insoluble fractions had inherent viscosities in sulfuric acid in the range of 0.39–0.52 dl./g. Increasing the reaction time from 6 to 48 hr. tended to increase the yield of the insoluble fraction, but had no effect on its inherent viscosity.

Polymer XI was prepared by refluxing a dimethylformamide solution of the monomers overnight, and polymers VIII and XVI were prepared by heating a dimethylformamide solution of the monomers at 100°C. for 6 hr. Polymers X, XII, XIII, XIV, and XV were prepared by heating a dimethylacetamide solution of the monomers at 100°C. for 6 hr.

The methyl groups of polymer XVI were oxidized with refluxing aqueous alkaline permanganate solution to give a thiazole polymer containing carboxylic acid groups at the 5-positions of the thiazole rings (polymer XVII). Polymer XVII was prepared to determine the effects of the carboxyl group on the solubility of thiazole polymers.

The polymerization of dithioperfluorosuccinamide with p-bis(bromoacetyl)benzene was attempted in refluxing dimethylformamide, but the attempt was not successful. The thioamide apparently decomposed under the conditions of the experiment; and it appeared to be unstable, as indicated by a strong odor of hydrogen sulfide, even during storage under normal laboratory conditions.

Model compounds I, IV, VI, and IX were prepared for comparison with the structures and properties of polymers I, IV, VI, and IX, respectively.



The compounds were prepared by the condensation of  $\alpha$ -bromoacetophenone with the appropriate dithioamide. Model compounds IV and VI were prepared earlier by Mulvaney and Marvel.¹⁰ For comparison with the inherent viscosities of the polymers, the inherent viscosities of model compounds I, IV, VI, and IX in sulfuric acid were 0.03, 0.02, 0.03, and 0.02 dl./g., respectively, and the inherent viscosities of both model compounds IV and IX in formic acid were 0.05 dl./g.

### STRUCTURE OF POLYMERS

Correct clemental analyses of polymers IV, VI, and VII, and ultraviolet spectra of the polymers and model compounds were given by Mulvaney and Marvel as evidence for the structure of these polymers. Since the other thiazole polymers were prepared by the same general reaction as that used to prepare polymers IV, VI, and VII, their structures, as represented by the repeat units in Table II, are assumed. This assumption is substantiated by the presence of absorption bands characteristic of the thiazole ring in the infrared spectra of the polymers and by the fair agreement between calculated and observed elemental analyses, which are shown in Table III.

Additional evidence was obtained to establish the structure of polymers I, IV, VI, and IX by comparing the infrared spectra of the polymers with those of model compounds. The infrared spectrum of each polymer agreed in all significant details with the infrared spectrum of its model compound.

	Inherent viscosity,			Found				Calcı	Calculated	
Polymer	$solvent^{a}$	C, %	Н, %	N, %	S, %	Br, %	C, %	Η, %	N, %	S, %
I	0.21, S.A.	56.37	2.90	10.36	23.77	1.35	58.36	2.51	11.35	25.93
II	0.24, S.A.	58.51	3.40	9.88	24.0	1.19		3.15	10.77	24.62
III			3.64	9.36	22.65	0.22		3.73	10.34	23.62
IV		62.05	4.99	8.97	21.0	<0.10	64.34	4.73	9.38	21.43
A	1.78, F.A.	66.83	6.42	7.45	16.84	0.19	67.61	6.25	7.89	18.02
I.1		65.59	3.27	8.61	16.68	4.80	63.88	3.16	8.28	18.92
III		65.90	3.48	8.64	18.18	3.55	64.93	3.14	8.42	19.23
IIIA	0.10, S.A.	66.64	3.81	6.05	14.2	4.3	69.19	3.55	6.73	15.37
XI		70.42	3.95	7.31	14.7	<0.1	72.99	3.55	7.09	16.21
X		59.13	3.40	11.64	17.0	1.7	62.60	2.85	12.88	19.63
IX		57.78	4.04	7.86	15.6	0.32	1	!	ł	1
IIX		66.71	3.70	5.35	13.8	2.9	67.71	3.42	6.58	15.04
IIIX		68.67	3.78	6.02	14.4	1.1	69.28	3.43	6.73	15.39
VIX	0.33, S.A.	65.15	3.57	9.24	14.1	1.4	65.98	3.18	10.04	15.29
XV	0.59, F.A.	73.10	4.09	5.38	12.5	0.2	73.88	3.73	5.74	13.13
IVX	0.08, S.A.	63.19	4.21	5.81	15.0	8.3		3.97	7.26	16.58
IIVX	1	64.19	4.37	7.05	14.2	1.9	61.83	3.16	7.22	16.51

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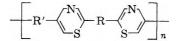
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TABLE III

### **PROPERTIES OF THE POLYMERS**

### **General Characteristics**

The character of the units between thiazole groups, which are represented by R and R' in the general formula,



was found to greatly affect the properties of the polymers.

In polymers in which R' was a 1,4-phenylene unit and R was 0-8 methylene units, the melting points and thermal stabilities of the polymers decreased and the solubilities and molecular weights of the polymers increased as the number of methylene units in R increased. Polymers having no methylene units were not fiber or film forming; polymers with two methylene units formed brittle fibers; and polymers with four or eight methylene units formed strong, flexible fibers. When R was also 1,4-phenylene, 1,3phenylene, 4,4'-biphenylene, or 2,6-pyridylene, the thermal stabilities of the polymers were generally much higher, but the solubilities and molecular weights were lower, and the polymers formed only brittle and fragile fibers However, when R was 2,2'-biphenylene, the properties of the and films. polymer were similar to those of the polymer containing four methylene units, except for solubility. The former polymer was soluble in organic solvents when its inherent viscosity in sulfuric acid was less than 0.39 dl./g. Polymers in which R and R' were both 1,4-phenylene units and the thiazole rings contained methyl or carboxyl at the 5-positions of the thiazole rings, had very low molecular weights, were not fiber- or film-forming, and were soluble only in strong acids. The thermal stability of the polymer containing methyl groups was high.

When R' was diphenylene ether and R was 1,4-phenylene, 1,3-phenylene, or 2,6-pyridylene, the molecular weights of the polymers were low. The polymers had high thermal stabilities, were soluble only in strong acids, and formed brittle, fragile fibers. However, when R was 2,2'-biphenylene, the polymer melted at about 250°C., was soluble in organic solvents, had a relatively high molecular weight, and formed strong, flexible fibers and films.

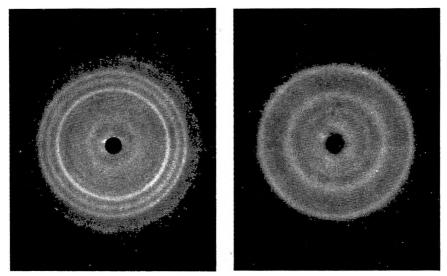
The properties of the polymers appeared to depend primarily upon the flexibility of the polymer chain backbone; greater flexibility is correlated with higher molecular weight, increased solubility, and lower melting point.

### Molecular Weight

As indicated by inherent viscosities, molecular weights by bromine endgroup analyses, and fiber- and film-forming abilities, the relative molecular weights of the polymers were as follows: polymers IV and V, very high; polymers III, IX, and XV, high; polymers XI, XIII, and XIV, medium; polymers I, II, VI, VII, VIII, X, and XII, low; polymers XVI and XVII, very low.

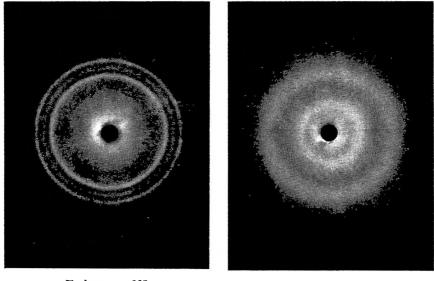
# Crystallinity

Each of the polymers had a detectible amount of crystallinity as indicated by birefringence. X-ray diffraction diagrams (Fig. 1) have also shown some crystallinity in polymers I, IV, VI, and IX. From the examination of several x-ray diagrams for each of these polymers, the order of increasing crystallinity was polymer IX, polymer I, polymer IV, and polymer VI.



Polymer I (a)





Polymer VI Polymer IX (c) (d)

Fig. 1. Powder x-ray diffraction diagrams of polymers: (a) I; (b) IV; (c) VI; (d) IX.

### **Thermal Properties**

The thermal properties in nitrogen of polymers I-XVI are summarized in Table IV, and those of the model compounds in Table V. The differential thermal analysis curves of polymers I, VI, VI, and IX and their model compounds are shown in Figure 2. The differential thermal analysis curves of all of the polymers, with the exception of polymers XVI and XVII, are shown in Figure 3. The differential thermal analyses were carried out in nitrogen at a heating rate of 10°C./min.

Polymers III, IV, V, IX, and XV-the polymers with the more flexible chains-melted in the range of 164-265°C., and, as indicated by differential

	Melting point	Decomposition tempera	ture, °C.	Weight
Polymer	by DTA, °C. ^a	Visual observation ^b	DTA®	loss, %
I	Noned	>500, discolored at 280	>500	4
II	None	>300, discolored at 200	>500	3
III	265	315	290	23
IV	250		487	0
V	164		493	2
VI	None	>500, discolored at 384	>500	3
VII	None	>500, discolored at 250	>500	1
VIII	None	>500, discolored at 340	>500	2
IX	240 - 250		>500	1
Х	None	>500, discolored at 200	>500	4
XI	240	>500, discolored at 275– 290	Partial at 290	
XII	None	>500, discolored at 245	>500	2
XIII	340	>500, discolored at 250	>340	2
XIV	None	>500, discolored at 250	>500	2
XV	220 - 240		>500	0
XVI		>500, discolored at 315		9

TABLE IV

^a Determined in nitrogen at a heating rate of 10°C./min. Calcined aluminum oxide was used as the reference material.

^b Determined by visual observation of sample in a capillary tube under nitrogen.

^c After heating in nitrogen at 250°C. for 24 hr.

^d Did not melt below 500°C.

Model compound	Melting point, °C.	Boiling point, °C.	Decomposition temperature, °C.
I	230	342	-
IV	85	<i>—</i>	315
VI	218	278	
IX	58	400	

TABLE V Thermal Properties of Model Compounds by DTA^a

^a Determined in nitrogen at a heating rate of 10°C./min. Calcined aluminum oxide was used as the reference material.

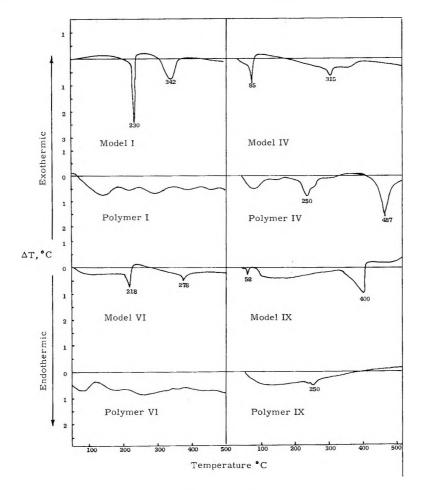


Fig. 2. Differential thermal analysis curves of polymers I, IV, VI, and IX, and their model compounds heated in nitrogen.

thermal analyses, polymer III decomposed at  $290^{\circ}$ C., polymers IV and V decomposed at  $487-490^{\circ}$ C., and polymers IX and XV did not decompose up to  $500^{\circ}$ C. The high decomposition temperatures of these polymers indicate that the molten polymers are stable over a wide temperature range. Polymer XIII melted at  $340^{\circ}$ C. and polymer XI partially melted at  $240^{\circ}$ C., both without apparent decomposition. The other polymers did not melt or decompose up to  $500^{\circ}$ C.

The melting and decomposition temperatures of the model compounds, which are summarized in Table IV, are in good agreement with those of the corresponding polymers. Model compounds IV and IX melted below 100°C., whereas the corresponding polymers melted at about 250°C.; and model compounds I and VI melted above 200°C., whereas the corresponding polymers did not melt below 500°C. Model compound IV was the only model compound that decomposed below its boiling point, and polymer IV was the only corresponding polymer that decomposed below 500°C.

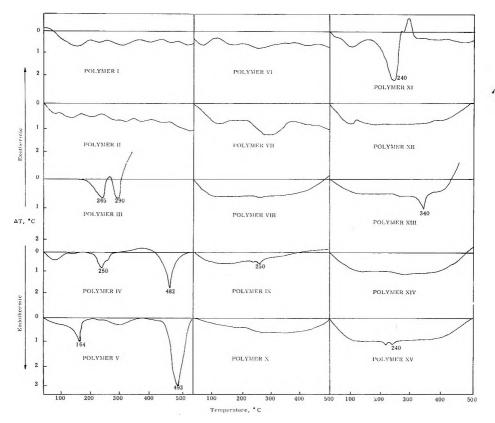


Fig. 3. Differential thermal analysis curves of polymers I-XV heated in nitrogen.

The weight losses of the polymers, with the exception of polymer XI, were determined after they were heated at  $250^{\circ}$ C. for 24 hr. in nitrogen. The results are shown in Table IV. Polymer III lost 23% in weight; polymer VI lost 9%; polymers I, II, V-X, and XII-XIV lost less than 5%; and polymers IV and XV lost no weight. When heated at  $250^{\circ}$ C. for 24 hr. in air, polymers IV, VI, and XV lost 15%, 3%, and 0% in weight, respectively. For comparison, Nylon HT-1 and Teflon (polytetrafluoroethylene) lost 0.0% and 1.8%, respectively, when heated under similar conditions.

The percentage weight losses of polymers I and VI, Nylon HT-1, and Teflon when they were heated in nitrogen from 400 to 600°C. in 50°C. steps are given in Figure 4. Each temperature was maintained for 1 hr. and changing from one temperature to another required about 5 min. Polymer I had greater thermal stability than Nylon HT-1 or polymer VI. Below about 500°C., Teflon had the best thermal stability; but above this temperature, Polymer I was somewhat better. The thermal stability of Polymer VI was the lowest of the group studied.

### Solubility

Table VI summarizes data obtained on the solubilities of the polythiazoles in some strong acids and highly polar solvents. The polythiazoles,

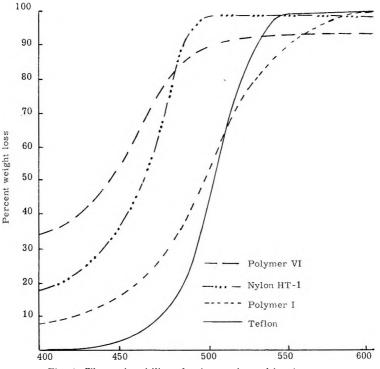


Fig. 4. Thermal stability of polymers heated in nitrogen.

with two exceptions, were found to be soluble only in strong acids. The exceptions were the polymers having a 2,2'-biphenylene group between thiazole rings, polymers IX and XV. These two polymers were also soluble in dimethylformamide, dimethylacetamide, and tetrahydrofuran. Polymer IX was insoluble in the organic solvents when its inherent viscosity in sulfuric acid was 0.39 dl./g. or greater.

The data in Table VI indicate that solubility of the polythiazoles is strongly dependent on the rigidity of the polymer chain. Replacing the 1,4-phenylene group (polymers X and XIV) did not appear to increase the polymer solubility, nor did the introduction of a methyl or carboxyl group in the 5-position of the thiazole ring (polymers XVI and XVII). Oxidation of some of the methyl groups of polymer XVI to carboxyl groups (polymer XVII) did not significantly change the solubility characteristics of the polymer, probably because of the low degree of conversion of methyl to carboxyl groups. The low carboxyl content of polymer XVII was shown by elemental analysis and by lack of solubility of the polymer in a 20-30%aqueous solution of sodium hydroxide.

The following additional data were obtained on the solubilities of polymers I–VII.

Polymers I-VII were soluble in hot or cold naphthalenesulfonic acid. Phosphoric acid dissolved polymers II-VII, but it did not dissolve polymer I. Polymers IV and V were the only ones in this series of polymers that were soluble in boiling concentrated hydrochloric acid.

				Solut	oilityª			
Polymer	Sulfuric acid	Ben- zene- sulfonic acid	Tri- fluoro- acetic acid	Formic acid	Di- methyl acet- amide	Di- methyl form- amide	Tetra- hydro- furan	Di- methyl sulfoxide
I	+	+	_	_	_	_	_	_
II		+	-	-	-	$\rightarrow$	-	-
III	+	+	+	+		_	_	_
IV	+	+	+	+	-	- ,	-	_
V	+	+	+	_	_	-0	_	_
VII	+	+	+	-	—	_	_	-
VIII	+	+	+	—	—	—	—	—
IXb	+	+	+	+	+	+	+	—
IX ^c	+	+	-	_	—	_	-	_
X	+	+	$\oplus$	_		-	-	
XI	+	+	+	$\oplus$	_	_	_	-
XII	+	+	$\oplus$	_	_	—	_	_
XIII	+-	+	$\oplus$	_	_	_	_	_
XIV	+	+	$\oplus$	_	_	-	_	_
$\mathbf{X}\mathbf{V}$	+	+	+	+	+	+	+	_
XVI	+	+	+	-	-	-	-	-
XVII	+	+	+	$\oplus$	-	_	_	_

TABLE VI

Solubilities of Thiazole Polymers in Strong Acids and Highly Polar Solvents^a

^a Code: + soluble;  $\oplus$  partially soluble; - insoluble.

^b  $\eta_{\text{inh}}$  in sulfuric acid of 0.22–0.26 dl./g.

^c  $\eta_{\text{inh}}$  in sulfuric acid of 0.39–0.52 dl./g.

Polymers III, IV, and V formed crystalline salts with sulfuric acid, benzenesulfonic acid, and naphthalenesulfonic acid that were slightly soluble (2-3%) by weight) in hot nitrobenzene, triethylene glycol, and *N*-methylpyrrolidone. The minimum temperatures for complete solution of the salts were: 75°C. for polymer V, 120°C. for polymer IV, and 150°C. for polymer III.

Polymers I, VI, and VII did not form crystalline sulfates, and the polymers wetted with sulfuric acid were not soluble in organic solvents. Solutions of polymers I and VI in sulfuric acid or benzenesulfonic acid could be diluted with nitrobenzene or *m*-cresol without precipitating the polymer, but only dilute solutions could be prepared in these mixed solvents.

Weak organic acids, such as acetic acid and benzoic acid, dissolved polymers I–VII. A few organic solvents, such as benzyl alcohol, triethanolamine, and *m*-cresol, dissolved very small amounts of polymers IV and V, but only at temperatures of about 200 °C. or above.

### **Fiber- and Film-Forming Properties**

The fiber- and film-forming properties of the polythiazoles having the highest inherent viscosities obtained are given in Table VII.

Evaluations of the fiber-forming properties of the polythiazoles were made by inserting a stainless-steel probe in a melt (melt spinning) or solution (dry spinning) of the polymer and withdrawing it slowly, and by ex-

	$\eta$ inh	F	ib <b>er</b> formation	l ^a	Film
Polymer	dl./g.b	Wet-spun	Melt-spun	Dry-spun	formation
I	0.21	No	No	No	No
II	0.24	No	No	No	No
III	0.87°	Yes (b, fr)	No	No	Yes (b, fr)
IV	3.96°	Yes (t, fl)	Yes (t, fl)	Yes (t, fl)	Yes (t, fl)
V	1.78°	Yes (t, e)	Yes (t, e)	Yes (t, e)	Yes (t, e)
VI	0.16	No	No	No	No
	0.27	Yes (b, fr)	No	No	Yes (b, fr)
VII	0.17	No	No	No	No
VIII	0.19	Yes (b, fr)	No	No	Yes (b, fr)
IX	0.26°	Yes (b, fr)	Yes (t, s)	Yes (t, s)	Yes (t, s)
Х	0.13	Yes (b, fr)	No	No	Yes (b, fr)
XI	0.34	Yes (b, fr)	No	No	Yes (b, fr)
XII	0.22	Yes (b, fr)	No	No	Yes (b, fr)
XIII	0.49	Yes (b, fr)	No	No	Yes (b, fr)
XIV	0.33	Yes (b, fr)	No	No	Yes (b, fr)
$\mathbf{X}\mathbf{V}$	0.59°	Yes (b, fr)	Yes (t, s)	Yes(t, s)	Yes (t, s)
XVI	0.08	No	No	No	No
XVII	0.06	No	No	No	No

TABLE VII Fiber- and Film-Forming Properties of Thiazole Polymers

* b, fr = brittle, fragile; t, e = tough, elastic; t, fl = tough, flexible; t, s = tough, stiff.

^b In sulfuric acid unless otherwise indicated.

° In formic acid.

truding a solution of the polymer from a hypodermic syringe beneath the surface of the liquid coagulant (wet spinning). The film-forming properties were determined by pouring a small amount of solution containing at least 10% of the polymer onto the surface of a pool of mercury in a flat-bottomed dish. The dish and its contents were heated on a water bath to evaporate the solvent, and the film that formed was removed from the surface of mercury with tweezers for examination of film properties. If a film was not formed by this method, a solution of the polymer was cast onto a steel sheet. The sheet was heated on a hot-plate to evaporate the solvent and to sinter the polymer, if possible, into a coherent film.

Tough fibers and films were obtained from polymers IV, V, IX, and XV. The fibers and films made from polymers IV, IX, and XV were stiff, and the fibers and films made from polymer V were rubbery. Fibers were formed from these four polymers by all three methods of spinning, but the fibers made from polymers IX and XV by melt and dry spinning were stronger than those made by wet spinning. Unless the inherent viscosities of polymers IV and V were greater than approximately 0.8 dl./g. in formic acid, the polymers formed brittle fibers. An inherent viscosity in formic acid greater than 2 dl./g. was required for obtaining good fiber-forming properties for Polymer IV. Polymers III, VI, VIII, and X-XIV could be spun into fibers only by wet spinning, and the fibers and films they produced were brittle and fragile. Polymers I, II, VII, and XVI could not be formed into fibers or films.

Fiber was made from Polymer IV having an inherent viscosity of 2.5 dl./g. in formic acid on laboratory continuous spinning equipment. The fibers were wet spun by extruding a 10% solution of the polymer dissolved in formic acid into a 30% aqueous formic acid coagulating bath. The fibers were drawn  $0.75\times$ , washed, dried, and taken up on a tube core. These fibers were approximately 6 den./filament and had a tenacity of approximately 1.5 g./den. and an elongation at break of 20%.

### CONCLUSIONS

The results of this research program have shown that thiazole polymers can be made that have merit for fibers and films in respect to strength and thermal stability, but entirely suitable polymers for use in heat-resistant fibers and films have not yet been made. The properties needed in a polythiazole for use in preparing heat-resistant fibers and films are solubility in organic solvents, very high melting point or infusibility, thermal stability, and high molecular weight. High molecular weight polymers have been prepared that are soluble in organic solvents and that form strong, tough fibers; but they melt below 250°C. Other polymers have been prepared that are infusible and thermally stable up to 500°C., but they have low molecular weights and are soluble only in strong acids.

From examination of the structures and properties of the thiazole polymers that have been prepared, the properties appear to depend primarily upon the flexibility of the polymer chain backbone—greater flexibility is correlated with higher molecular weight, improved fiber-forming ability, increased solubility, and lower melting point. On the basis of these observations, attempts are being made to prepare polymers having the desired properties for heat-resistant fibers and films by controlling the flexibility of the polymer chain backbone.

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### Résumé

On a polymérisé dix-sept thiazols par la polycondensation de bis- $\alpha$ -bromocétones avec des dithioamides; les polymères ont été étudiés pour la fabrication de fibres et de films, résistants à la chaleur. Avec quatre de ces polymères, on a obtenu des fibres et des films durs, et pourtant ces polymères ont un point de fusion bas (164-250°C). Tous les autres polymères, sauf un, n'entrent pas en fusion au-dessous de 500°C, ils ont une stabilité thermique excellente, mais ils n'ont pas de bonnes propriétés pour la formation de fibres et de films, à cause de leur faible poids moléculaire. Tous les polymères préparés possèdent une certaine cristallinité. Deux de ces polymères sont solubles dans les solvants organiques; les autres sont seulement solubles dans des acides forts. Des composés modèles ont été préparés pour quatre de ces polymères et leurs propriétés et structures comparées à celles des polymères.

### Zusammenfassung

Siebzehn Thiazolpolymere wurden durch Polykondensation von Bis- $\alpha$ -bromoketonen mit Dithioamiden dargestellt und die Polymeren auf ihre Fähigkeit zur Bildung hitzebeständiger Fasern und Filme untersucht. Feste Fasern und Filme wurden aus vier der Polymeren hergestellt; diese Polymeren besassen aber niedrige Schmelzpunkte (164– 250°C). Alle anderen untersuchten Polymeren mit Ausnahme eines schmolzen unterhalb 500°C und besassen eine ausgezeichnete thermische Beständigkeit, lieferten aber wegen ihrer niedrigen Molekulargewichte keine guten Faser- und Filmbildungseigenschaften. Alle dargestellten Polymeren besassen eine gewisse Kristallinität. Zwei Polymere waren in organischen Lösungsmitteln löslich; die anderen lösten sich nur in starken Säuren. Für vier der Polymeren wurden Modellverbindungen dargestellt und die Eigenschaften und Struktur dieser Verbindungen mit denjenigen der Polymeren verglichen,

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# Study of Swelling in Two New Ion Exchange Membranes

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### Synopsis

The synthesis of two new ion-exchange membranes is presented. These are a partially sulfonated polystyrene-divinylbenzene polymerized within a poly(vinylidene fluoride) matrix. Each of these systems allows control of ion exchange capacity and physical properties over a wide range. The second is especially useful, in that ion-exchange capacity and swelling characteristics may be controlled independently. It also has the distinct advantage of giving a clear, flexible film even with high crosslinking. On the basis of certain simplifying assumptions an equation is derived which permits approximate calculation from equilibrium water uptake data of an elastic constant which measures the resistance of the membrane to swelling forces. Equilibrium water content data for the two membrane systems are treated with this equation and analyzed in terms of internal structure.

In many applications of ion-exchange membranes it is desirable to have a high ion-exchange capacity and fully dissociated ionic groups in membranes of good dimensional stability and strength. These characteristics are to a certain extent mutually exclusive, in that a high ion-exchange capacity gives rise to high swelling pressure and high equilibrium water uptake, with resultant deterioration of physical properties. It is the task of the polymer chemist, therefore, to achieve the optimum balance for his specific purpose through control of the ion-exchange capacity and/or of the resistance of the resin matrix to swelling forces.

The work that follows gives examples in which these objectives are at least partially realized. It is divided into two parts. The first section describes the synthesis and general characterization of two new ion-exchange membrane systems based on polystyrenesulfonic acid. The second section presents a study of the swelling characteristics of these two membranes in relation to their internal structures.

# SYNTHESIS AND CHARACTERIZATION OF MEMBRANES

### Case I: Partially Sulfonated Polystyrenesulfonic Acid

Following is a sulfonation procedure through which one may control accurately over a wide range the ion-exchange capacity of the resulting waterinsoluble polystyrenesulfonic acid resin. In a typical preparation, 60 g. of polystyrene (Lustrex HH 77, M.W. = 40,000 NA) was dissolved in 1200 ml. of ethanol-stabilized chloroform (0.31% EtOH) in a two-liter resin kettle equipped with a stirrer and addition funnel. A solution of 42 g. of  $99 \pm \%$  iron-free chlorosulfonic acid in 150 ml. chloroform was added dropwise with stirring over a 2-hr. period at room temperature. The partially sulfonated polystyrenesulfonic acid precipitated from the chloroform solution. Stirring was continued for an additional half hour. The liquid was decanted and the sulfonated polystyrene taken up in 1000 ml. methanol. The polymer was spray-dried from this solution to give a white powder which was washed to water neutrality in a filter press and dried at 50°C. for three days.

The polystyrenesulfonic acid prepared by the above procedure has an ion-exchange capacity of  $1.80 \pm 0.05$  meg. H⁺/g. dry resin. Other ion-exchange capacities may be obtained merely by adjusting the quantity of chlorosulfonic acid added to the reaction mixture. At ion-exchange capacities greater than 3 meq. H⁺/g. dry resin, the polymer becomes water-soluble and methanol-insoluble. The resin may be compression-molded in the acid form into an ion-exchange membrane at its glass transition temperature of 161°C. These films are flexible and fairly strong when wet, but become brittle when completely dry.

# Case II: Interpolymer of Crosslinked Polystyrene–Divinylbenzenesulfonic Acids within an Inert Matrix

Sheets of clear poly(vinylidene fluoride) film, usually about 0.2 cm. in thickness, were equilibrated in acetone at  $35^{\circ}$ C. for 24 hr. The swollen films were then quickly immersed in a bath consisting of monostyrene, divinylbenzene, and a 50/50 mixture of benzoyl peroxide and dicumyl peroxide in a concentration of 0.1% based on monostyrene. The bath should be large in order to favor effective displacement of the acetone in the films by the monomer-peroxide mixture. After removal from this bath, the membranes were placed between interleaves of stiff aluminum foil and heated to  $150^{\circ}$ C. in a flat bed press for 51 min. at 2000 psi. This process was repeated until the membrane weight increased 15–20% over that of the original film. This gives a compatible interpolymer mixture of crosslinked polystyrene-divinylbenzene with poly(vinylidene fluoride).

These films were then sulfonated by immersion in a chloroform solution of 15% chlorosulfonic acid for a period of 24 hr. This was followed by a washing in distilled water and hydrolysis for 37 hr. in distilled water at  $65^{\circ}$ C.

A clear transparent membrane is obtained which contains one sulfonic acid group for each aromatic ring. The films are flexible, even when dry, and have excellent physical properties. As will be discussed below, the equilibrium swelling in water can be controlled by adjusting the concentration of divinylbenzene in the monomer bath.

In order to confirm that this is in fact an interpolymer system and not a free radical graft of styrene to the poly(vinylidene fluoride), the following experiments were performed. Several membrane samples were placed under a sun lamp for several days. This degraded the polyelectrolyte to such an extent that it could be leached from the membrane with distilled water. The solids obtained after evaporation of the extract water corresponded to 98.5% of the polystyrenesulfonic acid present in the membrane. The elemental analysis of these solids gave C, 52.43%; H, 4.25%; S, 16.85%; F, 0.1%; double bonds, 7.0%, which corresponds very closely to pure polystyrenesulfonic acid.

The components of the system were also separated in another way. Membrane samples were heated in a bath composed of equal weights of acetone and dimethylacetamide at  $50^{\circ}$ C. for three days. Decanting the solvent from the jellylike mass remaining and evaporating it down to dryness left a white powder which proved to be essentially pure poly(vinylidene fluoride). Analysis of the dried jelly showed it to be crosslinked polysty-renesulfonic acid. Since there can be no chemical degradation involved here, this confirms the interpolymer nature of the membrane.

	Divinylbenzene, % based on styrene	Transverse resistivity, ohm-cm. (H ⁺ form, 1000 cycles a.c.)
29.8% Polystyrene-divinylbenzenesulfonic acid	0.0	15.0
70.2% poly(vinylidene fluoride)	3.0	18.4
	4.5	22.0
	7.0	29.2
	9.0	31.8
	12.0	40.0
23.0% Polystyrene-divinylbenzenesulfonic acid	0.0	16.7
77.0% poly(vinylidene fluoride)	3.0	26.5
	4.5	34.3

TABLE I

Without the sunlamp treatment, the interpolymer membrane containing no divinylbenzene crosslinks yielded no leachable polystyrenesulfonic acid, even when boiled for two weeks in water. This is in spite of the fact that, being fully sulfonated, it should be completely water-soluble. This undoubtedly is due to extensive chain entanglement and is an example of the well described "snake cage" effect in mixed bulk polymerizations.

In a mixture as we have here of a polyelectrolyte imbedded in nonpolar matrix, there is always the danger of discontinuity in the polyelectrolyte phase, thus rendering the material a poor ion exchanger and a poor electrical conductor due to absence of pathways between ionic sites. Such discontinuity is not important in the membrane described above as is apparent from the transverse resistivity data shown in Table I. These data were obtained at room temperature with fully hydrated membranes. The resistivities are not excessively high and are about what one would expect taking into account only the volume fraction of the conducting material.

### R. B. HODGDON, JR. AND J. R. BOYACK

### SWELLING CHARACTERISTICS

Crosslinked polyelectrolytes in aqueous media imbibe water and swell until the water activity is the same in both the gel and the liquid phases. Crosslinked, fully sulfonated polystyrene-divinylbenzenesulfonic acid has received the bulk of swelling studies over the last twenty years due to its extensive use in the field of ion exchange and due to the excellent chemical stability and ease of fabrication of these materials. References 1–12 give a selection from the work done in this field and Helfferich's book¹³ gives a good review of the subject.

Briefly, the relationships emerging from these studies are that swelling is enhanced by high "free ion" content of the resin, large and strongly hydrated counterions, and low valence of the counterions, whereas swelling is suppressed by high electrolyte concentration in the equilibrating solution and by increased crosslinking in the resin.

Swelling data are reported below for the two ion exchange membranes described above in equilibrium with pure water.

### Theory

The swelling of an ion-exchange resin is most easily visualized on the basis of a model proposed by Gregor.¹⁴ This model conceives of the gel phase as being analogous to a compartment whose walls are moveable, but attached to each other by elastic springs, and which contains an electrolyte solution whose concentration is equal to that of the pore liquid in the actual resin. This compartment is conceived to be separated from the external water by a semipermeable barrier which is impermeable to the ions associated with the resin. Thus, if water were to enter the compartment as a result of osmotic forces, the compartment would expand until the contractile force of the springs became equal to the osmotic pressure of the internal solution. Using this model, the free energy change,  $\Delta G$ , associated with swelling consists of two parts, one arising from the mixing of the water with the internal electrolyte, and another arising from the potential energy stored in the elastic polymer network. The change in free energy is a minimum at equilibrium, so that

$$(\partial \Delta G / \partial n_w)_{\text{mixing}} + (\partial \Delta G / \partial n_w)_{\text{elastic}} = 0 \tag{1}$$

where  $n_w$  signifies the number of moles of water in the gel phase. To a first approximation we may consider the polymer network to have the nature of Hookian springs in three dimensions, giving

$$\Delta G_{\text{elastic}} = \frac{1}{2} K' (\Delta V)^2 \tag{2}$$

where K' is a proportionality constant and  $\Delta V$  the change in volume on swelling. Taking the derivative of eq. (2) yields

$$(\partial \Delta G / \partial n_w)_{\text{elastic}} = K' \Delta V \bar{V}_w \tag{3}$$

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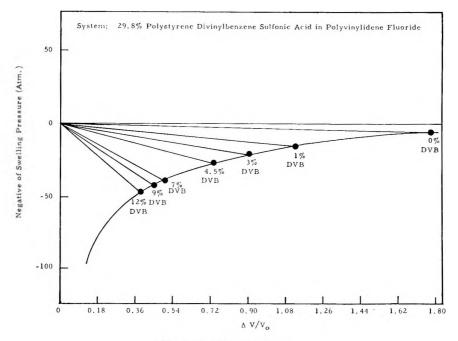


Fig. 1. Swelling equilibrium.

where  $\overline{V}_{w}$  is the molar volume of water. Equation (3) can be written since absorbed water adds very nearly its own volume to the swollen system. This has been experimentally confirmed to within experimental error for the two membranes under consideration in this paper.

In order to evaluate the first term in eq. (1), we make the assumption of ideal behavior, which will be modified later. This gives

$$\Delta G_{\text{mixing}} = n_w R T \ln x_w + n_p R T \ln x_r \tag{4}$$

In eq.  $(4)x_w$  is the mole fraction of water and  $x_r$  that of the resin, which is taken to be entirely made up of the contribution of the counter ions. Differentiating eq. (4) gives

$$(\partial \Delta G / \partial n_w)_{\text{mixing}} = RT \ln x_w \tag{5}$$

Combining eqs. (4) and (5) and dividing through by  $\bar{V}_w$  results in

$$K\Delta V/V_0 = -(RT/\bar{V}_w) \ln x_w \tag{6}$$

In eq. (6) K' has been replaced by  $K/V_0$ ,  $V_0$  being the dry resin volume. Equation (6) is illustrated in Figure 1 for the data of Table III. The straight lines are plots of the left-hand side for various degrees of crosslinking, while the curved line is a plot of the right hand side. The left-hand side of eq. (6) expresses the elastic force which counterbalances the osmotic swelling pressure given by the right-hand side. The constant K is an intrinsic constant of the polymer network whose value represents the resistance of the network to swelling forces and can be correlated with internal structure.

# **Results and Discussion**

The elastic constant K could be evaluated without resort to the assumption necessary to obtain eq. (5) if the swelling pressure could be measured directly. This has been done^{9,12} with other systems by comparing the resin of interest isopiestically with a reference resin of the same composition but having a very small amount of crosslinking so that its swelling pressure may be taken as zero. With the membranes under consideration here, this approach is impossible because of the lack of any suitable reference system. In the one case no chemical crosslinking is present to begin with, and in the other the swelling pressure is not zero even with no crosslinking in the polyelectrolyte because of the effect of the inert matrix. We shall, therefore, use eq. (6) to evaluate K from the observed equilibrium swelling by estimating a reasonable value for the counter ion concentration in the pore liquid and, from this, calculating  $x_{w}$ .

In attempting to estimate the counterion concentration, one must take into account the ion binding which occurs in all polyelectrolyte systems. Ion binding in water-soluble polyelectrolytes is independent of molecular weight and of concentration, the most important factor being the linear charge density on the polymer chain. Free ion fractions of 0.1–0.5 have been found^{15–21} for soluble strong polyelectrolytes with high charge densitics. Mock and Marshall¹⁹ found 38% dissociation for fully sulfonated polystyrenesulfonic acid. There have been few studies of ion binding in ion exchange resins. Harris and Rice²⁰ have applied their theory of polyelectrolytes to ion-exchange resins and have calculated ion binding for model resins. For a resin which swells in water at equilibrium to 150% of

Ion-exchange capacity, meq./g. dry	Temp. °K.	• T7 / T7	К,
resin	· <b>N</b> .	$\Delta V/V_0$	atm.
1.65	291	0.35	119
1.65	301	0.38	106
1.65	311	0.42	95
1.65	321	0.46	73
1.80	301	1.09	14
1.80	311	1.32	9.6
1.80	321	1.43	8.1
1.80	331	1.57	7.6
2.15	301	1.87	6.0
2.15	311	1.91	5.2
2.15	316	2.10	4.8
2.15	331	3.12	2.4

TABLE II

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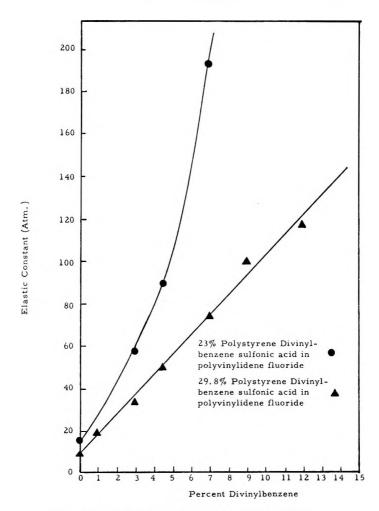


Fig. 2. Variation of elastic constant with crosslinking.

its original volume, they arrive at a counterion dissociation of close to 40%. In treating our data, we shall assume that the free ion fraction is 35% in all the membranes and that this fraction of the counterions forms an ideal solution in the pore liquid of the membrane. Because of the uncertainty of these assumptions, our results are only semiquantitative. However, they still allow interesting correlations to be made.

Table II gives the results obtained at various temperatures with three examples of the partially sulfonated polystyrene-divinylbenzenesulfonic acid membrane of case I. Table III along with Figure 2 presents the data for interpolymer membranes of case II. The  $\Delta V/V_0$  values were determined by measuring the water uptake in distilled water at a controlled temperature. In the case I membrane the value of the elastic constant must depend on a pseudo-crosslinking arising from coherence of hydrophobic hydrocarbon sections of the polymer chains and chain entanglement. It is apparent from Table II that, for this membrane at constant temperature, a small increase in ion-exchange capacity drastically lowers the value of the elastic constant. The reason for this effect is linked to the greater probability of coherence between hydrocarbon sections of the chains in membranes with lower ion exchange capacities. This factor, however, probably does not account for all of the large change in the elastic constant found in going from 1.65 meq.  $H^+/g$ .

The percentage of sulfonation is 18, 20, and 25% for the ion exchange capacities 1.65, 1.80, and 2.15 meq. H⁺/g., respectively. The small difference in sulfonation between the first two membranes does not seem to justify the large variation observed in the elastic constant. One can consider other factors to explain the magnitude of this change, the most important,

TABLE IIIElastic Constants for Interpolymer Membranes as a Function of Divinylbenzene Con-<br/>tent,  $T = 296^{\circ} K$ .

Di	Divinylbenzene, %		
System	based on styrene	$\Delta V/V_{0}$	K, atm.
23.0% Polystyrene-divinylbenzene,	0.0	1 02	15.2
77.0% poly(vinylidene fluoride);	3.0	0 58	57.9
ion-exchange capacity $= 1.25$	4.5	0.40	89.3
meq./g.	7.0	0.29	193
	9.0	0.17	390
29.8% Polystyrene-divinylbenzene-	0.0	1.70	9.3
sulfonic acid, 70.2% poly(vir.yli-	1.0	1, 15	18.9
dene fluoride); ion-exchange ca-	3.0	0 85	32.8
pacity = $1.62 \text{ meq./g.}$	4.5	0 69	49.4
	7.0	0 51	73.3
	9.0	0.44	99.
	12.0	0 39	117

perhaps, being chain entanglement. This characteristic would be expected to have a marked dependence on the history of the membrane. For instance, in a membrane soaked in water the restrictions due to chain entanglement would gradually diminish as the chains rearrange themselves by segmental notion to relieve strain. The experimentally determined Kvalues would then diminish gradually with time.

Increasing temperature decreases the value of the elastic constants shown in Table II. Two effects are operative here. The elasticity of the individual polymer chains increases with increasing temperature as does also the water solubility of the hydrocarbon chain segments, thus reducing the effective pseudo-crosslinking.

From Figure 2 we see that for no crosslinking, both interpolymer membranes still exhibit an appreciable elastic constant, the value of which is about the same for the two different compositions. The poly(vinylidene fluoride) itself is not crosslinked, but its hydrophobic character together with the presence of crystalline regions acts to introduce effective "pseudo" crosslinks.

If sufficient polyelectrolyte is present in the interpolymer membrane, the dependence of the elastic constant on divinylbenzene content is linear, as in the lower curve in Figure 2. If one considers the polyelectrolyte network alone, it is apparent that this network is initially already swollen by the inert matrix polymer. It is conceivable that, for small amounts of polyelectrolyte with high crosslinking, a situation may occur in which areas of the polyelectrolyte network reach a saturation condition of nearly full extension. This would greatly increase the resistance to further swelling. The upward curvature of the top curve in Figure 2 suggests that this may be the case for the membrane containing the smaller amount of polyelectrolyte.

### CONCLUSION

We have discussed here two ion-exchange membrane systems which offer the possibility of controlling their physical and exchange properties over a wide range. For the case I membrane this control is effected by changing the ion exchange capacity. The higher exchange capacities lead to low resistance to swelling and high equilibrium water content, which may be disadvantageous for some applications. The case II interpolymer membrane system is particularly attractive, in that it allows independent control within wide limits of the ion exchange capacity, through variation of the amount of polyelectrolyte incorporated, and of the resistance to swelling forces, through variation of the divinylbenzene content. The presence of the poly(vinylidene fluoride) matrix also insures a flexible, strong membrane, even with high crosslinking.

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### Résumé

On présente la synthèse de deux nouvelles membranes échangeuses d'ions. Elles sont formées d'une résine d'acide polystyrène sulfonique partiellemnt sulfonée et d'un système interpolymérique, composé de polystyrène-divinylbenzène sulfoné, polymérisé dans une matrice de fluorure de polyvinylidène. Chacun de ces systèmes permet le contrôle de la capacité d'échange et des propriétés physiques dans un large domaine. Le second est spécialement utile par le fait que la capacité d'échange d'ions et les caractéristiques de gonfiement peuvent être contrôlées indépendamment. Il possède également l'avantage de donner un film clair et flexible, même lorsqu'il est fortement ponté. Sur la base de certaines suppositions permettant de faire des simplifications, on a déduit une équation, qui permet de faire des calculs approximatifs d'une constante d'élasticité à partir des résultats de l'absorption d'eau à l'équilibre, et qui permet de mesurer la résistance de la membrane aux forces de gonfiement. Les résultats concernant la teneur en eau à l'équilibre de ces deux membranes sont traités au moyen de cette équation et analysés en vue d'obtenir la structure interne.

### Zusammenfassung

Die Synthese zweier neuer Ionenaustauschmembranen wird angegeben. Es sind dies ein partiell sulfoniertes Polystyrolsulfonsäureharz und ein Interpolymersystem, bestehend aus in einer Polyvinylidenfluoridmatrix polymerisiertem sulfoniertem Polystyrol-Divinylbenzol. Jedes dieser Systeme erlaubt eine Kontrolle der Ionenaustauscherkapazität und der physikalischen Eigenschaften in einem weiten Bereich. Das zweite ist besonders interessant, da die Ionenaustauscherkapazität und Quellungscharakterisitik unabhängig voneinander eingestellt werden können. Es besitzt auch den entschiedenen Vorteil, dass es sogar bei hoher Vernetzung einen klaren, flexiblen Film liefert. Unter gewissen vereinfachenden Annahmen wird eine Gleichung abgeleitet, welche die angenäherte Berechnung einer elastischen Konstanten als Mass für den Widerstand der Membranen gegen Quellungskräfte aus der Gleichgewichts-Wasseraufnahme gestattet. Daten für den Gleichgewichts-Wassergehalt der beiden Membransysteme werden mit dieser Gleichung behandelt und anhand der inneren Struktur analysiert.

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# Effect of Temperature on Ozone Cracking of Rubbers

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### **Synopsis**

The rates of growth of single ozone cracks have been measured for vulcanizates of a series of butadiene-styrene copolymers, over a temperature range from  $-5^{\circ}$ C. to  $95^{\circ}$ C. The rates appear to be determined by two mechanisms. At low temperatures, near the glass transition temperature, they are quantitatively related to the segmental mobility of the polymer. The principal rate-controlling step in this case is concluded to be movement of the polymer chains after scission to yield new surface. At high temperatures the rate approaches a limiting value of  $10^{-3}$  cm./sec./mg. of ozone/l. This is about 1/1000 of the maximum possible value when instantaneous reaction of one incident ozone molecule causes scission of one network chain.

## **INTRODUCTION**

In an earlier communication¹ it was noted that the rate of growth of ozone cracks increased markedly with temperature, for rubbers of relatively low segmental mobility. It was concluded that the segmental mobility governs the rate of crack growth in these cases. In accordance with this concept, the rates were increased when a plasticizer was included in the mix formulation, and the rates for different rubbers were in the order of their expected segmental mobilities, with two exceptions: polychloroprene, for which a lower degree of reactivity with ozone was assumed, and relatively mobile rubbers, such as natural rubber, for which the rate was virtually unaffected by temperature changes or plasticization. It seemed probable that reaction with ozone had become the rate-determining step in the latter case, so that further increases in segmental mobility were without effect.^{1,2}

A quantitative study has now been carried out, and is described below, of the effect of segmental mobility on the rate of growth of single ozone cracks. In order to vary the mobility over a wide range without altering the specific chemical reaction leading to molecular scission, a series of butadiene-styrene copolymers, containing 0-80% styrene, was examined over a wide temperature range, from  $-5^{\circ}$ C. to  $95^{\circ}$ C.

### **EXPERIMENTAL DETAILS**

### Materials

The butadiene-styrene copolymers were prepared by emulsion polymerization at  $50^{\circ}$ C. The polybutadiene sample (Budene, 94% cis-1,4)

Mix Formulations and Vulcanization	Conditions	$\mathbf{Employed}$	to Pr	epare Test	Sheets
	Α	В	С	D	E
cis-Polybutadiene	100				
75/25 Butadiene/styrene copolymer		100			—
44/56 Butadiene/styrene copolymer			100		
33/67 Butadiene/styrene copolymer				100	
20/80 Butadiene/styrene copolymer					100
Zinc oxide	5	5	5	5	5
Stearic acid	<b>2</b>	2	3	3	2
Sulfur	1	1	<b>2</b>	2	2
Benzothiazyl 2-cyclohexyl sulfen-					
amide (CBS)	0.7	0.7	1.5	1.5	1.5
Vulcanization time, min. at 145°C.	90	90	90	90	90

TABLE I	
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was obtained from The Goodyear Tire and Rubber Company. Each polymer was compounded and vulcanized as described in Table I to yield thin vulcanized sheets. The sheets were extracted with hot acetone to remove antioxidants, by-products of the vulcanization reaction, etc. Test pieces in the form of parallel-sided strips were then cut from them.

## **Glass Transition Temperatures**

The glass transition temperatures  $T_g$  were estimated for each material from Gehman low temperature torsion flex measurements,³ by means of Trick's procedure.⁴ The values obtained are given in Table II. For materials B, C, D, and E values were also calculated from Wood's relationship⁵ for emulsion copolymers prepared at 50°C.:

	Glass Transition Temperatures	
Material	Styrene content, $(\%$ by weight)	T _g , °C.
A	0	-110
В	25	-57
$\mathbf{C}$	56	-13
D	67	+10
$\mathbf{E}$	80	+38

$T_{a}$ (	(°C.)	= (·	-85	+	135S)/	/(1	-0.5S	)
19	U.)	= ( -	- 60	+	1000)/	Υ <b>L</b>	-0.50	2

where S is the weight fraction of styrene in the copolymer. These values were found to be closely similar to those given in Table II.

#### **Test Piece**

Each test piece was about 5 cm. long, 0.6 cm. wide, and 0.03 cm. thick. A sharp cut about 0.05 cm. long was made through the central region as

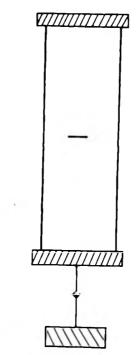


Fig. 1. Crack growth test piece.

shown in Figure 1. A weight of about 8 g. was applied to the lower end of the test piece yielding a tensile stress of about 0.45 kg./cm.², an extension of about 3%, and a value for the potential energy T available for cut growth by unit area⁶ of about 650 erg/cm.². This value is considerably larger than the minimum necessary for ozone crack growth to occur in unprotected rubbers,⁶ about 100 erg/cm.². It is too small, however, to induce tearing. No cut growth occurred in the absence of ozone, and the growing cut came to a halt if the ozone supply was stopped. It has previously been shown that the rate of growth of a single ozone crack is independent of the applied stress provided this is (1) above the minimum value, and, (2) not so large that tearing occurs.¹ The present stress values lie within this range.

The test piece was suspended from the roof of a glass test chamber immersed in a water bath held at the required temperature. Growth of the cut when an ozonized oxygen gas stream was passed through the test chamber was observed by means of a low power microscope with a calibrated eyepiece scale.

#### **Ozone Supply**

A stream of ozonized oxygen was obtained as before¹ by passing cylinder oxygen through a drying tower and then around a quartz mercury-vapor lamp (Hanovia lamp, No. 84A-1). The gas stream passed through a glass coil immersed in the bath to attain the bath temperature, and then through the test chamber to a collecting flask, for analysis of ozone by Wadelin's method.⁷ The rate of gas flow was 20 l./hr., corresponding to about three changes of the test atmosphere per minute. The ozone concentration was generally  $3.0 \pm 0.2$  mg./l.

## EXPERIMENTAL RESULTS AND DISCUSSION

## **Rate of Crack Growth**

The cut was found to grow equally at both ends, and linearly with time. The rate R of crack growth has therefore been taken as the velocity of one tip, i.e., one-half of the rate of growth of the whole cut.

The measured rates for the five materials examined are plotted in Figure 2 against the test temperature. They are seen to form a series of parallel relations displaced to higher temperatures with increasing styrene contents of the copolymers. The general parallelism resembles that shown by the viscous response of polymers having different glass transition temperatures. The measured rates were accordingly replotted against the interval  $T - T_{\varphi}$  by which the test temperature exceeded the glass transition temperature (Fig. 3). In this representation the results for all the materials were found to lie on a single curve over the entire temperature range, for rates which varied 3000-fold.

The variation with temperature of the segmental jump frequency  $\phi$  is given for amorphous polymers by the Williams, Landel, and Ferry relation⁸

$$\ln(\phi_T/\phi_{T_g}) = 40(T - T_g)/(52 + T - T_g)$$
(1)

to a first approximation, where  $\phi_{T_0}$ , the jump frequency at the glass temperature, is about  $10^{-1}$ /sec.^{9a} This relation is plotted as a broken curve

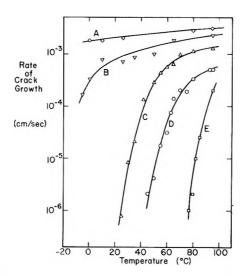


Fig. 2. Experimental relations between the rate of crack growth and temperature.

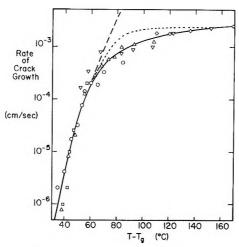


Fig. 3. Relation between the rate of crack growth and  $T - T_{o}$ . The materials are represented by the same symbols as in Figure 2. The broken curve is of the form given in eq. (1), adjusted vertically to coincide with the experimental results at low temperatures. The dotted curve is of the form given in eq. (4).

in Figure 3, with the vertical position chosen to coincide with the experimental results at low temperatures. Over a 30°C, temperature range, corresponding to a 500-fold range of crack growth rate, it is seen to describe the experimental results satisfactorily. At temperatures more than 60°C, above  $T_g$ , however, the measured rates depart from this temperature dependence and approach a limiting value of about  $3 \times 10^{-3}$  cm./sec.

It thus appears that the rate of growth of ozone cracks at low temperatures is determined by the segmental mobility, whereas at higher temperatures it approaches a constant value. These two features are discussed separately below.

#### **Temperatures near** $T_{g}$

One possible mechanism for the observed temperature dependence is the slow diffusion of ozone through a partially-degraded surface layer to reach the effective crack tip. As the rate of diffusion of gases is proportional to the segmental mobility of the polymer molecules, the rate of crack growth would depend on temperature in the observed way. Another possible mechanism is the slow rearrangement of molecular positions to yield new surfaces after ozonolytic scission. The retardation time  $\tau_1$  for a single chain is directly related to the jump frequency  $\phi^{\text{9b}}$ :

$$\tau_1 = 2N^2 a^2 / \pi^2 \delta^2 \phi, \qquad (2)$$

where N is the number of "independent" segments comprising the chain, a is the segment length, and  $\delta$  is the jump distance for a segment. The rate of crack growth would therefore vary with temperature in the observed way if slow movement of the rubber molecules in and near the surface were the rate-controlling step. There are two reasons for considering the second mechanism more important, if not dominant. They are: the observed rates are in fairly good quantitative agreement with those calculated from chain response times (below), and the rate of crack growth is not simply proportional to the concentration of ozone (below), as would be expected for a diffusion-controlled process.^{10a}

A third, more complex, rate-controlling mechanism might be considered in which both slow diffusion and simultaneous chemical reaction occur. However, except in the unlikely case that the (assumed first-order) rate constant governing the reaction varies with temperature in the same way as the coefficient of diffusion, the rate of crack growth would not depend on temperature in accordance with eq. (1), as is observed. Also, the rate would again be expected to be proportional to the ozone concentration,^{10b} contrary to experiment.

**Calculated Chain Response Times.** The coincidence of the relation for  $\phi_T$  given in eq. (1) with the experimental results of Figure 3 was achieved by employing the scaling factor

$$R_{\tau} = (1.2 \times 10^{-12} \,\mathrm{cm.})\phi_{\tau} \tag{3}$$

The fundamental retardation time  $\tau_1$  for a single chain may be calculated in terms of  $\phi$  by means of eq. (2). We take as reasonable values; N = 100, a = 10 A.,  $\delta = 2$  A. Hence,

$$au_1 = 5 \times 10^4/\phi$$

Substituting in eq. (3) we obtain

$$R_T = (6 \times 10^{-8} \text{ cm.}) / \tau_{1T}$$

This result seems quite reasonable. The bracketed quantity represents the amount by which the cut is found to advance within the response time of a single chain; in accordance with this concept it is of molecular dimensions.

A check on the validity of the absolute values of  $\phi$  and hence  $\tau_1$  is afforded by comparing the value obtained for  $\tau_1$  from eq. (2) with that obtained from creep or dynamic measurements. At a temperature of  $T_{\sigma}$  + 50°C.,  $\phi$  is calculated to be  $3 \times 10^7$ /sec. from eq. (1). On substituting in eq. (2), a value for  $\tau_1$  is obtained of  $1.7 \times 10^{-3}$  sec. This is in good agreement with the value of about  $6 \times 10^{-3}$  sec. deduced from the maximum in the retardation time spectrum reported by Bueche,^{9°} when reduced to the same temperature.

Effect of Ozone Concentration. Measurements were made of the rate of cut growth at 40°C for materials A and C, using various concentrations of ozone. The results are plotted on logarithmic scales in Figure 4. A direct proportionality would be shown by a linear relationship with a slope of unity. This is found to be the case for material A, in accordance with previous work.¹ For material C the dependence on ozone concentration is much smaller, the slope being only about 0.2. Moreover the test tem-

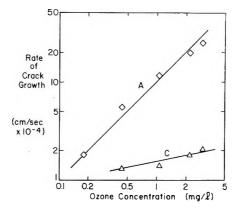


Fig. 4. Relations between the rate of crack growth at 40 °C. and the concentration of ozone for materials A  $(T - T_g = 150 ^{\circ}\text{C.})$  and C  $(T - T_g = 53 ^{\circ}\text{C.})$ .

perature of 40°C., i.e., 53°C. above  $T_{g}$  for material C, is rather high to be considered characteristic of the low temperature region, since departures from eq. (1) are evident above about  $T_{g} + 60$ °C. (Fig. 3). It seems likely that the dependence on ozone concentration at lower temperatures would be still smaller.

If delayed molecular motion is the rate-controlling step at low temperatures, the rate of cut growth would be expected to be independent of the ozone concentration. The small dependence observed suggests that this mechanism is correct.

# **Rate of Crack Growth at High Temperatures**

The dependence of the rate of crack growth upon temperature at high temperatures is seen to be quite small (Fig. 3). An apparent energy of activation was calculated for material A, using the measured rates over the temperature range 0-100°C., corresponding to the range  $T_{g} + 110$ °C. to  $T_{g} + 210$ °C. The value obtained was 1.4 kcal./mole, decreasing to 1 kcal./mole when allowance was made for the increase of collision frequency with temperature. Even this low value probably contains a residual contribution from the viscous mechanism dominant at low temperatures. It appears, therefore, that the scission process does not require significant amounts of thermal energy.

In order to make a quantitative comparison with the experimentally observed rates of crack growth, we consider an ideal process in which the mere collision of a suitably oriented ozone molecule with a butadiene unit results in chain scission, no activation energy being required for reaction. An estimate of the maximum possible rate of crack growth under these circumstances is obtained below from simple collision theory.

The number of ozone molecules incident on unit surface per second at ambient temperature is about  $8 \times 10^{19}c$ , where c is the ozone concentration in milligrams per liter. For a crack tip of width d in a sheet of thickness t

(both assumed larger than molecular dimensions) the rate of incidence of ozone molecules is thus about  $8 \times 10^{19} \text{ cdt/sec.}$  The number of network chains per unit volume is about  $6 \times 10^{19}$  for a normal vulcanizate, having a molecular weight between crosslinks of 10,000. Thus, ahead of the crack tip there are about  $6 \times 10^{19} \text{ dt}$  chains per unit distance. The maximum possible rate of crack growth is obtained by assuming that each ozone molecule impinging at the crack tip reacts instantaneously to sever one network chain. The value obtained is therefore about 1.3 cm./sec./mg. of ozone/l.

At high temperatures the rate of crack growth appears to approach a limiting value (Fig. 3) which is directly proportional to the ozone concentration. It corresponds to about  $0.8 \times 10^{-3}$  cm./sec./mg. of ozone/l., in fair accord with the value obtained previously¹ at somewhat lower temperatures, namely  $0.3 \times 10^{-3}$  cm./sec./mg. of ozone/l.

The limiting rate is thus about one-thousandth of the maximum possible value deduced above. The factor relating them may be considered a measure of the probability of reaction per collision, reduced below unity due to various steric requirements of the absorption and reaction processes. It may, however, be a serious underestimate of the real probability of reaction, since no allowance has been made for the lowered ozone concentrations and hence rates of incidence which would be expected near reactive surfaces, or for inefficient reaction of ozone, i.e., with chains which have already been severed.

An activation energy of the order of 1 kcal./mole or less and a "steric" factor of greater than  $10^{-3}$  suggests that the scission reaction is extraordinarily efficient. This might be attributed to the initiation by each ozone molecule of a chain reaction, presumably involving oxygen, leading to a number of scissions. Such an explanation seems unlikely, however, since McCool¹¹ has reported that oxygen-free ozone caused similar cracking to ozone diluted with oxygen.

We conclude that the maximum rate of crack growth is in accord with the simple collision theory of reaction rates when a value of  $10^{-3}$  is assumed for the probability of reaction of an incident ozone molecule, and the energy of activation is treated as negligibly small. Previously,¹ the rate has been shown to decrease as the degree of crosslinking, and hence the number of network chains, is increased. This is also in accord with the present simple kinetic scheme.

#### **Effect of Butadiene Content**

The experimental measurements suggest that the limiting rate of crack growth at high temperatures is proportional to the butadiene content, and hence to the degree of unsaturation of the copolymer. This trend is obscured by the large experimental scatter and also by variations in the degree of crosslinking of different materials. For simplicity, therefore, differences in unsaturation have been ignored in the present work.

#### CONCLUSIONS

The rate of growth of ozone cracks is apparently determined by two mechanisms. At temperatures near the glass transition temperature it is directly proportional to the segmental jump frequency  $\phi_T$ , probably reflecting the sluggish motion of rubber molecules in and near the surface, and largely independent of the ozone concentration. At high temperatures it is not very dependent on the segmental mobility, and hence on the temperature, but is directly proportional to the ozone concentration. Over the entire temperature range the rates may be very approximately described by considering the two mechanisms of delay as additive, i.e.,

$$1/R = (1/R_1) + (1/R_2) \tag{4}$$

where  $R_1$  is the low-temperature rate, given by eq. (3), and  $R_2$  is the high-temperature rate, given by

$$R_2 = 0.8 \times 10^{-3} c \text{ cm./sec.}$$

where c is the ozone concentration in milligrams/liter. The predictions of eq. (4) are represented by the dotted line in Figure 3. The transition from one delay mechanism to another is clearly not as abrupt as eq. (4) suggests; in consequence, the predicted values at intermediate temperatures are about twice as large as the measured values. However, eq. (4) should provide a useful guide to the behavior of unprotected rubbers over a wide range of temperatures and ozone concentrations.

The rate  $R_1$  at low temperatures is quantitatively related to the retardation time of a single network chain, the cut advancing by a molecular distance during this time interval. The rate  $R_2$  at high temperatures is in accord with the simple collision theory of reaction rates, with a "steric" factor of about  $10^{-3}$  and a negligibly small energy of activation.

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#### Résumé

On a mesuré la vitesse de croissance des crevasses provoquées par l'ozone sur des vulcanisats d'une série de copolymères butadiène-styrène, dans un domaine de températures allant de  $-5^{\circ}$ C à  $95^{\circ}$ C. Les vitesses sont déterminées par deux mécanismes. Aux basses températures, près de la température de transition vitreuse, elles dépendent quantitativement de la mobilité des segments du polymère. On peut conclure que, dans ce cas, l'étape principale, déterminante de la vitesse est le mouvement des chaînes de polymères après la rupture pour former une nouvelle surface. À températures élevées, la vitesse approche une valeur limite de  $10^{-3}$  cm/sec/mg d'ozone/l. C'est environ 1/1000 de la valeur maximale possible, lorsque la réaction immédiate d'une molécule d'ozone incidente provoque une rupture d'un réseau de la chaîne.

#### Zusammenfassung

Die Wachstumsgeschwindigkeit einzelner Ozonrisse wurde in Vulkanisaten einer Reihe von Butadien-Styrolcopolymeren im Temperaturbereich von  $-5^{\circ}$  bis 95°C gemessen. Die Geschwindigkeit scheint durch zwei Mechanismen bestimmt zu sein. Bei niedrigen Temperaturen in der Nähe der Glasumwandlungstemperatur steht sie in quantitativer Beziehung zur Segmentbeweglichkeit des Polymeren. Der wichtigste geschwindigkeitsbestimmende Schritt ist in diesem Fall die Bewegung der Polymerketten nach der Spaltung zur Bildung einer neuen Oberfläche. Bei hoher Temperatur nähert sich die Geschwindigkeit einem Grenzwert von  $10^{-3}$  cm/sec/mg Ozon/l. Das ist etwa ein Tausendstel des bei momentaner Reaktion eines auftretenden Ozonmoleküls unter Spaltung einer Netzwerkkette möglichen Maximalwerts.

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# Kinetic Study of the Polymerization of $\alpha$ -d-Styrene and/or Styrene by Homogeneous Catalysis. Part II*

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#### **Synopsis**

Initial rates of polymerization using the  $(C_5H_5)_2TiCl_2-Al(C_2H_5)_2Cl$  homogeneous catalyst system, were determined for homo and copolymerizations of styrene, styrene- $\alpha$ - $C^{14}$ ,  $\alpha$ -d-styrene, p-methylstyrene, and m-methylstyrene. Homopolymerization rates of styrene as a function of Al/Ti ratio indicate three rate maxima of apparently equal magnitude near Al/Ti ratios of 3.0, 11.0, and 16.0. Copolymerizations of  $\geq 97.5\% \alpha$ d-styrene and styrene as a function of Al/Ti ratio yielded no rate maxima but appeared to be a linear function of the Al/Ti ratio employed.  $\alpha$ -d-Styrene yielded higher initial polymerization rates than styrene under all tested experimental conditions. These rate increases as a function of monomer deuteration at the  $\alpha$  position are related to a higher concentration of active centers. A reaction scheme is proposed in which the predominant mode of formation of active centers occurs via alkylation of titanium but by a cationic mechanism. The observed isotope effect with the use of  $\alpha$ -d-styrene is related to the stability of the cationically formed active centers. Destruction of these active centers is is suggested to result in either an  $\alpha$ -alkylated new monomer and/or low molecular weight oligomers. An isotopically controlled unimolecular decomposition step is suggested as a mode of termination and/or destruction of potential active centers resulting in divalent titanium; probably  $(C_2H_5)_2$ Ti. The predominant mode of termination and/or destruction of active centers appears to occur by a bimolecular mechanism which is related to the experimentally observed monomer dependence of the initial rate of polymerization.

### **INTRODUCTION**

It has been shown^{:=0} that during the reaction of an aluminum alkyl and  $(C_5H_5)_2TiCl_2$ , soluble species are produced which have the ability to catalyze the polymerization of some olefins. The rate of polymerization was shown to be proportional to the concentration of intermediate complexes formed, specifically,⁵ it was shown that the rate of polymerization of ethylene was proportional to the concentration of an alkylated complex of tianium e.g.  $(C_5H_5)_2TiRCl\cdotAlR_2Cl$ .

The formation of an alkylated complex  $(C_5H_5)_2Ti(C_2H_5)Cl \cdot Al(C_2H_5)Cl_2$ (II) and its reduction to a final inactive form  $(C_5H_5)_2TiCl \cdot Al(C_2H_5)Cl_2$ (III), resulting from a reaction of  $(C_5H_5)_2TiCl_2$  and  $Al(C_2H_5)_2Cl$ , have been

* Part I: See Reference 9. This paper comprises a portion of a dissertation submitted by P. A. Jarovitzky in partial fulfillment of the requirements for the degree of Doctor of Philosophy in the Graduate School of the Polytechnic Institute of Brooklyn. associated with changes in the spectral intensities at 520 and 750 mµ, respectively.⁴ It was further shown⁴ that formation of II can occur by a unimolecular rearrangement of  $(C_5H_5)_2TiCl_2 \cdot Al(C_2H_5)_2Cl$  (I) or by a reaction of the latter with excess  $Al(C_2H_5)_2Cl$ ; also, the disappearance of II was shown to be zero-order and first-order in respect to II in the range of Al/Ti ratios  $\leq 2/1$  and  $\geq 4/1$ , respectively, both measured in the absence of monomer.

Breslow and Newburg³ observed for the  $(C_5H_5)_2TiCl_2-Al(C_2H_5)_2Cl$ catalytic system that dialkylated complexes of titanium may play a role in these catalytic reactions. These authors also found that the rate of polymerization of ethylene, when conducted in toluene, appears to go through a maximum near Al/Ti ratios of 4; no such effect was noted when solvent was *n*-heptane. In toluene the viscosity-average molecular weights decreased drastically at Al/Ti  $\geq 1$ . Only a small decrease of viscosity-average molecular weights was observed in hexane with increasing Al/Ti ratios in the range of 2.0 and 6.0. The physical properties of the polyethylene prepared by this homogeneous process are as good as those obtained by heterogeneous Ziegler-Natta catalysis. A linear polymer with a narrow molecular weight distribution resulted by homogeneous catalysis, indicating that here as well as for Ziegler-Natta catalysis, coordinated growth of polymeric chains probably occurs.

Chien,² studying the kinetics of the reaction between  $(C_5H_5)_2TiCl_2$  and  $Al(CH_3)_2Cl$  as a catalyst for the polymerization of ethylene, indicated that chain termination is a result of a bimolecular decomposition of active centers, resulting in disproportionation of alkyl groups. This appeared to be the preferred termination step, at least in the studied range of Al/Ti ratios of 2–3. Also, the overall activation energy for the ethylene polymerization by this homogeneous method was 11.75 kcal./mole, compared to 11.5  $\pm$  0.05 kcal./mole reported by Natta for the polymerization of propylene by TiCl₃·Al(C₂H₅)₃ heterogeneous catalysis.

Although ionic or nearly ionic species were indicated by Long,¹ Shilov et al.⁵⁻⁸ suggest an essentially 100% ionic character to the catalytically active species, resulting from a reaction of  $(C_5H_5)_2TiCl_2$  and aluminum sesquihalides. The latter supported their work by conductometric studies. Furthermore, Shilov et al.^{5,8} suggested that a reaction which destroys the catalytic site involves an  $\alpha$ -H exchange with an alkyl group from the catalyst, resulting in a new,  $\alpha$ -alkylated monomer and an inactive catalyst site. It is this type of reaction which has been claimed to be responsible for the inability of these catalytic systems to polymerize propylene or *n*-heptene.⁸

In our own laboratory it was shown,^{9,10} that the use of  $\alpha$ -d-styrene instead of styrene results in a higher effective concentration of active centers by heterogeneous TiCl₄·Al(C₂H₅)₃ and homogeneous (C₅H₅)₂TiCl₂·Al-(C₂H₅)₂Cl catalysis. It was further shown⁹ that the rate of formation of III was first order in II in the presence of monomer and one-half order in II in the absence of monomer. The monomers being styrene and/or  $\alpha$ -d-styrene and Al/Ti ratio = 18.2 It was also shown that  $(-d(II)/dt)_0$  < (-d(II)/dt)M, where the subscripts zero and M refer to the absence and presence of monomer, respectively, and (-d(II)/dt)D > (-d(II)/dt)H, where the subscripts D and H refer to  $\alpha$ -d-styrene and styrene, respectively. The existence of a single isosbestic point near 650 m $\mu$  as shown earlier⁴ was also confirmed. It was also shown that primarily CH₄ rather than CH₃D was collected during a reaction of  $(C_5H_5)_2TiCl_2\cdot Al(CH_3)_3$  with 100%  $\alpha$ -d-styrene. A reaction scheme was proposed to account for the experimental observations.

Polymerizations conducted with  $CD_2$ =CD₂ by Ziegler-Natta catalysis¹² showed no rate or molecular weight increase when compared to ethylene. More recently, using  $CD_2$ =CD₂ and a homogeneous  $(C_5H_5)_2TiCl_2 \cdot Al-(CH_3)_2Cl$  catalyst¹¹ system, no rate but molecular weight increases were obtained compared to ethylene. It was further shown¹³ by the use of NMR, that for  $(C_5H_5)_2TiCl_2 \cdot Al(CH_3)_3$  or  $Al(CH_3)_2Cl$  catalytic systems and using phenylacetylene as the monomer, only the titanium moiety appeared to be involved in the formation of active centers. Similar results have been obtained using styrene as the monomer and a  $(C_5H_5)_2TiCl_2 \cdot Al(CH_3)_3$ catalytic system.¹⁵

It is the purpose of the following to further elucidate the proposed mechanism⁹ of  $(C_5H_5)_2TiCl_2 \cdot Al(C_2H_5)_2Cl$  catalysis for the polymerization of styrene and/or  $\alpha$ -d-styrene, in the light of additionally available data.

#### **EXPERIMENTAL**

#### **Monomer Preparation and Purification**

 $\alpha$ -d-Styrene.  $\alpha$ -d-Styrene was prepared by reduction with LiAlD₄ as described earlier.^{9,10} Mass spectroscopy indicated a 97.5% purity, the majority of the impurity being styrene itself. Monomer was triply distilled in vacuum.

**Styrene.** Commercial samples of Matheson styrene used were either triply distilled in vacuum only or treated as follows: (1) extracted with ca. 10% aqueous potassium hydroxide solution, (2) washed with distilled water until wash water remained neutral, (3) dried over molecular sieves overnight, (4) distilled in vacuum over calcium hydride. Both of these methods proved to be equally acceptable in respect to reproducibility of observed polymerization rates and final polymer intrinsic viscosities.

**Styrene**- $\alpha$ -C¹⁴. The preparation of styrene- $\alpha$ -C¹⁴ and subsequent determination of radioactive carbon in the polymer, carried out by means of a proportional counting technique, were reported earlier.¹⁴

*p*-Methylstyrene. A commercially available sample (Borden Company) was used after vacuum distillation: b.p. 59.5°C./15 mm.

*m*-Methylstyrene. The monomer was conveniently prepared by a Grignard reaction with *m*-bromotoluene and acetaldehyde. The resulting alcohol was pyrolyzed over alumina at ca.  $300^{\circ}$ C. to give the desired product in a 48.5% overall yield and pure as shown by a single peak via

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vapor-phase chromatography. The monomer was vacuum distilled; b.p. 83°C./13 mm.

## **Solvents**

Benzene was purified by a process described earlier¹⁰ and stored over calcium hydride. Hexane was vacuum distilled over calcium hydride and stored over calcium hydride.

#### **Determination of Polymerization Rates**

The experimental technique for the determination of rates of polymerization is that used and reported earlier for the heterogeneous Ziegler-Natta system,¹⁰ a dilatometer with a 3 mm. precision bore capillary being used. Specifically a 0.37F (formality) solution of  $Al(C_2H_5)_2Cl$  was prepared and the  $(C_5H_5)_2TiCl_2$  used is a commercially available sample from Chemicals Procurement Laboratories, Inc.

Polymerization rates were measured in respect to a critical time  $T_c$ , defined as the time elapsed between first contact of  $(C_5H_5)_2\text{TiCl}_2$  and  $Al(C_2H_5)_2Cl$  and the addition of monomer. Reaction conditions were varied in respect to  $T_c$ , Al/Ti ratio, total monomer concentration, and type of monomer and/or solvent employed.

Homopolymerization and/or copolymerization rates were determined for styrene or styrene- $\alpha$ -C¹⁴, with  $\alpha$ -d-styrene, p-methylstyrene, or mmethylstyrene being used as comonomers.

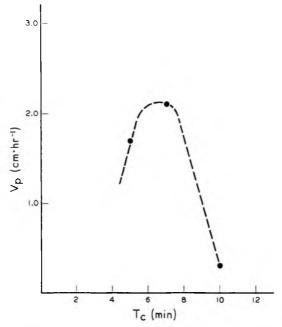


Fig. 1. Effect of critical time  $T_c$  on initial polymerization rate of styrene by homogeneous catalysis with  $Al(C_2H_6)_2Cl-(C_3H_5)_2TiCl_2$ .

								Total				-
Run	$(C_2H_5)_2TiCl_2,$ mole/l.	Al/Ti	Styrene, mole-%	$\alpha^{-d-}$ Styrene, mole- $\%$	$\alpha$ - $d$ - $n$ - Styrene, Benzene, Hexane, mole- $\%$ vol $\%$ vol- $\%$	<i>n-</i> Hexane, vol-%	Temp., °C.	monomer [M _T ], mole/l.	r $T_c$ , min.	$v_{p}$ , cm./hr.	Conversion, $\%$	$[\eta]$ (29.3°C., $C_6H_6$ )
IV-38	0.009	2.1	100	0	100	0	29.25	0.41	1	2.000	16.9	
" 42	11	3.0	**	**	**	11		11	5	1.636	1	I
" 44	**	**	33	**	11	13	11	2.2	**	1.785	16.5	
" 36	**	**	12	11	11	**		11	r-	2.118	16.9	0.09
6 ,,	11		11	33	33	13	55	. 7.7	10	0.300	0	1
" 46	11	33	2.5	6.79	11	11			2	2.591	17.0	0.06
" 34		5.0	100	0	11	23	13	11	**	1.582	16.4	
" 30	11	6.0	33	12	**	**	**	11		1.165	16.5	
" 11	a.	8.6	**	**	11	**	**		s	0.735	Trace	1
" 56		23	2.5	97.5	13	11	11		2	2.803	17.8	0.06
52		11	100	0	23.5	71.8	17	. 2.2	10	1	14.9	0.08
48	0.008	9.2		33	20.4	75.6		0.36	15	1.320	9.2	0.08
24	0.009	9.8	22		100	0		0.41	1	1.718	14.8	
. 17	22	10.8	23	11	**	55		**	13	2.218	12.7	0.06
22	11	12.0	22	11	**	11		11	11	2.043	19.2	
" 28		12.9			11	13		11		1.380	15.4	
" 15	11	11		23	25	11		11	23	0.636	6.4	
" 26		15.0			55	**			11	1.743	12.6	
" 32	11	17.2	55	33	22	11	11	11	2.2	1.800	15.6	
" 13	11		**	22	22	22		11	x	0.439	9.4	
E. D. Avg.		18.2	17	11	11	11	$26 \pm 0.5$		5	1.124	10.8	0.05 - 0.07
E. D. 11	11	11	50	50	11	22	26.5		**	1.779	15.0	0.06
E. D. 13	17	17	0	100	11	11	26.2	22	**	3.236	15.5	0.05
E. D. 6	17	23	100	0	13	11	24.2	1.02	"	4.474	16.0	0.06
V-4	11	3.0	**	11	**	**	29.25	0.82	1	6.302	17.4	0.07

TABLE I^a

	Como	Comonomer in feed, mole-%	mole-%	Styrene-o-C14			-
Run	Styrene- α-C ¹⁴	<i>p</i> -Methyl- styrene	<i>m</i> -Methyl- styrene	in polymer, mole-%	$V_{p'}$ cm./hr.	$\underset{\%}{\text{Conversion}},$	$(29.3^{\circ}C.) C_{6}H_{6})$
IV-64	50	50	0	$30.21 \pm 0.35$	5.708	39.5	0.07
99- ,,	50	50	0	$27.47 \pm 0.89$	1	30.9	0.07
69- 11	0	100	0	I	9.003	68	0.11
"-62	0	0	100	I	2.214	Trace	1

TABLE II Copolymerizations of Styrene- $\alpha$ -C¹⁴ and Styrene Derivatives by Homogeneous Catalysis with  $\frac{1}{\Delta MC}$  H MC H MC L

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All reported polymerization rate data were obtained by a least-square analysis of the raw data but are reported only in terms of centimeters/hour. A value in terms of moles/liter/hour would be subject to a considerable error, the magnitude of which would be directly proportional to unprecipitated reaction products. As it will be pointed out in the body of this report, relatively large amounts of methanol HCl-soluble reaction products are formed by this mode of catalysis and with the use of styrene and/or  $\alpha$ -d-styrene and/or styrene derivatives. These soluble oligomers then have contributed to the measured rate without being accounted for in the reported per cent conversion.

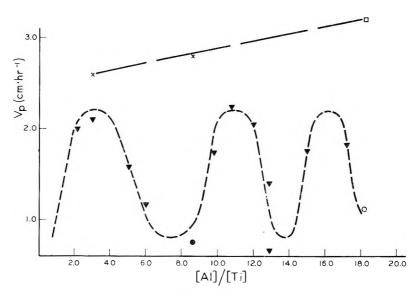


Fig. 2. Effect of Al/Ti ratio on initial polymerization rate with styrene and/or $\alpha$ -d-styrene by homogeneous catalysis with Al(C₂H₅)₂Cl-(C₅H₅)₂TiCl₂: (O) 100% styrene,  $T_c = 5 \text{ min.}$ ; ( $\checkmark$ ) 100% styrene,  $T_c = 7 \text{ min.}$ ; ( $\bigcirc$ ) 100% styrene,  $T_c = 8 \text{ min.}$ ; ( $\Box$ )  $\geq$  97.5%  $\alpha$ -d-styrene,  $T_c = 7 \text{ min.}$ ; ( $\times$ )  $\geq$  97.5%  $\alpha$ -d-styrene,  $T_c = 7 \text{ min.}$ 

Polymerization data obtained for homopolymers and/or copolymers of styrene and/or  $\alpha$ -d-styrene are summarized in Table I. Polymerization data obtained for copolymers of styrene- $\alpha$ -C¹⁴ and p-methylstyrene and homopolymers of the styrene derivatives are summarized in Table II.

A plot of polymerization rates for styrene as a function of  $T_c$  at Al/Ti ratio of 3.0 is shown in Figure 1.

A plot of polymerization rates as a function of Al/Ti ratio for styrene and monomer mixtures of  $\geq 97.5\%$   $\alpha$ -d-styrene and styrene is shown in Figure 2.

A plot of polymerization rate of styrene as a function of monomer concentration is shown in Figure 3.

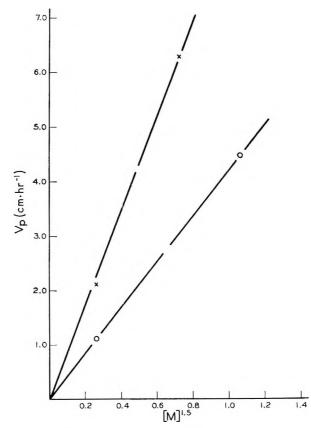


Fig. 3. Initial styrene polymerization rate vs.  $[M]^{1.5}$  by homogeneous catalysis with  $Al(C_2H_5)_2Cl-(C_8H_5)_2TiCl_2$ : (×) Al/Ti = 3.0; (O) Al/Ti = 18.2.

#### DISCUSSION

Based upon the data presented in Tables I and II and plotted as Figures 1-3, a reaction scheme is proposed and shown in Figure 4. It is the purpose of the following to justify the proposed scheme which is essentially a more detailed version of the one presented earlier,⁹ in the light of new experimental evidence obtained in this laboratory as well as data previously published by a number of authors.

When  $(C_5H_5)_2TiCl_2$  is reacted with  $Al(C_2H_5)_2Cl$  in the absence of monomer, a series of color changes result which are very much affected by the nature of the solvent employed. If the solvent is benzene, the original orange-red solution of only  $(C_5H_5)_2TiCl_2$  in benzene is quickly changed to a dark reddish-green which will then change to a lighter but predominantly blue solution. If the solvent employed is hexane there is no color developed for the original  $(C_5H_5)_2TiCl_2$ -hexane mixture, probably primarily due to its poor solubility in hexane. Upon the addition of  $Al(C_2H_5)_2Cl$  a yellow color develops which slowly darkens to a yellow-brown. These shades of yellow are quite stable up to the point of monomer introduction, upon which an

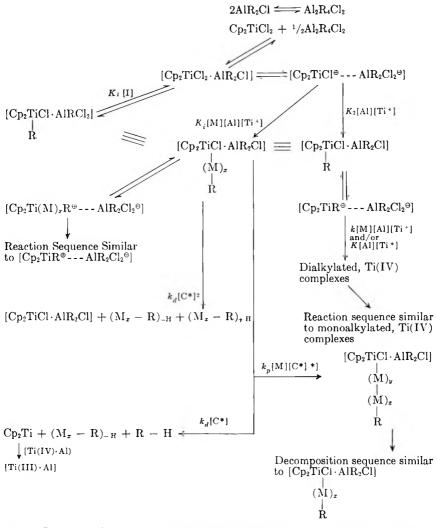


Fig. 4. Reaction scheme for the polymerization of styrene by homogeneous catalysis with  $Al(C_2H_5)_2Cl-(C_5H_5)_2TiCl_2$ .

immediate development of green occurs which quickly changes to a predominantly blue solution; e.g., the change to the blue is much quicker than in a benzene solution, once a green shade has formed, all other conditions being equal. As has been pointed out previously,⁹ the use of monomer accelerates the production of the inactive blue solution. Specifically, the use of  $\alpha$ -d-styrene produces a blue solution faster than does styrene. Moreover, the use of solvent of high hexane content rather than benzene alone, as well as the use of  $\geq 97.5\%$   $\alpha$ -d-styrene rather than 100% styrene results in a high yield of a solid polymeric product under experimental conditions which for 100% styrene and 100% benzene yield only trace quantities of solids; (compare IV-11, IV-56, and IV-52 of Table I). It is suggested that benzene produces an equilibrium which favors ionic species, e.g.,

$$[(C_{5}H_{5})_{2}TiCl_{2} \cdot Al(C_{2}H_{5})_{2}Cl] \rightleftharpoons [(C_{5}H_{5})_{2}TiCl_{2} \dots Al(C_{2}H_{5})_{2}Cl_{2}]$$
(1)

the stability of which appears however, not to be due to dielectric effects of the solvent but rather due to complexation with the  $\pi$ -electron systems of an aromatic moiety; e.g.,

 $\boxed{(C_5H_5)_2TiCl} \xrightarrow{\bigoplus} \cdots Al(C_2H_5)_2Cl_2 \xrightarrow{\Theta}$ 

which is a type of Friedel-Craft adduct. This further suggests that toluene probably functions primarily as a  $\pi$ -complexer rather than providing a high dielectric medium. It is then plausible that I is converted to an active species for polymerization by alkylation on titanium but that this reaction can be accomplished in at least three ways. Two of these methods have been suggested earlier,⁴ e.g., a unimolecular rearrangement of I to form  $(C_5H_3)_2$ TiRCl·Al $(C_2H_5)$ Cl₂(II) and by a reaction of I with excess Al $(C_2H_5)_2$ -Cl to form II. It is now proposed that the alkylation of I with excess  $Al(C_2H_5)_2Cl$  occurs primarily with its ionic form, as shown in Figure 4, in solvents which either have high dielectric properties and/or are aromatic, while unimolecular formation of II probably occurs in solvents which have low dielectric properties and/or are nonaromatic. Complex II arising from a reaction of AlR₂Cl and the ionic form of I is probably better represented by  $(C_5H_5)_2$ TiRCl·AlR₂Cl. A third possibility of forming active centers occurs in aromatic and/or solvents of high dielectric properties with monomer and the ionic forms of species I and II; this, in turn, appears to be a faster reaction than alkylation by excess  $Al(C_2H_5)_2Cl$ , as shown in eq. (2) for the ionic forms of I, but omitting the solvation of the ion pair.

$$\begin{bmatrix} (C_{5}H_{5})_{2}Ti\overset{\oplus}{C}l_{-} \dots Al(C_{2}H_{5})_{2}Cl_{2}] & \xrightarrow{CH_{2}=CHR} \\ H & & & \\ \hline \\ (C_{5}H_{5})_{2}Ti-CH_{2}-C & \oplus \dots Al(C_{2}H_{5})_{2}Cl_{2} \end{bmatrix} \xrightarrow{^{1/2}(AIR_{2}Cl)_{2}} \\ \overset{(C_{5}H_{5})_{2}TiCl \cdot Al(C_{2}H_{5})_{2}Cl(=II-M) \\ \downarrow \\ CH_{2} \\ R-C-H \\ C_{2}H_{5} \\ (2) \end{bmatrix}$$

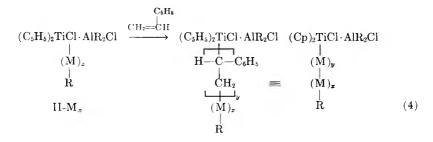
Species II-M is essentially like II, differing only in the nature of R. While this is a mode of production of active centers, it can equally well be a mode of cationic propagation, e.g., with formation of

$$\begin{array}{ccc} (C_{\delta}H_{5})_{2}TiCl \cdot Al(C_{2}H_{\delta})_{2}Cl & \equiv (Cp)_{2}TiCl \cdot AlR_{2}Cl \\ & & & & \\ & & & \\ CH_{2} & & & & \\ CH_{2} & & & & \\ & & & & \\ R-C-H & & & \\ & & & \\ C_{2}H_{\delta} & & \\ \end{array}$$

where  $(Cp) = (C_5H_5)$  and where x may be unity and if larger than unity is probably small under these experimental conditions. It was therefore of interest to copolymerize styrene with styrene derivatives which support an  $\alpha$ -carbonium ion, e.g., p-methylstyrene. These experiments are summarized in Table II. The use of styrene- $\alpha$ -C¹⁴ permitted determination of copolymer composition by using a method reported earlier.¹⁴ The data of Table II (using run IV-36 of Table I as a reference) indicate that: (a) the rate of homopolystyrene formation is much slower than the rate of homopoly-p-methylstyrene formation; (b) a 50/50 mole-% feed of styrene and p-methylstyrene results in polymer of  $\geq$ 70 mole-% of p-methylstyrene, near 30% conversion; (c) the increase in the rate of polymerization is an approximate linear function of the p-methylstyrene content of the comonomer mixture.

Visually, the rate of appearance of the blue color was much enhanced (almost doubled) when p-methylstyrene was used rather that styrene. These data collectively support a predominantly cationic initiation mechanism. The use of m-methylstyrene (IV-62 in Table II) results in a rate of polymerization which is the same (within experimental error) as that for styrene itself. Visually, the rate of appearance of blue is the same for both m-methylstyrene and styrene. Nevertheless, m-methylstyrene results in a 100% methanol·HCl-soluble reaction product. These data, although at present not clearly understood, suggest a mode of termination without accompanying destruction of active centers, suggesting a penultimate effect in coordinated anionic growth resulting in termination by monomer.

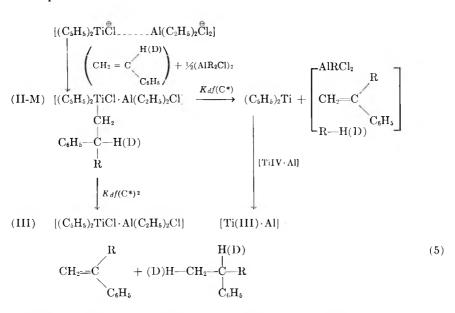
It should be noted that the orientation of monomer in respect to titanium in species II-M should be such that the more stable carbonium ion results and therefore contrary to the orientation one would expect for an essentially nonionic or coordinated-anionic mechanism via monomer insertion into II. The latter could then be referred to as normal or coordinated catalysis proposed earlier by many authors: e.g., a coordinated-anionic propagation of styrene, as shown in eqs. (3) and (4) for II and II-M_z.



Here y represents the number of monomer units incorporated by Coordinate-anionic propagation. It is expected that a ratio of y/x would increase with decreasing stability of an intermediate monomer carbonium ion, e.g., ethylene should by this mechanism have a maximum ratio of y/x.

For propylene however, the same alkylated products would probably be obtained by either use of the ionic species of I to form II or a normal initiation by II.

It is proposed that the reaction of the ionic species of I or II provides the clue to the observed isotope effect by the use of  $\alpha$ -d-styrene, e.g., the increase in the rate of polymerization. This is shown in eq. (5) for the ionic species of I:



Neither a unimolecular nor a bimolecular decomposition mechanism of active centers (C^{*}) alone appears to be able to account for all experimental facts; i.e., both should be retarded by  $\alpha$ -deuterium or have a low value for the isotope factor f; e.g., one must explain both, the increase in rate of polymerization and the increase in production of inactive species with the use of  $\alpha$ -d-styrene when compared to styrene.

The earlier and more general scheme⁹ indicated the formation of an unknown species X, which in turn must result in inactive complexes of Ti(III)

but probably at a slower rate than a more direct formation of inactive Ti(III) complexes from a decomposition of active centers.

It is now felt that X is produced by a unimolecular decomposition of active centers and probably corresponds to divalent titanium; e.g.,  $(C_5H_5)_{2}$ -Ti. The latter can react further with  $[Ti(IV)\cdot A]$  complexes to result in inactive  $[TiIII\cdot A]$  complexes by disproportionation. The disproportionation reaction of Ti(II) and Ti(IV) would probably be the rate-determining step for the production of inactive  $[Ti(III)\cdot A]$  complexes by unimolecular decomposition of active centers.

The decomposition of species II- $M_x$  by either mechanism would result in the formation of an  $\alpha$ -alkylated new monomer when x = 1. When x > 1, low molecular weight oligomeric products would result. A similar mechanism has been suggested for the failure of this and similar catalytic systems to polymerize propylene and heptene.^{8,11}

A bimolecular disproportionation of active centers has been suggested to be the exclusive mode of polymer termination in the  $(C_5H_5)_2TiCl_2Al(CH_3)_2-Cl$  system.²

Spectral data collected by the writers⁹ and others⁴ at 520 mµ for the  $(C_5H_5)_2TiCl_2 \cdot Al(C_2H_5)_2Cl$  system indicate a decomposition of active centers (if in fact absorption at 520 mµ represents the absorption of active centers) which is zero- to first-order, depending on the Al/Ti ratio and/or the presence of monomer.

Moreover, careful examination of the spectra indicates that in the presence of monomer absorption for the  $(C_5H_5)_2TiCl_2 \cdot Al(C_2H_5)_2Cl$  system also occurs at ca. 450 m $\mu$ . The disappearance of this peak, however, appears to vary between one-half and first order in respect to the absorbing species for lower and higher monomer concentrations respectively; e.g. also showing no correspondence to a bimolecular decomposition.

It is felt at present that little weight can be given to spectral changes in this system, since all available polymerization data taken collectively for the  $(C_5H_5)_2TiCl_2 \cdot Al(C_2H_5)_2Cl$  system appear to favor a bimolecular decomposition of active centers as the predominant mode of termination.

Initial efforts to polymerize styrene by the  $(C_5H_5)_2TiCl_2 \cdot Al(C_2H_5)_2Cl$ system in the presence of varied substrates have shown that if the substrate represents a large surface area (e.g., activated charcoal), the lifetime of active centers can be almost doubled, and this supports a bimolecular decomposition mechanism of active centers.

Examination of Figure 2 indicates that three rate maxima exist near Al/Ti ratios of 3.0, 11.0, and 16.0. Although three rate maxima are indicated, available intrinsic viscosity data show only a small dependence on Al/Ti ratio in this range. Polymers were rated visually as to their color after purification by methanol washing and vacuum drying at ca.  $60^{\circ}$ C. and 10–15 cm Hg. It was evident that drying under these conditions produced a deterioration of polymer color roughly inversely proportional to the rate at which they were formed. All samples appeared to contain some low molecular weight products as shown by Schliering of the methanol wash of the solid reaction product. It is believed that low molecular weight

oligomers are formed under all experimental conditions but especially so at those Al/Ti ratios where rate minima are indicated. As per the reaction scheme shown in Figure 4, the decomposition of complexes of type II-M_x would explain the low molecular weight oligomeric products representing cationically formed oligomers. The use of  $\alpha$ -d-styrene results in solid, polymeric products at all tested Al/Ti ratios and in polymerization rates which, contrary to styrene, appear to be a linear function of the Al/Ti ratio employed.

It is believed that the excessive formation of methanol-HCl-soluble reaction products with styrene is based on a maximum concentration of ionic species, yielding maximum concentrations of active centers, but where the decomposition rates are larger than the propagation rates. The fact that further increases in the Al/Ti ratio can again yield rate as well as molecular weight maxima may then reflect a stepwise build-up of equilibria as suggested by the reaction scheme shown in Figure 4. Eventually this may lead to dialkylated, tetravalent titanium at minimum concentration of ionic species.

While it is most difficult at best to explain the existence of three rate maxima in the Al/Ti range of 3.0-16.0, it is, however, reasonable to suggest (based on the scheme as shown in Fig. 4) that these maxima are due to: (a) different modes of production of species of type II which may differ in their stability and/or mode of reduction to inactive species or (b) different modes of production of dialkylated species which may differ in their stability and/or mode of reduction to inactive species.

A combination of both (a) and (b) may then yield three rate maxima. At Al/Ti near 3.0 essentially monoalkylated species may be involved compared to an Al/Ti ratio near 10.0 where essentially dialkylated species may be involved. It is probable that the rate maximum near Al/Ti near 11.0 is a complicated function of both monoalkylated and dialkylated species.

An attempt is made below to evaluate kinetically the scheme presented in Figure 4 with the following assumptions: (a)  $K_1[I] \ll K_2[Ti^+][Al] < K_i[Ti^+][Al][M]$ ; (b) steady-state conditions can be applied to the production of active centers; (c) bimolecular disproportionation of active centers is the predominant mode of decomposition. Then:

$$d[C^*]/dt = K_i[Ti^+][Al][M] - k_d f[C^*]^2 = 0$$

where f denotes the fact that an isotope effect is operative, i.e., a small value of f is expected for  $\alpha$ -d-styrene and a large value of f for styrene. Thus

$$[C^*] = (K_i[Ti^+][Al][M]/K_df)^{1/2} = K[M]^{0.5}$$

and

$$V_p = K_p[\mathbf{C}^*][\mathbf{M}]^r$$

where  $V_p$  = observed polymerization rate,  $K_p$  = overall polymerization constant, [C^{*}] = concentration of active centers of type (C₅H₅)₂TiRCl·-  $AlR_aCl_b$ , [M] = monomer concentration, and r = order of propagation with respect to monomer.

Then

$$V_{p} = K_{p} K [M]^{r+0.5}$$

It is therefore suggested that the experimentally observed monomer dependence is an overall monomer dependence derived from the propagation reaction proper and the production of an effective concentration of active centers  $[C^*]$ ; e.g.,

$$V_{p} = K_{p}[C^{*}][M]^{r} = K_{p}K[M]^{r+a} = K_{p}K[M]^{x}$$

where x = experimentally observed overall monomer dependence, r = real or true monomer dependence of the propagation reaction, a = monomer dependence of [C^{*}].

Based on the above, the overall monomer dependence x can then be expected to be equal to 1.5 for a predominantly bimolecular terminationreduction.

Based on the data of Table I plotted in Figure 3, the polymerization rate does appear to be proportional to  $[M]^{1.5}$  at the two extremes of experimental Al/Ti ratios.

A similar treatment for Ziegler-Natta catalysis with styrene and/or  $\alpha$ -d-styrene has yielded identical results.¹⁰

We wish to thank Mr. Toby Chapman of the Polytechnic Institute of Brooklyn, Department of Chemistry, for supplying the styrene derivatives and the radioactive counting of the copolymers prepared with styrene- $\alpha$ -C¹⁴.

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#### Résumé

Les vitesses initiales de polymérisation ont été determinées dans le cas de la polymérisation et de la copolymerisation du styrolène,  $\alpha$ -C¹⁴ styrolène,  $\alpha$ -d-styrolène, pméthylstyrolène et *m*-méthylstyrolène avec un système catalyseur homogène  $(C_sH_s)_{2}$ -TiCl₂-Al(C₅H₅)₂Cl. Les vitesses d'homopolymérisation du styrolène en fonction du taux Al/Ti indiquent la présence de trois maxima de vitesse, d'intensités sensiblement égales, ayant lieu pour des taux Al/Ti voisins de 3.0, 11.0 et 16.0. Des copolymérisations à  $\geq$  97.5% d'a-d-styrolène et de styrolène ne présentent plus de maximum de vitesse en fonction du taux Al/Ti mais semblent suivre une relation linéaire en fonction du taux utilisé. L' $\alpha$ -d-styrolène présente des vitesses initiales de polymérisation plus grandes que celles du styrolène dans les conditions expérimentales employées. Cet accroissement des vitesses en fonction de la deutération du monomère en position  $\alpha$  est à relier avec une plus grande concentration des centres actifs. Un schéma réactionnel est proposé dans lequel le mode de formation prédominant des centres actifs à lieu par alcoylation du titane mais par un mécanisme cationique. L'effet isotopique observé dans le cas de l' $\alpha$ -d-styrolène est à relier à la stabilité des centres actifs cationiquement formés. La destruction de ces centres actifs semble produire soit un nouveau monomère  $\alpha$ -alcoylé, et des oligomères de bas poids moléculaire. On a proposé un pas de décomposition monomoleculaire isotopiquement contrôlé comme mode de terminaison ou de destruction des centres actifs potentiels provenant du titane divalent, probablement du  $(C_5H_{\delta})_2$ -Ti. Le mode prédominant de terminaison ou de destruction des centres actifs semble se produire par un mécanisme bimoléculaire en rapport avec la relation expérimentale observée entre la vitesse initiale de polymérisation et le monomère.

#### Zusammenfassung

Die Anfangspolymerisationsgeschwindigkeiten der Homo- und Copolymerisationen von Styrol, Styrol- $\alpha$ -C¹⁴,  $\alpha$ -d-Styrol, p-Methylstyrol und m-Methylstyrol wurden bestimmt, wobei das homogene (C5H5)2TiCl2-Al(C2H5)2Cl Katalysatorsystem verwendet wurde. Die Geschwindigkeiten der Homopolymerisation von Styrol zeigen in Abhängigkeit vom Al/Ti Verhältnis drei Maxima von offensichtlich gleicher Grösse in der Nahe der Al/Ti Verhaltnisse von 3.0, 11.0 and 16.0. Copolymerisationen von  $\geq$ 97.5%  $\alpha$ -d-Styrol in Abhängigkeit vom Al/Ti Verhältnis wiesen keine maximalen Geschwindigkeiten auf, waren aber dem angewandten Al/Ti Verhältnis direkt proportional. a-d-Styrol hatte unter allen angewandten experimentellen Bedingungen höhere Angangspolymerisationsgeschwindigkeiten als Styrol. Diese Geschwindigkeitszunahmen in Abhängigkeit von der Deuterierung am  $\alpha$ -Kohlenstoffatom stehen mit der höheren Konzentration an aktiven Zentren in Zusammenhang. Es wird eign Reaktionsmechanismus vorgeschlagen, in dem die Bildung von aktiven Zentren hauptsächlich durch Alkylierung des Titans erfolgt, wobei aber ein kationischer Mechanismus vorliegt. Der bei der Verwendung von  $\alpha$ -d-Styrol beobachtete Isotopeneffekt wird auf die Beständigkeit der kationisch gebildeten aktiven Zentren zurueckgeführt. Es wird vorgeschlagen, dass die Zerstörung dieser aktiven Zentren entweder zu  $\alpha$ -akylierten neuen Monomeren und/oder zu niedermolekularen Oligomeren führt. Als eine Abbruchsreaktion und/oder Zerstörung von möglichen aktiven Zentren wird eine isotopisch kontrollierte monomolekulare Zersetzung vorgeschlagen, wobei bivalente Titaniumverbindungen, wahrscheinlich  $(C_5H_5)_2$ Ti, entstehen. Die überwiegende Abbruchsreaktion und/oder Zerstörung von aktiven Zentren scheint über einen bimolekularen Mechanismus zu erfolgen, der auf die experimentell beobachtete Abhaengigkeit der Anfangspolymerisationsgeschwindigkeit von der Monomerenkonzentration zurueckgeführt wird.

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# Ferrocene-Containing Polymers. V. Polycondensation of *N*,*N*-Dimethylaminomethylferrocene

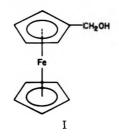
EBERHARD W. NEUSE and EDWARD QUO, Polymer Laboratory, Missile & Space Systems Division, Douglas Aircraft Company, Inc., Santa Monica, California

#### Synopsis

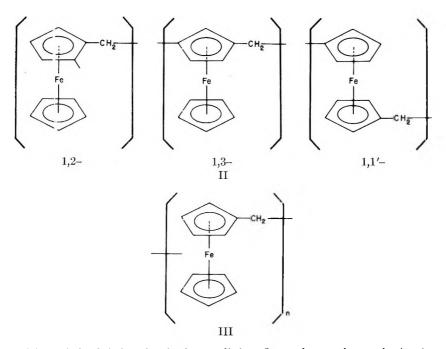
The self-condensation of the ferrocenyl Mannich base, N,N-dimethylaminomethylferrocene, in the presence of a ZnCl₂-HCl catalyst system in the melt phase leads to soluble polymers containing ferrocenylene units interlinked by methylene groups. The crude condensation products exhibit number-average molecular weights in the range 4000-8000. Elemental and infrared spectroscopic analyses as well as viscometric data show the structure to be essentially identical with that of the polymer derived from hydroxymethylferrocene described in an earlier communication. The optimum molar ratio of the reactants (Mannich base, ZnCl₂, and HCl) is 2:1:2. Dimethylammonium tetrachlorozincate has been isolated as by-product, and an intermediary complex composed of Mannich base, ZnCl₂, and HCl in the same 2:1:2 ratio has been intercepted during the polycondensation. Some mechanistic inferences are discussed.

#### **INTRODUCTION**

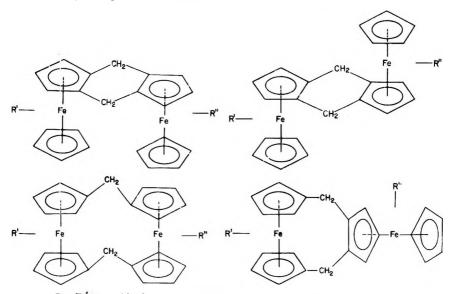
In a recent communication,¹ the acid-catalyzed polycondensation of ferrocenyl carbinols was described. The polymers obtained were composed of recurring units of the type  $+C_{10}H_8Fe-CHR+$ , with R standing for H, CH₃, and C₆H₅ in the instances investigated (following conventional usage, the abbreviated forms  $C_{10}H_9Fe$ - and  $-C_{10}H_8Fe$ - denote the monosubstituted ferrocenyl and disubstituted ferrocenylene groups, respectively). Accordingly, in the simplest case with hydroxymethylferrocene (I) as starting material, the resulting polycondensation product was assigned the novolac-type structure  $+C_{10}H_8Fe-CH_2+_{\pi}$ .



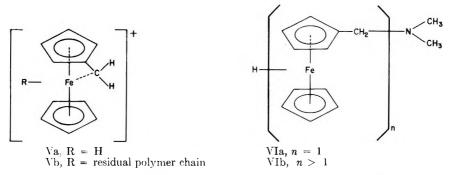
A random distribution sequence was assumed, which involved the homoand heteroannular dispositions depicted by the segment structures II. For the purpose of this paper, the structure of the hydroxymethylferrocene polymer may be represented by the simplified scheme III, in which the



position of the left-hand substituent link reflects the random substitution pattern involving the segments II. As a result of a terminating selfsubstitution reaction, the backbone of III was believed to contain a terminal ( $\mathbb{R}'' = \mathbb{H}$ ) or internal ( $\mathbb{R}'' =$  residual polymer chain) double-bridged segment as represented by the four possible homo- and heteroannular structures IV. Propagation was assumed to proceed by an ionic mechanism, and metallocarbonium ions, in the simplest case exhibiting the general structure V, were postulated as intermediates.



IV,  $\mathbf{R}'$  = residual polymer chain;  $\mathbf{R}'' = \mathbf{H}$  or residual polymer chain



It has now been found that a polymer having essentially the same structure III results from polycondensation of N,N-dimethylaminomethylferrocene (VIa). This Mannich base² is a precursor in the sequence of preparative steps leading to carbinol I. The new synthesis described in this paper, therefore, represents a more direct route to polymer III.

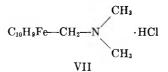
# **RESULTS AND DISCUSSION**

#### **Polycondensation Reaction and Polymer Structure**

The self-condensation of Mannich bases derived from phenolic compounds to form low-molecular polymers of the novolac type, i.e., compounds with aromatic nuclei and methylene groups alternating in the chain, has recently been reported in the literature.³ Polycondensation through elimination of dimethylamine was brought about by simply heating the starting material at 200°C. in the absence of catalysts. The reaction was assumed to proceed via polynuclear compounds bearing terminal or possibly internal amino groups, carbonium ions being involved in the formation of these intermediates.

Attempts in this laboratory to eliminate dimethylamine from the corresponding ferrocenyl derivative VIa by applying analogous experimental conditions were unsuccessful, and no polymer formation was observed. Therefore, the effect of a variety of acidic compounds as potential catalysts was investigated. The generation of iron-carbonium ions of the type V would be expected in the presence of such catalysts. These transitory species should propagate by a mechanism similar to that operative in the polycondensation reactions of the carbinol I, except that polymeric amines would possibly be involved as intermediates in place of ethers. The experiments showed mineral acids such as HCl and H₂SO₄ to be inefficacious in catalyzing linear polycondensation, with competing reactions resulting instead in crosslinking and decomposition of the ferrocene unit. Similar side-reactions, albeit coupled with some polymer formation, were observed with strong Lewis acids, such as AlCl₃ or BF₃. In contrast, the weak Lewis acid, zinc chloride, proved to be a highly efficacious catalyst and, hence, was employed in all reactions herein described. However, in order to attain high polymer yields within acceptable reaction times, it was necessary to use the compound in a concentration as high as 50 mole-%and in combination with 100 mole-% of hydrogen chloride. HCl could be

introduced either as hydrochloric acid or in the form of the hydrochloride of the Mannich base, VII (prepared by reaction or equimolar amounts of VIa and HCl in methanol). The latter procedure, while offering the



advantage of accurate dosage coupled with short reaction times, was not always found to give reproducible yields, probably because of incomplete homogenization of the reactants owing to the infusibility of VII. By adding, instead, the required equimolar amount of HCl as aqueous hydrochloric acid, the initial reaction mixture remained liquid long enough to allow for more homogeneous distribution of the Lewis acid. Therefore, this procedure, which also avoided the additional step of preparing the hydrochloride VII, was preferred in spite of the longer reaction times involved.

The polycondensations were carried out by reacting in the melt phase, in a molar ratio of 2:1:2, the Mannich base, VIa, with zinc chloride and concentrated aqueous hydrochloric acid (analogously, for condensations

Expt.	Crude Polymer		Anal. found ^b for crude polymer				
no.	$\overline{M}_n$	M.p., °C.ª	C, %	Н, %	Fe, %		
1	4,150	150 ^d	66.44	5.47	27.51		
<b>2</b>	9,800		66.66	5. <b>57</b>	27.78		
3	4,900	$170^{d}$	66.78	5.30	27.68		
4	3,200	$140^{d}$	66.80	5.25	27.72		
5	1,320	130	67.25	5.33	24.31°		
6	3,150	$150^{d}$	66.62	5.21	27.62		
7	5,850	155	66.98	5.09	27.78		
8	1,780	200 ^f	66.30	5.42	25.79 ^g		
9	4,850	160 ^d	67.08	5.22	27.43		
10	5,750	$170^{d}$	66.79	5.24	27.82		

TABLE II

^a Upper limiting value of melting range.

^b Anal. Calcd. for III: C, 66.71%; H, 5.09%; Fe, 28.20%.

^c Up to 0.8% low for higher molecular compounds. See experimental part.

^d Partial melting.

• Impure; contains 0.52% N.

' Sintering only.

^s Impure; contains 1.86% Cl.

of the hydrochloride VII with zinc chloride, the molar ratio employed was 2:1). The temperatures applied ranged from 150 to 180°C., preferably 170°C., with total heating times of 3–7 hr. Upon suitable separation from both the dimethylamine salt VIII (see below) and traces of cross-linked material, the crude polymer was obtained as a yellow powdery solid in yields of 85–95%, with number-average molecular weights  $\overline{M}_n$  in the range of 4000–8000. The first two experiments summarized in Table

tur		Conce	ntrations	centrations of reactants, mole	s, mole		Temp	Time	polymer,	
no.	VIa	III	XI	$ZnCl_2$	HCI	H ₂ O	°C.	hr.	theory	HCl introduced as:
г	I	1.0	1	0.5	1	Ţ	170	33	84.1	Hydrochloride of Man- nich base
0	1.0	ľ	1	0.5	1.0	3.305	170	7	93.3	38% Hydrochloric acid
e	1.0	1	1	0.5	1.1	3.635	155	1	84.5	38% Hydrochloric acid
4	1.0	1	1	0.5	0.5	1.654	170	11	65.0	38% Hydrochloric acid
ũ	1.0	l	1	0.2	0.4	1.323	170	11	25.1	38% Hydrochloric acid
9	1.0	1	!	0.5	1	3.305	170	11	61.6	ZnCl ₂ (hydrolysis)
7	1.0	1	I	1.0	i	1.0	170	10	82.3	ZnCl ₂ (hydrolysis) ^a
s	1.0	I	l	0.5	I	1	170	15	28.7	1
6	1	I	1.0	1	1	1	170	2	92.2	Amorphous IX
10	1	1	1.0	I	1	1	170	7	90.0	Crystalline IX

TABLE I

# FERROCENE-CONTAINING POLYMERS. V 1503

I are representative examples of both procedures discussed. The pertinent analytical data for the crude polymers are given in lines 1 and 2 of Table II. In both instances, the elemental analyses show satisfactory agreement with structure III.

Slight increases in the concentration of HCl over the stoichiometric limits, while resulting in essentially unchanged yields and compositions, led to noticeable reductions in the overall heating time, as is demonstrated by experiment 3. At the same time, however, increasing crosslink formation and even decomposition of the ferrocene unit was observed, necessitating careful control of the proceeding condensation to ensure termination at the point of optimum content of soluble polymer. With HCl concentrations increasing well above the 1.1 mole level (for every mole of Mannich base), the yield in soluble polymer dropped progressively in favor of crosslinked matter and decomposition products, to reach near-zero level with a twofold molar excess of HCl after 2 hr. at a temperature as low as 130°C. On the other hand, with concentrations of both or either one of the catalyst components reduced below the 2:1:2 ratio, correspondingly decreased yields and molecular weights were observed even at considerably prolonged reaction periods. In addition, the condensation products frequently showed deviations in elemental composition from that of structure III. Typical experiments demonstrating these observations are listed in Tables I and II as experiments 4, 5, and 8. The last-named experiment was conducted with the use of zinc chloride as the sole catalyst. If, in this instance, water was added in concentrations of 0.5-3.5 mole/ mole of Mannich base, run 6 being a typical example, considerably improved yields were observed, coupled with good agreement between found and calculated composition. Here, the amount of HCl required as cocatalyst was probably generated by partial hydrolysis of the zinc salt. Consistent with this view, still further yield improvements were achieved by employing an equimolar ratio of Mannich base, zinc chloride, and water (No. 7) so as to establish approximately the same 2:1:2 stoichiometry of VIa, ZnCl₂, and HCl as employed in examples 1 and 2. The hydrolysis of zinc chloride was confirmed in experiments 4, 5, 6, and 7 by the isolation of basic zinc chloride, ZnCl₂·4Zn(OH)₂, identified by x-ray diffraction.

For analytical purposes, in several instances the crude polycondensation products were subdivided into fractions of improved monodispersity. This was accomplished by fractional precipitation of the chromatographically prepurified polymers in the conventional manner. Each fractionation series was so conducted as to bring the total number of fractions to 12–15. Individual  $\overline{M}_n$  values of fractions thus obtained were in the range of 1500–20,000. The analytical data on 12 subfractions of a typical polymer batch are collected in Table III, along with melting points,  $\overline{M}_n$ , and weight fraction. Again, agreement in elemental composition with structure III is demonstrated for all fractions, as was previously shown for the unfractionated polymers. In particular, the constancy of the composition with

Fraction		М.р.,"	Weight	1	Anal. Found	<b>l</b> b
no.	$\overline{M}_n$	°C.	fraction, % ^c	C, %	Н, %	Fe, %
1	19,900		9.1	<b>66.5</b> 0	5.20	27.85
<b>2</b>	15,700		11.6	66.79	5.15	27.59
3	12,200	_	12.2	66.83	5.09	27.80
4	10,100	_	8.9	66.67	5.16	27.95
5	9,000		5.1	66.51	5.08	27.76
6	7,900	200e	13.2	66.97	5.33	27.97
7	6,400	200e	4.9	66.71	5.07	28.01
8	4,850	170–200°	8.8	66.49	5.22	28.07
9	3,250	160-175 ^f	11.1	66.66	5.14	27.91
10	2,940	160 - 165	6.8	66.89	5.20	28.28
11	2,260	155	4.6	66.99	5.31	27.83
12	1,710	150	3.7	66.60	5.08	28.13

TABLE III

" Upper limiting value of melting range.

^b Mean values from duplicate determinations. Anal. Calcd. for III: 66.71%; H, 5.09%; Fe, 28.20%.

 $^{\circ}$  In % of total weight of fractions collected. Evaporation residue from final mother liquor, mainly consisting of decomposition products (<5% of initial polymer weight. Only partially soluble in benzene) is not included in this compilation.

^d Up to 0.8% low for higher-molecular compounds. See experimental part.

° Sintering only.

f Partial melting.

varying molecular weight, as required for III, becomes apparent from this tabulation.

In conformity with these analytical findings, the polymer did not differ in appearance and properties from the polycondensation product III of hydroxymethylferrocene.¹ While the crude polymer, due to mutual depression by its polyhomologous constituents, showed partial melting in the 130–160°C. range, the fractionated material, with the exception of the lower members, was no longer fusible within the temperature range investigated (up to  $300^{\circ}$ C.). The infrared spectra of the fractionated and unfractionated polymer, within comparable molecular weight ranges, proved to be superimposable with those of polymer samples derived from the carbinol I, showing absorption characteristic of the substituted ferrocene system and the methylene bridging unit as discussed previously¹ at greater length.

Employing a number of sufficiently monodisperse fractions, a viscositymolecular weight relationship was established. To this end, dynamic viscosities  $\eta$  were measured at different concentrations in benzene solution, from which in the usual manner the intrinsic viscosity  $[\eta]$  was derived. In Figure 1, the  $[\eta]$  values are plotted on a log-log scale against the numberaverage molecular weight. The graph obeys a common Mark-Houwink relation of the following type:

$$[\eta] = 8.2 \times 10^{-4} M^{0.40}$$

For comparison, the plot contains three points determined on fractions of the hydroxymethylferrocene polymer. The points, depicted by filled-in

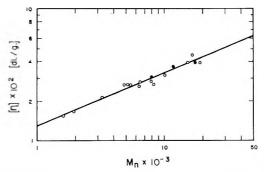


Fig. 1. Intrinsic viscosity  $[\eta]$  vs. number-average molecular weight  $\overline{M}_n$  for polymer III prepared by condensation of: (O) N,N-dimethylaminomethylferrocene; ( $\bullet$ ) hydroxymethylferrocene.

circles, show satisfactory coincidence with the curve, thus giving further evidence for identity of both polymer series III in their essential structural features. The low value of the exponent in the above relationship suggests the polymeric molecules to be more globular than rodlike in shape, as was earlier concluded for a related polymer series.¹ Such globular shape, brought about by side-chain formation, is further substantiated by spectroscopic data (below).

Assuming an ionic mechanism involving electrophilic attack by cationic species of the type V, the resulting polymer backbone is unlikely to be composed of building units strictly identical with respect to the relative substituent positions. Rather, as in the case of polymer III derived from carbinol, one has to assume a mixed structure in which isomeric recurring units as represented by the three segment formulae II are randomly distributed along the chain. Aside from steric influences, these orientations are probably governed primarily by inductive and hyperconjugative effects resulting in homoannular activation and, hence, predominant homoannular substitution along the backbone (steric factors would suggest slight predominance of the 1,3-pattern⁴⁻⁸).

With increasing chain length and correspondingly diminishing concentration of monosubstituted ferrocenyl endgroups an increasing extent of branching should be expected,¹ with branch points for steric reasons appearing prevailingly on heretofore unsubstituted "hetero" rings (see below). In order to demonstrate this expected decreasing availability of unsubstituted rings with growing molecular weight, the per cent homoannularity was determined spectroscopically for 15 fractions of different molecular weight following a previously described procedure¹ based on a quantitative evaluation of the  $9-\mu$  band.⁹ The fractions were randomly selected from various fractionation runs, employing polymer batches obtained under the experimental conditions of runs 1–4 and 7 of Table I. The per cent homoannularity is defined as the ratio, in per cent, of the number of ferrocene units bearing an unsubstituted cyclopentadienyl ring

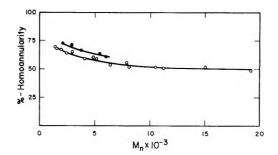


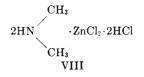
Fig. 2. Per cent homoannularity vs. number-average molecular weight  $\overline{M}_n$  for polymer III prepared by condensation of: (O) N,N-dimethylaminomethylferrocene; ( $\bullet$ ) hydroxymethylferrocene.

to the total number of ferrocene units in a given molecule. Figure 2 presents a plot of the values found as a function of  $\overline{M}_n$ .

It can be seen from this graph that early prevalence of homoannularity in the backbone is indeed quickly offset by a growing extent of branching via hetero-ring substitution as observed in the analogous curve for the hydroxymethylferrocene polymer¹ replotted in Figure 2 for comparison.* In the idealized structure III this branching effect was not taken into account.

# **Dimethylamine Salt VIII and Adduct IX**

The requirement, discussed above, for a 2:1:2 molar ratio of Mannich base, ZnCl₂, and HCl to achieve optimum polycondensation conditions strongly suggests that ZnCl₂ and HCl, if used in concentrations not exceeding the stoichiometry, rather than functioning as catalysts in the strictest sense of the word, be considered as reactants that are consumed during the process of condensation. In support of this view, it was possible to isolate from the final reaction mixtures a saltlike by-product in 75–85% yield, for which elemental analysis was in agreement with the composition VIII of an adduct of dimethylamine, ZnCl₂, and HCl in the molar ratio 2:1:2. For this complex in its crystalline state (investigated as protio- and deuterocompound), chemical, infrared, and NMR spectroscopic evidence points to the ionic structure of dimethylammonium tetrachlorozincate.



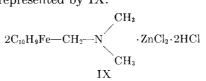
In aqueous solution, the salt was found to dissociate into the dimethylammonium cation and the tetrachlorozincate anion following eq. (1). Molecular weight determinations conducted in ethanolic solution were

^{*} The upward shift of this curve suggests a lower degree of branching for the hydroxymethylferrocene polymer as compared to the Mannich base condensation product, which may be the result of the substantially milder reaction conditions applied  $(0.75-1.5 \text{ hr. at} 110-125 ^{\circ}\text{C}. \text{ compared to } 1-11 \text{ hr. at } 155-170 ^{\circ}\text{C}.)$ 

consistent with this ionization scheme, the found  $\overline{M}_n$  value being little higher than one-third of that calculated for the undissociated compound, which suggests the tetrachlorozincate dissociation equilibrium ( $\operatorname{ZnCl}_4^{2-} \rightleftharpoons$  $\operatorname{Zn}^{2+} + 4 \operatorname{Cl}^-$ ) to be far to the left.

$$2HN \underbrace{CH_{3}}_{CH_{3}} \cdot ZnCl_{2} \cdot 2HCl \rightleftharpoons 2 \begin{bmatrix} CH_{3} \\ H_{2}N \\ CH_{3} \end{bmatrix}^{+} + [ZnCl_{4}]^{2-}$$
(1)

This high-yield formation of by-product VIII, pointing to the possibility of intermediary occurrence of defined Mannich base adducts of analogous composition, prompted an investigation of the reaction products of polycondensation experiments that were terminated prematurely. It was felt that the interception and characterization of such intermediates would shed some light upon the mechanism of polycondensation. From reactions initiated as in examples 1 and 2 of Table I and interrupted at an early stage of condensation, it was indeed possible to isolate in yields up to 85% an x-ray-amorphous, glassy compound which could be slowly dissolved at room temperature in water or methanol (heating resulted in partial hydrolvsis) to crystallize from these solutions as yellow, nonhygroscopic prisms exhibiting a defined melting point and x-ray diffraction pattern. Elemental analyses and molecular weight determinations in 2-butanone (nonpolar solvents such as dibromomethane resulted in association) showed this compound in its amorphous, i.e., supercooled melt form as well as in its crystalline state to be composed in a 2:1:2 ratio of starting material VIa,  $ZnCl_2$ , and HCl as represented by IX.



Consistent with this adduct composition, crystalline IX was also obtained directly by interaction of hydrochloride VII with zinc chloride in methanolic solution. The adduct was found to self-condense in the melt phase in the absence of any additional catalyst, giving polymer III in the same high yields (runs 9 and 10 of Tables I and II) as obtained by employing the 2:1:2 combination of VIa, ZnCl₂, and HCl. In polar solvents IX dissociates into protonated Mannich base and tetrachlorozincate anion [eq. (2)], as was shown by chemical reactions, molecular weight measurements in ethanol, and proton magnetic resonance data.

$$2 C_{10}H_{9}Fe-CH_{2}-N$$

$$CH_{3}$$

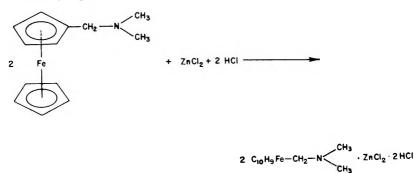
$$C$$

From this dissociation behavior one would, in analogy with the dimethyl-

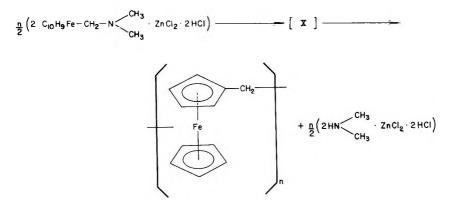
ammonium salt VIII, assume an N,N-dimethyl(ferrocenylmethyl)ammonium tetrachlorozincate structure. However, while for the compound in the dissolved state (chloroform) such ammonium structure is indeed indicated by the strong and very broad infrared absorption near  $3.7\mu$ , infrared data on KBr pellets of the crystalline or amorphous compound are inconsistent with N protonation in the solid state (lack of absorption in the NH⁺ stretching region at  $3.8-4.2\mu$ , where the ammonium salt VII absorbs strongly). Possibly, coordinate covalent N  $\rightarrow$  Zn bonding is involved here, as would be supported by the ease of self-polycondensation of IX in contrast to the indifferent VII or corresponding Mannich basehydrochloric acid mixtures.

#### **Reaction Mechanism**

On the basis of (1) the 2:1:2 ratio determined as optimum in the polycondensation of Mannich base,  $ZnCl_2$ , and HCl, (2) the isolation of the tetrachlorozincate VIII, (3) the interception, in high yields, of adduct IX, and (4) the capability of the latter intermediate to undergo nearly quantitative polycondensation to give III, it is now possible to draw some plausible conclusions regarding the overall mechanism of polycondensation. In the first stage, the three components interact to form adduct IX as depicted by eq. (3).



The second phase of the reaction, represented in simplified, schematic form by eq. (4), involves the overall sequence of ionization, propagation, and termination steps leading to polymer III and by-product VIII.



Considering the low probability of simultaneous ionization at two sites in the same molecule of IX, the generation of metallocarbonium ions Va from this adduct is likely to proceed in two steps. This necessarily leads to the assumption of intermediary occurrence of an additional complex of the overall composition X arising from IX as a result of the first ionization step. In eq. (4) the possible involvement of the hypothetical adduct X (work on the isolation of which is in progress) has been taken into account.

$$\begin{array}{c} C_{10}H_{3}Fe-CH_{2}-N \\ CH_{3} \\ CH_{3} \\ CH_{3} \\ CH_{3} \\ CH_{3} \\ CH_{3} \end{array} \\ CH_{3} \\ CH_{3$$

For cations V formed from IX and X, and later also from corresponding polyhomologs of these two intermediary complexes, it would appear reasonable to assume further reaction in much the same manner as in the polycondensation of ferrocenyl carbinol.¹ These cations, mononuclear initially (Va) and polynuclear in an advanced stage (Vb), may undergo reaction by any of the three following steps: (1) nuclear substitution of complexes IX and X and their polyhomologs; (2) self-substitution by the cation's carbonium site on the penultimate ferrocene unit; (3) nuclear substitution of nitrogen-free polymer. Step 1, a growth reaction, would lead to polymeric complexes polyhomologous to IX and X (in reactions employing ZnCl₂ and HCl in concentrations insufficient for these components to combine with the entire starting amount of VIa as adduct IX, free polynuclear Mannieh base species VIb as well as complexes different from polyhomologs of IX and X may also arise). The self-substitution of step 2 would result in the formation of a terminal double-bridged segment of one of the types IV and, hence, would give rise to polymer species devoid of amino groups (for steric reasons, this self-substitution step is restricted to those cationic species exhibiting either a 1,2- or a 1,1'-disposition of the substituents on the last ferrocene unit, whereas 1,3-orientation precludes such intramolecular attack); being a nongrowth reaction, it would thus eliminate the terminal  $\alpha$ -carbon atom of the cation as a site of further reaction.* Step 3, again, is a growth reaction leading to higher polyhomologs of the nitrogen-free polymer species resulting from step 2.

In the initial phase of polycondensation, step 1 must prevail. However, as elimination of amino groups proceeds (these groups being involved in

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^{*} For cations Va generated from I in sulfuric acid medium, Rinehart and co-workers¹⁰ demonstrated a reaction course leading to the diferricinium cation of 1,2-diferrocenylethane (related reactions involving the ferrocenylphenylcarbinyl cation have been discussed by McEwen et al.^{11,12}). An analogous reaction course involving cations Va or Vb could be visualized as an additional termination step in the present case, giving rise to polymeric ethane derivatives with the two ferrocene units adjacent to the ethyl bridge existing in the ferricinium state. However, in reactions of the present type conducted in the melt phase the instantaneous concentrations of Va and Vb are probably too low to allow for dimerization of these cations in their mesomeric radical ion forms. In accord with this assumption, no chlorine (or hydroxyl generated therefrom through hydrolysis) was ever detected analytically in the polymeric end products.

the formation of VIII), polymeric Mannich base complexes created in this first step, while showing a growth in molecular weight, decrease in concentration. Consequently, further cation reaction must progressively occur via the remaining two steps, until Mannich base complexes are no longer available for ionization and all polymeric species present in the melt consist essentially of nitrogen-free products of the composition III. Further growth by step 3 of the nitrogen-free polymers formed in the course of step 2 may arise from substitution on any one ferrocene unit of the polymer chain including the terminal ferrocenylene group created by step 2 as part of the double-bridged segment.

In all cases of endgroup substitution, the result is linear chain extension. In more advanced stages of polycondensation, however, as the concentration of endgroups is reduced, the statistical probability for cation attack on internal ferrocenylene units with resulting side-chain formation should increase. The prevailing 1,3-substitution pattern lacks any sterically favored sites on the "homo" rings. Therefore, additional substitution will predominantly occur on unsubstituted "hetero" rings, thus resulting in the observed decrease of the per cent homoannularity with rising molecular weight. As in the previous work,¹ the asymptotic trend of the curve in Figure 2 may be interpreted in terms of a balance of the growth process between the initiation of branches and their early linear growth.

## **EXPERIMENTAL**

### Materials and General Analytical Procedures

The procedure described by Lindsay and Hauser² was employed for the preparation of N,N-dimethylaminomethylferrocene (VIa), b.p. 130– 132°C./3 mm. The hydrochloride VII, fine yellow needles infusible up to 300°C., was prepared in 80.5% yield from VIa and HCl in methanol.

ANAL. Calc.: Cl, 12.73%; Fe, 20.06%. Found: Cl, 13.02%; Fe, 20.40%.

All other materials and solvents were obtained from commercial sources and were purified as described.¹ Iron determinations were performed by titration of Fe²⁺ with dichromate; polymeric samples required a HNO₃-HClO₄ mixture for complete dissolution. Values were usually 0.5-0.8%low for high molecular compounds requiring long acid digestion times. Carbon, hydrogen, nitrogen, and chlorine analyses were conducted by G. I. Robertson, Jr., Florham Park, N. J. Viscosity and molecular weight measurements were conducted as in the earlier paper.¹ For infrared recording, a Perkin-Elmer Model 521 double-beam spectrophotometer equipped with grating optics was used. X-ray powder diffraction diagrams were recorded with a Norelco x-ray diffractometer, using vanadium-filtered K $\alpha$  chromium radiation. Principal interplanar spacings, d are listed in decreasing order of intensity within the  $2\theta$  range 10-35. High-resolution NMR spectra were obtained at 25°C. with a Varian Associates, Model A60, NMR spectrometer operating at 60 Mcycle/sec. over a sweep width of 500 cycle/sec. Chemical shifts,  $\tau$ , are given in ppm relative to tetramethylsilane (TMS) as internal standard with an assigned

value of 10.00 (external standard for recordings in H₂O or D₂O solution). Coupling constants J are given in cycles/second with average spread  $\pm$  0.2 cycle/sec. at 100 cycle/sec. sweep width ( $\pm$  2 cycle/sec. for the quadrupole coupling signals).

## **Polycondensation Reactions: Formation of III**

With the use of the equipment described earlier¹ for ferrocenyl carbinol condensations, the components were heated with stirring under nitrogen for reaction periods and at molar ratios and temperatures as specified in Table I. The reaction products were freed by water extraction from excess  $ZnCl_2$  and tetrachlorozincate VIII.

VIII formed colorless prisms, m. p. 173-176°C., from methanol-ether.

ANAL. Calcd. for C₄H₁₆Cl₄N₂Zn: C, 16.05%; H, 5.39%; Cl. 47.37%; N, 9.36%; Zn, 21.84%; mol. wt. 299. Found: C, 16.48%; H, 5.57%; Cl, 47.02%; N, 9.51%; Zn, 20.95%;  $\overline{M}_{n}$ , 120 (methanol). X-ray diffractogram: 7.10, 5.69, 6.04, 4.23, and 3.90 A.

The products were reprecipitated from benzene solution by 95% aqueous isopropanol. Concentration of the mother liquor in each case gave a small second polymer crop. The combined portions were washed with isopropanol and were dried for 10 days at  $60^{\circ}$ C. *in vacuo*. Yield and analytical data for the products thus obtained are recorded in Tables I and II. The polymer showed the appearance, solubility, and spectral behavior of the hydroxymethylferrocene polycondensation product described previously.¹

A number of subfractions was carried out in the conventional manner¹ to obtain fractions of enhanced monodispersity for the plots in Figures 1 and 2. For the 12 subfractions of a typical series the analytical data are collected in Table III. The solvents and precipitants used in these subfractions were deaerated, and all operations were conducted under a nitrogen blanket to prevent oxidation. Fractions prepared without observing these precautions were tan to brown in color and showed decreased solubility in carbon tetrachloride, carbon disulfide and even benzene; the infrared spectrum exhibited carbonyl bands of medium intensity near 6.1  $\mu$ . This oxidation sensitivity was enhanced with rising molecular weight. Typical elemental analytical findings for a partially oxidized fraction with  $\overline{M_n} = 7000$  ( $\overline{M_n}$ determined on benzene-soluble portion, 71.2% by weight) are as follows: C, 63.14%; H, 5.05%; Fe, 24.68%.

## **Formation of Adduct IX**

The reactants, Mannich base (VIa), anhydrous zinc chloride, and 38% aqueous hydrochloric acid, were heated for 15 min. in a 2:1:2 molar ratio at 170°C. as described before. Extraction of the melt with boiling chloroform and precipitation by ether gave crude IX (84.3% yield), which was purified by reprecipitation in the same manner. The dried (20 days at 50°C. in high vacuum) complex was a pulverizable, x-ray-amorphous solid; m.p. 80–100°C.

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ANAL. Calcd. for  $C_{26}H_{36}Cl_1Fe_2N_2Zn$ : C, 44.90%; H, 5.22%; Cl, 20.39%; Fe, 16.06%; N, 4.03%; mol. wt. 695.5. Found: C, 44.68%; H, 5.42%; Cl, 20.71%; Fe, 15.91%: N, 3.93%.  $\overline{M}_n$ , 1340 (dibromomethane, average of 3 determinations); 620 (2-butanone) 230 (ethanol).

The compound was similarly prepared (79.5% yield) by heating the wellground mixture of VII and  $\text{ZnCl}_2$  (molar ratio 2:1) for 6 min. at 170°C. and working up the melt as described above.

Crystallization from water yielded the adduct as orange prisms, m.p. 128-130°C.

ANAL. Found: C, 44.59%; H, 5.34%; Cl, 19.89%; Fe, 16.54%; N, 4.01%; Zn, 8.95%;  $M_n$ , 1270 (dibromomethane); 660 (2-butanone); 240 (ethanol). X-ray diffractogram: 5.67; 4.48; 5.95; 5.15; 4.92; 3.88; 3.50 A. Allotropic modification from 2-butanone: 4.27; 4.56; 5.40; 3.51 A.

The same crystalline compound was also directly obtained from a 2:1 molar mixture of VII and  $\text{ZnCl}_2$  in methanolic solution. The crystals dissolved readily in water and methanol, less so in higher aliphatic alcohols, ketones and chlorohydrocarbons, and were practically insoluble in ether, hexane and benzene. From aqueous solution, AgNO₃ immediately precipitated chloride ion (titration of the aqueous solution with 0.1N AgNO₃ solution against sodium chromate gave 20.71% Cl). On addition of KOH, basic zinc chloride precipitated with concomitant liberation of VIa (picrate, m.p. and mixed m.p.² 175°C.

ANAL. Calcd. for C19H20FeN4O7: N, 11.87%; Found: N, 11.68%.

The same picrate was directly obtained from methanolic solution of IX by addition of picric acid.)

The proton magnetic resonance spectra recorded on aqueous solutions of IX, practically identical with those of VII, gave proton signals ( $\tau$  values in parentheses) for the substituted ferrocene ring (5.66 ppm), unsubstituted ferrocene ring (5.78 ppm), methylene (5.91 ppm), and methyl (7.32 ppm) groups in the expected 4:5:2:6 area ratio. In common with VIII, the annonium proton failed to give an individual signal owing to rapid exchange with the solvent, and both the methyl and methylene peaks emerged as singlets. On acidification of the aqueous (and also methanolic) solution ( $5.0 \times 10^{-3}N$ ) with HCl, proton exchange was sufficiently suppressed to give rise to doublet splitting of the methyl signal (J = 4.2 cycle/sec.). However, in contrast to VIII (triplet centered at  $\tau = 2.25$  ppm, with J = 52 cycle/sec.), the conditions of temperature and concentration ( $25^{\circ}$ C., 16% w/v solution) applied did not permit triplet formation due to N¹⁴ quadrupole interaction,¹³ nor was an N-H singlet observed (probably merged with O-H).

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### Résumé

L'auto-condensation de la base de Mannich ferrocényle, le N,N-diméthyl aminométhylferrocène, en présence du système ZnCl₂-HCl comme catalyseur dans la phase fondue, conduit à des polymères solubles, contenant des unités ferrocénylènes intercalées de groupes méthylènes. Les produits de condensation bruts fournissent des poids moléculaire moyens en nombre de 4000 à 8000. Les analyses élémentaires et la spectroscopie infrarouge, aussi bien que les résultats viscosimétriques, montrent que la structure est essentiellement identique à celle du polymère dérivé de l'hydroxyméthyl ferrocène, précédemment décrit dans une communication antérieure. Le rapport molaire optimum des réactifs (base de Mannich, ZnCl₂ et HCl) est 2:1:2. Le tétrachlorozincate de diméthyl-ammonium a été isolé comme produit secondaire, et un complexe intermédiaire, composé de la base de Mannich, du ZnCl₂ et HCl, a été isoléda ns le rapport 2:1:2, durant la polycondensation. Certaines conclusions concernant le mécanisme sont soumises à discussion.

#### Zusammenfassung

Die Selbstkondensation der Ferrocenyl-Mannichbase, N,N-Dimethylaminomethylferrocen, in Gegenwart eines ZnCl₂-HCl-Katalysatorsystems in der Schmelze führt zu löslichen Polymeren mit methylengruppenverknüpften Ferrocenylenbausteinen. Das robe Kondensationsprodukt besitzt Zahlenmittel-Molekuarlgewichte im Bereich 4000-8000. Elementaranalyse und Infrarotspektroskopie sowie viskosimetrische Daten zeigen, dass die Struktur im wesentlichen mit derjenigen des in einer früheren Mitteilung beschriebenen, von Hydroxymethylferrocen abgeleiteten Polymeren identisch ist. Das 2:1:2-Dimethylammoniumtetrachlorzinkat wurde als Nebenprodukt isoliert und ein Komplex aus Mannichbase, ZnCl₂ und HCl im gleichen 2:1:2-Verhältnis wurde als Zwischenprodukt während der Polykondensation abgefangen. Einige mechanistische Gesichtspunkte werden diskutiert.

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# Hydrodynamic Friction Coefficients for Cellodextrins in Water*

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#### **Synopsis**

The diffusion coefficients for the cellobiose through cellohexaose members of the cellodextrin series were determined in water. The molecular friction coefficients calculated on the basis of the Einstein diffusion equation can be represented by,  $\zeta_N = N\zeta_a + 2\zeta_e$ , where  $\zeta_a$  is the monomeric friction coefficient of an anhydroglucose unit,  $\zeta_e$  is a friction coefficient assigned to a terminal monomer unit due to its additional hydrodynamic surface, and N is the degree of polymerization. For the cellodextrins,  $\zeta_a$  is  $1.25 \times 10^{-9}$ dyne-sec./cm., and  $\zeta_e$  is  $2.42 \times 10^{-9}$  dyne-sec./cm. The monomeric friction coefficient of the anhydroglucose unit was found to agree with the value calculated from literature data on the diffusion of cellulose in cadoxen. The calculations were based on the Ptitsyn-Eizner theory for the hydrodynamic behavior of the "wormlike" chain. The partial specific volumes of the cellodextrins were found to decrease from glucose to cellotriose and then to increase from cellotriose to cellohexaose.

## INTRODUCTION

Marrinan and Hermans¹ have analyzed viscosity, sedimentation, and light-scattering data on cellulose derivatives in dilute solution and have written the expressions derived by Debye and Bueche² and Kirkwood and Riseman³ for sedimentation and intrinsic viscosity in a form which is independent of the applicability of Gaussian statistics. The modified Kirkwood-Riseman equations were found to be compatible with existing data and acceptable values for the size of the monomer units were obtained. The theory of Kurata and Yamakawa^{4,5} which takes into account both intramolecular and intermolecular interaction between chain segments is also well suited to the structural interpretation of experimental data. Finally, Ptitsyn and Eizner^{6,7} have derived expressions for the intrinsic viscosity and the friction coefficient of the "wormlike" chain⁸ and have shown that reasonable values for the persistence length and radius of the momomer unit can be obtained for cellulose derivatives.

The monomeric friction coefficient plays an important role in all of the hydrodynamic theories. In the past, the treatments of Debye and Bueche and Kirkwood and Riseman have lead to values of the monomeric friction

^{*} This work was supported by a grant from the Pioneering Research Program which is administered by the Pioneering Research Committee of The Institute of Paper Chemjstry on behalf of several sponsors.

coefficient that are too small.^{9,10} At least part of the difficulty is due to the manner in which the hydrodynamic theories are applied.¹

In their work on sodium carboxymethyl cellulose, Sitaramaiah and Goring¹¹ used the computational procedure suggested by Marrinan and Hermans to determine the monomeric friction coefficient which was compared with the friction coefficient estimated from the diffusion coefficient of sucrose in water. A more acceptable estimate would be desirable; however, suitable diffusional data are not as yet available.

There is a distinct need for diffusion measurements on low molecular weight oligosaccharides in the molecular weight region where hydrodynamic shielding is unimportant. In the present work the diffusional behavior of the cellobiose through cellohexapse members of the cellodextrin series is examined in an attempt to obtain an acceptable value for the monomeric friction coefficient of an anhydroglucose unit in water.

# **EXPERIMENTAL**

### Materials

Two cellodextrin series containing the cellobiose through cellohexaose members were obtained through the courtesy of N. S. Thompson and W. Bliesner. In addition, Eastman cellobiose was used in certain experiments.

The cellodextrins were isolated by chromatographic separation on a column containing an adsorbent composed of a 50–50 mixture of charcoal (Darco G-60) and Cellite (Cellite 545). The adsorbent was pretreated with stearic acid-ethanol solutions^{12,13} to prevent irreversible adsorption of the cellodextrins.

Whatman cellulose powder was hydrolyzed with fuming hydrochloric acid,¹⁴ neutralized with sodium bicarbonate, and filtered to remove salts and undissolved materials. The filtrate containing the cellodextrins was added to the column and washed with distilled water to remove salts and glucose. The cellodextrins were eluted with a solution consisting of 40 vol.-% ethanol in water. The isolated sugars were then purified by the procedure described by Wolfrom and Dacrons.¹⁵

At one point in the preparation, the samples were inadvertently subjected to bacterial attack. The solutions were heated to destroy the bacteria and the sugars were recrystallized to constant melting or decomposition points. Fringe analysis¹⁶ from subsequent diffusion experiments indicated that all samples were of high purity.

### Partial Specific Volume and Diffusion

Several sources of water were used during the course of this work. Partial specific volume measurements were conducted in ordinary distilled water, and the diffusion measurements on cellobiose were conducted in distilled water obtained by distilling deionized water containing alkaline potassium permanganate. All other experiments were conducted in water prepared according to the procedure described by Bauer.¹⁷ All solutions were prepared by weight.

#### **CELLODEXTRINS**

Density determinations were conducted at  $30.00 \pm 0.005$  °C. in Sprengle bottles. Partial specific volumes were calculated from density measurements by means of Kraemer's formula.¹⁸

Diffusion experiments were conducted in free diffusion in a Spinco Model H electrophoresis-diffusion instrument using 2-ml. and 11-ml. Tiselius cells, the Rayleigh diffusiometer, and green light from a G. E. H 100 A-4 mercury vapor lamp. All experiments were conducted with the cellodextrin solution diffusing against pure water. Fringe patterns were recorded on Eastman type M photographic plates. The fringe fraction was determined from photographs taken during the boundary sharpening procedure. The fringe fraction and fringe positions were measured with a Gaertner traveling microscope.

Fringes were paired according to the procedure of Longsworth^{19,20} and diffusion coefficients, D, were calculated from

$$(x_{J-j} - x_j)/2MZ^* = 2(Dt)^{1/2}$$
(1)

where  $x_{J-j}$  and  $x_j$  are fringe locations,  $Z^*$  is the reduced cell coordinate, M the magnification factor, and t the time. Zero time corrections were applied by using eq. (2):

$$D' = D(1 + \Delta t/t') \tag{2}$$

where t and t' are the true and experimentally observed diffusion times, respectively, and D and D' are, respectively, the true and slightly erroneous diffusion coefficients based on t and t'.

Computations were carried out on an IBM 1620 computer. Values of D' were calculated from eq. (1) on the basis of experimental times t' and then used to calculate the zero-time correction from a least-squares treatment of eq. (2). The zero-time correction was then applied to the original times and the entire calculational procedure repeated until the zero time correction was less than 1 sec.

The refractive index difference,  $\Delta n$ , across the boundary was calculated from the equation,

$$\Delta n = J\lambda/a,\tag{3}$$

where J is the total number of fringes, a is the cell thickness, and  $\lambda$  is the wavelength of the monochromatic light. A cell thickness of a = 0.6457 cm. was obtained for the 2-ml. micro cell and a = 2.596 cm. for the 11-ml. standard cell. The wavelength of the monochromatic light is  $\lambda = 5462$  A.

## **EXPERIMENTAL RESULTS**

The results of the diffusion experiments on the cellodextrins in water are given in Table I and for cellobiose in aqueous 0.2958M NaCl in Table II. The diffusion coefficients are reported in terms of  $D_A$ , the diffusion coefficient based on the reduced height-area ratio along with the standard deviation for the diffusion coefficient, the total number of fringes, J, and the zero time correction  $\Delta t$ . A single cellobiose experiment was conducted in a

						Std.	
Compound	$\Delta C$ , mole/1.	$\bar{C}_{,}$ mole/l.	ſ	Δť, sec.	$D_A \times 10^6$ , cm. ² /sec.	dev. $\times 10^6$ , cm. ² /sec.	Cell size, ml.
Cellobiose	0.02824	0.01412	32.68	56.8	5.706	0.018	2
	0.01823	0.00912		42	5.713	0.016	Ultra-
							centri-
							fuge
	0.008648	0.004324	39.42	65.2	5.739	0.012	11
	0.002684	0.001342	12.24	50.2	5.944	0.060	11
Cellotriose	0.013522	0.006761	21.98	50.2	4.868	0.017	5
	0.009656	0.004828	63.91	43.5	4.864	0.009	11
	0.006126	0.003063	41.41	82.1	4.844	0.011	11
	0.001878	0.00039	13.44	73.1	4.908	0.022	11
Cellotetraose	0.010016	0.005008	87.06	117.2	4.202	0.009	11
	0.004765	0.002383	43.38	80.2	4.278	0.006	11
Cellopentaose	0.002074	0.001037	21.18	39.1	3.817	0.022	11
Cellohexaose	0.0008929	0.0004465	11.28	48.4	3.382	0.026	11

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#### CELLODEXTRINS

ΔC, mole/l.	<i>Ē</i> , mole∕l.	J	$\Delta t$ , sec.	$D_A  imes 10^6$ , cm.²/sec.	Std. dev. $\times$ 10 ⁶ , cm. ² /sec.	Cel size ml.
0.02778	0.01389	31.72	17	5.636	0.010	2
0.00832	0.00416	37.57	66	5.643	0.013	11
0.00286	0.00143	12.82	167	5.665	0.061	11

TABLE I

Spinco Model E ultracentrifuge with the use of a double-sector boundary cell and the Rayleigh optical system.

In the case of cellobiose and cellotriose, diffusion coefficients were determined as a function of concentration. For the higher members it was only possible to conduct experiments at low concentrations due to the limited quantities of material available and inherent solubility limits.

Diffusion coefficients are shown in Figure 1 as a function of concentration. For cellobiose, there is a marked increase in  $D_A$  at low concentrations. It is apparent that this behavior is sharply depressed by the addition of NaCl. It was not possible to conduct an extensive investigation in this low concentration region, since low concentrations result in low total fringe numbers, making reliable fringe analysis impossible.

The refractive index difference across the boundary may be expressed as,

$$\Delta n = K_1 \Delta C + K_2 \Delta C^2 \tag{4}$$

where  $\Delta C$  is the concentration difference in grams per milliliter. The coefficients  $K_1$  and  $K_2$  are given in Table III.

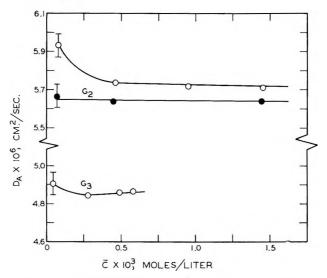


Fig. 1. Diffusion coefficients for cellobiose  $(G_2)$  and cellotriose  $(G_3)$  as a function of mean concentration in water at  $30^{\circ}$ C.; (O) measurements in water; ( $\bullet$ ) measurements in 0.2958M NaCl.

TABLE III
Difference in Refractive Index Between Cellodextrins Solutions and Water at 30.00 $\pm$
0.02°C. According to Equation (4)

Compound	$K_1   imes  10^4$	$K_2 \times 10^4$
Cellobiose	2.787	0.0073
Cellotriose	2.775	$-0.038_{6}$
Cellotetraose	2.68	$0.02_7$
Cellopentaose	2.59	
Cellohexaose	2.68	_

The results of the partial specific volume determinations are given in Table IV and Figure 2 for the cellodextrins and other sugars. The rather large error reported for the partial specific volume of cellohexaose is the result of the very low solubility of this polysaccharide in water.

In order to conduct an analysis on the effect of molecular weight on diffusion it will be necessary to neglect the increase in diffusion coefficient at low concentrations and assume that this will cause an error of only a few per cent. The diffusion coefficients,  $D_N$ , for the cellodextrin series will be taken as,  $D_1 = 7.58 \times 10^{-6}$ ,  $D_2 = 5.71 \times 10^{-6}$ ,  $D_3 = 4.87 \times 10^{-6}$ ,  $D_4 =$  $4.28 \times 10^{-6}$ ,  $D_5 = 3.82 \times 10^{-6}$  and  $D_6 = 3.38 \times 10^{-6}$  cm.²/sec., where the subscript N refers to the degree of polymerization of the cellodextrin in

TABLE IV

Partial Specific Volumes of the Cellodextrins and Other Polysaccharides in Aqueous Solution

Compound	Molecular weight	Concentration, mole/l.	Partial specific volume, ml./g.	Partial molar volume, ml./mole
Glucose ^a	180.16		0.621	111.9
Cellobiose ^b	342.30	0.03100	0.6148°	210.4
Cellotriose ^b	504.45	0.01910	0.6109°	308.2
		$0.00960_3$	0.6110°	308.2
Cellotetraose ^b	666.59	0.01497	0.6132°	408.5
Cellopentaose ^b	828.73	$0.00621_3$	0.6279°	520.3
Cellohexaose ^b	990.86		$0.63^{d}$	
Sucrose ^e	342.30		0.613	209.9
Maltose	342.30		0.6170	211.2
Raffinose ^a	594.52		0.6078	306.6
Dextran ^g			0.603 ^h	
Amylose ⁱ			0.60	-

^a Data of ref. 21.

^b Data from present work, temperature 30.00°C.

^c Estimated error  $\pm$  0.0002 ml./g.

^d Estimated error  $\pm 0.05$  ml./g.

^e Data of ref. 27.

^f Data of ref. 26.

^g Data of ref. 24.

^h Estimated error  $\pm$  0.003 ml./g.

ⁱ Data of ref. 25.

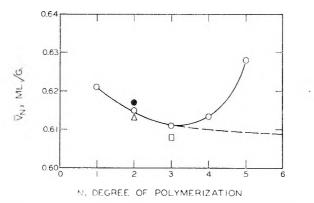


Fig. 2. Partial specific volumes of the cellodextrins and other sugars. (O) cellodextrins; ( $\bullet$ ) maltose; ( $\triangle$ ) sucrose; ( $\Box$ ) raffinose.

question. The value for glucose was obtained from the work of Gladden and Dole²¹ after correcting for viscosity and temperature differences.¹⁶

## DISCUSSION

## **Diffusion Relations**

Gosting¹⁶ has discussed a number of theoretical and empirical expressions used in the correlation of diffusion data. Only two of these will be considered here. Longworth¹⁹ has proposed the empirical equations,

$$D = A/(M^{1/3} - B)$$
(5)

and

$$D = A' / (\bar{V}^{1/_3} - B) \tag{6}$$

where A, A', B, and B' are empirical constants,  $\overline{V}$  is the partial molar volume, and M is the molecular weight. According to these equations, a plot of  $DM^{1/3}$  or  $D\overline{V}^{1/3}$  versus D should yield a straight line, as shown in Figures 3 and 4. A least-squares fit of the data results in the relations,

$$D = 28.0 \times 10^{-6} / (M^{1/3} - 2.04) \tag{7}$$

and

$$D = 25.2 \times 10^{-6} / (\bar{V}^{1/3} - 1.52) \tag{8}$$

Equations (7) and (8) fit the data to within  $\pm 5\%$  and  $\pm 2\%$ , respectively, as found by Longworth.¹⁹ The straight lines in Figures 3 and 4 represent eqs. (7) and (8), respectively. Reasonably good agreement is observed in both plots, although the agreement is somewhat better in the molar volume correlation.

It is possible to describe the molecular weight dependence of diffusion in a more fundamental manner. To do this the Einstein diffusion equation is written as

$$D_N = kT/\zeta_N \tag{9}$$

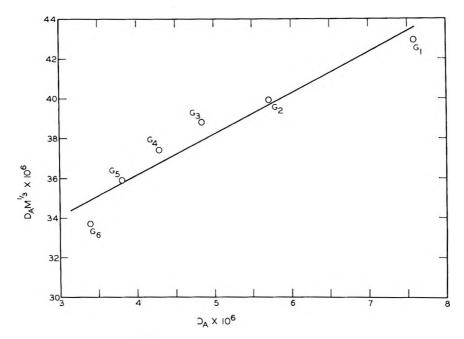


Fig. 3. The product  $D_A M^{1/3}$  as a function of  $D_A$  for the cellodextrins in water at 30°C.

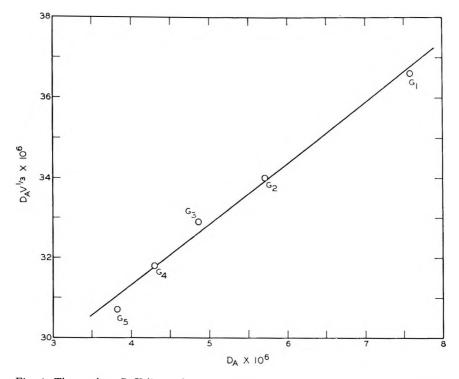


Fig. 4. The product  $D_A V^{1/3}$  as a function of  $D_A$  for the cellodextrins in water at 30°C.

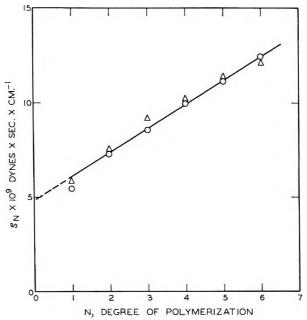


Fig. 5. Molecular friction coefficients for the cellodextrins and maltodextrins in water at  $30^{\circ}$ C.: (O) cellodextrins; ( $\Delta$ ) maltodextrins.

where  $\zeta_N$  is the friction coefficient of the molecule and the subscript N refers to the degree of polymerization. Let  $\zeta_a$  represent the friction coefficient of an anhydroglucose unit and let  $\zeta_e$  be an added frictional effect to be assigned to a terminal monomer unit due to the additional hydrodynamic surface of the end. The friction coefficient for the cellodextrin series can then be written as

$$\zeta_N = N\zeta_a + 2\zeta_e \tag{10}$$

If  $\zeta_a$  and  $\zeta_e$  are assumed to be independent of molecular weight, then a plot of  $\zeta_N$  versus N should yield a straight line as shown in Figure 5. Neglecting the diffusion coefficient of glucose, a least-squares treatment of the data indicates that the friction coefficient of the cellodextrin series in units of dyne-seconds per centimeter can be represented by

$$\zeta_N = N1.25 \times 10^{-9} + 2 \times 2.42 \times 10^{-9} \tag{11}$$

Bourne et al.²² have determined the integral diffusion coefficients of a series of maltodextrins in aqueous 0.05M glucose solutions at  $25^{\circ}$ C. After correction to  $30^{\circ}$ C. for temperature and viscosity effects, the friction coefficients for the glucose through maltohexaose members can be represented by eq. (10) with  $\zeta_a = 1.26 \times 10^{-9}$  and  $\zeta_e = 2.46 \times 10^{-9}$  dyne-sec./cm. This is in excellent agreement with the results obtained for the cellodextrins, as shown in Figure 5, where the results for both series are displayed.

The fact that the same value for the monomeric friction coefficient is obtained from both series is of considerable interest. It means that it is not necessary to differentiate between  $\alpha$ - and  $\beta$ -linkages insofar as the monomeric friction coefficient of the anhydroglucose unit is concerned.

## **Hydrodynamic Theories**

Sitaramaiah and Goring¹¹ have employed the modified equations¹ for the Kirkwood-Riseman and Debye-Bueche theories in analysis of their results on the sedimentation and diffusion of sodium carboxymethyl cellulose, CMC. For CMC in aqueous 0.1M NaCl the monomeric friction coefficient was found to be a function of the molecular weight. For the Kirkwood-Riseman theory the extrapolated value at zero molecular weight was  $\zeta_a = 1.3 \times 10^{-9}$  dyne-sec./cm., which yields a value of  $\zeta_a/\eta_0$  of 14 A., where  $\eta_0$  is the viscosity of the solvent. This is in agreement with the value of  $\zeta_a/\eta_0 = 15.6$  A. for the cellodextrins in water. The agreement, however, must be considered fortuitous in view of the fact that a constant value of  $\zeta_a$  could not be found for CMC by this procedure. The range of degree of polymerization for CMC was 202–1611, which is such that the random coil assumption of the Kirkwood-Riseman theory would be expected to fail.

In the Ptitsyn-Eizner⁶ theory which is based on the wormlike chain, the same CMC diffusion-molecular weight data can be described by a constant value of  $\zeta_a/\eta_0 = 39.6$  A. and a corresponding persistence length of 63 A. The friction coefficient is somewhat larger than that obtained for the cello-dextrins, as would be expected from the larger size of the CMC monomer unit.

From the data of Henley²³ for the diffusion of cellulose in cadoxen, the Ptitsyn-Eizner theory yields  $\zeta_a/\eta_0 = 18.3$  A. and a persistence length of 51 A. The friction factor agrees well with that obtained from the cello-dextrins and is only slightly larger, as would be expected from the increase in size due to the cellulose-cadoxen complex.

In spite of the uncertainty which arises in comparing cellulose derivatives with the cellodextrins, it would seem that the Ptitsyn-Eizner theory can lead to realistic quantitative values of the monomeric friction coefficient. At present it does not appear necessary to introduce complications of internal circulation or molecular distortion in a gravitational field¹¹ to explain the hydrodynamic behavior of cellulose derivatives.

## **Partial Specific Volume**

The partial specific volumes of the cellodextrins decrease from glucose to cellotriose where they reach a minimum and then increase, as shown in Figure 2. The initial decrease is due to the replacement of intermolecular distances with the shorter carbon-oxygen bond distances.

If  $\overline{V}_a$  is the partial molar volume of an anhydroglucose unit and  $\overline{V}_e$  is the partial molar volume associated with the end of the molecule, then the partial molar volume  $\overline{V}_N$  for the cellodextrin series can be written as

$$\bar{V}_N = N \bar{V}_a + 2 \bar{V}_e \tag{12}$$

At low N, a plot of  $\overline{V}_N$  versus N becomes asymptotic to a straight line, from which, according to eq. (12), we find that  $\overline{V}_a = 98.15$  and  $\overline{V}_e = 6.93$  ml./ mole.

The partial specific volume calculated on the basis of eq. (12) is shown as the dashed line in Figure 2. At high degrees of polymerization the partial specific volume is expected to approach a limiting value of 0.605 ml./g., which agrees well with values reported for dextran²⁴ and amylose.²⁵ It should be noted that in spite of structural differences and slight differences in hydration that the disaccharides maltose²⁶ and sucrose²⁷ compare favorably with cellobiose and the trisaccharide raffinose²⁰ compares favorably with cellotriose.

The partial specific volumes of cellotetraose and cellopentaose are significantly higher than would be expected on the basis of eq. (12). The hydration, the moles of  $H_2O$  per HO-group, is known to decrease from glucose to cellobiose²⁶ and this might be used to explain an increase in the partial specific volume. The increase, however, is most pronounced for cellotetraose and cellopentaose where the terminal anhydroglucose units are, respectively, 10.3 and 15.4 A. apart. These distances are great enough so that only minor changes of hydration with degree of polymerization would be expected. The added volume required by cellotetraose and cellopentaose is at present unexplained. Unfortunately, the solubility of cellohexaose and higher members is too low for accurate partial specific volume measurements.

We are indebted to J. E. Tostevin for permission to use the results of his diffusion experiments conducted in the ultracentrifuge. The IBM 1620 program used in the present work is due in large part to his efforts. We are also grateful to J. A. Carlson and E. O. Dillingham for assisting us in the use of the facilities of the Lou Calder Plant Biochemistry Laboratory.

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#### Résumé

Les coefficients de diffusion du cellobiose à travers les régions de cellohexaose de la série des cellodextrines ont été déterminés dans l'eau. Les coefficients de frottement moléculaire, calculés sur la base de l'équation de diffusion d'Einstein, peuvent être représentés par  $\varsigma_N = N \varsigma_a + 2 \varsigma_e$ ,  $\varsigma_a$  était le coefficient de frottement du monomère, d'une unité d'anhydroglucose, et  $\varsigma_e$  était le coefficient de frottement, attribué à l'unité monomérique terminale, due à sa surface hydrodynamique supplémentaire, N étant le degré de polymérisation. Pour les cellodextrines  $\varsigma_a$  est 1.25 10⁻⁹ et  $\varsigma_e$  est 2.42 10⁻⁹ en unités dynes  $\times$  sec  $\times$  cm⁻¹. Le coefficient de frottement monomérique de l'unité d'anhydroglucose correspond avec les valeurs calculées sur la base de données de la littérature concernant la diffusion de la cellulose dans le cadoxène Les calculs sont basés sur la théorie de Ptitsyn-Eizner relative au comportement hydrodynamique de la chaîne enpaloté statistique. Les volumes spécifiques partiels des cellodextrines diminuent du glucose au eellotriose et augmentent ensuite du cellotriose au cellohexaose.

#### Zusammenfassung

Die Diffusionskoeffizienten für Zellobiose durch die Zellohexaoseglieder der Zellodextrinreihen in Wasser wurde bestimmt. Der mit der Einstein'schen Diffusionsgleichung berechnete molekulare Reibungskoeffizient kann durch  $\zeta_N = N\zeta_a + 2\zeta_c$  dargestellt werden, wo  $\zeta_a$  der Monomerreibungskoeffizient eines Anhydroglukosebausteins und  $\zeta_c$ ein dem endständigen Monomerbaustein wegen seiner zusätzlichen hydrodynamischen Oberfläche zugeschriebener Reibungkoeffizient und N der Polymerisationsgrad ist. Bei den Zellodextrinen ist  $\zeta_a = 1,25.10^{-9}$  und  $\zeta_c = 2,42.10^{-9}$  dyn. sec.-cm.⁻¹. Der Monomerreibungskoeffizient des Anhydroglukosebausteins stimmte mit dem aus Literaturangaben über die Diffusion von Zellulose in Cadoxen berechneten Wert überein. Die Berechung beruht auf der Theorie von Ptitsyn-Eizner für hydrodynamisches Verhalten "wurmartiger" Ketten. Das partielle spezifische Volumen der Zellodextrine nahm von Glukose zu Zellotriose ab und dann von Zellotriose zu Zellohexaose zu.

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# **Poly-***α***-cyanostyrene**

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## **Synopsis**

The monomer  $\alpha$ -cyanostyrene polymerized at a very slow rate under the influence of free-radical initiators. Rapid polymerization to high molecular weight material was achieved by using anionic initiators (tri-*n*-butylphosphine and tetrakisdimethylaminotitanium). The polymer made at -78 °C. was colorless, fusible, soluble, and had a number-average molecular weight of over 5,000. The polymer prepared at 0°C. was brown, insoluble, and infusible. None of the polymer showed order in the x-ray diagram. The rate of dimerization of  $\alpha$ -cyanostyrene under a wide variety of conditions was measured. Two new derivatives of the intermediate, 3-(N,N-dimethylamino)-2-phenylpropionitrile were prepared: the methiodide, m.p. 242-245°C. (decomp.), and the picrate, m.p. 116.5-117.5°C.

The monomer  $\alpha$ -cyanostyrene is known,^{1,2} and copolymers of it with conjugate dienes have been claimed.³ Schildknecht points out that  $\alpha$ -cyanostyrene will not polymerize by itself.⁴ This note describes the preparation of high molecular weight homopolymers of  $\alpha$ -cyanostyrene via anionic initiation.

### RESULTS

Under the influence of anionic initiators,  $\alpha$ -cyanostyrene polymerizes rapidly in high yields to macromolecular substances (Table I). A diluent is required to help dissipate the heat of polymerization. The polymer prepared with the temperature initially at -78 °C is colorless, soluble [in dimethylformamide (DMF), dimethyl sulfoxide, ethylene carbonate, and N,N-dimethyl benzamide], has an intrinsic viscosity in DMF at 30 °C. of 0.30–0.66 (corresponding roughly to number-average molecular weights of 5,000–20,000), and sticks to a metal bar at 250–260 °C. The polymer prepared with the temperature initially at 0 °C. is brown, insoluble, and infusible. All polymers give amorphous x-ray diagrams as obtained and after heat treating 72 hr. at 40 °C. followed by 6 hr. at 100 °C. Polyacrylonitrile exhibits order in the x-ray diagram and is infusible on a metal bar.

Free-radical initiation of  $\alpha$ -cyanostyrene with azobisisobutyronitrile or benzoyl peroxide over the temperature range of 50–75°C. yields polymer at a very low rate of polymerization (ca. 0.02–0.21%/hr.). The traces of

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				Polymeriza	ation of α-C	Polymerization of $\alpha$ -Cyanostyrene		
	Monomer			Initiator	tor			Color channes
Solvent	concn., mole/l.	Temp., °C.	Time, hr.	Type	Concn., mole/l.	Concn., Conversion, mole/l. $\%$	Type of reaction	on adding MeOH
Toluene	2.3	-78	20	${\rm Ti}({\rm NMe}_2)_4$	0.13	51	Solid in 20 min.; white → brown	Purple, then white in
Toluene + THF $(3 \cdot 7, v/v)$	2.3	-78	20	n-Bu ₃ P	0.05	95	Solid in 10 sec.	White, then pink in 30
Toluene	2.3	0	4	$n-Bu_{3}P$	0,02	93	Solid in 1 sec.	White, then pink in 30
Toluene + THF	2.3	0	20	${\rm Ti}({\rm NMe_2})_4$	0.03	78	Solid in 15 sec.; brown	Brown
Toluene	1.32	-76	22	$Ti(NMe_{2})_{4}$	0.104	68	Thick gel in 30 sec.;	Purple to green to
Toluene	1.32	-76	22	$n-\mathrm{Bu}_{\mathrm{s}}\mathrm{P}$	0.027	96	Solid mass in 10 sec.;	wnite White
'foluene	1.32	92-	22	${\rm Ti}({\rm NMe}_2)_4$	0.027	86	yenow Thick gel in 30 min.;	Purple to green to
Toluene	1.32	0	22	$Ti(NMe_2)_4$	0.0126	88	Solid mass in 5 min.; dark brown	white Light brown

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#### POLY-α-CYANOSTYRENE

polymer are colored, soluble in DMF, melt on a hot bar below 200°C., and have an intrinsic viscosity of less than 0.20 in DMF at 30°C. Copolymerization of  $\alpha$ -cyanostyrene with styrene, by use of the free-radical initiators, proceeds at the same low rate. No polymerization occurs in the absence of the free-radical initiators.

## DISCUSSION

Attempts to prepare poly- $\alpha$ -cyanostyrene by free radical initiation were unsuccessful, probably because of the inactivity of the resonance-stabilized radical:



The propagation constant cannot be increased by the use of high temperatures because of the rapid rate at which  $\alpha$ -cyanostyrene dimerizes to an inactive product. Polymerization initiated by anionic initiators is extremely rapid, much faster than the rate of dimerization at the low temperatures used (cf. Tables I and II). The color changes which occur during polymerization and after the addition of methanol when using the Ti-(NMe₂)₄ initiator suggest either a change in valence of the titanium or the formation of a strong complex with the  $\alpha$ -cyanostyrene. The absence of regularity in the solid state for poly- $\alpha$ -cyanostyrene is shown by the fact that the polymer gives no regular pattern in the x-ray powder diagram, in contrast to polyacrylonitrile. The  $[\eta]-\overline{M}_n$  relationship indicates a very stiff chain which may account for its inability to crystallize.

## PROCEDURE

#### **Preparation of** $\alpha$ -Cyanostyrene

The  $\alpha$ -cyanostyrene was prepared by condensation of benzyl cyanide with formaldehyde in the presence of base.⁵ A suitable method for purification involved condensing  $\alpha$ -cyanostyrene with dimethylamine, purification of the 3-(N,N-diamethylamino)-2-phenylpropionitrile, and the pyrolysis of the hydrochloride salt of the latter.

## **3**-(*N*,*N*-Dimethylamino)-2-phenylpropionitrile

A 104-g. portion of freshly prepared crude  $\alpha$ -cyanostyrene was dissolved in 200 ml. of dioxane. The resulting solution was added to 90 g. (2.0 mole) of dimethylamine and 4 ml. of Triton B(benzyltrimethylammonium hydroxide) in 200 ml. of dioxane at a rate to maintain the temperature at 15–25°C. The mixture was aged at 45–50°C. for 3 hr., and the solution was poured into 1500 ml. of distilled H₂O. The organic layer was separated, and the water layer was extracted with three 300-ml. portions of benzene. The combined organic layer and extracts were washed with 500 ml. of H₂O and extracted with three 150-ml. portions of 10% HCl. The HCl extract was washed with two 200-ml. portions of benzene and then made alkaline by addition of 50% NaOH. The organic layer was separated, the aqueous layer extracted with three 75-ml. portions of benzene, and the combined extracts and organic layer were washed with 100 ml. of H₂O and dried over anhydrous sodium sulfate. The benzene was removed under vacuum, and the residue was distilled to give 74.3 g. (52.9% yield) of product boiling at 105-112°C./2 mm. Hg.

Two new derivatives, the methiodide, m.p. 242–245°C. (decomp.) and the picrate, m.p. 116.5–117.5°C., were prepared.

## 3-(N,N-Dimethylamino)-2-phenylpropionitrile Hydrochloride

Anhydrous HCl gas was added below the surface of a solution of 144 g. (0.825 mole) of 3-(N,N-dimethylamino)-2-phenyl propionitrile in 500 ml. of benzene while stirring and cooling to maintain the temperature below 40°C. The HCl salt precipitated and eventually formed a semisolid mass, at which point the introduction of HCl was discontinued. The solids were filtered and washed with 75 ml. of fresh benzene. After drying in a rotary dryer at 10 mm. Hg and room temperature, the yield was 120 g. (76%). The hydrochloride salt had amelting point of 130–135°C. (decomp.), (lit. value: 133–134°C.) and a molecular weight of 170 (theory 174).

## Pyrolysis of the Hydrochloride Salt of 3-(N,N-Dimethylamino)-2-phenylpropionitrile

A 5-g. sample of the hydrochloride was placed in a 50-ml flask and the pressure reduced to 2 mm. Hg. An oil bath was so placed that the bulb of the flask was covered and the flask was heated to  $160^{\circ}$ C. Liquid product which distilled out at 75–95°C. was collected in a receiver which was cooled in a Dry Ice-acetone bath. The product was dissolved in 10 ml. of cold ether, the solution washed with 10 ml. of 10% HCl, 10 ml. of H₂O and dried over anhydrous sodium sulfate. Removal of the ether and flash distillation of the product at 2 mm. Hg gave 2.8 g. of  $\alpha$ -cyanostyrene (54% yield).

## **Dimerization Rate Studies**

The rate of dimerization of  $\alpha$ -cyanostyrene was determined by following the change in molecular weight of the monomer-dimer mixture. The  $\alpha$ cyanostyrene used for these studies was crude material from the benzyl cyanide-formaldehyde condensation (fractionally distilled immediately before use). The molecular weights were determined by use of a microebulliometric apparatus built in these laboratories.⁷ The data were treated by the method of least squares applied to the second-order rate equation. The half life,  $t_{1/2}$ , was equal to 30  $(1 - X_2)/(X_2 - X_1)$ , where  $X_1$  was the initial mole fraction of dimer and  $X_2$  was the mole fraction of dimer after 30 hr. Typical data are plotted in Figure 1 for pure  $\alpha$ -cyanostyrene, and

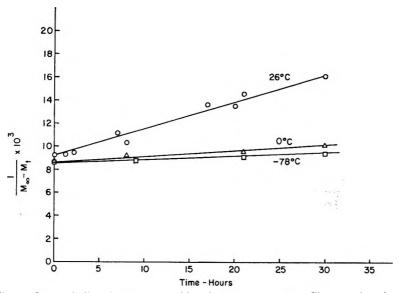


Fig. 1. Rate of dimerization of undiluted  $\alpha$ -cyanostyrene. Change of molecular weight with time ( $M_t$  denotes molecular weight at time t;  $M_{\infty}$  is molecular weight at  $t = \infty$ ).

the complete storage stability data are tabulated in Table II. The monomer was made available for polymerization as 25-50% solutions in toluenc. The solutions were stored for less than 18 hr. at -78°C. before use.

Condition of monomer	Temperature, °C.	Half life t _{1/2} , hr.
Undiluted	26	23
Undiluted	0	87
Undiluted	$-78^{a}$	188
50% in acetone	26	52
50% in acetone	0	400
50% in acetone	-78ª	1370
50% in benzene	26	130
72% in benzene	26	38
Contains 0.9% hydroquinone	<b>26</b>	15
Contains 1% p-nitrosodi-		
phenylamine	26	20
Saturated with cupric acetate	26	21

TABLE II Storage Stability of  $\alpha$ -Cyanostyrene

* Solids precipitated from the solution. The mass was warmed momentarily to obtain homogeneous samples for analysis.

## **Raw Materials**

CP toluene was refluxed for 10 hr. over sodium and fractionated in an all-glass apparatus which had been flamed three times and cooled under

pure, dry argon. CP tetrahydrofuran was purified by the same procedure as was used for toluene. Styrene (Monsanto, polymer grade) was dried three times over CaSO₄ and was fractionated in an all-glass apparatus in the same manner used for toluene. Azobisisobutyronitrile was recrystallized three times from ethanol, m.p. 102–103°C. Benzoyl peroxide was from Lucidol Corp. Tetrakisdimethylaminotitanium was prepared according to literature procedures.⁸ Tributylphosphine, b.p. 107–108°C./ 7.5 mm. Hg, was fractionated and stored in water-free equipment over argon. Argon (< 0.002% oxygen and < 0.0008% water) was dried further with Linde 5A molecular sieves before use.

## **Polymerization**

**Free-Radical Polymerization.** The monomer solution was charged to clean Pyrex tubes which had been flamed three times at 200°C. and cooled under pure argon. Initiator solution was added, and the tubes were sealed and immersed in a constant temperature bath for a given length of time. After completion of the reaction, the tubes were cooled to 25°C., opened, and poured into a fivefold excess of MeOH to precipitate the polymer. The polymer was purified by solution in DMF and reprecipitation in MeOH (in which the dimer of  $\alpha$ -cyanostyrene is soluble). Drying was accomplished at 40°C. at < 0.1 mm of Hg. All liquids were transferred by means of syringes which had been dried at 140°C. and cooled under pure argon.

Anionic Polymerization The monomer solution and solvents were charged to 25-ml-glass reaction flasks containing glass-coated magnetic stirrers. The apparatus had been freed of impurities by flaming three times under argon and held, thereafter, under a blanket of pure argon. After adjusting the bath temperature and waiting 15 min. for temperature equilibrium, the catalyst was added within 5 sec. At the end of the reaction period, dry excess MeOH at the temperature of the reaction was added to destroy the catalyst and to precipitate the polymer. Further workup and purification was the same as for the free radical-initiated reaction. All liquids were transferred in syringes as described above.

## Number-Average Molecular Weight

Mn was estimated by using a Mechrolab vapor-phase osmometer.

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#### POLY-α-CYANOSTYRENE

## Résumé

Lé  $\alpha$ -cyanostyrène monomère polymérise à très faible vitesse sous l'influence de radicaux libres initiateurs. La polymérisation rapide donnant des produits à haut poids moléculaire a été obtenue en utilisant des initiateurs anioniques (le tri-*n*-butylphosphine et le tétrakis-diméthylaminotitane). Le polymère obtenu à  $-78^{\circ}$ C était incolore, fusible, soluble et avait un poids moléculaire moyen de plus de 5000. Le polymère préparé à 0°C était brun, insoluble et infusible. Aucun des polymères ne montre une disposition régulière au diagramme des rayons-X. La vitesse de dimérisation de l' $\alpha$ -cyanostyrène a été mesurée dans de nombreuses conditions. Deux nouveaux dérivés de l'intermédiaire, le 3-(N,N-diméthylamino)-2-phénylpropionitrile, ont été préparés—le sel quaternaire avec l'iodure de méthyl p.f. 242-245°C (décomp.) et le picrate p.f. 116.5-117.5°C.

#### Zusammenfassung

Unter dem Einfluss radikalischer Starter polymerisiert das Monomere  $\alpha$ -Cyanstyrol mit sehr geringer Geschwindigkeit. Mit anionischen Startern (Tri-*n*-butylphosphin und Tetrakisdimethylaminotitan) wurde eine rasche Polymerisation zu hochmolekularen Stoffen erreicht. Das bei -78 °C erzeugte Polymere war farblos, schmelzbar, löslich und das Zahenmittel des Molekulargewichts betrug über 5.000. Das bei 0° C hergestellte Polymere war braun, unlöslich und umschmelzbar. Keines der Polymeren liess im Röntgendiagramm eine Änderung erkennen. Die Dimerisierungsgeschwindigkeit von  $\alpha$ -Cyanstyrol wurde unter einer grössen Vielfalt von Reaktionsbedingungen gemessen. Zwei neue Derivate des Zwischenprodukts 3-(N,N-Dimethylamino)-2-phenylpropionitril wurden dargestellt, nämlich das Methiodid F.p. 242–245°C (Zersetzung) und das Pierat, F.p. 116,5–117,5°C.

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# Poly(chloroaldehydes). I. Polychloral Stabilization*

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## Synopsis

Polychloral diol, unlike polyoxymethylene diol, is not readily capped in the presence of alkali catalysts. Polychloral is capped under acid conditions by acid anhydrides and chlorides and does not appear to undergo degradation during the process. Evidence for end-capping is provided by infrared analysis in the case of the low DP polychloral, metachloral. End-capped polychlorals possess good stability towards hot dimethylformamide and good stability at elevated temperatures (255°C.). From the melting points of copolymers, polychloral itself is estimated to have a melting point of about 460°C. The high melting point is consistent with the rigidity of the polymer chain. A means of estimating the DP of the polymer is proposed, based on a form of endgroup analysis. By this technique, metachloral is estimated to have a DP of about 50.

## **INTRODUCTION**

The structures of polymers derived from aldehydes polymerized through the carbonyl group can be classified as polyacetal diols because of their hydroxyl end groups. Any study involving the measurement of structural parameters at elevated temperatures (above the ceiling temperature) requires capping of the hydroxyl endgroups [eq. (1)] to prevent the decomposition of the polymer.

$$\begin{array}{ccc} \text{HO} \leftarrow \text{CHO} \rightarrow_n \text{H} + 2\text{R}^+ \rightarrow & \text{RO} \leftarrow \text{CHO} \rightarrow_n \text{R} + 2\text{H}^+ & (1) \\ & & & & \\ \text{R} & & & \text{R} \end{array}$$

Extensive work has been carried out on the end-capping of polyoxymethylene.¹ The method usually employed is an alkali-catalyzed acylation. The use of acid catalysts or acid reagents results in reduction of the polymer molecular weight by cleavage of the acetal links of the polymer chain, and hence is usually undesirable.

Only one report has been found on the end-capping of polychloral; indeed, recent review articles disclose only a small amount of work published on polychloral itself.² The one report on end-capping repeats many of the capping techniques described in the polyoxymethylene art, but gives little information as to the polymer structure.³ Our attempts

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to use base-catalyzed capping of polychloral resulted in polymer chemistry disasters with the loss of substantial amounts of the polymer. A more effective capping technique was needed.

This report describes an effective end-capping technique, provides some elucidation of the capped polymer structure and properties, and suggests a simple means of estimating polychloral molecular weights via a form of end-group analysis.

## **EXPERIMENTAL**

### **Polymer and Reagents**

The various polychlorals were washed with methanol and dried under vacuum at ambient temperatures prior to use. The acid chlorides were Eastman white label grade when available, and generally were used without additional purification. The acetic anhydride was distilled prior to use.

## **Typical Capping Procedure**

The polychloral is slurried in an excess of the capping reagent and stirred, under an atmosphere of dry nitrogen, usually at 180°C. for 30 min. After cooling, the mixture is decanted into methyl ethyl ketone. The precipitate is filtered, washed with methanol, and dried under vacuum.

#### **Capping Test**

The efficiency of the end-capping was determined by stirring the sample in dimethylformamide at 130°C. for 30 min. and recovering the undissolved polymer. The polymer which dissolves is decomposed, probably to monomer. Efforts at recovery from the reagent are fruitless. Polychloral which has not been end-capped essentially completely disappears in this treatment. Additional evidence of end-capping is obtained from the thermogravimetric analysis of the polymers at 255°C. under nitrogen, carried out in a Stanton thermobalance, Model HT-M. The end-capped polymer is substantially more heat-stable than the untreated polymer.

## Analyses

Considerable difficulty is encountered in carrying out infrared analyses of polychloral because of its intractability and its insolubility. Evidence for capping, however, is provided by the intensity of the C—OH infrared absorption of a thick mull in Nujol (0.04 g./2 drops) with the use of a CaF₂ prism. Novak and Whalley⁴ reported that the C—OH infrared absorption of polychloral occurs at 3360 and 3500 cm⁻¹.

The analysis of the carbon and hydrogen content of the polymer before and after esterification provides evidence of end-capping, depending upon the degree of polymerization (DP) of the polymer and the reagent used.

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## RESULTS

Table I summarizes some of the results obtained with various reagents. Most of the initial work on end-capping was carried out with low molecular weight polychloral (metachloral) prepared from chloral hydrate in sulfuric acid. Work with this polymer was carried out because it is known to contain C—OH end-groups, has a low DP, and chemical changes were expected to be discernible by infrared and elemental analysis techniques.

				% Stable	
Polychloral	D	Temp.,	Yield,	in	$k_{255}, {}^{b}$
type	Reagent	°C.	%	DMFa	%/min
Metachloral	None			0	1.50
(1	$C_6H_5COCl$	160	63	37	
"	"	180	63	80	0.20
" "	CH ₃ (CH ₂ ) ₃ COCl	125	76	68	0.35
"	$CH_3(CH_2)_{10}COCl$	180	76	69	0.15
"	$CH_3(CH_2)_{14}COCl$	180	75	48	
"	$Ac_2O$	140	64	71	0.21
"	$Ac_2O + NaOAc$	140	18	90	
$\mathrm{DP}{\sim}550^\circ$	None			6	3.70
" "	$CH_3(CH_2)_{10}COCl$	180	94	94	
"	C ₆ H ₅ COCl	180	93	81	1.08
"	CH ₃ COCl	140	93	95	
"	Ae ₂ O	140	75	97	
"	$Ac_2O + pyridine$	140	30	60	

 TABLE I

 Reagents for End-Capping of Polychlora

^a Dimethylformamide at 130°C.

^b Stability at 255°C., measured by decomposition rate under nitrogen.

^e Estimated degree of polymerization (DP), by method described later.

Evidently, the best yield of polymer with good stability to hot DMF is obtained in the absence of alkaline catalysts. The anhydrides are much more effective alone, without base. The most convenient reagents to use in the laboratory are the higher acid chlorides at about 180°C.

In low molecular weight polychloral, the C—OH infrared absorption is readily discernible. After esterification, this absorption disappears and a carbonyl absorption appears at 1753 cm.⁻¹ (Fig. 1). There is also evidence of an ester absorption at 1260 cm.⁻¹. Most samples have a carbonyl absorption at about 1770 cm.⁻¹, prior to capping, which is attributed to the presence of small amounts of chloral monomer. In the high molecular weight polychlorals (DP~500), neither the C—OH nor ester absorptions are readily detectable either prior to or after capping.

The thermal stability of the capped polymers is considerably higher than that of the uncapped polymers which were prepared in our laboratories and by Ilyina et al.⁵ Whereas uncapped polymer appears to melt and

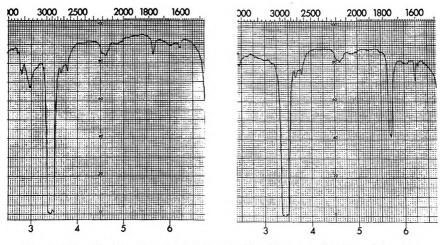


Fig. 1. Infrared absorption spectra of metachloral before and after end-capping.

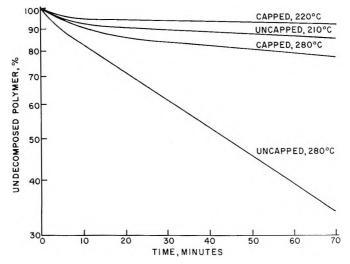


Fig. 2. Thermal decomposition of uncapped and end-capped metachloral at different temperatures.

decompose" above 200°C., the capped polymer possesses good stability at 255°C. (Table I). The marked increase in thermal stability after treatment is further evidence that capping has been achieved (Fig. 2). The energy of activation for decomposition of the uncapped polymer of metachloral (DP $\sim$ 50) is 19 kcal./mole. After end-capping, this polymer has a decomposition activation energy of 14 kcal./mole (Fig. 3). The changed activation energy is attributed to the decreased number of sites for the initiation of decomposition, resulting from the capping of the C—OH groups.

Additional evidence for end-capping was provided by the evaluation of the biological activity of the polymer. The uncapped polymer is an active herbicide, similar in activity to chloral. The capped polychloral, however, possesses little herbicidal activity. These observations demonstrate that the biological activity of uncapped polychloral is due to its breakdown to monomeric chloral.

An item of concern was the possibility that degradation may take place during the end-capping process. The amount of degradation appeared minimal, from the following observations: (a) there was little change in the relative ester absorption in the infrared even after additional heating

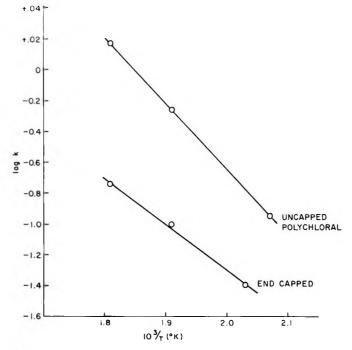


Fig. 3. Arrhenius plot of thermal decomposition rates of uncapped and end-capped metachloral.

in the capping reagent; (b) there was little change in the amount of polymer recovered after additional heating; (c) the powder x-ray diffraction pattern of the polychloral remained about the same; (d) in many cases, very high yields of capped polymer were obtained.

Attempts to determine the melting points of the capped polymers were unsuccessful. Investigation by use of both a hot stage on a polarizing light microscope and a melting point block indicated that the polymer appeared to slowly vaporize, without melting, as the temperature increased. Differential thermal analysis showed good stability of the polymer up until 220°C. No transition points were detected below this temperature. At 225°C., an endothermic reaction occurred, which increased with the temperature. Examination of the analysis sample cell after the measurement disclosed that the sample had vaporized.

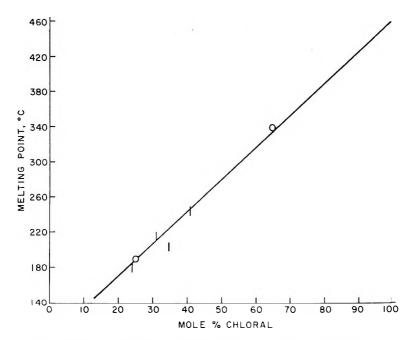


Fig. 4. Melting point of polychloral estimated from melting points of chloral-formaldehyde copolymers: (O) points obtained from literature.

A rough estimate of the melting point of polychloral was made from the melting points of some copolymers of chloral with formaldehyde and the use of some previously reported data.⁶ Two simplifying assumptions were made, namely, that formaldehyde is not isomorphous with chloral in the polymer crystal structure and that formaldehyde and chloral form copolymers with random distribution. The estimated value of the melting point is 460°C. (Fig. 4), which is unusually high. In the estimate, rather heavy reliance is placed on the previously reported point at 65 mole-%chloral, a figure we were unable to check, and which is described as a decomposition point rather than a melting point.

## DISCUSSION

The rapid degradation polychloral vis à vis polyoxymethylene in the presence of alkali can be explained in the light of the different electronegativities of the substituents. The inductive effect of the chlorines in polychloral promotes the ionization of the hydrogen-oxygen bond and the sub-

$$\begin{array}{ccc} \operatorname{RO} + \operatorname{CHO} +_{n}\operatorname{H} + \operatorname{OH}^{-} & \rightarrow & \operatorname{RO} + \operatorname{CHO} +_{n-1}\operatorname{CHO}^{-} + \operatorname{HOH} \\ & & & & & & \\ \operatorname{CCl}_{3} & & \operatorname{CCl}_{3} & & \\ & & & & \\ \operatorname{RO} + \operatorname{CHO} +_{n-2}\operatorname{CHO}^{-} + \operatorname{CHOCCl}_{3} & & (2) \\ & & & & \\ & & & & \\ \operatorname{CCl}_{3} & & \operatorname{CCl}_{3} & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & &$$

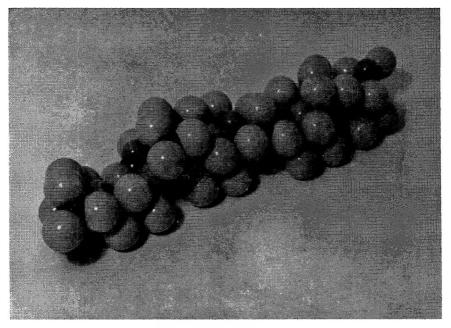


Fig. 5. Fisher-Hirschfelder-Taylor model of structure of polychloral (7 monomer units in 3 spiral turns).

sequent formation of the polymer anion which unzips stepwise to the monomer [eq. (2)]. The polymer will also degrade in this fashion when only one end is capped (i.e., R = ether or ester). A related factor is the relative polymerizabilities of the two monomers, but these are not yet known with certainty.⁷

In the presence of acid, polyoxymethylene is readily degraded because of hydrogen ion attack on the ether linkage followed by chain scission. Polychloral, on the other hand, is stable towards very strong acid. Low molecular weight polychloral (often referred to as metachloral), is prepared in the presence of concentrated sulfuric acid. The stability of polychloral to strong acid led to the use of the acyl halides as end-capping agents, as it was hoped that the polychloral would be stable to the HCl evolved during the reaction. Such actually proved to be the case, even at the reaction temperatures utilized. The estimated molecular weights before and after the capping remained about the same.

The cause of the stability to acids is not known definitely, but is ascribed to steric factors, predominantly. Models of the structure of polychloral show a very tightly packed helical arrangement of monomer molecules, and demonstrate a highly inaccessible acetal oxygen atom (Fig. 5). The stiffness and inflexibility of the polymer chains probably contribute considerably to the high melting point of the polymer. The effect of capping on the x-ray diffraction patterns was minimal, indicating the capping takes place heterogeneously at available sites and thus does not interfere with or

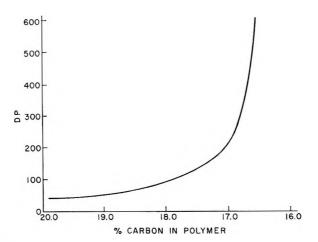


Fig. 6. Calculated variation of DP with per cent carbon in polychloral end-capped with two laurate groups.

alter crystallinity. Such was the situation even with capping of a polychloral of  $DP \sim 50$  with laurate end-groups.

The so-called "solubility" of the polymer is considerably altered by the capping. Thus, uncapped polychloral has in the past been referred to as soluble in pyridine, although the polymer cannot be recovered because of decomposition.⁸ The capped polymer, on the other hand, is insoluble.

An interesting supplement to this investigation was the development of the end-capping technique to provide a rapid means for estimation of number-average molecular weight. The technique simply involves placement of a long hydrocarbon chain on the polychloral ends, followed by an elemental carbon and hydrogen analysis. The carbon and hydrogen content of polychloral is so low that addition of hydrocarbon causes a marked change. This is demonstrated in Figure 6, showing the variation of carbon content with the DP of polychloral, using laurate end-groups. The accuracy is best at the lower DP's and begins to fall off considerably at a DP of about 300. Nevertheless, for purposes of estimation, the method proved adequate. The precision can be improved somewhat by the use of longer chains in the ester portion, by this method, the DP of metachloral is estimated to be about 50.

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#### Résumé

Le polychloral-diol, contrairement au polyoxyméthylène-diol, n'est pas aisément protégé en fin de chaîne, en présence de catalyseurs alcalins. Le polychloral a les fins de chaînes protégées par action en milieu acide des anhydrides et chlorures d'acide, et ne semble pas subir de dégradation pendant le processus. La preuve d'une protection en fin de chaînes est fournie par l'analyse infra-rouge dans le cas du polychloral de faible DP, métachloral. Les polychlorals protégés en fin de chaîne, possèdent une bonne stabilité vis-à-vis du diméthyl-formamide chaud et une bonne stabilité aux températures élevées (225°C). À partir des points de fusion des copolymères, on estime que le polychloral luimême possède un point de fusion de 460°C environ. Le point de fusion élevé est en accord avec la rigidité de la chaîne polymérique. On propose un moyen pour estimer le DP du polymère, en employant une forme d'analyse de groupement terminal. Par cette technique, on estime que l'métachloral' possède un DP d'environ 50.

## Zusammenfassung

Polychloraldiol kann im Gegensatz zu Polyoxymethylendiol in Gegenwart alkalischer Katalysatoren nicht leicht mit Endgruppen versehen werden. Polychloral erhält unter sauren Bedingunge Endgruppen durch Säureanhydride und -chloride und scheint während dieses Prozesses keinen Abbau zu erleiden. Die Endgruppen werden im Falle des niedermolekularen Polychlorals, Metachloral, durch Infrarotanalyse nachgewiesen. Mit Endgruppen versehener Polychloral besitzt gute Stabilität gegen heisses Dimethylformamid bei erhöhten Temperauturen (225°C). Aus den Schmelzpunkten von Copolymeren wird der Schmelzpunkt von Polychloral selbst zu etwa 460°C geschätzt. Der hohe Schmelzpunkt entspricht der Starrheit der Polymerkette. Zur Bestimmung des DP des Polymeren wird eine Form einer Endgruppenanalyse vorgeschlagen Nach diesem Verfahren wird der DP von Metachloral zu etwa 50 bestimmt.

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# Poly(chloroaldehydes). II. Polymerization of Chloral*

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### Synopsis

Chloral was polymerized by means of cationic and anionic initiators and the products compared. Anionic catalysts readily produce high molecular weight polymer (DP  $\sim$  300-600), but a DP of only 200 could be produced with cationic catalysts. The anionic system apparently initiates and propagates polymerization much more readily than the cationic system. This effect is attributed to the inductive effects of the chlorine atoms on the chloral. Little difference was found when products of similar DP were compared as to x-ray diffraction pattern, infrared spectrum and tractability. This is believed due to the single type of structure which is sterically favored. Various cyclic compounds of chloral could not be made to undergo polymerization under cationic initiation. The conditions required to effect ring opening were too rigorous to enable polymerization to take place.

## **INTRODUCTION**

The growing interest in the area of aldehyde polymerizations has produced occasional reports on polychloral, although not nearly in the volume for the unsubstituted lower aliphatic aldehydes.¹ The more recent work on polychloral has centered on the low-temperature ( $-78^{\circ}$ C.) polymerization with organometallic catalysts of the anionic or coordination type. Furukawa and co-workers found that chloral can be polymerized at  $-78^{\circ}$ C. with a BuLi catalyst.² Using a polymer prepared in a similar way, Ilyina and co-workers investigated some of the thermal properties of the uncapped polymer.³ No evaluation of end-capped polymers has been reported.

Polychloral can be prepared with a variety of catalyst types, but little has been done on the comparative characterization of the polymers, or ascertaining their molecular weights. This paper describes the utilization of three different catalyst systems in attempts to obtain high molecular weight polychloral, and the comparison of some of the basic properties of these polymers.

In addition to the above, attempts were made to polymerize various cyclic compounds of chloral. The cyclic trimer of formaldehyde, trioxane, is used commercially as a starting material for the preparation of poly-

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formaldehyde. It appeared reasonable, therefore, to examine cyclic compounds of chloral as starting materials for the preparation of polychloral.

## **EXPERIMENTAL**

The chloral monomer used in this work was purified by distillation under nitrogen and dried over molecular sieves. Vapor-pressure chromatography showed the chloral to be 99.9% pure, with <0.1% dichloroacetaldehyde as the major impurity. The water content was determined by a colorimetric Karl Fisher technique and could be controlled within a range of 2–20 ppm.

Polymerization was carried out in a resin kettle which was heated at 110°C. and then assembled under a stream of high purity nitrogen. Additions of monomer, solvent, and catalyst were carried out by means of heated and dried syringes. After polymerization, the polymer was filtered, washed with acidified methanol, methanol, then filtered and dried. The polymerizations and polymer treatments were carried out at temperatures below 40°C., which appears to be the ceiling temperature for polychloral.⁴

The degree of polymerization (DP) of the polymer was estimated with the aid of the end-capping technique described in the preceding paper⁵ of this series.

Infrared spectra were obtained on a Perkin-Elmer Model 21 spectrometer, using a Nujol null of the polymer. Powder x-ray diffraction patterns were obtained with nickel-filtered copper  $K\alpha$  radiation.

 $\alpha$ -Parachloral,  $\beta$ -parachloral, chloralide, hexachlorodimethyltetroxan, and 2-trichloromethyl-1,3-dioxolane, were prepared by following the directions reported in the literature for each of these compounds.⁶ Attempts were made to polymerize these materials alone and to copolymerize them with trioxane. The catalysts utilized included BF₃·Et₂O, BF₃, HF, HCl, AlCl₃, SbCl₃, and *p*-toluenesulfonic acid, at temperatures ranging from 0 to 145°C.

#### RESULTS

## **Cationic Polymerization**

A screening of various acid catalysts showed that the stronger Lewis acids, i.e., the metal halides, were most suitable for polymerizing chloral. The stronger the acid catalyst, the more effective the polymerization. Thus, AlCl₃, AlBr₃, and ZrCl₄ were more effective than SnCl₄. Most of the work was carried out with AlBr₃ because of its effectiveness and good solubility in organic solvents.

The concentration of the catalyst was varied in a solution of chloral in methylene chloride (1:6 mole ratio) at -20°C. (Fig. 1). The rate of polymerization increases with the catalyst concentration, but the optimum polymer DP appeared at a catalyst concentration of 6 mmole AlBr₃/mole chloral. At this catalyst concentration, the polymerization temperature was varied over the range from +10 to -75°C. (Fig. 2). The optimum

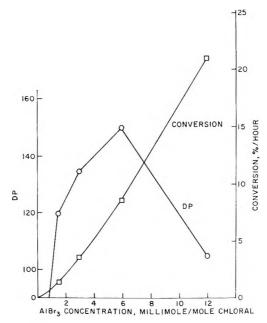


Fig. 1. Variation of polymer DP and average conversion rate with  $\rm AlBr_3$  catalyst concentration.

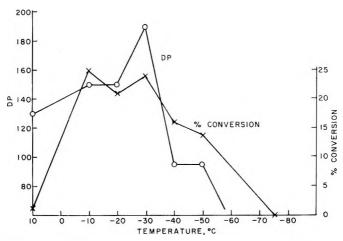


Fig. 2. Variation of polymer DP and total per cent conversion with polymerization temperature: 6 mmole  $AlBr_3/6$  mole of  $CH_2Cl_2$ /mole of chloral.

temperature for obtaining the highest DP of 190 in this system is at about  $-30^{\circ}$ C. At higher temperatures, transfer and termination reactions appear to predominate, whereas at lower temperatures, there is little initiation and propagation of the chains. Variation in the water content of the system over the range 10–120 ppm did not materially alter the polymer DP. Change in the solvent type from methylene chloride to linear and cyclic aliphatic hydrocarbons also had little effect on the DP.

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Alteration of the catalyst, solvent type, solvent concentration, water concentration, catalyst concentration, and polymerization temperature produced a change in polymerization rate, but altered the DP of the polymer only within a narrow range Some of the more pronounced effects on polymer DP were obtained by varying the polymerization temperature. For all the changes in conditions, we were not able to increase the DP above 200, and for the most part the DP varied within a range of 100-200.

## **Noncationic Polymerization**

Many experiments in this area to achieve high DP polymer were unnecessary, as this was readily attained with a variety of nonacid catalysts in good yields over a short polymerization period (Table I).

	TABLE 1           Noncationic Polymerization of Chloral											
Catalyst	Catalyst concen- tration, mmole/ mole chloral	Time,	Conver- sion, %	DP	Temp., °C.	Solvent						
$\overline{(C_4H_9)_3N}$	6.5	0.1	78	220	0	Nitrobenzene						
(C ₄ H ₉ ) ₃ CH ₃ NI	<b>4</b> ª	0.5	55	380	0	None						
u	<b>4</b> ª	0.5	<b>28</b>	260	0	Toluene						
"	<b>4</b> ^a	0.5	18	190	-20	"						
Et ₂ Zn	50	<b>24</b>	<b>28</b>	300	-78	Heptane						
$2,6 \text{ DPL}^{b} + \text{Et}_2\text{Zn}$	29	1	59	600	-48	Propylene						
"	"	"	43	170	-5							

	TABLE I		
Noncationic	Polymerization	of	Chloral

^a Catalyst dissolved in acetonitrile.

^b 2,6-Dimethoxyphenyllithium.

The catalysts found particularly effective for producing high DP polymer were the quaternary ammonium salts and organometallic compounds. The quaternary salts worked best at about  $0^{\circ}$ C. Lowering the temperature and increasing the dilution lowered the resulting polymer DP together with the conversion of monomer to polymer. With the combined Li and Zn compounds, high molecular weights could be obtained at temperatures below  $-45^{\circ}$ C., but above this temperature the polymer DP decreased. Tertiary amines were rapid initiators, but usually gave polymer of lower DP than the other catalysts.

The anionic and quaternary salt-catalyzed systems displayed a much higher sensitivity to water than the cationic system. This is demonstrated in the results obtained with the quaternary salt catalyst (Fig. 3). Both the polymer DP and yield decrease as the water content of the system is increased.

#### POLY(CHLOROALDEHYDES). II

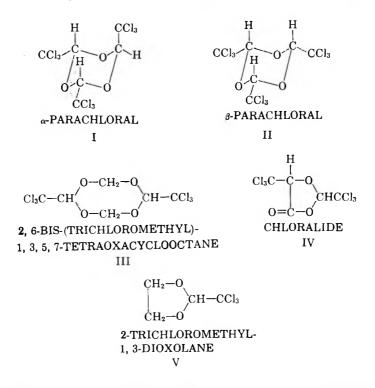
#### **Comparison of Infrared Spectra and X-Ray Diffraction Patterns**

The infrared spectra of the capped polymers was investigated in the range of 750–5000 cm.⁻¹, but no significant difference was observed in the spectra for the polymers derived from the various catalyst types. The absorption spectra and intensities of the bands were quite similar to those published by Novak and Whalley.⁷

The x-ray crystallinity demonstrated by the various samples appeared to be more affected by the DP than by the initiator. Samples of similar DP (over range 50-400) were compared, derived from the three catalyst types, and found to possess the same diffraction patterns and crystallinity. Most of the patterns resembled two reported by Novak and Whalley for the sulfuric acid- and pyridine-catalyzed polymers (designated A and B).⁷

#### **Cyclic Monomer Polymerization**

The various cyclic compounds (I-V) gave negative results in all efforts to initiate homopolymerization and copolymerization with trioxane. In the latter case, when polymer was formed, it was found to be polyformaldehyde.



The compounds are fairly stable, and only the use of the more elevated temperatures enables ring scission to take place. At that point, however, the temperatures exceed the polymer ceiling temperatures, and only decomposition takes place.

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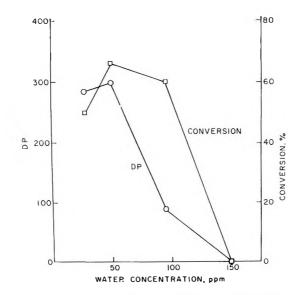


Fig. 3. Effect of water on polymer DP and yield with tributylmethylammonium iodide catalyst at  $0^{\circ}$ C.

#### DISCUSSION

The cationic polymerization of chloral cannot be terminated by  $\alpha$ hydrogen. This provides the expectation that high DP polymer would be Such is not the case, however, and it seems that traces of water obtained. or other system components probably cause the transfer and termination reactions. The similar DP's obtained regardless of the change in conditions indicate the termination reaction takes place fairly readily. The fairly rapid cationic polymerization of chloral at low temperatures indicates a low Arrhenius energy and an ionic mechanism, possibly by the route indicated in eqs. (1)-(4). Initiation mechanisms involving both separation of charges and a neighboring gegenion were considered. Although it is not certain which mechanism is correct, the first type had more appeal because of the observed lack of influence of small changes in the concentration of water on the reaction.

Initiation:

$$Cl_{3}CCHO + AlBr_{3} \rightarrow AlBr_{3}^{-}O - C + \text{ or } Br_{2}AlOC + AlBr_{4}^{-}$$

$$Cl_{3} CCl_{3} CCl_{3}$$

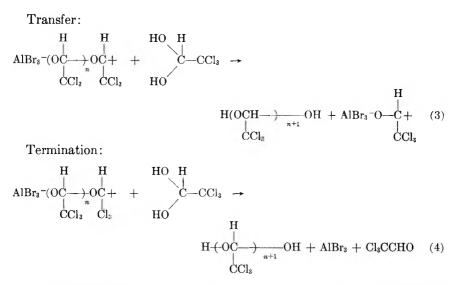
$$(1)$$

Propagation:

ł

$$\begin{array}{ccc} H & H & H \\ \downarrow \\ AlBr_{3}^{-}O & -C + + Cl_{3}CCHO \rightarrow AlBr_{3}^{-}OCOC +, etc. \\ \downarrow \\ CCl_{3} & CCl_{3} & CCl_{3} \end{array}$$
(2)

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In the anionic polymerization, higher DP's are more readily attained than in the cationic system. This also occurs when equivalent amounts of water are present in the polymerization systems. The anionic catalysts polymerized chloral much more readily and more rapidly than the cationic catalysts, indicating an even lower Arrhenius energy than required for the cationic system. Furthermore, the higher DP's in the anionic system indicate a higher relative ratio of propagation to termination reactions.

Chloral is an unusual monomer, in that it is susceptible to both cationic and anionic polymerization by virtue of its easily polarizable carbonyl group. Although weak anionic catalysts were sufficient to polymerize chloral, strong acids such as  $AlBr_3$  were required in the cationic system. The observations lead to the conclusion that chloral is more readily polymerized by anionic catalysis. The results are attributed to the inductive effects of the three chlorine atoms on the chloral molecule. The large number of electronegative substituents makes the carbonyl group more readily polarizable by anionic catalysts.

The structures, as well as the solubility and melting characteristics of the medium DP ( $\sim 200$ ) polymers prepared by anionic and cationic polymerization appear to be about the same. The production of similar polymers by two different mechanisms is not entirely surprising when one considers models of the potential structures of polychloral. The most sterically favored structure contains the chloral units in an isotactic relationship arranged in a helical configuration. This structure, which has been proposed by Novak and Whalley, is apparently assumed by the polychloral, regardless of the propagation mechanism.⁷

All of the polymers produced were highly intractable. The high value of the extrapolated melting point described in the first paper of this series⁵ explains the intractability under conventional molding conditions. To approach the melting point requires temperatures considerably above the point at which the polymer decomposes rapidly.

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The unsuccessful effort to polymerize the cyclic trimers of chloral is not altogether surprising, because the structural models showed the points of catalytic attack to be sterically hindered. In the case of the mixed cyclic acetals of chloral and formaldehyde, the reluctance to polymerize is apparently due to a combination of steric and inductive effects. The ring structures are broken only under fairly severe reaction conditions, which leads to degradation rather than the desired polymerization reaction. Of related interest is the observation that the cyclic trimer of acetaldehyde cannot be polymerized cationically by conventional techniques.⁸

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#### Résumé

Du chloral a été polymérisé au moyen d'initiateurs cationiques et anioniques, et les produits obtenus ont été comparés. Les catalyseurs anioniques produisent facilement un polymère de haut polds moléculaire (DP  $\sim$  300-600), mais un DP de 200 seulement a pu être réalisé avec les catalyseurs cationiques. Le système anionique initie et propage la polymérisation beaucoup plus facilement que le système cationique. Cet effet est attribué aux effets inductifs des atomes de chlore sur le chloral. On a trouvé une légère différence lorsqu'on compare des produits de DP semblables par diffraction aus rayons-X, par étude infra-rouge et par l'étude de la traction. On croit que ceci est dû au type unique de structure qui est favorisée stériquement. Différents composés cycliques du chloral n'ont pas pu être polymérisés par initiation cationique. Les conditions requises pour effectuer l'ouverture du cycle étaient trop sèvéres pour permettre à la polymérisation d'avoir lieu.

#### Zusammenfassung

Chloral wurde mit kationischen und anionischen Startern polymerisiert und die Polymerisationsprodukte verglichen. Anionische Katalysatoren führen leicht zu hochmolekularen Polymeren (DP  $\sim 300-600$ ), mit kationischen Katalysatoren konnte aber nur ein DP von 200 erreicht werden. Im anionischen System verläuft Polymerisationsstart und Wachstum offenbar viel leichter als im kationischen. Dieser Effekt wird auf die induktiven Effekte der Chloratome im Chloral zurückgeführt. Produkte mit ähnlichem DP zeigte nur geringe Unterschiede im Röntgenbeugungsdiagramm, im Infrarotspektrum und in der Verarbeitbarkeit. Wahrscheinlich ist dies dadurch bedingt, dass nur ein einziger Strukturtype sterische begünstigt ist. Verschiedene zyklische Chloralverbindungen konnten bei kationischem Start nicht zur Polymerisation gebracht werden. Die zur Ringöffnung erforderlichen Bedingungen waren zu extrem, um das Eintreten einer Polymerisation zu ermöglichen.

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## Preparation and Aromatization of Poly-1,3-cyclohexadiene and Subsequent Crosslinking. III*

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#### **Synopsis**

The polymerization of 1,3-cyclohexadiene with *n*-butyllithium has given white polymers with inherent viscosities up to 0.23 and conversions to 98%. Bromination and pyrolysis of these polymers lead to polyphenyls which can be successfully sulfonated, then fused in molten alkali to give phenols, and finally crosslinked with formaldehyde. The final products display good heat stability, in that there is no weight loss on heating to 400°C. and only 30% loss at 900°C.

#### **INTRODUCTION**

In previous work^{1,2} on the polymerization of 1,3-cyclohexadiene, Ziegler catalysts and cationic initiators were found to effect polymerization but only to give products with inherent viscosities of 0.11–0.16. However, considerable success was achieved in the aromatization of these products by bromination and subsequent pyrolysis.

Kovacic and co-workers³⁻⁷ have converted benzene to polyphenyl, which is brown in color. In contrast, the polymer obtained from cyclohexadiene is black, and the halogen content is approximately 1% or less. Dawans and LeFebvre⁸ have also reported the polymerization of cyclohexadiene and its subsequent aromatization but only discussed the final product in general terms. It was the purpose of this investigation to prepare high molecular weight polyphenyl, to convert it to a poly(phenyl hydroxide), and to crosslink it in the Bakelite manner, thereby obtaining a product superior in heat stability properties to either the simpler polyphenyls or Bakelite polymers.

## **RESULTS AND DISCUSSION**

### Polymerization of 1,3-Cyclohexadiene

Cyclohexadiene was prepared in good yield by the addition of bromine to cyclohexene followed by dehydrobromination.⁹ Monomer free from ben-

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zene and cyclohexene impurities was difficult to obtain, since 1,3-cyclohexadiene has been found to disproportionate readily.⁸ However, further addition of these impurities (benzene and cyclohexene) did not seem to affect the polymerization.

Previously untried Ziegler catalysts (Table I) were prepared and used but were found to be generally no more successful than those used before to obtain high molecular weight polymers. Attempted polymerizations with butyllithium at low temperatures, lithium dispersions, and titanium tetrachloride also gave very low yields or oils (Table II).

	Ziegler Catalysts											
No.	Hep- tane, ml.	Mono- mer, moles	AlR₃, moles	MX _n , moles	Time, days	Tem- pera- ture, °C.	Conver- sion, %	[η] inh				
1	50	0.0525	0.003ª	0.0015 ^b	12	30	_	-				
<b>2</b>	140	0.06	0.748ª	0.419°	14	30	1.9	_				
3	140	0.06	0.748ª	0.419°	14	-78	—					
4	140	0.06	0.748ª	$0.419^{e}$	14	75	Oil					
5	$140^{d}$	0.06	0.748ª	0.419°	14	30	3.6					
6	50	0.0525	0.003°	0.0015°	12	30	9.5					
7	50	0.0525	0.003e	$0.0015^{f}$	12	30	7.7	Insolubled				
8	100	0.0525	0.01e	$0.005^{b}$	22	30	Trace	$0.035^{d}$				
9	100	0.0525	0.01e	$0.005^{b}$	22	-20	Trace	_				
10	100	0.0525	0.01e	0.01 ^b	22	30	Trace					

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^a Triisobutylaluminum.

^b Titanium tetrachloride.

° Vanadium trichloride.

^d Benzene solvent.

^e Triethylaluminum.

^f Titanium tetrachloride.

TABI	LE II
Polymerizations of	1,3-Cyclohexadiene

No.	Catalyst and amount	Solvent	Yield, $\%$	$[\eta]_{inh}^{a}$
1	BuLi, 0.3 ml. ^b	Heptane	1	0.112
2	TiCl₄, 0.1 ml.ª	Heptane	9	0.142
3	Lithium, 0.405 g. ^e	Benzene	Oil	
4	Lithium, 0.180 g.°	Benzene	Trace	
5	Lithium, 0.060 g. ^e	Benzene ^f	Trace	_
6	Lithium, 1.550 g.º	Benzene ^f	Oil	

^a In benzene solvent at 30.0°C.

^b Volume of 3.1M solution in heptane.

° In a nitrogen atmosphere.

^d Volume of 7.55M solution in heptane.

^e Actual weight of lithium contained in a 30% mineral oil suspension.

^f In an argon atmosphere.

*n*-Butyllithium has been noted for its excellence as a catalyst for the specific *cis*-1,4 polymerization of conjugated dienes.^{8,10} Use of this catalyst in benzene solution of 1,4-cyclohexadiene did indeed afford polymers with consistently higher inherent viscosities, 0.23 (molecular weight of approximately 20,000) and conversions, 98%, than those of polymers obtained with Ziegler catalysts (Table III).

No.	Catalyst vol., ml. ^b	Time, hr.	$\frac{\%}{Conversion}$	$[\eta]_{inh}^c$
1	0.25	104	19	0.11
2	0.50	66 ^d	77	0.153
3	0.10	66 ^d	24	0.189
4	0.75	69 ^d	<b>62</b>	0.125
5	0.50	68	53	0.169
6	1.00	70 ^d	47	0.143
7	0.05	234	1.0	0.093
8	0.10	234	54	0.212
9	0.10	234°	3.5	0.131
10	0.10	234'	2.4	0.11
11	0.13	234 ^r	4.1	0.11
12	0.05	$234^{f}$	0.5	0.089
13	0.10	5 weeks ^f	48	0.165
14	0.10	5 weeks'	24	0.230
$15^{g}$	0.3	9 weeks	1.0	0.112
16 ^h	17	32 days	98.2	0.20

TABLE III Polymerizations of 1,3-Cyclohexadiene with Butyllithium^a

^a With 5 ml. monomer at room temperature except as noted.

^b Volume of 3.10*M* butyllithium solution in heptane.

^e In benzene with No. 100 viscometer at 30.0°C.

^d Under argon instead of nitrogen.

• At −20°C.

^f At 60°C.

^g At  $-80^{\circ}$ C. in 25 ml. of heptane.

 $^{\rm h}$  Run at 60 times the usual volume; catalyst added in 1.0-ml. increments over 30 days.

Tetrahydrofuran as a solvent for these butyllithium polymerizations proved satisfactory although viscosities were somewhat less than those obtained by the use of benzene as solvent (Table IV). Low temperatures can be utilized to increase the percent conversion and viscosity.

Infrared spectra of all polymer samples were essentially superimposable. The most significant band is the double-bond stretching frequency at 1650 cm.⁻¹. No band was observed for a hydroxyl group which might have arisen from chain termination by nucleophilic attack and heterocyclic ring cleavage of tetrahydrofuran.

It has been proposed⁸ that in benzene solution this polymerization is terminated by chain transfer and disproportionation to give cyclohexadiene

No.	Temp., °C.	Time, days	Catalyst vol., ml.*	Conver- sion, %	[ŋ] inb ^b
1	25	3	2.0	81	0.032
2	25	3	1.5	80	0.036
3	25	3	1.0	71	0.054
4	25	3	0.5	40	0.079
5	50	3	2.0	75	0.050
6	50	3	1.0	79	0.037
7	-20	7	2.0	82	0.038
8	-20	7	1.0	84	0.056
9	-80	6	1.0	85	0.115
10	-80	6	2.0	85	0.113

 TABLE IV

 Polymerization of Cyclohexadiene in Tetrahydrofurant

^a Volume of 3.1M solution of n-butyllithium in heptane.

^b In benzene at 30°C.

and phenyl endgroups. Elucidation was attempted with ultraviolet spectroscopy, but the results are only partially useful, in that the bands present (261.1, 254.7, 248.7, and 242 m $\mu$ ) could be due to cyclohexadiene or phenyl endgroups or to benzene solvent trapped in the lattice.¹¹ The only conclusion available is that chain termination by transfer does occur and is accompanied by an indeterminate amount of disproportionation.

In comparison, ultraviolet spectra of samples polymerized in tetrahydrofuran solution consisted only of very weak shoulders at approximately 265 m $\mu$ . This obviously denotes much less chain transfer and disproportionation. These data and the observation of the loss of yellow color (long-chain anions) near the completion of the reaction tend to support the termination mechanisms postulated for alkyllithium-catalyzed polymerization of conjugated dienes in tetrahydrofuran.^{12,13} The ultraviolet



spectra showed no dependence on reaction temperature in the tetrahydrofuran series.

## **Preparing Polyphenyl**

The aromatization^{1,2} of polycyclohexadiene has been investigated further and data are compiled in Tables V and VI. The bromination (Table V) with either N-bromosuccinimide or bromine⁸ was carried out at high temperature to promote allylic substitution. Bromine, in a ratio of two moles to each recurring unit, was the preferred agent, since it evidently gave a higher degree of bromination. The resultant product contained approximately only one bromine per recurring unit due to considerable dehydrobromination occurring simultaneously with bromination. Dawans and

	Brominating		Analysis		Empirical	Yield
No.	agent	C, %	Н, %	Br, %	formula	%≞
1	Br ₂	71.31	7.57	19.03	C ₆ H _{7.5} Br _{0.25}	95
<b>2</b>	$NBS^{b}$	77.54	4.81	15.91	$C_6H_{4.4}Br_{0.2}$	92.5
3	$\mathbf{Br}_2$	49.49	3.02	43.29	$C_{6}H_{4,4}Br_{0,8}$	83.3
4	$\mathbf{Br}_2$	54.05	3.27	37.23	$C_6H_{4.4}Br_{0.7}$	79.7
5	$\mathbf{Br}_2$	50.02	2.88	40.36	$C_6H_{4.1}Br_{0.75}$	78.6
6	$\mathrm{Br}_2$	53.22	3.88	43.40	$C_6H_{5,2}Br_{0,73}$	95
7	$\mathbf{Br}_2$	52.63	3.96	42.68	$C_6H_{5,4}Br_{0,73}$	83.8

TABLE V Bromination of Polycyclohexadiene

^a Based on the empirical formula.

^b N-Bromosuccinimide.

	Start- ing ma-	Time,	Temp.,		Analysi	8	Empirical	Yield,
No.	terial ^a	hr.	°C.	C, %	Н, %	Br, %	formula	% ^ь
1	l°	15	200	89.78	8.71	1.08	$C_6H_7Br_{0.01}$	83.5
		27	300					
2	2°	42	300	89.65	5.12	4.82	$C_6H_{4,1}Br_{0,05}$	87.5
3	3ª	25	350	87.04	4.22	4.68	$C_{6}H_{3.5}Br_{0.05}$	82.0
4	4d	25.5	350	87.74	4.35	1.36	$C_6H_{3.6}Br_{0.01}$	75.5
		17	160					
5	3°	16.5	260	72.24	3.74	19.84	$C_6H_{3.7}Br_{0.25}$	88.5
		19.5	300					
		17	160					
6	4	16.5	<b>260</b>	77.13	4.00	12.65	$C_6H_{3.7}Br_{0.15}$	77.8
		19.5	300					
7	$5^{d}$	56.5	350	82.89	4.26	6.27	$C_6H_{3.7}Br_{0.07}$	85.7
8	5°	24	300	76.74	3.70	10.92	$C_{6}H_{3.5}Br_{0.13}$	64.1
		31	350					
9	6°	120	400	95.32	5.12		$C_{6}H_{3,9}$	77.2
		42°	260					
10	7	23°	360	91.41	4.98	1.63	$C_6H_{3.92}Br_{0.16}$	85.5
		83	380					

TABLE VI Pyrolysis of Brominated Polymer

^a From Table II.

^b From polycyclohexadiene based on empirical formula.

• With no heat transfer agent, in vacuo.

^d With *p*-terphenyl heat transfer agent.

^e At atmospheric pressure.

LeFebvre,⁸ however, reported complete bromination and dehydrobromination in one step but used only one mole of bromine per recurring unit. Pyrolysis (Table VI), promoting complete dehydrobromination, to produce polyphenyl can be accomplished with or without a heat transfer agent (*p*terphenyl). The use of this agent is more difficult experimentally but per-

#### P. E. CASSIDY, C. S. MARVEL, AND S. RAY

mits utilization of lower temperatures and shorter reaction times. About 1% of bromine remains in almost all dehydrogenated polymers.

## **Crosslinking Polyphenyl**

Samples of polyphenyl from both cyclohexadiene and benzene were sulfonated with the use as reagents of chlorosulfonic acid, fuming sulfuric acid, and concentrated sulfuric acid (Table VII), the last being the most satisfactory experimentally. The carbon:sulfur ratio can be varied from 6:1 (1 sulfur per ring) to 36:1 (1 sulfur per 6 rings) merely by changing reaction time and temperature. As the degree of sulfonation decreased, the yield increased and the solubility decreased. If the sulfur:ring ratio was 1:1.5 or greater, the samples were soluble in acetone-water or ethanol-water. No other solvents were found.

	Start- ing ma-	Time,	Temp.,	Cemr., Yield,		Analysis			
No.	teriala	hr.	°C.	g. ^b	С, %	H, %	<b>S</b> , %	Sulfur: ring	
1	c	113	250	0.96 ^d	47.86	1.86	20.01	1:1	
<b>2</b>	с	48	200	1.93	43.97	2.73	16.19	4:5	
3	с	40	150	1.32	67.34	3.31	11.81	2:5	
4	с	19	100	1.05	79.31	4.10	5.88	1:6	
5	7	12	50	1.21	58.54	2.82	7.95	1:3.3	
6	7	24	100	1.38	49.85	2.10	11.16	1:2	
7	7	36	150	1.51	47.49	1.98	13.18	1:1.7	
8	7	48	200	$1.20^{e}$	46.93	1.75	13.07	1:1.7	
9	7	96	250	$0.38^{e,f}$	51.25	1.76	13.38	1:1.7	
10	7	40	115	1.30	56.45	2.74	11.77	1:2	
11	10	24	60	1.01	89.45	4.75	1.78	1:20	
12	10	24	200	$1.08^{e}$	57.81	2.79	12.29	1:2	
13	11 ^g	24	115	1.17	71.69	3.76	7.88	1:4	

TABLE VII Sulfonation of Polyphenyl

^a Product number from Table VI unless otherwise noted.

^b Based on 1.0 g. of starting material.

^c Polyphenyl prepared by Dr. P. Kovacic.

^d Inherent viscosity in 1:1 acetone-water at 30°C. is 0.148.

• Loss of product occurred during washing.

^f Inherent viscosity in 1:1 acetone-water at 30°C. is 0.057.

 $^{\mu}$  Fusion product number 11 from Table VIII was resultonated since it had a very low degree of substitution.

All sulfonated products were somewhat hygroscopic. Infrared analyses of mineral oil mulls of these compounds showed weak sulfonic acid bands at 3500, 1320, and 1040 cm.⁻¹ which are not present after alkali fusion.

A polyelectrolyte effect is exhibited for soluble samples. Shown in Figure 1 are the changes in viscosity and pH with changes in concentration for ethanol and aqueous ethanol solutions, respectively, of polyphenyl-

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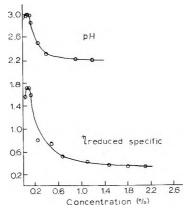


Fig. 1. Viscosity in ethanol and pH in ethanol-water (1:1) for sulfonated polyphenyl.

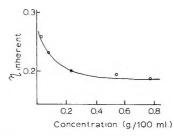


Fig. 2. Viscosity of sulfonated polyphenyl in acetone-water (1:1) (compound 1, Table VII).

sulfonic acid. This effect is less noticeable but still evident when aqueous acetone is used as solvent (Fig. 2).

Fusion of the sulfonated polymers was conducted with sodium hydroxidepotassium hydroxide mixtures to give products in which approximately 97% of the sulfonic acid groups were replaced by hydroxyl (Table VIII). Again, the polymer was black and brittle and soluble only in acetone-water or ethanol-water and only when the degree of substitution was high. Infrared analysis was poor due to the inability to make good mulls; however, a band at 3600 cm.⁻¹ (OH stretch), which had not been present previously, appears.

The only apparent difference between the two types of polyphenyl up to this point is that on fusion; compounds prepared from Kovacic's polyphenyl undergo a decrease in molecular weight, demonstrated by a decrease in inherent viscosity (0.148-0.034), whereas viscosities of sulfonated polymers from cyclohexadiene showed essentially no change (0.057-0.054) on fusion.

Poly(hydroxyphenyl) was crosslinked with formaldehyde (Table IX) with the usual base-catalyzed Bakelite procedure,¹⁴ and the products were submitted to thermogravimetric analysis. It is readily noted that the thermal stability increases with decreasing substitution (Fig. 3). The limit of this tendency was not determined.

	Starting material	Yield,	Analysis					
No.	no.ª	g. ^b	C, %	Н, %	<b>S</b> , %	Residue, %		
1	1	0.56°	47.79	2.99	1.11	$26.87^{d}$		
<b>2</b>	2	0.71	75.79	4.61	2.98	0.59		
3	3	0.63	84.08	4.65	0.47	${<}0.2$		
4	4	0.60	87.82	4.72	0.69	3.07		
5	5	0.65	82.32	4.21	0.26			
6	6	0.60	80.03	4.03	0.38	0.61		
7	7	0.52	77.46	3.86	0.58			
8	8	0.44	72.56	3.84	2.62	1.36		
9	9	$0.20^{e}$	70.72	3.82	1.67	1.14		
10	10	0.66	77.49	3.93	1.01			
11 ^f	11	0.98	89.02	4.67	0.55			
12	12	0.66	75.51	4.04	0.81	1.12		
13	13	0.85	86.64	4.83	0.29			

TABLE VIII Alkali Fusion of Poly(benzenesulfonic Acid)

^a Product number from Table VII.

^b Based on 1.0 g. of starting material.

^e Inherent viscosity in 1:1 acetone-water at 30°C. is 0.034.

^d Iron oxide due to incomplete washing with acid.

° Inherent viscosity in 1:1 acetone-water at 30°C. is 0.054.

 $^{\rm f}$  Since this compound had a very low degree of substitution it was resulfonated in reaction 13, Table VII.

	Starting	Wt. starting		Analysis				
No.	material no.ª	material, g.	Yield, g.	C, %	Н, %	Residue %		
1	2	1.26	1.36	68.68	4.53	6.23		
2	3	1.00	1.16	74.91	4.25	5.71		
3	4	1.00	1.25	81.01	4.80	8.22		
4	5	1.00	1.12	76.43	4.97	0.97		
5	6	1.00	1.04	77.19	3.91	1.57		
6	7	0.25	0.80	75.75	3.65	1.54		
7	8	0.75	0.77	71.74	3.71	2.74		
8 ^b	10	1.50°	1.35	82.45	3.40	1.12		
9	10	1.50°	1.34	80.61	3.26	2.85		

TABLE IX Crosslinking Reactions

^a Product number from Table VIII.

^b Acid-catalyzed reaction.

 $^{\rm o}$  Used 15.0 ml. of 37% aqueous formal dehyde in these runs.

Acidic catalysis for crosslinking was also investigated with only slight improvement. However, the samples used for Figure 4 were pyrolyzed before thermogravimetric analysis to remove water and low molecular weight fractions and thereby to improve the TGA curve.

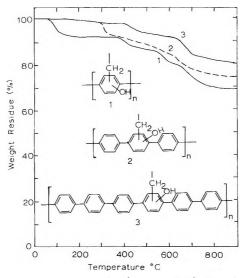


Fig. 3. Thermogravimetric curves for (1) polymer 1, Table IX; (2) polymer 2, Table IX; (3) polymer 5, Table IX.  $\Delta T = 150^{\circ}$ C./hr.; N₂ atmosphere.

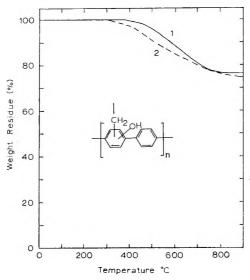


Fig. 4. Thermogravimetric curves for crosslinked polymers: (1) acid-catalyzed polymer 8, Table IX, and (2) base-catalyzed polymer 9, Table IX.  $\Delta T = 150^{\circ}$ C./hr., N₂ atmosphere.

All crosslinked products were hard, black, infusible powders and insoluble in all available solvents.

## **EXPERIMENTAL**

Elemental analyses were performed by Micro-Tech, Skokie, Illinois, and thermogravimetric analyses by Dr. G. Ehlers, Materials Laboratory, WADD.

#### Materials

All solvents were purified, distilled and dried thoroughly before use. The concentration of the commercial *n*-butyllithium in heptane (Beacon Chemical Industries, Cambridge, Mass.) was determined to be 3.10*M* by the double titration method.¹⁵ 1,3-Cyclohexadiene was distilled twice from a spinning band column (b.p. 78.0°C.,  $n_D^{30}$  1.4675) to give a product which still contained 4% benzene, 1% cyclohexene, and 2% cyclohexane impurities upon analysis by gas chromatography.

## Infrared and Ultraviolet Spectra

Infrared spectra of poly-1,3-cyclohexadiene samples were taken on a Perkin-Elmer Infracord from films prepared on salt windows from chloroform solutions. Spectra of other compounds were taken from Fluorolube mulls.

Solutions for ultraviolet spectra were prepared by dissolving 0.1–0.2 g. of polycyclohexadiene in 10 ml. of spectra grade chloroform. Spectra were then taken in 1 cm. cells on a Cary Model 11 recording spectrophotometer from 400 to 235 m $\mu$ .

#### Poly-1,3-cyclohexadiene

**From Ziegler-Type Catalysts.** In general, the procedures reported previously² were used (see Table I).

From Lithium Dispersions. In either a nitrogen or an argon atmosphere samples of a 30% lithium dispersion were weighed into syringe bottles containing deoxygenated benzene which were capped and shaken to suspend the lithium. Then 5.0 ml. (4.2 g.) of pure 1,3-cyclohexadiene was injected and the mixtures were shaken at room temperature for three weeks. The catalyst was carefully decomposed with isopropyl alcohol and then methanol to yield gummy grey residue (Table II).

**From** *n***-Butyllithium in Benzene.** Into a capped syringe bottle were injected 5.0 ml. each of 1,3-cyclohexadiene (4.2 g.) and benzene. The catalyst was added after thermal equilibration and the yellow solution was shaken.

In terminating the reaction, the viscous solution was diluted with benzene and precipitated slowly into 250 ml. of methanol containing N-phenyl-2-naphthylamine antioxidant to give a white fibrous solid which was washed with methanol and dried *in vacuo* (Table III).

ANAL. Calcd. for (C₆H₈): C, 90.00%; H, 10.00%. Found: C, 89.69%; H, 10.22%.

**From** *n***-Butyllithium in Tetrahydrofuran.** The same procedure is used here as with benzene solvent (Table IV).

#### **Bromination of Poly-1,3-cyclohexadiene**

With Bromine.⁸ In a 250-ml., three-necked flask equipped with a pressure-equalizing dropping funnel, mechanical stirrer, mantle, and con-

denser with an outlet over a sodium hydroxide solution trap, was placed 100 ml. of 1,1,2-trichloroethane and 10.0 g. of poly-1,3-cyclohexadiene. This solution was brought to reflux under nitrogen and a solution of 40 g. of bromine (C=C/Br₂ = 1/2) in 60 ml. of solvent was added slowly over 24 hr. After a total of 72 hr. of reaction, the mixture was cooled and poured into 1 liter of methanol to obtain a brown precipitate which was washed with methanol and dried (Table V).

With N-Bromosuccinimide. To a hot polymer solution prepared as that above was added cautiously a mixture of 24.5 g. of N-bromosuccinimide and 3.0 g. of benzoyl peroxide. The reaction mixture was poured into methanol and the precipitate was extracted thoroughly with methanol to remove succinimide to leave a yellow-brown polymeric residue (Table V).

### Pyrolysis of Brominated Poly-1,3-cyclohexadiene

Without Heat Transfer Agent. The brominated polycyclohexadiene was placed in a round-bottomed flask which was in turn repeatedly evacuated and filled with nitrogen to insure removal of oxygen. Then, while under vacuum, the flask was heated in a Wood's metal bath at the proper temperature for the alotted time. The black residue was pulverized, extracted with benzene, and then with methanol, and dried (Table VI).

ANAL. Calcd. for  $(C_6H_4)_n$ : C, 94.70%; H, 5.30%. Found: See Table VI.

With Heat Transfer Agent. This process was the same as that previously reported¹ except that the product was insoluble (Table VI).

## **Sulfonation of Polyphenyl**

Into a three-necked, round-bottomed flask equipped with a mantle, thermometer, mechanical stirrer, and gas inlet and outlet is placed the sulfuric acid (50 ml./g. of starting material unless otherwise stated). This is brought to the proper temperature under a nitrogen atmosphere. The polyphenyl is then added and after reaction the black mixture is cooled to room temperature and poured over ice. The black solid is isolated by suction filtration and washed well with water and dried in a vacuum oven at 100°C. Excessive washing with water results in a loss of product. If the degree of sulfonation is high, the pastelike product must be isolated and washed by using a centrifuge since filtration is very difficult (see Table VII for other experimental details).

## Alkali Fusion of Poly(phenylsulfonic Acid)

In an iron crucible were mixed 5.0 g. of potassium hydroxide and 5.0 g. of sodium hydroxide under nitrogen and heat was applied to produce a melt (300 °C.). To this was added with stirring 1.0 g. of sulfonated polyphenyl. The higher the degrees of sulfonation, the more the reaction foamed. After 12–24 hr. the mixture was cooled, dissolved in water and acidified with 6N hydrochloric acid. The black precipitate was isolated by filtration, washed well with concentrated hydrochloric acid to remove iron

impurities, washed with water, and dried in a vacuum oven at 100°C. (Table VIII).

#### Crosslinking of Poly(hydroxyphenyl)

Into a 50-ml. flask equipped with a magnetic stirrer and a reflux distilling head was placed 10 ml. of 37% aqueous formaldehyde and 0.10 g. of technical barium hydroxide (oxalic acid was used for acidic catalysis) and the solution was heated to reflux and 1.0 g. of poly(hydroxyphenyl)was added.¹⁴ After heating for 24 hr., the mixture was cooled and the product was removed by filtration. The black powder was triturated and washed well with water and dried *in vacuo*. The samples used for Figure 4 were heated at 300-400°C. for 38 hr. under vacuum prior to thermogravimetric analysis. The more highly substituted starting materials were obviously better for this reaction due to their greater solubility. In the elemental analyses of these products, the high thermal stability was probably responsible for the residues (Table IX).

The authors wish to thank Dr. Peter Kovacic for his samples of polyphenyl.

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## Résumé

La polymérisation du 1.3-cyclohexadiène avec le n-butyllithium donne des polymères blancs possédant une viscosité inhérente allant jusqu'à 0.23 et des taux de conversion allant jusqu'à 98%. La bromation et la pyrolyse de ces polymères donne des polyphényles, qui peuvent être sulfonés avec succès, puis subir la fusion alcaline pour donner des phénols et enfin être pontés avec le formaldéhyde. Les produits finaux résistent très bien à la chaleur. Il n'y a pas de perte de poids en chauffant jusqu'à 400°C et seulement 30% à 900°C.

#### POLY-1,3-CYCLOHEXADIENE. III

#### Zusammenfassung

Die Polymerisation von 1,3-Cyklohexadien mit *n*-Butyllithium lieferte weisse Polymere mit Viskositätszahlen bis zu 0,23 bei Umsätzen bis zu 98%. Bromierung und Pyrolyse dieser Polymeren führt zu Polyphenylenen, die erfolgreich sulfoniert und dann in geschmolzenem Alkali unter Bildung von Phenolen gelöst und schliesslich mit Formaldehyd vernetzt werden können. Die Endprodukte zeigen insofern gute Hitzebeständigkeit, als beim Erhitzen auf 400°C kein Gewichtsverlust und bei 900°C nur ein solcher von 30% auftritt.

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# Kinetics of Polymerization of Styrene Initiated by Substituted Benzoyl Peroxides. III. Induced Decomposition

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#### **Synopsis**

The polymerization of styrene has been initiated by redox systems consisting of diethylaniline and symmetrically substituted benzoyl peroxides. Decomposition rate constants and efficiencies of initiation were determined by the dead-end technique. Hammett plots of these rate constants and of those previously determined for polystyryl-radical induced decomposition of substituted benzoyl peroxides have the same slope, suggesting that an  $S_{H2}$  mechanism is involved in the radical attack on peroxides just as in the radical attack on disulfides. The predictive ability of a combined Hammett-type equation was shown to be excellent for the decomposition rate constants of initiating systems consisting of both substituted diethylaniline and substituted benzoyl peroxide. The effect of substituents on the efficiency of initiation remains unexplained.

In the preceding paper¹ a study of the kinetics of thermal decomposition of symmetrically substituted benzoyl peroxides at 90°C. produced values for the unimolecular decomposition rate constants and also for the constants for decomposition induced by the growing polystyryl free radical  $(k_x)$ . It is of interest to compare these latter values with the rate constant  $k_d$  for the well known decomposition induced by N,N-dialkylanilines.²⁻⁴ Walling and Indicator³ have shown that dimethylaniline (DMA) probably induces the decomposition of benzoyl peroxide via an  $S_N^2$  attack on the peroxide oxygen by the amine nitrogen.

The decomposition of unsubstituted benzoyl peroxide induced by substituted diethylanilines (DEA) has previously been studied⁵ and the decomposition rate constants correlated with the Hammett  $\sigma$ . The value of  $\rho$  was found to be -2.7. In the work reported in this communication, the same experimental procedure was followed, and rate constants and efficiencies were calculated by the "dead-end" technique.⁴ Measurements were made at 30 and at 60°C.

The value of the rate constants and efficiencies derived from the dead-end calculations are shown in Table I. Figure 1 shows a Hammett plot of these rate data together with the induced decomposition rate constants

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	Efficie	ency $f$	$k_d  imes 10^3$ , l./mole-sec.	
Substituent	30°C.	60°C.	30°C.	60°C.
p-Methoxy	0.04		0.65	
p-Methyl	0.07		1.14	
None	0.08	0.04	2.29	12.5
p-Chloro	0.12	0.06	19.4	55.1
<i>m</i> -Bromo	0.10		39.2	_
3,4-Dichloro	0.14	0.03	110.	646.

TABLE I
Decomposition Rate Constants and Efficiencies of Polymerization Initiation for
Symmetrically Substituted Benzoyl Peroxides Induced by Dimethylaniline

from the preceding paper.¹ The slope of the plot gives a value for  $\rho$  of +1.6. This value, obtained for 30 and 60°C., is the same as that obtained by Imoto and Choe² at 5°C. and demonstrates that  $\rho$  for the amine-induced decomposition is not temperature-dependent. This permits comparison with the 90°C. data obtained for the radical-induced decomposition,¹ which, since the data fall on the same line, has the same  $\rho$  value.

While this work was in progress Pryor and Guard⁶ obtained the first unambiguous proof that so-called  $S_H2$  reactions, bimolecular radical displacement reactions, have the same sort of transition state as the wellknown  $S_N2$  reactions. Their evidence took the form of a linear free

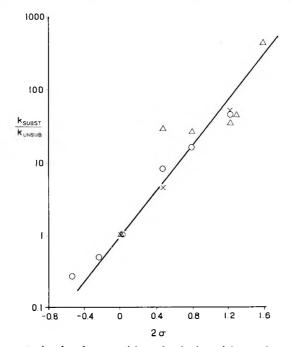


Fig. 1. Hammett plot for decomposition of substituted benzoyl peroxides induced by (O) dimethylaniline at 30°C.; dimethylaniline at ( $\times$ ) 60°C.; ( $\triangle$ ) polystyryl radicals at 90°C.

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energy relation between the rate constants for nucleophilic and free radical attacks on the disulfide bond. Pryor had earlier suggested⁷ that the  $S_{H2}$  reaction might occur when free radicals attack either disulfides or peroxides, but experimental proof had been lacking.

There is some question as to the point of attack of a polystyryl radical on benzoyl peroxide. Walling and Savas⁸ have suggested that the ability to form charge transfer complexes in the transition states determines whether the radical-induced decomposition of benzoyl peroxide proceeds via a direct attack at the peroxide oxygen or by a concerted mechanism involving attack by the radical on the *ortho* or *para* ring positions. Secondary alkyl radicals attack the ring, while acyl radicals and radicals derived from ethers and alcohols attack the peroxide bond itself.⁸ In the absence of product studies it cannot be definitively said which occurs in the case of a polystyryl radical. However, the polystyryl radical is certainly quite capable of behaving as an electron donor, as demonstrated by its copolymerization behavior. It can also readily stabilize charge transfer complexes with the peroxide linkage, so it is not unreasonable to assume that attack does occur at the peroxide bond, the same linkage which DMA attacks.

If this is true, then the data reported in this and the preceding paper¹ form exactly the same sort of proof for peroxides as Pryor has established for disulfides.⁶ The rate constants for peroxide decomposition induced by polystyryl radicals  $(k_x)$  and by dimethylaniline  $(k_d)$  obey the same linear free energy relation. It may therefore be concluded that the transition state requirements are quite similar, and that the radical-induced decomposition of peroxides follows an  $S_H 2$  mechanism analogous to the  $S_N 2$  mechanism of their induced decomposition.³

When symmetrically substituted peroxides are used, Figure 1 demonstrates that the following Hammett equation holds for the decomposition rate constant  $k_d$ :

$$\log (k_d(\mathbf{X}, \mathbf{H}) / k_d(\mathbf{H}, \mathbf{H})) = 1.6 \ (2\sigma_X) \tag{1}$$

where the subscript (X,H) refers to the peroxide substituent, X, and unsubstituted DMA. An earlier paper⁵ demonstrated that the analogous relation held for the reaction between unsubstituted peroxide and DEA having ring substituent Y:

$$\log \left( k_d(\mathbf{H},\mathbf{Y}) / k_d(\mathbf{H},\mathbf{H}) \right) = -2.7 (\sigma_{\mathbf{Y}}) \tag{2}$$

Since there is little difference between the reactivity of DMA and DEA we may combine eqs. (1) and (2) to obtain.

$$\log \left( k_d(\mathbf{x}, \mathbf{y}) / k_d(\mathbf{H}, \mathbf{H}) \right) = 1.6 \ (2\sigma_x) - 2.7 \ (\sigma_y) \tag{3}$$

We have tested this equation experimentally by using a variety of substituted diethylanilines and benzoyl peroxides with each other as initiators of styrene polymerization at 30°C. The values of f and  $k_d$  are given in Table II, along with the values of  $k_d$  calculated from eq. (3). The excellent agreement which can be noted over more than three orders of

DEA			$k_{d} imes 10^{2}$ , l	
substituent (X)	Benzoyl peroxide substituent (Y)	$f imes 10^2$	Observed	Calc'd. from eq. (3)
m-CH ₃	<i>m</i> -Br	7.7	6.01	6.91
	p-Cl	15.2	2.53	2.13
	<i>p</i> -CH ₃	9.9	0.212	0.112
p-Cl	<i>m</i> -Br	11.7	0.994	1.13
	$p ext{-Cl}$	11.1	0.202	0.354
	p-CH ₃	16.9	0.024	0.019
p-CN	<i>m</i> -Br	27.2	0.175	0.095
•	(Unsubsti-	> 25	<0.004	0.0022
	tuted)	(46) ^a		

TABLE II

Comparison of Observed and Calculated Rate Constants for Decomposition of Substituted Benzoyl Peroxides Induced by Substituted Diethylanilines

^a Calculated from values of initial  $R_p$  and calculated  $k_d$ .

magnitude variation in  $k_{d(X,Y)}$  suggests that the rate-determining step in decomposition is not at all complicated by ring substitution of either the amine or the peroxide.

However, when we consider the efficiencies of initiation contained in Table I and II and reference 5, it is more difficult to discern a pattern. Figure 2 shows a plot of some of the observed efficiencies versus  $2\sigma_X$  or  $\sigma_Y$ . It can be seen that when the peroxide is unsubstituted, electron-with-drawing groups on the amine strongly increase the efficiency. However when the amine is unsubstituted, electron-withdrawing groups on the peroxide increase the efficiency very little. And, if the amine has the electron-withdrawing *p*-chloro group, the efficiency is at a maximum for unsubstituted peroxide. This latter fact may be connected with the stabilization of benzoate radicals by both electron-withdrawing and electron-donating groups as noted in the previous paper.¹ A more detailed explanation of the efficiency variation must await further work.

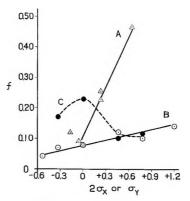


Fig. 2. Effect of substituents on efficiency:  $(\Delta) f$  vs.  $\sigma_{\mathbf{Y}}$  when  $\sigma_{\mathbf{X}} = 0$ ; (0) f vs.  $2\sigma_{\mathbf{X}}$  when  $\sigma_{\mathbf{Y}} = 0$ ; ( $\bullet$ ) f vs.  $2\sigma_{\mathbf{X}}$  when  $\sigma_{\mathbf{Y}} = +0.23$  (p-Cl).

Support of this work by the Petroleum Research Fund and by the National Institutes of Health is greatly appreciated.

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#### Résumé

La polymérisation du styrène a été initiée par des systèmes redox: la diéthylaniline et le peroxyde de benzoyle substitué symmétriquement. Les constantes de vitesse de décomposition et les efficacités a'initiation ont été déterminées par la technique de désactivation des fins de chaîne. Les diagrammes de Hammett pour ces constantes de vitesse et ceux déterminés antérieurement pour la décomposition induite du radical polystyryl des peroxydes de benzoyle substitués ont la même pente, ce qui fait supposer qu'un mécanisme  $S_{H2}$  intervient dans l'attaque des peroxydes par le radical, comme dans l'attaque des disulfures par un radical. On a montré qu'une équation combinée du type Hammett s'est avérée excellente pour prédire les constantes de vitesse de décomposition de systèmes initiateurs contenant de la diéthylaniline substituée et le peroxyde de benzoyle substitué. L'effet des substituants sur l'efficacité de l'initiation reste inexpliqué.

#### Zusammenfassung

Die Polymerisation von Styrol wurde mit Redoxysystemen aus Diäthylanilin und symmetrisch substituierten Benzoylperoxyden gestartet. Zersetzungsgeschwindigkeitskonstanten und Startausbeuten wurden nach dem "dead-end"-Verfahren bestimmt. In den Hammett-Diagrammen dieser Geschwindigkeitskonstanten und der früher für die Polystyrylradikal-induzierte Zersetzung substituierter Benzoylperoxyde bestimmten tritt die gleiche Neigung auf, was dafür spricht, dass beim Radikalangriff an Peroxyden ebenso wie beim Radikalangriff an Disulfiden ein  $S_{H2}$  Mechanismus auftritt. Eine Gleichung vom Hammett-Typ war ausgezeichnet zur Voraussage von Zersetzungsgeschwindigkeitskonstanten in Startersystemen aus substituiertem Diäthylanilin und substituiertem Benzoylperoxyd geeignet. Der Einfluss der Substituenten auf die Startausbeute bleibt ungeklärt.

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## Reactivity of Condensed-Ring Hydrocarbons as Polymerization Retarders*

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### **Synopsis**

Seventeen condensed-ring hydrocarbons have been investigated as retarders or inhibitors of styrene and methyl methacrylate polymerization. Rates were measured dilatometrically. Nine of the compounds tested retarded or inhibited the polymerization of styrene, but methyl methacrylate appears not to be affected by this class of substances. Styrene data obtained are examined in the light of Fukui's "frontier electron" formalism for correlating structure and reactivity. It is concluded that the principal locus of radical attack is at the meso carbon atoms, Fukui's  $(S_s)$  region, and that a substantial value of the  $(S_s)$  density index is required for retardation, although when the molecule also possesses an appreciable  $(S_p)$  index, a synergistic action is noted. The point is made that since condensed-ring hydrocarbons do not have "functional groups" in the sense that quinones and other retarders do, the effect of monomer reactivity is likely to be of added importance in determining retarder efficiency. The lack of retardation effects in polymerizing methyl methacrylate is interpreted from this standpoint. A reverse chaintransfer reaction is tentatively proposed to account for the observed behavior.

## **INTRODUCTION**

The relationship between structure and reactivity of condensed-ring hydrocarbons has been a subject of intense experimental and theoretical interest for over a generation. The extremely mobile  $\pi$ -electron systems, giving rise to variations in electron density, delocalizability, and other semiempirical parameters, permit these molecules to participate in many types of chemical reactions especially those involving free-radical intermediates. Greatly intensifying such interest is the well known carcinogenic activity of many condensed-ring hydrocarbons and their derivatives. Thus there has resulted a voluminous literature concerned with these compounds, broadly ranging from physical studies of their spectral and magnetic properties to biological animal screening programs. Emphasis has been experimental, theoretical, and even polemical upon occasion.

Considering the background of the field it is somewhat surprising to find that so little investigation has been carried out of the reactivity of condensed-ring systems in polymerizing monomers. A priori, it might be predicted that such compounds could well act as retarders or inhibitors of

^{*} Taken, in part, from the Ph.D. thesis of S. P. Sood, University of Hawaii, 1963.

vinyl polymerization. Yet only three brief reports have so far appeared in the literature,¹⁻³ the latest since the completion of this study. It seemed, then, of more than passing interest to investigate the quantitative kinetics of polymerization retardation and inhibition in the presence of such substances as one further step in the slow development of retardation mechanisms.

The present study was limited to the behavior of simple condensed-ring hydrocarbons, without side chains or heteroatoms, in the homo-polymerization of styrene and methyl methacrylate initiated by 2,2'-azobisisobutyronitrile. Another severe limitation is the very limited solubility of many of these compounds in the pure monomers and in other nonpolar aromatic and aliphatic solvents. This last factor probably precludes a truly complete mechanism study of this kind.

## **EXPERIMENTAL**

## **Materials**

Styrene monomer from Ram Chemicals Inc. was first distilled under reduced pressure in a nitrogen atmosphere. The distillate was washed several times with 2% sodium hydroxide, distilled water, 1% sulfuric acid, and finally with distilled water until the washings were neutral. It was then dried with calcium hydride overnight and refractionated in an all-glass apparatus employing a nitrogen bleed under reduced pressure. The column used was vacuum-jacketed and filled with about 90 cm. of glass helices. Only the constant-boiling middle fraction was collected. The monomer thus purified was stored in specially constructed containers under nitrogen and kept frozen in a Dry Ice-acetone mixture until used.

Methyl methacrylate from Rohm and Haas Co. was washed with 2% sodium hydroxide until there was no further dark coloration from the hydroquinone stabilizer. After rinsing with distilled water, the monomer was refrigerated overnight over a calcium chloride-sodium sulfate mixture. It was then fractionated in the same way as was styrene and stored in Pyrex, low-actinic flasks under refrigeration.

2,2'-Azobisisobutyronitrile from Eastman Organic Chemicals was recrystallized several times from methanol. Only the first crop of crystals was collected in each stage. This material was stored under refrigeration and recrystallized periodically.

The condensed-ring hydrocarbons used in this study are listed in Table I summarizing the experimental results. Most were obtained commercially, although some were synthesized for this work, for which particulars are available elsewhere.⁴ Briefly, these compounds were purified by extensive recrystallization and sublimation where practical. All were chromatographed by using alumina and silica columns (usually both). Melting points and, where possible, infrared spectra were checked with literature values.

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#### Dilatometry

Polymerization reaction rates were followed by vacuum dilatometry. The temperature was  $44.4^{\circ}$ C. and controlled within  $\pm 0.005^{\circ}$ C. The experimental procedure has been described earlier,⁵ and details, including calibration, may be found elsewhere.⁴ Slight modifications in the mixing steps were made necessary by the slow rate of dissolution observed with many of the hydrocarbon retarders, especially in the cold. Although the

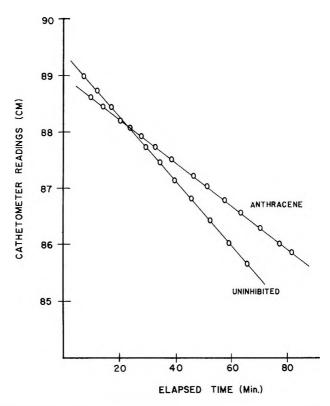


Fig. 1. Primitive kinetic data for vacuum dilatometric experiments, polymerization of styrene initiated by AIBN, with and without the presence of anthracene.

exact zero time was of importance only when inhibition periods were observed, all mixing and warming steps were performed in a uniform, timed sequence which gave satisfactory reproducibility. Preparation time varied between 10 and 20 min. depending upon solubility, and the first cathetometer readings of the liquid levels in the dilatometer capillaries could be made approximately 10-12 min. after immersion in the thermostat.

Figure 1 shows a sample plot of a run with styrene and initiator only and the same system retarded with anthracene. Figure 2 shows styrene runs in the presence of varying amounts of 3,4-benzpyrene which produced well defined inhibition periods of length T.

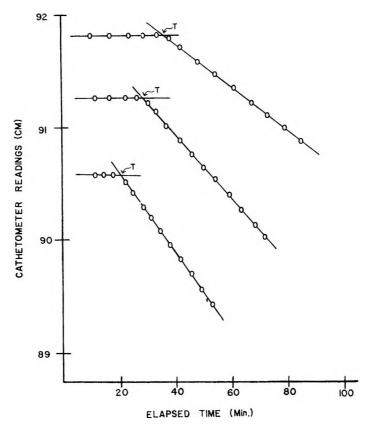


Fig. 2. Primitive kinetic data, polymerization of styrene initiated by AIBN in the presence of different concentrations of 3,4-benzpyrene.

#### RESULTS

Table I summarizes the experimental results obtained with styrene. Following Kice,⁶ we define  $\phi = r/r_0$ , where r is the rate of the retarded polymerization and  $r_0$  is the rate of the unretarded polymerization calculated for the same initiator concentration. Under our conditions  $r_0$  in per cent per hour was determined to be  $r_0 = 6.12$  [AIBN]^{1/2}, where [AIBN] is the molar concentration of initiator. The final column in Table I is a calculated rate value for those hydrocarbons which exhibited retardation. This was done where appropriate in order to obtain comparable rates for different reactions for one initiator concentration.

In addition to the hydrocarbons listed in Table I, 2,3-benzanthracene, pentacene, picene, and 2',1'-anthra-1,2-anthracene were tested. Their poor solubility in styrene monomer did not permit sufficient variation in concentration to allow reliable rate data to be collected.

Methyl methacrylate data are given in Table II. For this monomer the unretarded rate in per cent per hour was found to be  $r_0 = 29.3 \text{ [AIBN]}^{1/2} + 0.18$ , in satisfactory agreement with previous work.⁷

The absence of retardation action in this monomer even for 2',3'-naphtho-3,4-pyrene, a potent retarder of styrene polymerization, is perhaps the most striking feature of the present study.

## **Kinetic Analysis of Results**

We employ the generally serviceable Kice scheme as follows:

$I \rightarrow R \cdot$	Rate = $2k_d f$	(1)
$\mathbf{R} \cdot + \mathbf{M} \rightarrow \mathbf{R} \cdot$	$k_p[\mathbf{R} \cdot ][\mathbf{M}]$	(2)
$\mathbf{R}\cdot +\mathbf{X} \rightarrow \mathbf{Z}\cdot$	$k_x[\mathbf{R} \cdot ][\mathbf{X}]$	(3)
$\mathbf{Z} \cdot + \mathbf{M} \rightarrow \mathbf{R} \cdot$	$k_0[\mathbf{Z} \cdot ][\mathbf{M}]$	(4)
$1 \cdot + R \cdot \rightarrow$ Inactive products	$k_c[\mathbf{R}\cdot][\mathbf{Z}\cdot]$	(5)
$Z \cdot + Z \cdot \rightarrow$ Inactive products	$2k_{z}[\mathbf{Z}\cdot]^{2}$	(6)
$R \cdot + R \cdot -$ Inactive products	$2k_{\iota}[\mathbf{R}\cdot]^2$	(7)

where f represents the initiator efficiency, X the added retarder, and Z the radical formed by reaction of R  $\cdot$  with retarder, either by the addition of R  $\cdot$  to X or by transfer to R  $\cdot$  from X. The other symbols have their usual meaning. From the usual steady-state assumptions an expression relating the pertinent variables is obtained:

$$\phi^{2}[X]/(1 - \phi^{2})(1 + \{1 + [C(1 - \phi^{2})/\phi]\})^{1/2}$$

$$= 2k_{t}R/k_{p}k_{x}\{1 + [C(1 - \phi^{2})]/\phi^{2}\}^{1/2} + 2k_{0}k_{t}[M]/k_{x}k_{c} \quad (8)$$

where R is defined as  $-d \ln [M]/dt$  and  $C = 4k_tk_z/k_c^2$ . Since cross termination is known to be the preferred mode, the value of C is assumed to have an upper limit of unity and, usually, to be very much less than one. In the present work an assumed value of  $C = 1.0 \times 10^{-4}$  gave straight-line plots of the experimental data for retarded polymerizations (but not for inhibited ones). Equation (8) is limited, in that the concentration of X must remain sufficiently constant over a period of time long enough to permit an accurate measure of the initial rate, which itself must not be too small. By considering these points, eq. (8) simplifies to:

$$\phi^{2}[\mathbf{X}]/(1 - \phi^{2}) = k_{l}R/k_{p}k_{x} + k_{0}k_{l}[\mathbf{M}]/k_{x}k_{c}$$
(9)

which was the form used. The rate constants  $k_0$  may indeed be a combination of constants involving  $\mathbb{Z}$ . in such reactions as:

$$\mathbf{Z} \cdot \rightarrow \mathbf{R} \cdot + \mathbf{X} \tag{10}$$

$$Z \cdot + M \rightarrow ZH + R \cdot$$
 (11)

$$\mathbf{Z} \cdot + \mathbf{M} \to \mathbf{X} + \mathbf{P} + \mathbf{R} \cdot \tag{12}$$

where P represents a polymer molecule, not kinetically significant, and  $\mathbb{R}$ . is a monomeric chain-carrying radical. For long-chain conditions, eq. (9) reduces to:

$$(1 - \phi^2)/\phi^2 = (k_x k_c/k_0 k_t) [X]/[M]$$
(13)

Hydrocarbon	Hydro- carbon concn. $\times 10^3$ mole/l.	$[AIBN]^{1/2} \times 10^2,$ mole/l.	T, min.	<i>r</i> , %/hr.	φ	Calc. rate %/hr., at [AIBN] ^{1/2} $\times 10^2 =$ 4.75 mole/l.
Nerhthalana	39.0	6.16		0.357	0.954	
Naphthalene	121.	7.49		0.357 0.455	0.993	
Phenanthrene	27.7	5.77		0.357	1.01	
rnenantmene	27.7 21.1	6.83		0.357 0.415	0.993	
Chryson	$\frac{21.1}{12.7}$	4.64		0.413 0.267	0.933 0.942	
Chrysene					0.942 0.971	
Demon	14.6	6.73		0.400		
Pyrene	29.7	5.49		0.347	1.03	
	52.8	6.35		0.395	1.02	
Triphenylene	23.7	5.47		0.361	1.08	
	45.4	6.30		0.382	0.991	
Perylene	10.4	6.67		0.405	0.992	
	15.8	6.67		0.405	0.992	
1,2-Benzpyrene	7.56	4.64		0.285	1.00	
	13.7	4.64		0.287	1.01	
1,2,3,4-Dibenzanthracene	5.43	4.87		0.301	1.01	
	1.46	4.87		0.298	1.00	
1,2-Benzanthracene	4.21	4.65	16	0.292	1.01	
	4.82	4.65	17	0.289	1.02	
	5.49	4.65	18.5	0.267	0.94	
	6.22	4.65	20.5	0.257	0.91	
	8.11	4.65	24.5	0.286	1.00	
	9.20	4.65	27	0.290	1.02	
1,2,5,6-Dibenzanthracene	0.832	4.65	14.5	0.289	1.01	
	1.01	4.65	15.5	0.320	1, 12	
	1.47	4.65	17.5	0.249	0.875	
	1.90	4.65	19	0.233	0.82	
	2.15	4.65	20	0.305	1.07	
	3.50	4.65	25.5	0.294	1.03	
3,4-Benzpyrene	1.95	4.66	19	0.188	0.660	
	2.19	4.66	20	0.180	0.632	
	2.78	4.66	22.5	0.165	0.579	
	3.47	4.66	25.5	0.148	0.520	
	4.12	4.66	28	0.136	0.478	
	5.61	4.66	34.5	0.136	0.478	
Anthracene	3.70	4.75		0.252	0.866	
	6.65	4.75		0.226	0.777	
	8.92	4.75		0.208	0.715	
	10.4	4.75		0.199	0.684	
	12.6	4.75		0.184	0.631	
	15.8	4.75		0.163	0.560	
	18.0	4.75		0.151	0.520	
	19.25	4.75		0.147	0.509	
	33.1	4.75		0.126	0.433	
	34.9	4.75		0.121	0.416	

TABLE I	
Styrene Polymerization Rates in the Presence of Hydrocarbon Retarders	

Hydrocarbon	Hydro- carbon concn. $\times 10^3$ mole/l.	$[AIBN]^{1/_2} \times 10^2,$ mole/l.	<i>T</i> , min.	<i>r</i> , %/hr.	φ	Calc. rate %/hr., at [AIBN] ^{1/2} $\times 10^2 =$ 4.75 mole/l.
1.2,9,10-Dibenznaphtha-						
cene	0.175	4.75		0.277	0.953	
	0.619	4.75		0.245	0.843	
	1.31	4.75		0.203	0.698	
	1.73	4.75		0.182	0.625	
	2.445	4.75		0.152	0.523	
	3.54	4.75		0.125	0.430	
	4.34	4.75		0.113	0.388	
	5.09	4.75		0.100	0.344	
1,2,3,4-Dibenzpyrene	0.980	4.75		0.258	0.887	
	1.42	4.75		0.245	0.842	
	1.904	4.75		0.230	0.790	
	3.20	4.75		0.198	0.680	
	3.65	4.75		0.188	0.646	
	4.26	4.75		0.175	0.601	
1,2,7,8-Dibenznaphtha-						
cene	0.425	4.75		0.254	0.873	
	0.597	4.75		0.240	0.825	
	0.700	4.75		0.233	0.801	
	0.812	4.75		0.224	0.770	
	0.938	4.75		0.216	0.742	
2,3,7,8-Dibenzphenan-						
threne	0.712	5.42		0.271	0.816	0.242
	0.935	5.42		0.254	0.765	0.223
	1.17	5,42		0.236	0.711	0.207
	1.45	5.42		0.219	0.660	0.191
	1.63	5.42		0.208	0.629	0.183
2',3'-Naphtho-3,4-pyrene	0.21	6.43		0.176	0.451	0.131
	0.494	6.43		0.103	0.262	0.076
	0.807	6.43		0.072	0.183	0.053
	1.84	6.43		0.042	0.107	0.031
	2.25	6.43		0.034	0.0864	0.025

TABLE I (continued)

which compared with eq. (8) shows that the long-chain criterion is:⁵

$$k_0/k_c \gg R/k_p[\mathbf{M}] \tag{14}$$

which is in agreement with the observation of Kice⁸ that  $k_0/k_c$  is a measure of the relative stabilities of the intermediate radicals  $\mathbb{Z}_{\cdot}$ .

Table III gives kinetic data from plots of eq. (9), and Figure 3 shows a sample plot.  $k_i$  and  $k_p$  were calculated for this temperature from the relationships of Matheson and co-workers.⁹

Three of the compounds tested produced sharply defined inhibition periods. They were: 3,4-benzpyrene, 1,2,5,6-dibenzanthracene, and 1,2-

Hydrocarbon	$\begin{array}{c} \text{Hydrocarben}\\ \text{concn.,} \times 10^{3}\\ \text{mole/l.} \end{array}$	$\frac{[\text{AIBN}]^{1/2}}{\times 10^2},$ mole/l.	r, %/hr.	$\phi$
Naphthalene	16.5	4.24	1.62	1.14
•	4.79	5.26	1.77	1.03
Phenanthrene	6.09	7.05	2.22	0.98
Anthracene	11.8	5.25	<b>2</b> , $00$	1.17
	8.26	5.74	2.10	1.13
	4.49	5.53	1.66	0.92
3,4-Benzpyrene	3.52	5.80	1.77	0.94
	1.11	6.46	2.01	0.97
2',3'-Naphtho-3,4-				
pyrene	1.31	6.92	<b>2</b> . 05	0.94
	0.432	6.92	2.10	0.96

TABLE II Methyl Methacrylate Polymerization Rates in the Presence of Hydrocarbons

benzanthracene. As can be seen from Table I, the first of these caused a retarded rate after the inhibition period. In all three cases the length of the inhibition period (corrected by subtracting the time zero determined from a plot of T versus initial concentration of inhibitor)⁴ was directly proportional to the initial concentration of added hydrocarbon. If the stoichiometric coefficient  $\mu$  is calculated according to the well-known expression,  $T = \mu[\mathbf{Z}]/2k_d f$ , where T is the corrected inhibition time, [Z] the initial inhibitor concentration, and  $2k_d f$  the rate of initiation, it is found that the chain-

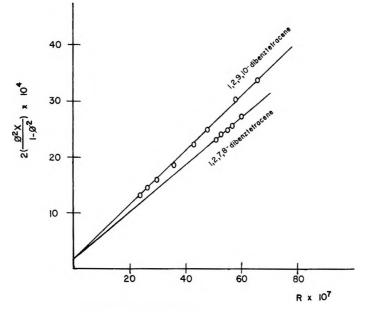


Fig. 3. Plot of kinetic eq. (9) for two typical retarders.

	k 2,		$k_o/k_c \times$	
	l./mole-sec.	$k_x/k_p$	1010	
2',3'-Naphtho-3,4-pyrene	22,000	240	8.5	
1,2,7,8-Dibenztetracene	1,460	13	4.5	
1,2,9,10-Dibenztetracene	1,260	13	3.4	
Anthracene	170	2	2.0	
3,4-Benzpyrene	1,360	14	24.0	
2,3,7,8-Dibenzphenanthrene	1,260	13	0.5	
1,2,3,4-Dibenzpyrene	550	6	10.6	

TABLE III Rate Constants for Retarders of Styrene Polymerization

stopping equivalence is very low. For all three substances it is approximately  $10^{-3}$ .

## DISCUSSION

Condensed-ring hydrocarbons differ from conventional polymerization retarders, i.e., quinones, phenols, nitro compounds, etc., in that they do not possess "functional groups" in the sense that this term is commonly used in organic chemistry. Their reactivity appears to be a function of the distribution and density of the electrons (especially  $\pi$ -electrons) in different "regions" of the molecules. Numerous attempts have been made to correlate chemical behavior with electronic pattern and energies as determined by molecular-orbital calculations. The various treatments differ in the approximations employed (all of them drastic simplifications) and in the terminologies used by their proponents. While one such system may show better correlation for certain classes of reactions than another, there is usually considerable equivalence in their respective approaches to the problem. Most recognize two distinct regions or loci of reactivity: (1) the "meso-atoms" (by analogy with the 9 and 10 positions of anthracene) and (2) the "exposed bond" (such as that connecting the 9 and 10 positions of phenanthrene). These regions are depicted in Figure 4 for the example of 1,2-benzanthracene.

An additional common feature is that each system defines at least one semiempirical parameter to express the relative energies of electrons in these two regions, and thus their tendency to interact with attacking reagents. The parameters are known by such names as "free valency," "localization energy," "super-delocalizability," "frontier electron density," and the like.

Within the scope of the present study, we have found the greatest degree of consistency in the treatment of Fukui and co-workers.¹² Very briefly, they relate chemical reactivity to what are called "frontier electrons." These are defined as the two electrons occupying the highest  $\pi$ -orbital in the ground state and are regarded as valencelike in nature. In the formation of a covalent  $\sigma$ -bond between the attacking reagent and the  $\pi$ -electron system, the position of greatest density of the two electrons in the highest

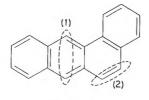


Figure 4.

molecular orbital of the ground state is most susceptible to attack by an electrophilic reagent. For a nucleophilic reagent it is the lowest vacant orbital in the ground state at which reaction is most likely to occur. Radical reactions, however, are predicted to be most likely to occur at the position of higher density of the two electrons, one in the highest ground-state orbital and the other in the lowest orbital. Positions (1) and (2) above are labeled  $(S_s)$  and  $(S_p)$  regions, respectively, with reactivity at each site directly proportional to a numerical index of frontier electron density.

In applying the Fukui scheme to the present data, it must be recognized that any conclusions can only be of the most guarded sort, not only because of the limited number of compounds available for test but also because of the limitations of the Fukui method itself, some of whose assumptions have been criticized.¹⁰⁻¹³ The following discussion then is of value primarily for its possible predictive value for future studies of alkyl-substituted and heterocyclic derivatives of these hydrocarbons.

From Table I it is seen that the first eight hydrocarbons did not retard styrene polymerization.

Table IV lists the hydrocarbons tested, in the same order as in Table I, with their Fukui super-delocalizability indices. The first eight compounds had no effect upon the polymerization rate of styrene; the next three gave inhibition periods (with a subsequently retarded rate in the case of 3,4benzpyrene); and the remaining compounds behaved as retarders.

It is immediately apparent that compounds not possessing an  $(S_s)$  region will not have any retarding effect with styrene. It seems also that retardation will not be observed for substances lacking an  $(S_p)$  region unless the  $(S_s)$ index is in excess of a threshold value lying somewhere between 0.72 and 0.93 (cf. 1,2,3,4-dibenzanthracene and anthracene). When both regions exist in the molecule, interaction of the two  $\pi$ -electron centers in the direction of enhanced reactivity may be expected. Thus 1,2,5,6-dibenzanthracene with a relatively low  $(S_s)$  index produces inhibition, and 3,4-benzpyrene with high values for both indices showed both inhibition and retardation.

It is probably safe to conclude that the principal locus of attack by a growing styryl radical is in the  $(S_s)$  region—at a *meso* carbon, at least for retarders. Although there are too few examples of inhibitors, it is not unreasonable to suggest that competition between attack at  $(S_s)$  and  $(S_p)$  regions may well determine whether a given compound will act in this way or as a retarder or as both.

	$(S_p)$ region	$(S_s)$ region
Naphthalene	_	
Phenanthrene	0.7306	
Chrysene	0.7811	
Pyrene	0.7865	
Triphenylene	_	
Perylene		_
1,2-Benzpyrene	0.8491	
1,2,3,4-Dibenzanthracene	_	0.7159
1,2-Benzanthracene	0.7594	0.8757
1,2,5,6-Dibenzanthracene	0.7844	0.5725
3,4-Benzpyrene	0.8151	1.0148
Anthracene		0.9348
1,2,3,4-Dibenzpyrene	0.7818	0.9696
1,2,9,10-Dibenznaphthacene	0.5332	0.8649
1,2,7,8-Dibenznaphthacene	0.5703	0.7899
2,3,7,8-Dibenzphenanthrene	0.7722	0.8189
2',3'-Naphthopyrene	0.7209	1.0542

TABLE IV Frontier Electron Density Indices for Hydrocarbons

On the basis of the data available no quantitative correlation between index values and  $k_x/k_p$  ratios emerges, although the strongest retarder, 2',3'naphthopyrene, has the highest  $(S_s)$  index, and the weakest retarder, anthracene, is the one retarder which receives no assist from an  $(S_p)$  region. Comparison of the  $k_0/k_c$  values shows much less of a spread than with  $k_x/k_p$ . This indicates that the intermediate radicals,  $Z \cdot$ , within ca. 1.5 orders of magnitude, have about the same stability. This may be rationalized partially if our assumption that  $\mathbf{R} \cdot$  radical attack occurs at a welldefined region (or two such) of the molecule rather than randomly. The result is that the range in the numbers of equivalent canonical structures for  $Z \cdot$  radicals is considerably less than the range in numbers of such structures which may be constructed from the parent hydrocarbons.

Perhaps the most significant reason for the discrepancies between the spread in  $k_x/k_p$  values compared with that for the corresponding  $k_0/k_c$  ones is that retarding efficiency is as closely tied to the mode of disappearance of Z · radicals as to their stability. Because of the steric bulk of the Z · radicals reaction (6) is even less likely than usual. For the same reason, reaction (5) may not be available in certain cases as in 2',3'-naphthopyrene, where the second  $(S_s)$  position is blocked. Since transfer to styrene monomer is known to be low, it is not likely that reaction (12) is an important mode of Z · destruction. Beyond this it is not safe to speculate until more is known about the relative copolymerization affinity (if any) of the hydrocarbons and also until we have more hints about  $(S_p)$  and  $(S_s) \pi$ -electron interaction. It is most unfortunate that pentacene and 2',1'-anthra-1,2-anthracene could not be tested in order to shed light on this last point.

Finally, some note should be taken of the dramatic difference between the reactivity of these condensed-ring hydrocarbons with styryl and with methyl methacryl radicals. Earlier it was pointed out that these retarders acted not by virtue of "functional groups" serving as radical interceptors but rather through differences in localized  $\pi$ -electron density. Retarding or inhibition efficacy will be a more subtle, less clear-cut function of molecular structure than with other classes of retarders—as may be inferred from the preceding discussion. In such a case it is to be expected that differences in monomer reactivity should cause pronounced differences in retarder reactivity.

For an observable retardation the  $\mathbb{R}$  · radical formed from the monomer must be sufficiently reactive to form  $\mathbb{Z}$  · with the hydrocarbon (perhaps initially as a  $\pi$ -complex). If the surrounding monomer is reactive enough to abstract  $\mathbb{H} \cdot$  from  $\mathbb{Z} \cdot$  or its complex, stabilization through re-aromatization results. If the monomer is not sufficiently reactive for this to happen and if another  $\mathbb{R} \cdot$ -capturing event does not take place quickly, the complex will break down to reform  $\mathbb{R} \cdot$  and X. Since styrene monomer is considerably more reactive than methyl methacrylate monomer, while the (inverse) reactivity difference of their radicals is less great, the polymerizing styrene system probably combines the two features to a greater extent than the methyl methacrylate system. Mechanistically, it is only necessary to invoke a reverse-transfer step to account for our observations:

$$Z + M \longrightarrow Z M \longrightarrow HM + RX$$
(15)

where RX is the alkyl-substituted hydrocarbon molecule. Comparing this with the usual process with a chain-transfer agent, S,

$$R + S \longrightarrow E \cdot S \longrightarrow RH + S \cdot (16)$$

it is seen that in reaction (15)  $\mathbb{H}$ . transfer is from radical to molecule while in reaction (16) it is from molecule to radical. The importance of reaction (15) will depend upon the reactivity difference of the two monomers and should be proportional to their reactivity difference with a given chain transfer agent. Put another way, in conventional chain transfer the more reactive radical abstracts the labile hydrogen from the transfer agent most readily, while in retarder stabilization the more reactive monomer abstracts  $\mathbf{H} \cdot \mathbf{most}$  readily.

In a comparison of transfer constants of styrene and methyl methacrylate with *n*-butyl mercaptan, Walling¹⁴ found the styryl radical to be 33 times as effective as the methyl methacryl radical in abstracting  $H \cdot$  from the sulfhydryl group.

It is interesting to note that the reverse transfer reaction (15) proposed here has also been suggested very recently¹⁵ as one possible explanation for the retarding action of diphenyl, another substance without the usual functional-group substituents.

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## Résumé

On a étudié l'effet retardateur ou inhibiteur de dix-sept hydrocarbures à noyaux condensés, sur la polymérisation du styrène et du méthacrylate de méthyle. Les vitesses ont été mesurées par dilatométrie. Parmi ces composés, neuf retardent ou inhibent la polymérisation du styrène, mais il semble que cette classe de substances n'affecte pas le méthacrylate de méthyle. Les données obtenues pour le styrène ont été examinées à la lumière du formalisme utilisé par Fukui "de la barrière électronique" en vue de relier structure et réactivité. On a conclu que l'attaque radicalaire se fait principalement sur l'atome de carbone méso, la région  $(S_s)$  de Fukui, et que l'effet retardateur requiert un indice de densité  $(S_s)$  important bien que l'on note une action synergétique lorsque la molécule possède aussi un indice  $(S_p)$  appréciable. On fait remarquer que l'effet de la réactivité du monomère a probablement une importance supplémentaire pour déterminer l'efficacité du phénomène retardateur puisque les hydrocarbures à noyaux condensés n'ont pas de groupes fonctionnels comme en ont les quinones et d'autres agents retardateurs. C'est de ce point de vue qu'on interprète le manque d'effet retardateur dans la polymérisation du méthacrylate de méthyle. On propose une réaction inverse de celle du transfert de chaîne pour rendre compte du comportement observé.

#### Zusammenfassung

Siebzehn kondensierte Ringkohlenwasserstoffe wurden als Verzögerer oder Inhibitoren der Styrol- und Methylmethacrylatpolymerisation untersucht. Die Geschwindigkeit wurde dilatometrisch gemessen. Neun der untersuchten Verbindungen verzögerten oder inhibierten die Styrolpolymerisation, Methylmethacrylat scheint jedoch von dieser Klasse von Substanzen nicht beeinflusst zu werden. An Styrol erhaltene Ergebnisse werden im Lichte des "Elektronenfront"-Formalismus von Fukui zur Korrelierung von Struktur und Reaktivität überprüft. Man kommt zu dem Schluss, dass der Hauptort des Radikalangriffs die Mesokohlenstoffatome, Fukui's  $(S_s)$ -Bereich, ist und dass ein wesentlicher Wert des  $(S_s)$ -Dichteindex zur Verzögerung erforderlich ist; da das Molekül daneben auch einen merklichen  $(S_p)$ -Index besitzt, wird eine synergistische

Wirkung festgestellt. Da kondersierte Ringkohlenwasserstoffe keine "funktionellen Gruppen" im Sinne der Chinone und anderen Verzögerer besitzen, ist wahrscheinlich der Einfluss der Monomerreaktivität von zusätzlicher Bedeutung bei der Bestimmung der Verzögererwirksamkeit. Der Mangel eines Verzögerungseffekts bei polymerisierendem Methylmethacrylat wird von diesem Gesichtspunkt aus interpretiert. Eine umgekehrte Kettenübertragungsreaktion wird versuchsweise zur Erklärung des beobachteten Verhaltens angenommen.

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# **Infrared Spectra of Polybutadienes**

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# Synopsis

It is shown, by analytical resolutions of the spectra of isomerized cis-1,4-polybutadienes, that the band due to hydrogen out-of-plane vibrations of cis-CH=CH groups appears at 740 cm.⁻¹ and that the apparent shift of this band to lower frequencies, as the amount of cis-CH=CH decreases in a polybutadiene, is due to the presence of other bands in this region. Some possibilities as to the origins of these other bands are discussed. It is also shown that there are some bands in the 10-11  $\mu$  region of polybutadiene spectra which are probably connected with vibrations of cis-CH=CH groups and that there probably are others which are not due to either cis-CH=CH or trans-CH=CH or CH₂=CH. Some possibilities regarding the origins of these bands are discussed. The bands found here explain in large measure the appearance of polarization spectra of high-cis 1,4-polybutadienes.

# **INTRODUCTION**

The frequency of the hydrogen out-of-plane vibration of the *cis*-CH=CH group in the spectra of polybutadienes has been the subject of considerable discussion. It is important not only in connection with determining the microstructures of polybutadienes but also in regard to the actual configuration of such polymers. On the basis of the spectra of emulsion and sodium polybutadienes Hampton¹ assigned this vibration to a band at 730 cm.⁻¹, while Binder² assigned it to a band at 680 cm.⁻¹. From the spectra of high-cis-1,4 polybutadienes, such as described by Natta³ and others, Silas, Yates, and Thornton⁴ considered all the absorption in the 12.5–15.5  $\mu$  region to be due to *cis*-CH==CH vibrations but Morero et al.⁵ assigned the above vibration to a band at 741 cm.⁻¹. It was also observed that the position of the *cis*-CH—CH band apparently shifted in the spectra of polybutadienes, made with Ziegler-type catalysts, from 741 cm.⁻¹ toward lower frequencies as the amount of cis-1,4 addition in the polymers decreased. Despite these differences in the assignment of the frequency of the *cis*-CH=CH band, microstructure determinations of polymers made in emulsion systems or with sodium or potassium catalysts were very similar.^{4,5,6} For polymers made with Ziegler-type catalysts, the microstructure determinations were likewise similar.4,5

The shift in the maximum of the absorption from 741 cm.⁻¹, in view of the uncertainty of the assignment of the frequency of the *cis*-CH=CH band, raised the question as to whether it was real or due to the presence

of other bands in this region which remained nearly constant in intensity as the amount of *cis*-1,4 addition decreased. Polarization spectra by Binder⁸ showed that not only was the absorption in the 13–15  $\mu$  region complex but also that, in the 10–11  $\mu$  region, other bands must be present which are not apparent in the usual absorption spectrum.

Various attempts to resolve these bands with prism instruments met with no success. Therefore an analytical method, based on calculating band envelopes was tried. The method used and the results obtained are described here.

### **EXPERIMENTAL**

#### **Isomerization of Polybutadienes**

Polymers containing various amounts of *cis*-CH=CH and *trans*-CH=CH were prepared by isomerizing high-*cis*-1,4 polybutadienes in the manner described by Golub.⁹ The starting polymers were made with alkyl aluminum and cobalt chloride or titanium tetraiodide catalysts. At first benzene solutions of the polymers, 1 g./100 ml, were isomerized with a mercury arc and diphenyl sulfide as initiator. The results reported here were obtained with heptane solutions of the polymers and allyl bromide as initiator. The reasons for using isomerized polymers and the change in the method of isomerization are given later. Aliquots were withdrawn from the reaction vessel at various time intervals and the amounts of *cis*-CH=CH and *trans*-CH=CH in the polymer determined by a method previously described,² except that the band at 1667 cm.⁻¹ was used to determine *cis*-CH=CH.

The results of the analyses showed that the amount of *cis*-1,4 addition in the polymer decreased according to a first-order rate law, as shown in Figure 5. The maximum amount of *trans*-CH=CH found in any of the isomerization experiments was about 75%. The rate of isomerization became very slow after 8 hr and, since considerable gel formed if the isomerization was carried on 24 hr., the reactions were generally stopped after 8 hr.

The main change in the long-wave  $(13-15 \ \mu)$  region of the spectra of the isomerized samples was a gradual shift of the maximum of the absorption at 741 cm.⁻¹ to lower frequencies. Thus the most that could be learned about the frequency of the *cis*-CH=CH band in this region was that it is probably near 740 cm.⁻¹.

# **Resolution of Spectra**

The first attempts to find individual bands in the 13–15  $\mu$  region of the spectra of the isomerized polybutadienes were graphical, each band being calculated by the Lorentz equation

$$D_{\nu} = a/[(\nu - \nu_0)^2 + b^2]$$
(1)

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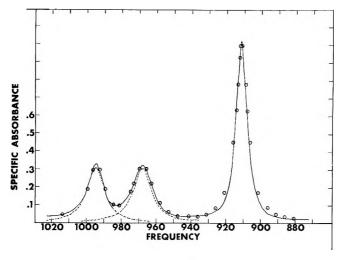


Figure 1.

where  $a = b^2 D_0$ ,  $2b = \Delta \nu$  at  $1/2 D_0$ ,  $\nu_0$  is the frequency of the band center,  $D_{\nu}$  is the absorbance at any frequency  $\nu$ , and  $D_0$  is the absorbance at  $\nu_0$ . It was found that simple spectra of emulsion and sodium polybutadienes in the 10-11  $\mu$  region could be represented by adding the absorbances of a few bands calculated with this equation. One such comparison is shown in Figure 1, and it is clear that the agreement between the calculated and observed spectrum is quite good. In these calculations the values of bwere taken from the bands.

When it was found, in this way, that a large number of bands would be necessary to fit the observed spectra in the 13–15  $\mu$  region, it was decided to resolve the spectra analytically. The absorbance, at any frequency  $\nu$ , in the spectrum is the sum of the absorbances of the individual bands at this frequency. Thus:

$$D_{\nu} (\text{obs}) = D^1 + D^2 + D^3 + \dots$$
 (2)

where  $D^1$ ,  $D^2$ ,  $D^3$ , etc. are the absorbances of bands 1, 2, 3, etc. at the frequency  $\nu$ . From eqs. (1) and (2),

$$D_{\nu} \text{ (obs.)} = a_1 D_0^{-1} + b_1 D_0^{-2} + c_1 D_0^{-3} + (3)$$

where the  $D_0$  are the absorbances at  $\nu = \nu_0$  for the individual bands and the coefficients,  $a_1$ ,  $b_1$ ,  $c_1$ , etc. are calculated from the band width b and the separations of the frequencies of the individual  $D_0$  from the frequency  $\nu$ . A group of simultaneous equations can then be set up which can then be solved for the several  $D_0$ 's.

The band widths b were found from the spectrum, as described below, and the  $D_0$  by trial and error, i.e., by finding the minimum number of bands necessary to fit the spectrum. Band envelopes were calculated by eq. (1) by using a constant band width and various values of  $D_0$ . These were

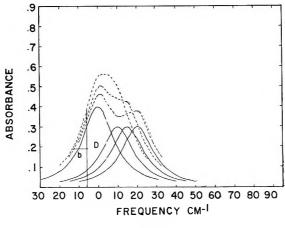
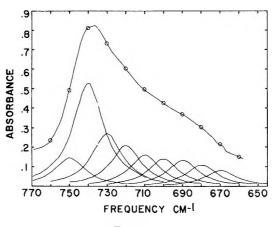


Figure 2.





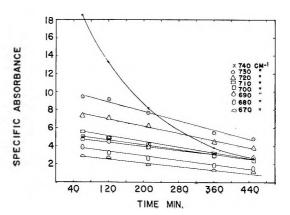
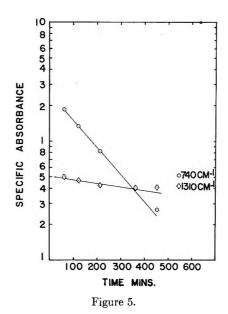


Figure 4.



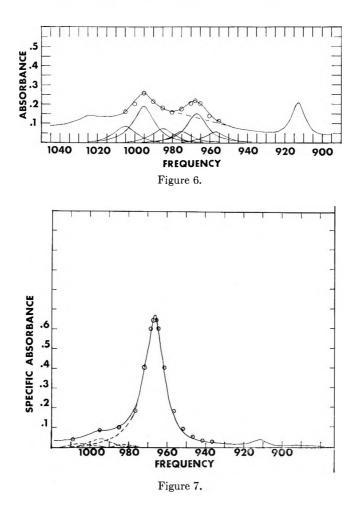
plotted (two envelopes) with various separations of the  $D_0$  and the absorbances added at various frequencies to give a synthetic spectrum. An example of this is shown in Figure 2. On taking a D at any frequency in this spectrum, not near the maximum, the interval between it and the curve at 1/2D was found. In all cases tried this interval was never more than the bused and sometimes about 1 cm.⁻¹ less for b near 10 cm.⁻¹. This same procedure was used with the actual spectra, the steep part between 13 and 13.5  $\mu$  being used. A value of 10 cm.⁻¹ was found for b from the spectrum in the 13–15  $\mu$  region.

trum in the 13-15  $\mu$  region. The coefficients,  $a_1$ ,  $b_1$ , etc., in eq. (3) were found with this value of band by placing bands at various frequencies in the spectrum. Then with the observed absorbances at these frequencies the  $D_0$  values were calculated as well as the band envelopes. The absorbances of the individual bands were added at other frequencies to determine how well they agreed with the actual absorbances at those frequencies. In this way it was found that, for b = 10 cm.⁻¹, bands at 750, 740, 730, 720, 710, 700, 690, and 680 cm.⁻¹ gave the best fit with the observed spectra. It was also found that, with the same bands, changing the b values by  $\pm 2$  cm.⁻¹ changed the  $D_0$  for the strong bands by about 0.005 absorbance units, or, for the same b, changing the band position by 2 cm.⁻¹ changed the  $D_0$  values by about the same amount. These then were about the errors in the band widths and positions and intensities.

The band width of the bands in the 9.5–11.2  $\mu$  region of the spectra of the isomerized polymers was obtained from the spectra directly. While the 910 cm.⁻¹ band had a width of 4.5 cm.⁻¹, the width of the 967 cm.⁻¹ band was found to be 6.5 cm.⁻¹. Since the 967 cm.⁻¹ band appeared to have a small shoulder, attempts were made to resolve the spectra with a

					Molar 5	pecific A	TABLE bsorbances	TABLE I Molar Specific Absorbances of Resolved Bands	lved Ban	ds					
		10-1	11 µ region	u						13-15 µ region	region				
Poly-1005 mer cm. ¹	995 cm. ⁻¹	985 cm. ⁻¹	975 cnì. ⁻¹	967 cm. ⁻¹	957 cm. ⁻¹	760 cm. ⁻¹	750 cm. ⁻¹	740 cm. ⁻¹	730 cm. ⁻¹	720 cm. ⁻¹	710 cm. ⁻¹	700 cm. ⁻¹	690 cm -1	680 cm. ⁻¹	670 em1
		3.21	3.06	21.67	1.22	0.00	5.19	18.58	9.47	7.33	5.66	4.95	4.73	3.84	2.86
		3.63	1.75	39.66	.54	0.74	3.63	13.30	9.15	7.11	4.91	4.87	4.53	3.22	2.71
		3.60	0.00	64.43	0.00	1.33	1.67	8.22	7.64	6.23	4.17	3.99	3.99	2.67	1.99
		3.87	0.00	89.65	0.00	1.40	0.93	3.82	5.50	4.43	3.20	2.86	2.92	1.89	1.31
		3.29	0.00	96.68	0.00	1.32	0.98	2.66	4.75	3.74	2.78	2.33	2.77	1.47	1.07
<b>PA</b> 3.62	7.67	3.13	2.45	6.14	2.47	0.00	6.98	26.04	8.23	77.7	5.77	4.66	6.52	3.49	3.80
		3.17	2.43	18.14	1.86	0.57	3.61	20.91	9.06	7.18	5.53	4.79	5.26	3.86	3.18
		3.29	0.37	36.74	0.85	0.86	2.53	15.13	10.86	5.77	5.51	4.21	5.47	3.29	2.92
		3.22	0.00	67.12	0.00	1.21	0.89	9.79	7.82	5.26	4.24	3.52	4.62	2.58	2.24
		3.83	0.00	82.63	00.00										
		3.18	00.00	89.44	$0^{\circ}, 00$										
		3.05	0.00	100.80	0.00										

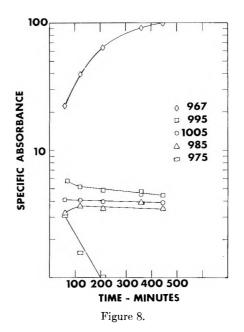
J. L. BINDER



band width of 4.5 cm.⁻¹, but good agreement between the calculated and observed spectra could not be obtained. Consequently a band width of 6.5 cm.⁻¹ was used for the bands between 1005 and 967 cm.⁻¹, and satisfactory agreement (generally within 0.005 absorbance units) was obtained when bands were taken at 1005, 995, 985, 975, 967, and 957 cm.⁻¹.

An example of the resolution of the bands in the  $13-15 \mu$  region for one of the isomerized polymers is given in Figure 3. This polymer was made with aluminum alkyl and cobaltous chloride. Figure 4 shows the molar specific absorbances of those bands for a series of isomerized polymers plotted against time, and Figure 5 shows a plot of the specific absorbances of the 740 cm.⁻¹ band against time of isomerization. The molar specific absorbances are given in Table I.

The resolution of the bands in the  $10-11 \mu$  region is given in Figure 6 for a high-*cis*-1,4-polybutadiene and in Figure 7 for one of the isomerized polymers. The molar specific absorbances of these bands for series of isomerized polybutadienes are given in Table I also. In this table, poly-



mers GA, GB, etc., were isomerized aluminum alkyl-cobaltous chloride polybutadienes and those in the PA, PB, etc. series were isomerized aluminum alkyl-titanium tetraiodide polybutadienes. These absorbances are plotted, in Figure 8, against time of isomerization.

Figures 3, 6, and 7 show that the agreement between the observed and calculated spectra is very good. Figures 4 and 5 show that in the  $13-15 \mu$  region only the 740 cm.⁻¹ band follows a first-order rate law. Figure 8 and Table I show that, probably within the experimental error, the 1005 and 985 cm.⁻¹ bands in the 10-11  $\mu$  region remain essentially constant in intensity during the isomerization and that the 995, 975, and the 957 cm.⁻¹ bands change in intensity according to a first order rate law.

It was shown in the following way that the side vinyl group contributed no absorption to the spectrum at or near 1000 cm.⁻¹. The ratio of the specific absorbances of the 990 and 910 cm.⁻¹ bands was found from the spectrum of a high 1,2-polybutadiene. With this ratio and the intensity of the 910 cm.⁻¹ band in these spectra, the intensity of the 990 cm.⁻¹ band was calculated. It was found to be negligible.

The absorbance versus frequency spectra necessary for this work were obtained in part from transmittance versus wavelength spectra and partly from absorbance versus wavelength spectra, all of which were recorded with a Beckman IR4 instrument. The gain was 3%, the period 8 sec., and the speed 0.2  $\mu$ /min. The chart was expanded in wavelength so that 0.1  $\mu$  required 1 in. of paper. In converting transmittance values and in plotting the absorbances the deviation of the 100% line and the mismatch of the cells were taken into account. Cells of various thicknesses were used so that the transmittance was at least 20%. In plotting the measurements

the scale used was such that 0.002 units in absorbance and 0.2 in frequency could be plotted. The accuracy of the attenuator comb was known to be 1%.

# DISCUSSION

# **Isomerization**

In this work high-cis-1,4-polybutadienes were isomerized to obtain polymers containing various amounts of cis-CH—CH and trans-CH—CH for two reasons. This guaranteed that the only change in the polymer was that due to converting cis-CH—CH to trans-CH—CH and that other features of the polymer would remain unchanged. Such a guarantee would be lacking for polymers made with catalysts which did produce various amounts of cis-CH—CH and trans-CH—CH. Mixtures of a highcis-1,4-polybutadiene and a high-trans-1,4-polybutadiene could have been used to prepare polymer solutions of various amounts of cis-CH—CH and trans-CH—CH but, for these, the absorption maximum at 740 cm.⁻¹ would not shift but merely decrease in intensity.

The isomerizations of *cis*-1,4-polybutadiene did not proceed as far as Golub⁹ reported, either with phenyl disulfide or allyl bromide initiators. In order to eliminate any question of the polymer reacting with initiator, it would have been better to isomerize with  $\gamma$ -radiation. Some experiments¹⁰ were made, but in all cases, so much gel formed that it seemed unwarranted to take the small amount of soluble material to be representative of the whole polymer.

Attempts to isomerize a *trans*-1,4-polybutadiene with phenyl disulfide or allyl bromide initiators were fruitless also. So much gel formed that it was impossible to get a satisfactory spectrum of a film. Thus it was not known how much isomerization occurred.

### **Resolution of Spectra**

While there is a question as to the actual shape of an infrared band, there is no doubt that the apparent trans-CH=CH band at 967 cm.⁻¹, the side vinyl band at 910 cm.⁻¹, or the  $(CH_2)_x$  band in paraffins or polyethylene at 720 cm.⁻¹ can be represented by the Lorentz equation, eq. (1), and that the spectrum in the 10-11  $\mu$  region can be calculated by adding the absorbances of individual bands. The same result was obtained by Richardson and Sacher¹¹ for polyisoprene spectra. In view of this it seemed unnecessary to take into account the effect of finite slit width as Ramsay¹² did to get true band intensities and envelopes. It was assumed here that the band widths b were the same for all bands in a particular wavelength region even though the slit width changed during the recordings. It is probable that the error caused by this assumption is not larger (about 0.005 absorbance units) than the change in the absorbances arising from shifting the positions of the bands slightly. Graphical resolutions have been used by many investigators (see Brode¹³ for references) to locate bands in in spectra. It is thought that the analytical approach is even better.

The general validity of the resolutions given here is attested to by the First, the polarization spectra of high *cis*-1,4-polybutadienes⁸ following. show the presence of additional bands in the 13–15 and 10–11  $\mu$  regions of Some of these appear at about the same frequencies as those the spectra. found by the resolutions which were done quite independently of the results of the polarization spectra. As is pointed out later, the bands found in the 10-11  $\mu$  region explain very well the appearance of the polarization spectra in this region. Second, some isomerized polymer spectra were obtained which had two distinct bands at 730 and 695 cm. It was impossible to get satisfactory agreement between the calculated and observed spectra with a band width of 10 cm.⁻¹, and reasonable agreement was not obtained until the band width used was reduced to 6 cm.⁻¹. It was found that these bands arose from diphenyl disulfide in the polymer, and they disappeared upon further purification of the polymers. Thus the agreement between the calculated and observed spectra appears to be a test of the validity of the resolutions. It might be that, with the same band width, good agreement could also be obtained if more bands were used. We have no test for the number necessary; it seemed better to keep the spectra as simple as possible.

The uniqueness of the resolution of the spectra, in the  $13-15 \mu$  region at least, is indicated by the fact that only one band was found which decreased in intensity with time of isomerization according to a first order rate law. If there is a *cis*-CH==CH band in this region this is to be expected. It was possible to find two bands, at 745 and 735 cm.⁻¹, which changed in intensity more rapidly than any of the others but neither of them followed a first order rate law. From the appearance of Figure 4 the question might arise as to whether it would be possible to find one band, similar to the 740 cm.⁻¹ band, such that the specific absorbances of the others remained constant. In the course of this work series of bands were tried, at 10 cm.⁻¹ intervals, starting at 747 cm.⁻¹ and changing the positions by 2–3 cm.⁻¹, i.e. 747, 737, 727 cm.⁻¹ etc.; 745, 735, 725 cm.⁻¹, etc.; however, such a band was not found.

The origins of the bands in the  $13-15 \mu$  region, aside from the 740 cm.⁻¹ band, cannot be definitely determined. Since it is generally acknowledged that the position of the *cis*-CH=CH band, in the long-wave region, is sensitive to the environment of this group, one possibility is¹⁴ that the other bands which are undoubtedly present, although the actual number may not be known exactly, are due to *cis*-CH=CH groups in different parts of the polymer chain. Thus, a *cis*-CH=CH group at the chain end, or second or third, etc. from the chain end, might absorb at a different frequency than a *cis*-CH=CH group in the middle of the chain. If this is the case it would be expected that the absorbances of these bands would be different in high molecular weight polymers than in low since, in the latter, there would be more chain ends.

Another possibility is that other structures or groups are present which would not be expected from the simple addition reactions of the monomer, or that the chain configuration changes, depending upon the catalyst. The possibility of other reactions occurring, especially with Ziegler-Natta catalysts, has already been mentioned.⁸ It should also be pointed out that the spectrum of a completely deuterated *cis*-1,4-polybutadiene, given by Golub and Shipman,¹⁵ is considerably different, and simpler, than that of the ordinary polybutadiene. Further evidence for extraneous structures or groups is enforced by the fact that the infrared spectra of films of high*cis*-1,4-polybutadienes, which are known by x-ray diffraction to be crystalline, have no crystallinity bands similar to those observed in spectra of *trans*-1,4 or 1,2-polybutadienes.

The resolution of the bands in the 10–11  $\mu$  region of the isomerized polybutadienes yields some interesting results. The 995 cm.⁻¹ band changed in intensity during isomerization according to a first-order rate law and thus must be connected with a vibration of the cis-CH=CH group. This then explains the changes observed in the parallel and perpendicular polarization spectra of a high-cis-1,4 polybutadiene. The constancy of the intensities of the 1005 and the 985 cm.  $^{-1}$  bands must mean that the structures giving rise to those bands remain unchanged in the polymer. This is the region in which bands that are assigned to cyclic structures appear. On this account it would be interesting to obtain the spectrum of a trans-1,4polybutadiene which was made by complete isomerization of a cis-1,4polybutadiene. It should be different from that of a trans-1,4 polymer made from the monomer directly. Unfortunately, a complete isomerization of cis-CH=CH to trans-CH=CH appears to be impossible. Perhaps it should be pointed out that the 1005, 995, and 985 cm.⁻¹ bands can not be due to side vinyl groups in these polymers. The changes in intensity of the 975 and 957 cm.⁻¹ bands also follow a first-order rate law and hence should be assigned to a vibration of cis-CH=CH. However since the intensities of these two bands decrease so rapidly with isomerization it is difficult to be sure.

Another point of interest is the intensity of the resolved 967 cm.⁻¹ band. As is shown in Figure 6, it is considerably more intense than would be deduced from the absorbance of the spectrum at 967 cm.⁻¹ and the absorbance of the dashed baseline at that frequency. This is a baseline that is often used in microstructure determinations of polybutadienes. Also, it is apparent that, if a symmetrical curve is drawn from the 995 cm.⁻¹ band, and the difference in absorbance of it at 967 cm.⁻¹ and the actual spectrum is taken as the absorption due to *trans*-CH==CH, the amount will be smaller than that of the resolved 967 cm.⁻¹ band. This procedure has also been used in microstructure determinations.

# CONCLUSIONS

In the 13–15  $\mu$  region of the spectra of *cis*-1,4-polybutadienes there is a band at 740 cm.⁻¹ which is undoubtedly due to the hydrogen out-of-plane

vibration of *cis*-CH=CH. There are other bands in this region which may also be due to a vibration of this group or to the presence of other structures in the polymer.

In the 10-11  $\mu$  region of the spectra of *cis*-1,4-polybutadienes there is at least one band at 995 cm.⁻¹ (there may be three) which is connected with a vibration of *cis*-CH=CH. There are two other bands, at 1005 and 985 cm.⁻¹, which are not due to vibrations of either *cis*-CH=CH or *trans*-CH=CH. Whether these are due to cyclic or other structures in the polymer is not known.

The trans-CH==CH band at 967 cm.⁻¹ in the spectrum of a high-cis-1,4- (95% cis-1,4) polybutadiene is considerably more intense than might be deduced from drawing baselines or from drawing a band envelope for the 995 cm.⁻¹ band.

The results given here explain, in part at least, the appearance of polarization spectra of high-cis-1,4-polybutadienes.

Many thanks are due H. C. Ransaw and G. E. Harris who recorded many of the spectra, made many of the measurements and helped with the reduction of the spectra used here. The author is indebted to K. W. Scott of the Goodyear Tire and Rubber Co. for irradiating polymer samples and is very grateful to J. J. Shipman, J. E. Field, E. F. Devlin, W. C. Sears, D. C. Smith, and R. E. Silas for their criticisms and suggestions regarding this work. The interest of F. W. Stavely and G. Alliger is greatly appreciated.

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#### Résumé

On a trouvé, par résolution analytique des spectres des *cis*-1,4-polybutadiènes isomérisés, que la bande attribuée aux vibrations d'hydrogène hors-du-plan des groupes *cis*-CH=CH apparaît à 740 cm⁻¹ et que le déplacement apparent de cette bande vers les fréquences plus basses, lorsque la teneur en *cis*-CH=CH diminue dans le polybutadiène, est provoqué par la présence d'autres bandes dans cette région. On discute des origines possibles de ces autres bandes. On a trouvé aussi qu'il y a certaines bandes dans la région de 10-11 mu du spectre du polybutadiène, qui sont probablement reliées aux vibrations des groupes *cis*-CH=CH et qu'il y en a probablement d'autres qui ne sont dues ni au *cis*-CH=CH, ni au *trans*-CH=CH ou CH₂=CH. On discute des origines possibles de ces bandes. Les bandes que l'on trouve ici expliquent dans une large mesure l'apparition de spectres de polarization des *cis*-1,4-polybutadiènes.

# Zusammenfassung

Durch analytische Auflösung des Spektrums von isomerisiertem cis-1,4-Polybutadien wird gezeigt, dass die Bande der Aus-der-Ebene-Schwingungen des Wasserstoffs von cis-CH=CH-Gruppen bei 740 cm⁻¹ auftritt und dass die Verschiebung dieser Bande mit abnehmender Menge an cis-CH=CH in einem Polybutadien zu niedrigeren Frequenzen auf das Vorhandensein anderer Banden in diesem Bereich zurückzuführen ist. Einige Möglichkeiten für den Ursprung dieser anderen Banden werden diskutiert. Weiters wird gezeigt, dass im Bereich von 10–11  $\mu$  des Polybutadienspektrums einige Banden auttreten, die wahrscheinlich mit Schwingungen der cis-CH=CH-Gruppen zusammenhängen und dass wahrscheinlich noch andere vorhanden sind, die weder auf cis-CH=CH, trans-CH=CH oder CH₂=CH zurückgefühert werden können. Einige Möglichkeiten für den Ursprung dieser Banden werden diskutiert. Die hier gefundenen Banden erklären zum Grossteil das Auftreten von Polarisationsspektren von hochgradigen cis-1,4-Polybutadienen.

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# Synthesis and Polymerization of N[2-(2-Methyl-4-oxopentyl)]-acrylamide—A New Reactive Vinyl Monomer*

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#### **Synopsis**

The synthesis and polymerization reactivity of N[2-(2-methyl-4-oxopentyl)]-acrylamide (diacetone acrylamide) is described. This reactive vinyl monomer is prepared in good yield from acetone, acrylonitrile and sulfuric acid. Diacetone acrylamide is a white crystalline solid with the water solubility characteristics of acrylamide and the organic solvent solubility of N-alkyl acrylamides. Diacetone acrylamide readily homopolymerizes and forms copolymers with a wide variety of comonomers. Reactivity ratios in the copolymerization of diacetone acrylamide with styrene and methyl methacrylate are reported and the Alfrey-Price Q and e values calculated. These results, along with data from the copolymerization of diacetone acrylamide with a group of typical vinyl monomers, are presented to indicate the high reactivity of this new monomer.

# **INTRODUCTION**

This paper describes the synthesis of a new reactive vinyl monomer—N[2-(2-methy)-4-oxopenty]) acrylamide (diacetone acrylamide). This monomer can be synthesized in good yield from readily available starting materials. Diacetone acrylamide possesses the reactivity of an activated double bond, an N-substituted amide, and a methyl ketone. This report will be limited to the synthesis of diacetone acrylamide and a preliminary investigation of its polymerization reactions.

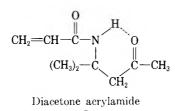
# **RESULTS AND DISCUSSION**

# **Monomer Synthesis**

Diacetone acrylamide (I) was prepared by neutralization of the reaction product of acrylonitrile, acetone, and sulfuric acid. Best yields were obtained by adding 2.4 mole of sulfuric acid to 2.4 mole of acetone and 1.0 mole of acrylonitrile.

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Decreasing the quantity of sulfuric acid or acetone gave lower yields of product. Optimum reaction temperature was 50-60°C. Temperatures above this range gave increased yields of a polymeric residue caused by sulfuric acid catalyzed condensation of the acetone. During neutralization to form diacetone acrylamide, the temperature should be held below 50°C. to avoid the possibility of basic hydrolysis of the product.

The structure assignment of diacetone acrylamide was based on nitrogen analysis and the infrared and NMR spectra. The principal characteristics of the spectra are given in Tables I and II. The NMR spectrum was obtained by use of tetramethylsilane as the internal standard and carbon tetrachloride as solvent. Further evidence for the assigned structure is the similarity of this reaction to that reported previously^{1,2} for the preparation of N-alkyl acrylamides from  $\alpha$ -olefins and acrylonitrile. In addition,

Absorption band, $\mu$	Assignment
3.05	N- H
3.4	С- Н
5.8	C=O (ketone)
6.05	C=O (amide)
6.25	C=C
6.5	N—H (amide II)
6.8,7.25	C—H
10.2, 10.8	$-CH=CH_2$

TABLE I

TABLE II Nuclear Magnetic Resonance Spectrum Characteristics of Diacetone Acrylamide

au Value	$\mathbf{Assignment}$
3.28	N—H
3.90	$C = CH_2$
4.55	>C=CH ₂ -CH=C
7.04	>CH ₂
	0
7.92	CH ₃ C—
8.60	$CH_3 \tilde{C}$ — $(CH_3)_2 C \langle$

diacetone acrylamide was also obtained when either diacetone alcohol or mesityl oxide was used to replace acetone.

# **Monomer Properties**

Diacetone acrylamide, unlike most substituted acrylamides, exhibits water solubility similar to that of acrylamide itself. Solubility in ethyl acetate, benzene, and acetone, however, is similar to that of the substituted acrylamides. These solubility data are summarized in Table III.

TADIE III

Solvent	Solubility, g./100 g. solvent at 25°C.
Water	>100
Ethanol	>100
1-Hexanol	98
Acetone	>100
Ethyl acetate	>100
Benzene	>100
Heptane	1.0
Petroleum ether	0.1

Diacetone acrylamide has good thermal stability and long shelf life. There is no evidence of polymer formation after one year storage of monomer at room temperature. The monomer will polymerize on storage above its melting point and in solution at room temperature. Diacetone acrylamide can be distilled under reduced pressure in the presence of inhibitor with no decomposition.

## **Homopolymerization**

Diacetone acrylamide was homopolymerized under a variety of conditions. Polymerization in aqueous solution using potassium persulfate initiator gave a water-insoluble powder which was only partially soluble in dimethylformamide, toluene, butanol, and acetone. The homopolymers prepared in benzene solution or in bulk were tough solids which would swell in water and dissolve in dimethylformamide, toluene, butanol, and methyl ethyl ketone. The product isolated from a benzene solution polymerization gave an intrinsic viscosity of 2.56 in dimethylformamide at  $30^{\circ}$ C. A homopolymer, which was prepared in 42% yield with the use of sodium in liquid ammonia, showed an intrinsic viscosity at  $30^{\circ}$ C. of 0.75 in dimethylformamide. Solubility of this polymer was similar to that of the homopolymers prepared in benzene solution with free radical initiation.

Differential thermal analysis of the poly(diacetone acrylamide)s showed softening at about 110°C. and decomposition at 280–290°C. These data were obtained in a nitrogen atmosphere with a heating rate of  $10^{\circ}$ C./min.

# Copolymerization

Initial copolymerization experiments indicated that diacetone acrylamide was a more reactive monomer than other N-alkyl acrylamides. Consequently, reactivity ratio determinations with styrene and methyl methacrylate were made, and the Alfrey-Price equations³ were used to calculate Q and e values. These results, given in Table IV, confirmed the increased reactivity. Composition curves from these experiments are shown in Figure 1.

	TABLE IV
	Reactivity Ratios of Diacetone
1	Acrylamide (M2) with Styrene and Methyl Methacrylate

$egin{array}{c} \mathbf{Monomer} \ \mathbf{M_1} \end{array}$	$r_1$	$r_2$	$Q_1$	$e_{t}$	$Q_2$	$e_2$
Styrene	$1.77 \pm .08$	$0.49 \pm .06$	1.00	-0.80	0.42	-0.42
Methyl methacrylate	$1.68 \pm .06$	$0.57 \pm .03$	0.74	0.40	0.41	-0.02

Copolymers of diacetone acrylamide with a group of typical vinyl monomers are summarized in Table V. The vinyl acetate and vinyl chloride copolymers contained significantly larger amounts of diacetone acrylamide than did the monomer charge. In both systems the viscosity of the copolymers increased with increasing incorporation of diacetone acrylamide. The copolymers were soluble in cyclohexanone and, with the exception of the high vinyl chloride copolymer, were also soluble in butanol and methyl ethyl ketone.

Copolymers rich in diacetone acrylamide were also formed with maleic anhydride, vinyl stearate, ethyl vinyl ether, and N-vinyl pyrrolidone.

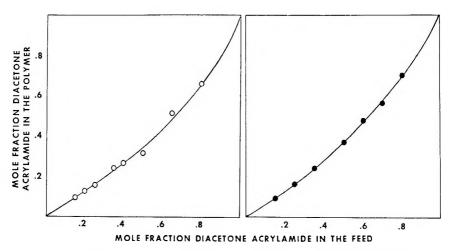


Fig. 1. Composition curves for copolymers: (O) styrene-diacetone acrylamide;  $(\bullet)$  methyl methacrylate-diacetone acrylamide.

The maleic anhydride copolymer, a fine white powder, analyzed for an equal mole ratio of monomer units.

Diacetone acrylamide formed copolymers with vinylidine chloride, acrylonitrile, methyl vinyl ketone, methacrylic and itaconic acids, and acrylamide in about the same ratio as charged. Intrinsic viscosities of the acid-containing copolymers increased in value as the copolymer concentration decreased. Nitrogen analysis of the acrylonitrile copolymers indicated that diacetone acrylamide content was richer than that in the feed.

	Time,	Temp.,	Conver- sion,	acry	cetone lamide, t%	Intrinsic viscosity in DMF
Comonomer	hr.	°C.	%	Charge	Product	at 30°C.
Vinyl acetate	4	65	82	75	89	1.35
Vinyl acetate	4	65	60	50	<b>79</b>	1.19
Vinyl acetate	4	65	35	25	65	0.99
Vinyl chloride	20	60	87	75	86	1.29
Vinyl chloride	20	60	80	50	70	1.05
Vinyl chloride	35	60	54	25	44	0.44
Maleic anhydride	16	60	73	63	68	
Vinyl stearate	20	70	70	75	87	0.67ª
Ethyl vinyl ether	20	70	83	75	90	0.82
N-Vinylpyrrolidone	20	70	91	75	83	0.57
Vinylidene chloride	18	60	70	50	55	0.37
Acrylonitrile	4	65	91	75	$\sim 75$	
Acrylonitrile	4	65	98	50	${\sim}50$	2.73
Acrylonitrile	4	65	87	25	$\sim 25$	3.06
Methyl vinyl ketone	20	70	83	75	72	0.61
Methacrylic acid	18	60	100	50	50	1.50
Methacrylic acid	3	70	99	60	60	2.9-6.0
Itaconic acid	20	70	100	75	. 75	0.68-1.34
Acrylamide	2	70	58	75	70	Insoluble
N-Vinyl carbazole	20	70	72	75	Good	0.32

 TABLE V

 Solution Copolymerizations of Diacetone Acrylamide (DA)

^a On soluble portion.

This high value may be due to difficulty in obtaining accurate nitrogen analysis on acrylonitrile-containing copolymers. Diacetone acrylamide was also copolymerized with acrylonitrile using sodium in liquid ammonia. Two fractions were obtained. One, obtained in 33% yield, was a yellow powder which was insoluble in methanol and contained about 75% acrylonitrile. The second fraction was a methanol-soluble viscous oil and contained about 75% diacetone acrylamide. The initial monomer charge contained equal parts by weight of each monomer.

*N*-Vinyl carbazole formed a copolymer with diacetone acrylamide. Infrared analysis was used to determine incorporation since both monomers have the same nitrogen content.

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Diacetone acrylamide was copolymerized with butadiene by use of a standard SB-R recipe at 50°C. for 18 hr. A white rubbery solid was isolated in 80% yield. The copolymer, which contained 10% diacetone acrylamide from a monomer charge of 25%, was only partially soluble in benzene. This soluble portion had a 0.15 intrinsic viscosity in benzene at  $30^{\circ}$ C.

# **EXPERIMENTAL**

#### Monomers

Diacetone acrylamide was prepared by adding 2.4 mole of 96% sulfuric acid to a mixture of 2.4 mole of acetone and 1.0 mole of acrylonitrile. (Acctone addition to acid-acrylonitrile is not recommended because of the violent reaction which occurs on mixing sulfuric acid and acrylonitrile.) During addition of sulfuric acid, the temperature of the mixture was allowed to rise rapidly to 50°C. and then was held at 52–60°C. with external cooling. After the addition was complete, the mixture was stirred for an additional 4 hr. at 50–60°C., then poured slowly with stirring into 480 g. of 25% sodium hydroxide solution. The temperature during neutralization was held near 20°C. by means of an ice bath. The organic layer was separated, washed with 25 ml. of 20% sodium hydroxide solution and stripped to 100°C. at 25 mm. Hg. The residue was distilled at 100–130°C. at 9 mm. Hg or 70-90°C. at 0.2 mm. Hg. The distillate was further purified for polymerization by dissolving in an equal weight of benzene and pouring into a large volume of cold petroleum ether. The solid product was filtered, washed with cold petroleum ether and air dried. Yields of 58–70% of a white crystalline solid, melting at 52–53.5°C., were obtained.

The other monomers used in this study were commercial materials and were purified before use.

#### **Reactivity Ratio Determinations**

The experimental methods were essentially those of Mayo and Lewis.⁴ Solution polymerizations in benzene were run under a nitrogen atmosphere in 4-oz. screw-cap bottles fitted with Teflon gaskets. Polymerization was initiated by azobisisobutyronitrile at 0.01 wt.-% based on monomer. Conversions were below 8.0%. The polymers were precipitated by pouring the benzene solution into naphtha or petroleum ether at room temperature. Purification was effected by repeated reprecipitations. The purified polymers were dried under vacuum to constant weight and the composition of the copolymers was determined by nitrogen analysis.

Reactivity ratios were determined from the differential form of the general copolymerization equation by using both the method of intercepts³ and the Fineman and Ross⁵ plots.

# **Polymerizations**

Copolymers of diacetone acrylamide with vinyl monomers were prepared in benzene solution under a nitrogen atmosphere. Benzoyl peroxide at 0.01-0.05 wt.-% based on monomer was used as catalyst. Polymerization time and temperature are given in Table V. Monomer concentration was in the range of 33-50 wt.-%. Copolymers were purified by reprecipitation from solution by a nonsolvent and dried under vacuum. Diacetone acrylamide incorporation was calculated from nitrogen analysis and confirmed by infrared spectra. Composition of copolymers with chlorinecontaining monomers was confirmed by chlorine analysis which agreed well with values based on nitrogen.

#### CONCLUSION

The synthesis and some properties of diacetone acrylamide have been reported. Preliminary experiments have indicated the potential of this chemical as a reactive vinyl monomer.

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#### Résumé

On décrit la synthèse et la réactivité de polymérisation du N(1,1-diméthyl-3-oxobutyl)-acrylamide (diacétone acrylamide). Ce monomère vinylique réactif est préparé avec un bon rendement à partir d'acétone, d'acrylonitrile et d'acide sulfurique. Le diacétone acrylamide est un solide cristallin blanc possédant les propriétés de solubilité dans l'eau de l'acrylamide et de solubilité dans des solvants organiques des N-acrylamides. Le diacétone acrylamide homo-polymérise facilement et forme des copolymères avec toute une série de comonomères. Les rapports de réactivité de la copolymérisation du diacétone acrylamide avec le styrène et le méthacrylate de méthyle sont donnés et les valeurs des fonctions d'Alfrey-Price Q et e sont calculées. Ces résultats, ainsi que les résultats de la copolymérisation du diacétone-acrylamide avec un groupe de monomères vinyliques typiques, sont présentés pour montrer la grande réactivité de ce nouveau monomère.

## Zusammenfassung

Die Synthese und die Polymerisationsfähigkeit von N(1,1-Dimethyl-3-oxobutyl)acrylamid(Diacetonacrylamid) werden beschrieben. Dieses reaktionsfähige Vinylmonomere wird in guter Ausbeute aus Aceton, Acrylnitril, und Schwefelsäure dargestellt. Diacetonacrylamid ist ein weisser, kristalliner Festkörper mit der für Acrylamid charakteristischen Wasserlöslichkeit und der für N-Alkylacrylamide charakteristischen Löslichkeit in organischen Lösungmitteln. Diacetonacrylamid liefert leicht Homopolymere und bildet mit einer grossen Vielfalt von Comonomeren Copolymere. Reaktivitätsverhältnisse für die Copolymerisation von Diacetonacrylamid mit Styrol und Methylmethacrylat werden mitgeteilt und die Q- und e-Werte nach Alfrey-Price berechnet.

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Diese Ergebnisse werden mit weiteren Daten für die Copolymerisation von Diacetonacrylamid mit einer Gruppe typischer Vinylmonomerer zum Beleg für die hohe Reaktivität dieses neuen Monomeren vorgelegt.

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# Polymerization of 4-Vinylcyclohexene by the Cyclic Polymerization Mechanism*

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# **Synopsis**

4-Vinylcyclohexene is an example of a 1,5-diene and is functionally capable of undergoing cyclic polymerization. Polymerization to soluble polymers was accomplished by cationic and Ziegler-type initiators. Cationic initiation resulted in 28% conversion to polymer, of which 85% was soluble, having intrinsic viscosity of 0.11 dl./g. Infrared and nuclear magnetic resonance analyses led to the conclusion that cyclization of the monomer occurred to the extent of almost 50%. Ziegler-type initiation resulted in 20% conversion to polymer of which 45% was soluble, essentially saturated, and having intrinsic viscosity of 0.04 dl./g. X-ray diffraction studies on these polymers indicated no appreciable degree of crystallinity.

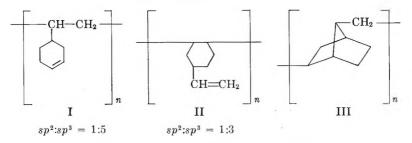
The principle of cyclopolymerization has now been well established.^{1,2} Numerous cyclic dienes have now been converted to polymers containing bicyclic units formed during the cyclopropagation step.³ It was the purpose of this work to determine whether or not 4-vinylcyclohexene, a Diels-Alder dimer of 1,3-butadiene, could be converted to a polymer containing bicyclic units, and if so, to what extent and under what conditions. 4-Vinylcyclohexene is an example of a 1,5-diene, and is functionally capable of undergoing cyclic polymerization leading to a poly(3,7-methylene[2.2.1]bicycloheptane) structure.

# **RESULTS AND DISCUSSION**

Polymerization of 4-vinylcyclohexene was accomplished by initiation with boron trifluoride, boron trifluoride-diethyl etherate, and with a Ziegler catalyst. Other initiators employed, namely, titanium tetrachloride, *n*-butyllithium, and  $\alpha,\alpha$ -azobisisobutyronitrile (AIBN), under the conditions studied were essentially ineffective in initiating polymerization of this monomer. Low-temperature (-70°C.) polymerization with boron trifluoride gas led to 28% conversion to polymer, of which 85% was soluble in chloroform and presumed to be noncrosslinked. This polymer had an intrinsic viscosity of 0.11 dl./g. Infrared and nuclear magnetic resonance analyses of the polymer led to the conclusion that some

* From the Ph.D. dissertation of Marion L. Miles, Department of Chemistry, University of Florida, April 1963.

residual unsaturation remained. After numerous purifications and lengthy Soxhlet extraction of the polymer, this unsaturation remained unchanged, leading to the conclusion that cyclization was not complete. The NMR spectrum of the polymer included a broad peak for  $sp^3$ -bonded hydrogens at a chemical shift of 8.6  $\pm$  1  $\tau$  and two peaks for  $sp^3$ -bonded hydrogens at approximately 4.5 and 5.2  $\tau$ . The  $sp^2:sp^3$  ratio of 1:12 can be interpreted in terms of structures I, II, and III



that the polymer is probably a copolymer of structural units I and III in approximately equal proportions, and that cyclization has occurred to the extent of approximately 50%. Structure II can reasonably be eliminated from consideration since internal double bonds are well known to be resistant to polymerization; however, it was not possible to distinguish between the type of residual unsaturation by either the infrared data or the NMR data. Calculations of the degree of cyclization based on the NMR results were made according to a procedure previously published.⁴

Two experiments were conducted in an attempt to increase the intrinsic viscosity of the polymer by reducing the catalyst concentration for the gaseous boron trifluoride initiation. Usually, the boron trifluoride gas was emitted over a solution of the monomer; the reaction flask was then sealed, and the mixture was left stirring for the remainder of the reaction period. In this set of experiments the gas was emitted and left over the solution for a certain period of time. It was then displaced with dry nitrogen, and the reaction was allowed to proceed for the allotted time. This procedure did not appreciably affect the viscosity, polymer melt temperature, or per cent soluble fraction, although it did decrease the yield. This type of behavior is consistent with a low degree of polymerization.

Continuous extraction of the chloroform soluble polymer with diethyl ether caused some fractionation to occur. Both the ether-soluble and insoluble fractions, however, gave NMR and infrared spectra essentially the same as those of the nonfractionated polymer.

The polymer obtained from the boron trifluoride etherate initiation was completely soluble in chloroform but gave a low value for the intrinsic viscosity (0.03 dl./g.). A high catalyst:monomer ratio was necessary for high conversion. The infrared spectrum of this polymer indicated very little unsaturation, and the NMR spectrum showed an  $sp^2:sp^5$  ratio of 1:28 (80% cyclization).

	Monomon		Column	Initiator	tor	Reaction	Reaction conditions	Polymer	mer
Polymer	Concn., mmoles	Solvent	vol. ml.	System	Concn., mmole	Temp., °C.	Time	Yield, $\%$	Soluble,
9a	14	CH2Cl2	8	$BF_3$	Gas	-70	1 hr.		
						then	u		
						Room	21 hr.	Ω.	20 ⁿ
9b	83	CH ₂ Cl ₂	10	$BF_3$	Gas	-70	68 hr.	20	62
9c	30	CH ₂ Cl ₂	12	$BF_{3}^{h}$	Gas	-70	24 hr.	6	<b>0</b> 6
6	30	CH2Cl2	12	$BF_3$	Gas	-70	24 hr.	28	85
	50	n-Heptane	5	TiCl ₄	0.85	0	72 hr.	None	
	12	n-Heptane	2.8	TiCl4	1.7	Room	16 days	Trace	
	12	n-Heptane	ભ	n-BuLi	50	Room	14 days	None	
9e	100	CH ₂ Cl ₂	ŝ	$BF_{s}(C_{s}H_{s})_{2}O$	7	0	28 days	35	100
	20	None		AIBN	(10 mg.)	70	14 days	Trace	
9f	12	n-Heptane	2.2	TiCl,	0.6	Room	14 days	20	45
				All (1-DU)3	0.0				

# 4-VINYLCYCLOHEXENE POLYMERIZATION

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	Polymer			Elementa	l analysis	
	melt tempera- ture,	Intrinsic	Cal	led.	Fo	und
Polymer	°C.	viscosity	C, %	Н, %	C, %	Н, %
9b	173	0.11	88.82	11.18	88.82	11.19
9c	168	0.07	88.82	11.18	88.69	11.22
9d	171	0.08	88.82	11.18	N.	D.ª
9e	108	0.03	88.82	11.18	84.50	10.43
9f	91	0.04	88.82	11.18	88.71	11.10

TABLE II hysical Properties of Soluble Polymers of 4-Vinylcyclohexer

" N.D. = not determined.

The Ziegler catalyst initiation yielded a polymer of which 45% was soluble in chloroform. This soluble fraction was essentially saturated and had a polymer melt temperature of 91°C. and an intrinsic viscosity of 0.04. Table I summarizes the polymerization conditions and yields for Table II summarizes the physical properties of the polythis monomer. X-ray diffraction studies on these polymers did not indicate any mers. appreciable degree of crystallinity. The pronounced tendency of this monomer to undergo cyclization during polymerization further supports an intramolecular interaction in monomers of this type as previously proposed,² since neither cationic nor Ziegler-type initiators ordinarily initiate polymerization of internal olefins. These results can be interpreted as additional evidence for the nonbonded interaction proposal² as a driving force to cyclic polymer, the nonbonded interaction providing a lower energy pathway to polymer through cyclization.

# **EXPERIMENTAL**

#### **Equipment and Data**

All temperatures herein are uncorrected and reported in degrees centigrade. Pressures are expressed in millimeters of mercury, having been determined by means of either a Zimmerli or McLeod gauge. Infrared spectra were obtained with a Perkin-Elmer Infracord double-beam infrared recording spectrophotometer or a Perkin-Elmer Model 21 doublebeam infrared recording spectrophotometer. Refractive indices were obtained with a Bausch and Lomb Abbe 34 refractometer equipped with an achromatic compensating prism.

Gas-liquid chromatographic analyses were made with a Wilkins Aerograph Model A-110-C gas chromatographic instrument with the use of helium for the eluent gas. Unless otherwise indicated, gas-liquid chromatographic analyses were made on a 5-ft. column packed with 20%Silicone GE SF-96 on firebrick, and on a 10-ft. column packed with 20%Carbowax 1000 on 42/60 firebrick.

# 4-VINYLCYCLOHEXENE POLYMERIZATION

Nuclear magnetic resonance (NMR) spectra were obtained with a Varian DP-60 nuclear magnetic resonance spectrometer at a frequency of 56.4 Mcycles with carbon tetrachloride as solvent. Melting point determinations of monomeric compounds were carried out in open capillary tubes in a Thomas-Hoover melting point apparatus. The polymer melt temperatures were determined by means of a Kofler micro hot stage. The polymer melt temperature is defined as the lowest temperature at which a wet streak is left on the hot stage upon pressing a sample of polymer with a spatula. Intrinsic viscosities were calculated from efflux times of solutions through a Cannon-Ubbelohde semimicro dilution viscometer set in a 25°C. constant temperature bath. X-ray diffraction spectra were obtained with a Norelco x-ray diffractometer Model 12045 and a proportional counter. Elemental analyses were performed by Galbraith Laboratories, Knoxville, Tennessee.

# Source and Purification of Materials

4-Vinylcyclohexene was obtained from Cities Service Research and Development Company. This material was dried for 48 hr. over anhydrous magnesium sulfate and then distilled immediately before use. It was shown to be pure by comparison of its boiling point, infrared spectrum, and refractive index data with literature values. Further criteria of purity were obtained by the fact that only one peak was obtained on the gas chromatographic columns previously referred to.

Tetrahydrofuran was obtained from Fisher Scientific Company. It was dried over sodium ribbon and then distilled. Allyl bromide and titanium tetrachloride were obtained from Peninsular ChemResearch, Inc. The allyl bromide was distilled before use, and the titanium tetrachloride was used as received. *n*-Butyllithium was obtained from Foote Mineral Company and used as received. Boron trifluoride (gas) was obtained from The Matheson Company and used as received. Triisobutylaluminum and triethylaluminum were obtained from Ethyl Corporation and used as received. Nitrogen used as a sweep gas in the polymerization experiments was Airco prepurified grade containing less than 20 ppm of oxygen.

#### **Polymerization of 4-Vinylcyclohexene**

# Cationic Initiation

**Boron Trifluoride-Diethyl Etherate Initiation.** Into a 50-ml. sample bottle was placed 10.8 g. (0.1 mole) of 4-vinylcyclohexene and 3 ml. of  $CH_2Cl_2$ . The bottle was immersed in a Dry Ice-acetone bath and dry nitrogen gas emitted over the solution. After 30 min. at this temperature the vessel was sealed with a serum cap and 1 g. (7 mmole) of boron trifluoride etherate was injected into the solution by means of a hypodermic syringe. The bottle was then removed from the bath and placed in a refrigerator (0°C.) for 28 days. The contents of the vessel was removed into 200 ml. of methanol, and the polymer which precipitated was removed

by filtration and dried in a vacuum oven. This material was taken up in 15 ml. of cold dichloromethane and then precipitated by pouring this solution into 200 ml. of acetone. The polymer was collected and vacuumdried at 60°C.; yield, 3.8 g. (35%); polymer melt temperature, 108°C.; intrinsic viscosity, 0.03 dl./g. (in chloroform). The infrared spectrum of this polymer revealed absorption bands as follows: 2930 cm.⁻¹(C—H), 1630 cm.⁻¹(C=C), 990 cm.⁻¹(CH=CH₂), 910 cm.⁻¹(CH=CH₂).⁵ The NMR spectrum shows an  $sp^2:sp^3$  hydrogen ratio of 1:28 (80% cyclization).

ANAL. Caled. for C₈H₁₂: C, 88.82%; H, 11.38%. Found: C, 84.50%; H, 10.43.

Boron Trifluoride Initiation. Into a three-necked 100-ml. flask equipped with a stirrer, reflux condenser connected to a mercury bubbler, and nitrogen inlet, was placed 9.0 g. (83 mmole) of 4-vinylcyclohexene and 10 ml. of dry spectrograde dichloromethane. The reaction vessel was immersed in a Dry Ice-acetone bath, and dry nitrogen was emitted over the solution. The solution was stirred for 30 min. at  $-70^{\circ}$ C., and then the nitrogen flow was stopped, and gaseous boron trifluoride was emitted over the solution. The reaction flask was sealed off. After a reaction time of 68 hr., the flask was opened, and its contents poured into 200 ml. of methanol. The polymer which precipitated was removed by filtration and then dried for 16 hr. at room temperature/3 mm. Hg; yield, 1.8 g. (20%). This polymer was taken up in 20 ml. of chloroform, filtered, and precipitated by pouring the solution into 200 ml. of methanol; yield, 1.4 g. (79%); polymer melt temperature; 173°C.; intrinsic viscosity, 0.11 dl./g. (in chloroform). The infrared spectrum of the soluble polymer (run in chloroform solution) revealed very little unsaturation. The NMR analysis gave an integrated peak area ratio for  $sp^2$ :  $sp^3$  hydrogen of 1:12 (50% cyclization).

ANAL. Calcd. for C₈H₁₂: C, 88.82%; H, 11.18%. Found: C, 88.82%; H, 11.19%.

#### Triisobutylaluminum-Titanium Tetrachloride Initiation

In a screw-cap vial which contained 2.2 ml. of high purity *n*-hexane was placed, by means of a micro hypodermic syringe, 0.12 g. (0.6 mmole) of triisobutylaluminum and 0.12 g. (0.6 mmole) of TiCl₄. After the catalyst had aged for 20 min. at room temperature 1.3 g. (12.0 mmole) of 4-vinyl-cyclohexene was added. All of the operations were, of course, carried out under a dry nitrogen atmosphere. The mixture was shaken well and allowed to stand at room temperature for 14 days after which it was decomposed by pouring into 200 ml. of methanol. The polymer which precipitated was removed by filtration and dried for 16 hr. at 50°C./1 mm.; yield, 0.26 g. (20%). This material was placed in a Soxhlet extractor and continuously extracted with benzene for 40 hr. The extract was poured into 200 ml. of methanol, and the polymer immediately precipitated. This soluble portion was dried for 16 hr. at room temperature/1 mm.; yield, 0.12 g. (45%); polymer melt temperature, 91°C.; intrinsic vis-

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cosity, 0.04 dl./g. (in benzene). The infrared and NMR spectra of the soluble polymer showed it to be essentially saturated.

ANAL. Caled. for C₈H₁₂: C, 88.82%; H, 11.38%. Found: C, 88.71%; H, 11.10%.

The authors are indebted to Dr. Wallace S. Brey, Jr. and his associates of this department for the NMR spectra and interpretations reported in this study.

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# Résumé

Le 4-vinylcyclohexène est un exemple de diène-1,5 et est capable de subir une polymérisation cyclique. La polymérisation, donnant des polymères solubles, a été initiée par des initiateurs du type cationique et du type Ziegler. L'initiation cationique fournit 28% de conversion en polymère dont 85% était soluble, et possédait une viscosité intrinsèque de 0.11. Des analyses infra-rouges et de résonance magnétique nucléaire démontrent que la cyclisation du monomère se produit à environ 50%. L'initiation du type Ziegler donnait une conversion en polymère de 25% dont 45% était soluble, essentiellement saturé, et ayant une viscosité intrinsèque de 0.04. Les études de diffraction des rayons-X sur ces polymères n'indiquent pas un degré de cristallinité appréciable.

#### Zusammenfassung

4-Vinylzyklohexen ist ein Beispiel für ein 1,5-Dien und ist funktionell zur zyklisierenden Polymerisation geeignet. Polymerisation zu löslichen Polymeren wurde durch kationische Starter und solche vom Ziegler-Typ erreicht. Kationische Anregung führte zu einem 28% igen Umsatz zueinem zu 85% löslichen Polymeren mit einer Viskositätszahl von 0,11. Infrarot- und kernmagnetische Resonanzanalyse führte zu dem Schluss, dass zu einem Ausmass von mindestens 50% Zyklisierung des Monomeren eintrat. Ziegler-Katalyse führte bei 20% igem Umsatz zu einem zu 45% löslichen, im wesentlichen gesättigten Polymeren mit einer Viskositätszahl von 0,04. Röntgenbeugungsuntersuchungen an diesen Polymeren zeigte keinen merklichen Kristallinitätsgrad.

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# Mechanism of the Anionic Polymerization of Methyl Methacrylate. IV. Calculated Molecular Weight Distributions Resulting from a Reversible Termination by a Bimolecular Exchange Reaction

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# Synopsis

The previous papers in this series contain the experimental results which demonstrated the complexity of the homogeneous, nonterminated, anionic polymerization of methyl methacrylate. In order to explain the observed broad molecular weight distributions, it was necessary to postulate reversible "pseudo-termination" reactions, by which a large fraction of the total anions present in the system became inactive toward further polymerization, yet had a finite probability of recovery of polymerization activity by some process, such as ligand exchange, ring opening of a cyclic complex, etc. In this paper, we have examined the quantitative consequences of a mechanism in which this pseudotermination reaction occurs by a bimolecular exchange of activity between one active and one inactive chain. It has been possible to calculate  $M_w/M_n$ , the ratio of weightaverage to number-average molecular weights, as a function of the fractional conversion  $\alpha$ , the initial monomer to initiator ratio,  $M_0/I_0$ , the fraction of total initiator as active chains,  $C_1/I_0$ , and the ratio of ra⁺e of exchange of activity to rate of propagation,  $k_L/k_p$ . The major results of these calculations are: (1) any value of  $M_w/M_n$  between 1 and infinity is possible at  $\alpha = 1$ ; (2)  $\overline{M}_w/\overline{M}_n$  at  $\alpha = 1$  decreases as  $k_l/k_p$  increases; (3)  $\overline{M}_w/\overline{M}_n$  at  $\alpha = 1$  increases as  $M_0/I_0$  increases when  $k_t/k_p$  and  $C_1/I_0$  are small-under some conditions  $\overline{M}_w/\overline{M}_n$  at  $\alpha = 1$  increases and then decreases slightly as  $M_0/I_0$  increases; (4)  $\overline{M}_w/\overline{M}_n$  goes through a maximum during polymerization if  $k_t \neq 0$ ; (5)  $\overline{M}_w/\overline{M}_n$  at any  $\alpha$  decreases as  $C_1/I_0$  increases, for constant  $M_0/I_0$  and  $k_l/k_p$ . Concentrations of individual chains of any given length as a function of time may be readily calculated for the two special cases  $k_t/k_p \rightarrow 0$  or  $\infty$ .

# Introduction

The great importance of association, dissociation, and exchange equilibria of the organometallic species which are responsible for both initiation and propagation in homogeneous anionic polymerization is universally recognized. In paper I of this series,¹ data were presented which demonstrated that in the homogeneous anionic polymerization of methyl methacrylate initiated by 9-fluorenyllithium, the fluorenyl group of the initiator becomes chemically attached to the polymer chain in an irreversible initiation step and that no irreversible termination processes occurred. The molecular weight distributions to be expected from a polymerization involving only initiation and propagation reactions have been extensively considered.²⁻⁴ For such a mechanism,  $\overline{M}_w/\overline{M}_n$  at 100% conversion equals 1.0 when initiation is rapid with respect to propagation and tends to 1.33 when initiation is very slow with respect to propagation. The polymers isolated from the fluorenyllithium-initiated polymerization, however, had  $\overline{M}_w/\overline{M}_n$  values which were frequently greater than 10. Furthermore, although none of the chains were irreversibly terminated, a large proportion had very low molecular weights, leading to a molecular weight distribution having two peaks. Kinetic studies^{2,5} showed that a strictly constant first-order rate of disappearance of monomer with time persisted to very high conversion after an initial almost instantaneous conversion of three monomer units per initiator molecule. Evidence was presented in the earlier papers to show that the tacticity of polymer chains produced in these polymerizations was determined by equilibria between electron-donating species and the lithium counterion and was independent of the kinetically important processes. It is therefore meaningful to consider the kinetics of polymerization separately from the mechanism which controls tacticity in this particular case.

The extreme deviation of the  $\overline{M}_w/\overline{M}_n$  ratio for methyl methacrylate polymerization from the expected behavior of an anionic polymerization consisting of a single initiation and propagation reaction prompted us⁵ to propose a mechanism which included the following assumptions: (1) initiation and the addition of the first three monomer units to each initiator molecule are extremely rapid; (2) as soon as three monomer units have been added, only a certain fraction of the anions remains active and continues to add monomer; (3) the total number of active anions in the solution never changes, and the rate of polymerization is the same whether the addition is isotactic or syndiotactic. This assumption leads to a rate of polymerization which is first order in monomer.

To these assumptions we have added, for the purpose of the present calculations, an additional postulate: (4) any active chain can interact at any time with any inactive chain by a bimolecular mechanism in such a way that the active chain becomes inactive and vice versa.

Coleman and Fox⁶ have independently proposed a multistate mechanism for homogeneous ionic polymerization. One major difference between their proposal and ours lies in the specific mode of transfer of a given chain from an active to an inactive state. Coleman and Fox have used independent probabilities for the change, while in our hypothesis the bimolecular exchange of activity leads to a strictly constant total concentration of chains of each type. The considerable mathematical simplification introduced by this constancy leads to another major difference between the two proposals. We have been able to avoid restricting our calculations to low conversion situations, i.e., assuming constant monomer concentration, which Coleman and Fox have done.

# **Derivation of Equations**

The present mechanism postulates two types of polymer chains, J and K. J chains grow by adding monomer; K chains do not grow, but have the ability to switch activity with a J chain.

$$\mathbf{J}_n + \mathbf{M} \xrightarrow{\kappa_p} \mathbf{J}_{(n+1)} \qquad \qquad n \ge 3 \qquad (1)$$

$$\mathbf{J}_n + \mathbf{K}_m \xrightarrow{k_t} \mathbf{J}_m + \mathbf{K}_n \tag{2}$$

where  $J_n$  is a J chain of *n* monomer units,  $K_m$  is a K chain of *m* monomer units, M is one monomer unit, and *n*,*m* are any integers  $\geq 3$ . Reactions of type (1) and (2) are preceded by an initial step, the instantaneous formation of chains having three monomer units. Thus, at t = 0, the following initial conditions exist:

$$J_3 = C_1$$
$$K_3 = C_2$$

where

$$C_1 + C_2 = I_0$$

and  $I_0$  = initial concentration of initiator and  $M = M_0$  = initial concentration of monomer.*

$$\sum_{n=3}^{\infty} nJ_n = 3C_1$$
$$\sum_{m=3}^{\infty} mK_m = 3C_2$$
$$\sum_{n=3}^{\infty} n^2 J_n = 9C_1$$
$$\sum_{m=3}^{\infty} m^2 K_m = 9C_2$$

Since the total number of J chains and of K chains is constant, at any time t

$$\sum_{n=3}^{\infty} J_n = C_1$$

and

$$\sum_{m=3}^{\infty} K_m = C_2$$

* For simplicity, we have eliminated the use of concentration brackets around the symbols  $I_0$ , M,  $M_0$ ,  $C_1$ , and  $C_2$  in this derivation. It should be understood that these quantities are in standard concentration units.

	a propriet para	rameters		Calculat	Calculated values for $(M_w/M_n)_{max}$	$(w/M_n)_{max}$		
$M_0/I_0$	$C_{1}/I_{0}$	$k_t/k_p$	Ômax	œmax	$(\bar{X}_n)_{\max}$	$(ar{X}_w)_{\max}$	$(\overline{M}_w/\overline{M}_n)_{\max}$	$(\bar{M}_w/\bar{M}_n)_{\alpha \rightarrow 1}$
20.0	0.01	0.001	3.041	0.952	22.80	1602.01	70.25	60.09
20.0	0.05	0.001	8.679	0.999	23.79	363.23	15.26	15.12
20.0	0.10	0.001	15.243	0.999	28.79	186.65	7.84	77.7
20.0	0.01	0.010	0.910	0.597	15.42	770.10	49.92	38.46
20.0	0.05	0.010	2.072	0.874	21.18	285.86	13.50	13.01
20.0	0.10	0.010	3.012	0.950	22.77	166.94	7.32	7.22
20.0	0.01	0.100	0.304	0.262	8.45	166.83	19.74	7.84
20.0	0.05	0.100	0.643	0.474	12.86	111.91	8.69	5.82
20.0	0.10	0.100	0.905	0.595	15.38	84.53	5.49	4.44
20.0	0.01	1.000	0.155	0.143	5.98	24.31	4.06	1.77
20.0	0.05	1.000	0.228	0.203	7.24	24.06	3.32	1.72
20.0	0.10	1.000	0.300	0.259	8.39	23.26	2.77	1 65
20.0	0.01	10.000	0.140	0.130	5.71	8.00	1.40	1111
20.0	0.05	10.000	0.147	0.136	5.84	8.06	1.37	1.10
20.0	0.10	10.000	0.155	0.143	5.98	8.10	1.35	1.10
20.0	0.01	100.000	0.149	0.138	5.87	6.55	1.11	1.04
20.0	0.05	100.000	0.149	0.138	5.87	6.54	1.11	1.04
20.0	0.10	100.000	0.150	0.139	5.89	6.55	1.11	1.04
60.5	0.01	0.001	1.745	0.825	52.93	4480.63	84.65	82.71
60.5	0.05	0.001	4.279	0.986	62.66	1123.66	17.98	17.92
60.5	0.10	0.001	6.736	0.998	63.42	577.44	9.10	01.6
60.5	0.01	0.010	0.541	0.417	28.27	1915.19	67.72	45.94
60.5	0.05	0.010	1.214	0.702	45.53	746.35	16.39	15.38
60.5	0.10	0.010	1.729	0.822	52.76	454.83	8.62	8.44
60.5	0.01	0.100	0.174	0.159	12.66	455.09	35.94	9.18
60 5	0.05	0.100	0.901	0 916	31 00	111	10.01	

TABLE I

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# S. KRAUSE, L. DEFONSO, D. L. GLUSKER

5.09 1.90	1.83	1.75	1.10	1.10	60.1	1.02	1.02	1.02	87.51	8.91	9.57	8.58	3.22	8.87	).65	2 .09	5.33	1.94	1.87	1.79	1.10	1.09	1.09	1.01	1.01	1.01	(continued)
	•	~				~		•																			
7.09	5.82	4.23	2.03	1.93	1.81	1.18	1.17	1.70	91.13	18.96	9.57	78.55	17.82	9.20	50.90	14.65	8.07	17 47	8.55	5.58	3.42	2.96	2.57	1.35	1.31	1.30	
$\begin{array}{c} 200.62\\ 63.87 \end{array}$	59.22	53.14	12.12	12.37	12.56	7.02	6.99	7.03	9392.45	2678.08	1431.68	3675.54	1489.67	943.82	948.08	518.01	381.75	150.14	121.92	103.14	21.40	21.56	21.68	7.92	8.03	7.92	
$\frac{28.27}{6.97}$	10.16	12.56	5.95	6.40	6.92	5.95	5.95	6.00	103.07	141.28	149.52	46.77	83.62	102.57	18.62	35.36	47.30	8.59	14.26	18.49	6.26	7.29	8.45	5.97	6.12	6.12	
$\begin{array}{c} 0.417\\ 0.065\end{array}$	0.118	0.158	0.048	· 0.056	0.064	0.048	0.048	0.049	0.667	0.921	0.976	0.291	0.537	0.663	0.104	0.215	0.295	0.037	0.075	0.103	0.021	0.028	0.036	0.019	0.020	0.020	
$\begin{array}{c} 0.541 \\ 0.068 \end{array}$	0.126	0.172	0.050	0.058	0.067	0.050	0.050	0.051	1.100	2.549	3.765	0.345	0.771	1.090	0.110	0.243	0.350	0.038	0.078	0.109	0.022	0.029	0.037	0.020	0.021	0.021	
0.100	1.000	1.000	10.000	10.000	10.000	100.000	100.000	100.000	0.001	0.001	0.001	0.010	0.010	0.010	0.100	0.100	0.100	1.000	1.000	1.000	10.000	10.000	10.000	100.000	100,000	100.000	
0.10 0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	
60.5 60.5	60.5	60.5	60.5	60.5	60.5	60.5	60.5	60.5	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	150.0	

P V 13	"A dinetable" noremeters	matane		Caluator	Colonlated values for / M / M	11/11/		
nv	ustante para	SIMAIII		Calculat	ed values for (1	W w/ MI n/max		
$M_0/I_0$	$C_{1}/I_{0}$	$k_t/k_p$	$\theta_{\max}$	αmax	$(\bar{X}_n)_{\max}$	$(ar{X}_w)_{ m max}$	$(\overline{M}_w/\overline{M}_n)_{\max}$	$(\bar{M}_w/\bar{M}_n)\alpha = 1$
200.0	0.01	0.001	0.951	0.613	125.73	11630.37	92.50	88.36
200.0	0.05	0.001	2.184	0.887	180.48	3456.25	19.50	19.08
200.0	0.10	0.001	3.187	0.958	194.74	1881.31	9.66	9.65
200.0	0.01	0.010	0.299	0.258	54.69	4445.24	81.28	49.05
200.0	0.05	0.010	0.668	0.487	100.45	1821.45	18.13	16.37
200.0	0.10	0.010	0.943	0.610	125 11	1166.70	9.32	8.94
200.0	0.01	0.100	0.095	0.090	21 12	1170.99	55.43	9.74
200.0	0.05	0.100	0.211	0.190	41.04	627.02	15.28	7.15
200.0	0.10	0.100	0.306	0.263	55.72	463.23	8.31	5.37
200.0	0.01	1.000	0.032	0.031	9.29	194.83	20.95	1.95
200.0	0.05	1.000	0.067	0.064	15 96	150.83	9.45	1.88
200.0	0.10	1.000	0.094	0.089	20 94	125.35	5.9×	1.79
200.0	0.01	10.000	0.017	0.016	6.37	26.45	4.15	1.10
200.0	0.05	10.000	0.024	0.023	7.74	26.60	3.43	1.09
200.0	0.10	10.000	0.032	0.031	9.20	26.78	2.8%	1.09
200.0	0.01	100.000	0.015	0.014	5.97	8.42	1.40	1.01
200.0	0.05	100.000	0.016	0.015	6.17	8.56	1.38	1.01
200.0	0.10	100.000	0.017	0.016	6.37	8.67	1.36	1 01

TABLE I (continued)

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89.93	19.40	9.80	49.91	16.64	9.08	9.89	7.25	5.44	1.97	1.89	1.81	1.09	1.09	1.09	1.01	1.01	1.01
95.55	91.54	9.82	87.90	18.86	9.59	68.30	16.87	8.90	34.16	12.18	7.14	8.12	5.47	4.07	1.89	1.81	1.72
21841.13	7306.30	4231.79	7869.19	3302.57	2181.06	2193.65	1101.21	841.29	423.94	287.06	226.08	56.78	54.44	50.51	11.34	11.75	12.03
228.59	373.90	430.64	89.52	175.13	227.22	32.12	65.27	94.45	12.41	23.56	31.65	6.98	9.95	12.41	5.99	6.49	6.98
0.451	0.741	0.855	0.173	0.344	0.448	0.058	0.124	0.182	0.018	0.041	0.057	0.007	0.013	0.018	0.005	0.006	0.007
0.600	1.354	1.933	0.190	0.422	0.595	0.060	0.133	0.202	0.019	0.042	0.059	0.008	0.014	0.019	0.006	0.007	0.008
0.001	0.001	0.001	0.010	0.010	0.010	0.100	0.100	0.100	1.000	1.000	1.000	10,000	10.000	10.000	100.000	100.000	100.000
0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10	0.01	0.05	0.10
500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0	500.0

The number-average degree of polymerization is given by

$$\bar{X}_{n} = \left(\sum_{n=3}^{\infty} nJ_{n} + \sum_{m=3}^{\infty} mK_{m}\right) / \left(\sum_{n=3}^{\infty} J_{n} + \sum_{m=3}^{\infty} K_{m}\right) = \left(\sum_{m=3}^{\infty} nJ_{n} + \sum_{n=3}^{\infty} mK_{m}\right) / (I_{0}) \quad (3)$$

and the weight-average degree of polymerization by

$$\overline{X}_{w} = \left(\sum_{n=3}^{\infty} n^{2} J_{n} + \sum_{m=3}^{\infty} m^{2} K_{m}\right) / \left(\sum_{n=3}^{\infty} n J_{n} + \sum_{m=3}^{\infty} m K_{m}\right)$$
(4)

The corresponding molecular weight averages are found by multiplying the degree of polymerization by the molecular weight of the monomer. In order to calculate  $\bar{X}_n$  and  $\bar{X}_w$  as a function of time, t, we must solve the following differential equations:

$$d\sum nJ_n/dt = -k_p M\sum nJ_n + k_p M\sum (n+1)J_n - k_t (\sum nJ_n) (\sum K_m) + k_t (\sum mK_m) (\sum J_n)$$
$$= k_p MC_1 - k_t C_2 \sum nJ_n + k_t C_1 \sum mK_m$$
(5)

$$d\sum mK_m/dt = k_t C_2 \sum nJ_n - k_t C_1 \sum mK_m$$
(6)

$$d\sum n^{2}J_{n}/dt = 2k_{p}M\sum nJ_{n} + k_{p}M\sum J_{n} - C_{2}k_{t}\sum n^{2}J_{n} + C_{1}k_{t}\sum m^{2}K_{m}$$
(7)

$$d\sum m^2 K_m/dt = C_2 k_t \sum n^2 J_n - C_1 k_t \sum m^2 K_m$$
(8)

$$-dM/dt = k_p M \sum J_n = k_p M C_1 \tag{9}$$

Equation (9) may be integrated directly to give

$$M = M_0 e^{-k_p C_1 t} (10)$$

Summing eqs. (5) and (6), substituting eq. (10) for M, and integrating between limits t = 0 and t, we obtain

$$\sum n J_n + \sum m K_m = 3 I_0 + M_0 (1 - e^{-\theta})$$
(11)

where  $\theta = k_p C_1 t$ . Substituting eq. (11) into eq. (5) and collecting terms, we obtain a standard first-order linear differential equation whose solution is

$$\sum nJ_{n} = 3I_{0} + M_{0}(1 - e^{-\theta}) - 3C_{2}e^{-hI_{0}\theta/C_{1}} + C_{2}(3 + M_{0}/I_{0}) (e^{-hI_{0}\theta/C_{1}} - 1) - [M_{0}hC_{2}/(hI_{0} - C_{1})] (e^{-hI_{0}\theta/C_{1}} - e^{-\theta})$$
(12)

where

$$h = k_t / k_p$$
$$h I_0 \theta / C_1 = k_t I_0 t$$

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Adding eqs. (7) and (8) and combining with eqs. (10) and (12) and integrating gives

$$\sum n^{2} J_{n} + \sum m^{2} K_{m} = 9 I_{0} + M_{0} [2(3 + M_{0}/I_{0}) + 1] \times (1 - e^{-\theta}) + M_{0}^{2} (1 - h)(1 - e^{-2\theta})/(hI_{0} - C_{1}) + 2M_{0}^{2} C_{1} C_{2} [e^{-[(hI_{0}\theta/C_{1})/(C_{1}) - \theta]} - 1]/I_{0} [(hI_{0})^{2} - C_{1}^{2}]$$
(13)

then

$$\bar{X}_n = \text{eq. (11)}/I_0 = 3 + (M_0/I_0) (1 - e^{-\theta})$$
 (14)

$$\bar{X}_w =$$
eq. (13)/eq. (11) (15)

and

$$\bar{X}_w/\bar{X}_n = \text{ eq. } (13)/I_0$$
 (16)

In order to evaluate the concentrations of individual chains at any time *t*, one must solve each of the differential equations of the form

$$dJ_{3}/dt = -k_{p}J_{3}M - k_{t}J_{3}C_{2} + k_{t}K_{3}C_{1}$$
(17)

$$dJ_n/dt = k_p J_{n-1} M - k_p J_n M - k_t J_n C_2 + k_t K_n C_1 \quad n \ge 4$$
(18)

$$dK_m/dt = k_t J_m C_2 - k_t K_m C_1 \qquad m \ge 4 \qquad (19)$$

This process is laborious in the extreme; however, for two limiting cases simple closed form solutions are possible:

For 
$$h = K_t/K_p \rightarrow 0$$

$$K_{3} = C_{2}$$

$$K_{m} = 0$$

$$J_{n} = C_{1}(M_{0}/C_{1})^{n-3} (1 - e^{-\theta})^{n-3} \times e^{-[M_{0}(1 - e^{-\theta})/C_{1}]}/(n-3)! \text{ for } m \ge 4 \quad (20)$$

For  $h \rightarrow \infty$ 

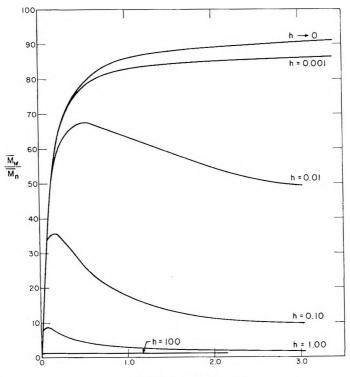
$$J_n = C_1 (M_0)^{n-3} (1 - e^{-\theta})^{n-3} e^{-[M(1 - e^{-\theta})]} / (n - 3)! \quad n \ge 3$$
(21)

$$K_m = C_2(M_0)^{m-3} (1 - e^{-\theta})^{m-3} e^{-[M(1 - e^{-\theta})]} / (m - 3)! m \ge 3 \quad (22)$$

Calculations of  $\overline{X}_w/\overline{X}_n$  were made for a large number of cases. These were programmed for a Bendix G15D computer. Calculation of the individual chain concentrations at any time is much more laborious and we include no cases here.

## **Results and Discussion**

The equations for the molecular weight averages and the ratio  $\overline{M}_{w}/\overline{M}_{n}$  include three adjustable parameters,  $M_{0}/I_{0}$ , which is actually an experimentally established quantity;  $C_{1}/I_{0}$  which can vary only between 0 and 1;



REDUCED TIME  $\theta = C_1 k_p t$ 

Fig. 1.  $\overline{M}_w/\overline{M}_n$  vs. reduced time,  $\theta = C_1k_pt$  as a function of  $h = k_t/k_p$ .  $M_0/I_0 = 60.5$ ;  $C_1/I_0 = 0.01$ .

and h, the ratio of  $k_t/k_p$ , the only parameter which can vary between wide limits. The Figures 1-3 and Table I show how  $\overline{M}_w/\overline{M}_n$  varies with each of these parameters singly and in combination. We have eliminated the time variable entirely by plotting  $\overline{M}_w/\overline{M}_n$  as a function of fractional conversion of monomer to polymer. Since  $M/M_0 = e^{-\theta} =$  $1 - \alpha$ , where  $\alpha$  is fractional conversion, the relationship between  $\theta$ , the reduced time variable, and  $\alpha$  is constant, regardless of variation in the adjustable parameters. Furthermore, expressing results in terms of  $\alpha$ establishes a natural limit to the calculations beyond which it is unnecessary to proceed, since  $\alpha$  tends to 1 long before  $\theta$  tends to infinity. At  $\theta = 5.00$ ,  $\alpha = 0.993$ ; at  $\theta = 10$ ,  $\alpha = 0.99995$ .

Equation (14) shows that  $\overline{M}_n$  depends only upon  $M_0/I_0$  and conversion and is independent of the values of h and  $C_1/I_0$ .

Figures 1 and 2 are plots of  $\overline{M}_w/\overline{M}_n$  versus  $\alpha$  for various values of the adjustable parameters. Figure 3 shows  $\overline{M}_w/\overline{M}_n$  at  $\alpha = 1$  versus  $C_1/I_0$  for various values of  $k_t/k_p$ . It is apparent that for certain values of  $k_t/k_p$ ,  $\overline{M}_w/\overline{M}_n$  goes through a pronounced maximum during the course of the polymerization. Indeed we find that for any finite value of  $k_t/k_p$  a maximum in  $\overline{M}_w/\overline{M}_n$  exists. If  $k_t/k_p$  is very small, 0.001 in our

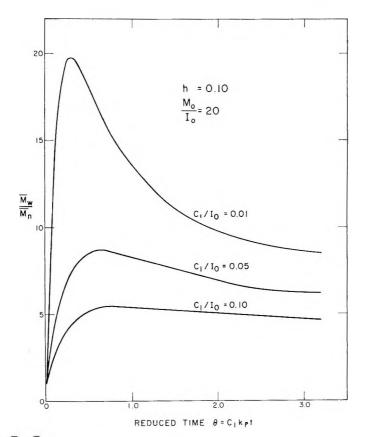


Fig. 2.  $\overline{M}_w/\overline{M}_u$  vs. reduced time,  $\theta = C_1 k_p t$  as a function of  $C_1/I_0$ .  $M_0/I_0 = 20.0$ ;  $h = k_l/k_p = 0.10$ .

calculations, then the maximum comes at very high conversions and is not very pronounced. At intermediate values of  $k_t/k_p$  the maximum may be more than double the final value of  $\overline{M}_w/\overline{M}_n$ . At any given  $M_0/I_0$ and  $C_1/I_0$  the conversion at the maximum  $\overline{M}_w/\overline{M}_n$  decreases as  $k_t/k_p$  increases. At any given  $k_t/k_p$  and  $M_0/I_0$  the conversion at the maximum  $\overline{M}_w/\overline{M}_n$  increases as  $C_1/I_0$  increases. In Table I we have compiled the values of conversion at which the given maximum  $\overline{M}_w/\overline{M}_n$  occurs, the value of this maximum, and that of  $\overline{M}_w/\overline{M}_n$  when  $\alpha$  approaches 1. If  $k_t/k_p = 0$ , no maximum occurs, and  $\overline{M}_w/\overline{M}_n$  increases continuously with conversion.

It may be noted from Table I that  $\overline{M}_w/\overline{M}_n$  at  $\alpha \sim 1$  increases as  $M_0/I_0$  increases in most cases, decreases as  $k_t/k_p$  increases, but does not necessarily tend to 1.0 as  $[M] \rightarrow 0$ . At first glance, this conclusion differs from that of Fox and Coleman⁶; however, it should be remembered that their stated conclusion that  $\overline{M}_w/\overline{M}_n \rightarrow 1.0$  as  $M \rightarrow 0$  was for constant monomer concentration, and in that sense is in agreement with our conclusion that the  $\overline{M}_w/\overline{M}_n$  generally increases as  $M_0/I_0$  increases. Actually,  $\overline{M}_w/$ 

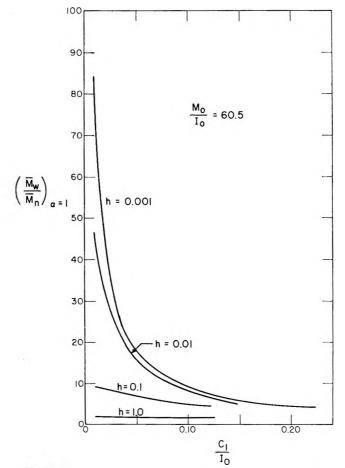


Fig. 3.  $\bar{M}_w/\bar{M}_n$  at  $\alpha = 1$  vs.  $C_1/I_0$  as a function of  $h = k_t/k_p$ .  $M_0/I_0 = 60.5$ .

 $\overline{M}_n$  at  $\alpha = 1$  may reach a maximum at some value of  $(M_0/I_0)$ . This value of  $M_0/I_0$  can be expressed as a function of  $C_1/I_0$  and h.

$$(M_0/I_0)_{\max} = 3/(7 - 6a) \tag{23}$$

where

$$a = 2 + I_0(1 - h)/C_1[(hI_0/C_1) - 1] - 2C_2/C_1[(hI_0/C_1)^2 - 1]$$
(24)

 $(M_0/I_0)_{\text{max}}$  does not exist for all values of h and  $C_1/I_0$ . When h = 100 and  $C_1/I_0 = 0.01$  for example,  $(M_0/I_0)_{\text{max}} = 3.189$ , but when h = 0.001 and  $C_1/I_0 = 0.01$ ,  $(M_0/I_0)_{\text{max}}$  calculated from eq. (24) is negative and, therefore, does not exist. Another conclusion of Fox and Coleman which apparently differs from our own, that  $\overline{M}_w/\overline{M}_n$  tends to 1.0 as t tends to infinity, was actually circumscribed by their assumption of fixed M, whereas we have allowed M to disappear by polymerization.

The assumptions in our present treatment of the fluorenyllithiuminitiated polymerization of methyl methacrylate might be considered a special case of the Coleman and Fox theory: that special case in which the independent probabilities for transfer from one state to another were equal, and in which the rate of polymerization in one of the states was 0. However, Coleman and Fox did not carry through the calculations in which M is allowed to decrease with time through the polymerization reaction, and were therefore not able to obtain all the conclusions shown in the present paper.

It should be reemphasized that our suggestion for a bimolecular exchange reaction was made on mathematical grounds as a simple way to obtain the exactly constant fraction of active chains demanded by the kinetics of the polymerization. If the difference in activity of the two states postulated here is considered to be the result of differing distributions of ligand about the counterions, it is apparent that, in reality, a number of states of differing activity may exist.

A specific example in which at least three states of differing activity have been demonstrated is that of the polymerization of styrene by butyllithium in the presence of tetrahydrofuran (THF).⁷ The species containing no THF or two THF's per lithium are very inactive relative to that containing a 1:1 complex at the chain end.

Although we have no direct evidence that only two states exist and that bimolecular exchange actually takes place, this simple hypothesis has proved to be capable of many predictions which are consistent with available experimental data, and several which are susceptible to direct experimental test. The most straightforward experiment to check the predictions presented in this paper will be a search for a pronounced maximum in  $\overline{M}_w/\overline{M}_n$  as a function of conversion under certain experimental conditions.

We have also carried through the calculations for a more complicated mechanism based on the experimental observation that the probability that an active chain becomes inactive apparently drops when the chain reaches a length of 8–10 units. This mechanism involved four states of differing activity with independent probabilities for transfer from one state to another. The maximum  $\overline{M}_w/\overline{M}_n$  derivable from this mechanism was 5.6, which was clearly too small to merit further consideration, since experimental ratios are much greater, up to 55. The bimolecular exchange mechanism presented in this paper not only leads to any desired  $\overline{M}_w/\overline{M}_n$  ratio, but also predicts bimodal molecular weight distributions for certain values of  $C_1/I_0$  and  $k_t/k_p$ .

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#### Résumé

Les publications précédentes de cette série contiennent les résultats expérimentaux, qui démontrent la complexité de la polymérisation anionique homogène "sans terminaison'' du méthacrylate de méthyle. En vue d'expliquer les larges distributions des poids moléculaires observées, il a été nécessaire de postuler l'intervention de réactions réversibles de "pseudo-terminaison" au cours desquelles une grande partie de l'ensemble des anions présents dans le système devient inactive vis-à-vis d'une polymérisation ultérieure, bien qu'une probabilité déterminée de réobtention d'une certaine activité de polymérisation par des processus tels que l'échange de liants, l'ouverture de cycle par l'intervention d'un complexe cyclique etc. puisse également se présenter. Dans la présente publication, nous avons examiné les conséquences quantitatives d'un mécanisme au cours duquel cette réaction de pseudo-terminaison a lieu du fait d'un échange bimoléculaire de l'activité entre une chaîne active et une chaîne inactive. Il a été possible de calculer  $M_w/M_n$ , rapport du poids moléculaire moyen en poids au poids moléculaire moyen en nombre, en fonction du degré de conversion alpha, du rapport initial en monomère et en initiateur,  $\overline{M}_0/I_0$ , de la fraction d'initiateur total en tant que chaînes actives  $C_1/I_0$  et du rapport de la vitesse d'échange de l'activité à la vitesse de propagation  $k_l/k_p$ . Les résultats principaux de ces calculs sont (1) toute valeur de  $M_w/M_n$  comprise entre 1 et l'infini est possible pour alpha = 1; (2)  $M_w/M_n$  pour  $\alpha = 1$  décroît quand  $k_i:k_p$  augmente; (3)  $\overline{M}_{\omega}/\overline{M}_n$  pour  $\alpha = 1$  augmente quand  $\overline{M}_0/I_0$  augmente si  $k_i:k_p$  et  $C_1/I_0$  sont petits—sous certaines conditions  $\overline{M_w}/\overline{M_n}$  pour  $\alpha = 1$  augmente et puis décroît faiblement quand  $M_0/I_0$  augmente; (4)  $\overline{M}_w/\overline{M}_n$  passe par un maximum au cours de la polymérisation si  $k_l = 0$ ; (5)  $\overline{M}_w/\overline{M}_n$  pour n'importe quelle valeur de  $\alpha$  décroît quand  $C_1/I_0$  augmente pour des valeurs constante de  $M_0/I_0$  et de  $k_l/k_p$ . Les concentrations en chaînes individuelles de n'importe quelle longueur donnée en fonction du temps peuvent être facilement calculées pour les deux cas spéciaux où  $k_l/k_p$  tend vers zéro ou bien vers l'infini.

#### Zusammenfassung

Die früheren Mitteilungen in dieser Reihe enthalten experimentelle Ergebnisse, welche den komplexen Charakter der homogenen "abbruchsfreien" anionischen Polymerisation von Methylmethacrylat zeigen. Zur Erlärung der beobachteten breiten Molekulargewichtsverteilung war die Annahme von reversiblen "Pseudoabbruchs"-Reaktionen notwendig, durch welche ein grosser Bruchteil des gesamten, im System vorhandenen Anions für weitere Polymerisation inaktiv wurde, jedoch eine endliche Wahrscheinlichkeit zur Wiedergewinnung der Polymerisationsaktivität durch gewisse Prozesse, wie Ligandenaustausch, Ringöffnung eines zyklischen Komplexes etc. besass. In der vorliegenden Mitteilung werden die quantitativen Folgerungen aus einem Mechanismus überprüft, bei welchem diese Pseudoabbruchsreaktion in einem bimolekularen Aktivitätsaustausch zwischen einer aktiven und einer inaktiven Kette besteht.  $\overline{M}_w/\overline{M}_n$ , das Verhältnis des Gewichtsmittels zum Zahlenmittel des Molekulargewichts, konnte als Funktion des Umsatzes  $\alpha$ , des Anfangsverhältnisses des Monomeren zum Starter,  $\overline{M}_0/I_0$ , des Bruchteils des als aktive Ketten vorhandenen gesamten Starters,  $C_1/I_0$ , und des Verhältnisses der Aktivitätsaustauschgeschwindigkeit zur Wachstumsgeschwindigkeit  $\tilde{\kappa}_{\ell}/k_{p}$  berechnet werden. Die Hauptergebnisse dieser Berechnung sind: (1) Bei  $\alpha = 1$ ist jeder Wert für  $\overline{M}_w/\overline{M}_n$  zwischen 1 und  $\infty$  unendlich möglich; (2)  $\overline{M}_w/\overline{M}_n$  bei  $\alpha = 1$ nimmt mit steigendem  $k_l/k_\rho$  ab; (3) Bei kleinem  $k_l/k_\rho$  und  $C_1/C_0$  nimmt  $\overline{M}_w/\overline{M}_n$  bei  $\alpha = 1$  bei steigendem  $\overline{M}_0/I_0$  zu; unter gewissen Bedingungen nimmt  $\overline{M}_w/\overline{M}_n$  bei  $\alpha = 1$ bei steigendem  $M_0/I_0$  zu und dann schwach ab; (4) Bei  $k_t = 0$  geht  $\overline{M}_w/\overline{M}_n$  im Verlauf der Polymerisation durch ein Maximum; (5)  $M_w/M_n$  nimmt für beliebiges  $\alpha$  bei konstantem  $M_0/I_0$  und  $k_t/k_p$  mit steigendem  $C_1/I_0$  ab. Die Konzentration individueller Ketten von beliebiger Länge kann als Funktion der Zeit für die beiden speziellen Fälle  $k_t/k_p \rightarrow 0$  oder unendlich leicht berechnet werden.

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# Glass Temperatures of Mixtures of Compatible Polymers

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#### Synopsis

Dilatometric glass transition temperatures were measured on mixtures of isotactic and syndiotactic poly(methyl methacrylate) and on mixtures of poly(isopropyl acrylate) with poly(isopropyl methacrylate). The glass temperatures of copolymers of isopropyl acrylate with isopropyl methacrylate fall on the same glass temperature versus composition curve as those of the homopolymer mixtures. The data are compared with theoretical predictions of Fox, Gordon and Taylor, and Kanig. None of these treatments can adequately explain the results.

## **INTRODUCTION**

Theoretical expressions which relate the glass transition temperatures of polymer-solvent mixtures to the composition of the mixtures generally involve not only the glass transition temperature of the pure polymer, but also a glass transition temperature for the solvent.¹⁻³ Most solvents, however, crystallize so readily on cooling that no glass is ever formed, and thus no glass transition temperature can be measured. It therefore seemed of interest to investigate the variation of glass transitions can be observed in both pure components.

Most polymer-polymer systems do not form solutions over the whole composition range because the very small entropy of mixing of these large molecules generally is not enough to outweigh even a very small positive, i.e., unfavorable, heat of mixing. We therefore report on only two compatible systems, especially since we considered it desirable to work with homopolymers whose glass transition temperatures were at least  $75^{\circ}$ C. apart. Some low conversion "random" copolymers of one of these systems were studied in order to find out whether the presence of two different monomer units in the same molecule caused similar or different effects than they did when present in different molecules.

## EXPERIMENTAL

#### **Polymers**

The syndiotactic poly(methyl methacrylate) was prepared by anionic polymerization in liquid  $NH_3$  at  $-70^{\circ}C$ , with the use of a mixture of sodium and lithium amides as initiator.⁴ The polymer had the x-ray

diffraction pattern of syndiotactic poly(methyl methacrylate).⁵ Its number-average molecular weight  $\overline{M}_n$  was  $9.52 \times 10^4$ , well above the value at which glass transition temperatures cease to vary with molecular weight. This value is probably about  $4 \times 10^4$ . Fox and Flory,⁶ working with polystyrene fractions, found that  $T_q$  stops increasing at a value of  $\overline{M}_n$ between  $2.2 \times 10^4$  and  $8.5 \times 10^4$ , while Ueberreiter and Kanig,⁷ working with fractions of the same polymer, found that the limiting  $T_{g}$  was reached at  $\overline{M}_n = 4.1 \times 10^4$ . They also found that the glass temperatures of mixtures of these fractions depended only on the  $\overline{M}_n$  of the mixtures, i.e., not on the molecular weight distributions. In the case of poly(methyl methacrylate), Beevers and White⁸ found that the limiting  $T_g$  was reached when  $\overline{M}_n$  was between  $3.8 \times 10^4$  and  $7.2 \times 10^4$ . For polyacrylonitrile, they⁹ found the limiting  $T_g$  between  $\overline{M}_n = 1.8 \times 10^4$  and  $6.6 \times 10^4$ .

The isotactic poly(methyl methacrylate) was prepared by anionic polymerization in toluene at 0°C. with phenylmagnesium bromide etherate as initiator.¹⁰ The sample had the x-ray diffraction pattern of isotactic poly(methyl methacrylate)¹¹ [the assignments of isotactic and syndiotactic configurations to the different stereo forms of poly(methyl methacrylate) were reversed in reference 8] and a J value of  $32.^{10}$  J values are a tacticity index based on the infrared spectrum of poly(methyl methacrylate). J values between 25 and 35 cenote isotactic samples, the lowest J values denoting the highest degree of isotacticity. The number-average molecular weight of this sample was  $2.97 \times 10^4$ . This sample, therefore, may not have exhibited the highest possible glass transition temperature of an isotactic sample.

Poly(isopropyl acrylate) was prepared from a 35% by weight solution of monomer in methyl propionate at 44.1°C. The azobisisobutyronitrileinitiated polymerization was taken to 30% conversion. The polymer had  $\bar{M}_n = 1.28 \times 10^5$ .

Two samples of poly(isopropyl methacrylate) were prepared, both at 44.1°C., azobisisobutyronitrile (AIBN) being used as the initiator. Sample I was prepared from 42% by weight solution of monomer in benzene, taken to 7% conversion. Sample II was prepared from a 22% by weight monomer solution in methyl propionate, taken to 20% conversion.  $\overline{M}_n$  of sample I was  $3.30 \times 10^5$ ; that of sample II was  $1.53 \times 10^5$ .

Three copolymers of isopropyl acrylate and isopropyl methacrylate were

	Comp	osition of mixture	polymeri: , wt%	zation	Con-		
Copolymer sample	IPA	IPMA	<i>p-</i> Xylene	$C_6H_6$	version, %	IPA, mole-%	${ar M_n}  imes 10^{-5}$
C1	8	10	78	4	5	30.8	2.85
C2	12	6	75	7	10	50.0	1.22
C3	15	3	75	7	6	73.7	0.845

TABLE I Polymerization Data for Isopropyl Acrylate (IPA)-

#### **GLASS TEMPERATURES**

prepared at 60°C. with AIBN as initiator in *p*-xylene solution. Small amounts of benzene were added to the solutions of monomer in *p*-xylene to serve as an internal standard for gas chromatography. Gas chromatography was used to follow the course of the copolymerizations and, thereby, to give data from which the average compositions of the copolymer samples could be calculated. Table I gives the polymerization data for these copolymer samples. The column giving mole per cent IPA refers to the composition of the copolymer as calculated from the gas chromatography data obtained during the polymerization. All values of  $\overline{M}_n$  were obtained from osmotic pressure measurements.

#### **Preparation of Polymer Mixtures**

Mixtures of polymers for dilatometric studies were prepared by mixing chloroform solutions of the two polymers and then evaporating the chloroform as slowly as possible. Chloroform solutions containing 5% of the mixed polymers of molecular weight >10⁶ showed no signs of phase separation after several days at room temperature. When the chloroform was evaporated quickly from solutions containing mixtures of poly(isopropyl acrylate) with poly(isopropyl methacrylate), the resulting films looked turbid; when the chloroform was evaporated slowly, the resulting films were usually clear.

## Dilatometry

Mercury was used as the containing liquid in dilatometers whose capillaries had 2 mm. diameter in all cases. After a polymer film was placed in a dilatometer and the dilatometer was sealed off, residual chloroform was removed by heating the dilatometer under vacuum at the temperature at which the sharp edges of the film began to flow (usually  $30-50^{\circ}$ C. above the glass temperature) for at least 8 hr. The mercury was then added at room temperature, and the dilatometer bulb was heated again to the "degassing" temperature so that the mercury could fill all the voids in the sample. The dilatometric runs were generally made starting at the low temperatures, using 5°C. temperature intervals below room temperature and  $10^{\circ}$ C. temperature intervals above room temperature, each temperature being held for a time sufficient to establish a height of mercury in the capillary which did not change in a 10-min. period (this means that the temperature was changed approximately every half hour). Most polymer mixtures were run several times in order to find out whether the data would appear different as the sample history changed.

### RESULTS

#### **Poly(methyl Methacrylate) Mixtures**

Figure 1 shows a typical volume-temperature plot for one of the mixtures of isotactic with syndiotactic poly(methyl methacrylate). Although drawing four straight lines instead of a curve through these points smacks of overinterpretation of the data, we emphasize that approximately the

Syndiotactic in mixture, %	T ₀ , °C.	$T_{1}$ , °C.	$T_{2_s}$ °C.	αG' × 10 ⁴	αG × 10 ⁴	$\alpha L \times 10^4$	$\alpha L' \times 10^4$	Temperature range over which data obtained, °C.
0	45	I	1	1	0.7	41, 8.	Ţ	-35 to 120
14.9	<b>5</b> 0	1	120	1	1.2	4.7	6.5	-35 to 190
.26.0	<b>5</b> 5	I	135	1	1.0	4.3	7.6	-30 to 200
(unren) "	55	1	127	1	1.4	4.6	6.9	-35 to 230
50.7	75	10	149	0.9	1.5	4.6	7.0	-30 to $190$
" (rerun)	73	20	140	1.0	1.6	4.8	6.0	-35 to 220
74.9	88	i.	160	1.0	1.7	4.6	6.3	-30 to 200
" (rerun)	88	16	140	1.3	2.1	5.0	5.4	-35 to $200$
79.4	94	30	159	1.1	1.8	4.6	6.5	-35 to 210
100	120	I	[	1	0 L	1 5	1	30 to 240

TABLE II Transition Temperatures of Poly(methyl Methacrylate) Mixtures

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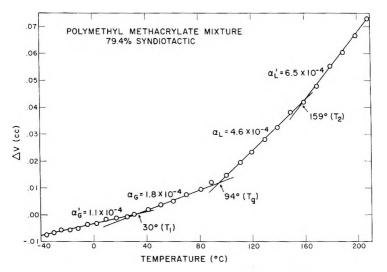


Fig. 1. Volume-temperature plot of a mixture of 79.6% by weight syndiotactic poly-(methyl methacrylate) with 21.6% by weight isotactic poly(methyl methacrylate).

same straight lines were drawn by both of us; furthermore, both of us obtained the same glass transition temperature from the plots. Most of the mixtures showed three transitions, although the two mixtures containing the least percentages of syndiotactic polymer did not exhibit the low temperature transition. The transition which fell between the glass temperatures of the homopolymers was chosen as the glass transition temperature of the mixture both because it was invariant with sample history, i.e., it did not change when a sample was rerun, and because the largest change in volume expansion coefficient occurred during this transition. Numerical results for the mixtures are shown in Table II. The meaning of  $T_1, T_2, \alpha G'$ , and  $\alpha L'$  is the same as that indicated in Figure 1.

## Isopropyl Acrylate–Isopropyl Methacrylate Homopolymer Mixtures and Copolymers

Most of the poly(isopropyl acrylate)-poly(isopropyl methacrylate) mixtures showed only a single break in the volume-temperature plots. Four of the mixtures, as can be seen from the footnotes in Table III, however, showed a high temperature transition. One of the poly(isopropyl methacrylate) samples, on the other hand, exhibited a low temperature transition. Data for these mixtures and copolymers are shown in Table III.

The glass transition temperature of sample I of poly(isopropyl methacrylate) could not be determined until the second rerun of the sample. The volume-temperature plots in the first two runs were quite curved. Sample II, which had a lower molecular weight than sample I, showed much greater reproducibility in its volume-temperature plots, both in mixtures and when run alone. All data reported on mixtures made up with sample I are from reruns.

PIPMA sample	PIPMA, wt%	<i>Т</i> _о , °С.	$ imes 10^4$	$ \stackrel{\alpha_L}{\times} 10^4 $	Temperature range over which data obtained, °C.
			Mixtures		
	0	-5	2.8	6.9	80
II	12.2	-2	3.4	6.7	160
II	30.2ª	15	3.0	6.4	160
II	" (rerun) ^b	15	3.0	6.4	160
Ι	49.8	25	2.7	6.8	140
II	<b>49</b> ,9°	25	2.7	6.7	160
Ι	70.3	41	2.6	6.6	140
II	71.0ª	39	2.6	6.7	-35 to 160
II	84.8	54	2.6	7.4	-35 10 160
Ι	85.4	53	2.4	6.5	140
I	89.6	61	<b>2</b> , $5$	6.9	140
II	90.6	60	2.4	6.8	160
Ι	94.8	65	2.5	7.0	140
I	" (rerun)	68	2.2	7.0	140
Ι	100 ^e	83	2.5	6.6	140
II	100	78	<b>2</b> .1	6.7	160
			Copolymer	s	
C1 ^f	28.6	10	2.3	6.9	110
$C2^{t}$	52.9	24	2.5	6.6	$-35$ to $\{130\}$
$C3^{f}$	71.7	41	2.3	6.5	(120

TABLE III Transition Temperatures of PIPA-PIPMA Mixtures and Copolymers

^B  $T_2 = 116$  °C.  $\alpha L' = 7.6 \times 10^{-4}$ .

^b  $T_2 = 110^{\circ}$ C.  $\alpha L' = 7.5 \times 10^{-4}$ .

°  $T_2 = 110$  °C.  $\alpha L' = 7.5 \times 10^{-4}$ .

^d  $T_2 = 113$  °C.  $\alpha L' = 7.5 \times 10^{-4}$ .

 ${}^{e}T_{1} = 11 {}^{\circ}C. \ \alpha G' = 1.8 \times 10^{-4}.$ 

^f Copolymer sample number from Table I.

## DISCUSSION

Figures 2 and 3 show glass transition temperatures versus composition by weight of the poly(methyl methacrylate) mixtures and the isopropyl acrylate-isopropyl methacrylate copolymer and homopolymer mixtures. In addition to the experimental data, Figure 2 shows a dashed line, which is simply the straight line between the glass transition temperatures of the homopolymers, and a solid line, which represents the Gordon-Taylor equation:²

$$T_{g} = \frac{w_{\rm A} T_{g\rm A}(\alpha_{\rm LA} - \alpha_{\rm GA}) + w_{\rm B} T_{g\rm B}(\alpha_{\rm LB} - \alpha_{\rm GB})}{w_{\rm A}(\alpha_{\rm LA} - \alpha_{\rm GA}) + w_{\rm B}(\alpha_{\rm LB} - \alpha_{\rm GB})}$$
(1)

which was derived for copolymers rather than polymer mixtures. In this equation,  $T_{g}$  is the glass temperature of the copolymer,  $T_{gA}$  and  $T_{gB}$  are the glass temperatures of the corresponding homopolymers, designated as A and B,  $w_{A}$  and  $w_{B}$  are the weight fractions of A and B in the copolymer, respectively, and  $\alpha_{LA}$ ,  $\alpha_{GA}$ ,  $\alpha_{LB}$ , and  $\alpha_{GB}$  are the thermal expansion coeffi-

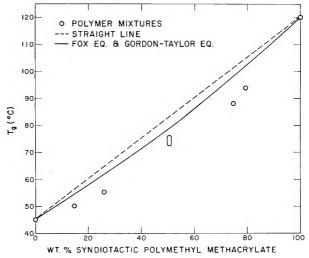


Fig. 2. Glass temperatures of poly(methyl methacrylate) mixtures.

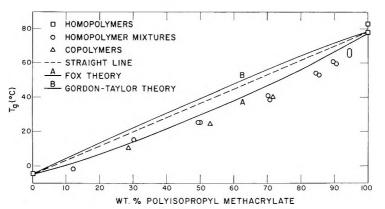


Fig. 3. Glass temperatures of isopropyl acrylate-isopropyl methacrylate homopolymer mixtures and copolymers.

cients of the corresponding homopolymers in the following order: homopolymer A above the glass temperature, homopolymer A below the glass temperature, homopolymer B above the glass temperature, and homopolymer B below the glass temperature.

On Figure 2 the solid line also represents the  $Fox^1$  equation, which was originally derived for both copolymer and mixtures of polymers with plasticizers:

$$T_g = T_{gA} T_{gB} / (w_A T_{gB} + w_B T_{gA}) \tag{2}$$

Figure 3 shows the data for the isopropyl acrylate-isopropyl methacrylate copolymers, homopolymers, and homopolymer mixtures. The data for the copolymers fall in line with the data for the homopolymer mixtures, a very surprising result. However, similar results have been obtained in dynamic mechanical measurements by Nielsen¹³ for 50/50 mixtures of poly(vinyl acetate) and poly(methyl acrylate) and for a random copolymer containing the two monomers in the same proportions. Glass transition temperatures are often considered to be associated with the onset of translational and vibrational motion of appreciable sections of the polymer backbone (comprising at least three monomer units). The moving portions of the polymer backbones are very different in the more or less random copolymers of isopropyl acrylate with isopropyl methacrylate than they are in the homopolymers in the mixtures. Even compatible polymers do not have their monomer units mixed as intimately as they are in copolymers.

The dashed line in Figure 3 is the straight line between the glass temperature of poly(isopropyl acrylate) and that of the low molecular weight sample of poly(isopropyl methacrylate). The solid curve labeled Arepresents the Fox equation [eq. (2)] between the same two glass temperatures, and the solid curve labeled B represents the Gordon-Taylor equation [eq. (1)] between these two glass temperatures. If the data for the high molecular weight poly(isopropyl methacrylate) sample had been used to calculate curves from eqs. (1) and (2), eq. (1) would have given the straight line between the glass transition temperatures of the homopolymers, and eq. (2) would have given a curve very similar to curve A.

On both Figures 2 and 3, the measured glass transition temperatures are well below any that can be calculated from eqs. (1) and (2). The Gordon-Taylor equation, which takes into account not only the glass transition temperatures of the homopolymers, but also the differences in their thermal expansion coefficients, gives especially poor results when compared with the data on the copolymers shown in Figure 3.

Recently, Kanig³ used the hole theory of liquids and the iso free volume theory of the glass transition temperature to derive general relationships for the glass temperatures of copolymers and of polymer-plasticizer mixtures. His relationship for the glass temperature of copolymers reduces to the Gordon-Taylor equation under certain conditions. Illers¹² found that many copolymer systems which did not follow the Gordon-Taylor relationship did follow the Kanig relationship:

$$(T_{gB} - T_{g})/\phi_{fA} = C_{1}\phi_{fA} + C_{2}$$
(3)

where  $C_1$  and  $C_2$  are constants for any particular copolymer system and

$$\phi_{fA} = w_A / [w_A + (\alpha_{LB} - \alpha_{GB}) w_B / (\alpha_{LA} - \alpha_{GA})]$$
(4)

If eq. (3) holds for a particular copolymer system, then a plot of  $(T_{gB} - T_g)/\phi_{fA}$  versus  $\phi_{fA}$  must be a straight line.

The relationship derived by Kanig for polymer-plasticizer mixtures is:

$$\frac{T_{gA} - T_g}{(T_g - T_{gB})\phi_{fB}} - \frac{T_{gA} - T_{gB}}{T_g - T_{gB}} = C_3 \frac{\phi_{fA}}{T_g - T_{gB}} + C_4$$
(5)

where  $\phi_{fB}$  is defined just like  $\phi_{fA}$  in eq. (4), changing all the A's to B's in the subscripts and vice versa. In those cases in which this equation holds, a plot of the left hand side of eq. (5) versus  $\phi_{fA}/(T_g - T_{gB})$  will be a straight line.

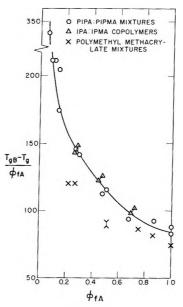


Fig. 4. Isopropyl acrylate-isopropyl methacrylate homopolymer mixtures and copolymers according to the Kanig theory for copolymers.

Figure 4 shows a plot according to eq. (3), i.e., Kanig's copolymer equation, of the data for the poly(methyl methacrylate) mixtures, the poly-(isopropyl acrylate)-poly(isopropyl methacrylate) mixtures, and the isopropyl acrylate-isopropyl methacrylate copolymers. In the case of the copolymers, the points were calculated on the basis of the data for both poly(isopropyl methacrylate) samples. For this reason, two points have been plotted for each copolymer sample. Figure 4 shows clearly that the data for the isopropyl acrylate-isopropyl methacrylate system do not fit Kanig's theory for copolymers. The data on the poly(methyl methacrylate) mixtures is more ambiguous; it is possible to draw a reasonably straight line through the points. However, one could just as easily draw a curve similar to the one drawn through the isopropyl acrylate-methacrylate points.

Attempts to calculate the data for either set of polymer mixtures according to eq. (5) result in plots in which the points do not fit either a straight line or any other reasonable curve. This may be happening, not because eq. (5) is incorrect, but because it is too sensitive to slight differences in the glass transition temperatures and thermal expansion coefficients, at least in the case of polymer mixtures in which the glass transition temperatures of the pure components are relatively close together.

However, no matter what the reason for the failure of eq. (5) for these mixtures, Figure 4 shows that eq. (3) does not apply either. In other words, neither the Gordon-Taylor theory for copolymers, the Fox theory for copolymers and mixtures, the Kanig theory for copolymers, or the Kanig theory for mixtures applies to the mixtures and copolymers discussed here. The Fox theory is the only one which takes into account the possibility that copolymers and mixtures might follow the same glass temperature-composition relationship. It seems obvious that a new theoretical treatment for the glass transition temperatures of copolymers and of mixtures is needed, one which allows for the fact that at least one system in which the homopolymers are reasonably compatible has the same glass temperaturecomposition relationship for homopolymer mixtures and for copolymers.

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## Résumé

On a mesuré, par dilatométrie, les températures de transition vitreuse de mélanges de polyméthacrylate de méthyle isotactique et syndiotactique, et de mélanges de polyacrylate d'isopropyle et de polyméthacrylate d'isopropyle. Les températures vitreuses des copolymères d'acrylate d'isopropyle avec le méthacrylate d'isopropyle sont les mêmes que celles des mélanges des homopolymères, dans un graphique température vitreuse/composition. On a comparé les résultats avec les prévisions théoriques de Fox, Gordon et Taylor, et Kanig. Aucune de ces théories ne peut expliquer d'une façon adéquate les résultats obtenus.

#### Zusammenfassung

An Mischungen von isotaktischem und syndiotaktischem Poly(methylmethacrylat) und an Mischungen von Poly(isopropylacrylat) mit Poly(isopropylmethacrylat) wurden dilatometrisch Glasumwandlungstemperaturen gemessen. Die Glasumwandlungstemperaturen der Copolymeren von Isopropylacrylat mit Isopropylmethacrylat liegen auf der gleichen Glastemperatur- und Zusammensetzungskurve wie diejenigen der Homopolymeren. Die Ergebnisse werden mit den theoretischen Voraussagen von Fox, Gordon-Taylor und Kanig verglichen. Keine dieser Theorien liefert eine ausreichende Erklärung der Ergebnisse.

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# Radiation-Induced Polymerization and Other Reactions of *n*-Perfluoropentadiene-1,4 at High Temperature and Pressure*

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## **Synopsis**

The radiation-induced polymerization of *n*-perfluoropentadiene-1,4 was studied at temperatures of 100-170°C. and pressures of 8,000-15,000 atm. Kinetic evidence indicates that polymerization occurs by a free radical reaction; the activation energy is between 14 and 17 kcal./mole and the activation entropy is  $-8 \pm 5$  e.u./mole. Transfer with monomer limits the number-average degree of polymerization to values of 40 or less except in special circumstances. Dimerization and double bond migration occur to some extent; *n*-perfluoropentadiene-1,3 is formed in the latter process. It and the 1,4-diene copolymerize; the latter undergoes cyclic addition so that the polymers are soluble and have little perfluorovinyl unsaturation. The polymers are brittle if the fraction of 1,3-diene in the polymer is less than 0.1. They are rubbery and of considerably higher molecular weight if the fraction of 1,3-diene is greater than 0.4. The thermal stability of the polymers decreases as the content of 1,3-diene increases.

#### **INTRODUCTION**

Studies are being carried out on the synthesis and polymerization of *n*-perfluoro- $\alpha,\omega$  dienes, containing 5, 6, 7, and 8 carbon atoms. It is expected that the polymerizations, to a considerable extent, will follow the alternating intra-intermolecular or cyclopolymerization mechanism described by Butler and Marvel.^{1,2} This paper presents results of studies on the 5-carbon diene. Applied to this compound, the expected process of cyclopolymerization can be represented as:

$$n(CF_2 = CF - CF_2 - CF = CF_2) \rightarrow -CF_2 - CF_2 -$$

Active centers add to the  $CF_2$  group at one end of the molecule, and the adduct attacks the other end; the result is the final structure shown.

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Two main problems are considered in this study. One is the elucidation of the polymer structure, necessarily in the presence of complicating reactions. The other is the treatment of polymerization rate as a function of temperature and pressure in the presence of these reactions.

Fully fluorinated monomers are difficult to polymerize. For this reason, the reactions were carried out at pressures between 8,000 and 15,000 atm. and temperatures between 100 and 165°C. Polymerization occurs at reasonable rates under such conditions. At high pressure the monomer 4-chloroperfluoroheptadiene-1,6 formed a saturated soluble polymer of high molecular weight.³

#### EXPERIMENTAL

The synthesis of the monomer has been described.⁴ As prepared, it contained about 1% *n*-perfluoropentadiene-1,3 (CF₂=CF-CF=CF-CF₃) and about 0.3% of an unidentified compound that was probably the 2,3-diene, (CF₃-CF=C=CF-CF₃), since an equilibrium exists between 1,4-diene, 1,3-diene, 2,3-diene, and 2-pentyne.⁵

The pressure vessels and irradiation techniques have been described previously.⁶ In essence, degassed monomer in a steel bomb at known temperatures and pressures was exposed to radiation of known intensity from an external Co⁶⁰ source. After removal from the bomb, the monomer and polymer were separated by heating the sample under vacuum. The final conditions were 100°C. at about 0.1  $\mu$  pressure for 3 hr. Appropriate runs were made in the absence of radiation. Polymer yields are accurate within 2%.

Measurements of the number-average degree of polymerization were made with a Mechrolab vapor-pressure osmometer, hexafluorobenzene being used as solvent. The values obtained are imprecise by about 5%. At this level of precision, no concentration dependence of the calculated value was found for a degree of polymerization equal to 68. Thus, any systematic error probably is small compared with the imprecision of the measurements. Intrinsic viscosities were determined in hexafluorobenzene at 29.6°C.

Large amounts of nonpolymeric products were formed under some conditions. The content of 1,3-diene sometimes increased; this compound was identified by boiling point and absorption at  $5.85 \ \mu$ .⁵ Often the amount of the compound believed to be the 2,3-diene increased. A fraction boiling at 40°C. at 30 mm. pressure is thought to consist of dimers. The number of species in this fraction, as judged by peaks in vapor-phase chromatograms, varied with reaction temperature. It was three in fractions from runs at 110 and 135°C. and five from runs at 160°C. Vapor-phase chromatography (VPC) was used to determine directly the nonpolymeric compounds, except for that of the 1,4-diene. Values determined by VPC are uncertain by 5–10%. The percentage of 1,4-diene in the recovered material was calculated as 100 minus the sum of all the other components.

Infrared spectra usually were obtained from specimens that had been heated at  $180^{\circ}$ C. at 0.1  $\mu$  pressure. Such specimens were pressed into

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films, usually at 140°C., between sheets of aluminum foil. Although the films often were brittle, small pieces could be obtained that were suitable for use in the beam-condenser attachment of a Perkin-Elmer 221. Film thickness was between 0.002 and 0.004 in.; it was measured with a micrometer. The symbol  $DP_n'$  refers to the degree of polymerization of these specimens, whereas  $DP_n$  is the degree of polymerization of samples heated at 100°C. and 0.1  $\mu$ .  $DP_n'$  is greater than  $DP_n$  because more of the very low polymer (n = 2, 3, 4, 5) evaporates at 180°C. and 0.1  $\mu$  than at 100°C. and 0.1  $\mu$  pressure.

Comparative pyrolyses were performed by placing tubes containing different samples side by side in an evacuated heated tube. The loss in weight of each sample was determined over two time intervals at each temperature. The pyrolysis was explored at temperatures of 295, 334, and 395°C. The residues from the pyrolyses at 295°C. were used at 334°C., and those from the latter temperature were used at 395°C. The rates so obtained were extrapolated to zero conversion.

## RESULTS

Oils or very low yields of solids were obtained at pressures of a few atmospheres at 110°C. The first experiments at high pressure resulted in formation of soluble, rubbery polymer. Little monomer was recovered; the 1,3-diene and the dimer fraction were the main products. In later experiments under the same reaction conditions it was found that brittle, solid polymers sometimes were formed with reduced formation of side products. These polymers were soluble and transparent when molded and so are believed to be glasses. The infrared spectra of both types of polymers and also the dimer fraction showed bands in the double-bond region at 5.6 and 5.85  $\mu$ . Absorption at these wavelengths is a characteristic of compounds containing the groups —CF=CF₂ and —CF=CF-, respectively.

In the course of this work several combinations of reaction conditions gave rubbery polymer in one instance and glassy polymer in another instance. Data from such experiments are paired in Table I. Listed are: reaction conditions, product composition, the fractional rate of polymerization  $R_p$ , intrinsic viscosity,  $DP_n$ ,  $DP_n'$ , the concentrations of -CF=CF- and  $-CF=CF_2$  groups in the polymer as calculated from infrared data, and a column headed FF', which has significance for the rate data.

The rate,  $R_p$ , is the fraction of polymer formed, divided by the product of irradiation time and the arithmetic mean of final and initial fractions of polymerizable monomer (which is taken as the sum of the fractions of 1,4- and 1,3-diene). The mean monomer fraction is used to correct for the high conversion, which approached 35% in some runs; it is an approximation to the average monomer concentration. The time at temperature and pressure is used in runs performed without radiation.

It is seen that the rubbers form more quickly than the glasses; they contain more internal double bonds and fewer perfluorovinyl groups. Both types of polymer formed in these experiments were completely

	Cond	Conditions														
	Dose	Pres- sure,			i							Degr	Degree of polymeri-	Conce	Concentration ^d	
Temp	Temp., rate.	×	Time.		Compc	osition,	Composition, wt%		1028	Polymer	.[4]	zat	zation ^e	C.	<i>c</i>	
°C.	°C. Mrad/hr.	10-3	hr.	1,4 ^b	1,3	2,3	Dimers	Dimers Polymer	10 ² hr1	type	dl./g.	$\mathrm{DP}_n$	$DP_{n'}$	mole/l.	DPn' mole/l. mole/l.	FF'
110	0.0077	11.4	2.00	69	11	1.1	17	2.17	1.21	Rubbery	0.26	ND	NDe	6.0	0.08	6.4
110	0.0077	11.4	1.53	98	1.1	0.3	0	0.38	0.25	Glassy	ΠŊ	18	ND	1.1	1.1	1.26
110	0.14	11.4	2.40	75	8.0	1.4	15	10.3	4.92	Rubbery	0.10	ΠŊ	ND	5.4	0.13	4.9
110	0.14	11.4	3.25	96	0.8	0.5	0	3,45	1.08	Glassy	0.04	23	69	0.8	0.47	1.24
103	0.047	14.9	8.20	6.6	3.2	2.2	45	43	10	Rubbery	0.68	ΠN	ND	3.9	0.01 -	26
															0.02	
103	0.047	14.9	3.25	96	0.8	0.1	0	3.51	1.1	Glassy	ND	35	99	1.0	0.35	1.22
170	0	8.0	0.5	ND	ND	ND	30	8.4	>21	Rubbery	0.20	ND	ND	6.2	0.19	ND
170	0	8.0	3.1	96	0	1.8	1.9	0.39	0.13	Glassy	ND	ΠŊ	ND	ND	ND	1.22

• ND signifies that the quantity was not determined.

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TABLE II Temperature and Pressure Effects in Experiments in which Glassy Polymer Formed

Temp	Pressure	Time		Com	position	Composition, wt% ^b		102R					
°C.	10-3	hr.	1,4	1,3	2,3	Dimers	Polymer	10 ² hr1	FF	mole/l.	mole/l.	$\mathrm{DP}_n$	$\mathrm{DP}_n'$
166	8.0	2.8	16	0	1.3	2.2	4.3	1.6	1.22	0.46	0.24	25	54
139	8.0	17.71	79	1.0	3.3	7.7	9.1	0.57	1.37	1.3	0.16	21	45
102	8.0	15.3	95	1.3	1.1	0	3.0	0.20	1.32	1.1	0.36	19	32
170	8.0	3.1c	<b>96</b>	0	1.8	1.9	0.39	0.13	1.22	ND	ND	ND	ND
166	11.4	1.5	72	0	6.2	17	4.7	3.70	1.22	1.3	0.23	23	36
138	11.4	3.7	86	0.6	2.3	6.4	5.1	1.50	1.29	1.2	0.16	28	50
110	11.4	14.6	93	0.7	0.4	0	5.7	0.41	1.21	0.9	0.35	21	40
110	11.4	3.5°	98	1.1	0	0	0.14	0.041	1.24	ND	ND	ND	ND
165	14.9	0.95	82	0	3.0	6.4	8.6	6.6	1.22	0.39	0.25	38	64
136	14.9	3.0	62	0.9	3.7	6.5	9.7	3.60	1.36	1.20	0,26	29	63
134	14.9	0.83	96	0	0.6	0.9	2.5	3.20	1.18	0.46	0.33	27	62
103	14.9	3.3	<b>96</b>	0.8	0.1	0	3.5	1.10	1.25	1.0	0.25	35	66
166	14.9	1.2e	66	0	7.5	24	2.4	2.0	1.22	1.1	0.42	ND	44

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e The radiation intensity was zero.

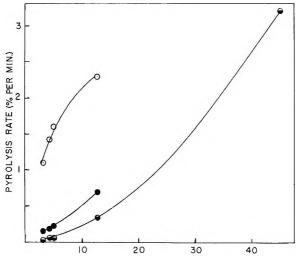
Ι,	$I^{1/2}$ ,						Conc	litions
$\frac{1}{\text{Mrad}}$ hr. $\times$ $10^2$	$(Mrad/hr.)^{1/2} \times 10$	$10^2 R_p$ , $10^2$ hr. ⁻¹	DP _n	[η], dl./g.	F'	Polymer type		Pressure, atm. $\times$ $10^{-3}$
0.77	0.88	1.24	ND	0.26	2.7	Rubber	110	11.4
14	3.7	4.9	ND	0.10	2.3	Rubber	110	11.4
0	0	0.04	ND	ND	1.13	Glass	110	11.4
0.77	0.88	0.25	18	ND	1.15	Glass	110	11.4
4.7	2.2	0.41	21	ND	1.11	Glass	110	11.4
14	3.7	1.10	23	0.04	1.13	Glass	110	11.4
4.7	2.2	0.20	19	ND	1.16	Glass	102	8.0
14	3.7	0.37	18	ND	1.11	Glass	102	8.0

TABLE III Effect of Intensity Variation on  $R_p$  and  $DP_n$ 

soluble. The intrinsic viscosities of the rubbery polymers were determined because their molecular weights were too high to be measured with the Mechrolab instrument.

It was found that glassy polymer was obtained always if the 1,4-diene was degassed immediately after synthesis and stored at  $-30^{\circ}$ C. Storage under nitrogen at the same temperature for periods of up to three weeks before degassing usually permitted formation of the glassy polymer. Monomer stored under air for several days at  $-5^{\circ}$ C. invariably formed rubbery polymer.

Reactions in which glassy polymer formed were consistent enough for kinetic study. Table II contains results of experiments run at different temperatures and pressures. Listings are much the same as in Table I. The dose rate was 0.047 Mrad/hr. in all except the thermal polymerizations.



% UNITS WITH INTERNAL DOUBLE BONDS

Fig. 1. Polymer pyrolysis rate vs. per cent units with internal double bonds: (O)  $394^{\circ}C_{\circ}$ : ( $\bullet$ )  $353^{\circ}C_{\circ}$ ; ( $\bullet$ )  $295^{\circ}C_{\circ}$ 

Two polymer samples, those formed at conversions to polymer of 8.6 and 9.7%, were not completely soluble. The gel fraction of these was about 0.05.

The effects of intensity variation at constant temperature and pressure on  $R_p$ , DP_n, or intrinsic viscosity are shown by data in Table III. Apparently  $R_p$  is nearly proportional to the square root of intensity, whether the polymeric product is glassy or rubbery. DP_n is substantially invariant with  $R_p$  for the glasses, but the intrinsic viscosity of the rubbery samples decreased as  $R_p$  increased.

Figure 1 shows plots of pyrolysis rate versus the per cent of the monomer units in the polymer that have internal double bonds. Three isotherms are shown. Pyrolysis rate increases with the content of internal double bonds.

### DISCUSSION

#### **Qualitative Considerations**

Several reactions occur simultaneously in these experiments; in addition to polymerization, there are three to five dimerization products and two products of double-bond migrations. It is not known what agent causes these side reactions to assume great importance in some cases. The fact that storage under air precedes such results suggests that some product of oxidation or oxidative hydrolysis is involved. The general trends of the data in Table II indicate that temperature increases accelerate bond migration and dimer formation, even when glassy polymer is formed. The fact that 1,3-diene was not observed in the product from any experiment run at temperatures between 160 and 170°C. can be explained by the presence of internal double bonds in the dimer fraction. That is, it is felt the 1.3-diene forms rapidly in this temperature range, but goes into dimers so much more rapidly that its concentration is decreased to an undetectable level ( $\sim 0.05\%$ ). Presumably then, the rate at which dimers form is connected intimately with the rate of bond migration. We will not concern ourselves with quantitative aspects of the rates of bond migration and dimerization because the situation appears too complicated to handle with the data available.

## **Copolymerization Hypothesis**

The 1,3-diene was regarded as being polymerizable, and it was thought that copolymerization of it with the 1,4-diene might explain the presence of internal double bonds in the polymer. The calculation below serves to demonstrate this.

Let us assume a copolymerization mechanism in which the rate of addition of a monomer unit to the attacking radical depends on the type of monomer but not on the radical. Then the fraction f of monomer units which have internal double bonds is:

$$f = \frac{k'_2 M'}{(k_2[M] + k'_2[M'])} = \frac{k'_2 M'_1}{(k'_2/k_2)([M']/[M])/[1 + \frac{k'_2[M']}{(k_2[M])}]}$$

where  $k_2$  and  $k'_2$  are propagation rate constants for addition of 1,4-diene and 1,3-diene, respectively, and [M] and [M'] are the concentrations of these dienes. The density of the polymer is 2.0 g./cc.; from this one calculates that the sum of the concentrations of all monomer units is 9.4 mole/l. Thus,  $c_i$ , the concentration of monomer units, which have internal double bonds, is:

$$c_i = 9.4f$$

Another expression for  $c_i$  is derived from the Beer-Lambert law; it is:

$$c_i = 2.3 \log (I_0/I)/lk_{5.85}$$

where  $k_{5.85}$  is the absorption coefficient at 5.85  $\mu$  in units of liters/molecentimeter, log  $I_0/I$  is the absorbance at this wavelength, and l is the film thickness.

To test the possible identity of the expressions for  $c_i$  a value is needed for  $k_{5.85}$ . One was obtained from the infrared spectrum of polyperfluorobutadiene-1,3, made at high pressure, in the following way. Polyperfluorobutadiene should contain one double bond per monomer unit; in concentration units this is 12 mole/l. Internal and external double bonds are present because 1,4- and 1,2-addition occur. The absorption coefficient for perfluorovinyl groups,  $k_{5.6}$ , was calculated to be 700 l./mole-cm. from the infrared spectrum of solutions of perfluoroheptene-1 in perfluoroheptane. From  $k_{5.6}$ , the concentration of perfluorovinyl groups was calculated to be 0.5 mole/l. By difference the concentration of internal double bonds is 11.5 mole/l.; this leads to a value of 29 l./mole-cm. for  $k_{5.85}$ . This method has the advantages that a relatively large error in the perfluorovinyl group determination has only a small effect on the calculated value of  $k_{5,85}$ , line widths in the infrared spectra of both calibrant and unknown are the same, and, hopefully, *cis* and *trans* ratios are similar. A value of  $k_{5.85}$  equal to 67 l./mole-cm. was obtained from the infrared spectrum of perfluorobutene-2 (cis and trans ratio unknown) in perfluoroheptane. The line width is much less than in the polymer spectra, so the value used in our calculations is 29 l./mole-cm.

A question of importance is, "what is the proper value of [M']/[M] to use in the expression for f?" For the glassy polymers the arithmetic mean of initial and final values is believed to be reasonable because [M']/[M]changed little from its initial value. With the rubbery polymers the final value probably is a better average than the arithmetic mean. That is, it is felt that M'/M probably increased rapidly from its initial value to something like its final value, and then remained relatively constant for most of the reaction. An indication of this is that in experiments that gave rubbery polymer one finds that where the sum of the final content of 1,4-diene plus 1,3-diene differed by a factor of about 12, the ratio [M']/[M] differed by a factor of only 3 to 4 (lines 1, 3, 5 of Table I).

Since  $k_2'/k_2$  is a ratio of rate constants it should be constant at one temperature and pressure. Thus one value of  $k_2'/k_2$  should apply to all data taken from runs at the same temperature and pressure. In Figure 2 is

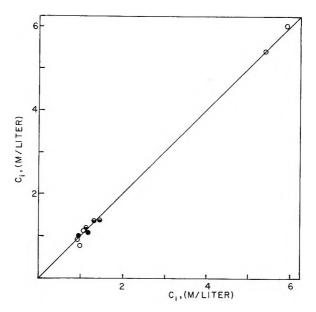


Fig. 2. Internal double bond concentration calculated by Beer-Lambert law vs. the same quantity calculated according to the copolymerization hypothesis: ( $\odot$ ) 109±1°C., 11,400 atm.,  $k'_2/k_2 = 11$ ; ( $\bullet$ ) 110°C., 8,000 atm.; 103°C., 15,000 atm.,  $k'_2/k_2 = 11$ ;  $\bullet$  137±3°C., 8,000, 11,400, and 14,900 atm.,  $k'_2/k_2 = 14$ .

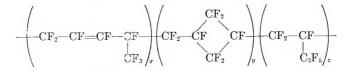
plotted  $c_i$  as calculated by the Beer-Lambert law versus  $c_i$  as calculated by the copolymerization hypothesis. A value of  $k_2'/k_2$  equal to 11 fits data from experiments performed at 109  $\pm$  1°C. and 11,400 atm. over a 10-fold range of [M']/[M]. The same value of  $k_2'/k_2$  fits data from runs at about the same temperature and pressures of 8,000 and 15,000 atm., indicating little effect of pressure on the ratio. A value of  $k_2'/k_2$  equal to 14 fits data from all but one run at 137  $\pm$  3°C., indicating little pressure effect, but a small temperature effect on the ratio. The temperature effect is equivalent to a difference in activation enthalpy between the individual rate constants of about 2500 cal./mole.

Irregularities are encountered in trying to apply the calculation to data from runs in which [M'] became too low to be detected. Glassy polymer formed in all such runs; the difficulty is connected with use of the arithmetic mean of final and initial values of [M']/[M]. If [M']/[M] is nearly zero long before the experiment ended then the mean is higher than the true average. The apparent value of  $k_2'/k_2$  is reduced by an amount that increases with the fraction of time [M']/[M] was zero. This is unknown, so data from such runs are not entered on the plot. These include all runs at the highest temperature at each pressure and one run at 134°C. With the use of the ratios of 11 and 14 found to fit at 108 and 138°C., respectively, a value of 17 is indicated at 165°C.

The values of  $c_i$  indicate that units derived from the 1,3-diene are present to the extent of 40-70% in the rubbery polymers and 4-14% in the glassy polymers. All other units presumably are derived from the 1,4-diene;

now it is desired to determine the fraction of these that do not undergo cyclopolymerization.

A perfluorovinyl group will enter the polymer for each unit of 1,4-diene that does not cyclopolymerize. Thus the fraction desired is equal to  $c_v/(9.5 - c_i)$  in high polymer, where  $c_v$  is the concentration of perfluoro-The value of 700 l./mole-cm., obtained as described above, vinyl groups. was used to calculate the values of  $c_v$  listed in Tables I and II. These lead to values of  $c_v/(9.5 - c_i)$  that are between 0.002 and 0.07 for the rubbers and 0.03 and 0.2 for the glasses. It is reasonable to suspect that some -CF = $CF_2$  groups are associated with chain ends. If one assumes one such group per polymer molecule, the fraction of 1,4-units that have not cyclized becomes  $(c_v - 9.5/\text{DP}_n')/(9.5 - c_i)$ . Where  $\text{DP}_n'$  is not given, the infrared spectrum was obtained on polymer that had not been heated at 180°C.; then  $DP_n$  should be used instead of  $DP_n'$ . The correction should be negligible for most of the rubbery polymers but is appreciable for the For these, the range of the fractions of 1,4-units that enter but glasses. do not cyclize is from 0.09 to slightly negative numbers, i.e., overcorrection sometimes occurs. However, in 11 of 14 cases, the ratios are between 0.01 and 0.07; this is close to the ratios for the rubbers. Reservations are felt concerning the absolute accuracy of the values of  $c_{\rm v}$  and any values derived from them, because they are based on an absorption coefficient pertaining to a small molecule in a liquid medium. However, even a twofold error in the absorption coefficient usually leads to the conclusion that cyclization follows about 90% of the additions of 1,4-units. Thus, the structure of the polymers probably can be represented as:



In the rubbery polymers, x/(x + y + z) is greater than 0.4; in the glasses, it is less than 0.14. The mode of addition of the 1,3-units has not been proved but is believed to be 1,4-addition because polyperfluorobutadiene contained many more internal double bonds than  $CF_2$ =CF- groups; this results in the x structure shown. In both types of polymer, y/(y + z) is greater than 0.9. No proof of ring size has been given, but the four-membered ring is expected on steric grounds, i.e., the attacking radical will join to the terminal carbon atom of the vinyl group.

The copolymerization process assumed has certain implications for the polymerization rates. These and other details of the rate behavior are considered below.

## **Polymerization Rates**

The polymerization mechanism is thought to be a free radical chain reaction because the G values for conversion to polymer are 120 or more, the rate increases with temperature (Table II), and about as the square root of radiation intensity at constant composition, temperature, and pressure (Table III). These are all characteristics of a free radical chain reaction. If 1,4-diene was the only monomer present the mechanism detailed in Table IV would be applicable; the usual assumptions are made that the kinetic chain length is great and that steady-state concentrations of radicals are achieved. In addition it is assumed that the cyclization rate constant is much larger than the product of monomer concentration and any possible propagation rate constants. This is in accord with the conclusions expressed above concerning the extent of cyclization.

	Polymerization Mech	nanism of Perfluro-pentadiene-1,4
Step	Reaction	Rate
	I M $\rightarrow$ R ₁	
Initiation		$(d[R_1]/dt) = k_i'I = 212G(i)I/NV = k_i/V$
	$\mathbf{R}_n + \mathbf{M} \xrightarrow{k_2} \mathbf{R}_{n+1}^*$	$\begin{cases} (d(\Sigma[\mathbf{R}_n^*])/dt) = k_2[\mathbf{M}](\Sigma[\mathbf{R}_n]) \\ -(d[\mathbf{M}]/[\mathbf{M}]dt) = k_2(\Sigma[\mathbf{R}_n]) = R_p' \end{cases}$
Propagation	$R_n + M \rightarrow R_{n+1}^*$	$\int -(d[M]/[M]dt) = k_2(\Sigma[R_n]) = R_n'$
	kc	
Cyclication	$\mathbf{R}_n^* \to \mathbf{R}_n$	$-\left(d\Sigma[\mathbf{R}_n^*]/dt\right) = k_c(\Sigma[\mathbf{R}_n^*])$
	$k_z$	
Transfer	$R_n + M \rightarrow P_n + F$	$\mathbf{R}_1  (d[\mathbf{P}_n]/dt) = k_3(\boldsymbol{\Sigma}[\mathbf{R}_n])[\mathbf{M}]$
	k4	
Termination	$\mathbf{R}_n + \mathbf{R}_m \to \mathbf{P}_n + \mathbf{I}$	$\mathbf{P}_m - (d[\mathbf{R}]/dt) = d[\mathbf{P}_n]/dt = 2k_4(\Sigma[\mathbf{R}_n])^2$

 TABLE IV

 Polymerization Mechanism of Perfluro-pentadiene-1,4

In Table IV the symbols M, R, P, and I refer to monomer, radicals, polymer, and radiation intensity, respectively. The symbols  $k_2$ ,  $k_c$ ,  $k_3$ , and  $k_4$  are rate constants;  $R_p'$  is the fractional rate of conversion of monomer to polymer. The symbols n and m refer to the number of monomer units in the species being considered.

Since initiation results from absorption of energy from  $\gamma$ -rays the rate of initiation in bulk monomer,  $k_i'I$ , also is given by the expression (212  $G_iI/NV$ ), where I is the radiation intensity in units of 100 electron volts per gram per unit time,  $G_i$  is the number of radicals produced per 100 e.v. of absorbed energy, 212 is the molecular weight of the monomer, V is its molar volume, and N is Avogadro's number. At constant intensity  $k_i'I$ also equals  $k_iV^{-1}$ , where  $k_i$  is the fractional rate of initiation. The form used for the initiation rate is dictated by convenience; the symbol  $k_1$  is reserved for thermal initiation.

The assumption concerning the cyclization rate constant leads to the conclusion that the fraction of radical species  $R_n^*$  disappearing by processes other than cyclization is less than the ratio of initiation (or termination) to propagation. Thus, this fraction can be ignored since the kinetic chain is long; the steady state equation for species  $R^*$  becomes:

$$d(\Sigma[\mathbf{R}_{n}^{*}])/dt = k_{2}[\mathbf{M}](\Sigma[\mathbf{R}_{n}]) - k_{c}(\Sigma[\mathbf{R}_{n}^{*}]) = 0$$

The same assumption justifies neglect of additions of M to species R*.

The terms in the above equation occur also in the steady-state equation for  $R_n$ ; on summing to zero they disappear from the latter equation. As a

result, the cyclization rate constant does not enter the rate equation, which is the same as that obtained in the absence of cyclization:

$$R_{n'} = -d[M]/[M]dt = (k_{i}'I/2k_{4})^{1/2}k_{2}$$
(1)

Transfer reactions involving species  $R_n^*$  and monomer can be ignored because  $(\Sigma[R_n^*])$  is much less than  $(\Sigma[R_n])$ . Thus, the expression for  $(DP_n^{-1})$  at constant temperature and pressure, if disproportionation is assumed, is:

$$(DP_n^{-1}) = (k_3/k_2) + (2k_4R_p'/k_2^2[M])$$
(2)

If combination is assumed, the second term is  $(k_4 R'_p / k_2^2 [M])$ . This is the equation for  $DP_n^{-1}$  in a polymerization not complicated by cyclication.

#### **Copolymerization Rates**

The presence of a comonomer affects the form of eqs. (1) and (2). To apply absolute rate theory to the data one should define the overall rate in terms of the individual rate constants of the chain reaction. In general copolymerization theory the overall rate expression is too complicated to handle because there are four propagation constants, several initiation constants, and at least three termination constants. In our work some simplification appears possible because only two propagation constants sufficed to relate  $c_i$  to the monomer composition. Furthermore, it probably is valid to ignore effects of monomer composition on the initiation rate because all the compounds present are expected to have very similar values of  $G_i$ .

The propagation reactions that were considered in assessing the structure of the polymers were:

м′	$+ \mathbf{R}_n \xrightarrow{k_{2'}} \mathbf{R'}_{n+1}$
M′	$+ \mathbf{R}_{n'} \xrightarrow{k_{2'}} \mathbf{R}_{n+1'}$

where

$$-d[\mathbf{M}']/di = k_2'[\mathbf{M}'](\Sigma[\mathbf{R}_n] + \Sigma[\mathbf{R}_n'])$$
$$\mathbf{M} + \mathbf{R}_n' \xrightarrow{k_2} \mathbf{R}_{n+1}$$
$$\mathbf{M} + \mathbf{R}_n \xrightarrow{k_2} \mathbf{R}_{n+1}$$

where

$$-d[\mathbf{M}]/dt = k_2[\mathbf{M}](\Sigma[\mathbf{R}_n] + \Sigma[\mathbf{R}_n'])$$

Radicals ending in M' are denoted R'. If it is assumed that the termination rate constant is independent of the radical species then the sum of the concentrations of different radicals is the same as in the absence of M'. The rate equation is:

$$R_{p} = \left(\frac{k_{i}'I}{2k_{4}}\right)^{1/2} k_{2} \left(\frac{[M]}{[M_{0}]} + \frac{k_{2}'[M']}{k_{2}[M_{0}]}\right) = \left(\frac{k_{i}'I}{2k_{4}}\right)^{1/2} k_{2} F$$
(3)

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In this equation  $[M_0]$  is the sum [M] + [M']; thus,  $R_p$  is the total fractional rate at which polymer is formed. The symbol F denotes the ratio by which  $R_p$  by eq. 3 exceeds  $R_r'$  by eq. 1; this ratio we term the acceleration factor.

The variation in  $c_i$  with monomer composition led to a value of  $k_2'/k_2$  of 11 at 11,400 atm. pressure and 104°C. Data in the first four lines of Table I were obtained from experiments run under these conditions. If the mechanism is correct one should be able to use the equation above to predict the relative rates of formation of rubbery and glassy polymer. The predicted ratios are lower than those observed, being 2.1 versus 4.9 and 1.9 versus 4.5, respectively.

A considerably large acceleration factor is calculated if the rate constants for termination of species R' are much less than that for mutual termination of R. If species R' can not terminate the reaction rate becomes:

$$\mathbf{R}_{p} = \left(\frac{k_{i}'I}{2k_{4}}\right)^{1/2} k_{2}F\left(1 + \frac{k_{2}'[\mathbf{M}']}{k_{2}[\mathbf{M}]}\right) = \left(\frac{k_{i}'I}{2k_{4}}\right)^{1/2} k_{2}FF'$$
(4)

where the acceleration factor is FF'. Values of FF' are listed in Tables I and II. This equation predicts rate ratios of 5.1 and 4.0 when applied to the same pairs of data as above. This is close enough to reality to be regarded as in accord with the copolymerization hypothesis. Of course a termination rate of zero is unrealistic but a 10 to 100-fold difference between rate constants for termination should result in about the same difference in  $R_p$  for glassy and rubbery polymer as calculated above. The form of the equation will be more complicated because it will contain three termination rate constants.

Only experiments in which glassy polymer formed are considered in subsequent discussion of the rate data. In such experiments F varied from 1.08 to 1.17, and FF' from 1.18 to 1.37. The true acceleration factor will be more than F but less than FF'. Judging by the calculations above it will be very close to FF'. Therefore, eq. (4) should describe the rate behavior with reasonable accuracy; according to this equation  $R_p/FF'$ equals  $R_p'$ , the polymerization rate of the pure, 1,4-diene [compare eqs. (1) and (4)]. Furthermore, the temperature and pressure dependence of  $R_p'$  and  $R_p/FF'$  should be described by a single exponential function because the individual rate constants in the expression appear as a product, permitting summation of the individual exponents.

#### Effect of Temperature and Pressure on $R_p/FF'$

At constant intensity it is convenient to replace  $k_i'I$  in eq. (4) by  $k_iV^{-1}$ , which was defined above. Equation (4) becomes:

$$R_{p}/FF' = (k_{i}/2k_{4}V)^{1/2}k_{2}$$
(5)

Absolute rate theory offers the most straightforward interpretation of the effects of temperature and pressure on  $R_p/FF'$ . Each rate constant

can be expressed in terms of this theory, i.e.,  $k_j = V(k/h)T \exp(-\Delta F_j^*/RT)$  for second-order reactions (propagation, transfer, and termination), where V is the molar volume, k is the Boltzmann constant, h is the Planck constant, T is the absolute temperature,  $\Delta F_j^*$  is the free energy change in forming the transition complex of reaction j, and R is the gas constant. These expressions for the k's are substituted in eq. (5). It is assumed that  $G_i$  and so  $k_i$  are independent of temperature and pressure. This assumption is in accord with the small temperature dependence of radiation-induced reactions that do not proceed by a chain mechanism. The equation for  $R_p/FF'$  is:

$$\frac{R_{\mathfrak{p}}}{FF'} = \left(\frac{kT}{2h}\right)^{1/2} k_i^{-1/2} \exp\left\{\frac{-\Delta F_2^* + \Delta F_4^*/2}{RT}\right\}$$
(6)

Equation (6) is transformed by standard methods into equations relating log  $(R_p/FF')$  to temperature at constant pressure and to pressure at constant temperature.⁷ These equations are:

 $\log (10^{5}R_{p}/FF') = \frac{1}{2} \log T + [-(\Delta H_{2}^{*} - 0.5 \Delta H_{4}^{*})/2.3 RT] + C_{1} (7)$ 

for constant pressure data and,

$$\log (10^{5}R_{p}/FF') = [-(\Delta V_{2}^{*} - 0.5 \Delta V_{4}^{*})/2.3 RT]P + C_{2}$$
(8)

for constant temperature data.

In these equations  $\Delta H^*$  and  $\Delta V^*$  are the respective enthalpy and volume changes that occur when the transition state forms, P is the pressure, and the C's are integration constants. In deriving these equations it is assumed that  $\Delta H_2^* - 0.5 \ \Delta H_4^*$  is independent of temperature at constant pressure and that  $\Delta V_2^* - 0.5 \ \Delta V_4^*$  is independent of pressure at constant temperature.

An analogy to the Arrhenius plot is in Figure 3; three isobars are shown. An imprecision of 5% in  $R_p$  and one degree in T was indicated by our earlier work along these lines. If this imprecision is assumed the data taken from experiments at 14,900 and 11,400 atm. can fall on straight lines; the variation possible in the slopes of these lines is equivalent to an uncertainty of 1 kcal./mole in  $\Delta H_2^* - 0.5 \Delta H_4^*$ . Greater scatter is exhibited by data from experiments at 8000 atm.; the overall trends indicate that the observed value of  $R_p/FF'$  is too high at the lowest temperature and pressure. This point is ignored in drawing the 8000 atm. isobar. The uncertainty in  $\Delta H_2^* - 0.5 \Delta H_4^*$  at 8000 atm. is between 2 and 3 kcal./mole if the remaining pair of points have the same imprecision as assumed for the other two isobars.

Figure 4 is a plot of log 10⁵  $R_p/FF'$  versus pressure; isothermal data were obtained from Figure 3 as the intersections of values of the abscissa with the isobars. The uncertainty in values of  $\Delta V_2^* - 0.5 \ \Delta V_4^*$  is about 1 cc./mole if  $R_p/FF'$  is imprecise by 5% and P is imprecise by 100 atm. The good linear variation of log  $R_p$  with P would not have been obtained if  $(-\Delta V_2^* + \Delta V_4^*/2)$  had varied with pressure in the experimental range.

In Table V are listed values of thermodynamic quantities present in the

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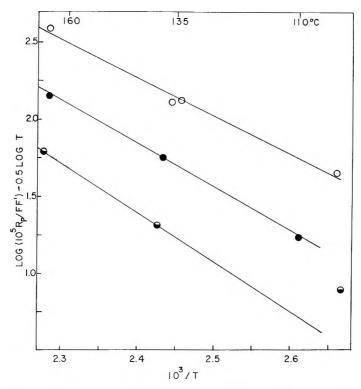


Fig. 3. Arrhenius-type plot of rate function (all data were obtained at a dose rate of 0.047 Mrad/hr.): (○) 14,900 atm.; (●) 11,400 atm.; (●) 8,000 atm.

rate expressions or derived from them. At different temperatures the  $\Delta V^*$  terms were not significantly different. Therefore, one value is listed to cover the temperature 100-170 °C. Values of  $\Delta H_2^* - 0.5 \Delta H_4^*$  appear to decrease as pressure is increased. A term closely related to the  $\Delta H^*$  and  $\Delta V^*$  terms is the activation energy term,  $\Delta E^*$ ; it is calculated by use of the relation  $\Delta E = \Delta H - P\Delta V$  at constant pressure. This  $\Delta E^*$  term is larger than the  $\Delta H^*$  term because the  $\Delta V^*$  term is negative; it does not change over the experimental temperature and pressure range. The activation energy term is much larger than found in ordinary polymerization at low pressure.

The actual values of  $\Delta F_2^* - 0.5 \Delta F_4^*$  and  $\Delta S_2^* - 0.5 \Delta S_4^*$  (calculated from the general relation  $\Delta F = \Delta H - T \Delta S$ ) depend on the initiation rate, as shown by the presence of  $k_i$  in eq. (6). The value of  $G_i$  was taken to be 10, and calculations were made of these terms; these results also are listed in Table V. Using different values of  $G_i$  affects the results of the calculation only slightly. For example, if  $G_i$  is taken to be 30, then one calculates that at 14,900 atm. and 168°C. the  $\Delta F^*$  term is 15.1  $\pm$  .1 kcal./mole and the  $\Delta S^*$  term is  $-8 \pm 5$  e.u./mole.

The change in the  $\Delta F^*$  term with temperature at constant pressure is small (~400 cal./mole), so only one value is listed at each pressure. Of

$\Delta H^*$ , scal./mole	$\Delta V^*$ , cc./mole	$\Delta E^*$ , kcal./mole	$\Delta F^*,$ kcal./mole ^b	ΔS*, e.u./mole ^b
$.4 \pm 1.0$	$-10.5 \pm 1$	$15.2 \pm 1.4$	$14.3 \pm 0.2$	$-7.0 \pm 2.2$
$2.5 \pm 1.0$	$-10.5 \pm 1$	$15.5\pm1.3$	$15.0\pm0.2$	$-6.1\pm2.3$
$7\pm 2.0$	$-10.5 \pm 1$	$16.7 \pm 2.2$	$16.0\pm0.2$	$-3.4\pm4.5$

TABLE V

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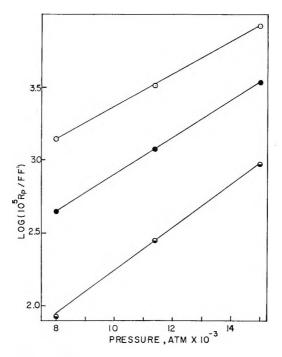


Fig. 4. Plot of log  $(10^{6}R_{p}/FF')$  vs. pressure (All data were obtained at a dose rate of 0.047 Mrad/hr.) ( $\odot$ ) 167°C.; ( $\bullet$ ) 140°C.; ( $\bullet$ ) 106°C.

course,  $(\Delta F_2^* - 0.5 \ \Delta F_4^*)/T$  decreases as temperature increases. The  $\Delta F^*$  term decreases as pressure increases because of the decrease in the  $\Delta H^*$  term. The values of the  $\Delta S^*$  term are so uncertain that they do not change significantly over the experimental range. However, the  $\Delta S^*$  term is quite small in absolute amount, being about half that of the comparable term for the polymerization of perfluoroheptene-1.⁸ The  $\Delta F^*$  term for perfluoroheptene-1 is about 3 kcal./mole larger than that for the 1,4-pentadiene. All of this difference is due to the smaller entropy term of the latter. It is speculated that the small entropy term is connected with the diene character of the monomer; in a crude sense a diene should have twice the probability of orientation favorable for reaction as would a monoolefin.

Reversal of polymerization was observed with perfluoroheptene-1. It is characterized by the occurrence of a maximum in the rate as temperature is increased. That it was not found in this work is attributed to the fast cyclopropagation. Radicals that can lose monomer units by depropagation are present in too low concentration to be important.

Table II contains data from three thermal polymerizations in addition to those already considered. The thermal rate is always less than 20% of the radiation-induced rate. The correction to the radiation-induced rate is less than 2% because of the square-root relation between overall rate and initiation rate; this was ignored in the discussion above. However, the variations in thermal rate can be used to calculate  $\Delta H_1^*$  and  $\Delta V_1^*$ , the enthalpy and volume changes associated with the formation of the transition complex of the thermal initiation act; the values were  $5 \pm 2$  kcal./mole and -6 cc./mole, respectively, at 14,900 atm. and 168°C. The activation enthalpy is very much lower than encountered in hydrocarbon work. The negative value of  $\Delta V_1^*$  is in accord with the argument that thermal initiation should result from an associative process.⁹

#### **Degree of Polymerization**

If it is assumed that monomer transfer involves reaction of species M with all kinds of radicals with a single rate constant, the equation connecting  $DP_n^{-1}$  with  $R_p$  and monomer composition at constant temperature and pressure is:

$$DP_{n^{-1}} = (k_{3}/k_{2}F') + \left\{ 2k_{4}R_{p}[M_{0}]/k_{2}^{2}[M^{2}](F')^{4} \right\}$$
(9)

The first term is connected with monomer transfer; the second term is connected with the termination process and would be half as large if combination were assumed. It is thought that if transfer is substantial it is with species M because the presence of large amounts of dimer, 1,3-diene, and 2,3-diene are not associated with especially low values of  $DP_n$ .

There are difficulties in applying this equation because of the dimerization reactions and possible fractionation during polymer isolation. The effects of these are negligible when  $DP_n$  is high but can be quite substantial in our results, since the observed values of  $DP_n$  vary from 18 to 38. The presence of excess dimer lowers  $DP_n$ , while evaporation of dimer and trimer raises  $DP_n$  in comparison with values for which equation 9 was derived.

In Table III are listed some experiments to which eq. 9 can be applied. The variation in F' is small enough to be ignored in the experiments in which glassy polymer formed; dimerization rates were very small under these conditions. Thus, the observed values of  $DP_n$  will be higher than predicted by eq. (9) except for the possible 5% error in the measurement. If it is assumed that most probable distributions form during the reaction and if dimer and trimer are removed quantitatively in some cases but not at all in others, then the possible deviation of the observed  $DP_n$  from that calculated by eq. 7 is thought to be +1 unit and -4 units.

By plotting  $DP_n^{-1}$  versus  $R_p$  with due allowance for these uncertainties and extrapolating to  $R_p$  equal to zero one finds that  $k_3/k_2$  is 0.05  $\pm$  0.01 at 11,400 atm. and 110°C. Thus, although the transfer constant is rather uncertain, it appears that transfer largely but not necessarily completely determines  $DP_n$ , since  $k_3/k_2F'$  and  $DP_n^{-1}$  are about equal. Conclusions from the data at 8,000 atm. and 110°C are similar. Apparently, transfer is important under the other reaction conditions also because the overall variations in  $DP_n$  and  $DP_n'$  of the glassy polymers are factors of four and two, respectively whereas  $R_p$  varied by 30-fold. In the absence of transfer  $DP_n$  should vary by the same factor as  $R_p$ , assuming no change occurs in the ratio of disproportionation to combination.

It is necessary to compare values of  $[\eta]$  in trying to judge the effect of monomer composition on  $DP_n$ . The ratio of the intrinsic viscosity of

rubbery polymer to that of the glassy polymer formed at the same temperature, pressure, and intensity is 2.5. The compositions differ in the two types of polymer; this may affect the relation between  $[\eta]$  and  $DP_n$ , so the ratio of  $DP_n$ 's is unknown. However,  $DP_n$  of the rubber almost certainly is larger than that of the glass. If transfer determines  $DP_n$ eq. (9) predicts the ratio of  $DP_n$  of the rubber to that of the glass will be the same as the ratio of the F' values; this is 2.1. The larger ratio of 5.3 is obtained if transfer is negligible and the other term of eq. (9) determines  $DP_n$ .

Considering now the variation in the intrinsic viscosity of the rubbery polymer with intensity, at constant temperature and pressure, one sees that  $[\eta]$  decreased by a factor of 2.6 as  $R_p$  increased by a factor of 4.3. Polymer compositions are similar, and if the distributions are alike the ratio of DP_n's should be between 2.6 and 6.7 (i.e., 2.6²), depending on the solvent power of C₆F₆. There is some difference in the values of F' for the two samples. Equation (9) predicts that DP_n will be lower at high intensity by a factor of 1.2 due to the ratio of F' values, if transfer controls DP_n, and a factor of 7.4 if transfer is insignificant.

Thus, comparisons of  $DP_n$  of rubbery polymer with that of glassy polymer and with that of another sample of rubbery polymer suggest that transfer is not all-important. This would imply that the correct value of  $k_3/k_2$  is about at the lower limit of the range given above, i.e., it is 0.04 at 11,400 atm. and 110°C.

The specific reaction involving transfer is not established. Donation of an F atom from the radical to olefin is favored in fluorocarbon compounds containing one double bond.¹⁰ However, with the 1,4-diene abstraction of F by the radical from the center carbon gives a radical of abnormal stability,  $CF_2$ =CF-CF-CF-CF-CF, and so may favor abstraction as the transfer process. Each donation of F to monomer introduces one perfluorovinyl group into the polymer; each abstraction introduces two such groups.

## **Polymer Pyrolysis**

The pyrolyses were performed in an attempt to satisfy a speculation concerning polymer stability. This was that the branches not associated with the rings would contribute instability to the polymer. Since each unit of 1,3-diene in the polymer contains such a branch it was expected that the pyrolysis rate would increase with the content of 1,3-diene units. This was found to be the case, as seen in Figure 1. Effects of initial  $DP_n'$  appear to be minor, in keeping with the observation that the monomer fraction formed during pyrolysis was small.¹¹ The double bonds may also contribute to instability but the branches are involved to some extent because the saturated polymers of perfluoropropylene and perfluoroheptene-1 also decompose at 300°C.¹² On the basis of the results in Figure 1, it is believed that a homocyclopolymer of the 1,4-diene would pyrolyze at a rate of about 1%/min. at 400°C. This is much better stability than exhibited by any fully fluorinated polymer except polytetrafluoroethylene. Possibly the cyclic structure tends to prevent depropagation and so reduces the length of the kinetic chain.

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#### Résumé

On a étudié la polymérisation, induite par radiation, du *n*-perfluoropentadiène-1,4 entre les températures de 100° et 170°C et aux pressions de 8.000 et 15.000 atm. La cinétique indique que la polymérisation a lieu par réaction radicalaire. L'énergie d'activation est de l'ordre de 14 à 17 kcal/môle et l'entropie d'activation de l'ordre de  $-8 \pm 5$  u.e./môle. Le transfert sur monomère limite le degré de polymérisation moyen en nombe à une valeur de 40 ou moins, sauf dans des circonstances spéciales. Il se peut qu'il y ait une dimérisation ou une migration de la double soudure, il se forme, dans ce dernier cas, le diène-1,3 qui copolymérise avec le diène-1,4. Le diène-1,4 subit des additions cycliques jusqu'à ce que les polymères soient solubles et aient une légère insaturation perfluorovinylique. Les polymères sont soit cassants, soit élastiques et de haut poids moléculaire, suivant que la fraction de diène-1,3 dans les polymères est inférieure à 0.1 ou supérieure à 0.4. La stabilité thermique de ces polymères diminue par l'augmentation de la fraction de diène-1,3.

#### Zusammenfassung

Die strahlungsinduzierte Polymerisation von *n*-Perfluorpentadien-1,4 wurde bei Temperaturen zwischen 100 und 170°C und Drucken von 8.000 und 15.000 atm untersucht. Die kinetischen Ergebnisse zeigen, dass die Polymerization eine radikalische Reaktion ist; die Aktivierungsenergie liegt zwischen 14 und 17 kcal/Mol und die Aktivierungsentropie beträgt  $-8 \pm 5$  EU/Mol. Übertragung mit dem Monomeren setzt das Zahlenmittel des Polymerisationsgrades mit Ausnahme besonderer Umstände auf Werte von 40 oder weniger herab. In gewissem Ausmass tritt Dimerisierung und Doppelbindungswanderung auf; bei letzterem Prozess wird *n*-Perfluorpentadien-1,3 gebildet. Dieses und das 1,4-Dien copolymerisieren; letzteres zeigt zyklische Addition, sodass die Polymeren löslich sind und nur wenige Perfluorvinyldoppelbindungen besitzen. Wenn der 1,3-Dienbruchteil m Polymeren geringer als 0,1 ist, sind die Polymeren spröde. Bei einem 1,3-Dienbruchteil grösser als 0,4 sind sie kautschukartig und besitzen beträchtlich höheres Molekulargewicht. Die thermische Stabilität der Polymeren nimmt mit steigendem 1,3-Diengehalt ab.

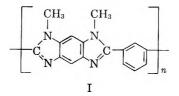
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## NOTE

#### Poly-2,6-(m-phenylene)-3,5-dimethyl-Diimidazolebenzene*

A variety of polybenzimidazoles has been made previously,¹⁻⁴ and the remarkable thermal stabilities of such polymers containing benzimidazole nuclei as recurring units have been noted. An improvement of the oxidative stability of polybenzimidazoles was attempted by replacing hydrogen atoms on the nitrogen atom of the imidazole rings with methyl groups. This modified polybenzimidazole (I) was prepared by melt condensation of 1,3-dimethylamino-4,6-diaminobenzene with diphenyl isophthalate.



Previously the analogous phenyl derivative had been made² and very little difference was noted in the thermal and oxidative stabilities of the unsubstituted and substituted polymers. The thermogravimetric analysis of the methyl derivative made in air and in nitrogen (Fig. 1) shows that the decomposition in air appears to be slightly less than was observed for an unsubstituted related polymer and for the phenyl derivative.² The thermal stability in nitrogen appears to be little affected by the methyl substitution.

#### Experimental

1,3-Dimethylamino-4,6-dinitrobenzene. 1,3-Dichloro-4,6-dinitrobenzene⁵ (47.4 g., 0.2 mole), sodium acetate (32.8 g., 0.4 mole) and 100 ml. of nitrobenzene were placed in a 300-ml., three-necked flask, provided with a stirrer and inlet and outlet tubes and surrounded by an oil bath. The bottom of the inlet tube was kept slightly above the liquid surface to prevent clogging and the outlet tube was connected with a Liebig condenser. The oil bath was heated to  $160^{\circ}$ C., and, then, methylamine gas [which was freshly liberated by adding dropwise an aqueous solution of methylamine hydrochloride (54.4 g., 0.8 mole) onto sodium hydroxide (32.0 g., 0.8 mole)] was introduced through the inlet tube over 6 hr. Then 100 ml. of methanol was added to the mixture and the precipitate was collected on a filter, washed several times with water and then with hot methanol, and finally recrystallized from dimethylformamide-methanol (1:1). Light-brown crystals were obtained in 90% yield (40.6 g.), m.p. 320-321°C.

ANAL. Calcd. for  $C_8H_{10}N_4O_4$ : C, 42.48%; H, 4.46%; N, 24.77%; O, 28.29%. Found: C, 42.38%; H, 4.46%; N, 24.74%; O, 28.48%.

1,3-Dimethylamino-4,6-diaminobenzene. Adams platinum catalyst (40 mg.), 1,3dimethylamino-4,6-dinitrobenzene (3.0 g., 0.013 mole) and 60 ml. of glacial acetic acid were placed in a 250-ml. glass bottle. After replacing the atmosphere completely with hydrogen, the pressure was kept at 30 psi at room temperature. The bottle was shaken for 24 hr. under these conditions. Then the reaction mixture was filtered, and the filtrate

* The work described herein was supported by Contract AF 33(657)9969 with the Materials Laboratory, Wright Air Development Division, Wright-Patterson Air Force Base, Ohio. This is the fifth paper on polybenzimidazoles. For the fourth paper see Foster and Marvel.⁴

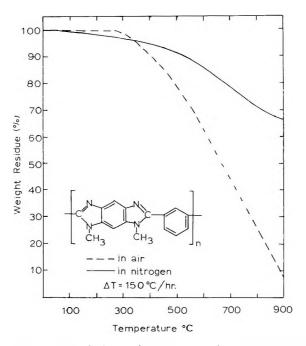


Fig. 1. Thermogravimetric analysis of poly-2,6-(*m*-phenylene)-3,5-dimethyldiimidazolebenzene.

poured directly into 60 ml. of ice-cold concentrated hydrochloric acid. This filtration was carried out in a nitrogen atmosphere without exposing the mixture to air because the resulting amine was readily oxidized. The 1,3-dimethylamino-4,6-diammobenzene tetrahydrochloride which precipitated was collected on a filter and then purified by dissolving in a minimum amount of water and pouring this solution into ice-cold concentrated hydrochloric acid. White crystals separated and were collected on a filter. The yield was 52% (2.14 g.), m.p. 152-155°C. (dec.).

ANAL. Calcd. for  $C_8H_{18}N_4Cl_4$ : C, 30.77%; H, 5.77%; N, 17.95%; Cl, 45.51%. Found: C, 30.86%; H, 5.95%; N, 17.17%; Cl, 42.25%.

Into a 100-ml., three-necked flask, which was placed in an ice-water bath, 20 ml. of 20% sodium hydroxide solution in oxygen-free water was placed. The atmosphere in the flask was kept under nitrogen. Then a solution of the amine tetrahydrochloride (3.0 g., 0.01 mole) in 10 ml. of oxygen-free water was added and stirred for 1 hr. under these conditions. Yellow crystals of the free amine were precipitated, filtered off in a nitrogen atmosphere, and dried under vacuum. The yield was 58% (0.93 g.), m.p. 127-129°C. This amine always seemed to contain some inorganic residue as shown in the analysis.

ANAL. Calcd. for C₈H₁₄N₄: C, 57.83%; H, 8.43%; N, 33.74%. Found: C, 55.80%; H, 7.74%; N, 31.45%; residue, 2.74%.

Melt Condensation of 1,3-Dimethylamino-4,6-diaminobenzene with Diphenyl Isophthalate. The general melt condensation procedure¹ was used. Diphenyl isophthalate (1.775 g., 5.58 mmole) and 1,3-dimethylamino-4,6-diaminobenzene (0.927 g., 5.58 mmole) were placed in a 100-ml. flask without exposing the amine to air. The mixture was heated in a nitrogen atmosphere for a 0.5 hr. at 280°C. and then under vacuum for another 0.5 hr. at the same temperature. The resulting prepolymer was pulverized and again heated under vacuum for 20 hr. at 350°C. A yellow-brown polymer was obtained. This was washed with hot 95% ethanol (reflux) for five days and then dried under vacuum at 150°C. The yield was 90% (1.3 g.).

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#### NOTE

ANAL. Calcd. for  $(C_{16}H_{12}N_4)_x$ : C, 73.83%; H, 4.65%; N, 21.53%. Found: C, 73.92%; H, 5.06%; N, 20.97%.

The polymer was slightly hygroscopic, soluble in concentrated sulfuric acid, and partly soluble in dimethyl sulfoxide. The inherent viscosity was measured with 0.2% solution in concentrated sulfuric acid, giving 0.214 at 30 °C.

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## ERRATUM

## Kinetic Study of the Polymerization of $\alpha$ -d-Styrene and/or Styrene by Homogeneous Catalysis. Part I

(article in J. Polymer Sci., A2, 4113-4121, 1964)

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On page 4114, Equation (2) should read:

